

Abstract

The CALIS procedure in SAS/STAT is a general structural equation modeling (SEM) tool. This workshop introduces the general methodology of SEM and the applications of the CALIS procedure. Historical topics such as casual models, path diagram, confirmatory factor-analysis, measurement error model, and linear structural relations (LISREL) are reviewed. Applications of the CALIS procedure to SEM are demonstrated with examples in social, educational, behavioral, and marketing research. Specifically, the following how-to techniques of the CALIS procedure (SAS/STAT 9.22) are covered: (1) Specifying structural equation models with latent variables by using the PATH modeling language; (2) Interpreting the model fit statistics and estimation results; (3) Testing models with multiple groups and multiple models; (4) Analyzing direct and indirect effects; (5) Modifying structural equation models.

This workshop is designed for statisticians and data analysts who want to overview the applications of the SEM by the CALIS procedure. Attendees should have a basic understanding of regression analysis and experience using the SAS language. Previous exposure to SEM is useful, but not required.

Citation of this workshop:

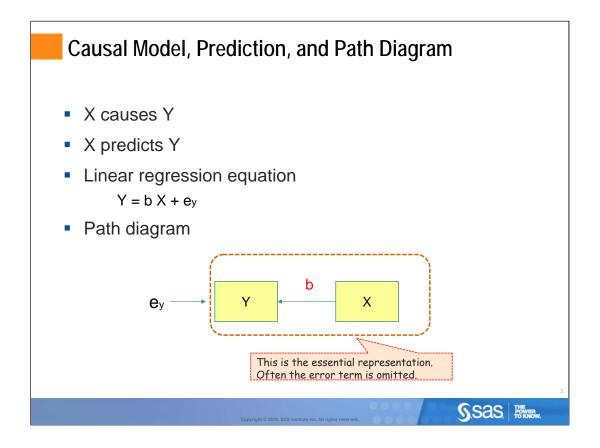
Yung, Y.-F. (2010). Introduction to Structural Equation Modeling Using the CALIS Procedure in SAS/STAT® Software. Computer technology workshop presented at the Joint Statistical Meeting on August 4, 2010, Vancouver, Canada.

SAS/STAT 9.22 or later is assumed for this workshop

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In this workshop, SAS/STAT 9.22 (TS2M3) or later is assumed for the CALIS procedure. Some of the code might work with PROC TCALIS (an experimental procedure) in SAS/STAT 9.2 (TS2M2). However, there is a major syntactical difference between PROC TCALIS and PROC CALIS. In PROC TCALIS, the parameter specification for each path in the PATH statement must **not** be preceded by an equal sign. But this equal sign is required in PROC CALIS when you specify parameters. Also, PROC TCALIS does not support the generalized path specifications (for variances, covariances, means, and intercepts) and multiple-path specifications when you use the PATH modeling language, which is the main focus of today's talk.

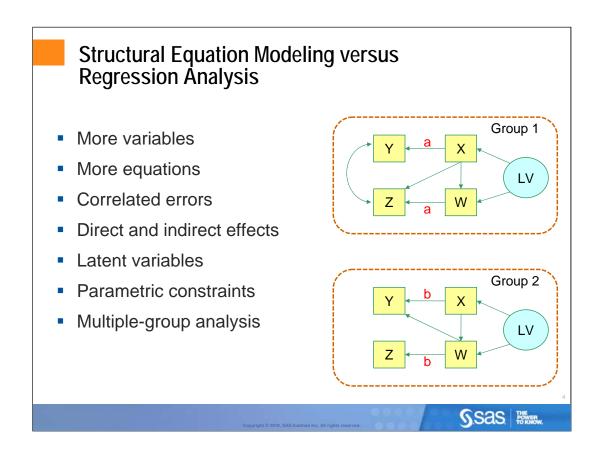


The central idea of structural equation modeling is the study of causal relationship between variables. For example, you have an X and an Y variable. X is the cause of Y, or doing X results in Y. To give a more realistic example: eating more vegetables (X) brings down your cholesterol level (Y). However, this causal structure is only an idealized framework. In making causal inferences, you must have isolated all other background variables and establish temporal sequence of the variables. Because of the complicated philosophical issues involved in making causal inferences, in general SEM would avoid claiming causal inferences.

A predictor-outcome framework might be more appropriate philosophically. The semantic is now "X predicts Y". Mathematically and statistically, this idea is represented in the simple linear regression analysis, as shown in the linear regression equation:

$$Y = b*X + e$$
.

The path diagram for this representation is shown in the slide, where b is called the effect, regression coefficient, or path coefficient. Notice that an error term is added to show that the prediction of Y from X is not perfect. But essentially, the predictor-outcome framework is represented by the Y \leftarrow X path in the path diagram.



What are the differences between SEM and regression analysis? What more can SEM offer than the linear regression analysis?

You can view SEM as a much more complicated system for multiple predictor-outcome relationships. SEM can handle the following situations where linear regression analysis is of limited usefulness:

- 1. More variables (not just X and Y, but you can also add W and Z into the path diagram).
- 2.More equations or functional relationships (not just $X \rightarrow Y$, but you can also analyze $W \rightarrow Z$ simultaneously).
- 3.Correlated errors, system of equations can have correlated errors . For example, the double-headed arrow between Y and Z.
- 4.Direct and indirect effects: X has a direct effect on Z and an indirect effect on Z via its effect on W. That is, $X \rightarrow Z$ and $X \rightarrow W \rightarrow Z$ are direct and indirect effects, respectively.
- 5. Latent variables. For example, LV in the path diagram has effects on X and W.
- 6.Parametric constraints. For example, the constraints on the path coefficients or effects labeled as 'a' in the upper path diagrams.
- 7.Multiple-group analysis. For different groups of populations, the overall structure of the model are the same, but the path constraints could be different---while the constrained effect in Group 1 is denoted as 'a,' the constrained effect in Group 2 is denoted as 'b,' which will have a different estimate than that for 'a' in Group 1.

Other Names for Structural Equation Modeling (SEM)

- Path analysis
- LISREL model (Jöreskog 1973, Keesling 1972, Wiley 1973)
- Covariance structures analysis
- Analysis of moment structures
- Confirmatory factor analysis
- Causal modeling
- CALIS: Covariance Analysis of Linear Structural Equations

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SEM has a lot of synonyms in the field: Path analysis (attributed to Sewall Wright), LISREL model (JKW model), covariance structures analysis, analysis of moment structures, confirmatory factor analysis, causal modeling, and etc. In terms of the statistical methodology involved, all these names are more or less the same.

PROC CALIS, which stands for covariance analysis of linear structural equations, is a software that was designed to handle all these analyses under the umbrella term SEM. Hopefully, one day PROC CALIS would also be remembered as a synonym of SEM.

SEM Software AMOS, EQS, LISREL, MPLUS, ... Why PROC CALIS? Which is best?

There are several well-known software in the field for doing SEM: AMOS, EQS, LISREL, and MPLUS, and may be more. Why PROC CALIS? Which is best? Although these are very interesting questions, as the current developer of PROC CALIS procedure I am not at liberty to judge other SEM software. This workshop gives you an introductory tour of SEM with the use of PROC CALIS. Therefore, you might compare PROC CALIS with other software on your own after learning some of the features of PROC CALIS.

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A Very Brief History of PROC CALIS

- Original developer: Wolfgang Hartmann (80's)
- Influences
 - o Statistical/mathematical: COSAN (McDonald 1978, 1980)
 - o Syntax: EQS (Bentler 1985, 1995)
- TCALIS (SAS 9.2, 2008): experimental version
- "New" CALIS (SAS 9.22, 2010): PATH modeling language, multiple-group analysis, mean structures, name-free approach to parameter specifications, and much more

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Let us start with a brief history of PROC CALIS.

In eighties, Wolfgang Hartmann designed and developed the first version of PROC CALIS. The statistical and mathematical model was greatly influenced by the COSAN model proposed by R. P. McDonald. In fact, there was evidence that Cosan, instead of Calis, might have been proposed as the name of the procedure. The most popular syntax in PROC CALIS, however, was under the influence of the EQS program by Peter Bentler. The LINEQS syntax in PROC CALIS for model specification is basically a twin brother of the syntax of the EQS program.

I picked up the development of the software around 2000. I actually rewrote the mathematical foundations of the software. I kept the optimization techniques and initial estimation techniques so that the new CALIS is compatible with the old CALIS.

In 2008, an experimental version called TCALIS was released. Since then, I have modified the syntax a little more and fixed some major bugs.

The new CALIS (SAS 9.22) has been released this year. If you have used PROC CALIS before, you will notice one major change: the emphasis on the PATH modeling language. You can see examples using the PATH statement everywhere in the PROC CALIS documentation. Other noteworthy new features are: multiple-group modeling, redesigned mean structure analysis, and the name-free approach to parameter specifications. Certainly, there are many more new features than these, as you will learn from this workshop and elsewhere.

Structure of the Workshop

- First Part: Basic Modeling
 - 1. A brief description of the process of SEM
 - 2. The PATH modeling language in PROC CALIS
 - 3. Specifying models and interpreting results
 - 4. LISMOD a language tailored to LISREL users
- Second Part: "Advanced" Modeling
 - 1. Multiple-group analysis
 - 2. Analyzing direct and indirect effects
 - 3. Testing specific hypotheses
 - 4. Model modifications

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The first part of the workshop is about the basic SEM modeling using PROC CALIS. I will describe the research process of SEM briefly. Then I will introduce the PATH modeling language in PROC CALIS by using a simple linear regression example. Next, I will move on to more complicated examples that analyze confirmatory-factor models. I will use PROC CALIS in these examples to show how you can specify SEM models by the PATH modeling language, in relation to the path diagram representations. I will show you how to interpret the results generated by PROC CALIS. I will end the first part by showing you how a LISREL model can be specified by the LISMOD statement in PROC CALIS.

The second part of the workshop is about "advanced" modeling---relatively speaking. I will show how multiple-group analysis can be done in PROC CALIS. Other important topics such as direct and indirect effect analysis, testing specific hypotheses, and model modifications are discussed.

Emphases of the Workshop

- Introducing the structural equation methodology and applications through examples – What is SEM?
- Analyzing structural equation models with PROC CALIS – How to do SEM?

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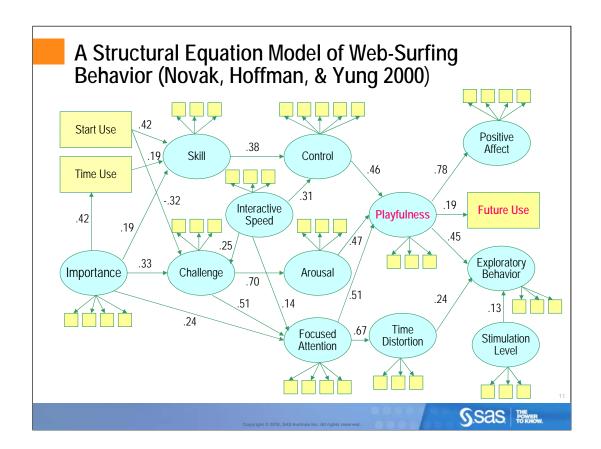
There are two emphases of this talk.

One, I want to show you an overall picture of SEM. This addresses the "what is SEM?" question. I will not give you a technical definition, but I will show you SEM examples so that you will have a "real" feeling about the applications of SEM.

Two, I want to show you how to use PROC CALIS. This addresses the "How to do SEM?" question. I hope that in the end of the workshop, you will find that PROC CALIS is very useful for SEM.

Illustrating the Process of Structural Equation Modeling

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This is a structural equation model about web-surfing behavior. The researchers hypothesize that the "Playfulness" of a web-site would enhance the future use ("Future Use") of the same web-site. However, the theory does not end there. The researchers then hypothesize what would make a web-site to be perceived as playful. Three additional constructs are hypothesized in the path diagram: "Control" (of the web-page), "Arousal" (of interest), and "Focused Attention" are determinants of "Playfulness." In fact, the researchers hypothesized even further. For example, they use "Start Use" (when the users started to use computers) and "Time Use" (how often they use computers) as remote "causes" of a lot of latent constructs in the path diagram. In sum, this is a relatively large SEM that theorizes complicated relationships among constructs.

In this path diagram, the oval shapes represent latent variables, which are not measured but serve as useful constructs in the model (e.g., "Playfulness"). The rectangles represent measured or observed variables (e.g., "Start Use", "Time Use", "Future Use"). In order to analyze the latent constructs, some measured variables (or indicators) are needed. In the path diagram, those small unlabeled rectangles are measured indicators for the latent constructs. In this research, these measured indicators are rating responses on a questionnaire. For example, "I lost track of the time when using this web-site" (this is not an exact item from the actual research) could be an item for the "Time Distortion" construct.

Given this path diagram for the theory about web-surfing behavior, an SEM software fits the model based on the observed data and informs you the model fit and the estimates of the effects (path coefficients) in the path diagram. The SEM software also tells you the significance of these estimates. If the model does not fit the data well, the SEM software would suggest ways to improve the model.

Key Features of SEM

- Analyzing complicated relationships among variables
- Path diagram representations for models
- Ability to handle latent and observed variables simultaneously
- Testing the model fit and significance of the parameters
- Suggesting ways to improve the model

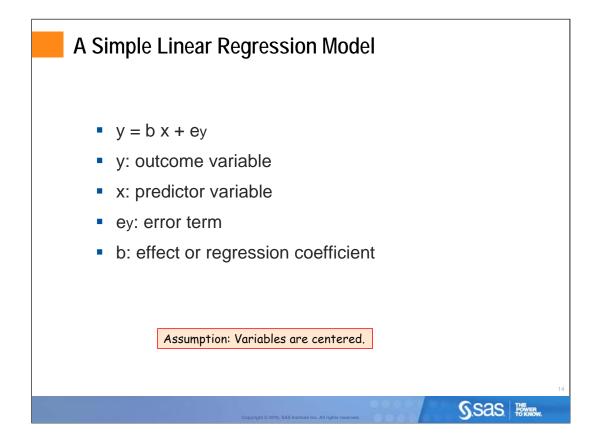
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Here is a list of the key features of SEM:

- Analyzing complicated relationships among variables
- Path diagram representations for models
- Ability to handle latent and observed variables simultaneously
- •Testing the model fit and significance of the parameters
- •Suggesting ways to improve the model

Basics: A Simple Regression Model and the PATH Modeling Language

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To introduce the PATH modeling language in PROC CALIS, a simple linear regression model is used. In the regression equation, y is the outcome variable, x is the predictor variable, e_y is the error term and b is the effect or regression coefficient. The regression model written in this form assumes that x and y are centered with means zero. But this assumption will not affect the generality to un-centered variables.



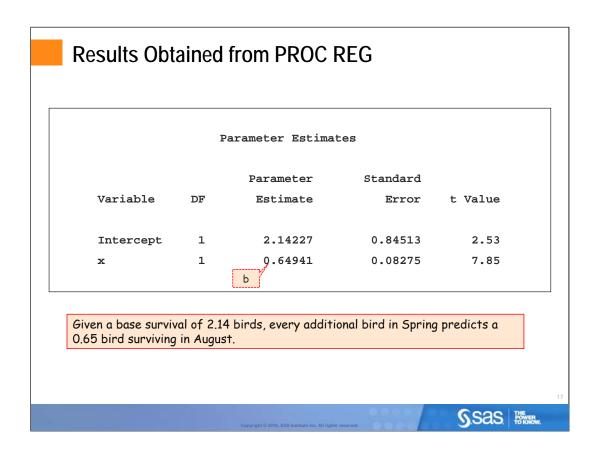
- Fuller (1987) p.34
- y: average of the number of birds in August
- x : average of the number of birds in Spring (April/May)
- Averages were based on the number of birds sighted by 15 trained observers
- Goal: How many birds will survive 3 months?

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On p.34 of Fuller's book "Measurement Error Models", he describes a data set about the counting of hen pheasants in April and August. Fifteen trained observers counted the number of birds in the two occasions. Y is the number of birds in August and X is the number of birds in April. The goal of the linear regression is to predict the number of birds in August (Fall) by the number of birds in April (Spring).

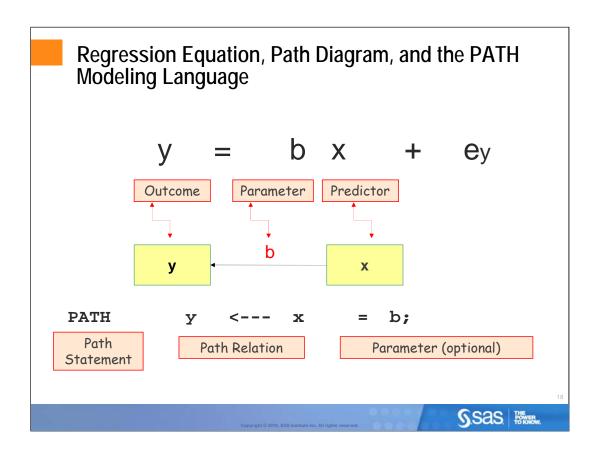
```
Regression Analysis by PROC REG
data hens;
  input y x @@;
  datalines;
               6.6
                   9.8 12.3 10.8 11.9 9.7 11.9 9.3 12
                    8.1 10.9 8.7 10.4 8.7 10.2 7.4 7.4
     9.6 6.9 7.5
10.1 11
              11.8
                    7.3
                         8.2
proc reg data=hens;
  model y = x;
run;
                                                Sas Books
```

To conduct a linear regression analysis, you can use a SAS procedure called PROC REG. The syntax is quite simple. First, define your data set. Second, call PROC REG with the interested data set specified in the PROC REG statement. Then, the model statement specifies that y = x, which means y is predicted by x. No error term needs to be specified, although PROC REG does assume that prediction is not perfect so that the error does exist with nonzero variance in the regression.



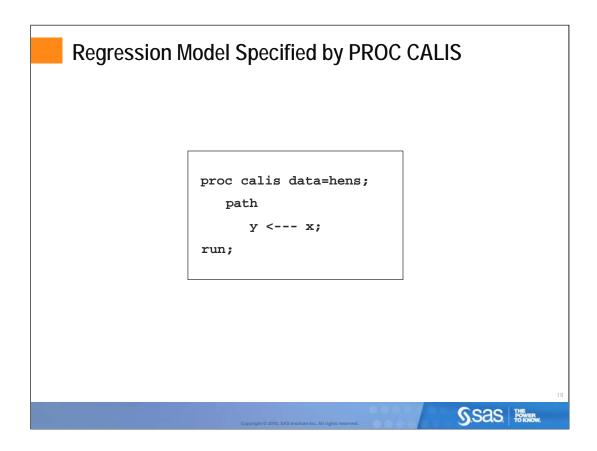
This table shows the essential results from PROC REG. The output shows an estimate of 0.65 for the regression coefficient b. The intercept estimate is 2.14. PROC REG also shows the standard error estimates and the t values for judging statistical significance. Both estimates are statistically significant.

An interpretation about these regression estimates is this: "Given a base survival of 2.14 birds, every additional bird in Spring predicts a 0.65 bird surviving in August (Fall)."

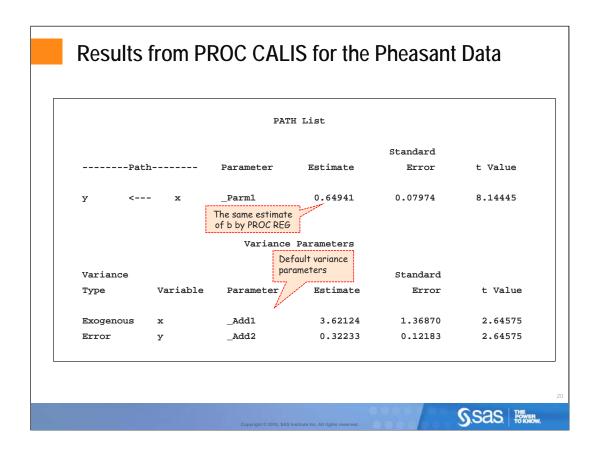


As shown previously, you can represent the linear regression model by the path diagram, which is also a representation scheme for SEM. Hence, regression models could be specified as SEM by using the path diagram.

Here is what you do to specify a simple linear regression model in PROC CALIS. You use the PATH statement to specify the path in the regression model. In this case, it is just Y<---X in the PATH statement. Optionally, you can denote the corresponding path coefficient parameter. For example, you can put "= b" at the back of the path to denote the parameter label or name.



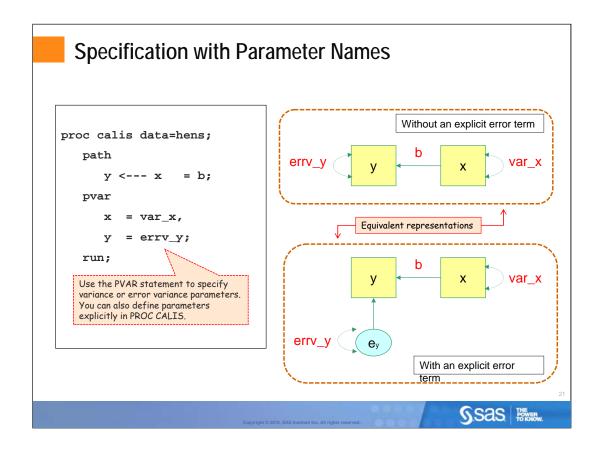
This is the entire PROC CALIS syntax for the simple linear regression model. Isn't that easy and simple?



