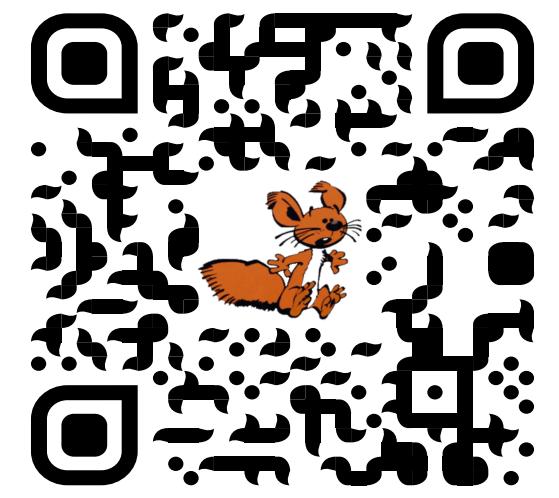
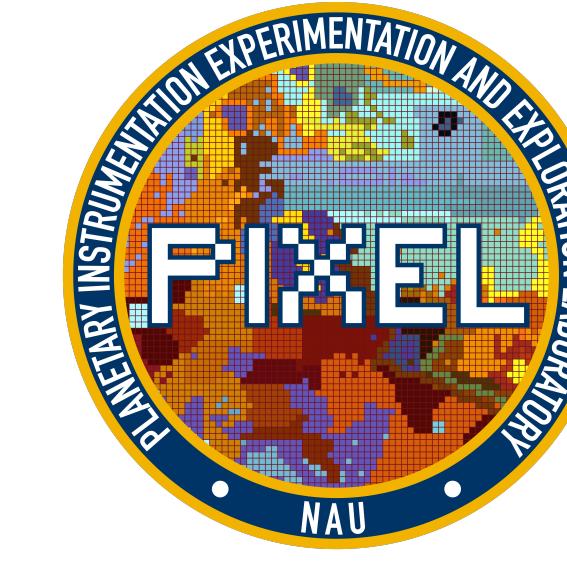


