

# Functional Thinking

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a metaphor  
an essay  
a history lesson





new language:  
easy

new paradigm:  
hard

"functional" is  
more a way of  
thinking than  
a tool set

# Execution in the Kingdom of Nouns

Steve  
Yegge

[http://steve-yegge.blogspot.com/  
2006/03/execution-in-kingdom-of-nouns.html](http://steve-yegge.blogspot.com/2006/03/execution-in-kingdom-of-nouns.html)



v e r b s

# UndoManager . execute()

undo()

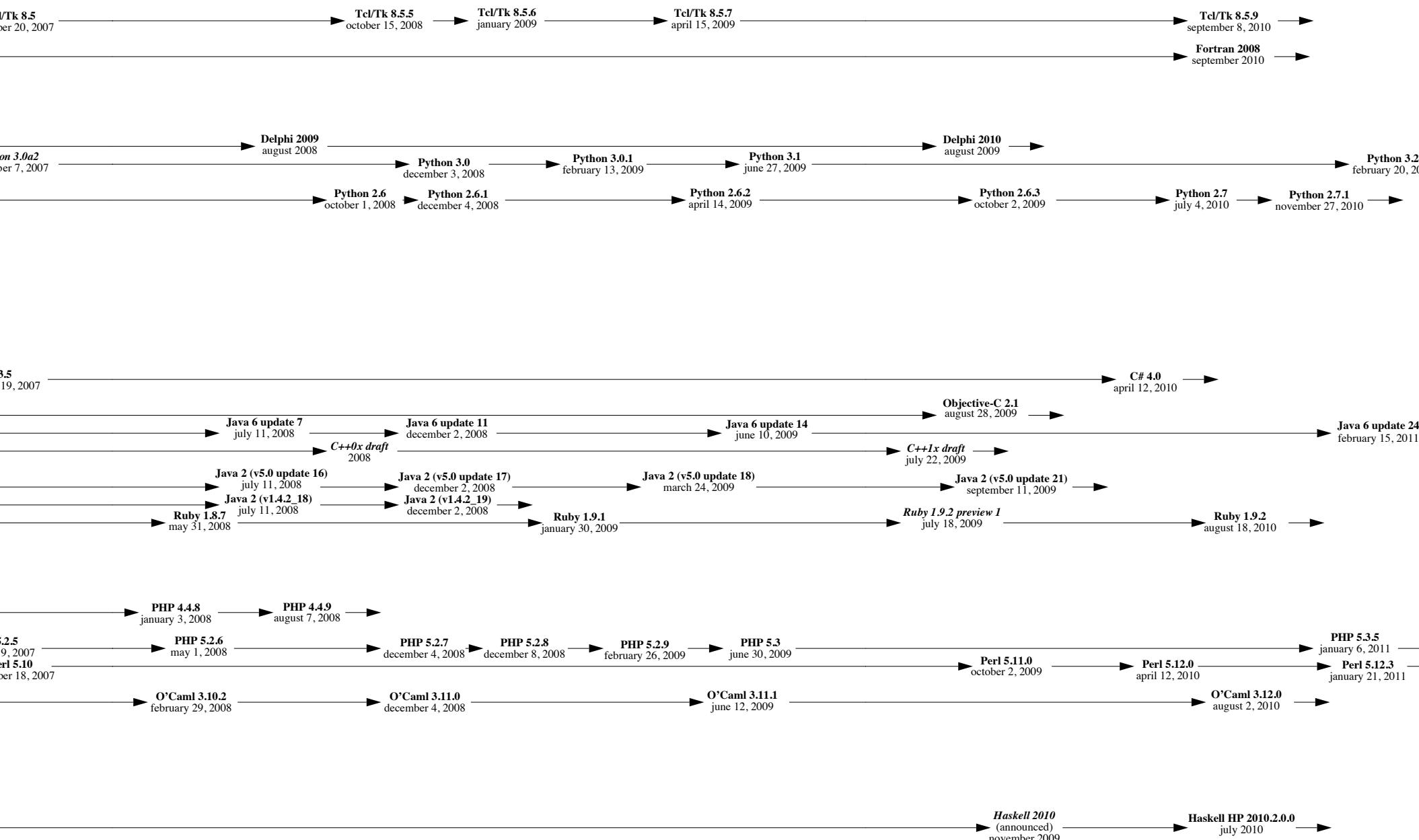


# [http://oreilly.com/news/languagelos\\_0504.html](http://oreilly.com/news/languagelos_0504.html)

2008

