# Simple thermal model

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#### 0.1 Introduction

Write from scratch thermal model for single homogeneous material with no temperature-dependence and no atmosphere to test against KRC.

KRC run: no atmosphere, Fake the geometry matrix for circular orbit with same semi-major axis as Mars, but zero eccentricity and obliquity.

Fiddle with declination of planets spin axis, but then discover that the BFRM matix is all that matters; set its elements to 1. or 0. Then test print (LP2 true, set flags to print solar dec and half day at evey latitude and season)

Test run has downvis at -60 same as at +60 all year, so obliquity must be zero.

#### 0.2 Take-away

Should not allow time doubling in the first two physical layers. For  $0.1~\mathrm{K}$  numerical accuracy, KRC runs should use finer layers than current standard and extend to depth of about  $100~\mathrm{diurnal}$  skin-deepths

## 1 Formulation

Start with initial temperature profile, Compute average radiation flux for the first interval. Use this and T set from prior step to find new  $T_S$ , and then use that boundary condition to set the heat flow into the top layer for the next time istep.

Thus, model times are at the end of the interval over which the boundary condition was averaged. With 0-based indexing and N times per sol; local Hour is 24\*i/N.

With material properties the same for every layer, the JGR equations reduce to:

$$(21) \Longrightarrow F_{1_i} = \frac{2\Delta t_i \kappa}{(1. + R)B_i^2}$$

where  $R \equiv B_+/B_i$  is RLAY. And

$$(22) \Longrightarrow \ F_{3_i} = \frac{1+R}{1+1/R} \equiv \frac{1+R}{\frac{1}{R}(R+1)} \equiv R$$

Initial estimate:

$$(11) \Longrightarrow \langle T_s^4 \rangle = (1. - A) S_M \langle \mu_0 \rangle / \epsilon \sigma$$

Upper Boundary condition

(13) 
$$\Longrightarrow W = (1. - A)S_M \mu_0 + k \frac{\partial T}{\partial z}_{(z=0)} - \epsilon \sigma T^4$$

$$(29) \Longrightarrow \frac{\partial W}{\partial T} = -k/X_2 - 4\epsilon\sigma T^3$$

where  $X_2$  is the depth to the center of the first soil layer. X or z increases downward.

No time division. Set first physical layer to have thickness FLAY.

$$(16) \Longrightarrow \frac{\Delta T_i}{\Delta t} = -\frac{H_{i+.5} - H_{i-.5}}{B_i \rho C_p}$$

Linear gradient between layer mid-points

$$(17+3) \Longrightarrow H_{i+,5} = -k \frac{T_{+} - T_{i}}{B_{i}/2 + B_{+}/2} \quad \text{and} \quad H_{i-,5} = -k \frac{T_{i} - T_{-}}{B_{i}/2 + B_{-}/2}$$

$$\Delta T_{i} = \frac{k}{\rho C_{p}} \frac{2\Delta t}{B_{i}} \left[ \frac{T_{+} - T_{i}}{B_{i} (1+R)} - \frac{T_{i} - T_{-}}{\frac{B_{i}}{R} (1+R)} \right]$$

$$\Delta T_{i} = \kappa \frac{2\Delta t}{(1+R) R^{2}} [T_{+} - (1+R) T_{i} + RT_{-}] \iff (18s)$$

$$\Delta T_i = \kappa \frac{2\Delta t}{(1+R)B_i^2} [T_+ - (1+R)T_i + RT_-] \iff (18s)$$

which reduces to (18) if R=1

#### 1.0.1 Virtual layers

Set heat flow at bottom to zero by setting the under-layer to same temperature as the bottom physical layer.

Set the temperature  $T_V$  of the virtual over-layer by requiring that the thermal gradient from its center to center of first physical layer  $T_F$  be the same as from surface  $T_S$  to that point

$$\frac{T_S - T_F}{B_F/2} = \frac{T_V - T_F}{B_V/2 + B_F/2} \mapsto (T_S - T_F) \frac{B_V + B_F}{B_F} = T_V - T_F \mapsto T_V = T_F - (1 + 1/R)(T_S - T_F)$$

#### Perturbation 1.1

Each 'mset'=parr[4] days, perturb temperature at midnight by minus the diurnal average for each layer relative to diurnal average for layer 'Lset'=parr[19]

#### 1.2Total depth

Useful relation for computing depth to bottom of physical layers.

$$y \equiv \sum_{k=0}^{n} r^{k} = \frac{1 - r^{n+1}}{1 - r}$$
 and  $z \equiv \sum_{k=0}^{n} r^{k} = \frac{r(1 - r^{n})}{1 - r}$ 

Solve for n:

$$n_0 = (\ln[1 + y(r-1)] / \ln r) - 1$$
 and  $n_1 = \ln\left[\frac{z(r-1)}{r} + 1\right] / \ln r$ 

But if r = 1, above degenerate;

$$n_0 = y - 1$$
 and  $n_1 = z$ 

For KRC, where first physical layer is F=FLAY, r=RLAY and the total depth D; use  $n_{0(y=D/F)}$ . Because the first physical layer index is number 2, to ensure total depth D or more,  $NLAY=ceil(n_0)+2$ 

IDL routine NUMGEOMLAY is useful for computing number of layers or total depth.

Table 1: Parameters of the KRCSIMPLE routine. Those marked with '-' do not affect the numerical result; those marked with 'c' were constant for this study; primary changes are maked with '+'

```
0.0000 Flag to modify this, +2=only compute depth chart
   0
        mod.
   1
        nlay
                     49.000
                             n1: number of real layers
   2
         n/H
                     1024.0
                             n2: times per "hour"
       H/sol
                             Output Hours per sol
   3
                     48.000
   4
        mset
                     3.0000
                             season per reset
   5
                             n5: seasons per year
          n5
                     20.000
        dBug
   6
                     0.0000
                             bit-encoded: +1=stop before return +2=convrgPlot,+4=more plots
  7
                             timestep to stop ^=^=^=^=^
       kStop
                    -2.0000
                                                            integer
                   0.024000
                             scaled thickness of first layer
  8
        flay
  9
                     1.0620
                             layer thickness ratio
        rlay
                 1.0000e-05
  10
                             convergence test
         ggt
c 11
         Alb
                    0.25000
                             albedo
c 12
        emis
                     1.0000
                             emissivity
c 13
          ΤI
                     200.00
                             inertia
                             density
c 14
        dens
                     1600.0
                             specific heat
c 15
          Ср
                     647.00
- 16
        quit
                     0.0000
                             - to exit
  17
        mSaf
                    0.80000
                             minimum safety factor
                             starting temperature if positive
       Tinit
                     0.0000
  18
  19
        Lset
                     2.0000
                             physical layer to use for reset INT
                             Season delta T
  20
                 1.0000e-07
        delT
- 21
       etime
                     41.685
                             OUT: elapsed time
- 22
       depth
                     6.9906
                             OUT bottom scaled depth
```

### 1.3 Stability and convergence tests

The safety factor relative to classical convergence,  $B/\sqrt{2\kappa\Delta t}$ , is constrained to be larger than parr[17], default 0.8.

## 1.4 Results

#### 1.4.1 Run L

SIMPLE run L, 20 models listed in Table 2. Models 16:19 had the same layer structure: changes were increasing steps/hour and for 19, reducing ggt 1.e-5 to 1.e-8 and reducing the "last season" criterium of the maximum change in midnight temperature of any layer from 1.e-7 to 1.e-10. This last change in tolerance had negligable effect,  $T_S$  at the 48 times of day for Model 18 - Model 19 had a mean of 1.65e-08 and StdDev of 5.38e-09.

Variation with RLAY and FLAY is shown in Fig 1. Similar tests with KRC; see Figure 3.

KRC case 10 -SIMPLE L:9 has range of -0.19 to +0.16

Run L, Model 19 versus 18 shows that tighter tolerances had negligable effect.

Columns in legend for KRCSIMPLOT, e.g., Figure 1:

0-based model index

N1 = NLAY = number of layers

n2 = times per "hour"

flay = scaled thickness of first layer

rlay = layer thickness ratio

D = bottom scaled depth

SIMPLE run M had all models with 768 time/Hour and depths about 5:8 D. Variations were only of F and R. Reference model has depth of 8.25; increasing to 26 made virtually no difference (MAR= 2.e-6).

SIMPLE run X had 9 difference time-steps by factors of 2, all had 49 layers. Models 0:6 used flay=0.024 and lie on a nearly straight line in log time : log MAR space if the reference is the finest time-step model. Model 7:9 used flay=0.05 for stability and are twice as deep. Using KRC extreme-fine model as reference, models with 1024 to 16384 time-steps per 1/2 hour all had MAR near 0.033 K. The model with flay=0.05 and 256 steps per 1/2 hour had the best performance; MAR= 0.34 K in 22 seconds. Models with flay=0.024, steps=256 and flay=0.05, steps=128 were similar with MAR=0.04 and time about 11 sec. Flay=0.05, steps=64 had MAR=.06 in 5.8 sec.

Table 2: Values for the models in SIMPLE run L. Columns with numbers correspond to model parameters in Table 1; saFac is the stability safety factor for the top layer. Tdel is the surface temperature at 7 hours (index 14) relative to the average for all models, to help in curve identification. Lower part: Difference of surface temperature from model 18 over the 48 output times; MAR= Mean absolute residual

SIMPLE L											
mod.	0	2	4	8	9	10	20	21	22		
i n	lay	n/H	mset	flay	rlay	ggt	delT	etime	depth	saFac	Tdel
0	32	96	2	0.120	1.200	1.00e-05	1.00e-07	8.98	204.49	3.25	0.176
1	13	96	2	0.120	1.200	1.00e-05	1.00e-07	2.82	5.82	3.25	0.177
2	19	96	2	0.120	1.100	1.00e-05	1.00e-07	2.88	6.14	3.25	0.132
3	27	96	2	0.120	1.050	1.00e-05	1.00e-07	3.67	6.56	3.25	0.107
4	39	96	2	0.120	1.020	1.00e-05	1.00e-07	3.86	6.99	3.25	0.090
5	46	96	2	0.120	1.010	1.00e-05	1.00e-07	3.92	6.97	3.25	0.085
6	58	96	2	0.120	1.000	1.00e-05	1.00e-07	4.07	6.96	3.25	0.079
7	14	96	2	0.100	1.200	1.00e-05	1.00e-07	2.78	5.92	2.71	0.085
8	21	96	2	0.100	1.100	1.00e-05	1.00e-07	3.61	6.40	2.71	0.044
9	30	96	2	0.100	1.050	1.00e-05	1.00e-07	3.65	6.64	2.71	0.022
10	18	96	2	0.050	1.200	1.00e-05	1.00e-07	3.46	6.41	1.35	-0.092
11	28	96	2	0.050	1.100	1.00e-05	1.00e-07	3.58	6.71	1.35	-0.116
12	42	96	2	0.050	1.050	1.00e-05	1.00e-07	3.80	6.76	1.35	-0.129
13	67	96	2	0.050	1.020	1.00e-05	1.00e-07	4.10	6.92	1.35	-0.138
14	140	96	2	0.050	1.000	1.00e-05	1.00e-07	5.00	7.00	1.35	-0.144
15	34	96	2	0.050	1.100	1.00e-05	1.00e-07	5.83	12.27	1.35	-0.116
16	38	96	2	0.050	1.100	1.00e-05	1.00e-07	7.44	18.20	1.35	-0.116
17	38	192	2	0.050	1.100	1.00e-05	1.00e-07	14.93	18.20	1.91	-0.065
18	38	384	2	0.050	1.100	1.00e-05	1.00e-07	29.87	18.20	2.71	-0.040
19	38	384	2	0.050	1.100	1.00e-08	1.00e-10	46.21	18.20	2.71	-0.040
		ence f				18 in K					
mode	1	0		1	2	3 4		6	7	8	9
		10	1			3 14	15	16 1			
MA		0.081				040 0.045			061 0.0		24
			0.02		5 0.04		0.022 0.0				
mea		-0.016				016 0.020		0.023 -0.			12
a. 15		.020 -				8 0.009 -				-0.000	
StdDe		0.096				052 0.051			066 0.0		26
	0	.036	0.03	2 0.04	3 0.04	9 0.053	0.032 0.0	0.01	1 0.000	0.000	

Table 3: Models parameters for SIMPLE runs M and X. Lower part of each: difference of surface temperature from specified model within the run.

