CSE 4554
Machine Learning Lab

Experiment No: 3
Name of the experiment: Logistic Regression with Regularization, Decision Trees, KNN and Naive Bayes

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Contents

1 Objectives

- To know the basics of Logistic Regression

- To know about Regularization

- To know the use of Decision Trees, KNN and Naive Bayes classifier

- To understand how to do result analysis

2 Problem Discussion

2.1 Logistic Regression

Logistic regression is a supervised learning algorithm used for binary classification. It models the probability that an instance belongs to a specific class by fitting a logistic function to the data.

The hypothesis function for logistic regression is:

$$h_\theta(x) = \frac{1}{1 + e^{-\theta^T x}}$$

Where x is the input feature vector and θ are the model parameters.

2.1.1 Cost Function

The cost function for logistic regression is given by:

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^{m} \left[y^{(i)} \log(h_\theta(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_\theta(x^{(i)})) \right]$$

Minimizing this cost function using gradient descent updates the model parameters.

2.1.2 Model Training

Model training is essentially minimization of the loss function. We achieve that with the Gradient Descent technique, which can be broken into a few steps:

1. First, we find derivatives of the loss function with respect to each weight. Derivatives can tell which direction and by how much we should change weight to make the model loss a bit smaller.

2. Updating each weight according to derivative until the local minimum is found, i.e. model doesn't improve anymore so we can stop.

2.2 Regularization

Firstly why do we need Regularization? The biggest reasons for regularization are

1. to avoid overfitting by not generating high coefficients for predictors that are sparse.

2. to stabilize the estimates especially when there's collinearity in the data.

For Point No.1 - is inherent in the regularization framework. Since there are two forces pulling each other in the objective function, if there's no meaningful loss reduction, the increased penalty from the regularization term wouldn't improve the overall objective function. This is a great property since a lot of noise would be automatically filtered out from the model.

To give you an example for 2), if you have two predictors that have the same values, if you just run a regression algorithm on it since the data matrix is singular, your beta coefficients will be Inf if you try to do a straight matrix inversion. But if you add a very small regularization lambda to it, you will get stable beta coefficients with the coefficient values evenly divided between the equivalent two variables.

In L2 regularization, the penalty term is proportional to the square of the coefficients:

$$J(\theta) = -\frac{1}{m}\sum \left[y\log(h_\theta(x)) + (1-y)\log(1-h_\theta(x)) \right] + \frac{\lambda}{2m}\sum \theta_j^2$$

Where λ is the regularization parameter.

In L1 regularization, the penalty term is proportional to the absolute value of the coefficients:

$$J(\theta) = -\frac{1}{m}\sum \left[y\log(h_\theta(x)) + (1-y)\log(1-h_\theta(x)) \right] + \frac{\lambda}{m}\sum |\theta_j|$$

Secondly, When Do we need L1 and L2 regularization?

The main intuitive difference between the L1 and L2 regularization is that L1 regularization tries to estimate the median of the data while the L2 regularization tries to estimate the mean of the data to avoid overfitting. L1 regularization tends to push some coefficients to zero, effectively selecting a simpler model by eliminating less important features. This is particularly useful when you have many features and want to perform feature selection.

3 Decision Trees

Decision trees are a non-parametric supervised learning method used for both classification and regression. They are simple yet powerful algorithms that make decisions by recursively splitting the dataset based on feature values.

3.1 Tree Structure

A decision tree consists of:

- **Nodes**: Each node represents a feature and a condition to split the data.

- **Branches**: The branches represent the outcomes of the condition.

- **Leaves**: The leaves represent the final classification or decision.

3.2 Splitting Criteria

Common criteria for splitting nodes include:

- **Gini Impurity**: Measures how often a randomly chosen element would be incorrectly classified.

- **Entropy**: Measures the amount of uncertainty in the data.

The tree grows by recursively splitting the data until it reaches a stopping condition, such as maximum depth or minimum number of samples per node.

4 K-Nearest Neighbors (KNN)

KNN is a simple, instance-based learning algorithm used for classification and regression. It operates by identifying the k-nearest points (neighbors) to a given input and then making a prediction based on the majority label of those neighbors.