This slide shows the results from PROC CALIS.

The estimated effect of x on y, denoted as y <--- x in the output, is 0.65, which is the same as that in the PROC REG results. Because you did not name this regression coefficient parameter (but you specify the path nonetheless), PROC CALIS generates a unique parameter name called _Parm1 for it. The standard error estimate and the t value are a little bit different from that of the PROC REG results. This is because different degrees of freedom for computing the standard errors are used in the two approaches.

In PROC CALIS, it also includes results for two more parameters in the SEM. The variance of x and the error variance of y are treated as model parameters. Their estimates are also shown in the PROC CALIS results. Note that PROC CALIS creates default parameter names for these default variances even though you did not specify them. In this example, these variance parameters are named "_Add1" and "_Add2", respectively.

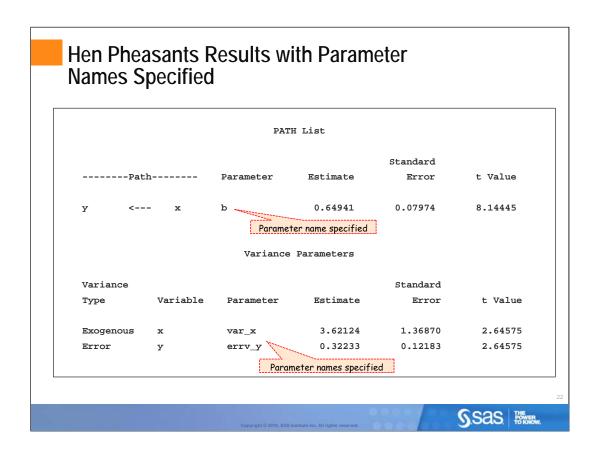


You could name all the parameters in PROC CALIS by putting your preferred names.

In the path diagram at the top right corner, the parameters are shown in red. In the regression model, b is the regression coefficient, var_x is the variance for the predictor variable x, and errv_y is the error variance of y. This path diagram representation is equivalent to the one shown at the bottom right corner, where an explicit error term is attached to Y. The error term is represented by an oval shape because it is treated as a latent variable. This representation has the same set of parameters, only that errv_y is now attached to the error variable directly.

You can specify these parameters explicitly in PROC CALIS. In the left panel of the slide, the parameter b is specified after the y <--- x path, separated by an equal sign. To specify the variances or error variances in the model, you can use the PVAR statement. For example, " $x = var_x$ " means that the variance of x is a parameter called " var_x ".

Notice that naming parameters is entirely optional. For this example, naming parameters appears to serve only as an illustration. Later in this talk, you will find situations where the use of parameter names is not only useful, but also necessary.



As shown in this slide, the numerical results from PROC CALIS with explicit parameter names specified are the same as those without using parameter names. The only difference is that now you can use these parameter names to locate the corresponding results directly.

Keys to the PATH Modeling Language

- As easy as drawing a path diagram
- PATH statement specifies the functional relationships required specification
- PROC CALIS sets variances and error variances by default – optional specification (most of the time)
- Naming free parameters is optional

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So far, I have shown you that:

- 1. The PATH modeling language is as easy as drawing a path diagram.
- 2. You can use the PATH statement to specify the paths in path diagram, with or without specify the parameter names for the path coefficients.
- 3. You can also specify the variance or error variance parameters explicitly. In most practical applications, variances and error variances have already been set by default and you do not need to worry about specifying them. The essential part of SEM is specified in the PATH statement.
- 4. Naming parameters is optional in PROC CALIS.

Measurement Errors in Predictors

- Bird counting might involve measurement errors in x
- x = fx + ex
- fx: true score, but not observed
- x : observed, but with measurement error ex

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Let us make a little step forward to show a special SEM feature that linear regression cannot handle easily.

In the bird counting example, we did not take into account that bird counting could involve measurement errors. In the current context, the measurement error in bird counting could be due to the environment factors in the forest: obstruction from the tree branches, "biased" angles from the bird observers, and etc.

Mathematically, you can hypothesize a variable called fx to represent the "true" counts obtained from the bird observed. The observed number of birds x is the sum of fx, the true score, and ex, an error term.

What you got from the data is x, the observed fallible score. However, ideally, you would want to use fx, the true score in your regression analysis.

A Measurement Error Model for the Pheasant Data

Structural Equation

$$y = b fx + ey$$

Measurement equation

$$x = fx + ex$$

- Can you estimate b?
- Problem: The measurement equation introduces an additional parameter: Var(ex) (variance of ex or error variance of x)

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The preceding idea is formalized as the following SEM with a latent variable fx.

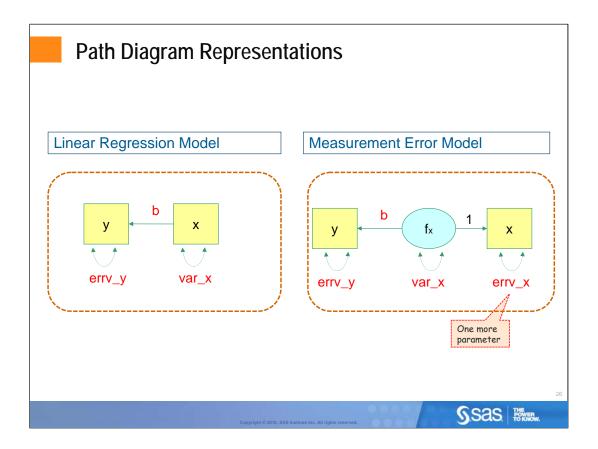
In the so-called structural model, y is predicted from fx, the true score, in the linear regression model. This so-called structural equation takes the role of the original linear regression equation---only now you are supposed to have a better model by using the measurement error-free fx as the predictor.

In the so-called measurement model, you hypothesize that the observed variable x is obtained as the sum of fx and an measurement error term e x.

Can you estimate b with the latent variable fx in the structural equation?

This answer is yes.

But the technical problem encountered here is that the measurement equation introduces one additional parameters in var(ex)---error variance of x. This problem will make the SEM unidentified. In a very loose sense, this means that your model estimates more parameters than would be allowed by the given information of the data set. Consequently, the parameters in the model are not estimable. I will describe a method to deal with this identification problem later.



This slide compares the linear regression model with the measurement error model by the use of path diagram. It demonstrates why the measurement error model has one more parameter to estimate.

In the left panel, the path diagram for the simple linear regression analysis is shown.

In the right panel for the measurement error model, we still have x and y as the observed variables. But now we have a latent variable fx that takes the role of the predictor of y. Var_x in this model now represents the true variance of the predictor fx. The new parameter in the measurement error model is errv_x (error variance of x). With this additional parameter, we need to make additional assumption to estimate the model parameters.

Constraining the Error Variances

- Bird counting is more accurate in fall (y) than in spring (x)
- In an independent study, error variance (for x) in spring is six times as much as that (for y) in fall
- Fuller's recommendation: Var(ex) = 6 Var(ey)

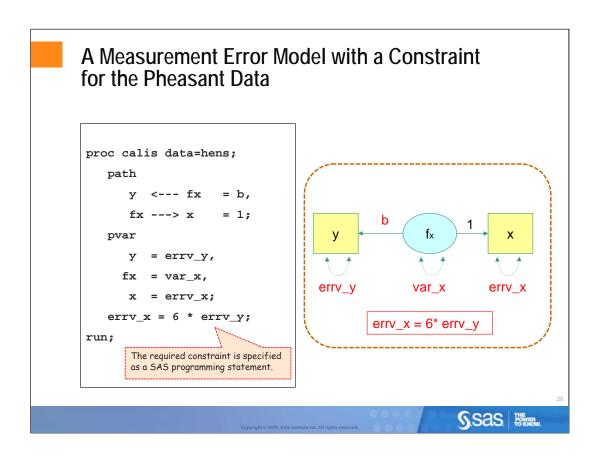
$$errv_x = 6* errv_y$$

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Fortunately, we have a reasonable assumption about the relative size of the error variances in the model.

This assumption is based on the fact that bird counting in Fall is more accurate than that in spring. The reason is that the fallen leaves in Fall makes the counting of birds less obstructive.

The assumption we are going to make is based on an independent study about the relative error variances in x and in y. In Fuller's book, the ratio of these variances is about 6. Mathematically, Var(ex) = 6*Var(ey). That is, error variance for x is six times as much as the error variance of y. Or, in the PROC CALIS specification, you want to state the following parametric constraint in the modeling: errv_x=6*errv_y.



It turns out that it is pretty straightforward to specify this parametric constraint in PROC CALIS. You just simply add one more line of code to represent this relationship, as shown in the SAS code of the slide. In the SAS literature, this line of code is called a SAS programming statement, which is used extensively in the DATA step of SAS. You can use as many SAS programming statements as you want to describe the relationships of the parameters in the model.

		PAT	H List		
		Standard			
Path		Parameter	Estimate	Error	t Value
у <	- fx	b	0.75158	0.09228	8.14427
		Variance	esti	rger estimated effe mated without takin surement error into	g the
Variance			Standard		
Type	Variable	Parameter	Estimate	Error	t Value
Error	У	errv_y	0.08205	0.03101	2.64575
Exogenous	fx	var_x	3.12893	1.36180	2.29765
Error	x	errv_x	0.49231	0.18608	2.64575

After you take the measurement error into account, the regression coefficient b is now 0.75, which is a larger effect than 0.649, which you obtained from the linear regression model without taking the measurement error in x into account. Therefore, the previous regression analysis underestimated this effect because it failed to incorporate the measurement error into the model. However, with SEM, you can easily incorporate the measurement errors into the analysis.

Estimates of the variances and error variances are shown in the next table. You can see that the constraint specified in the PROC CALIS is honored in the estimation. The error variance estimate of x is 0.49, which is six times as much as the error variance estimate of y, which is 0.08.

Some Features of the PATH Modeling Language

- Specifying paths in the PATH statement is straightforward
- Deals with latent variables easily variables are latent if they are not present in the data set
- PVAR statement for specifying variances and error variances
- PCOV statement for specifying covariances and error covariances (to be shown)
- Parameter dependency can be specified by the SAS programming statements. For example,

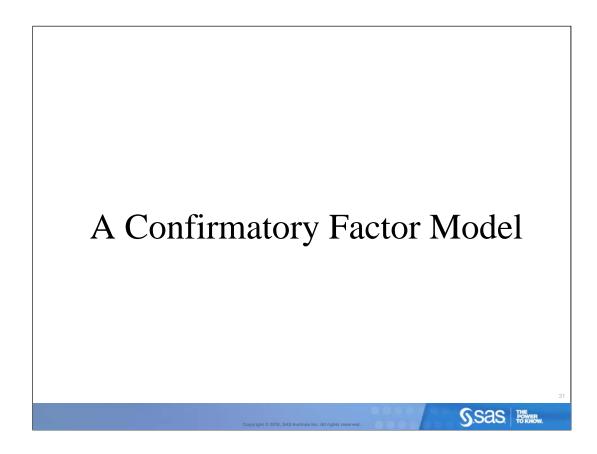
```
parm1 = 4 * parm2 + exp(parm4) ** parm6;
```

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This slide summarizes some features of the PATH modeling language.

- 1.It is as straightforward as drawing the paths.
- 2.It can deal with latent variables easily.
- 3. You can use the PVAR statement to specify variances or error variances (double-headed arrows attached to individual variables in the path diagram).
- 4. You can use the PCOV statement to specify covariances or error covariances (double-headed arrows attached to pairs of variables in the path diagram).
- 5. You can specify parameter dependency by using the SAS programming statements directly. Indeed, even very strange and complicated (continuous) parametric functions are supported in PROC CALIS.



We now move on to a more complicated type of structural equation models called confirmatory factor models.

Political Democracy Data

- Bollen (1989) Chapter 7
- Two latent factors: political democracy in 75 developing countries in 1960 and 1965
- Four indicator measures for the latent factors in each year:
 - Freedom of press (Press60, Press65)
 - Freedom of group oppositions (Freop60, Freop65)
 - o Fairness of elections (Fair60, Fair65)
 - Elective nature of the legislative body (Legis60, Legis65)
- Purpose of the confirmatory factor analysis: Validate the measurement indicators

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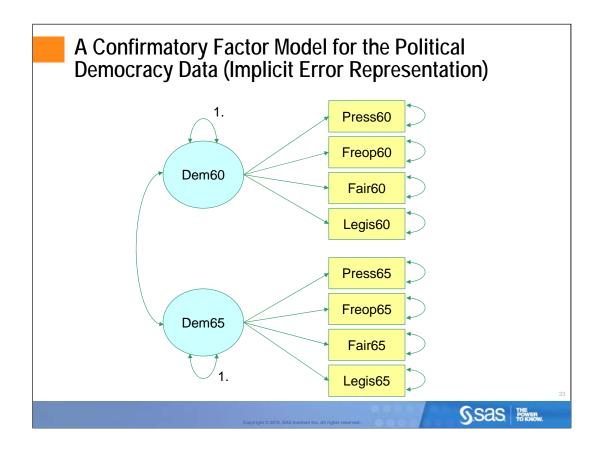
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This example is based on an example in Chapter 7 of Bollen's classic textbook: Structural Equation Modeling.

In this example, two latent factors for measuring political democracy in 75 developing countries in 1960 and 1965 were hypothesized.

These two latent factors are not observed, but they have some related observed variables that serve as indicators. In each year, you measure four variables to gauge the political democracy: freedom of press, freedom of group oppositions, fairness of elections, and elective nature of the legislative body.

The purpose of the confirmatory factor analysis is to validate these measurement indicators statistically.

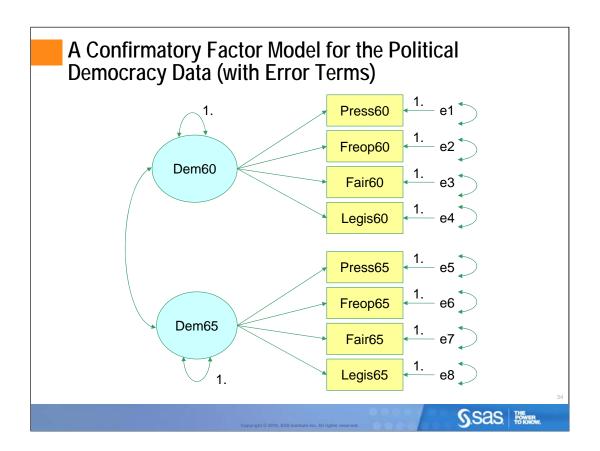


This path diagram shows the hypothesized confirmatory factor model.

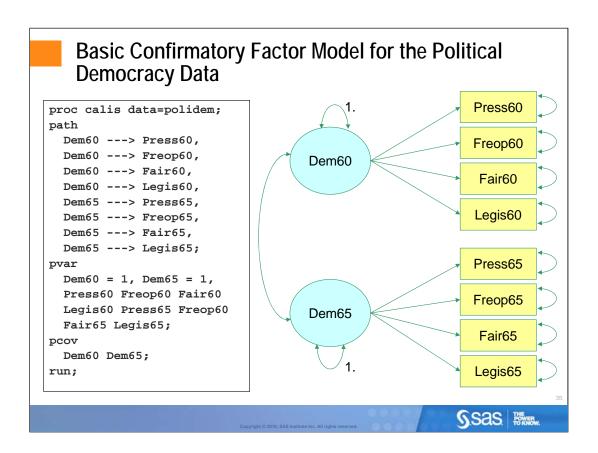
In the path diagram, two latent factors are represented by two ovals. Dem60 is the political democracy in 1960 and Dem65 is the political democracy in 1965. They are linked to the respective measured variables, as shown in the path diagram. These single-headed paths represent the typical factor-observed variable relationships.

The double-headed arrow that connects Dem60 and Dem65 represents the covariance parameter between the two factors. It means that the two factors are correlated. Double-headed arrows that are attached to Dem60 and Dem65 individually represent the variance parameters of the two factors. In the model, you fix these variances to 1 so that the scales of the factors are identified. This is conventionally done because the scale of latent factors is arbitrary (you do not measure latent variables directly so that they could be defined on any unit of measurement).

The double-headed arrows that are attached to the observed variables represent the error variances. They signify the fact that the factors in the model do not account for 100% of the variances of the observed variables. The error variances are the unique part of the variances in the variables that are not due to their relationships with the factors in the model.



This is an alternative path diagram representation with the use of explicit error terms. Notice that the double-headed arrows for the observed variables now shift to the error terms. This path diagram representation is shown here only for illustration purposes. In this workshop, I rely on the path diagram representation that does not use explicit error terms.

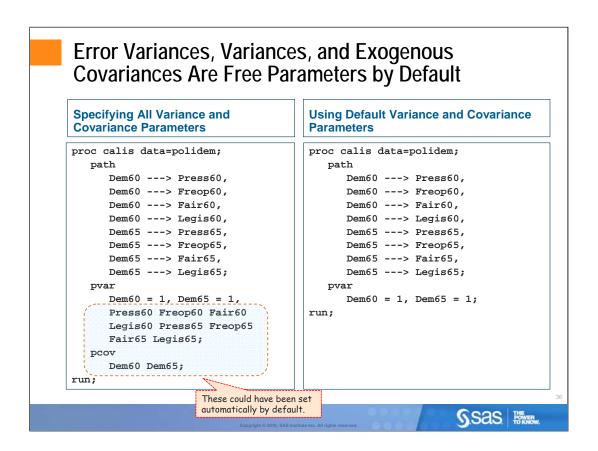


Specifying the CFA model is not much harder than the previous measurement error model. Basically, you only need to specify more paths for the CFA model.

In the PATH statement, you specify all the single-headed paths (arrows) in the path diagram.

In the PVAR statement, you specify all double-headed arrows that are attached to individual variables. PVAR actually stands for partial variance---you can specify the variances and error variances in this statement. "Dem60 =1" means that the variance of Dem60 is fixed to one. Similarly for "Dem65=1". The eight observed variable are specified in the PVAR statement to signify that their error variances are free parameters in the model.

In the PCOV statement, you specify pairs of variables that have covariances or error covariances as parameters in the model. In the current path diagram, Dem60 and Dem65 are correlated.



To make model specification more efficient and error-free, PROC CALIS employs default free parameters in the model. These default free parameters are set because they are commonly employed in practice.

For example, because predictions of outcome variables are usually not perfect, the error variances are free parameters by default. This means that all the PVAR specifications for the observed variables are not necessary because PROC CALIS would have treated them as free parameters by default.

Similarly, the variances of Dem60 and Dem65 and their covariance are default free parameters because they are assumed in most practical applications. In the current example, this means that the PCOV statement specification for the covariance between Dem60 and Dem65 is not necessary.

However, because the variances of Dem60 and Dem65 are fixed to 1 (for identification of the latent variable scales), they must be specified explicitly in the PVAR statement. Otherwise, these variances would have been free parameters by default.

			PATH	List		
					Standard	
	Path-		Parameter	Estimate	Error	t Value
Dem60	>	Press60	_Parm1	2.20567	0.25122	8.77998
Dem60	>	Freop60	_Parm2	3.00132	0.39735	7.55335
Dem60	>	Fair60	_Parm3	2.31033	0.34026	6.78989
Dem60	>	Legis60	_Parm4	2.89483	0.31582	9.16619
Dem65	>	Press65	_Parm5	2.04790	0.25930	7.89771
Dem65	>	Freop65	_Parm6	2.68003	0.33258	8.05834
Dem65	>	Fair65	_Parm7	2.70879	0.31804	8.51711
Dem65	>	Legis65	_Parm8	2.76604	0.30830	8.97190

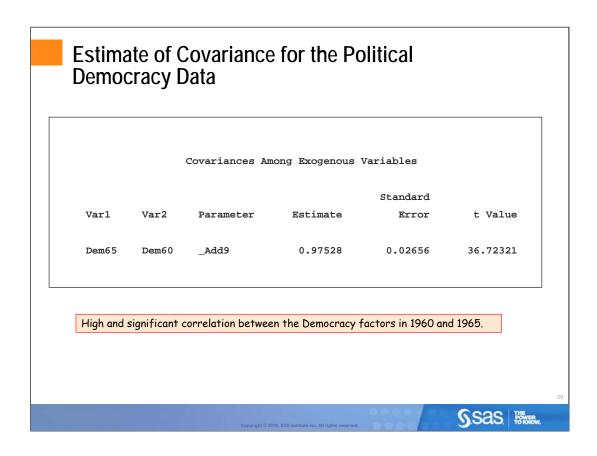
This table shows the estimates of path coefficients from PROC CALIS.

In the factor analysis literature, these path coefficients are also called loadings. To validate the relationships between the democracy factors and the observed variables, the t-values must be examined for statistical significance. Using normal approximation, t values with their absolute values bigger than 1.96 are significantly different from zero.

In a typical factor-analysis study, you would want all these t-values to be significant in order to claim nonzero factor-variable relationships. An insignificant t-value means that the corresponding variable is not an indicator for the purported factor. Insignificant t-values for path coefficients would challenge the validity of your factor model.

