

Answer to Question no. 3

If there are N places and M roads, it means there are M number of edges and N number of vertices. For task 1 and task 2, the time complexity will be $M \log N$. For both tasks we used Dijkstra Algorithm. For traversal, here we used BFS and to store the shortest path we used min heap. For extracting it takes $O(\log N)$ time in min heap. When we traverse using BFS it takes $O(N+M)$ time. So, the total time complexity will be $O(M \log N)$ for task 1. For same reason, the time complexity of task 2 will be $O(M \log N)$.

If the number of Titans in all road becomes 1, then we should not think about the ~~shortest~~ weight at all. For those we just have to care about the shortest path as it will give me less titan.

Pseudocode:

Dijkstra(Graph, source):

distance : []

visited : []

for each v in Graph:

distance[v] $\leftarrow \infty$

push in min heap (distance[v], v)

visited \rightarrow false.

while minheap \neq empty

$u \leftarrow$ min heap, extract

if visited[v]:

continue.

for each neighbour in graph:

if distance[n] > distance[u[i]] + Graph[u[i]][n]

distance[n] = u
parent[n] = u[i].