4.1 Distance Metric

KNN relies on a distance metric to determine the closeness of data points. The most commonly used distance metric is the Euclidean distance:

$$d(x,y) = \sqrt{\sum_{i=1}^{n}(x_i - y_i)^2}$$

Where x and y are feature vectors.

4.2 Classification

For classification tasks, KNN assigns the majority class label among the k-nearest neighbors. The value of k is a hyperparameter that must be chosen carefully to balance bias and variance.

5 Naive Bayes Classifier

The Naive Bayes classifier is a probabilistic model based on Bayes' theorem. It assumes that the features are conditionally independent, meaning the value of one feature does not affect the value of another feature.

5.1 Bayes' Theorem

Bayes' theorem is stated as:

$$P(C|X) = \frac{P(X|C) \cdot P(C)}{P(X)}$$

Where:

- $P(C|X)$ is the posterior probability of class C given the features X.

- $P(X|C)$ is the likelihood of the features given the class.

- $P(C)$ is the prior probability of the class.

- $P(X)$ is the prior probability of the features.

5.2 Assumption of Independence

Despite its simplicity, the Naive Bayes classifier performs surprisingly well in many applications, especially when the assumption of independence holds approximately true.

6 Result Analysis

Evaluating the performance of machine learning models requires a variety of metrics. Some commonly used metrics for classification problems include:

6.1 Confusion Matrix

The confusion matrix is a table that describes the performance of a classification model by displaying the counts of true positives, false positives, true negatives, and false negatives.

6.2 Accuracy, Precision, Recall, F1-Score

- **Accuracy**: The ratio of correctly predicted instances to total instances.

- **Precision**: The ratio of correctly predicted positive instances to all predicted positives.

- **Recall**: The ratio of correctly predicted positives to all actual positives.

- **F1-Score**: The harmonic mean of precision and recall.

These metrics give a clear understanding of a model's performance, especially in the case of imbalanced datasets.

7 Data

The first step for any machine learning problem is getting the data. There is no machine "learning" if there is nothing to "learn" from. So for this lab we will be using a dataset named **"Hear Disease Prediction Dataset"** which you can download from Kaggle. You will also find all the details about the dataset in the website. For today's lab use the two class portion of the dataset.

8 Tasks

8.1 Load Dataset (CO 1, PO 1, PO 5):

Load the classification dataset. Explore the dataset using pandas methods such as `head()`, `info()`, and `describe()`.
CO 1: Understanding supervised learning algorithms and how data is handled.
PO 1: Requires foundational knowledge of engineering (data loading and manipulation).
PO 5: Involves the use of modern tools such as pandas for data handling.

8.2 Import Libraries (CO 1, PO 1, PO 5):

Import the necessary libraries for data processing and model evaluation.

```python
1  # For data creation and other tasks
2  import numpy as np
3  import pandas as pd
4  import random
5
6  ## Metrics to evaluate the models
7  from sklearn.metrics import accuracy_score
8
9  # For plotting the graphs
10 import matplotlib.pyplot as plt
11 import seaborn as sns
12
13 # For splitting the data
14 from sklearn.model_selection import train_test_split
```

CO 1: Implementing supervised learning techniques.
PO 1: Requires engineering knowledge in handling tools for machine learning.
PO 5: Application of libraries like NumPy, Matplotlib, and Seaborn for modern data analysis.

8.3 Initialize Weights and Bias(CO 1, PO 2):

Initialize Weights and Bias as 0 and randomly. Note how these two initializations vary.

```python
1  def weightInitialization(n_features):
2      # your code here (w and b should be the required shape)
3      return w, b
```

CO 1: Understanding of weight initialization for logistic regression.
PO 2: This task requires problem analysis and application of machine learning algorithms.

8.4 Sigmoid Function (CO 1, PO 1):

```python
1  def sigmoid_activation(z):
2      # your code here
3      return y
```

CO 1: Understanding supervised learning by implementing the sigmoid function.
PO 1: Requires basic engineering knowledge to implement the activation function.