SIMPLE M										
i nlay	n/H n	nset	flay	rlay	ggt	delT	etime	depth	saFac	Tdel
0 11	384	2	0.100	1.300	1.00e-05	1.00e-07	14.76	5.64	5.42	0.183
1 14	384	2	0.050	1.300	1.00e-05	1.00e-07	14.91	6.40	2.71	-0.006
2 17	384	2	0.025	1.300	1.00e-05	1.00e-07	14.91	7.13	1.35	-0.074
3 14	384	2	0.100	1.200	1.00e-05	1.00e-07	14.81	5.92	5.42	0.149
4 18	384	2	0.050	1.200	1.00e-05	1.00e-07	14.97	6.41	2.71	-0.027
5 22	384	2	0.025	1.200	1.00e-05	1.00e-07	15.12	6.78	1.35	-0.086
6 21	384	2	0.100	1.100	1.00e-05	1.00e-07	15.16	6.40	5.42	0.109
7 28	384	2	0.050	1.100	1.00e-05	1.00e-07	15.37	6.71	2.71	-0.051
8 37	384	2	0.025	1.100	1.00e-05	1.00e-07	19.95	8.25	1.35	-0.099
9 49	384	2	0.025	1.100	1.00e-05	1.00e-07	41.59	26.43	1.35	-0.099
Ts diffe:	rence fi	com	model		8					
model	0		1	2	3 4	5	6	7	8	9
MAR	0.152	0.	103 0.	085 0.	0.051	0.036 0		012 0.0	00 0.00	00
mean	-0.046	-0.	044 -0.	042 -0.	017 -0.018	-0.017 0	0.005 0.	0.0	00 -0.00	00
StdDev	0.162	0.	102 0.	082 0.	112 0.052	0.035 0	0.077 0.	018 0.0	00 0.00	00
OTMDID V										
SIMPLE X	/11		£7	1		4-17		4	F	T4-1
i nlay	n/H n			rlay	ggt	delT	etime	depth	saFac	Tdel
i nlay 0 49	1024	3	0.024	1.062	1.00e-05	1.00e-07	41.69	6.99	2.12	0.011
i nlay 0 49 1 49	1024 2048	3 3	0.024 0.024	1.062 1.062	1.00e-05 1.00e-05	1.00e-07 1.00e-07	41.69 83.94	6.99 6.99	2.12 3.00	0.011 0.016
i nlay 0 49 1 49 2 49	1024 2048 4096	3 3 3	0.024 0.024 0.024	1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52	6.99 6.99 6.99	2.12 3.00 4.25	0.011 0.016 0.018
i nlay 0 49 1 49 2 49 3 49	1024 2048 4096 8192	3 3 3 3	0.024 0.024 0.024 0.024	1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64	6.99 6.99 6.99	2.12 3.00 4.25 6.00	0.011 0.016 0.018 0.019
i nlay 0 49 1 49 2 49 3 49 4 49	1024 2048 4096 8192 16384	3 3 3 3	0.024 0.024 0.024 0.024 0.024	1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40	6.99 6.99 6.99 6.99	2.12 3.00 4.25 6.00 8.49	0.011 0.016 0.018 0.019 0.020
i nlay 0 49 1 49 2 49 3 49 4 49 5 49	1024 2048 4096 8192 16384 512	3 3 3 3 3	0.024 0.024 0.024 0.024 0.024 0.024	1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81	6.99 6.99 6.99 6.99 6.99	2.12 3.00 4.25 6.00 8.49 1.50	0.011 0.016 0.018 0.019 0.020 0.002
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 6 49	1024 2048 4096 8192 16384 512 256	3 3 3 3 3 3	0.024 0.024 0.024 0.024 0.024 0.024 0.024	1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26	6.99 6.99 6.99 6.99 6.99 6.99	2.12 3.00 4.25 6.00 8.49 1.50 1.06	0.011 0.016 0.018 0.019 0.020 0.002 -0.017
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 6 49 7 49	1024 2048 4096 8192 16384 512 256 128	3 3 3 3 3 3 3	0.024 0.024 0.024 0.024 0.024 0.024 0.024 0.050	1.062 1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26 11.32	6.99 6.99 6.99 6.99 6.99 6.99 14.56	2.12 3.00 4.25 6.00 8.49 1.50 1.06	0.011 0.016 0.018 0.019 0.020 0.002 -0.017 -0.010
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 6 49 7 49 8 49	1024 2048 4096 8192 16384 512 256 128 256	3 3 3 3 3 3 3 3	0.024 0.024 0.024 0.024 0.024 0.024 0.050 0.050	1.062 1.062 1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26 11.32 22.66	6.99 6.99 6.99 6.99 6.99 6.99 14.56	2.12 3.00 4.25 6.00 8.49 1.50 1.06 1.56 2.21	0.011 0.016 0.018 0.019 0.020 0.002 -0.017 -0.010 0.028
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 6 49 7 49 8 49 9 49	1024 2048 4096 8192 16384 512 256 128 256 64	3 3 3 3 3 3 3 3 3	0.024 0.024 0.024 0.024 0.024 0.024 0.050 0.050	1.062 1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26 11.32	6.99 6.99 6.99 6.99 6.99 6.99 14.56	2.12 3.00 4.25 6.00 8.49 1.50 1.06	0.011 0.016 0.018 0.019 0.020 0.002 -0.017 -0.010
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 6 49 7 49 8 49 9 49 Ts diffe	1024 2048 4096 8192 16384 512 256 128 256 64 rence fi	3 3 3 3 3 3 3 3 3	0.024 0.024 0.024 0.024 0.024 0.024 0.050 0.050 0.050 model	1.062 1.062 1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26 11.32 22.66 5.86	6.99 6.99 6.99 6.99 6.99 6.99 14.56 14.56	2.12 3.00 4.25 6.00 8.49 1.50 1.06 1.56 2.21	0.011 0.016 0.018 0.019 0.020 0.002 -0.017 -0.010 0.028 -0.086
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 7 49 8 49 9 49 Ts differmodel	1024 2048 4096 8192 16384 512 256 128 256 64 rence fr	3 3 3 3 3 3 3 3 3 3 3	0.024 0.024 0.024 0.024 0.024 0.024 0.050 0.050 0.050 model	1.062 1.062 1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 4 3	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26 11.32 22.66 5.86	6.99 6.99 6.99 6.99 6.99 6.99 14.56 14.56	2.12 3.00 4.25 6.00 8.49 1.50 1.06 1.56 2.21 1.11	0.011 0.016 0.018 0.019 0.020 0.002 -0.017 -0.010 0.028 -0.086
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 7 49 8 49 9 49 Ts differ model MAR	1024 2048 4096 8192 16384 512 256 128 256 64 rence fi	3 3 3 3 3 3 3 3 3 0 0	0.024 0.024 0.024 0.024 0.024 0.024 0.050 0.050 0.050 model 1	1.062 1.062 1.062 1.062 1.062 1.062 1.062 1.062 1.062	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 4 3 4 000 0.000	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26 11.32 22.66 5.86	6.99 6.99 6.99 6.99 6.99 14.56 14.56 14.56	2.12 3.00 4.25 6.00 8.49 1.50 1.06 1.56 2.21 1.11	0.011 0.016 0.018 0.019 0.020 0.002 -0.017 -0.010 0.028 -0.086
i nlay 0 49 1 49 2 49 3 49 4 49 5 49 7 49 8 49 9 49 Ts differmodel	1024 2048 4096 8192 16384 512 256 128 256 64 rence fi	3 3 3 3 3 3 3 3 3 0 	0.024 0.024 0.024 0.024 0.024 0.024 0.050 0.050 0.050 model 1 001 0.	1.062 1.062 1.062 1.062 1.062 1.062 1.062 1.062 1.062 2 001 0.000 -0.0	1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 1.00e-05 4 3 4 000 0.000	1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07 1.00e-07	41.69 83.94 165.52 333.64 672.40 20.81 10.26 11.32 22.66 5.86	6.99 6.99 6.99 6.99 6.99 14.56 14.56 14.56	2.12 3.00 4.25 6.00 8.49 1.50 1.06 1.56 2.21 1.11 8 02 0.00	0.011 0.016 0.018 0.019 0.020 0.002 -0.017 -0.010 0.028 -0.086

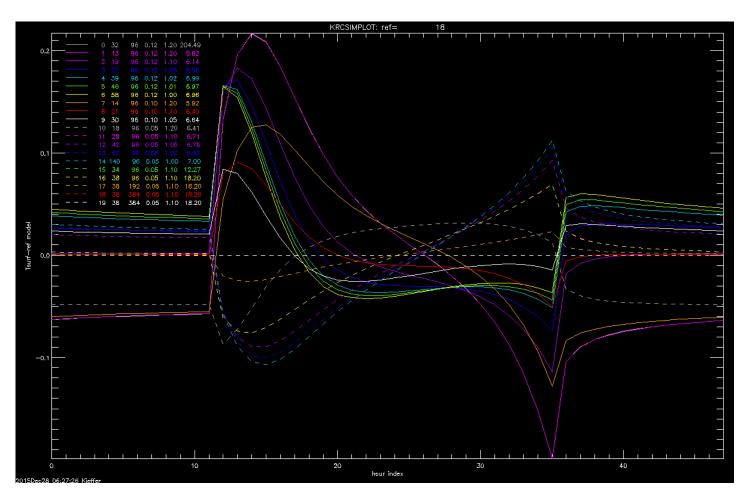


Figure 1: Last-season diurnal temperatures for model set L, relative to model L19. Legend linked to Table 1, see text. Models 0:6 all have flay=0.12 with decreasing rlay and similar depth; models 7:9 have flay=.10 . Models 11:19 (dashed lines) all have flay=0.05, 10:15 with decreasing rlay. Models 15:19 approach an ideal case by first increasing the total depth, then the time resolution and finally the convergence requirements. ksclotL18.png

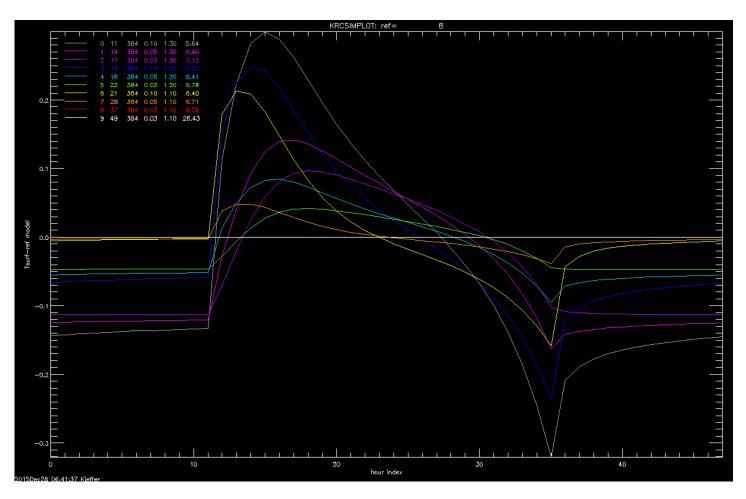


Figure 2: SIMPLE run M, all with 768 time/hour, relative to model 8. ksclotM8.png

## 2 KRC runs and comparisons

Generate idealised geometry matrix with circular orbit and zero obliquity. Use equator ( and  $\pm$  30 and 60 °). After first few runs, generate KRC version 3.2.3 by making these changes:

increase first layer for time doubling to 4 (third physical layer)

tday8.f, line 171, change J.GT.2 to J.GT.3

set FLAY to be the first physical layer. This is just for convenience of the user.

Change the default to 0.1 for better accuracy.

Add total depth to printout.

Printout of layers for time doubling: increase the format items

If TDAY(1) detects an error, go to the next case rather than stopping the run.

Did all these changes between Run E and F. Runs:

1102592 Dec 12 16:16 MarsCirA.t52

14327552 Dec 19 16:56 MarsCirB.t52

23144192 Dec 21 18:55 MarsCirC.t52

14327552 Dec 23 05:22 MarsCirD.t52

11021312 Dec 23 09:20 MarsCirE.t52

Generate version KRC 3.2.3 with associated changes to FLAY making MarsCirF.t52. Cases (0-based) 0:1 has slightly different input. Cases 2:9 had MAR delta-Ts of 3.e-7, max was 2.e-6

 $\begin{array}{c} 11021312~{\rm Dec}~24~10:23~{\rm MarsCirF.t52}\\ 12271232~{\rm Dec}~25~18:05~{\rm MarsCirG.t52}\\ 23144192~{\rm Dec}~26~07:03~{\rm MarsCirH.t52}\\ 1339136~{\rm Dec}~26~21:56~{\rm MarsCirX.t52}\\ \end{array}$ 

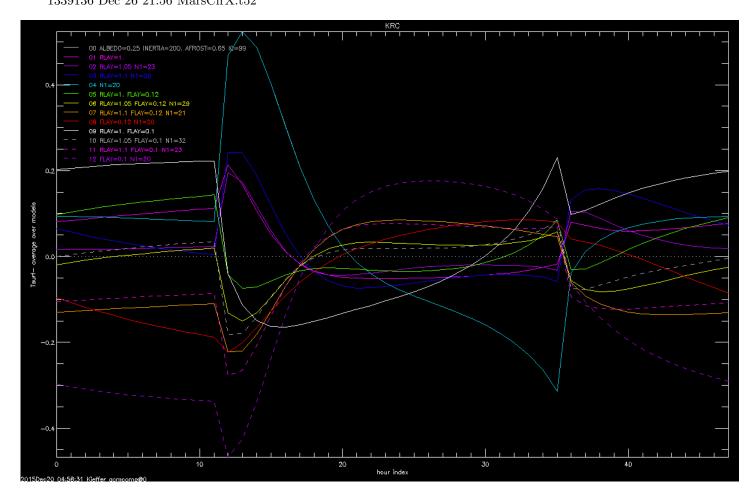


Figure 3: KRC run with circular orbit, zero obliquity and at equator; 13 models of different RLAY and FLAY; initial values are 1.2 and 0.18. N1 mostly set to yield total depth near 7.5 skin depths; exceptions are case 0 very deep, 4 about 32, 8 is 23 and 13 is 18. All use N2=4608, or 96 times each 1/2 hour. Case 10 should be the most accurate. krcCirB.png

KRC MarsCirC run, starting with case 3 has first physical layer of 0.100 to match SIMPLE runs. MarsCirC vers L:19; sets differing only in depth at about 6,12 and 16 diurnal skim depths are virtually the same. 5,11 and 17 have time-steps per  $\frac{1}{2}$  hour

of 96, 32 and 16 respectively and rlay=1.1 . Cases 8,14 and 20 have the same set of time-steps but rlay=1.2. Closest match to SIMPLE L:19 is rlay=1.1 and 32 time steps, see Fig. 4.