# A Faster Way to Account for Pixel Footprint Projection on Planetary Surfaces with Python: the SPiP Module

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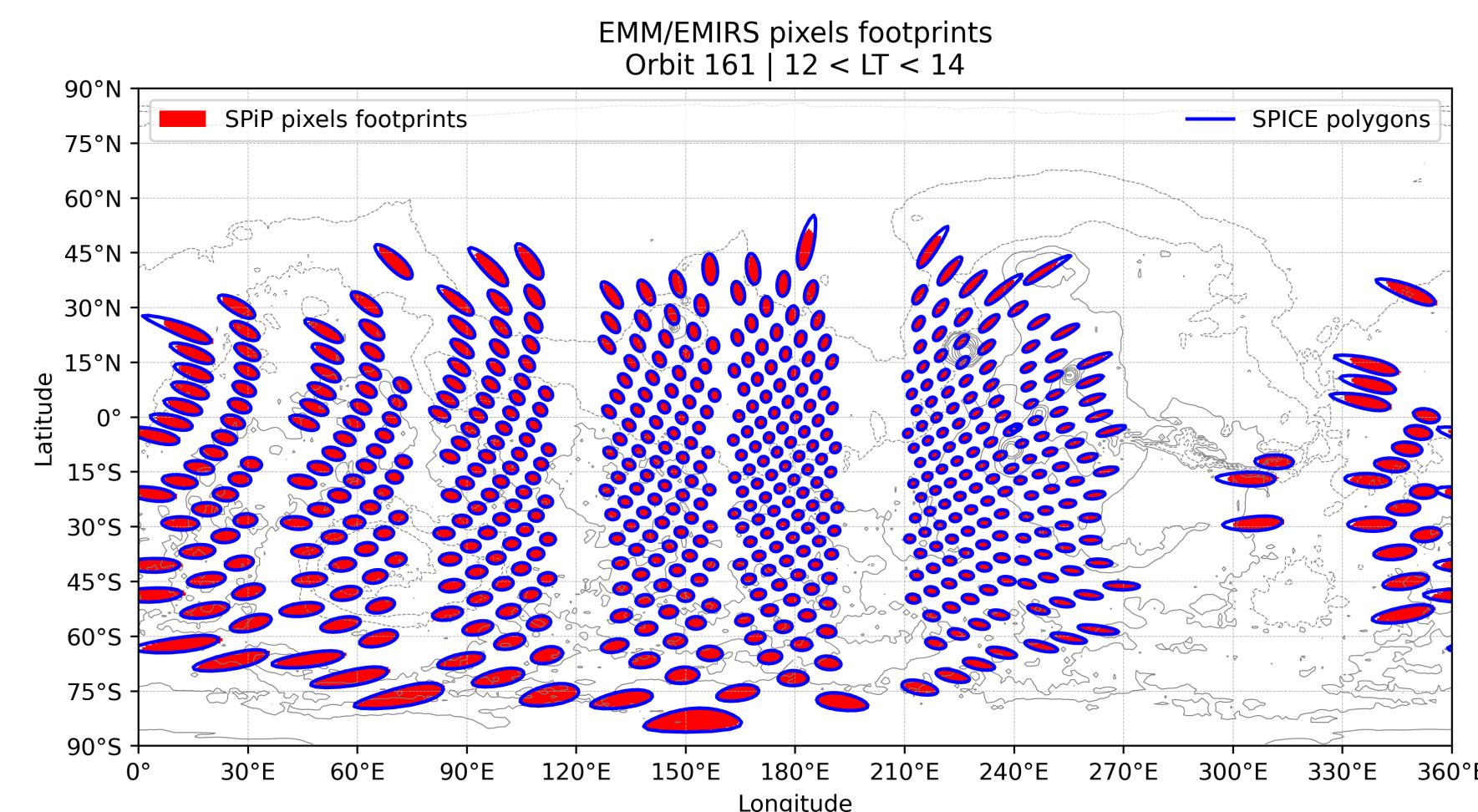
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## THE SPiP MODULE

SPiP: Spacecraft Pixel footprint Projection

- Python 3 module
- Developed for the EMIRS instrument onboard the EMM "Hope" spacecraft
- Currently in version 1.1