8.5 Model Optimization Function (CO 1, PO 2, PO 3):

```python
1  def model_optimize(w, b, X, Y):
2      # First find out the number of data
3      # Get the Prediction
4      # Find the cost/loss
5      # Calculate the gradients
6      grads = {"dw": dw, "db": db}
7      return grads, cost
```

CO 1: Understanding how to minimize cost and optimize the logistic regression model.
PO 2: Problem analysis and optimization techniques are applied here.
PO 3: Designing and developing solutions through the model optimization process.

8.6 Model Optimization (CO 1, PO 3, PO 5):

```python
def model_fit(w, b, X, Y, learning_rate, no_iterations):
    costs = []
    for i in range(no_iterations):
        grads, cost = model_optimize(w, b, X, Y)
        dw = grads["dw"]
        db = grads["db"]

        # Update the weights here
        if (i % 10 == 0):
            costs.append(cost)

    #final parameters
    coeff = {"w": w, "b": b}
    return coeff, costs
```

CO 1: Understanding optimization methods through iterations.
PO 3: Developing and refining solutions by optimizing model parameters.
PO 5: Using tools and methods to optimize machine learning models.

8.7 Use Logistic Regression for Your Dataset (CO 1, PO 1, PO 5):

```python
# Split the data into train and test sets in 70:30 ratio
# Train the model with logistic regression
# Get predictions and check the accuracy score
```

CO 1: Implementing supervised learning using logistic regression.
PO 1: Requires basic engineering knowledge to apply logistic regression.
PO 5: Utilization of logistic regression model tools (e.g., sklearn).

8.8 Plot the Cost for Each Epoch (CO 4, PO 4, PO 10):

Task: Use the costs list to plot the cost vs. epoch curve.
CO 4: Understanding how to evaluate and analyze model performance through cost reduction.
PO 4: Investigation of optimization problems through visualization.
PO 10: Communicating results through graphical analysis.

8.9 Plot Training vs Testing Accuracy (CO 4, PO 4, PO 10):

Task: Plot training vs testing accuracy graph
CO 4: Understanding how to evaluate and analyze model performance through accuracy plots
PO 4: Investigation of optimization problems through visualization.
PO 10: Communicating results through graphical analysis.

8.10 Use Smaller Portion of Training Data (CO 4, PO 4):

Task: Show how accuracy of the test dataset changes when you use 10%, 20%, and so on of the training dataset.
CO 4: Understanding model evaluation when data is constrained.
PO 4: Investigating the performance of the model with different amounts of training data.

8.11   L1 and L2 Regularization (CO 2, PO 2, PO 5):

```
1 def model_optimize(w, b, X, Y, reg=None, lambda=0.1):
2     # Regularization effects on cost and optimization
3     grads = {"dw": dw, "db": db}
4     return grads, cost
```

CO 2: Understanding the concepts of regularization (L1/L2).
PO 2: Problem-solving through regularization techniques.
PO 5: Applying regularization through modern tools and libraries.

8.12   Accuracy Change with Regularization (CO 2, PO 4):

Task: Train the model for different regularization values and epochs. Display test accuracies in a table.
CO 2: Understanding the impact of regularization on model performance.
PO 4: Investigating how regularization affects accuracy across different training runs.

8.13   Logistic Regression Class from sklearn (CO 1, PO 5):

Task: Use the Logistic Regression model from the sklearn library and find the accuracy after training.
CO 1: Application of logistic regression from 'sklearn'.
PO 5: Utilizing modern tools and techniques in machine learning.

8.14   Decision Trees from sklearn (CO 3, PO 3, PO 5):

Task: Use the Decision Tree model from the sklearn library and find the accuracy after training.
CO 3: Understanding and applying decision trees.
PO 3: Developing solutions using decision tree algorithms.
PO 5: Application of decision tree tools.

8.15   Naive Bayes from sklearn (CO 3, PO 3, PO 5):

Task: Use the Naive Bayes model from the sklearn library and find the accuracy after training.
CO 3: Understanding Naive Bayes classification.
PO 3: Applying Naive Bayes for problem-solving in classification tasks.
PO 5: Using tools like 'sklearn' for implementing Naive Bayes.

8.16   Calculate different accuracy metrics:

Task: Find accuracy, F1 Score, Recall, Confusion Matrix etc