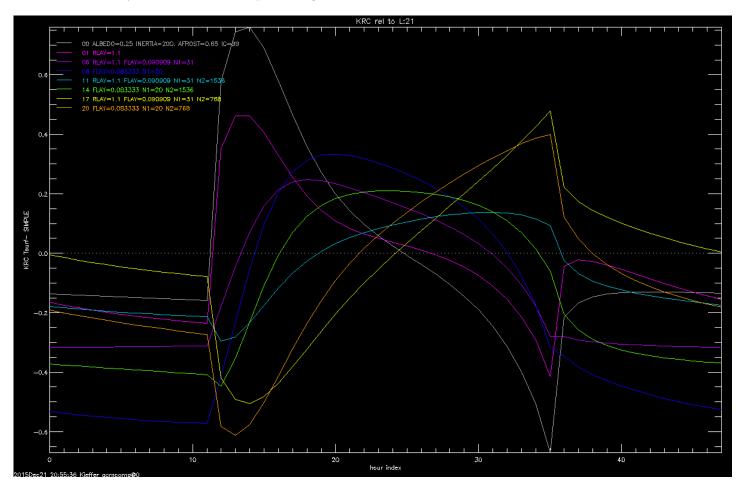


Figure 4: KRC run C with flay set so that top physical layer is 0.1. Depths of 8,12 and 18 indistinguishable. krcCirC.png

KRC run D. Cases 1:6 have 50 uniform layers of 0.1 to total 4.9 D; cases 7:12 have Rlay=1.2 with first physical layer 0.10, 18 layers to 10.5 D, which executed 3 times faster. Each set of 6 had standard convergence, then individually DDT/10, GGT/10, DTMAX/10, add DDT/10, add GGT/10. Virtually no difference between the 6 cases of either set, see Fig. 5. The last case has CONVF increased from 2 to 32, moving first time doubling from 2 to 7 and increasing run time by 27%. Relative to SIMPLE L:19, first 6 range -0.13 K (dusk) to +0.13 (after sunrise); second 6 -0.55 (dawn) to +0.35 (noon). Last case similar to first six, suggesting that KRC standard CONVG is too small.

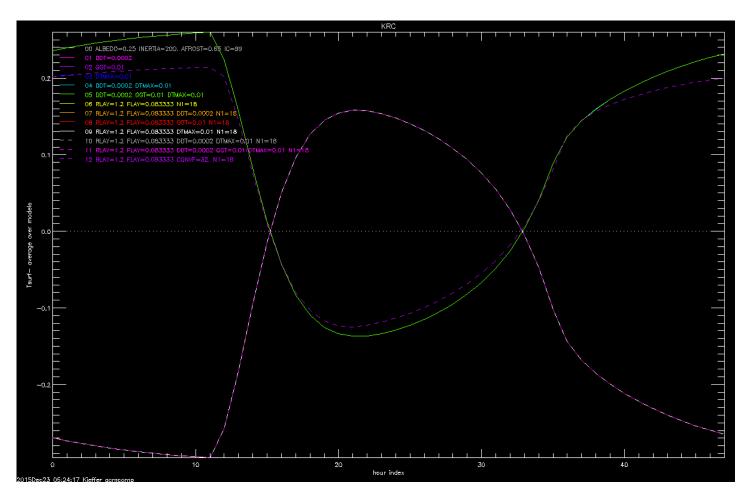


Figure 5: KRC run D relative to SIMPLE L:19; variation with changes of DDT, GGT and DTMAX are indistinguishable as only the last curve of sets 0:5 and 6:11 are visible. Setting CONVFG high, which lessens the time doubling, has an effect. krcCirD.png

KRC run E. All with 18432 time-steps/sol, or 384 each 1/2 hour, and depths of about 7. Matrix of RLAY=1.3, 1.2, 1.1 and first physical layer of 0.1, 0.05, and 0.025. Preceded by one case with NLAY=50, rlay=1.1. First 4 cases started time doubling at layer 2, then layer 4 or more. Results relative to SIMPLE L19 shown in Fig. 6; all relative maxima are in the morning and minima at night. Larger RLAY move relative maximum later in the day and increases value by about 0.1 K. Larger FLAY increases Tmax by 0.,05,.15.

For first physical layer 0.025, rlay=1.1, depth of 8.2, n/h of 384, first time-doubling layer or 13, KRC -SIMPLE has MAR of 0.017 K, mean diff is -.009 K with StdDev=0.017 K.

For KRC with RLAY=1.2 and topLay=0.1, MAR=0.154, mean =-0.059, StdDev=0.156; so this is adequate for 0.2K accuracy.

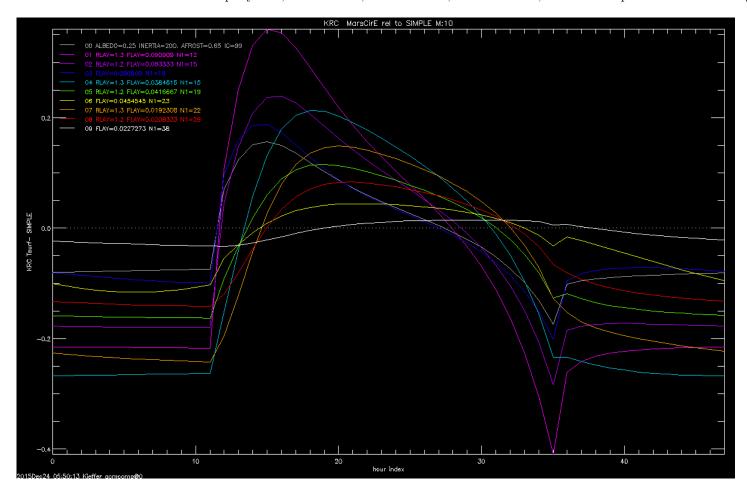


Figure 6: KRC run E relative to SIMPLE L:18; all with N2=18432 or 384 per 1/2 hour, CONVF=8., RLAY=1.1, FLAY=0.0769. Matrix of RLAY=1.3, 1.2, 1.1 and first physical layer of 0.1, 0.05, and 0.025. krcCirE.png

KRC run F. Apart from adjusting FLAY to the new convention, same input as run E. First case (0) differs because of flay, cases 1:3 have lower limit of time-doubling starting with 3. Cases 4:9 differences from Run E are less than 7.5e-7 K. See Fig. 7

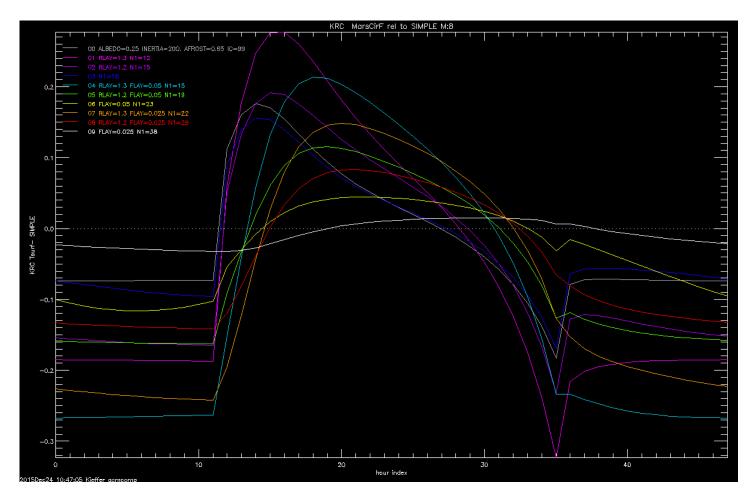


Figure 7: KRC run E relative to SIMPLE M:8; all with N2=18432 or 384 per 1/2 hour, CONVF=8., Matrix of RLAY=1.3, 1.2, 1.1 and first physical layer of 0.1, 0.05, and 0.025. krcCirF.png

Run G, several sets of 10 cases, first for each is NLAY=20 (very first is 50), then then 3x3 matrix of flay and rlay. Set 1 is N2=24576 (512 per 1/2hour), convg=8; then 256, convg=4; then 128, convg=2; then 64, convg=1, then 31 and then 16 per 1/2hour

Run H, similar to G, with some additional fine cases; results shown in Fig. 8 and 9. Making the convergence requirement about 3 significantly improves accuracy with little increase in run-time.

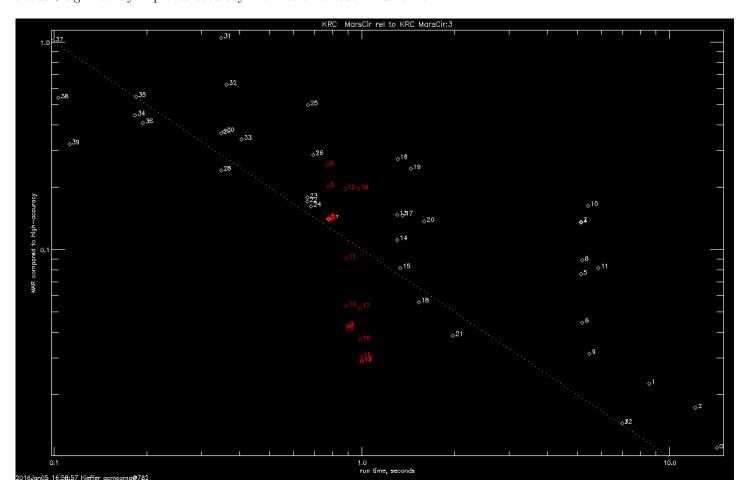


Figure 8: Abscissa: execution time for one latitude in seconds. Ordinate: accuracy for cases in Table 4 as the MAR relative to case 3 in run X, which is at KRC limits for resolution; shown in white. In each of the 6 groups with similar run times, RLAY decreases most rapidly with index, then FLAY. The dotted line indicates MAR=0.1/time in K/s . Shown in red are the results for Run I, which corresponds to H:27 except for NLAY and CONVG. marHI.png

Run I: all with RLAY=1.1, FLAY=0.05 and N2=6144.; set of decreasing number of layers from 30 to 22. Three sets, with CONVG 2,4 and 8; if adequately deep (D=5.), MAR is .140, .042, and 0.029 respectively. Increase in error less than factor of 2 if NLAY=24 or more; D=3.98.

Run J: same style as I, but FLAY=0.1 and N2=1536, then 768; NLAY 21 to 18. All 768 had MAR 0.15 or more. with N2=1536, if CONVG 3 or more, MAR about 0.07; NLAY=20 (D=5.12) was optimum.

Newton iterations on surface power balance continue until the change in  $T_S$  is less than GGT.

DTM is the RMS of change in layer temperatures at midnight: =  $\sqrt{\sum_{1}^{N_1} \Delta T_{\text{midnight}}}/N1$ 

If DTM is less than DTMAX or if the fractional change in DTM over the prior day is less than DDT, the next day will be the last for the current season, unless DTM then increases or becomes greater than DTMAX.

Convergence results stored in .t52 files ares:

NDJ4, the number of days computed in each season, for each latitude

DTM4, DTM for each latitude

Run V: 2048 per hour, RLAY=1.062, FLAY=0.024, 50 layers and CONVF=8, with each of GGT, DDT, and DTMAX set to twice, 1/2 and 1/5 their normal values; MAR 1.e-13 at most. Setting CONVG=2 yielded MAR=0.11.

For run V, all DTM4 are 0 and all NDJ4 are 3.

Run V2 only decreased GGT by a factor of 10 between cases, covering 1.e-2 to 1.e-5. MAR, relative to the last, is 2.9e-07, 8.5e-10, 4.5e-14 and 0. Run times for the first two were 7 and 2% less than the last. All DTM4 are 0 and all NDJ4 are 3.