		Variance	Parameters		
Variance				Standard	
Type	Variable	Parameter	Estimate	Error	t Value
Exogenous	Dem60		1.00000		
	Dem65		1.00000		
Error	Press60	_Add1	2.01359	0.41048	4.90549
	Freop60	_Add2	6.57189	1.20964	5.43294
	Fair60	_Add3	5.42661	0.96546	5.62076
	Legis60	_Add4	2.83887	0.61417	4.62229
	Press65	_Add5	2.63180	0.49311	5.33709
	Freop65	_Add6	4.19276	0.79422	5.27906
	Fair65	_Add7	3.46180	0.68155	5.07928
	Legis65	Add8	2.88292	0.59927	4.81068

Estimates of variances and error variances are shown in this table. The variances of Dem60 and Dem65 are fixed to 1 and therefore there are no significance tests for these variances. All other error variance estimates are significantly larger than zeros. This also means that the factors do not account for all the variances of the observed variables. This is natural because deterministic relationships between factors and observed variables are rare.



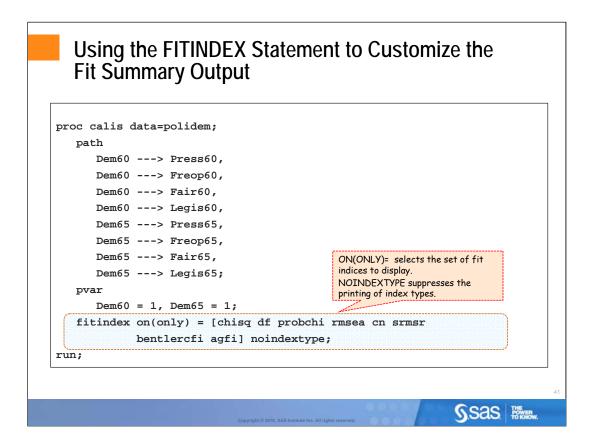
This table shows the covariance between Dem60 and Dem65. This estimate is also the estimated correlation between the two latent factors because the variances of the factors are fixed to one. This correlation is extremely high, possibly because the political democracy status do not change much during those 5 years.

	Fit Summary		
Modeling Info	N Observations N Variables N Moments	75 8 36	
	N Parameters N Active Constraints Baseline Model Function Value	17 0 6.1482	
Absolute Index	Baseline Model Chi-Square Baseline Model Chi-Square DF Pr > Baseline Model Chi-Square Fit Function	454.9633 28 <.0001 0.6009	
INCA	Chi-Square Chi-Square DF Pr > Chi-Square	44.4686 19 0.0008	
	Z-Test of Wilson & Hilferty Hoelter Critical N Root Mean Square Residual (RMSR) Standardized RMSR (SRMSR)	3.1383 51 0.5388 0.0494	
Parsimony Index	Goodness of Fit Index (GFI) Adjusted GFI (AGFI) Parsimonious GFI RMSEA Estimate	0.8658 0.7457 0.5875 0.1346	***
	RMSEA Lower 90% Confidence Limit RMSEA Upper 90% Confidence Limit Probability of Close Fit ECVI Estimate	0.0833 0.1865 0.0062 1.1240	A lot of fit indices, but researchers
	ECVI Lower 90% Confidence Limit ECVI Upper 90% Confidence Limit Akaike Information Criterion Bozdoran CAIC	0.9065 1.4608 78.4686 134.8659	usually report just a few of them.
Incremental Index	Schwarz Bayesian Criterion McDonald Centrality Bentler Comparative Fit Index	117.8659 0.8438 0.9403	
	Bentler-Bonett NFI Bentler-Bonett Non-normed Index Bollen Normed Index Rhol	0.9023 0.9121 0.8560	
	Bollen Non-normed Index Delta2 James et al. Parsimonious NFI	0.9416 0.6122	

We have looked at the estimates and concluded that the relationships between the factors and the variables are strong and significant. Those results validated the individual factor-variable relationships.

To gain support for the overall confirmatory factor model, you would want to examine the model fit statistics. This table shows various fit indices computed by PROC CALIS. In the SEM field, a large number of fit indices have been proposed. There is no consensus as to which indices are best to report in the research. But researchers tend to report some of the most popular ones in their respective fields.

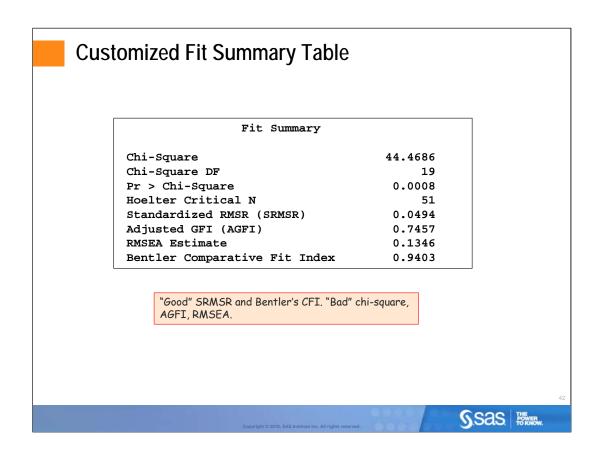
Because a large number of indices might be confusing, PROC CALIS provides a way to customize this fit summary table.



You can use the FITINDEX statement to customize your fit summary table.

Use the ON(ONLY)= option to select your "favorite" fit indices.

Use the NOINDEXTYPE option to suppress the printing of the fit index types.



This is the customized fit summary output by using the previous FITINDEX statement specifications.

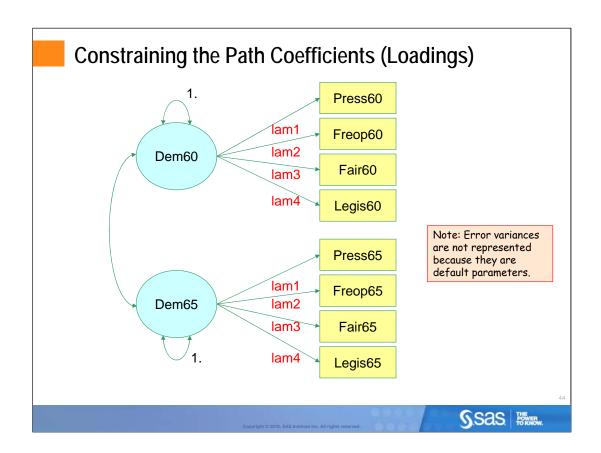
This table contains the more popular fit indices reported in research (as recognized by the author).

In practice, the model fit chi-square model statistic, its df, and the corresponding p-value are routinely reported even though very few researchers in the field would use the model fit chi-square alone to judge model fit. As shown in this table, the p-value is very small so that statistically it means that the hypothesized model should be rejected. However, it is a known issue in SEM that even very useful SEM models with minimum departures from the data would be rejected statistically. Therefore, researchers in the SEM field tend to focus more on other fit indices to judge model fit.

The SRMSR, AGFI, RMSEA, and CFI are four of the most popular fit indices in the SEM field. See the glossary page for the descriptions of these fit indices. For the SRMSR and RMSEA, the smaller the values the better the fit. Usually, values under 0.05 indicate good model fit. Therefore, the SRMSR says that the current model is good, but the RMSEA says that the current model is bad. For the AGFI and Bentler's CFI, the larger the values the better the model fit. Therefore, the AGFI says that the current model is bad, but the CFI says that it is good. Because these indices do not consistently indicate a good model fit, it is safe to say that the current CFA model is promising, but it needs further confirmation.

A Confirmatory Factor Model with Loading Constraints

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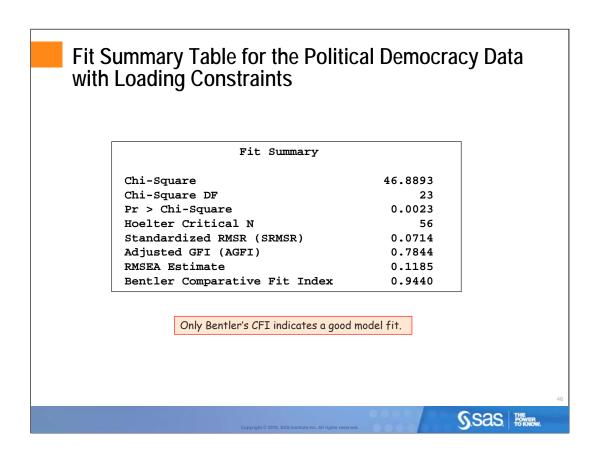


In addition to fitting a basic confirmatory factor model, PROC CALIS enables you to set up parameter constraints easily. The main tool is to use parameter names in the specification.

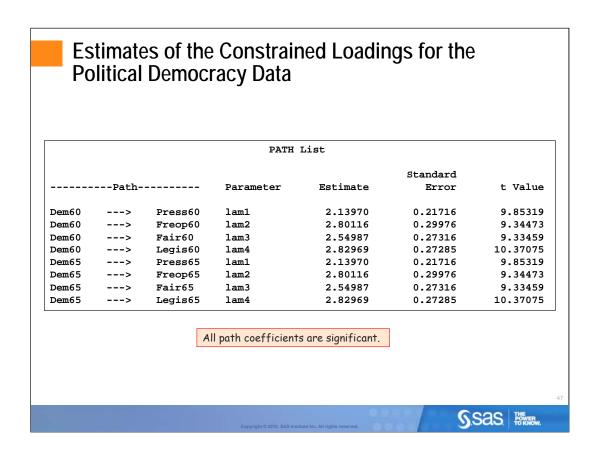
For the political democracy example, the researcher wants to constraint the factor loadings (path coefficients) across time. The theoretical reason is that basically the measured variables are the same in the two years. In the path diagram, you can represent equality constraints by putting the same parameter names or labels to the pairs of the related paths. For example, lam1 is the loading of Press60 on Dem60. It is also the loading of Press65 on Dem65. Similarly, you can set the other 3 sets of constraints in the path diagram.

Fitting a CFA Model with Constraints on the Loadings proc calis data=polidem; path Dem60 ---> Press60 = lam1, These constrain the path coefficients. Dem60 ---> Freop60 = lam2,Dem60 ---> Fair60 = lam3,Dem60 ---> Legis60 = lam4,Dem65 ---> Press65 = lam1, Dem65 ---> Freop65 = lam2, Dem65 ---> Fair65 = lam3, Dem65 ---> Legis65 = lam4; Dem60 = 1, Dem65 = 1;fitindex on(only) = [chisq df probchi rmsea cn srmsr bentlercfi agfi] noindextype; run; Sas Book

In the PATH modeling language, the constraints could be handled similarly. The code shown in this slide is modified from the previous code by adding the parameter names in the paths. The syntax is to add an equal sign and then the parameter names after the path specifications in the PATH statement. With the same parameter names for the pairs of the related paths, the estimates would be exactly the same.



This table shows the fit summary of the model with the loading constraints. Because of the constraints, this model does not fit as well as the previous model. The SRMSR is larger than 0.05. The AGFI is much smaller than 0.9. The RMSEA is much larger than 0.05. All these show a bad model fit. However, Bentler's CFI (0.94) shows a good model fit.



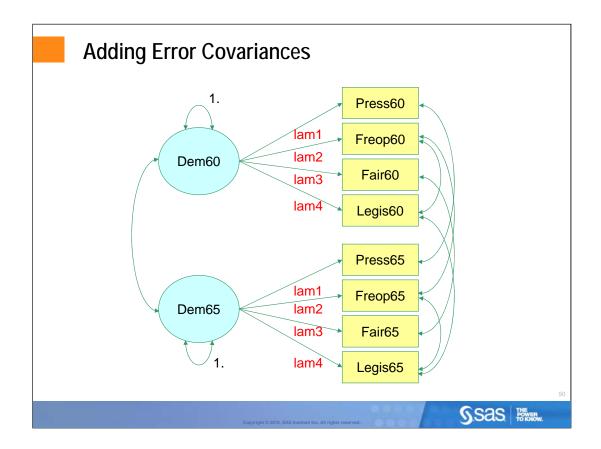
As required from the model, paths with the same loading parameter have the same estimates. For example, both Dem60--->Press60 and Dem65--->Press65 have a loading estimate of 2.14 (lam1). All loading estimates, again, are statistically significant. This shows that all the purported factor-variable relationships are supported.

Estimates of Variances and Covariances for the Political Democracy Data with Loading Constraints Variance Parameters Standard Variance Variable t Value Type Parameter Estimate Error Exogenous Dem60 1.00000 Dem65 1.00000 _Add1 Error Press60 2.01017 0.40312 4.98647 _Add2 Freop60 6.72037 1.21196 5.54503 _Add3 Legis60 0.60956 4.73243 2.88468 _Add4 Press65 2.61966 0.49456 5.29699 _Add5 Freop65 4.16958 0.79818 5.22383 Legis65 0.59556 4.78593 _Add6 2.85029 _Add7 Fair60 5.40824 0.97833 5.52803 _Add8 Fair65 3.55382 0.67700 5.24935 Covariances Among Exogenous Variables Standard Var1 Var2 Parameter Estimate Error t Value Dem65 Dem60 _Add9 0.97480 0.02682 36.34662 Sas 聯編

All the error variance estimates are also significant. The correlation between Dem60 and Dem60 is very high and significant.

A Confirmatory Factor Model with Correlated Errors

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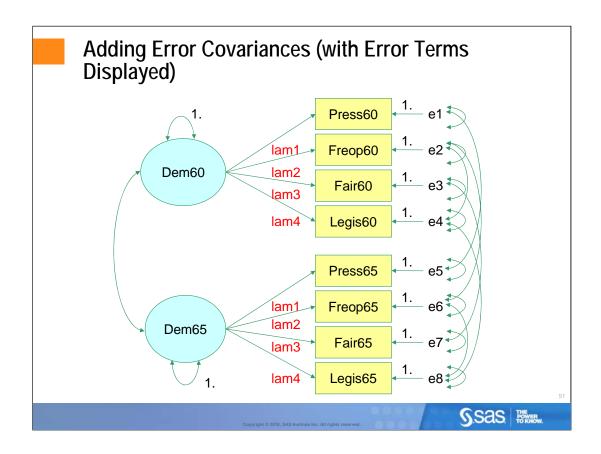
With the loading constraints, you observed a worse model fit.

The four equality constraints on the loadings you basically reduce the number of model parameters by 4. This naturally leads to a worse model fit than if you would allow all the loadings to be freely estimated.

Now you consider an opposite direction. Instead of reducing parameters by putting equality constraints, you want to add more parameters to the model. Adding more parameters to your model would improve the model fit. But the drawback of adding more parameters is that it makes your model more complicated, which is usually judged as an undesirable property for a scientific theory. It does not mean that you cannot add parameters. It only means that you should add only those parameters that could be justified by theoretical or substantive reasons.

In this example, it has been argued that freedom of group opposition and the elective nature of the legislative body have a part of their correlation that is beyond their common latent factors could explain (see Bollen). In SEM, this "extra" correlation is conceptualized as a correlation (or covariance) between the errors of the two variables. In the path diagram, this error covariance is represented by a double-headed arrow connecting the two variables. That is, Freop60 and Legis60 are connected by a double-headed arrow in 1960. By the same argument, Freop65 and Legis65 are also connected by a double-headed arrow to represent error covariance.

In addition, it is argued in Bollen that each of the variable pairs that were of the same nature but were measured at different times have a part of correlation that is beyond their common latent factors could explain. For example, Press60 and Press65 are connected by a double-headed arrow to represent their error covariance, which explains the part of the covariance between the two variables that is beyond the explanation by the covariance between Dem60 and Dem65. Similarly, the Freop-, Fair-, and Legis- pairs are all connected by double-headed arrows to represent error covariances.



The path diagram in this slide is equivalent to the previous representation that does not use explicit error variables.

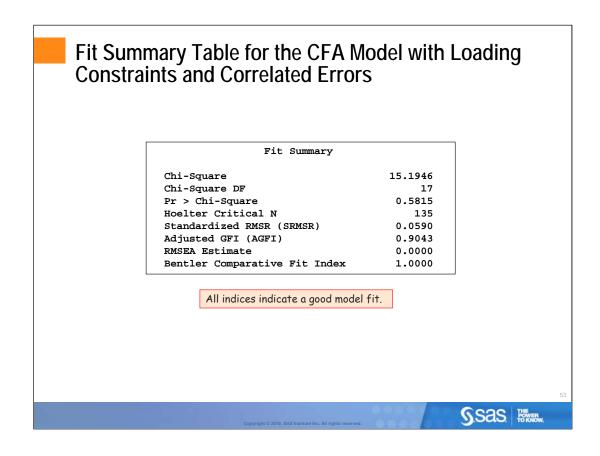
In this path diagram, error terms for the measured variables are shown. The double-headed arrows are shifted to the error terms. This makes it obvious that those double-headed arrows are covariances between the error variables (but not as partial covariances between the observed variables, as shown in the previous slide).

Therefore, this path diagram representation is conceptually clearer about what are really being correlated in the model. However, the addition of the error terms makes the path diagram more cluttered. In this workshop, I would stick with the path diagram representation that does not use explicit error terms.

Fitting a CFA Model with Loading Constraints and Correlated Errors proc calis data=polidem; path Dem60 ---> Press60 = lam1,Dem60 ---> Freop60 = lam2,Dem60 ---> Fair60 = lam3,Dem60 ---> Legis60 = lam4, = lam1,Dem65 ---> Press65 Dem65 ---> Freop65 = lam2,Dem65 ---> Fair65 = lam3,Dem65 ---> Legis65 = lam4; Use the PCOV statement to specify error covariances. Dem60 = 1, Dem65 = 1;Freop60 Legis60, Freop65 Legis65, Press60 Press65, Freop60 Freop65, Fair60 Fair65, Legis60 Legis65; fitindex on(only) = [chisq df probchi rmsea cn srmsr bentlercfi agfi] noindextype; run; Sas Books

With the six additional pairs of correlated errors, you have six more error covariance parameters in the model.

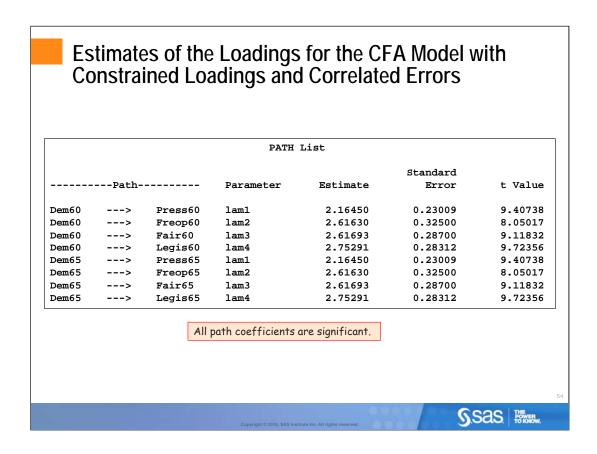
In the PATH modeling language, you can specify these covariance parameters in the PCOV statement. In this example, this means that you enumerate the six pairs of measured variables in the PCOV statement. For example, the first pair is Freop60 and Legis60, which represent a covariance parameter between their error terms.



This model is supposed to fit better because of the added parameters for the error covariances.

In fact, the model fit chi-square is not statistically significant. This supports the hypothesized model in the population.

All other fit indices show good or excellent fit. The SRMSR is 0.059, which is only slightly larger than the 0.05 criterion. The AGFI is 0.90, which is an indication of good model fit by convention. The RMSEA is essentially zero, which is the smallest RMSEA you could ever get. The CFI is 1, which is also the largest CFI you could ever get.



All loading (path coefficients) estimates are statistically significant, supporting the relationships between the latent factors and the measured variables.

Estimates of the Variances for the CFA Model with **Constrained Loadings and Correlated Errors** Variance Parameters Standard Variance Type Variable Parameter Estimate Error t Value 1.00000 Exogenous Dem60 Dem65 1.00000 _Add1 Error Press60 1.91664 0.43982 4.35780 _Add2 1.39023 5.50661 Freop60 7.65544 _Add3 Legis60 3.27028 0.73387 4.45621 _Add4 Press65 2.52969 0.52882 4.78360 Freop65 _Add5 4.87208 0.94384 5.16199 _Add6 Legis65 3.25392 0.73319 4.43805 _Add7 Fair60 5.03798 0.98299 5.12514 0.71220 Fair65 _Add8 3.32508 4.66875 All error variance estimates are significant. Sas Books

All error variance estimates are significant.

	C	Covariances Amo	ong Exogenous V	ariables	
Standard					
Var1	Var2	Parameter	Estimate	Error	t Value
Dem65	Dem60	_Add9	0.96603	0.02928	32.99044
		Covariano	es Among Error	5	
Error	Error			Standard	
o£	of	Parameter	Estimate	Error	t Value
reop60	Legis60	_Parm1	1.42826	0.69666	2.05017
reop65	Legis65	_Parm2	1.26677	0.59365	2.13389
ress60	Press65	_Parm3	0.58548	0.37178	1.57478
reop60	Freop65	_Parm4	2.09624	0.74763	2.80386
air60	Fair65	_Parm5	0.74805	0.62336	1.20003
Legis60	Legis65	_Parm6	0.47686	0.46214	1.03186

The first table shows the correlation between the two latent factors. Again, the correlation is very high and significant.

The second table shows the estimates for the newly added covariances between errors. Three of these covariances are significant, while the others are not. For example, Freop60 and Legis60, Freop65 and Legis65, and Freop60 and Freop65 are three error covariances that have t values larger than 1.96. The other three pairs have insignificant t-values. This means that adding these three covariances might be somewhat undesirable because their estimates are actually not significantly different from zero, casting doubts about their presence in the model.

The lesson here is that even though adding error correlations (or covariances) might improve the model fit, you should not routinely add error covariances only to boost the model fit. Adding unjustified error covariances makes your model more complicated and harder to interpret, especially when some error variance estimates turn out to be insignificant.

