

$$\begin{matrix} \begin{bmatrix} ABC \\ ABC \end{bmatrix} & \begin{bmatrix} ABC \\ CAB \end{bmatrix} & \begin{bmatrix} ABC \\ BCA \end{bmatrix} & \begin{bmatrix} ABC \\ BAC \end{bmatrix} & \begin{bmatrix} ABC \\ CBA \end{bmatrix} & \begin{bmatrix} ABC \\ ACB \end{bmatrix} \\ I & \bar{R}_j & \bar{R}_i & \chi_c & \chi_B & \chi_A \end{matrix}$$

$$\bullet I \quad \bar{R}_j \quad R_i \quad \chi_A \quad \chi_B \quad \chi_C$$

$$I \quad I \quad \bar{R}_j \quad R_i \quad \chi_A \quad \chi_B \quad \chi_C$$

$$\bar{R}_j \quad \bar{R}_i \quad \bar{R}_i \quad \bar{R}_j \quad \chi_B \quad \chi_C \quad \chi_A$$

$$R_i \quad R_i \quad I \quad \bar{R}_j \quad \chi_C \quad \chi_A \quad \chi_B$$

$$\chi_A \quad \chi_A \quad \chi_C \quad \chi_B \quad I \quad R_i \quad \bar{R}_j$$

$$\chi_B \quad \chi_B \quad \chi_A \quad \chi_C \quad \bar{R}_j \quad I \quad R_i$$

$$\chi_C \quad \chi_C \quad \chi_B \quad \chi_A \quad R_i \quad R_j \quad I$$

(lines 4-5)

$$G_\Delta = \{I, R_i, \bar{R}_j, \chi_k\}$$

• ~~Asociativa~~

• Cerrada respecto a la operación

$$\star : \{R_i \in G_\Delta, \bar{R}_j \in G_\Delta\} \exists R_k = R_i \star R_j \in G.$$

$$R_i \star \bar{R}_j = I \quad y \quad I \in G_\Delta$$

$$(I \cdot R_i) \star \bar{R}_j = I \cdot (R_i \star \bar{R}_j) \Rightarrow R_i \star \bar{R}_j = I. \quad I \cdot I = I$$

• Asociativa

$$\bullet \text{Neutro} \Rightarrow \exists \hat{g} \in G \Rightarrow g_i \square \hat{g} = g_i = \hat{g} \square g_i$$

$$\boxed{R_i \cdot I = R_i}$$

$$\bullet \text{Inverso} \quad g_i \in G \Rightarrow \exists g_i^{-1} \in G \Rightarrow g_i \square g_i^{-1} = g_i^{-1} \square g_i = g$$

$$R_i \cdot \bar{R}_j = I$$



## Ejercicio 10

$$|P_n\rangle \Rightarrow p(x) = a_0 + a_1x + a_2x^2 + \dots + a_{n-1}x^{n-1} = \sum_{i=0}^{n-1} a_i x^i$$

$$a) \quad P(x) \oplus Q(x) = (a_0 + a_1x + a_2x^2 + \dots + a_{n-1}x^{n-1}) + (b_0 + b_1x + b_2x^2 + \dots + b_{n-1}x^{n-1})$$

$$= (a_0 + b_0) + (a_1x + b_1x) + (a_2x^2 + b_2x^2) + (a_nx^n + b_nx^n)$$

~~$$= (a_0 + b_0) + (a_1 + b_1)x + (a_2 + b_2)x^2 + \dots + (a_{n-1} + b_{n-1})x^{n-1}$$~~

$$\hookrightarrow \text{mult} \quad \alpha \cdot P(x) = \alpha a_0 + \alpha a_1x + \alpha a_2x^2 + \dots + \alpha a_{n-1}x^{n-1}$$

$$\bullet \quad \forall |P_i\rangle, |P_j\rangle, |P_k\rangle \in P \Rightarrow (|P_i\rangle + |P_j\rangle) + |P_k\rangle = |P_i\rangle + (|P_j\rangle + |P_k\rangle)$$

• Neutro

$$|0\rangle + |P_i\rangle = |P_i\rangle + |0\rangle = |P_i\rangle \quad \forall |P_i\rangle \in P$$