Table 4: Summary results for KRC run on MarsCirH.inp. Columns are: Tdel= difference in K at 7 Hours, MAR= Mean Absolute Residual in K, Deep= scaled depth to the bottom of physical layers; Scong= Convergence safety factor for top physical layer; secs= execution time in seconds for one latitude; RLAY= layer thickness geometric ratio; FLAY= top physical layer in diurnal skin depths; CVG= convergence safety factor; Nlay= number of layers, including the virtual; N2= time-steps per sol. Last partial column in time-steps per Hour (1/24 of a sol)

i	RLAY	FLAY	CVG	NLAY	Ntime	Deep	Sconv	secs	MAR	Tdel
0	1.062	0.024	8.00	50	98304	6.99	9.01	14.22	0.000	0.00
1	1.062	0.024	8.00	50	49152	6.99	4.51	8.56	0.012	-0.02
2	1.100	0.025	8.00	37	98304	7.48	9.78	12.12	0.026	0.01
	1.100	0.025	8.00	37	49152	7.48	4.89	7.00	0.016	-0.02
4	1.300	0.100	8.00	13	49152	7.43	78.22	5.14	0.146	0.28
5	1.200	0.100	8.00	16	49152	7.20	78.22	5.14	0.087	0.22
6	1.100	0.100	8.00	23	49152	7.14	78.22	5.20	0.055	0.18
7	1.300	0.050	8.00	16	49152	8.36	19.56	5.14	0.145	0.03
8	1.200	0.050	8.00	20	49152	7.74	19.56	5.19	0.099	0.05
9	1.100	0.050	8.00	30	49152	7.43	19.56	5.48	0.042	0.06
10	1.300	0.025	8.00	18	49152	7.13	4.89	5.42	0.172	0.00
	1.200	0.025	8.00	24	49152	8.16	4.89	5.86	0.089	-0.02
	1.100	0.025	8.00	37	49152	7.48	4.89	6.99	0.016	-0.02
	1.300	0.100	4.00	13	12288	7.43	19.56	1.30	0.158	0.21
	1.200	0.100	4.00	16	12288	7.20	19.56	1.30	0.122	0.12
15	1.100	0.100	4.00	23	12288	7.14	19.56	1.33	0.092	0.12
	1.300	0.050	4.00	16	12288	8.36	4.89	1.30	0.283	-0.02
17	1.200	0.050	4.00	20	12288	7.74	4.89	1.36	0.155	-0.02
	1.100	0.050	4.00	30	12288	7.43	4.89	1.53	0.064	-0.00
19	1.300	0.025	4.00	18	12288	7.13	1.22	1.44	0.253	-0.10
20	1.200	0.025	4.00	24	12288	8.16	1.22	1.59	0.141	-0.13
21	1.100	0.025	4.00	37	12288	7.48	1.22	1.97	0.037	-0.08
22	1.300	0.100	2.00	13	6144	7.43	9.78	0.66	0.181	0.12
23	1.200	0.100	2.00	16	6144	7.20	9.78	0.66	0.186	-0.03
24	1.100	0.100	2.00	23	6144	7.14	9.78	0.68	0.170	0.00
25	1.300	0.050	2.00	16	6144	8.36	2.44	0.67	0.507	-0.17
26	1.200	0.050	2.00	20	6144	7.74	2.44	0.69	0.294	-0.13
27	1.100	0.050	2.00	30	6144	7.43	2.44	0.78	0.147	-0.08
28	1.300	0.100	1.00	13	3072	7.43	4.89	0.35	0.249	-0.07
29	1.200	0.100	1.00	16	3072	7.20	4.89	0.35	0.369	-0.37
30	1.100	0.100	1.00	23	3072	7.14	4.89	0.36	0.377	-0.25
31	1.300	0.050	1.00	16	3072	8.36	1.22	0.35	1.056	-0.53
32	1.200	0.050	1.00	20	3072	7.74	1.22	0.36	0.631	-0.39
33	1.100	0.050	1.00	30	3072	7.43	1.22	0.41	0.346	-0.25
34	1.300	0.100	1.00	13	1536	7.43	2.44	0.18	0.448	-0.49
35	1.200	0.100	1.00	16	1536	7.20	2.44	0.18	0.552	-0.51
36	1.100	0.100	1.00	23	1536	7.14	2.44	0.19	0.415	-0.26
37	1.300	0.100	1.00	13	768	7.43	1.22	0.10	1.016	-1.19
38	1.200	0.100	1.00	16	768	7.20	1.22	0.10	0.540	-0.68
39	1.100	0.100	1.00	23	768	7.14	1.22	0.11	0.324	-0.65

Table 5: KRC runs E, F, I. See Table 4 caption

i RLAY	FLAY	CVG	NLAY	Ntime	Deep	Sconv	secs	MAR	Tdel	
E:9										
0 1.100	0.077	8.00	50	18432	81.32	17.36	10.15	0.076	0.18	
1 1.300	0.091	8.00	12	18432	5.13	24.24	9.26	0.199	0.36	
2 1.200	0.083	8.00	15	18432	4.93	20.37	9.35	0.147	0.24	
3 1.100	0.091	8.00	18	18432	3.69	24.24	9.73	0.083	0.21	
4 1.300	0.038	8.00	15	18432	4.92	4.34	9.77	0.185	0.09	
5 1.200	0.042	8.00	19	18432	5.34	5.09	10.43	0.102	0.05	
6 1.100	0.045	8.00	23	18432	3.25	6.06	12.02	0.045	0.02	
7 1.300	0.019	8.00	22	18432	15.77	1.08	11.11	0.144	-0.02	
8 1.200	0.021	8.00	29	18432	17.07	1.27	11.96	0.079	-0.01	
9 1.100	0.023	8.00	38	18432	7.50	1.52	15.55	0.000	0.00	
F:9										
i RLAY	FLAY		NLAY	Ntime	Deep	Sconv	secs	MAR	Tdel	
0 1.100	0.100	8.00	50	18432	105.72	29.33	10.38	0.074	0.20	
1 1.300	0.100	8.00	12	18432	5.64	29.33	9.91	0.162	0.27	
2 1.200	0.100	8.00	15	18432	5.92	29.33	9.94	0.120	0.20	
3 1.100	0.100	8.00	18	18432	4.05	29.33	10.24	0.070	0.18	
4 1.300	0.050	8.00	15	18432	6.40	7.33	10.03	0.185	0.09	
5 1.200	0.050	8.00	19	18432	6.41	7.33	10.70	0.102	0.05	
6 1.100	0.050	8.00	23	18432	3.57	7.33	12.29	0.045	0.02	
7 1.300	0.025	8.00	22	18432	20.51	1.83	11.37	0.144	-0.02	
8 1.200	0.025	8.00	29	18432	20.48	1.83	12.23	0.079	-0.01	
9 1.100	0.025	8.00	38	18432	8.25	1.83	15.81	0.000	0.00	
I rel X:3	}									
i RLAY	FLAY	CVG	NLAY	Ntime	Deep	Sconv	secs	MAR	Tdel	
0 1.100	0.050	2.00	50	6144	52.86	2.44	0.79	0.140	-0.10	
1 1.100	0.050	2.00	30	6144	7.43	2.44	0.78	0.140	-0.10	
2 1.100	0.050	2.00	28	6144	6.06	2.44	0.78	0.140	-0.10	
3 1.100	0.050	2.00	26	6144	4.92	2.44	0.78	0.138	-0.10	
4 1.100	0.050	2.00	24	6144	3.98	2.44	0.78	0.145	-0.13	
5 1.100	0.050	2.00	22	6144	3.20	2.44	0.77	0.201	-0.08	
6 1.100	0.050	2.00	20	6144	2.56	2.44	0.77	0.256	0.31	
7 1.100	0.050	4.00	30	6144	7.43	2.44	0.90	0.043	-0.09	
8 1.100	0.050	4.00	28	6144	6.06	2.44	0.90	0.043	-0.09	
9 1.100	0.050	4.00	26	6144	4.92	2.44	0.89	0.041	-0.09	
10 1.100	0.050	4.00	24	6144	3.98	2.44	0.89	0.053	-0.12	
11 1.100	0.050	4.00	22	6144	3.20	2.44	0.89	0.091	-0.08	
12 1.100	0.050	4.00	20	6144	2.56	2.44	0.88	0.196	0.30	
13 1.100	0.050	8.00	30	6144	7.43	2.44	1.00	0.029	-0.05	
14 1.100	0.050	8.00	28	6144	6.06	2.44	1.00	0.029	-0.05	
15 1.100	0.050	8.00	26	6144	4.92	2.44	0.99	0.030	-0.05	
16 1.100	0.050	8.00	24	6144	3.98	2.44	0.99	0.037	-0.07	
17 1.100	0.050	8.00	22	6144	3.20	2.44	0.98	0.053	-0.03	
18 1.100	0.050	8.00	20	6144	2.56	2.44	0.97	0.196	0.34	

Table 6: KRC run G. See Table 4 caption

G:9									
i RLAY	FLAY	CVG	NLAY	Ntime	Deep	Sconv	secs	MAR	Tdel
0 1.050	0.090	8.00	50	24576	17.86	31.68	2.90	0.042	0.17
1 1.300	0.100	8.00	13	24576	7.43	39.11	2.58	0.152	0.28
2 1.200	0.100	8.00	16	24576	7.20	39.11	2.59	0.104	0.22
3 1.100	0.100	8.00	23	24576	7.14	39.11	2.64	0.066	0.20
4 1.300	0.050	8.00	16	24576	8.36	9.78	2.59	0.180	0.08
5 1.200	0.050	8.00	20	24576	7.74	9.78	2.69	0.092	0.07
6 1.100	0.050	8.00	30	24576	7.43	9.78	3.03	0.031	0.06
7 1.300	0.025	8.00	18	24576	7.13	2.44	2.87	0.155	0.00
8 1.200	0.025	8.00	24	24576	8.16	2.44	3.18	0.073	-0.02
9 1.100	0.025	8.00	37	24576	7.48	2.44	3.93	0.000	0.00
10 1.300	0.100	4.00	13	12288	7.43	19.56	1.30	0.160	0.24
11 1.200	0.100	4.00	16	12288	7.20	19.56	1.30	0.123	0.15
12 1.100	0.100	4.00	23	12288	7.14	19.56	1.33	0.094	0.15
13 1.300	0.050	4.00	16	12288	8.36	4.89	1.30	0.280	0.01
14 1.200	0.050	4.00	20	12288	7.74	4.89	1.35	0.152	0.01
15 1.100	0.050	4.00	30	12288	7.43	4.89	1.52	0.062	0.02
16 1.300	0.025	4.00	18	12288	7.13	1.22	1.44	0.249	-0.07
17 1.200	0.025	4.00	24	12288	8.16	1.22	1.60	0.135	-0.10
18 1.100	0.025	4.00	37	12288	7.48	1.22	1.98	0.026	-0.05
19 1.300	0.100	2.00	13	6144	7.43	9.78	0.66	0.181	0.15
20 1.200	0.100	2.00	16	6144	7.20	9.78	0.66	0.182	-0.00
21 1.100	0.100	2.00	23	6144	7.14	9.78	0.68	0.169	0.03
22 1.300	0.050	2.00	16	6144	8.36	2.44	0.67	0.504	-0.14
23 1.200	0.050	2.00	20	6144	7.74	2.44	0.69	0.290	-0.10
24 1.100	0.050	2.00	30	6144	7.43	2.44	0.78	0.142	-0.05
25 1.300	0.100	1.00	13	3072	7.43	4.89	0.35	0.246	-0.05
26 1.200		1.00	16	3072	7.20	4.89	0.35	0.361	-0.34
27 1.100	0.100	1.00	23	3072	7.14	4.89	0.36	0.372	-0.22
28 1.300	0.050	1.00	16	3072	8.36	1.22	0.35	1.052	-0.50
29 1.200	0.050	1.00	20	3072	7.74	1.22	0.36	0.625	-0.36
30 1.100	0.050	1.00	30	3072	7.43	1.22	0.41	0.340	-0.22
31 1.300	0.100	1.00	13	1536	7.43	2.44	0.18	0.441	-0.46
32 1.200	0.100	1.00	16	1536	7.20	2.44	0.18	0.545	-0.48
33 1.100	0.100	1.00	23	1536	7.14	2.44	0.19	0.409	-0.24
34 1.300	0.100	1.00	13	786	7.43	1.25	0.12	0.323	0.12
35 1.200		1.00	16	786	7.20	1.25	0.12	0.311	0.13
36 1.100	0.100	1.00	23	786	7.14	1.25	0.14	0.258	-0.07

Table 7: KRC runs J and X. See Table 4 caption

J rel X:3									
i RLAY	FLAY	CVG	NLAY	Ntime	Deep	Sconv	secs	MAR	Tdel
0 1.100	0.100	2.00	22	1536	6.40	2.44	0.21	0.122	-0.21
1 1.100	0.100	2.00	21	1536	5.73	2.44	0.21	0.122	-0.21
2 1.100	0.100	2.00	20	1536	5.12	2.44	0.21	0.121	-0.21
3 1.100	0.100	2.00	19	1536	4.56	2.44	0.21	0.120	-0.22
4 1.100	0.100	2.00	18	1536	4.05	2.44	0.21	0.128	-0.23
5 1.100	0.100	3.00	21	1536	5.73	2.44	0.22	0.072	-0.18
6 1.100	0.100	3.00	20	1536	5.12	2.44	0.23	0.072	-0.18
7 1.100	0.100	3.00	19	1536	4.56	2.44	0.22	0.073	-0.18
8 1.100	0.100	3.00	18	1536	4.05	2.44	0.22	0.083	-0.20
9 1.100	0.100	4.00	21	1536	5.73	2.44	0.24	0.067	-0.14
10 1.100	0.100	4.00	20	1536	5.12	2.44	0.24	0.068	-0.14
11 1.100	0.100	4.00	19	1536	4.56	2.44	0.24	0.071	-0.14
12 1.100	0.100	4.00	18	1536	4.05	2.44	0.23	0.077	-0.16
13 1.100	0.100	6.00	21	1536	5.73	2.44	0.25	0.066	-0.10
14 1.100	0.100	6.00	20	1536	5.12	2.44	0.25	0.067	-0.10
15 1.100	0.100	6.00	19	1536	4.56	2.44	0.25	0.070	-0.11
16 1.100	0.100	6.00	18	1536	4.05	2.44	0.25	0.070	-0.13
17 1.100	0.100	2.00	21	768	5.73	1.22	0.13	0.171	-0.48
18 1.100	0.100	2.00	20	768	5.12	1.22	0.13	0.171	-0.48
19 1.100	0.100	2.00	19	768	4.56	1.22	0.13	0.174	-0.49
20 1.100	0.100	2.00	18	768	4.05	1.22	0.13	0.182	-0.51
21 1.100	0.100	3.00	21	768	5.73	1.22	0.13	0.158	-0.42
22 1.100	0.100	3.00	20	768	5.12	1.22	0.13	0.159	-0.42
23 1.100	0.100	3.00	19	768	4.56	1.22	0.13	0.162	-0.42
24 1.100	0.100	3.00	18	768	4.05	1.22	0.13	0.163	-0.44
25 1.100	0.100	4.00	21	768	5.73	1.22	0.14	0.153	-0.40
26 1.100	0.100	4.00	20	768	5.12	1.22	0.14	0.154	-0.40
27 1.100	0.100	4.00	19	768	4.56	1.22	0.14	0.157	-0.41
28 1.100	0.100	4.00	18	768	4.05	1.22	0.14	0.158	-0.43
29 1.100	0.100	6.00	21	768	5.73	1.22	0.15	0.148	-0.40
30 1.100	0.100	6.00	20	768	5.12	1.22	0.14	0.149	-0.40
31 1.100	0.100	6.00	19	768	4.56	1.22	0.14	0.152	-0.40
32 1.100	0.100	6.00	18	768	4.05	1.22	0.14	0.152	-0.42
X:3									
i RLAY	FLAY	CVC	NLAY	Ntimo	Deep	Sconv	5065	MAR	Tdel
0 1.062	0.024	8.00	50	Ntime 98304	Беер 6.99	9.01	secs 14.24	0.011	-0.02
1 1.062	0.024	8.00	50	49152	6.99	4.51	8.56	0.011	-0.02 -0.04
2 1.062	0.024	8.00		196608	6.99	18.02	24.03	0.023	-0.04
3 1.062	0.024	8.00		393216	6.99	36.04	44.22	0.003	0.00
4 1.100	0.024	8.00	37	49152	7.48	4.89	7.00	0.000	-0.04
5 1.100	0.025	8.00	40	49152	10.04	4.89	7.00	0.014	-0.04
5 1.100	0.025	0.00	40	49102	10.04	4.09	1.00	0.014	0.04