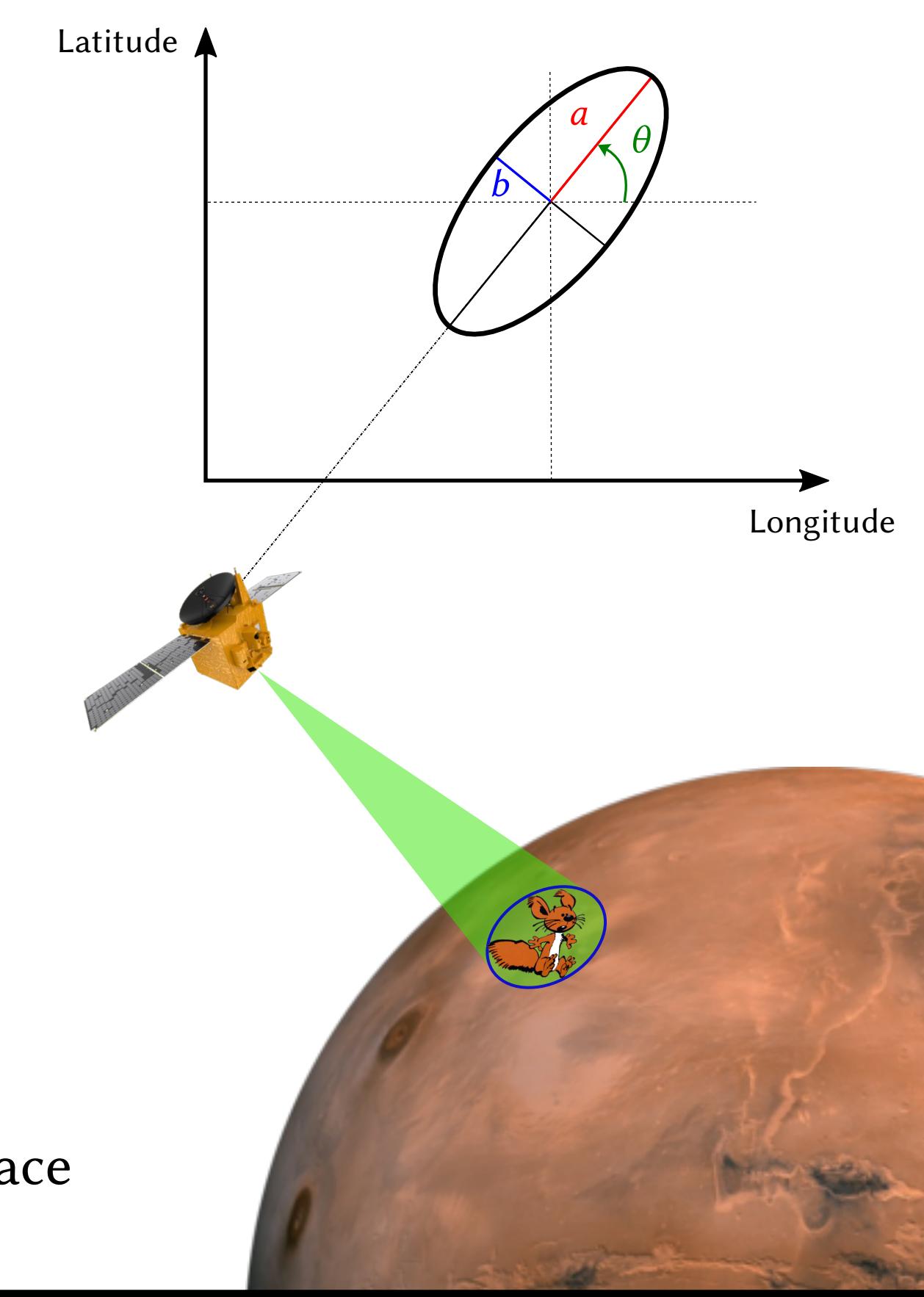
Uses 3D trigonometry to approximate the footprint of a pixel projected on a planetary surface.

Comparison between footprints computed by SPiP and the 20-points polygons derived by the SPICE kernel.

## PROJECTING THE PIXEL FOOTPRINT WITH 3D TRIGONOMETRY

Ellipse parameters retrieved

- $a$ : semi-major axis
- $b$ : semi-minor axis
- $\theta$ : orientation

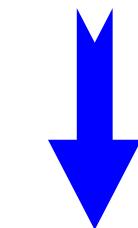


Parameters we need

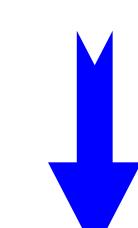
- Center longitude of the pixel
- Center latitude of the pixel
- Sub-spacecraft longitude
- Sub-spacecraft latitude
- Emergence angle
- Instrument pixel FOV
- Distance between spacecraft and planet surface