2009

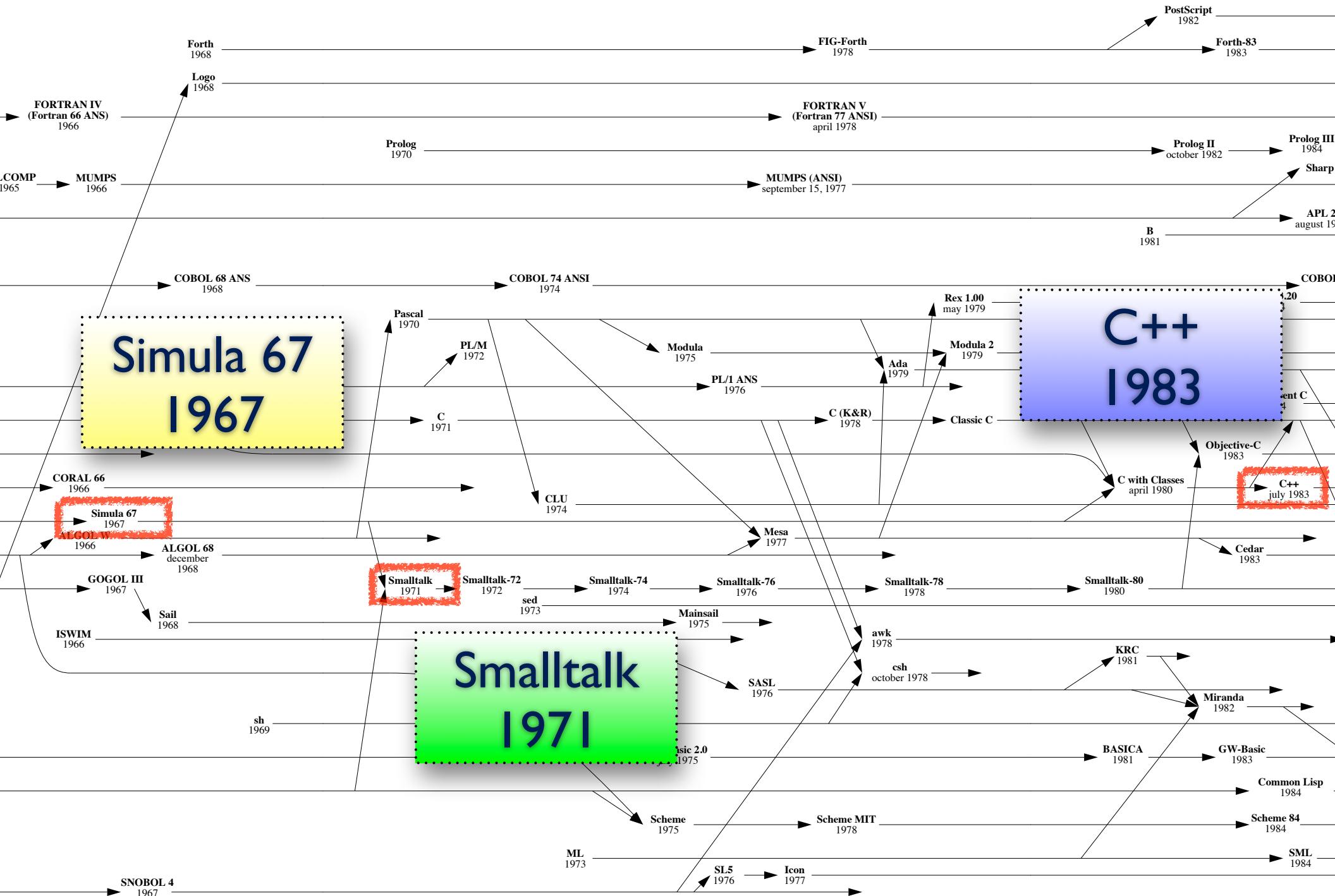
2010



1970

1975

1980



academic  
offshoot

functional  
programming

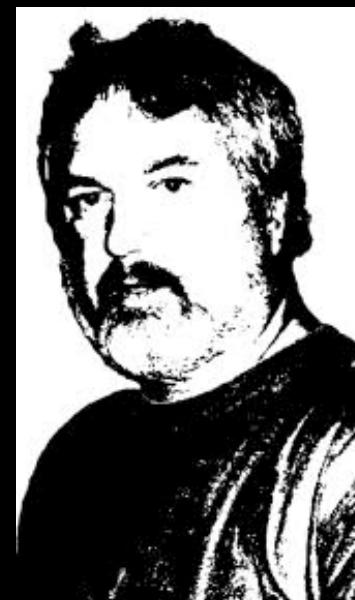
mainstream  
technology

practical  
offshoot

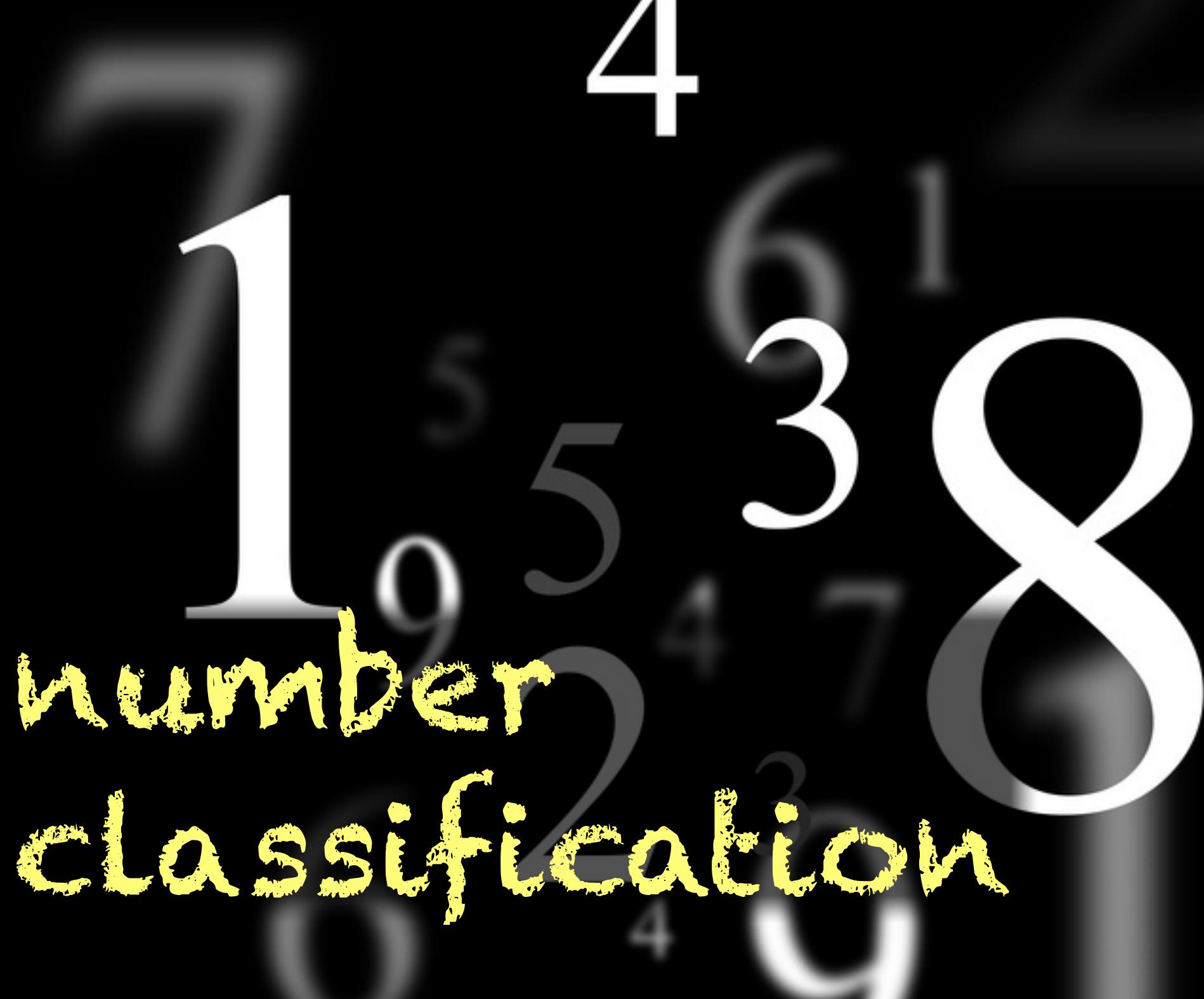
OO makes code  
understandable by  
encapsulating moving  
parts.