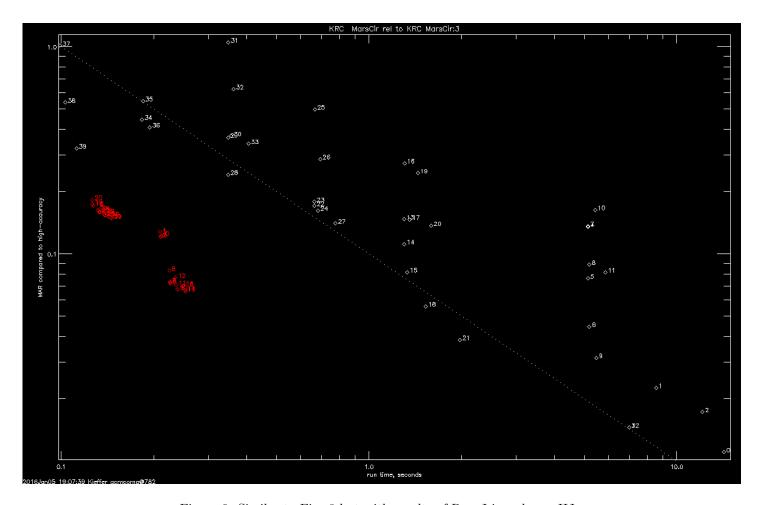


Figure 9: Similar to Fig. 8 but with results of Run J in red. marHJ.png

Table 8: KRC run x

---

#### 2.0.2 Long runs

KRC run X; MarsCirX.inp, all 2048/hour up to 16384/hour.

To obtain 0.01 K accuracy takes about 15 seconds

The succession of increasing the number of time steps by a factor of 2 shown in Fig. 10 suggests that the finest used, case 3, is within 0.002 K of limit. A corrollary is that with 2048 times per hour, Case 1, the MAD from the limit is about .025 K. Case 4 and 5, which differ only in depth, hav a mean absolute difference (MAD) of 1.e-5 K. Case 1 (blue) and 4 (purple) are similar except to RLAY being 1.062 and 1.1 and have a MAD of .025 K.

SIMPLE X.sav: layer to match KRC X, with n per 1/2 hour of 256 to 16384, and 64 to 256 with flay=0.05

Largest difference in cases in common with KRC X is 0.008 K

For 2048 to 16384 per 1/2 hour, KRC is about 10 times faster than SIMPLE with mset=3.

Direct comparison of KRC and SIMPLE, both run with small timesteps and layers, is shown in Figure 12. It is clear that the limit of finer time-steps in SIMPLE would have a MAR close to the 0.032 K; the shape looks like KRC has slightly lower thermal inertia.

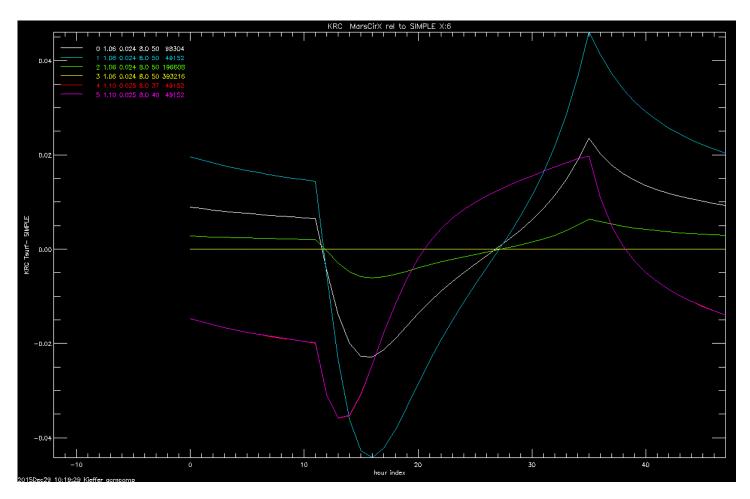


Figure 10: KRC MarsCir run X surface temperatures relatives to SIMPLE run X case 6 ??MORE g781X3.png

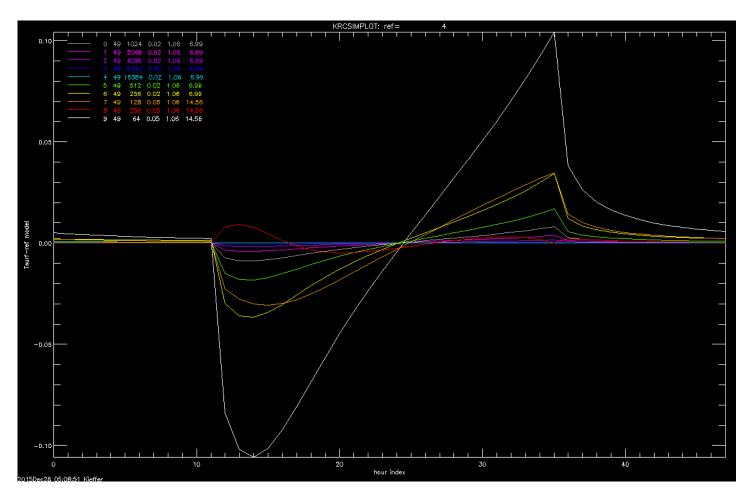


Figure 11: SIMPLE run X, matching the finest time-steps of KRC. All models have 49 physical layers, corresponding to maximum of KRC, a total depth of 6.99 D, and rlay=1.06, matching KRC run X. Models 0 to 6 have time steps of 512 to 32768 per Hour. Models 8:9 have flay=0.05 (and are deeper, which matters little). See Fig. ?? ksclotX4.png

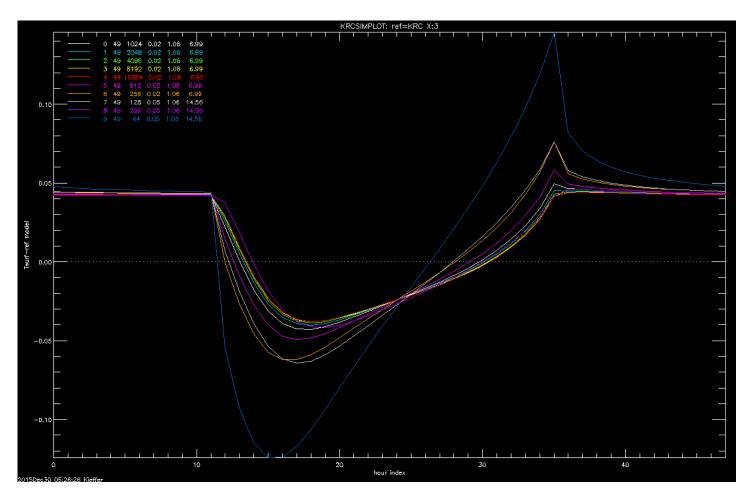


Figure 12: SIMPLE run X relative to KRC run X case 3 (n2=max allowed). Model 4 (red) had the same conditions as case 3 but MAR is .032; shape looks like KRC has slightly lower thermal inertia. ksclotXmKRCX3.png

## 3 Theory for thick slab

#### 3.1 Summary

Had the concept that a "quenched slab" model could forecast the convergence temperture for layers below the annual skindepth. Developed and tested this (early Jan 2016) but found that the existing KRC asymptotic exponential prediction (EPRED) algorithm did a better job.

#### 3.2 Introduction

For real planets with eccentric orbits and obliquity, multi-year runs are required to address the lower boundary. No practical way to set the lower boundary exactly, and the numerical approach can be slow.

However, ignoring both the diurnal and annual variation, the approach of the lower (insulating) boundary to equilibrium is similar to the problem of quenching a thick slab, that is, start with a slab of thickness 2l of uniform temperature  $T_0$  (the KRC initial T) and force both boundaries to a different (and unknown) ultimate lower boundary average. Without loss of generality; the ultimate temperature can be taken as 0.

There is an analytic solution for slab quenching which I will call  $S(\eta, \tau)$  where the dimensionless variables are  $\eta = x/L$  where x is distance from the "surface" and L is the slab [half] thickness, and  $\tau = \kappa t/L^2$  where  $\kappa$  is the diffusivity and t is time. S predicts the normalized temperature at a location X from the center of the slab that started a T=1 and is boundary-quenched to T=0 at t=0. The slab center is the location of no heat flow and thus corresponds to the bottom of a IB=0 KRC model. For a KRC run with NRSET < N3 and IB=0, the time of quenching is effectively the last layer reset, which will happen one or more times during the first season of a run; for normal KRC runs quenching happens after sol 3.

The average [annual] of the lower layers will approach the surface temperature average only if the thermal properties are temperature independent and there is no heat flow; for a fixed geothermal heat flow  $H_g$ , the gradient of the average temperature will be  $H_g/k$ .

If T-constant properties and no geothermal heat flow, all layers and the surface should have the same annual-average temperature. In this case; after each few years one could offset the layer temperatures by  $\langle T_S \rangle - \langle T_i \rangle_a$  (this is done in KRCSIMPLE). Otherwise, need a forecast of the  $U_i$ , then ultimate value of  $\langle T_i \rangle_a$  if the model were to run forever. This forecast may be made though matching curve-shape of the S model to determine what fraction of the approach to  $U_i$  was accomplished in the prior N years of run.

Convenient units for using S are x as layer center depth from the bottom of the model in diurnal scale-heights (D), which requires that the  $\kappa t$  input be in units of SI/ $D^2$ , DIFFU \* 86400.\*PERIOD \* J5\*DELJUL / SCALE\*\*2 . Then S is the fraction of the way that T has changed between the starting (or last reset ??) time and the ultimate value:

$$T_t = T_0 + (1 - S_t)(T_U - T_0)$$
 or  $T_U = T_0 + (T_t - T_0)/(1 - S_t)$  or 
$$\Delta T \equiv T_U - T_t = (T_t - T_0)(\frac{1}{1 - S_t} - 1)$$
 eq: S1 (1)

where  $\Delta T$  is the perturbation to be applied to a layer.

If unsure of what to use for  $T_0$ , can try a two-point solution of:  $1 - S_i = (T_i - T_0)/(T_U - T_0)$ . Change variable to  $Q = T_U - T_0$  yielding

$$Q = (S_2 - S_s)/(T_2 - T_1)$$
 and  $T_0 = T_1 - (1 - S_1)Q$  eq: S2 (2)

$$T_U = T_0 + Q$$
 and  $\Delta T \equiv T_U - T_2$  eq: S3

May need to estimate the annual mean temperature corresponding to the first season of the run. Do this by assuming that the offset (for each layer) between the annual mean and the first season remains virtually constant over the years. Test this by ... ?? NOPE

#### 3.3 Approach

KRC saves the maximum and minimum diurnal temperature for all physical layers at the end of each season, as well as the midnight temperature. From these can easily derive a good estimate of the diurnal average temperature  $P_{i,k}$  where i is the layer index and k is the sol count (error negligable well below the diurnal skin depth D); and the annual average  $Y_{i,y}$  where y is the year count.

For the moment ignoring the jump perturbation KRC normally makes during the first season, the annual layer temperatures after a few years and a few more years.

Input values to the S model (effectively  $\eta$  and  $\tau$ ) can be computed from the KRC parameters and the season index.

There is no point in adjusting the temperature for layers shallower than a few annual skin-depths

Using diurnal (Tmin+Tmax)/2 as an average temperature may be poor until below several (5 ?) skin-depths. Because temperature near Tmax are brief compared to those near Tmin, this "average" is expected to decrease with increasing depth until deep enough into the soil that the diurnal curve is virtually sinusoidal.

The 60S latitude without atmosphere is an extreme test in that the T range is about 100 to 240.

#### 3.4 The S model

Solutions found 2014mar9 in:

http://www.ewp.rpi.edu/hartford/~wallj2/CHT/Notes/ch05.pdf saved as /work2/Reprints/TherMod/Wallj2ch05.pdf

Similar treatment at found 2016jan12

http://www.ewp.rpi.edu/hartford/~ernesto/C\_Su2003/MMHCD/Notes/Notes\_pdf/s02.pdf

CJ:2.4-3 refers to Carslaw and Jaeger, Conduction of Heat in Solids, 2nd Edition: Section 2.4, equation 6.