## SPiP VS POLYGONS

Testing if a point is within a 20-points polygon



20 tests to perform: 1 per side



Time-consuming, not efficient



Testing if a point is within an ellipse



VS

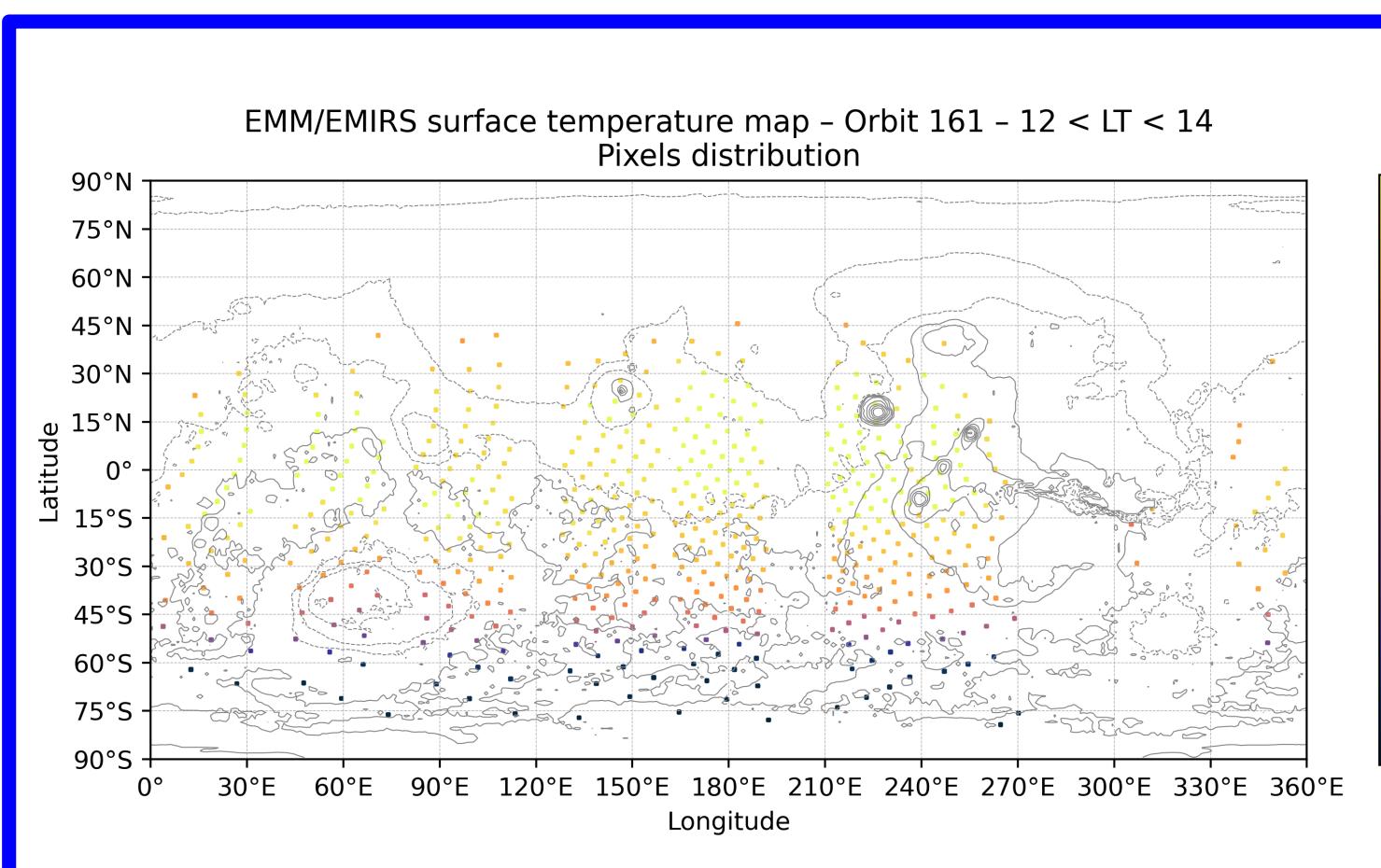
Testing if  $(x, y)$  verify 1 single equation

$$\frac{[(x - x_0) \cos(\theta) + (y - y_0) \sin(\theta)]^2}{a^2} + \frac{[(x - x_0) \sin(\theta) - (y - y_0) \cos(\theta)]^2}{b^2} \leq 1$$

- + Can be computed in one time for the whole grid using numpy arrays (#PythonPower)

