Goal: using toy system, do a "comprehensive computational study illustrating different tradeoffs"

Along that vein, we've set up a simulation environment for a two-state system

$$\mathbf{x}_{\mathsf{t}+1} = \mathbf{A}\mathbf{x}_{\mathsf{t}} + \mathbf{B}\mathbf{u}_{\mathsf{t}} + \mathbf{w}$$

$$\mathbf{A} = \begin{bmatrix} 1 + \alpha & 0 \\ 0 & 1 \end{bmatrix},$$

$$\mathbf{B} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\mathbf{w} \sim \mathcal{N}(\mathbf{0}, \mathbf{\sigma})$$

$$\mathbf{x}_{\mathsf{0}} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \text{ for all trajectories}$$
Each trajectory takes exactly 5 steps

Observations from basic RL experiments:

- -More uncontrollability impairs ability to converge (1)
- -More instability takes longer to converge (unclear whether ultimate performance changes, see 2)
- -More noise decreases end performance (3)

Todo:

- 1. Theoretical result on convergence? (not for control audience)
- 2. Run longer experiments
- 3. Normalize all performance metrics by control LQR optimal performance***, given explicit instantiation
 - ***Working out the details of how to evaluate performance, RL is finite horizon evaluation but we care about infinite horizon for theoretical comparisons

Moving to bigger picture:

We're seeing a story come out of the comparisons. From model-based to model-free, we want to compare performance for the following:

- 1. Totally model-based, everything pre-known (including noise, plant, etc) LQR
- 2. Naive sysID on plant (and noise?)+assume correct ID & do ^^LQR
- 3. Nik' stuff: do control that's robust to specific errors in ID
- 4. Model-ish-based RL: output a linear controller (easy to evaluate quality in theoretical terms)*~*
- 5. Model-Free RL: Policy gradient methods

~ use control metrics as RL reward function?

This seems like a nice Control-RL tutorial in a classroom setting

For ACC:

Either: 1 long paper, need better metrics to visualize "convergence", "bias", and "variance" of each experiment on a single plot

Or: Sister papers #1,2 #4,5 (3?)