Political Democracy and Industrialization: A Full Structural Equation Model

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Political Democracy and Industrialization

- Bollen (1989) Chapter 8
- A full structural equation model (a full LISREL model)
- Additional variables for measuring industrialization (Indust) in 1960
 - Gross national product per capita (Gnppc60)
 - Energy consumption per capita (Enpc60)
 - Percent of labor force in industrial occupations (Indlf60)
- Purposes: Validate the measurement model and the structural relationships

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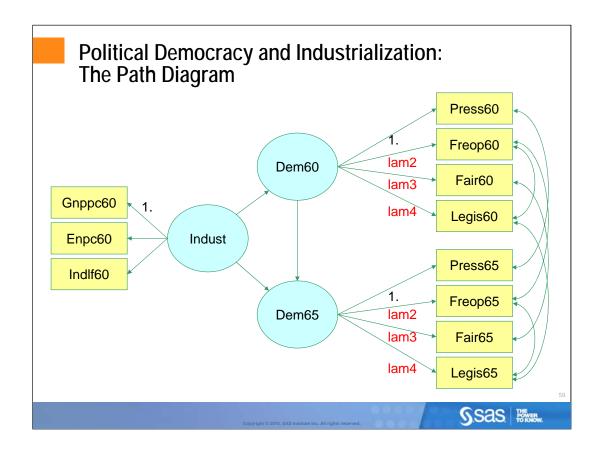
Sas POWER

We continue with the previous model and add one more latent factor and its indicators into the model.

This example illustrates a full structural equation model (or a full LISREL) model. Essentially, this means that our focus is not only on validating the relationships between the latent factors and the measured variables (that is, the measurement model), but also on validating the functional relationships among latent variables (that is, the structural model).

For example, you have a latent factor called industrialization (Induct) that is supposed to be reflected by three observed variables: gross national product per capita (Gnppc60), energy consumption per capita (enpc60), and percent of labor force in industrial occupations (Indlf60). All these variables were measured in 1960.

The industrialization (Induct) latent variable serves as a predictor of the two democracy factors (Dem60 and Dem65). This kind of functional relationships between latent variables has not been explored in the confirmatory factor models discussed previously.

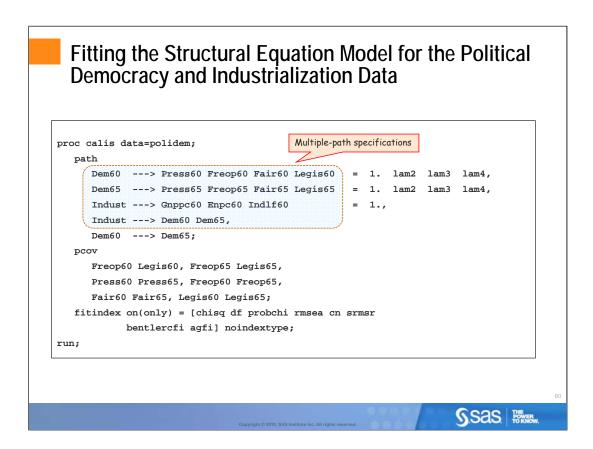


The entire SEM model is depicted in the path diagram of the current slide. The most notable addition is the paths from Indust to Dem60 and Dem65--- industrialization in 1960 serves as a predictor of democracy in both 1960 and 1965. Three observed variables serve as indicators of the industrialization: Gnppc60, Enpc60, and Indlf60.

There are two main modifications from the preceding confirmatory factor model.

First, instead of allowing Dem60 and Dem65 to freely covary in the CFA, the current model treats Dem60 as a predictor of Dem65.

Second, a different method for identifying the latent factor scales is used in the current model. In the preceding CFA model, variances of Dem60 and Dem65 are fixed to one. But because they become endogenous in the current model, you can no longer use this type of scale identification method. Instead, one of their observed indicator variables (that is, Press60 and Press65) now has a fixed path coefficient at one. Similarly, the path coefficient from Indust to Gnppc60 is fixed to one for scale identification.

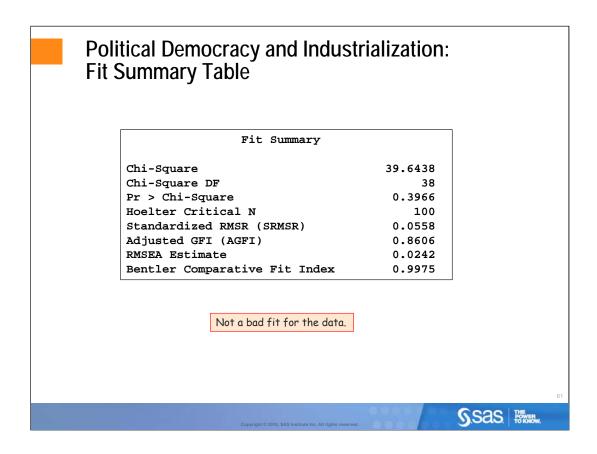


You can use PROC CALIS to specify this structural equation model easily.

In the PATH statement, I use a multiple-path specification syntax. In the first specification, Dem60 is a predictor of 4 outcome variables: Press60, Freop60, Fair60, and Legis60. This specifies four paths in a single path specification. After using an equal sign, I specify four parameters for the four paths. The first one is a fixed constant 1, which is applied to the Dem60 ---> Press60 path. The second one is a free parameter lam2, which is applied to the Dem60 ---> Freop60 path, and so on.

In the next 3 path specifications, I also use the multiple-path specification syntax. The second multiple-path syntax specifies that Dem65 is a factor with four indicators. The path coefficients (loadings) are also specified explicitly. The third multiple-path syntax specifies that Indust is a factor of three observed indicators, with a fixed one for the effect of Indust on Gnppc60. The path coefficients for the paths Indust--->Enpc60 and Indust--->Indlf60 are unnamed free parameters (with the empty specifications). The fourth multiple-path syntax specifies that Indust is a predictor of both Dem60 and Dem65. The corresponding path coefficients are (unnamed) free parameters in the model.

The last path in the PATH statement specifies Dem60 as a predictor of Dem65. Notice that no PVAR statement is used because fixing the Dem60 and Dem65 variances to one is not used in the current model. The scales of the latent factors are identified by fixing some path coefficients to 1.



The fit of the structural model is acceptable, if not exceptionally good.

The model fit chi-square is not significant, supporting the hypothesized model. The SRMSR is close to 0.05. The AGFI is 0.86, which shows a reasonable fit. The RMSEA indicates a very good model fit, as the value (.0242) is much lower than 0.05. The CFI is almost 1, which shows a perfect model fit.

Political Democracy and Industrialization: Estimates of Path Coefficients PATH List Standard -----Path-----Parameter Estimate Error t Value Dem60 ---> 1.00000 ---> lam2 0.14020 8.49336 Dem60 Freop60 1.19079 9.68988 ---> Fair60 lam3 1.17454 0.12121 Dem60 Dem60 Legis60 lam4 1.25099 0.11757 10.64006 Dem65 ---> Press65 1.00000 Dem65 Freop65 lam2 1.19079 0.14020 8.49336 ---> Dem65 Fair65 lam3 1.17454 0.12121 9.68988 ---> 10.64006 Dem65 Legis65 lam4 1.25099 0.11757 1.00000 Indust ---> Gnppc60 Indust Enpc60 _Parm01 2.17966 0.13932 15.64530 ---> Indlf60 _Parm02 1.81821 0.15290 11.89126 Indust _Parm03 1.47133 Indust ---> Dem60 0.39496 3.72529 Indust Dem65 $_{\tt Parm04}$ 0.60046 0.22722 2.64267 ---> 11.47648 Dem60 Dem65 _Parm05 0.86504 0.07538 Sas Book

All path coefficients are significant---a pretty good sign.

Variance Parameters					
Variance				Standard	
Type	Variable	Parameter	Estimate	Error	t Value
Exogenous	Indust	_Add01	0.45466	0.08846	5.13991
Error	Press60	Add02	1.87973	0.44229	4.25001
	Freop60	_Add03	7.68378	1.39404	5.51189
	Legis60	_Add04	3.26801	0.73807	4.42779
	Press65	_Add05	2.34432	0.48851	4.79895
	Freop65	_Add06	5.03534	0.93993	5.35716
	Legis65	_Add07	3.35236	0.71788	4.66983
	Gnppc60	_Add08	0.08249	0.01986	4.15376
	Enpc60	_Add09	0.12206	0.07105	1.71776
	Indlf60	_Add10	0.47297	0.09197	5.14268
	Fair60	_Add11	5.02270	0.97587	5.14691
	Fair65	_Add12	3.60813	0.72394	4.98402
	Dem60	_Add13	3.92767	0.88311	4.44753
	Dem65	_Add14	0.16668	0.23158	0.71975

Some error variances are not significant: Enpc60 and Dem65. Enpc60 is an indicator of the Industrialization in 1960. This insignificant error variance means that the Indust factor predict Enpc60 perfectly. However, the corresponding t-value is 1.71, which could be judged as marginally significant.

The error variance for Dem65 is also not significant, as evident by the non-significant t-value of 0.72. This means that given Indust and Dem60, Dem65 can be predicted almost perfectly.

Political Democracy and Industrialization: Estimates of Covariances Covariances Among Errors Standard Error Error ο£ οf Parameter Estimate Error t Value Legis60 1.45956 Freop60 _Parm06 0.70251 2.07764 _Parm07 0.58859 1.39032 Freop65 Legis65 2.36212 _Parm08 Press60 Press65 0.59042 0.36307 1.62619 2.21252 0.75242 2.94054 Freop60 Freop65 _Parm09 _Parm10 Fair60 Fair65 0.72123 0.62333 1.15706 _Parm11 Legis60 Legis65 0.36769 0.45324 0.81125 Sas Power

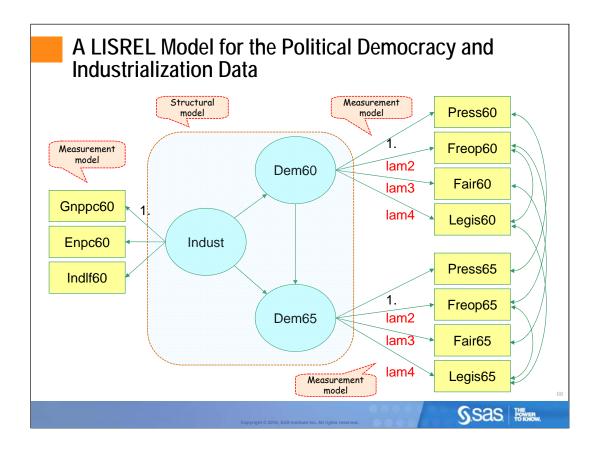
Again, there are some insignificant error covariances. This result challenges their presence in the model.

Political Democracy and Industrialization: Squared **Multiple Correlations** Squared Multiple Correlations Total Error Variable Variance Variance R-Square 0.12206 2.28211 0.9465 Enpc60 Fair60 5.02270 11.79895 0.5743 Fair65 3.60813 10.09361 0.6425 Freop60 7.68378 14.64875 0.4755 Freop65 5.03534 11.70144 0.5697 Gnppc60 0.08249 0.53715 0.8464 Indlf60 0.47297 1.97602 0.7606 3.26801 Legis60 10.95502 0.7017 Legis65 3.35236 10.70953 0.6870 Press60 6.79166 0.7232 1.87973 Press65 2.34432 7.04548 0.6673 Dem60 3.92767 4.91193 0.2004 4.70116 Dem65 0.16668 0.9645 Sas Book

The square multiple correlations are usually used to measure the percentage of overlapping variance between the predictors and the outcome variables. In the current example, R-squares range from 0.2 to extreme high values such as 0.95 and 0.96.

The smallest R-square is the one for predicting Dem60, which is 0.2. This actually is not that small an R-square value for social science data.

But the R-square (0.96) for Dem65 is extremely high. This means that Dem65 is almost perfectly predicted from democracy and industrialization in 1960.



This full SEM model is also a good illustration of the LISREL model.

The path diagram for the preceding model remains unchanged here. In order to call this path diagram a LISREL model, you have to identify the LISREL components in this path diagram. The two main components in LISREL are the measurement models and the structural model.

First, the measurement models are identified. A measurement model is about how observed variables are related to the latent variables or constructs in the model. Specifically, the measurement model involving industrialization is the measurement model of x because Indust serves as an exogenous (independent) variable in the path diagram. The measurement model involving Dem60 and Dem65 is the measurement model of y because Dem60 and Dem65 are endogenous (dependent) variables in the path diagram.

Second, the structural model is identified and highlighted in the center of the path diagram. The structural model describes the functional relationships among the latent variables (constructs) in the path diagram.

Therefore, all the essential component of the LISREL model is identified in the current path diagram.

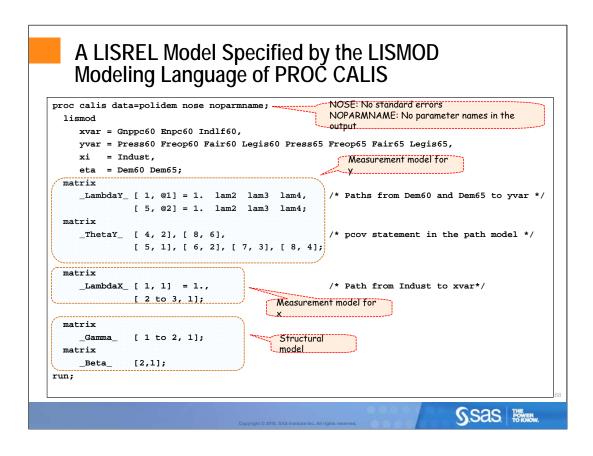
path	Measurement model: Relationships between latent and observed indicators			
Dem60> Press60 Freop60 Fair6 Dem65> Press65 Freop65 Fair6	55 Legis65 = 1. lam2 lam3 lam4,			
Indust> Gnppc60 Enpc60 Indlf6 Indust> Dem60 Dem65, Dem60> Dem65;	50 = 1., Structural model: Relationships among latent constructs			
pcov Freop60 Legis60, Freop65 Legis65, Press60 Press65, Freop60 Freop65, Fair60 Fair65, Legis60 Legis65;	,			
fitindex on(only) = [chisq df probo bentlercfi agfi] noindexty				

In the PATH modeling language, you can also identify the code for the measurement models and the structural model. The preceding code is recited here for illustrations.

In the PATH statement, the first three multiple-path specifications are concerned with the measurement of the latent constructs. In addition, all specifications in the PCOV statement are for the covariances of the measurement errors.

The last two specifications in the PATH statement are for the structural model. They describe the functional relationships between Indust, Dem60, and Dem65.

After identifying the LISREL components in the path diagram and in the SAS code, you now have a clue to specify the LISREL model in PROC CALIS. Essentially, it should be clear that the same path diagram is being used by the PATH modeling language and the LISREL model. The only task is to transcribe the code in the PATH modeling language to the language for the LISREL model.



PROC CALIS supports the so-called LISMOD modeling language. In order to fully understand the PROC CALIS code for the LISREL model, knowledge about matrix algebra is needed. But I will only describe the code in a conceptual way.

In the LISMOD statement, you first classify your variables into one of the four categories:

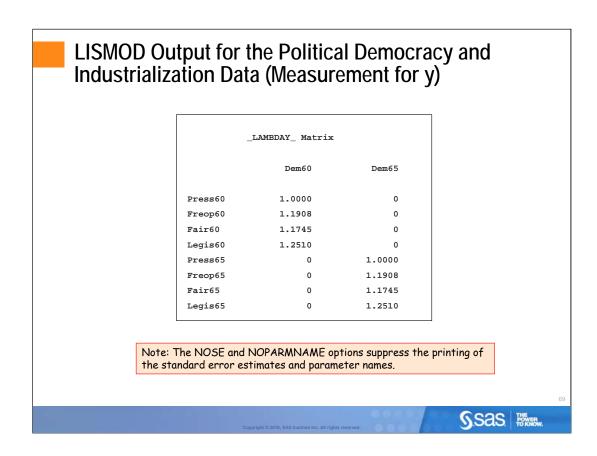
- 1.x-variables: observed indicators for the exogenous (independent) latent factors in the model.
- 2.y-variables: observed indicators for the endogenous (dependent) latent factors in the model.
- 3.xi-variables: exogenous (independent) latent factors in the model.
- 4.eta-variables: endogenous (dependent) latent factors in the model.

The LISREL model or LISREL program had been developed as a matrix-based language. Parameters in the models are specified as matrix elements in some specific model matrices with Greek names. PROC CALIS supports the matrix input of these LISREL model matrices. For example, in the measurement model for y, _LambdaY_ is the matrix that relates the y-variables to the eta-variables. Instead of specifying the paths as in the PATH statement, the MATRIX statement for _LambdaY_ serves the same purpose in the LISMOD modeling language. The MATRIX statement for _ThetaY_ specifies the error variances and covariances of the y-variables, much like the specifications of the PCOV statement in the PATH modeling language. In other words, the PATH model specifications are transcribed into the LISMOD model specifications for the y-variables.

Similarly, the MATRIX statement for _LAMBDAX_ specifies the parameters in the measurement model for the x-variables.

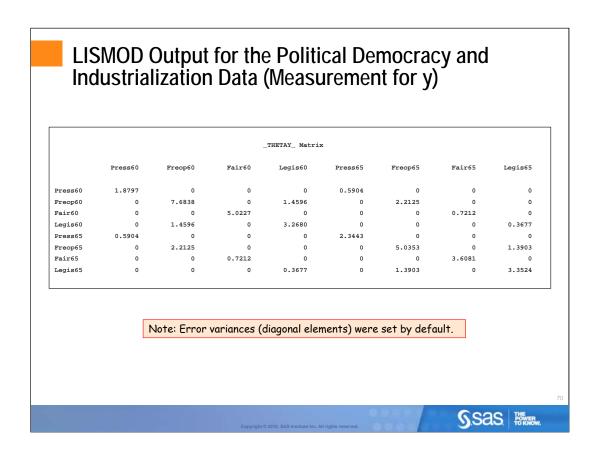
Finally, the structural relationships or the path relationships among the latent factors are specified in the MATRIX statements for the _GAMMA_ and _BETA_ matrices.

To simplify the output, I used two options in PROC CALIS statement. The NOSE option suppresses the printing of standard errors and the NOPARMNAME option suppresses the printing of the parameter names.

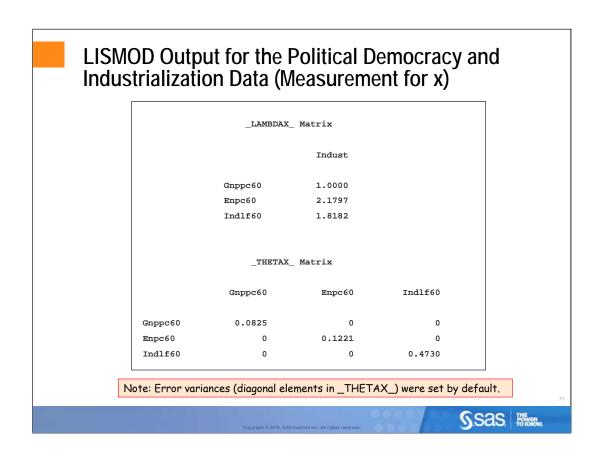


The following few slides show the output from PROC CALIS for the LISREL model. All the results are matrix-oriented. Details for these results have been discussed for the PATH model output and will not be repeated here. In general, you can find correspondence between the LISMOD and the PATH results.

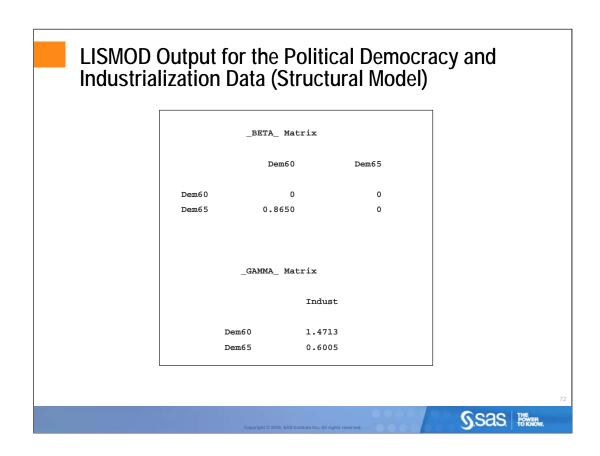
This slide shows the measurement model for the y-variables.



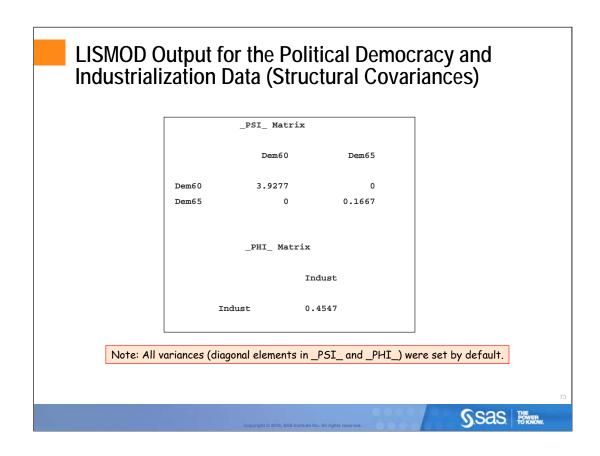
This slide shows the measurement error variances and covariances for the y-variables.