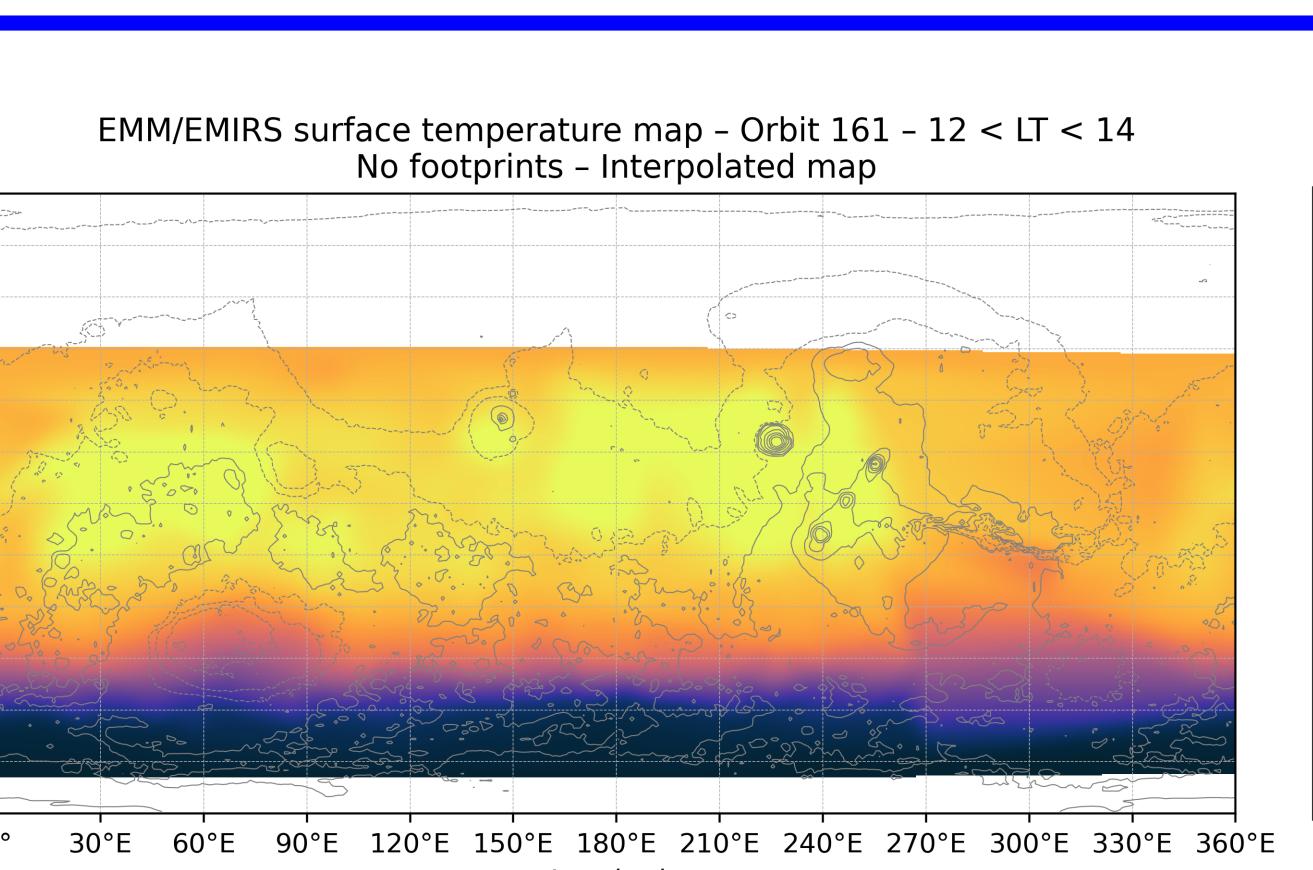
## WHY IS IT IMPORTANT TO ACCOUNT FOR THE SPATIAL EXTENT OF THE PIXELS?

