Performance Analysis in C++

The principle challenge of HPC is understanding your stack.

The *first* challenge is *defining correctness*, and asserting on invariants.

The *second* challenge is market competitiveness, which is based principally on usability.

- >> Adaptive numerical algorithms instead of user parameters
- >> Progress reporting
- >> Widely compatible data formats
- » Curated algorithms, rather than choice of algorithms

The *last* challenge is performance analysis, which is today's topic.

As you optimize code, you will begin to develop intuitions about what C++ code is fast and what is slow

- >> std::array is faster than std::vector
- >> float is faster than double
- >> if checks break the pipeline
- >> std::vector is faster than std::list
- >> std::vector::reserve is faster than std::vector::push_back

But tomorrow a smart compiler writer could make all this stuff false.

What does a performance benchmark need to do?

- >> Call the function repeatedly until statistical confidence is gained about its runtime, and no longer
- >> Not get optimized out by the compiler
- >> Test multiple inputs for signs of scaling problems
- >> Be usable

Use google/benchmark!

The installation is simple:

```
$ git clone https://github.com/google/benchmark.git
$ mkdir build_benchmark; cd build_benchmark
build_benchmark$ cmake -DCMAKE_BUILD_TYPE=Release ../benchmark
build_benchmark$ make -j`nproc`
build_benchmark$ make test
build_benchmark$ sudo make install
```

google/benchmark minimal working example

```
#include <cmath>
#include <benchmark/benchmark.h>
static void BM_Pow(benchmark::State& state)
    while (state.KeepRunning())
        auto y = std::pow(1.2, 1.2);
BENCHMARK(BM_Pow);
BENCHMARK_MAIN();
```

google/benchmark minimal working example

Build sequence:

```
CXX=clang++
all: run_benchmarks.x run_benchmarks.s
run_benchmarks.x: run_benchmarks.o
    $(CXX) -o $@ $< -lbenchmark -pthread
run_benchmarks.o: run_benchmarks.cpp
    $(CXX) -std=c++14 -03 -c $< -o $@
run_benchmarks.s: run_benchmarks.cpp
    $(CXX) $(CPPFLAGS) -S -masm=intel $<</pre>
clean:
   rm -f *.x *.s *.o
```

google/benchmark minimal working example

```
Run:
./run_benchmarks.x
Run on (4 X 1000 MHz CPU s)
2016-06-23 17:58:41
                                    CPU Iterations
                    Time
Benchmark
BM_Pow
                                   3 ns 264837522
                    3 ns
```

In fact 3 ns seems a bit fast for this operation. The compiler might have (correctly) reasoned that the repeated call to std::pow is useless, and optimized it out.

We can generate the assembly of this function via

clang++ -std=c++14 -03 -S -masm=intel run_benchmarks.cpp

We can see all function calls in the assembly via

```
$ cat run_benchmarks.s | grep 'call' | awk '{print $2}' | xargs c++filt
benchmark::State::KeepRunning()
benchmark::Initialize(int*, char**)
benchmark::RunSpecifiedBenchmarks()
benchmark::State::ResumeTiming()
benchmark::State::PauseTiming()
__assert_fail
operator new(unsigned long)
benchmark::internal::Benchmark::Benchmark(char const*)
benchmark::internal::RegisterBenchmarkInternal(benchmark::internal::Benchmark*)
operator delete(void*)
_Unwind_Resume
std::pow isn't one of them!
```

- >> The compiler's goal is to remove all unnecessary operations from your code
- Your goal is to do unnecessary operations to see how long a function call takes

This problem is so pervasive that google/benchmark has created a function to deal with it: benchmark::DoNoOptimize:

```
double y
while (state.KeepRunning()) {
    benchmark::DoNotOptimize(y = std::pow(1.2, 1.2));
}
```

The purpose of this is to tell the compiler to *not* optimize out the assignment of y.

But benchmark::DoNotOptimize can't keep the compiler from evaluating std::pow(1.2, 1.2) at compile time.