FP makes code  
understandable by  
minimizing moving  
parts.

Michael Feathers, author of "Working with Legacy Code"



# number classification



perfect #

$$\sum(\text{f}(\#)) - \# = \#$$

(sum of the factors of a #) - # = #

(sum of the factors of a #) = 2#

$$6: 1 + 2 + 3 + 6 = 12 \quad (2 \times 6)$$

$$28: 1 + 2 + 4 + 7 + 14 + 28 = 56 \quad (2 \times 28)$$

$$496: \dots$$

# classification

- |                       |           |
|-----------------------|-----------|
| $\Sigma(f(\#)) = 2\#$ | perfect   |
| $\Sigma(f(\#)) > 2\#$ | abundant  |
| $\Sigma(f(\#)) < 2\#$ | deficient |

imperative

# imperative classifier

```
package com.nealford.conf.tdd.perfectnumbers;

import java.util.Set;
import java.util.HashSet;
import static java.lang.Math.sqrt;

public class Classifier6 {
    private Set<Integer> _factors;
    private int _number;

    public Classifier6(int number) {
        if (number < 1)
            throw new InvalidNumberException(
                "Can't classify negative numbers");
        _number = number;
        _factors = new HashSet<Integer>();
        _factors.add(1);
        _factors.add(_number);
    }

    private boolean isFactor(int factor) {
        return _number % factor == 0;
    }

    public Set<Integer> getFactors() {
        return _factors;
    }

    private void calculateFactors() {
        for (int i = 1; i <= sqrt(_number) + 1; i++)
            if (isFactor(i))
                addFactor(i);
    }

    private void addFactor(int factor) {
        _factors.add(factor);
        _factors.add(_number / factor);
    }

    private int sumOfFactors() {
        calculateFactors();
        int sum = 0;
        for (int i : _factors)
            sum += i;
        return sum;
    }

    public boolean isPerfect() {
        return sumOfFactors() - _number == _number;
    }

    public boolean isAbundant() {
        return sumOfFactors() - _number > _number;
    }

    public boolean isDeficient() {
        return sumOfFactors() - _number < _number;
    }

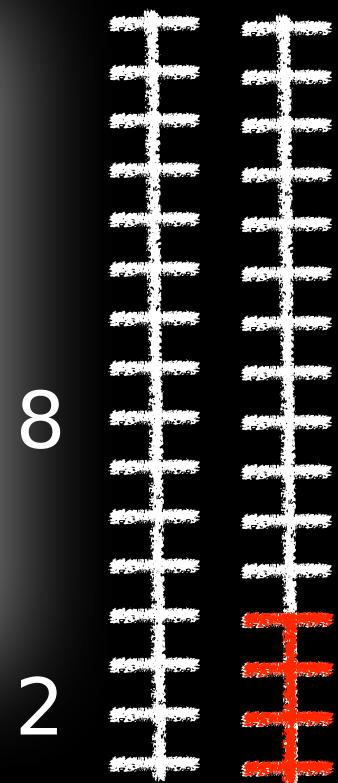
    public static boolean isPerfect(int number) {
        return new Classifier6(number).isPerfect();
    }
}
```



```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {  
        if (number < 1)  
            throw new InvalidNumberException(  
                "Can't classify negative numbers");  
        _number = number;  
        _factors = new HashSet<Integer>();  
        _factors.add(1);  
        _factors.add(_number);  
    }  
  
    public boolean isPerfect() {...  
  
    public boolean isAbundant() {...  
  
    public boolean isDeficient() {...  
  
    public static boolean isPerfect(int number) {...  
}
```

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
        private boolean isFactor(int factor) {  
            return _number % factor == 0;  
        }  
  
        public Set<Integer> getFactors() {  
            return _factors;  
        }  
  
        public boolean isPerfect() {...  
        public boolean isAbundant() {...  
        public boolean isDeficient() {...  
        public static boolean isPerfect(int number) {...  
    }
```

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...  
  
    private void calculateFactors() {  
        for (int i = 2; i < sqrt(_number) + 1; i++)  
            if (isFactor(i))  
                addFactor(i);  
    }  
  
    private void addFactor(int factor) {  
        _factors.add(factor);  
        _factors.add(_number / factor);  
    }  
}
```



```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...  
  
    private void calculateFactors() {...  
  
    private void addFactor(int factor) {...  
  
private int sumOfFactors() {  
    calculateFactors();  
    int sum = 0;  
    for (int i : _factors)  
        sum += i;  
    return sum;  
}
```