Here assume constant thermal properties.

#### 3.4.1 The semi-infinite case

Mathmatically:

$$\frac{\partial T}{\partial t} = \kappa \frac{\partial^2 T}{\partial x}$$

With boundary conditions

$$T(x,0) = T_0$$
 and  $T(0,t) = 0$ 

Solution is

$$\frac{T(x,t)}{T_0} = \operatorname{erf}\left(\frac{x}{2\sqrt{\kappa t}}\right) \qquad \text{CJ}: 2.4 - 3 \qquad \text{eq}: \text{sic}$$
 (4)

where the error function erf, available as a function in IDL and Fortran, is:

$$\operatorname{erf}(z) = \frac{2}{\sqrt{\pi}} \int_0^z \exp\left(-\xi^2\right) d\xi$$

#### 3.4.2 The finite slab case

$$\frac{\partial T(x,t)}{\partial t} = \kappa \frac{\partial^2 T(x,t)}{\partial x}$$

Slab thickness L with boundary conditions

$$T(0,t) = T(L,t) = 0$$
 and  $T(x,0) = f(x)$ 

Solution ( $\S4.1$ , p.7) is

$$T(x,t) = \sum_{n=1}^{\infty} \left[ B_n \sin\left(\frac{n\pi x}{L}\right) \right] \exp\left(-\left(\frac{n\pi}{L}\right)^2 \kappa t\right)$$

where

$$B_n = \frac{2}{L} \int_0^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx$$

For the special case of  $f(x) = T_i = \text{constant}$ ,  $B_n = -T_i \frac{2(-1+(-1)^n)}{n\pi}$ . Alternate terms are 4 and 0, which yields

$$\frac{T(x,t)}{T_i} = \frac{4}{\pi} \sum_{n=0}^{\infty} \underbrace{\frac{1}{2n+1} \sin\left(\frac{(2n+1)\pi x}{L}\right)}_{fx} \underbrace{\exp\left(-\left(\frac{n\pi}{L}\right)^2 \kappa t\right)}_{ft}$$

Coded as IDL **slabdiffu** of L, vector of x and vector of  $\kappa t$ .

CJ 3.3-6 is for slab from 0 to l, initial temperature  $v = \text{constant } V_0$ , and boundaries held at 0. Solution must be symmetric around x = l/2

$$\frac{T(x,t)}{T_i} = \frac{4}{\pi} \sum_{n=0}^{\infty} \frac{1}{2n+1} \sin\left(\frac{(2n+1)\pi x}{2l}\right) \exp\left(-\left(\frac{(2n+1)\pi}{2l}\right)^2 \kappa t\right)$$
 CJ: 3.3 – 6

CJ 3.3-8 is for slab from -1 to +1 Solution must be symmetric around x = 0. CJ 3.4-2 is basically the same relation.

$$\frac{T(x,t)}{T_i} \equiv S = \frac{4}{\pi} \sum_{n=0}^{\infty} \underbrace{\frac{-1^n}{2n+1} \cos\left(\frac{(2n+1)\pi x}{2l}\right)}_{fx} \exp\left(-\left(\frac{(2n+1)\pi}{2l}\right)^2 \kappa t\right)$$
 CJ: 3.3 – 8 eq: Smod (5)

Using dimensionless parameters:

$$S = \frac{4}{\pi} \sum_{n=0}^{\infty} \underbrace{\frac{-1^n}{2n+1} \cos\left(\frac{(2n+1)\pi}{2}\eta\right)}_{fx} \exp\left(-\left(\frac{(2n+1)\pi}{2}\right)^2 \tau\right)$$

Within the summation, the initial factor and the sine or cosine term are of order unity; and the exp term decreases in magnitude with increaseing n. The summation error will be of order the last term in the exp factor;  $E \sim \exp\left(-\left(\frac{(2n+2)\pi}{L}\right)^2(\kappa t)_{\min}\right)$ . Treating E as a fractional tolerance; need  $n \geq \frac{L}{\pi}\sqrt{-\ln E/(\kappa t)_{\min}} - \frac{1}{2}$ 

#### **3.4.3** Beware

Slab are commonly defined as extending from -l to +l, or ) to L; which yield different equations.  $\label{lem:http://www-unix.ecs.umass.edu/~rlaurenc/Courses/che333/lectures/Heat%20Transfer/Lecture9.pdf$ 

gets a similar results ( using dimensionless variables), but then exp term has  $(2n+1)^2$  rather than  $n^2$ 

http://www-unix.ecs.umass.edu/~rlaurenc/Courses/che333/lectures/Heat%20Transfer/Lecture9.pdf

use a slab thickness of 2H. Page 14 also has in effect (2n+1) rather than n in the exp term.

#### 3.5 Extreme case: 6°S with no atmosphere

Several characteristics are shown in Figures 15, 16, 17, 14and 18.

The Slab model seems not as successful as the asymptotic exponential prediction algoritm used by KRC for prediction to the end of each season; see Fig. 13.

#### 3.6 Asymptotic exponential prediction: EPRED

tthmod @651 case and latitude set by pari[7] and 17 pari[21:22] set the first and last years for the pivot point, ; code will limit to safe values.

## 4 KRC runs with real eccentricity and obliquity

File names: input=Mars3.inp, print=MarsA.prt, and binary files =MarsA.pt52 and higher letters.

Real Mars geometry matrix, 40 season/year, N2=1536, CONVF=3. FLAY=0.1, RLAY=1.1, first case has N1=50. Spin-up for 2 years and un for 8 more, start save aft

Run A: as above

Run B: Rlay=1.125 to get deeper. N1 from 50 to 18 by 2's. Case 0 has bottom of 256.0 . Layer Tmin and Tmax stored only to number of hours (48) -2, so Case 2 with 46 layers and D=159.5 is the first for which the bottom layer is stored in the .t52 file; ffor this maximum range of lowest layer is  $\Delta T$ =0.004 K

yy=NUMGEOMLAY(46,flay=[.1,.07,.05],rlay=[1.1,1.11,1.12,1.125, 1.13, 1.14, 1.15])
ratio NUMGEOMLAY: NLAY= 46

```
NUMGEOMLAY: NLAY=
ratio
         0.1000 0.0700 0.0500
first=
         79.18 55.43 39.59
1.1000
1.1100
         109.62 76.73 54.81
         152.22 106.56
1.1200
                       76.11
         179.55 125.68 89.77
1.1250
1.1300
         211.88 148.32 105.94
         295.42 206.80 147.71
1.1400
1.1500
         412.39 288.67 206.19
```

Run C: Similar to run B but record all seasons. RLAY=1.14 Range in time is small, and many cases increase in time with less accuracy (difference from deepest model)!

Run D: Extend N5 to 640, 16 years. All N1 from 45 to 36, then even values to 28. KOMMON,KASE= 10000000 649152 RASE,MASE,MTOT= 15.404713 15 9737280

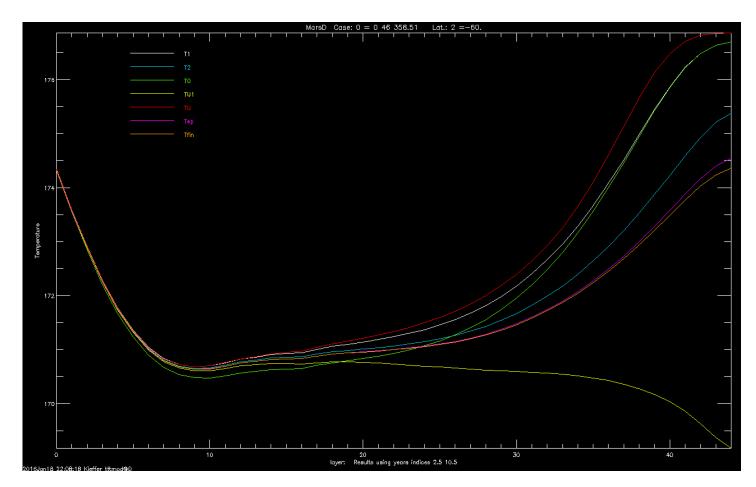


Figure 13: Forward predictions for layer temperatures for KRC run D, 60S no atm.. In legend: T1= annual mean temperature at time 1, year 2; T2= annual mean temperature at time 2, year 10; T0= initial temperature derived using 2-point S-model; TU1= ultimate temperature using 1-point S-model; TU= ultimate temperature using 2-point S-model; Tep= asymptotic exponential prediction to the last year using time 2 and the two years prior; Tfin= annual mean temperature for the last year of the KRC run, year 16. tm652.png

#### 4.1 Plot control in tttmod

kv3 reads the .t52 file and passes arrays to tttmod.

@640 Based on pari[13], calc diurnal average tave for: surface, one layer, or bottom.

pari[14] sets the reference case, negative means each case,

Pari[15] sets reference year. Form the diurnal average relative to the reference case, trel

pari[7:8] set the range of cases to be retained in trek and trf

Beginning 2016jan20, begin to convert all **ttmod** layer indicies for input, plots and print to be compatible with KRC, which is the 1-based number including the virtual layer. Thus in IDL code referring to the ddd array, which starts with the top physical layer, the values are 2 smaller. In the 3-column **ttmod** plot legends, the case is 0-based and the number of layers is the KRC NLAY; these values are stored in **nlac** in **ttmod** and the highest valid IDL layer index is 2 smaller.

@64 Clot Trel , and abs(trel) as log, for each latitude @643

640: get the diurnal Tave to be used

64: CLOT Secular relative temps for each lats REQ 640

641: CLOT tref REQ 64

642: CLOT all latitudes at once REQ 64

643: CLOT surf and bot end of year for all lats REQ 64

644: Many CLOTs one model

645: MAR for the last year

646: Secular layers for 1 lat and case

647: Layer variation for 1 lat and case REQ 646

648: Bottom temp trends REQ 783

649: Bottom temp trends all lats at once REQ 648 INCOMPLETE

65: S model

#### 652: S forecast for a run REQ 65 644

Using TTTMOD @113,123, which leads to @64 to show the diurnal average temperture through each year relative to that of the last year. See that there can be noise at the 0.005K level in Ts, especially for the deepest case; Fig. 21.

#### 4.2 Extreme case: 60°S with no atmosphere

Several characteristics are shown in Figures 15, 16, 17, 14 and 18.

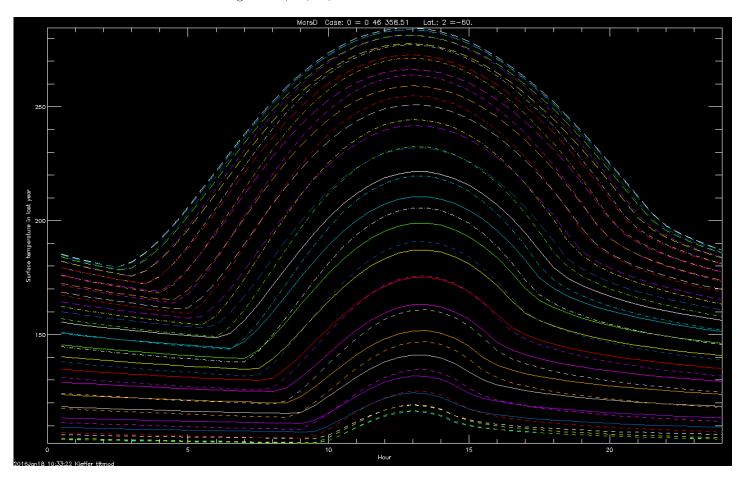


Figure 14: KRC run D, 60S no atm., diurnal surface temperature for each season of the last year. tm644h.png

For runs of 8 years, the annual and secular variation of the diurnal mean temperature are comparable at about 0.7K for total depths of about 154 D. To get to 0.2 K, need model depth of about 200 D and runs of 16 years.; see Fig 19.

The average annual temperature for the surface is within 0.1K by the eand of year 2; see Fig 20

The results for annual average are more regular than for using the last season of each year, Fig. 22. The model with total thickness 117 D have converged to within about 0.

Looking at the diurnal mean of the bottom layer for cases of different total depth for a situation with extreme seasonal variation, Fig. 19, secular trends are less than about 0.1k in 7 years for total depth of 101D, 10 years for 117D, and 13 years for 134D.

The seasonal variation of the mean diurnal temperature for the same depth is little effected by thaving additional deeper layers, see Fig. 24, although convergence is slowed.

Comparing Ts each year with that of the last year for each hour, lat, season of reference case 0, see that the mjor departures are related to different number of convergence days NDJ4. The time of day of maximum difference is not consistent, but can form the MAR over hours, and then over season, showing that surface temperature errors can be under 0.05K by using total depth of at least 100D and 3 years (spin-up of 2 years), see Figure 26.