To keep the compiler from evaluating std::pow(1.2, 1.2) at compile time, we simply need to ensure that is doesn't know what values it needs to evaluate. Here's a solution:

```
std::random_device rd;
std::mt19937 gen(rd());
std::uniform_real_distribution<double> dis(1, 10);
auto s = dis(gen);
auto t = dis(gen);
double y;
while (state.KeepRunning())
{
    benchmark::DoNotOptimize(y = std::pow(s, t));
}
```

However, benchmark::DoNotOptimize forces the result to be stored into RAM, which takes time over register storage:

```
template <class Tp>
inline BENCHMARK_ALWAYS_INLINE void DoNotOptimize(Tp const& value) {
    asm volatile("": "+m" (const_cast<Tp&>(value)));
}
```

Even then we might still have to play tricks on the compiler. One of my favorites: Write the result to /dev/null outside the loop:

```
double y
while (state.KeepRunning()) {
    benchmark::DoNotOptimize(y = std::pow(s, t));
}
std::ostream cnull(0);
cnull << y;</pre>
```

Stop compiler optimizations: Full boilerplate

```
#include <cmath>
#include <ostream>
#include <random>
#include <benchmark/benchmark.h>
static void BM_Pow(benchmark::State& state) {
    std::random_device rd;
   std::mt19937 gen(rd());
   std::uniform_real_distribution<double> dis(1, 10);
   auto s = dis(gen);
   auto t = dis(gen);
   double y;
   while (state.KeepRunning()) {
       benchmark::DoNotOptimize(y = std::pow(s, t));
    std::ostream cnull(0);
    cnull << y;</pre>
BENCHMARK(BM_Pow);
BENCHMARK_MAIN();
```

Now our timings are more in line with our expectations:

```
Run on (1 X 2300 MHz CPU )

2016-06-24 20:11:40

Benchmark Time CPU Iterations

BM_Pow 80 ns 80 ns 9210526
```

Templated Benchmarks

It's often useful to find out how fast your algorithm is in float, double, and long double precision. Google benchmark supports templates without too much code duplication

Templated Benchmarks

```
template<typename Real>
static void BM_PowTemplate(benchmark::State& state) {
    std::random_device rd;
    std::mt19937 gen(rd());
    std::uniform_real_distribution<Real> dis(1, 10);
    auto s = dis(gen);
    auto t = dis(gen);
   Real y;
   while (state.KeepRunning()) {
        benchmark::DoNotOptimize(y = std::pow(s, t));
    std::ostream cnull(nullptr);
    cnull << y;</pre>
BENCHMARK_TEMPLATE(BM_PowTemplate, float);
BENCHMARK_TEMPLATE(BM_PowTemplate, double);
BENCHMARK_TEMPLATE(BM_PowTemplate, long double);
```

Templated Benchmarks

The results are sometimes surprising; for instance double is found to be faster than float:

```
Run on (1 X 2300 MHz CPU )
2016-06-25 00:07:26
                                                      CPU Iterations
                                      Time
Benchmark
BM_PowTemplate<float>
                                   136 ns
                                                            5468750
                                                  127 ns
BM_PowTemplate<double>
                                     95 ns
                                                    94 ns
                                                             700000
BM_PowTemplate<long double>
                                                   403 ns
                                                             1699029
                                    404 ns
```

Sometimes you need to analysis the scaling properties of your algorithm. Let's try an example with an algorithm with terrible scaling: Recursive Fibonnaci numbers:

```
uint64_t fibr(uint64_t n)
{
   if (n == 0)
      return 0;

   if (n == 1)
      return 1;

   return fibr(n-1)+fibr(n-2);
}
```