This slide shows the results of the measurement model for the x-variables, including the path coefficients and the error variances.



This slide shows the functional relationships between latent constructs.



This slide shows the error variances of the eta-variable and the variance of the xivariable.

Features of the LISMOD Modeling Language

- Supports the JKW (LISREL) models (not the LISREL program)
- Supports mean structure analysis
- Users input:
 - The ordered lists of x, y, ξ , and η variables
 - MATRIX statements to define free and fixed parameters
 - Names for parameters (not required for free parameters)
- Default covariance structure parameters of the LISMOD language:
 - Diagonal elements of all covariance matrices (all variances)
 - Lower triangular elements of the _PHI_ matrix (covariances of the ξ variables)

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In sum, the LISMOD modeling language in PROC CALIS supports the LISREL model by providing syntax to specify the essential components of the LISREL model. However, LISMOD itself does not interpret a LISREL program.

The LISMOD modeling language in PROC CALIS also supports the mean structure analysis. This is done by providing additional MATRIX statement input for the mean model matrices in the LISREL model.

If you understand the LISREL model, here are three things you input by using the LISMOD language:

- 1. The ordered lists of x, y, ξ , and η variables
- 2.MATRIX statements to define free and fixed parameters
- 3. Names for parameters (not required for free parameters)

(Note: This slide was updated after the printing of the handout)

The Default covariance structure parameters in the LISMOD language are:

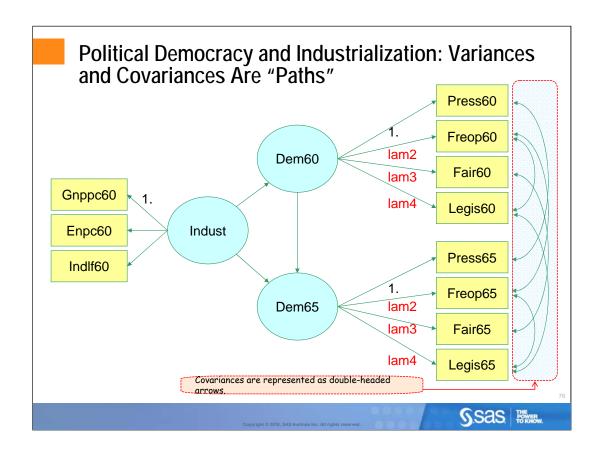
- 1. Diagonal elements of all covariance matrices (all variances)
- 2.Lower triangular elements of the PHI matrix (covariances of the ξ- variables)

Specifying the default parameters explicitly is certainly allowed, especially when you need to set constraints on these parameters.

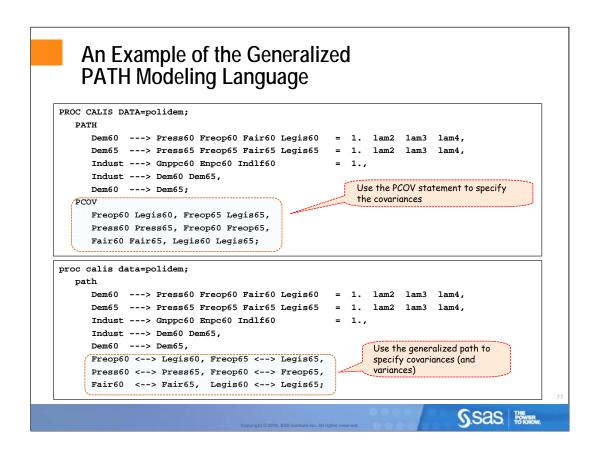
In addition, when the mean structures are modeled, the intercepts of the x- and y- variables are default free parameters, while the intercepts of the η - variables and the means of the ξ - variables are fixed zeros by default.

The Generalized PATH Modeling Language

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To generalize the PATH modeling language, error covariances in the path diagram could also be specified as "paths" in PROC CALIS. In fact, covariances in the path diagram are already represented as double-headed arrows, as shown in the political democracy and industrialization example.



The top panel shows the use of PCOV statement to specify the covariances. The bottom panel shows that these covariances are specified as double-headed paths, which resemble their representations in the path diagram.

The two PROC CALIS specifications shown above are equivalent.

Political Democracy and Industrialization: Output with **Generalized Paths** PATH List Standard -----Path-----Estimate t Value Parameter Error 1.00000 Dem60 ---> Press60 0.14020 lam2 1.19079 8.49336 Dem60 ---> Freop60 Dem60 ---> Fair60 lam3 1.17454 0.12121 9.68988 Dem60 ---> Legis60 lam4 1.25099 0.11757 10.64006 Dem65 Press65 1.00000 Freop65 lam2 1.19079 0.14020 8.49336 Dem65 lam3 1.17454 0.12121 9.68988 Dem65 Legis65 lam4 1.25099 10.64006 Indust Gnppc60 1.00000 ---> ---> _Parm01 2.17966 0.13932 15.64530 Indust Enpc60 _Parm02 Indlf60 1.81821 0.15290 Indust ---> 11.89126 ---> _Parm03 1.47133 0.39496 3.72529 Indust Dem60 _Parm04 Indust ---> Dem65 0.60046 0.22722 2.64267 _Parm05 11.47648 Dem60 ---> Dem65 0.86504 0.07538 _Parm06 Legis60 Freop60 <--> 1.45956 0.70251 2.07764 Freop65 <--> Legis65 _Parm07 1.39032 0.58859 2.36212 _Parm08 0.59042 0.36307 1.62619 2.21252 0.75242 2.94054 Freop60 Freop65 _Parm09 Fair60 Fair65 _Parm10 0.72123 0.62333 1.15706 0.36769 0.45324 Legis60 Legis65 Parm11 0.81125 Sas 聯編

The results obtained from PROC CALIS now shows the covariance estimates as "paths" in the PATH list. This table could be used directly in research paper for reporting the SEM estimation results.



Features of the Generalized PATH Modeling Language

- Extension of the PATH modeling language
- Represents all generalized paths in the PATH statement
- Variance-path: Y <--> Y
- Covariance-path: X <--> Y
- Mean or intercept (one-path): 1 ---> Y

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In sum, the generalized path modeling language enables you to specify all types of arrows in the path diagram as "paths," including the variance, covariance, intercept, and mean parameters.

Variance of Y is a path like Y <--> Y.

Covariance between X and Y is a path like X <--> Y

Mean or intercept for Y is one-path like 1--->Y.

Default Free and Fixed Parameters in PROC CALIS

- Default free parameters
 - Variances of and covariances among all exogenous (independent) variables (observed or latent, except for error terms)
 - o Error variances of all endogenous (dependent) variables
 - o Means or intercepts of all **observed** variables
- Default fixed zeros
 - o Unspecified paths and error covariances
 - o Means or intercepts of all latent variables

The main purpose of setting default parameters is to enable you to specify only the functional relationships among variables in most practical applications.

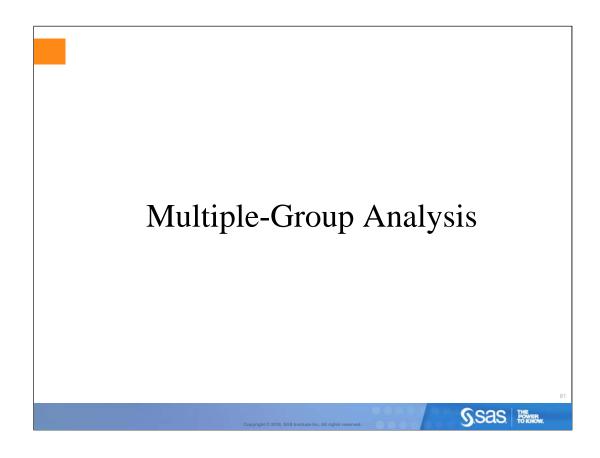
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Knowing the default free and fixed parameters in PROC CALIS are useful because it enhances the coding efficiency and accuracy. Here is a list of default free parameters and fixed zeros used in PROC CALIS:

(This slide has been changed slightly after the printing of the handout)

- Default free parameters
 - o Variances of and covariances among all **exogenous** (independent) variables (observed or latent, except for error terms)
 - o Error variances of all endogenous (dependent) variables
 - Means or intercepts of all observed variables
- Default fixed zeros
 - Unspecified paths and error covariances
 - o Means or intercepts of all latent variables

At the first glance, it might seem to be tedious and demanding that modelers must remember all these default parameter rules to specify an SEM accurately. However, the default parameterization used in PROC CALIS matches that of regression analysis and it is designed with the following main purpose in mind: In most practical applications, you would only need to specify the functional relationships among variables (that is, the single-headed paths in the path diagram) and the fixed variances of the latent variables.



Multiple-group analysis represents an important class of SEM applications.

PROC CALIS Syntax for Specifying a Multiple-Group Analysis proc calis; group 1 / data=ds1; /* ds1: data set for Group 1 */ group 2 / data=ds2; /* ds2: data set for Group 2 */ model 1 / group=1; /* Group 1 is fitted by Model 1 */ /* Insert the Model Specification for Group 1 */ model 2 / group=2; /* Group 2 is fitted by Model 2 */ /* Insert the Model Specification for Group 2 */ run;

The skeleton of the multiple-group syntax of PROC CALIS is shown in this slide.

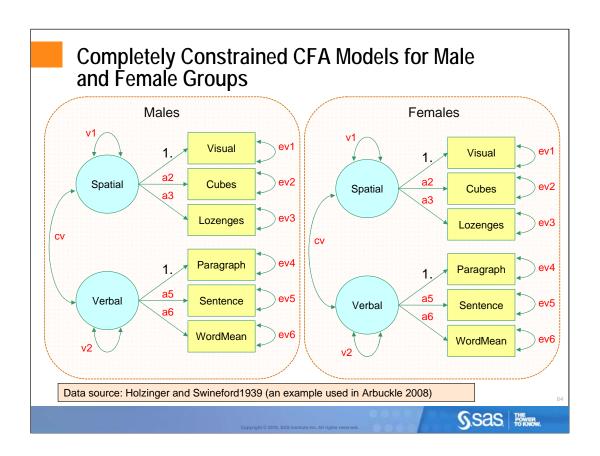
In this specification, you have two independent groups, which are stored in separate data sets 'ds1' and 'ds2.' You define two models: Model 1 and Model 2, respectively, for fitting to the two groups.

Under each MODEL statement, you specify the model by one of the modeling languages supported by PROC CALIS. For example, a PATH statement or a LISMOD statement.

```
Group-Model Mapping and Model Referencing
proc calis;
   group 1 / data=ds1;
   group 2 / data=ds2;
                                     Both Groups 1 and 2 are fitted by
   group 3 / data=ds3;
   model 1 / group = 1,2;
       path
           x1 ---> x2-x5,
           x2 ---> x3-x5,
           x3 ---> x5
                              = effect1;
                                             Model 2 makes reference to Model 1,
   model 2 / group = 3;
                                              but with a unique parameter for the
                                             path from \times 3 to \times 5. All other paths
       refmodel 1;
                                              are constrained between the two
       path
                                             models.
           x3 ---> x5
                               = effect2;
run:
    Note: REFMODEL does not constrain default free parameters in the two models.
    It constrains only those parameters that are specified explicitly.
                                                                Sas E
```

This example shows three groups of data. Model 1 is fitted to Groups 1 and 2 by the PATH model specified immediately after. Model 2 is fitted to Group 3. To define Model 2, a REFMODEL statement is used. REFMODEL 1 means that the specifications in Model 1 is referenced here. This means that all **explicit** specifications in Model 1 are copied into the current model. For example, all the PATH statement specifications in Model 1 are copied into Model 2. However, REFMODEL allows modifications from the reference model. In this example, the x3 --->x5 path is re-specified with a new path coefficient called 'effect2.' This 'effect2' in Model 2 is a different parameter than 'effect1' in Model 1, even though both model have this x3--->x5 path. Except for this x3--->x5 path, Models 1 and 2 share all the remaining specified paths with the same set of path coefficients.

Notice that by using the REMODEL statement to connect models, all (and only) the **explicit** specifications in the models are constrained (unless being modified or respecified). The constraints, however, will not apply to default parameters (assuming that they are not explicitly specified). To constrain the default parameters, they will have to be specified explicitly in the MODEL definitions.



Let us use an example to illustrate the multiple-group analysis. The Holzinger and Swineford data are sued. This data set is also used in Arbuckle's AMOS manual.

In this research, visual and verbal test scores were observed. Visual, Cubes, and Lozenges are spatial tests. Paragraph, Sentence, and WordMean are verbal tests. CFA models were hypothesized for the two groups: one group is for males and the other for females. The basic factor structures for the groups are the same. Two latent factors 'Spatial' and 'Verbal' are assumed for the measured variables. All parameters (including those default parameters in PROC CALIS) in the two models for the groups are labeled in red.

This is a completely constrained multiple-group model because the two path diagrams for males and females are exactly the same (that is, both have the same path structures and the same set of parameters).



Different Methods to Specify the Completely **Constrained Models**

- 1. Male and female groups fit by two models, but with all parameters (including all default parameters) being constrained in the models
- 2. Male and female groups fit by a single model definition
- 3. Male and female groups fit by two models that are constrained through the REFMODEL specification

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In PROC CALIS, you can use one of the following three ways to specify the preceding completely constrained model:

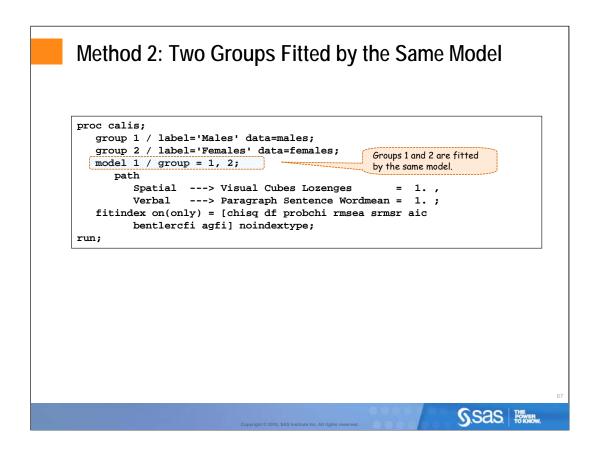
- 1. Male and female groups fitted by two models, but with all parameters (including all default parameters) being constrained in the models
- 2. Male and female groups fitted by a single model definition
- 3. Male and female groups fitted by two models that are constrained through the **REFMODEL** specification

I will describe each of these methods.

Method 1: Two Groups Fitted by the Two Completely **Constrained Models** Models are group 1 / label='Males' data=males: constrained through group 2 / label='Females' data=females; the use of the same model 1 / group = 1; parameter names. path Spatial ---> Visual Cubes Lozenges = 1. a2 a3, Verbal ---> Paragraph Sentence Wordmean = 1. a5 a6; Visual Cubes Lozenges Paragraph Sentence Wordmean = ev1-ev6, Spatial = v1, Verbal = v2; pcov Spatial Verbal = cv; model 2 / group = 2; path Spatial ---> Visual Cubes Lozenges Verbal ---> Paragraph Sentence Wordmean = 1. a5 a6; pvar Visual Cubes Lozenges Paragraph Sentence Wordmean = ev1-ev6, Spatial = v1, Verbal = v2; Spatial Verbal = cv; fitindex on(only) = [chisq df probchi rmsea srmsr aic bentlercfi agfi] noindextype; run; Sas Books

The first method is to define two models for the two groups. The model specifications under the two MODEL statements must be exactly the same.

This method is intuitive, but a little clumsy because you need to specify all parameters with matching names in the models (although you can cut-and-paste the model specifications to ensure an exact copy). You also need to specify each parameter in the model, including the default parameters, which you might sometimes miss.



The second method is very simple and intuitive. You specify one model and fit this model to the two gender groups. This ensures the groups are fitted exactly by the same model.

The advantage of this method is that it is simple, intuitive, and no parameter names are necessary for constraining models. Also, you do not need to specify any of the default parameters explicitly for setting up constraints.

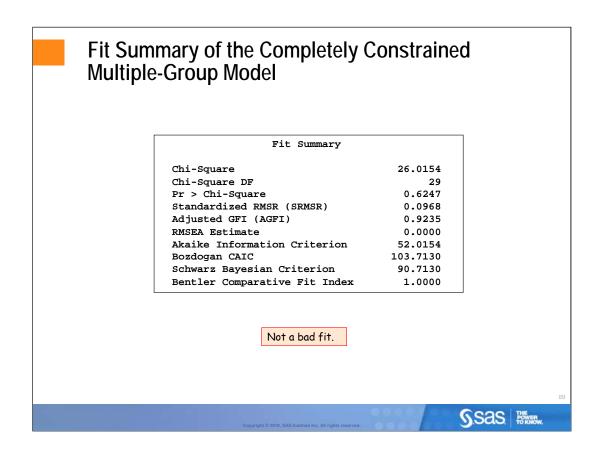
This is an ideal specification method if this model is all what you want to fit. However, if you are going to fit a sequence of multiple-group models to the groups, you might want to consider the next method.

Method 3: Two Groups Fitted by the Two Models That Are Constrained Through the REFMODEL proc calis; group 1 / label='Males' data=males; group 2 / label='Females' data=females; model 1 / group = 1; Spatial ---> Visual Cubes Lozenges Verbal ---> Paragraph Sentence Wordmean = 1.; Visual Cubes Lozenges Paragraph Sentence Wordmean Spatial Verbal; Spatial Verbal; The REFMODEL statement makes reference model 2 / group = 2; to all explicit specifications in Model 1. refmodel 1; fitindex on(only) = [chisq df probchi rmsea srmsr aic bentlercfi agfi] noindextype; run; Note: This method is used for the completely constrained model and the subsequent models with parameter constraints. **Sas** 機概

The third method constrains the models by the REFMODEL statement. As discussed previously, the REFMODEL copies all the **explicit** specifications from the reference model to the target model. In this slide, all path coefficients, variance parameters, and covariance parameters are specified in Model 1, which is fitted to Group 1 (Males). Model 2, which is fitted to Group 2 (Females), makes reference to Model 1 without any modifications or re-specifications.

Notice that in order to completely constrain the two models for the two groups, all parameters, including those could have been set by default by PROC CALIS (e.g., specifications in the PVAR statement and PCOV statement), must be specified **explicitly** in Model 1. This way, Model 2 will copy all these parameter specifications via the REFMODEL statement specification.

Unlike Method 1, this method does not require the use of parameter names for constraints across models. Constraints are done via the REFMODEL statement. Although not as intuitive as Method 2, this method would be useful if you need to consider fitting a sequence of multiple-group models, which will be illustrated later.



The completely constrained model provide a good fit of the data. The model fit chi-square is not significant. The RMSEA is perfect, although the SRMSR is not very good. The AGFI and the CFI are also good. The AIC, the CAIC, and the SBC are also printed. These indices cannot be interpreted by their absolute values, but will be useful when you compare the fits of different multiple-group models. You will use these indices to select the "best" multiple-group model for the data later.



Fitting Less Restrictive Multiple-Group Models

- Completely constrained multiple-group model: Error variances, structural covariances, and loadings are all constrained
- Release the constraints on error variances
- Release the constraints on structural covariances
- Release the constraints on the loadings Completely unconstrained

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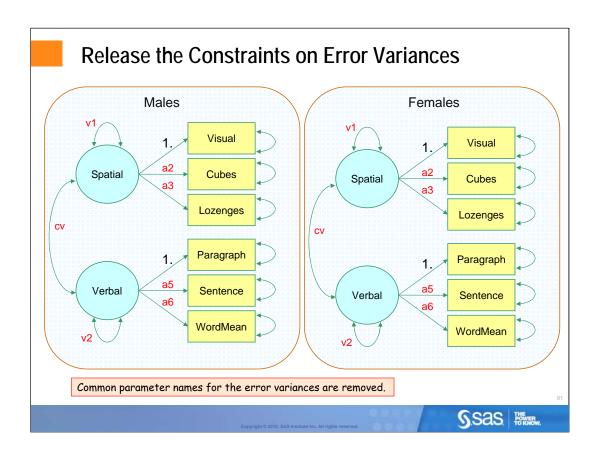
We have fitted the completely constrained multiple-group model by the REFMODEL method. We can further fit less constrained multiple-group model by modifying our PROC CALIS code.

We can release the constraints on error variances.

Then we can release the constraints on the structural covariances (among latent variables).

Finally, we can release the constraints on the path coefficients (or loadings).

I am going to show these step by step.



The path diagrams for the multiple-group model that releases the constraints on the error variances are shown above.

Except for the error variance parameters, all the remaining parameters are labeled. This means that only the error variance parameters are not invariant across the models for the groups.