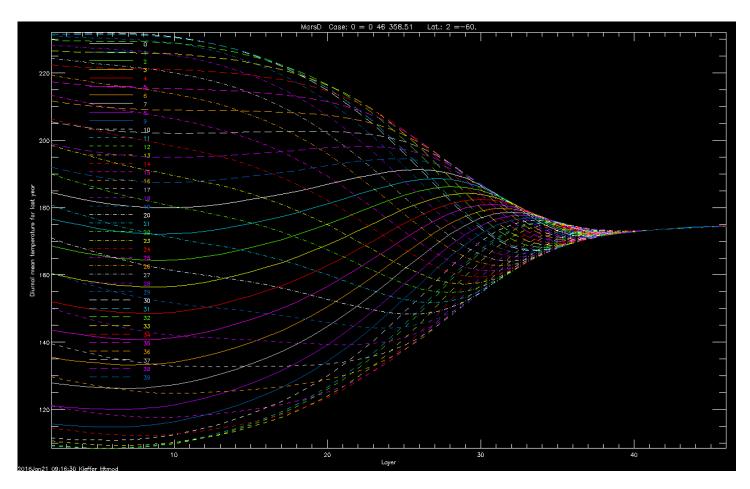


Figure 15: KRC run D, 60S no atm., Seasonal variation of the diurnal mean versus depth. Abscissa is physical layer 0-based index. Legend indicates season index. tm644s.png

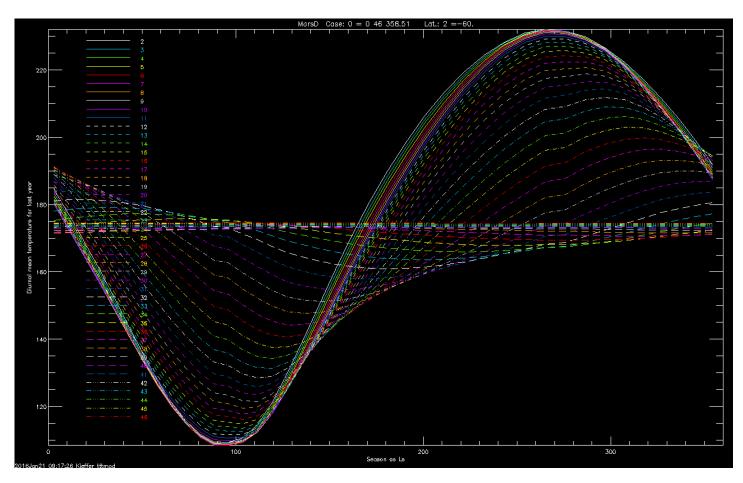


Figure 16: KRC run D, 60S no atm., Layer diurnal mean versus season. Legend indicates 1-based physical layer. tm644l.png

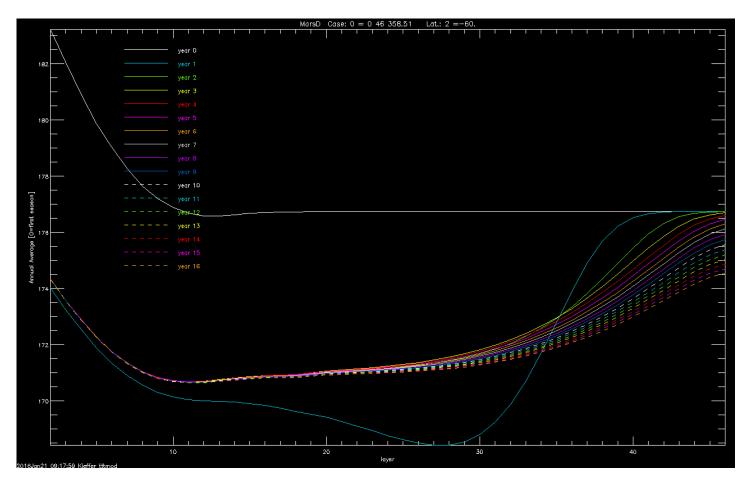


Figure 17: KRC run D, 60S no atm. showing average annual temperature versus depth for successive years. Year 0 is at the end of the first season, all others are at the end of the year. Abscissa is physical layer 0-based index. tm644a.png

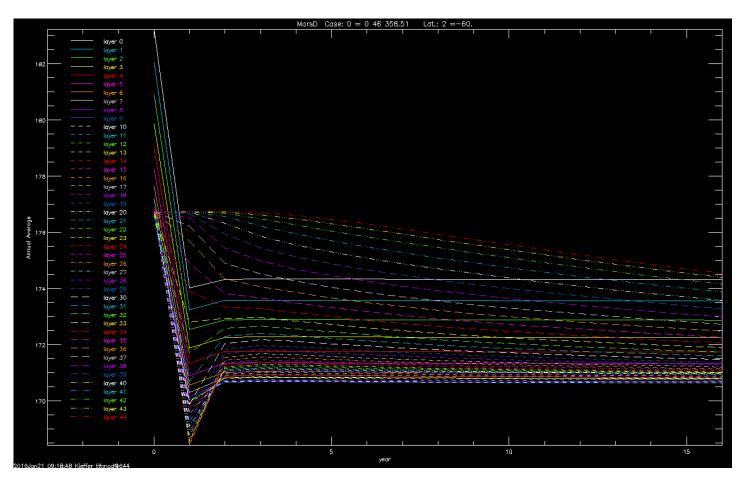


Figure 18: KRC run D, 60S no atm. showing average annual temperature versus time for each layer. Year 0 is at the end of the first season, all others are at the last season of the year. Layers shallower than about 25 show little variation after two years. tm644y.png

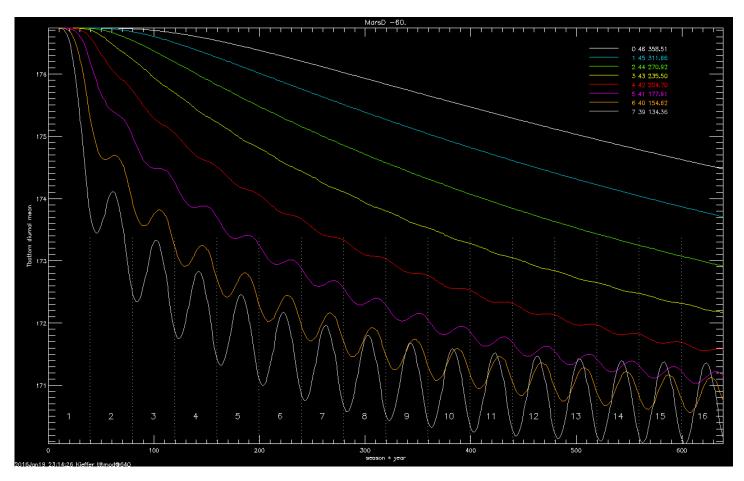


Figure 19: Diurnal mean temperature for the bottom layer for KRC run D 60S. The legend indicates the case index, the number of layers (physical +1) and the model total thickness in diurnal skin-depths. tm640D2bot.png

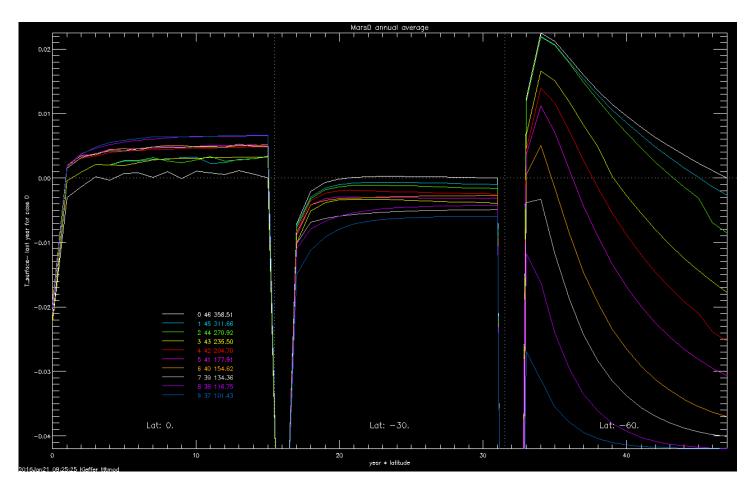


Figure 20: Annual average surface temperatures for each year and latitude relative to those for the last year of the run for Case 0 (very deep) tm643taD.png

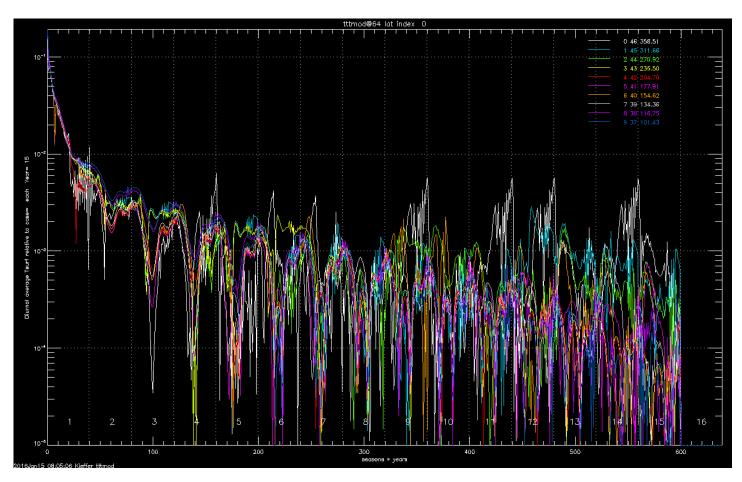


Figure 21: Diurnal average surface temperatures at the equator for each year relative to those over the last year of the run. The legend indicates the case index, the number of layers (physical +1) and the model total thickness in diurnal skin-depths. tm64bD0.png

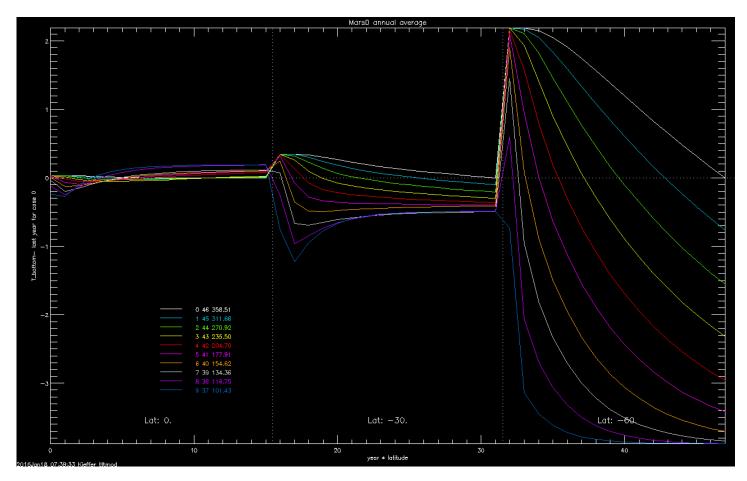


Figure 22: Annual average bottom temperatures for each year and latitude relative to those for the last year of the run for Case 0 (very deep) tm643baD.png

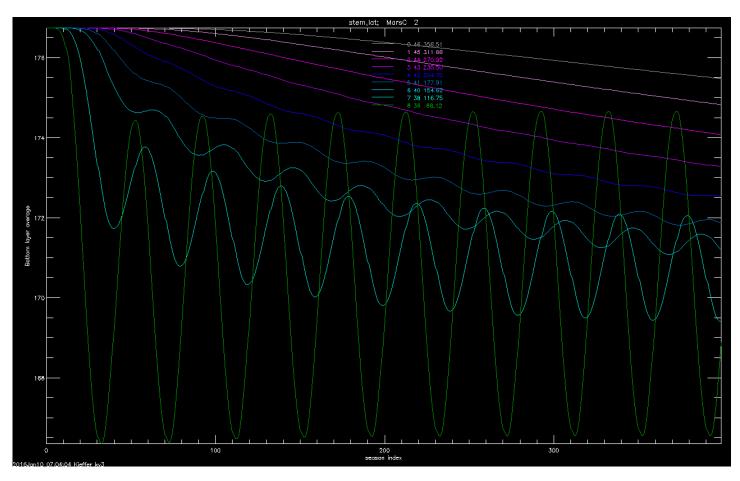


Figure 23: Average diurnal temperature  $((\min+\max)/2)$  of the lowest layers through all seasons and years. The annual oscillation magnitude is similar to the secular trend over years 5 to 10 (arbitrary) for a case with about 39 layers g785C2.png

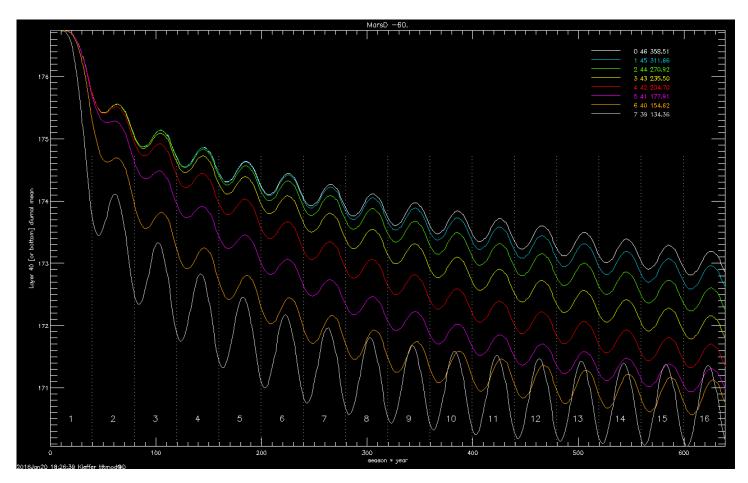


Figure 24: Seasonal variation of layer 40, 145 D, for 60S; this is the bottom layer for case 6 [orange]. Annual oscillation is slightly attenuated by having one additional layer, case 5 [purple] but little more with deeper layers. Bottom layer amplitude increases a factor of about 2 if there is one less total layer [gray]; however the annual average has hnearly converged in 16 years for case 7. tm640D2L40.png