Our benchmark code is

```
static void BM_FibRecursive(benchmark::State& state)
    uint64_t y;
    while (state.KeepRunning())
      benchmark::DoNotOptimize(y = fib1(state.range_x()));
    std::ostream cnull(nullptr);
    cnull << y;</pre>
BENCHMARK(BM_FibRecursive)->RangeMultiplier(2)->Range(1, 1<<5);
```

```
BENCHMARK(BM_FibRecursive)->RangeMultiplier(2)->Range(1, 1<<5)
will request a benchmark with state.range_x() taking values of
[1, 2, 4, 8, 16, 32].</pre>
```

```
Run on (1 X 2300 MHz CPU )
2016-06-25 00:38:14
                                       Time
                                                      CPU Iterations
Benchmark
BM_FibRecursive/1
                                      7 ns
                                                     7 ns
                                                             83333333
BM_FibRecursive/2
                                                             72916667
                                                    15 ns
                                     15 ns
BM_FibRecursive/4
                                     37 ns
                                                    37 ns
                                                             17156863
BM_FibRecursive/8
                                    268 ns
                                                   268 ns
                                                              2868852
BM_FibRecursive/16
                                                                64815
                                  13420 ns
                                                 13392 ns
BM_FibRecursive/32
                                              24320000 ns
                               24372253 ns
                                                                   25
```

Can we empirically determine the asymptotic complexity of the recursive Fibonacci number calculation?

Pretty much . . . !

google/benchmark will try to figure out the algorithmic scaling, if you ask it to. Example:

```
static void BM_FibRecursive(benchmark::State& state)
{
    uint64_t y;
    while (state.KeepRunning())
    {
        benchmark::DoNotOptimize(y = fib1(state.range_x()));
    }
    std::ostream cnull(nullptr);
    cnull << y;
    state.SetComplexityN(state.range_x());
}

BENCHMARK(BM_FibRecursive)->RangeMultiplier(2)->Range(1, 1<<5)->Complexity();
```

The result?

BM_FibRecursive/1	9	ns	9 ns	72916667
BM_FibRecursive/2	19	ns	19 ns	44871795
BM_FibRecursive/4	42	ns	43 ns	14112903
BM_FibRecursive/8	270	ns	268 ns	2611940
BM_FibRecursive/16	11305	ns	11264 ns	54687
BM_FibRecursive/32	27569038	ns	27555556 ns	27
BM_FibRecursive_BigO	828.24	N^3	827.83 N^3	
BM_FibRecursive_RMS	31	%	31 %	

It erroneously labels the algorithm as cubic; though we can see the fit is not tight.

Passing a lambda to Complexity()

If google/benchmark only tries to fit to the most common complexity classes. You are free to specify the asymptotic complexity yourself, and have google/benchmark determine goodness of fit.

The complexity of the recursive Fibonacci algorithm is ϕ^n , where $\phi := (1 + \sqrt{5})/2$ is the golden ratio, so let's use ϕ^n as a lambda . . .

Passing a lambda to Complexity()

Syntax:

```
BENCHMARK(BM_FibRecursive)
   ->RangeMultiplier(2)
   ->Range(1, 1<<5)
    ->Complexity([](int n) {return std::pow((1+std::sqrt(5))/2, n);});
```

Result:

```
BM_FibRecursive/1
                            9 ns
                                           9 ns
                                                  79545455
BM_FibRecursive/2
                                                  44871795
                           19 ns
                                          19 ns
BM_FibRecursive/4
                                                  20588235
                                          37 ns
                           37 ns
BM_FibRecursive/8
                          228 ns
                                         228 ns
                                                   3125000
BM_FibRecursive/16
                         9944 ns
                                                     60345
                                        9943 ns
BM_FibRecursive/32
                                    23866667 ns
                     23910141 ns
                                                         30
BM_FibRecursive_BigO
                           4.91 f(N)
                                            4.90 f(N)
BM_FibRecursive_RMS
                             0 %
                                           0 %
```

(Note: All lambdas are denotes as f(N), so you have to know what you wrote in your source code to understand the scaling.)