### WITHOUT SPiP

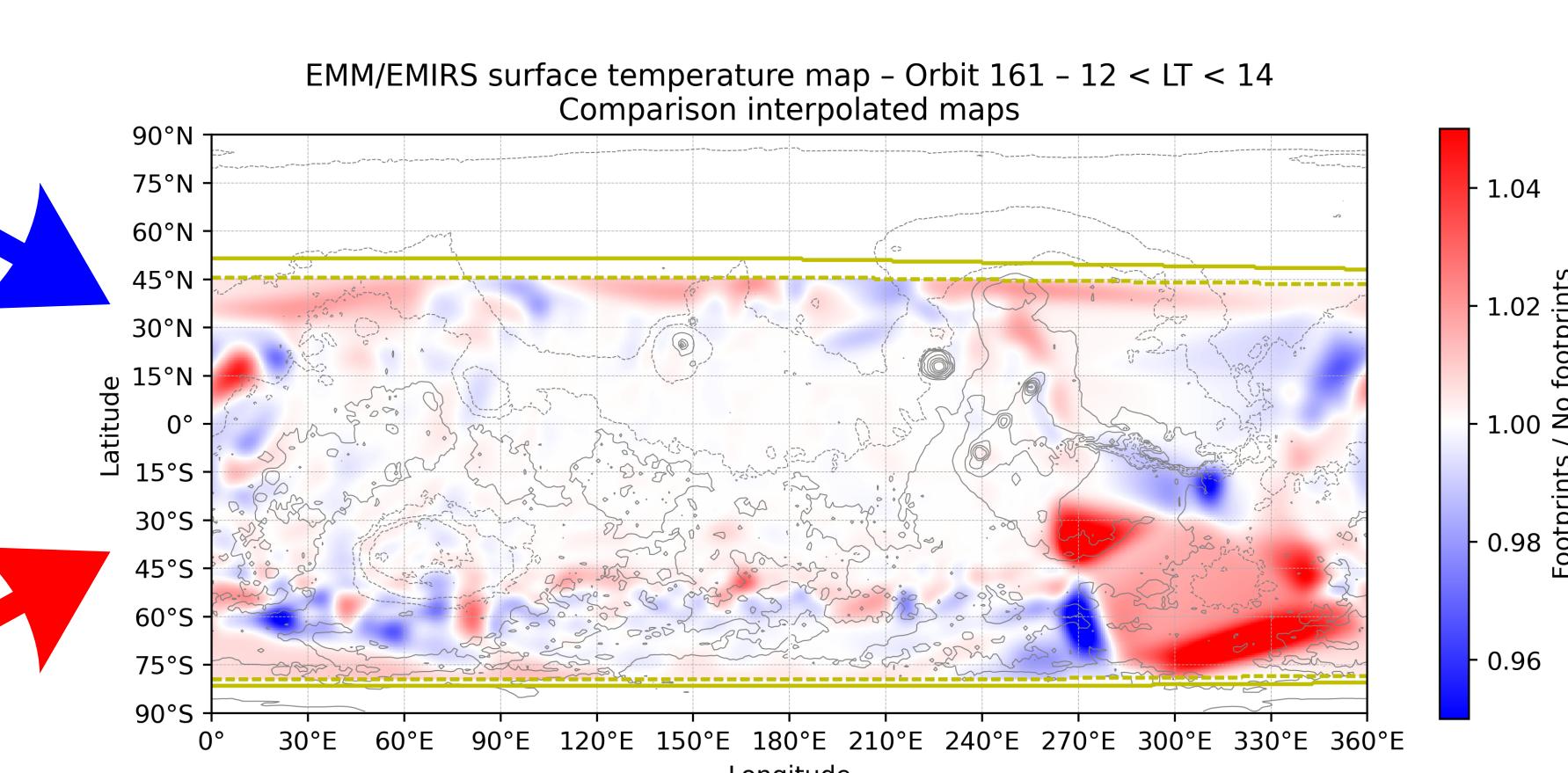


Interpolation  
& Smoothing

Interpolation  
& Smoothing



Ratio  
map with the pixels footprints  
map without considering the pixels footprints



- Interpolated data values may vary up to +/- 5%
- Latitude coverage increases by 6°

## CONCLUSION & PERSPECTIVES

- SPiP provides an easy and quick way to handle the spatial extent of pixels from orbital instruments on the surface.
- Already used to generate all L3 gridded products from the EMIRS instrument available on the EMM SDC.
- Future work:
  - Replace perfect sphere by ellipsoid.
  - More instruments/celestial bodies?

## ACCESSING SPiP

On GitHub: <https://github.com/NAU-PIXEL/spip>

DOI: 10.5281/zenodo.7714205