Releasing the Constraints on the Error Variances proc calis; group 1 / label='Males' data=males; group 2 / label='Females' data=females; model 1 / group = 1; path Spatial ---> Visual Cubes Lozenges Verbal ---> Paragraph Sentence Wordmean = 1.; /* Visual Cubes Lozenges Paragraph Sentence Wordmean */ Spatial Verbal; pcov Spatial Verbal; model 2 / group = 2;refmodel 1; fitindex on(only) = [chisq df probchi rmsea srmsr aic bentlercfi agfi] noindextype; run; Comment out the error variance specifications in the PVAR statement, and let PROC CALIS set two distinct sets of default error variances for the two models. Sas Man

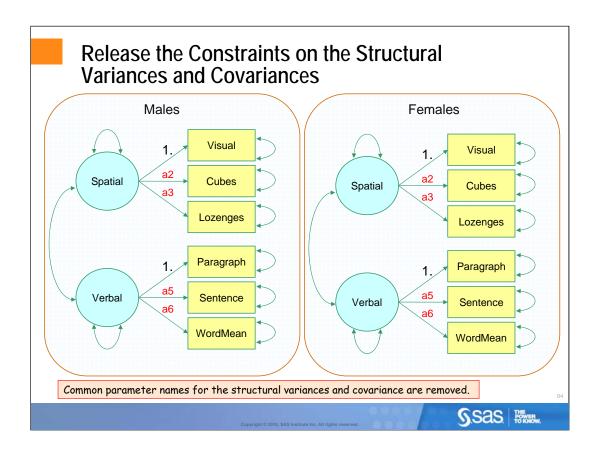
In terms of PROC CALIS specification, this means that the model for females makes reference to the model for males with regard to those constrained parameters only.

This could be done very easily from modifying the completely constrained multiple-group model. All you need to do is to comment out the PVAR statement specifications for the observed variables.

When Model 2 makes reference to Model 1, only those explicit specifications would be constrained between the two models. Because the error variances are not specified in both models (that is, commented out from the previous code), PROC CALIS would generate different sets of default error variance parameters for the two models. In other words, the error variance constraints are released in this PROC CALIS specification.

Fit Summary of the Multiple-Group Model with Constraints on Loadings and Structural Covariances Fit Summary Chi-Square 22.0334 Chi-Square DF 23 Pr > Chi-Square 0.5182 Standardized RMSR (SRMSR) 0.0903 Adjusted GFI (AGFI) 0.9163 RMSEA Estimate 0.0000 60.000 135.5913 Akaike Information Criterion Bozdogan CAIC Bozdogan CAIC 135.5913 Schwarz Bayesian Criterion 116.5913 Bentler Comparative Fit Index 1.0000 Sas. THE POWER TO KNOW.

The model fit chi-square still is not significant, indicating a good model fit. The RMSEA, the AGFI, and the CFI are all good. However, the SRMSR does not indicate a good model fit.



How about releasing the constraints on the structural covariances?

In the path diagram, only the path coefficients are constrained now (by using the same set of parameter names). This means that only the path effects are invariant across the models for the groups.

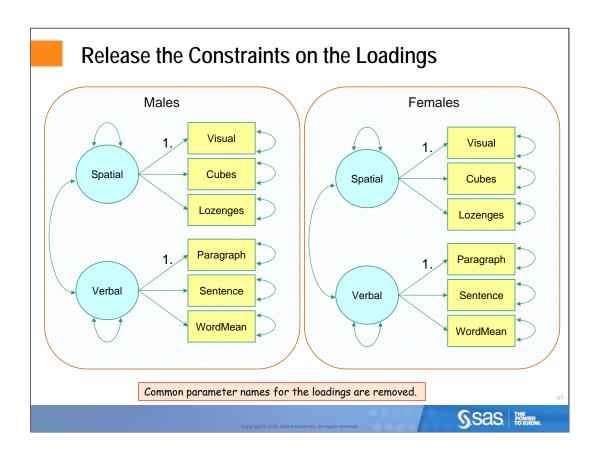
Releasing the Constraints on the Error Variances and Structural Covariances proc calis; group 1 / label='Males' data=males; group 2 / label='Females' data=females; model 1 / group = 1; Spatial ---> Visual Cubes Lozenges 1., Verbal ---> Paragraph Sentence Wordmean = 1.; pvar Visual Cubes Lozenges Paragraph Sentence Wordmean Spatial Verbal; pcov Spatial Verbal; model 2 / group = 2; refmodel 1; fitindex on(only) = [chisq df probchi rmsea srmsr aic bentlercfi agfi] noindextype; Comment out the PVAR and PCOV statements, and let the PROC CALIS set two distinct sets of default variances and covariances for the two models. Sas Books

This new multiple-group model can be specifying by commented out the explicit specifications of the structural covariances (variances and covariances among latent variables) in Model 1.

When Model 2 makes reference to Model 1, it copies the explicit specifications in the PATH statement of Model 1. Error variances, structural variances and covariances in the two models are now set by default and are unconstrained between the two models.

Fit Summary of the Multiple-Group Model with Loading Constraints Fit Summary 18.2915 Chi-Square Chi-Square DF Pr > Chi-Square 0.5682 Standardized RMSR (SRMSR) 0.0539 Adjusted GFI (AGFI) 0.9179 RMSEA Estimate 0.0000 Akaike Information Criterion 62.2915 Bozdogan CAIC 149.7796 Schwarz Bayesian Criterion 127.7796 Bentler Comparative Fit Index 1.0000 Sas Piller

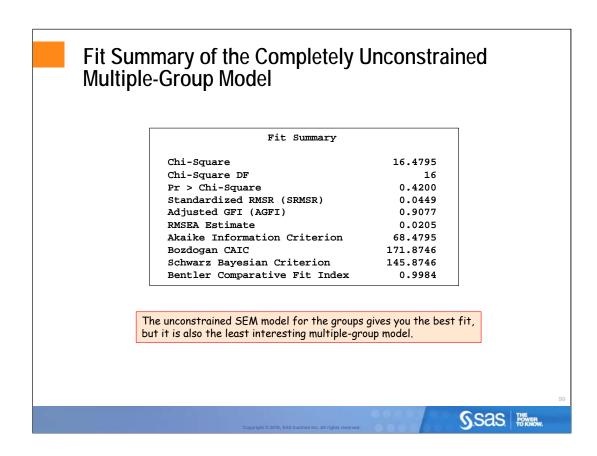
The model fit chi-square is not significant. Now, the SRMSR is acceptable. The AGFI, the RMSEA, and the CFI continue to be very good.



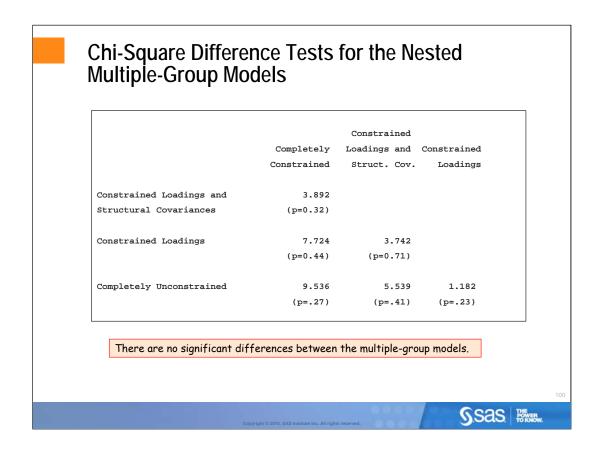
Finally, for the completely unconstrained multiple-group the path diagrams for the two groups are the same, but no parameter names (except for fixed values of 1) are used to denote constraints.

Completely Unconstrained Multiple-Group Model proc calis; group 1 / label='Males' data=males; group 2 / label='Females' data=females; model 1 / group = 1; path Spatial ---> Visual Cubes Lozenges = 1. , Verbal ---> Paragraph Sentence Wordmean = 1. ; model 2 / group = 2; path Spatial ---> Visual Cubes Lozenges = 1. , Verbal ---> Paragraph Sentence Wordmean = 1. ; fitindex on(only) = [chisq df probchi rmsea srmsr aic bentlercfi agfi] noindextype; run; The REFMODEL statement is not used here because the two models are not constrained with each other.

Because the two models for the groups are totally unrelated, you should not need to use the REFMODEL statement any more. Instead, the two models are defined exactly by the same PATH statement specifications. However, because no common parameter names are used for the path coefficients, the two models are not constrained.



All fit indices indicate very good fit of the completely unconstrained multiple-group model.



Which model is the best for the data?

Chi-square difference tests provide a statistical method to see if models are significantly different from each other. This slides shows the chi-square difference tests for comparing the four multiple-group models.

As all p-values are bigger than 0.05, it means all these multiple-group models are not significantly different from each other.

	Constrained			
	Completely Loadings and Constrained Comp			Completely
	Constrained	Struct. Cov.	Loadings	Unconstrained
Chi-Square	26.0154	22.0334	18.2915	16.4795
Chi-Square DF	29	23	20	16
Pr > Chi-Square	0.6247	0.5182	0.5682	0.4200
Standardized RMSR (SRMSR)	0.0968	0.0903	0.0539	0.0449
Adjusted GFI (AGFI)	0.9235	0.9163	0.9179	0.9077
RMSEA Estimate	0.0000	0.0000	0.0000	0.0205
Akaike Information Criterion	52.0154	60.0334	62.2915	68.4795
Bozdogan CAIC	103.7130	135.5913	149.7796	171.8746
Schwarz Bayesian Criterion	90.7130	116.5913	127.7796	145.8746
Bentler Comparative Fit Index	1.0000	1.0000	1.0000	0.9984
Absolute indices: Chi-square, SR Parsimonious indices: AGFI (larg RMSEA, A Incremental indices: Bentler CF	ger is better), IC, CAIC, SBC	(smaller is bette	r)	

We can also compare the four models by means of the fit index values.

The model fit chi-square value always favors the model with the largest number of parameters. So, according to the model fit chi-square, the completely unconstrained model is the best model. The SRMSR also favors the completely unconstrained model simply because it can be viewed as a monotone transformation of the chi-square value. However, you should not select your best model based on the absolute indices such as model-fit chi-square value or the SRMSR because these indices do not take model parsimony into account. Complicated models might have perfect model fit chi-square and SRMSR values (i.e., 0). But these complex models should not be selected as the best models because they have very little scientific value.

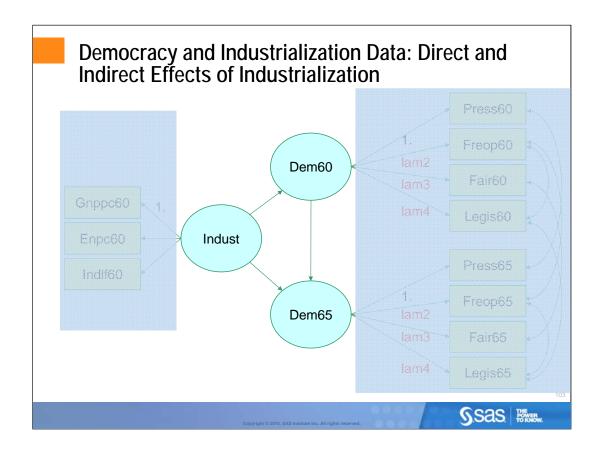
The AGFI, the RMSEA, the AIC, the CAIC, and the SBC all takes model parsimony into account. For the AGFI, the larger the better. For other indices, the smaller the better. All these parsimonious indices point to the completely constrained model as the best multiple-group model for the data.

Lastly, the incremental fit index Bentler CFI favors the completely constrained model too. However, virtually all multiple-group model in this comparison are equally good according to the CFI. Notice that incremental indices such as the CFI measures how a target model measures better than a so-called baseline model. They do not take model parsimony into account. In addition, they depend on how good the baseline model is used in the computing formula. If the baseline model is very bad (such as the commonly-used uncorrelatedness model), all competing models would have good incremental fit only because the baseline model is much worse. For this reason, incremental fit indices might not serve as good criteria for model selection.

Analyzing Direct and Indirect Effects

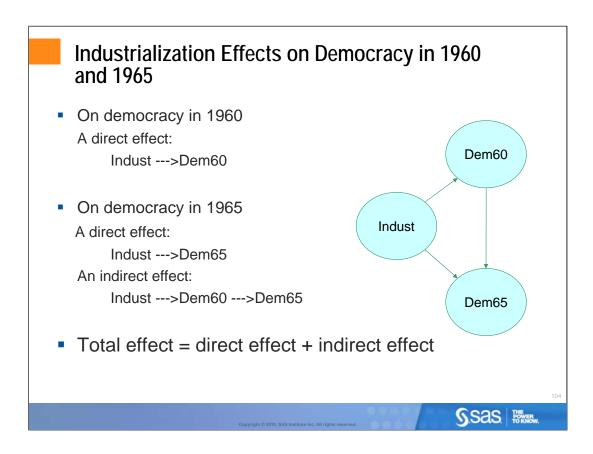
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Analyzing direct and indirect effects is something unique to SEM.

Let us look at the model for the democracy and industrialization data. Only the structural part of the SEM is shown to illustrate the idea.

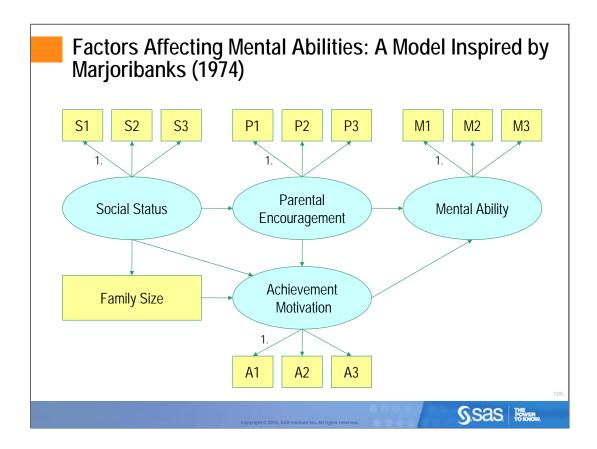


First, let us look at the effect of industrialization on the democracy measure in 1960. The direct effect of Indust on Dem60 refers to the path Indust ---> Dem60. This effect can be estimated directly from any SEM software.

On the democracy measure in 1965, industrialization has a direct and indirect effect. The direct effect refers to the path Indust ---> Dem65. The indirect effect is indicated by the track Indust ---> Dem60 ---> Dem65.

When you add up the direct and indirect effect, it gives you the total effect.

In SEM, the direct effects are estimated as the path coefficients. Indirect effects and total effects are functions of the parameter estimates. Fortunately, PROC CALIS can compute these functions efficiently and it can also provide standard error estimates for these effects.



This slide shows a more interesting example about analyzing direct, indirect, and total effects.

The example is inspired by a model of Marjoribanks (1974). The current model is a simplification and the data are generated. The results here do not represent the original study, but would serve well for illustration purposes.

The main idea of the study is to model the mental ability of students. The mental ability is a latent construct, which is supposed to be determined (predicted) by parental encouragement and achievement motivation, both of which are formulated as latent construct in the model. Two remote causes (predictors), social status and family size, have direct effects on parental encouragement and achievement motivation. However, these two remote causes affect the mental ability only indirectly. Social status is also formulated as a latent variable, while family size is an observed variable. For all the latent variables, observed indicators are used and they are represented by small rectangles in the path diagram.

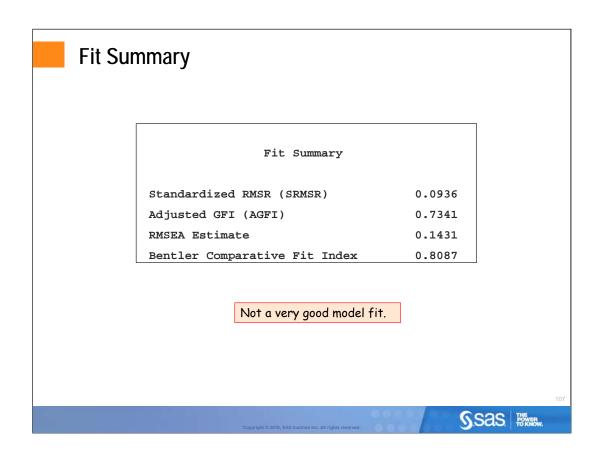
There are some motivating questions about this path diagram regarding the direct and indirect effects. For example,

- 1.Even though social status does not affect the mental ability, it does have an indirect effect on the mental ability via parental encouragement and achievement motivation. One would like the SEM software to compute this this indirect effect and its significance.
- 2.Parental encouragement has a direct and an indirect effects on the mental ability. What is the overall total effect of parental encouragement on the mental ability. One would also like the SEM software to compute all these effects and their significance.

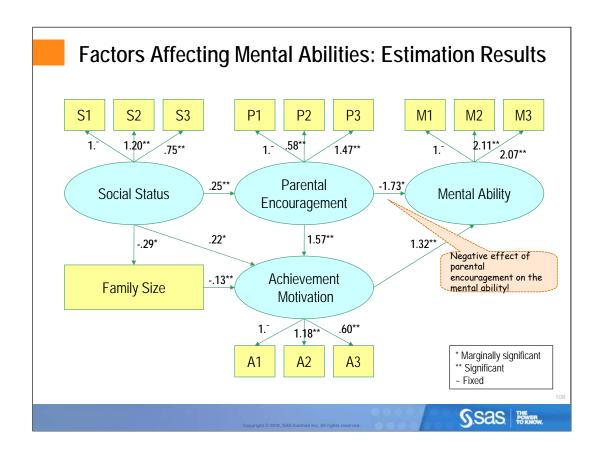
```
Factors Affecting Mental Abilities: PROC CALIS Code
proc calis data=mental nobs=115 effpart;
                                            The EFFPART option analyzes
  path
                                           the effect partitioning in the
                                           model.
     /* Structural Model */
     SocialStatus ---> ParentalEncouragement FamilySize
                       AchievementMotivation,
     FamilySize ---> AchievementMotivation,
     ParentalEncouragement ---> AchievementMotivation MentalAbility,
     AchievementMotivation ---> MentalAbility,
     /* Measurement Model */
     SocialStatus
                          ---> S1 S2 S3 = 1.,
     ParentalEncouragement ---> P1 P2 P3 = 1.,
     AchievementMotivation ---> A1 A2 A3 = 1.,
                           ---> M1 M2 M3
  fitindex on(only)=[agfi srmsr rmsea bentlercfi] noindextype;
run;
                                                               Sas Hiller
```

Now, the PATH specification for the target model should be easy for you. You can specify the measurement model and the structural model by the multiple-path syntax. You can look at the path diagram and write down the paths in the PATH statement. Notice that each path in the path diagram represents a direct effect of one variable on another variable.

The only new option introduced here is the EFFPART option in the PROC CALIS statement. EFFPART stands for effect partitioning. In other words, it partitions the total effects of any variable on any other variable into direct and indirect effects. PROC CALIS will compute these effects and the standardized version---all with standard error estimates provided.



The model fit actually does not look too good for this simulated data. But this is not the concern here. We want to study the effect partitioning, assuming that we are satisfied with the model fit.



Before diving into the results for the effect partitioning, I want to look at the estimates shown in the path diagram. I want to throw in one more motivation to study direct and indirect effects in a structural equation model.

In this path diagram, estimates are shown with their significance marked. Two asterisks after an estimate means the estimate is statistically significant. One asterisk after an estimate means that the estimate is marginally significant.

I want to focus on the effects of parental encouragement on mental ability. The direct effect is -1.73. This means that parental encouragement has a negative effect on mental ability. This sounds a little strange at the first glance. But if we look at the bigger picture in the path diagram, we can understand why that is so. Notice that parental encouragement has a positive effect on achievement motivation, which in turns has a positive effect on mental ability. The whole picture suggests that purely parental encouragement do not necessarily affect mental ability in a positive way. Sometimes, the more encouragement would only add more pressure to the individual's mental performance---hence the negative direct effect on mental ability observed in the path diagram result. However, when the parental encouragement can affect something more internal of the individuals---namely, the individual's achievement motivation, then it will result in a higher mental ability score. Hence, there is a positive indirect effect of parental encouragement on the mental ability.

In sum, an interesting question in this path diagram result is that what is the overall total effect of parental encouragement on mental ability, given that it has a negative direct effect and a positive indirect effect?

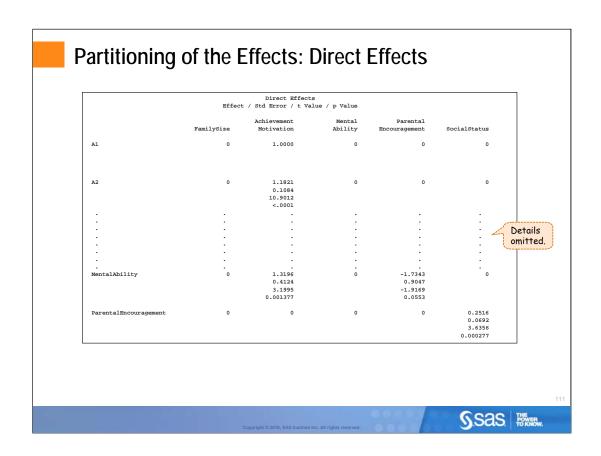
Partitioning of the Effects: A Prerequisite Stability Coefficient of Reciprocal Causation = 0 Stability Coefficient < 1 Total and Indirect Effects Converge NOTE: The stability coefficient is 0, which is less than one. The condition for converged total and indirect effects is satisfied.

Before you can analyze direct and indirect effects, you should check whether a prerequisite is satisfied. In order to study the effect partitioning legitimately, the so-called stability coefficient must be less then 1. PROC CALIS provides such a check. When you see these messages from the PROC CALIS output, you could proceed to examine your effect partitioning results.