Other tricks:

Standard complexity classes don't need to be passed as lambdas:

```
Complexity(benchmark::o1);
Complexity(benchmark::oLogN);
Complexity(benchmark::oN);
Complexity(benchmark::oNLogN);
Complexity(benchmark::oNSquared);
Complexity(benchmark::oNCubed);
```

Benchmarking data transfer

To get data about data transfer rates, use state. SetBytesProcessed¹:

¹ Taken directly from the google/benchmark docs.

Benchmarking data transfer

state. SetBytesProcessed adds another column to the output:

```
Run on (1 X 2300 MHz CPU )
2016-06-25 19:25:23
Benchmark
                       Time
                                       CPU Iterations
BM_memcpy/8
                                                        883.032MB/s
                       9 ns
                                             87500000
                                      9 ns
BM_memcpy/16
                                                        1.70305GB/s
                       9 ns
                                      9 ns
                                             79545455
BM_memcpy/32
                                                        3.50686GB/s
                                      8 ns
                                             79545455
                        9 ns
BM_memcpy/64
                                                        5.35243GB/s
                       11 ns
                                             62500000
                                     11 ns
BM_memcpy/128
                      13 ns
                                                        8.97969GB/s
                                             53030303
                                     13 ns
BM_memcpy/256
                                                        15.1964GB/s
                       16 ns
                                             44871795
                                     16 ns
BM_memcpy/512
                                                        24.4167GB/s
                                             36458333
                       19 ns
                                     20 ns
BM_memcpy/1024
                                             28225806
                                                        38.6756GB/s
                       25 ns
                                     25 ns
BM_memcpy/2k
                                                         38.147GB/s
                       50 ns
                                     50 ns
                                             10000000
BM_memcpy/4k
                     122 ns
                                    122 ns
                                              5833333
                                                        31.2534GB/s
BM_memcpy/8k
                                                         34.726GB/s
                      220 ns
                                    220 ns
                                              3240741
```

Running a subset of your benchmarks:

Each benchmark takes ~1 second to run. If you need to analyze only one of the benchmarks, use the --benchmark_filter option:

```
./run_benchmarks.x --benchmark_filter=BM_memcpy/32
Run on (1 X 2300 MHz CPU )
2016-06-25 19:34:24
Benchmark
                      Time
                                     CPU Iterations
BM_memcpy/32
                                                      2.76944GB/s
                     11 ns
                                   11 ns
                                           79545455
BM_memcpy/32k
                                                      13.9689GB/s
                   2181 ns
                                 2185 ns
                                             324074
BM_memcpy/32
                                                      2.46942GB/s
                                   12 ns
                                           54687500
                     12 ns
BM_memcpy/32k
                                                      16.6145GB/s
                   1834 ns
                                 1837 ns
                                             357143
```

Error bars

In general you will get a pretty good idea about the standard deviation of the measurements just by running it a few times. However, if you want error bars, just specify the number of times you want your benchmark repeated:

BENCHMARK(BM_Pow)->Repetitions(12);

Error bars

Run on (1 X 2300 MHz CPU)
2016-06-25 19:57:40
Benchmark

Benchmark	Time	CPU	Iterations
BM_Pow/repeats:12	70 ns	70 ns	10294118
BM_Pow/repeats:12	73 ns	73 ns	10294118
BM_Pow/repeats:12	71 ns	71 ns	10294118
BM_Pow/repeats:12	70 ns	70 ns	10294118
BM_Pow/repeats:12	71 ns	71 ns	10294118
BM_Pow/repeats:12	72 ns	72 ns	10294118
BM_Pow/repeats:12	73 ns	73 ns	10294118
BM_Pow/repeats:12	71 ns	71 ns	10294118
BM_Pow/repeats:12	70 ns	70 ns	10294118
BM_Pow/repeats:12	73 ns	73 ns	10294118
BM_Pow/repeats:12	71 ns	71 ns	10294118
BM_Pow/repeats:12	76 ns	75 ns	10294118
BM_Pow/repeats:12_mean	72 ns	72 ns	10294118
BM_Pow/repeats:12_stddev	2 ns	2 ns	0