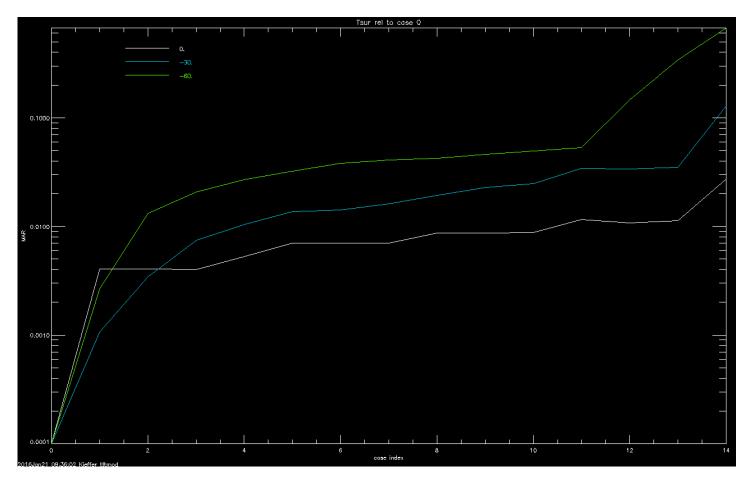


Figure 25: MAR of the Surface temperature (all hours, all seasons) in the last year relative to those of the last year of case 0 (very deep). tm645aD.png

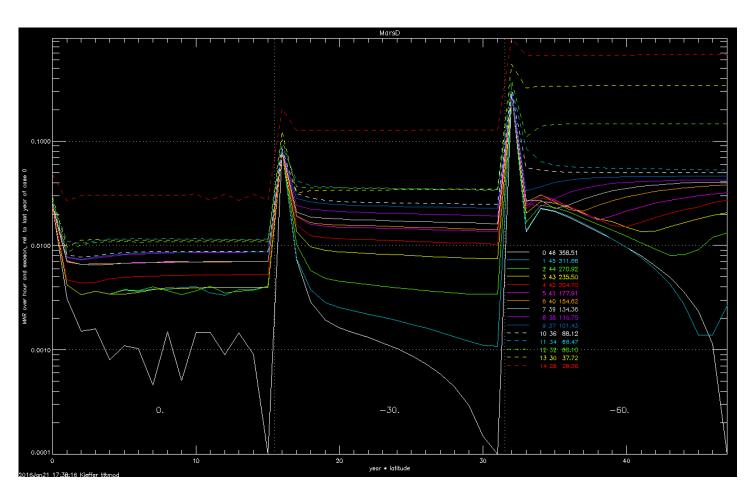


Figure 26: MAR of the surface temperature over hour and season for each year of KRC run D, relative to these temperatures for last year of case 0 (very deep). The year-to-year oscillation at the .005 K leve are related to differences in the number of integration days NDJ4. tm645yD.png

## 5 Accuracy estimates for Real bodies: start of a plan

Objective is to estimate numerical errors for real bodies and to develop recommendations for convergence parameters.

Primarily for surface temperatures, but include results for the bottom layer

With atmosphere for Mars, without for some eccentric-orbit asteroid Run both skip and soly versions homogeneous and layered with and without temperature dependence A few inertias Shallow and deep that bracket practical annual cases minimum and large annual variation (latitudes of 0,-30,-60)? a case that ignores annual wave? Practical results would be N2=384 \*[1,4,?]

Runs: skip / soly, Mars / Asteroid latitudes: Mars: 0,-30,-45. Asteroid: 0,30,60,-30, -60 But practically for soly runs can only have one latitude unless few years Cases: base case I=300 homogeneous Homogeneous: I=50,300,1800 Layers: 50 over 1800, IC=small and large N2= 384 and 1536

## 6 J. Spencer model

John Spencer made public a thermal model described in: A Rough-Surface Thermophysical Model for Airless Planets, Icarus, v. 83, ppp27-38, (1990).

Download tar from https://www.boulder.swri.edu/ $\sim$ spencer/thermprojrs/ into /home/hkieffer/krc/Spencer/thermprojrs/ . Copy the \*.pro into -/idl/other/ so that IDL can find them. Look at readme.txt Then do:

thermprojrs, tsurf, tod, rhel = 1.523712, alb = 0.2, rot = 1.0, emvty = 1., ti = 2.e5, ntinc = 6144

```
to get 128 time steps for each of 48 "hours".
```

```
Albedo= 0.20, Upper layer TI= 2.00e+05, Heat flow= 0.00e+00erg cm-2 s-1
Thermal conductivity= 2.67e+03 erg cm-1 s-1 K-1
Skindepth for upper layer = 1.564 cm
Theta= 1.089
Input C/R to continue :
Equilibrium temperatures: Peak= 302.29, Dark= 0.00
Maximum conductive stability criterion= 0.050
Maximum Radiative stability criterion = 0.009
```

Energy Conservation Report at end of each run:

	Mean	Mean	Total	Net Power	Mean	
	Power In	Power Out	Energy	Out	Surf.	Deep
Run	W m-2	W m-2	In/Out	W m-2	Temp.	Temp.
0	1.507e+02	1.507e+02	0.9999	-7.836e-03	214.00	213.75
1	1.507e+02	1.507e+02	1.0000	3.487e-04	214.01	213.79

Done in gcmcomp @ 7799. Found that I need to shift Spencer earlier by one hour to match. Compare to MarsCirG:24, which has same number of time steps. Spencer always warmer; MAR= 3.2; see Fig. 27. A quick look at the code did not see that any roughness parameters are involved.

#### 7 earlier studies

```
-/cr/InSight/HP3/Thermod.tex 2014 March
-/krc/Doc/thin.tex 2014 May
```

## A ERROR handling in v3.2.2

If TDAY(1) detects potential instability (convergence too small), it prints message to IOERR and sets IRET=2, finishes calculations and returns.

```
KRC finds IRD.NE.1, so calls TPRINT(2), writes error message to IOSP, (if disk open, calls TDISK(4) ) quits.
```

TDISK writes each case place, so cannot omit a case; need to set some flag in that case. Because t5x values stored in FFF, which is not re-zeroed with each file, it could contatin values toha look reasonable for a prior file in same KRC run. Thus, the safe thing to do would be to write the first season with null values for some flag.

Need to force J5=JDISK, this will set JOUT=0 [TDISK line 223] Can set NDJ4 all to zero as a flag for null season NDJ4(MAXN4E) is in latcom, MAXN4E = 38 Desire it to write a blank case to disk and go to next case!

If blowup occurs in TDAY(2), sets IRET=2, prints messages to IOSP, Calls TPRINT(7), TDISK (2,I) [if disk open), TPRINT(2), and returns.

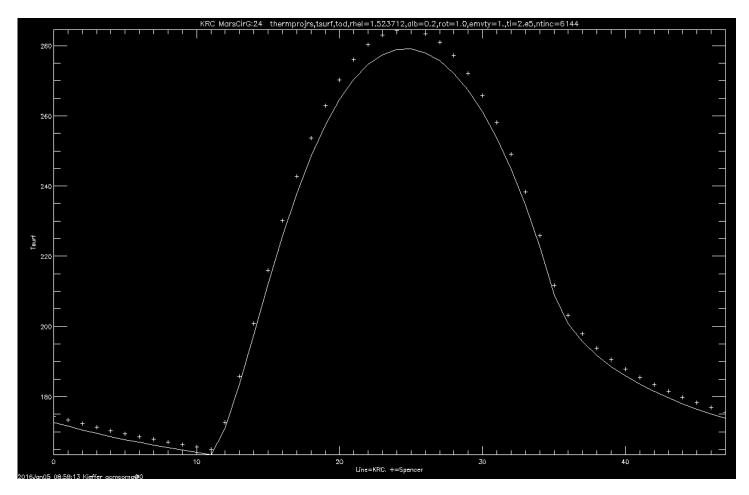


Figure 27: Spencer model run with inertia 200 SI and 256 timestep per hour, plus signs, compared to KRC run with the same number of time-steps, line. Spenc.png

TLATS then sets IRL=2 and returns
TSEAS will not do another season, and returns a 2
KRC finds IRS not 1, write error messages to IOPM and IOSP and proceeds to next case

#### A.1 TDISK and BINF5

#### Monitor::

```
Case 18 DTIME: total, user, system=
                                      3.0485
                                                3.0485
                                                         0.0000
                                         19 ====
======= RUN-CASE
                                    1
   0.370 seconds at start of season
                                     80 of
                                            640
   0.745 seconds at start of season
                                    160 of
                                            640
   1.121 seconds at start of season
                                    240 of
   1.497 seconds at start of season
                                    320 of
   1.872 seconds at start of season
                                    400 of
   2.248 seconds at start of season
                                    480 of
                                            640
   2.624 seconds at start of season 560 of
   3.000 seconds at start of season 640 of
   3.006 seconds at end of season 640 of 640
                 RBUF=0/ ========= end of job
Case 19 DTIME: total, user, system=
                                                         0.0000
                                      3.0055
                                                3.0055
BINF5: ARCH S= litend <
BINF5 2013jan02 called with ID=
                                         5
                                                    48
                                                                            3
                                                                                                  19
                                                                                     644
BINF5 error: W IRET, IERR=
                                              -5
ID=
             5
                                                3
                                                         644
                                                                      19
                                                                                  0
                                                                                              5
                        48
```

25

```
END KRC
               Total time [s] = 53.809822
---- looking inside binf5.F and /home/hkieffer/src/cnew/cisis/primio.c
 -4 is error from PIO_WT; -5 is
    (void) sprintf(errbuf, "Error writing %ld bytes at byte %ld to file %s",
                 (long) nbytes, (long) ibyte, fb->filnam);
 CALL PIO_CL (FID, 1, IECL) ! close and delete the binary file
 From Print file
 IDX= 4 JJJ=
              5 48
                       7 3 644 0 0
                                          5 25
                         336 1008
                                                             Ω
                                                                         0
              48
                                             645120
                10000000
 KOMMON, KASE=
                             649152
 RASE, MASE, MTOT= 15.404713
                                        15
                                               9737280
    2.683 seconds at end of season 640 of 640
BINF5 W IRET, IERR=
                                       -5
#####
KRCv3.2.3 RUN-CASE 1-18 2016 Jan 10 07:32:03 PAGE= 55
----- TYPE LOC VALUE ----- Parameter changes
Changed>> 2 1 20.00
                            NLAY N1
 Case 18 DTIME: total, user, system=
                                       3.0485
                                                 3.0485
                                                          0.0000
#####
   20
         1.2375
                   0.0402
                            8.2024
                                      0.2664
                                               458.380
                                                        5.850
                           8.8212
                                     0.2865
 Lower layer of time doubling: 5 7 10 12 15 17 20
    3.006 seconds at end of season 640 of 640
    END OF DATA ON INPUT UNIT
 Case 19 DTIME: total, user, system=
                                       3.0055
                                                 3.0055
                                                          0.0000
 JJJ=
                                      7
                                                                       19
                                                                                                5
                         48
                                                           644
                                                                                    0
               5
 Wrote bin5 file: type and iret=
                                         52
   File name=/work1/krc/test/MarsD.t52
     END KRC
              Total time [s] = 53.809822
```

BINF5 in v 3.2.3, binf5.2015 mar11 deletes file after a write error! Modified 2016jan10 to ask if file should be deleted or only closed.

25

## B IDL KRC-related Programs 2016jan06

```
Made by cd to -/idl/krc
fgrep -in ';_Titl' *.pro > q Get all title lines
fgrep ':1:' q
                         Look for those without an executable before them
EXAMT52
         Read KRC style 52 files to test low I capability
GCMCOMP
         Read KRC type 52 files Compare to Haberle, Mellon, Vasa., Lewis
KRCAMOEBA interface to KRC Thermal model: Amoeba convergence to data
         interpolate KRC global average temperature to make global map
KRCGA
KRCVERTEST Compare runs of different versions of KRC
KRCV
         Test output for KRC vector insolation geometry
KV3
          Check consistency of KRC within and between versions
MAPREBIN Put Albedo, inertia, elevation maps to uniform grid
         details INCOMPLETE
PORBTEST Various checks of KRC PORB regular and test output
QKRCHEMI Test hemispherical integration for remote viewer
QVH
          Investigate Vicki Hamilton 2006 2013 differences
```

## C Binary file type 52 guide

```
Sample of kv3@188. all but krccom are available in TTTMOD
                           = Array[48, 5, 3, 640, 15]
                DOUBLE
(hour, item, latitude, season, case)
itemt = Tsurf Tplan Tatm DownVIS DownIR
                DOUBLE
                           = Array[45, 2, 3, 640, 15]
(layer, item, latitude, season, case)
itemd = Tmin Tmax
GGG
                DOUBLE
                           = Array[6, 3, 640, 15]
(item,latitude,season,case)
itemg = NDJ4 DTM4 TTA4 FROST4 AFRO4 HEATMM
UUU
                DOUBLE
                           = Array[3, 2, 15]
(nlat,item,case)
itemu = Lat. elev
                           = Array[640, 5, 15]
VVV
                DOUBLE
(season,item,case)
itemv = DJU5 SUBS PZREF TAUD SUMF
KRCCOM is in kcom:
** Structure <d1f268>, 7 tags, length=1704, data length=1704, refs=1:
   FD
                              Array [96]
                    DOUBLE
   ALAT
                    DOUBLE
                              Array [37]
   ELEV
                    DOUBLE
                              Array [37]
                              Array[40]
   ID
                    LONG
   LD
                    LONG
                              Array[20]
   TIT
                    BYTE
                              Array [84]
                              Array[20]
   DAYTIM
                    BYTE
```