	Effec	Total Effects t / Std Error / t Va	lue / p Value		
	FamilySize	Achievement Motivation	Mental Ability	Parental Encouragement	SocialStatus
A1	-0.1287	1.0000	0	1.5701	0.6523
AI.	0.0360	1.0000	· ·	0.5176	0.0942
	-3.5769			3.0337	6.9258
	0.000348			0.002416	<.0001
A2	-0.1522	1.1821	0	1.8560	0.7710
	0.0420	0.1084		0.6051	0.1036
	-3.6274	10.9012		3.0672	7.4398
	0.000286	<.0001		0.002161	<.0001
•		•	•		•
-	•	•	•	•	•
•	•	•	:	•	
:			:	:	2
-					
•					
•			•		
MentalAbility	-0.1699	1.3196	0	0.3376	0.4244
	0.0572 -2.9696	0.4124 3.1995		0.4045 0.8346	0.1280 3.3159
	0.002982	0.001377		0.4039	0.000914
	01002502	0.0025//		0.1033	01000311
ParentalEncouragement	0	0	0	0	0.2516
					0.0692
					3.6356
					0.000277

With the EFFPART option, PROC CALIS produces tables for total, direct, and indirect effects separately. These tables could be large. I just annotate these results here. Some results are not shown.

This table is about the estimates of the total effects, their standard errors, t-values, and significance levels.



This table is about the direct effects , their standard errors, t-values, and significance levels.

	Effec	Indirect Effect t / Std Error / t Va				
		Achievement	Mental	Parental		
	FamilySize	Motivation	Ability	Encouragement	SocialStatus	
Al	-0.1287	0	0	1.5701	0.6523	
	0.0360			0.5176	0.0942	
	-3.5769			3.0337	6.9258	
	0.000348			0.002416	<.0001	
A2	-0.1522	0	0	1.8560	0.7710	
	0.0420			0.6051	0.1036	
	-3.6274			3.0672	7.4398	
	0.000286			0.002161	<.0001	
•						
•					•	/
•		•	•		•	Deta
•	•	•	•	•	•	omit
:	•	:	•		:	
	:		•	:	•	
MentalAbility	-0.1699	0	0	2.0719	0.4244	
	0.0572			1.0483	0.1280	
	-2.9696			1.9763	3.3159	
	0.002982			0.0481	0.000914	
ParentalEncouragement	0	0	0	0	0	

This table is about the indirect effects , their standard errors, t-values, and significance levels.

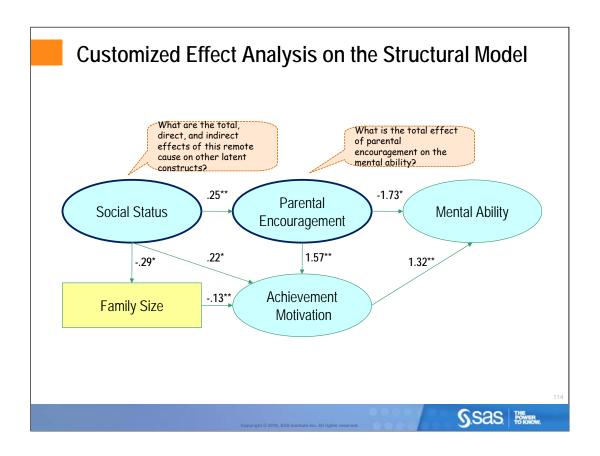
Customized Effect Analysis

- The EFFPART option displays all logical possible effects of the variables
- Columns: Five variables, each of which serves as a predictor at least once:
 - o FamilySize
 - AchivementMotivation
 - MentalAbility
 - o ParentalEncouragement
 - SocialStatus
- Rows: Sixteen variables, each of which serves as an outcome variable at least once (all variables except for SocialStatus)

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When you have large tables like those shown in previous slides, you are likely to be doing exploratory analysis without specific questions in your mind. The effect tables could get very large and you might have a difficult time to look for the particular results that you are interested in. For example, the columns of the effect tables consist of five variables, each of which serves as a predictor at least once in the path diagram. These five variables have direct or indirect effects on the row variables. The rows consist of sixteen variables, each of which serves as an outcome variable at least once. In the current path diagram, it includes all variables except for the SocialStatus variable.

However, if you have specific research questions in your mind, you are recommended to do customized effect analysis that is supported by PROC CALIS.



In the beginning, we already have these motivating questions.

1. For the social status variable, What are the total, direct, and indirect effects of this remote cause on other latent constructs, especially on the mental ability?

2. What is the total effect of parental encouragement on the mental ability?

```
Factors Affecting Mental Abilities: Customized
     Effect Analysis
proc calis data=mental nobs=115;
     /* Structural Model */
     SocialStatus --> ParentalEncouragement FamilySize AchievementMotivation,
     FamilySize ---> AchievementMotivation,
     ParentalEncouragement ---> AchievementMotivation MentalAbility,
     AchievementMotivation ---> MentalAbility,
     /* Measurement Model */
                                                       The EFFPART
     SocialStatus ---> S1 S2 S3 = 1.,
                                                       statement defines the
     ParentalEncouragement ---> P1 P2 P3 = 1.,
                                                        customized effects of
     AchievementMotivation ---> A1 A2 A3 = 1.,
     MentalAbility ---> M1 M2 M3 = 1.;
     SocialStatus
                       -> ParentalEncouragement AchievementMotivation
                          MentalAbility,
     ParentalEncouragement -> MentalAbility;
run;
                                                               Sas Books
```

PROC CALIS supports the customized effect analysis. This can be done by the EFFPART statement, as shown in the PROC CALIS code in this slide.

First, you want to study the effect partitioning of social status on these three variables: parental encouragement, achievement motivation, and mental ability. Hence, you use the following code in the EFFPART statement:

SocialStatus -> ParentalEncouragement AchievementMotivation MentalAbility,

Second, you want to study the effect partitioning of parental encouragement on mental ability. Hence, you use the following code in the EFFPART statement:

ParentalEncouragement -> MentalAbility;

	Effects of Socials	Status	
Effect /	Std Error / t Val	ue / p Value	
	Total	Direct	Indirect
ParentalEncouragement	0.2516	0.2516	0
Dinast affact	0.0692	0.0692	
Direct effect	3.6356	3.6356	
•	0.000277	0.000277	
AchievementMotivation	0.6523	0.2193	0.4330
Direct and indirect	0.0942	0.1147	0.1203
effects	6.9258	1.9125	3.5985
	<.0001	0.0558	0.000320
MentalAbility	0.4244	0	0.4244
Indirect effect	0.1280		0.1280
-only	3.3159		3.3159
	0.000914		0.000914

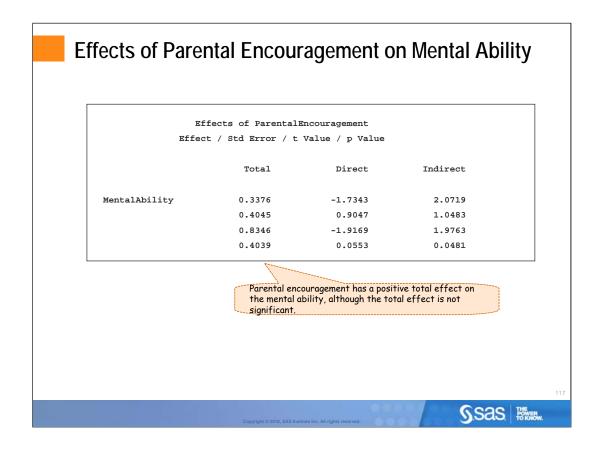
The effect partitioning results from PROC CALIS are shown in this slide and the next one.

The effects of social status on the three specific latent variables are shown in this table.

On the parental encouragement, social status has a direct effect only, which is positive and significant.

On the achievement motivation, social status has both a direct and an indirect effects. Both of these effects are significant. The total effect is the sum of the direct and indirect effect. The total effect is also significant.

On the mental ability, social status has only an indirect effect, which is also significant.



This slide shows the effect partitioning of parental encouragement on mental ability.

The direct effect is negative, as shown previously in the path diagram. This direct effect is marginally significant.

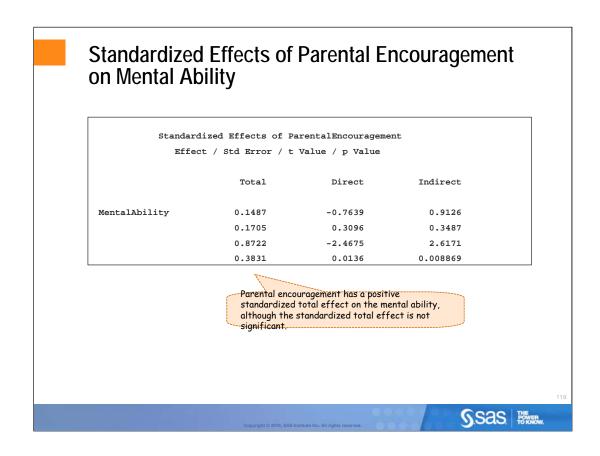
The indirect effect is positive and is statistical significant. This is a piece of "comforting" information---parental encouragement does affect the mental ability positively, but only through its effect on achievement motivation.

The total effect, which is the sum of direct and indirect effect, however, is not significant.

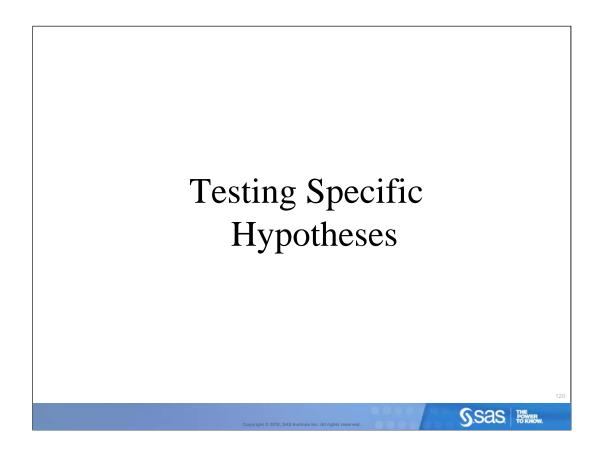
This example shows that SEM effect analysis can show some effect patterns that simply cannot be analyzed by linear regression analysis adequately. The SEM effect analysis provides something more detailed and refined regarding the totality of the theory. In this regard, the customized effect analysis supported by PROC CALIS is very useful.

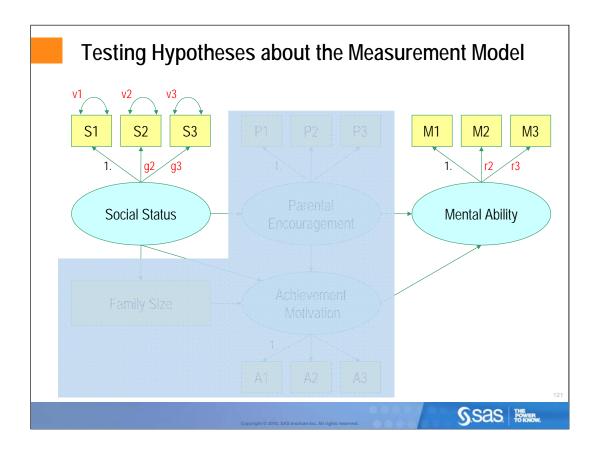
Standard	dized Effects of So	ocialStatus	
Effect /	Std Error / t Valu	ue / p Value	
	Total	Direct	Indirect
ParentalEncouragement	0.6675	0.6675	C
	0.0833	0.0833	
	8.0141	8.0141	
	<.0001	<.0001	
AchievementMotivation	0.6990	0.2350	0.4640
	0.0597	0.1207	0.1153
	11.7105	1.9478	4.0231
	<.0001	0.0514	<.0001
MentalAbility	0.4960	0	0.4960
	0.0850		0.0850
	5.8374		5.837
	<.0001		<.00

PROC CALIS also provides the standardized results for effect analysis. Standard errors, t-values, and p-values are also computed for the standardized effect estimates.



This slide shows the standardized effects of parental encouragement on mental ability. The pattern is quite similar to the unstandardized version.





Testing specific hypotheses is an interesting topic. Here we look at some examples.

In the mental ability model, you have some indicator variables for the latent variables. Two latent variables are selected to illustrate the testing of specific hypotheses.

For the mental ability factor, one might want to test the hypothesis that the loadings (path coefficients) are the same for the M2 and M3 indicators. In the path diagram, r2 and r3 are labeled as the path coefficients. You want to test whether r2 and r3 are equal within the model.

For the social status factor, you not only want to test the hypothesis that the loadings (path coefficients) are the same for the three indicators, but you also want to see if their corresponding error variances are the same in the population. In the path diagram, g2, g3, v1, v2, and v3 are parameters of interest. You want to test simultaneously whether g2, g3 are equal to 1 and v1, v2, and v3 are the same in the population.



Specific Hypotheses

Parallel items for measuring SocialStatus

H1: g2 = 1

H2: q3 = 1

H3: v1 = v2

H4: v2 = v3

Equality of loadings for MentalAbility items M2 and M3

H5: r2 = r3

 Sum of the loadings for M2 and M3 is two times as much as the sum of the loadings for S1 and S2

H6:
$$(r2 + r3) / (g2 + g3) = 2$$





The test of equal loadings and equal error variances for the social status items is a test of parallel items. This could be stated more formally as the following four component hypotheses H1, H2, H3, and H4, as shown in the slide. These four hypotheses need to be tested simultaneously. Rejection of the simultaneous test means the items are not parallel.

The test of equal loadings for the measurement indicators of the mental ability factor is simpler. It is stated in H5. Rejection of H5 means that r2 and r3 are not equal in the population.

Finally, you can invent any strange hypothesis that can be expressed as a continuous function of the model parameters. For example, H6 states that the ratio of the sum of r2 and r3 to the sum of g2 and g3 is 2. This hypothesis may or may not make sense. But it is included here to demonstrate the flexibility of PROC CALIS.



PROC CALIS Hypotheses Testing: $h(\theta) = 0$

Parallel items for measuring SocialStatus:

H1: h1 = g2 - 1 = 0

H2: h2 = g3 - 1 = 0

H3: h3 = v1 - v2 = 0

H4: h4 = v2 - v3 = 0

Equality of loadings for MentalAbility items M2 and M3

H5: h5 = r2 - r3 = 0

 Sum of the loadings for M2 and M3 is two times as much as the sum of the loadings for S1 and S2

H6: h6 = 2(g2 + g3) - (r2 + r3) = 0





Before I show you the PROC CALIS code, it is useful to reformulate the hypotheses into the forms that match the PROC CALIS input.

PROC CALIS tests hypotheses of the form $h(\theta)=0$, where $h(\theta)$ is any continuous function of the model parameters (for example, the error variances and the path coefficients in the model).

The hypotheses in the previous slide could all be rewritten in this required form, as shown in this slide. With these forms, you are ready to specify those hypotheses in PROC CALIS.

```
Testing Specific Hypotheses about the Measurement
   Model Using PROC CALIS
proc calis data=mental nobs=115;
  path
      SocialStatus ---> ParentalEncouragement FamilySize AchievementMotivation,
      FamilySize ---> AchievementMotivation,
      ParentalEncouragement ---> AchievementMotivation MentalAbility,
      AchievementMotivation ---> MentalAbility,
SocialStatus ---> S1 S2 S3 = 1. g2 g3,
                                                              Specify g2, g3, r2, r3, v1, v2, and v3 explicitly.
      ParentalEncouragement ---> P1 P2 P3 = 1.,
     AchievementMotivation ---> A1 A2 A3 = 1.,
MentalAbility ---> M1 M2 M3 = 1. r2 r3;
                                                                 Use the SIMTEST statement
  pvar S1-S3 = v1-v3;
                                                                 to test simultaneously
  simtest parallel_social_items=[h1 h2 h3 h4];
                                                                 hypotheses. Use the
  testfunc h5_equal_load_m2_m3 h6_proportional_sum;
                                                                 TESTFUNC statement to test
  h1 = q2 - 1;
                                                                 individual hypotheses.
  h2 = g3 - 1;
                                                                Use the SAS programming
  h3 = v1 - v2;
                                                                statements to define the
  h4 = v2 - v3;
                                                                parametric functions in the
  h5_equal_load_m2_m3 = r2 - r3;
                                                                 tests.
  h6\_proportional\_sum = 2*(g2 + g3) - (r2 + r3);
run;
                                                                           Sas 機概
```

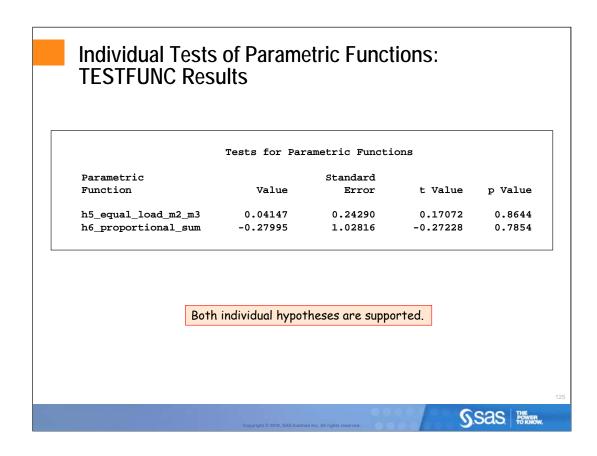
First, you have to label or name the parameters in the correct locations of the model specification. For example, g2 and g3 are the path coefficients for S2 and S3, respectively; and r2 and r3 are the path coefficients for M2 and M3, respectively. Notice that you did not name these parameters in the preceding model specifications. Naming these parameters were optional because you did not reference them. However, because you are going to refer to these parameters in the hypothesis testing, you must name or label them in the respective locations now. Similarly, the error variances for S1-S3 are named as v1-v3, as shown in the PVAR statement.

The main tools for testing specific hypothesis in PROC CALIS are the SIMTESTS and the TESTFUNC statements.

The SIMTEST statement enables you to test simultaneous hypotheses like the parallel hypothesis with four component hypotheses. Here we have h1, h2, h3, and h4, all of which are treated just as the names of the hypotheses that are defined later.

The TESTFUNC statement enables you to test individual hypotheses like the equality of loadings and the proportionality hypotheses described previously. Here I use long names such as h5_equal_load_m2_m3 and h6_proportional_sum to remind me of the nature of the target hypotheses.

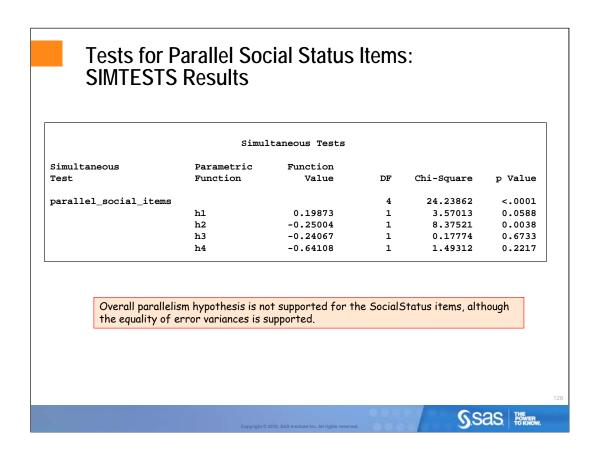
Now I use the so-called SAS programming statements to define the hypotheses: h1-h4, h5_equal_load_m2_m3, and h6_proportional_sum. The SAS programming statements are just like common mathematical equations. These six SAS programming statements define the parametric functions in the target hypotheses. PROC CALIS tests all parametric functions equaling zero.



The TESTFUNC specification produces the results shown in this table.

You fail to reject the equality of loadings for M2 and M3 because the p-value is bigger than 0.05. So, the equality of the loadings is supported.

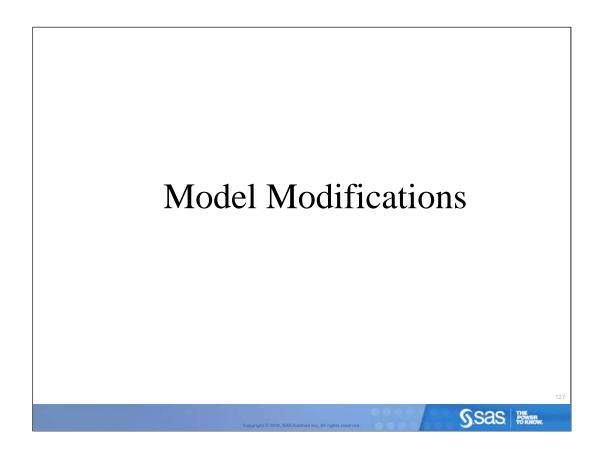
You also fail to reject the proportional sum hypothesis (p-value=0.79).



The SIMTESTS statement specification produces the output shown in this table.

For the parallel hypothesis, the simultaneous test is rejected (p <.0001). The parallel item hypothesis is not supported.

PROC CALIS also provides individual tests for the component hypotheses. This would be useful for doing an ad hoc analysis to probe what fails the simultaneous hypothesis. For example, both h1 and h2 are at least marginally significant. But h3 and h4 are not significant. Recall that h1 and h2 are about the equality of the loadings (path coefficients) while h3 and h4 are about the equality of error variances. The current results show that the items might have the same error variances but not the same loadings in the population.





Fit Summary	
Chi-Square	196.7455
Chi-Square DF	59
Pr > Chi-Square	<.0001
Standardized RMSR (SRMSR)	0.0936
Adjusted GFI (AGFI)	0.7341
RMSEA Estimate	0.1431
Bentler Comparative Fit Index	0.8087

- Large SRMSR and RMSEA
- Small AGFI and CFI
- Model modification: suggests ways to improve the model fit
- Lagrange multiplier (LM) tests: which parameters you can add to significantly decrease the model fit chi-square value

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The mental ability model did not fit well. The SRMSR and the RMSEA are large, while the AGFI and the CFI are small. When you encounter a bad model fit, it would jeopardize your interpretations of the model parameters, effect analysis, hypothesis testing, and etc.

Model modification is a statistical technique that suggests ways to improve your model fit. The most common model modification technique is done through the so-called Lagrange multiplier (LM) tests. Essentially, the LM tests suggest which parameters you could add to the model to significantly lower the model fit chi-square value. When the model fit chi-square is lowered, most other fit indices (but not all, especially those parsimonious indices that take model complexity into account) might also improve.

```
Using the MODIFICATION Option

proc calis data=mental nobs=115 modification;
path

SocialStatus ---> ParentalEncouragement FamilySize
AchievementMotivation,
FamilySize ---> AchievementMotivation,
ParentalEncouragement ---> AchievementMotivation MentalAbility,
AchievementMotivation ---> MentalAbility,
SocialStatus ---> S1 S2 S3 = 1.,
ParentalEncouragement ---> P1 P2 P3 = 1.,
AchievementMotivation ---> A1 A2 A3 = 1.,
MentalAbility ---> M1 M2 M3 = 1.;
run;
```

The option you can use to do model modification in PROC CALIS is the MODIFICATION option in the PROC CALIS statement. You can simply add this option to the PROC CALIS statement when you run your model. This example shows that the LM tests for model modification is requested for the original mental ability model, which does not have a very good model fit.

Rank Order of the 10 Largest LM Stat for Path Relations				
				Parm
То	From	LM Stat	Pr > ChiSq	Change
P2	P1	56.19414	<.0001	-0.73639
P1	P2	56.19349	<.0001	-0.72904
A2	M2	19.17647	<.0001	0.22842
A2	ParentalEncouragement	18.57947	<.0001	-2.31463
A2	MentalAbility	17.20340	<.0001	0.95581
ParentalEncouragement	A1	17.04464	<.0001	0.27042
A1	ParentalEncouragement	15.86099	<.0001	1.88904
FamilySize	A2	14.43548	0.0001	-1.14590
A1	MentalAbility	13.88705	0.0002	-0.75314
A2	Р3	12.96818	0.0003	-0.57151

PROC CALIS output several tables for the LM tests. The results are shown in different tables, according the type of the parameters. This table shows the ranking of LM statistics for adding the (single-headed) paths into the mental ability model. It gives you the ten paths that can improve the model fit chi-square statistic the most.

The top one is the p1 ---> p2 path. The LM statistic 56.19 means that if you include this path into the model, you can expect to reduce the model fit chi-square by about 56. This is a substantial improvement because you can get this big improvement by just losing one degree of freedom. The second one is the p2 ---> p1 path. Essentially, this will give the same amount of model improvement as the first path. The third one is not that dramatic, but still give you a substantial improvement. Adding the M2 ---> A2 path reduces the model fit chi-square by 19.

Do you want to add these paths into your model? Let us discuss this after we examine more results about the LM tests.

Raine Order Or ene 10 10	rgest LM S	Stat for Error	Variances and	Covariance
Error	Error			Pari
of	of	LM Stat	Pr > ChiSq	Change
P2	P1	56.19312	<.0001	-1.9647
ParentalEncouragement	A1	12.26622	0.0005	0.46050
ParentalEncouragement	A2	12.08031	0.0005	-0.4835
FamilySize	A2	11.22650	0.0008	-1.8820
M2	A2	10.26408	0.0014	1.5589
S2	S1	7.78117	0.0053	1.5531
MentalAbility	A2	7.48800	0.0062	0.7816
AchievementMotivation	A1	6.95709	0.0083	-0.5290
P2	A3	6.54315	0.0105	0.7600
A3	A2	6.21429	0.0127	-0.67173

This table shows the LM tests (statistics) for the error variances and covariances. On the top of the list is the covariance between the errors of P2 and P1. Adding the covariance between the errors of these two variables reduces the model fit chi-square statistic by 56. This is actually the same improvement that we have seen for adding either the P2 --- > P1 or

P1 ---> P2 path. The next one in the list has a much less improvement. The LM statistic is only 12.26.

For this particularly model, these two tables are all that PROC CALIS produces for the LM statistics. The question now is which parameter or parameters you want to add to the model. This could not be answered by just looking at the LM statistics. But it might also involve some judgment about how reasonable the added parameters are. Do these added parameters render your model un-interpretable, or even contradictory to your theoretical claims, despite the fact that they improve your model fit substantially?

Notes on the LM Statistics

- Chi-square reductions are linear approximations
- Chi-square reductions are not additive
- Modifications suggested might not be substantively meaningful

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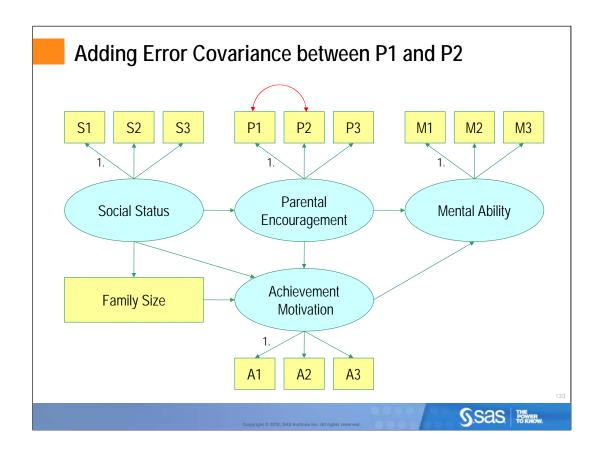
Before giving an answer to the current model modification analysis, some important general points about the LM statistics are discussed.

First, the model fit chi-square reductions as indicated by the LM test statistics are only linear approximations. This means that if you actually refit the model by adding the suggested parameter, the actual chi-square reduction might be more or less.

Second, the chi-square reductions as suggested by the LM test statistics are not additive. That means that you cannot add two or more parameters into the model and expect the actual reduction in the new model is exactly the sum of the corresponding LM statistics. Usually, the actual reduction would be smaller (although it could be larger).

Last but not least, modification suggested by the LM statistics might not be substantively meaningful.

All these three points are important in deciding which parameter you want to add to the current mental ability model for improving the model fit.



Considering the top suggestions from the results of the LM test statistics, I would add the covariance between P1 and P2. The added parameter is shown in the path diagram.

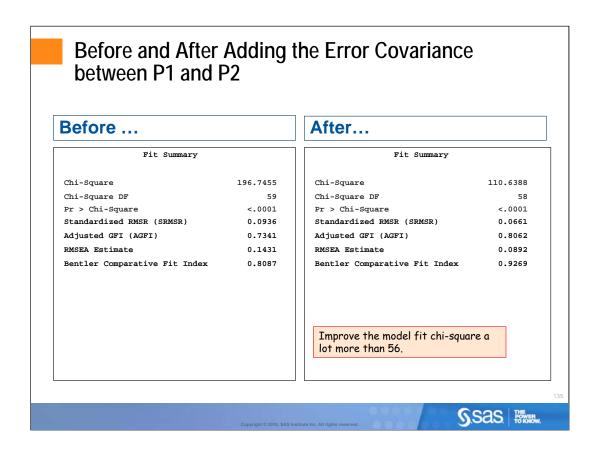
Basically, all the top LM suggestions --- the P2 ---> P1 and P1 ---> P2 paths, and the error covariance between P1 and P2 are just different manifestations of the same lack of fit about a covariance element in the original model. That is, the covariance between P1 and P2 was not well-explained by the original model. Adding either of these will lead to a better fitting of the covariance between P1 and P2. In addition, adding either of these will give you an approximate model fit chi-square improvement of 56. But, you would not get three times of this amount by adding all these three. In fact, if you were to add all these three parameters, it is very likely that your model is not identified, meaning that you would not get unique estimates.

Among the top three choices, the error covariance is chosen because the interpretation of added error covariance is a little "cleaner." P1 and P2 are measurement indicators of the same factor (Parental Encouragement). The error covariance interpretation is that these two indicators have some sort of correlation that is unexplained by their common factor. The added error covariance represents the covariance explained by some unknown sources. However, if I were to add either the P1 ---> P2 or P2 ---> P1 paths, it would create some conflicts with purported common factor structure for the two indicator variables.

Note that the current conclusion is based on a very general argument that aims at preserving the original factor-variable structure. It is not a universal principle. In practice, you have to also consider the substantive grounds of the added parameters.

Adding Covariance between the Errors of P1 and P2 proc calis data=mental nobs=115 modification; path SocialStatus ---> ParentalEncouragement FamilySize AchievementMotivation, FamilySize ---> AchievementMotivation, ParentalEncouragement ---> AchievementMotivation MentalAbility, AchievementMotivation ---> MentalAbility, SocialStatus ---> S1 S2 S3 = 1., ParentalEncouragement ---> P1 P2 P3 = 1., AchievementMotivation ---> A1 A2 A3 = 1., MentalAbility ---> M1 M2 M3 = 1.; pcov P1 P2; run;

Now that I have decided to add the covariance between P1 and P2, I refit the model by adding the PCOV statement specification for the two variables, as shown in the SAS code in this slide. I also use the MODIFICATION option one more time to see if there could be any further suggested improvements.

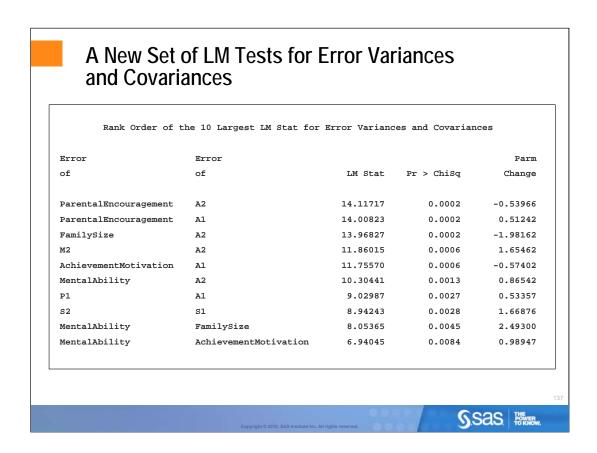


Before you add the error covariance between P1 and P2, your model fit chi-square was about 197. After adding the covariance, the model fit chi-square is about 111. This improvement is actually larger than what the LM statistic suggested, which was 56.

Other fit indices also improve. The SRMSR and the RMSEA are now close to be acceptable. The AGFI and the CFI are boosted to higher levels.

Rank Or	der of the 10 Largest LM S	tat for Path	Relations	
				Parm
То	From	LM Stat	Pr > ChiSq	Change
A2	м2	23.93741	<.0001	0.23830
A2	ParentalEncouragement	22.22260	<.0001	-2.30398
A2	MentalAbility	21.70998	<.0001	0.90790
A1	ParentalEncouragement	19.34281	<.0001	1.96513
A1	MentalAbility	18.10545	<.0001	-0.75752
ParentalEncouragement	A1	17.30632	<.0001	0.32504
A1	M2	15.06992	0.0001	-0.17617
A2	FamilySize	15.06786	0.0001	-0.17675
FamilySize	A2	14.29265	0.0002	-0.89658
AchievementMotivation	A1	11.75569	0.0006	-0.35962

The new set of LM tests for paths suggests the addition of the M2 ---> A2 path. The LM statistic is about 24. If you compare this result with the first LM results regarding the same path, you notice that the LM statistics changes as the fitted model changes. Previously, the same path had an LM statistic of 19. This illustrates the nonlinearity and non-additivity of the LM statistics.



There is also a new set of LM tests for adding error covariances.

You might want to improve your model further by adding some parameters from these two LM tables, although I will not attempt to do more here.

Customized LM Tests

- Principled modification process
- Restrict the set of parameters of interest for the LM tests

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Model modification by using the MODIFICATION option is kind of "blind-search" procedure that you try to improve your model without any definite directions. As discussed before, the LM test statistics might not give you suggestions that are substantively meaningful.

However, in some occasions you might want to restrict your attention to certain set of potential paths or parameters in your model, rather than all possible parameter space searched by the MODIFICATION option.

If you want to do such a principled modification process, you can use the customized LM tests supported in PROC CALIS.

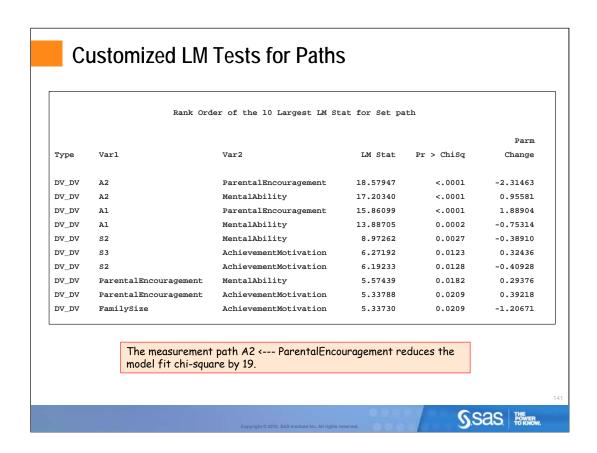
Customized LM Tests by Using the LMTESTS Statement proc calis data=mental nobs=115; path SocialStatus ---> ParentalEncouragement FamilySize AchievementMotivation. FamilySize ---> AchievementMotivation, ParentalEncouragement ---> AchievementMotivation MentalAbility, AchievementMotivation ---> MentalAbility, SocialStatus ---> S1 S2 S3 = 1.ParentalEncouragement ---> P1 P2 P3 AchievementMotivation ---> A1 A2 A3 = 1., ---> M1 M2 M3 = 1.;MentalAbility lmtests corr_err=[coverr] path=[LV->LV LV->MV]; run; Explore the set of LM tests called "path," which Explore the set of LM tests called "corr_err," which contains all the contains all potential latent variable paths (LV-> LV) and measurement paths (LV -> MV) to be potential error covariance parameters (COVERR) to be freed Sas Book

The customized LM tests define sets of parameters of interest so that your model modification process (or LM statistics output) would be limited to those sets of parameters. PROC CALIS provides the LMTESTS statement syntax to achieve the customized LM tests.

The mental ability model is used again. This time I define two sets of parameters of interest. The first set of LM tests is called "corr_err" (it is just a name you assign). This set of parameters contains the parameter region COVERR, which is a keyword that denotes all error covariances in the model. The second set of LM tests is called "path"—a name you assign. This set of parameters do not exhaust all paths in the model. It contains the parameter regions LV->LV and LV->MV, which are keywords that denotes the latent variable (LV) to latent variable (LV) paths and the latent variable (LV) to manifest variable (MV) paths, respectively. Therefore, this customized set "path" excludes paths from observed variables to observed variables, or from observed variables to latent variables so that the factor structures of the model could not be potentially destroyed by adding these paths. The LM tests for these paths are simply not included in the results for the "path" set.

Rank Order of the 10 Largest LM Stat for Set corr_err					
					Parm
Type	Var1	Var2	LM Stat	Pr > ChiSq	Change
COVERR	P2	P1	56.19312	<.0001	-1.96473
COVERR	ParentalEncouragement	A1	12.26622	0.0005	0.46050
COVERR	ParentalEncouragement	A2	12.08031	0.0005	-0.48351
COVERR	FamilySize	A2	11.22650	0.0008	-1.88205
COVERR	M2	A2	10.26408	0.0014	1.55895
COVERR	S2	S1	7.78117	0.0053	1.55314
COVERR	MentalAbility	A2	7.48800	0.0062	0.78161
COVERR	AchievementMotivation	A1	6.95709	0.0083	-0.52904
COVERR	P2	A3	6.54315	0.0105	0.76007
COVERR	A3	A2	6.21429	0.0127	-0.67173

This table shows the customized LM tests of the "CORR_ERR" set. Essentially, this table is the same as one of the standard tables produced with the MODIFICATION option because both tables have the same parameter region "COVERR."



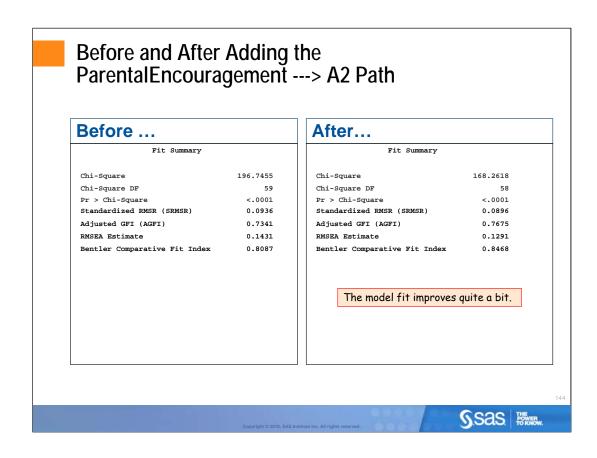
The second customized set of LM tests suggests that adding the dependent variable (DV) to dependent variable (DV) path A2 <--- ParentalEncouragement improves the model fit the most amongst all paths in the "path" set. The chi-square improvement is about 19, which is statistically significant.



Adding the first path suggested by the second set of customized set is represented by the path diagram shown above. The path in red shows that A2, which is an indicator of Achievement Motivation, is now also an indicator of Parental Encouragement. Although the factor-variable functional relationship is preserved in this suggested path diagram, A2 becomes factorially-complex. The also implies that A2 might not have been a good (unique) measure of achievement motivation.

Adding the ParentalEncouragement ---> A2 path proc calis data=mental nobs=115; path SocialStatus ---> ParentalEncouragement FamilySize AchievementMotivation, FamilySize ---> AchievementMotivation, ParentalEncouragement ---> AchievementMotivation MentalAbility, AchievementMotivation ---> MentalAbility, SocialStatus ---> S1 S2 S3 = 1., ParentalEncouragement ---> P1 P2 P3 A2 = 1., AchievementMotivation ---> A1 A2 A3 = 1., MentalAbility ---> M1 M2 M3 = 1.; run;

Nonetheless, you add this new path for A2, as shown in the above PROC CALIS code. All you need to do is to add A2 as one of the observed indicators of the ParentalEncouragement factor.



These two tables compare the fit indices before and after adding the ParentalEncouragement ---> A2 path. The model fit chi-square actually drops more than 19, which was suggested by the LM statistic in the preceding results. All other fit indices improve quite a bit too.

Finally, a caution about all model modification: you should validate your newly-established model by new data. The reason is that the model modification process is subject to the capitalization on chance. Using a principled modification process by the customized LM tests might not avoid the chance problem completely. Confirmation from new data is always recommended.



More About PROC CALIS

- Many other different modeling languages: COSAN, FACTOR, LINEQS, MSTRUCT, and RAM – All support multiple-group analysis and mean structures
- Other estimation methods (default ML): GLS, WLS (ADF), ULS, DWLS, and FIML
- Standardized solutions with standard error estimates
- Analysis of missing patterns (SAS/STAT 9.3)

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Sas Burn

In this workshop, I mostly use the PATH modeling language to fit SEM. I also briefly mentioned the LISMOD as an interface for the LISREL model. There are actually quite a few more modeling language in PROC CALIS: COSAN, FACTOR, LINEQS, MSTRUCT, and RAM. All of these languages support multiple-group analysis and mean structure analysis.

I have also used the default ML (maximum likelihood) estimation method in this workshop, but PROC CALIS supports many other estimation methods as well: GLS (generalize least squares), WLS (weighted least squares), ULS (unweighted least squares), DWLS (diagonally-weighted least squares), and FIML (full information maximum likelihood).

I have only used unstandardized results in most examples, but PROC CALIS also provide standardized solutions with standard error estimates.

Finally, analysis of missing patterns will be available with the FIML method in SAS/STAT 9.3. I hope to add more functionalities to PROC CALIS in the future.



Glossary

Manifest – Observed variables (measured variables) in the data set.

Latent – Unobserved variables.

Endogenous - Dependent /mediating variables; at least one single-headed arrow points to it; used as an outcome variable in an equation; can also be a predictor variable in other equations.

Exogenous – Independent variables; no single-headed arrows point to it; never used as an outcome variable in the model; used only as a predictor in the model.

Factor – A latent (unmeasured) variable that is treated as a hypothetical construct (systematic source) in the model.

Error – An exogenous term for uncertainty (unsystematic source) associated with an endogenous manifest variable (or any endogenous variable, in a more general definition).

Disturbance – An exogenous term for uncertainty (unsystematic source) associated with an endogenous latent variable.

Path diagram representation

- Rectangles: Observed / manifest variables.
- Ovals / circles: Latent variables (factors, errors, and disturbances). Errors and disturbances are not necessarily put into ovals/circles.





Glossary

- Single-headed arrows: Directed paths, direct effects, path coefficients; specified in the PATH statement.
- Double-headed arrows that point to individual variables: Variance parameters of exogenous variables or error variance parameters of endogenous variables; specified in the PVAR statement.
- Double-headed arrows that point to two distinct variables: Covariance parameters between exogenous variables or error covariance parameters between endogenous variables; specified in the PCOV statement.

Fit assessment

- model fit chi-square statistic: Nonsignificance means that the theoretical model is supported; not a very practical index because it almost always rejects all approximating models that are practically useful.
- AGFI (adjusted goodness-of-fit index) and Bentler's CFI (comparative fit index): Two popular fit indices that indicate good model fit when their values are above 0.9.
- SRMR (standardized root mean square residual) and RMSEA (root mean squared error approximation): Two popular fit indices that indicate good model fit when their values are below 0.05.
- AIC, CAIC, and SBC: Information criteria for comparing competing models. The smaller the better.







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