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...  
  
    private void calculateFactors() {...  
  
    private public boolean isPerfect() {  
        return sumOfFactors() - _number == _number;  
    }  
  
    public public boolean isAbundant() {  
        return sumOfFactors() - _number > _number;  
    }  
  
    public public boolean isDeficient() {  
        return sumOfFactors() - _number < _number;  
    }  
}
```

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {…}  
  
    private boolean isFactor(int factor) {…}  
  
    public Set<Integer> getFactors() {…}  
  
    private void calculateFactors() {…}  
  
    private void addFactor(int factor) {…}  
  
    private int sumOfFactors() {…}  
  
    public boolean isPerfect() {…}  
  
    public boolean isAbundant() {…}  
  
    public boolean isDeficient() {…}  
  
    public static boolean isPerfect(int number) {…}  
}
```



internal state

cohesive

composed

testable

refactorable

(slightly more)  
functional

```
public class NumberClassifier {  
  
    public boolean isFactor(int number, int potential_factor) {  
        return number % potential_factor == 0;  
    }  
  
    public int sum(Set<Integer> factors) {...  
  
    public boolean isPerfect(int number) {...  
  
    public boolean isAbundant(int number) {...  
  
    public boolean isDeficient(int number) {...  
}
```

# (slightly) more functional classifier



```
package com.nealford.conf.ft.numberclassifier;

import static java.lang.Math.sqrt;
import java.util.HashSet;
import java.util.Iterator;
import java.util.Set;

public class NumberClassifier {

    static public boolean isFactor(int number,
        int potential_factor) {
        return number % potential_factor == 0;
    }

    static public Set<Integer> factors(int number)
    HashSet<Integer> factors =
        new HashSet<Integer>();
    for (int i = 1; i <= sqrt(number); i++)
        if (isFactor(number, i)) {
            factors.add(i);
            factors.add(number / i);
        }
    return factors;
}

static public int sum(Set<Integer> factors) {
    Iterator it = factors.iterator();
    int sum = 0;
    while (it.hasNext())
        sum += (Integer) it.next();
    return sum;
}

static public boolean isPerfect(int number) {
    return sum(factors(number)) - number == number;
}

static public boolean isAbundant(int number) {
    return sum(factors(number)) - number > number;
}

static public boolean isDeficient(int number) {
    return sum(factors(number)) - number < number;
}
```

```
public class NumberClassifier {  
  
    public boolean isFactor(int number, int potential_factor) { ...  
  
        public Set<Integer> factors(int number) {  
            HashSet<Integer> factors = new HashSet<Integer>();  
            for (int i = 1; i <= sqrt(number); i++)  
                if (isFactor(number, i)) {  
                    factors.add(i);  
                    factors.add(number / i);  
                }  
            return factors;  
        }  
    }  
}
```

```
public class NumberClassifier {  
  
    public boolean isFactor(int number, int potential_factor) { ...  
  
    public Set<Integer> factors(int number) { ...  
  
        public int sum(Set<Integer> factors) {  
            Iterator it = factors.iterator();  
            int sum = 0;  
            while (it.hasNext())  
                sum += (Integer) it.next();  
            return sum;  
        }  
    }  
}
```

```
public class NumberClassifier {  
  
    public boolean isFactor(int number, int potential_factor) { ...  
  
    public Set<Integer> factors(int number) { ...  
  
    public boolean isPerfect(int number) {  
        return sum(factors(number)) - number == number;  
    }  
  
    public boolean isAbundant(int number) {  
        return sum(factors(number)) - number > number;  
    }  
  
    public boolean isDeficient(int number) {  
        return sum(factors(number)) - number < number;  
    }  
}
```

no internal  
state

```
public class NumberClassifier {  
    static public boolean isFactor(int number, int potential_factor) {...  
    static public Set<Integer> factors(int number) {...  
    static public int sum(Set<Integer> factors) {...  
    static public boolean isPerfect(int number) {...  
    static public boolean isAbundant(int number) {...  
    static public boolean isDeficient(int number) {...  
}
```

less need for scoping

refactorable

testable

"functional" is  
more a way of  
thinking than  
a tool set

1st class/  
higher order  
functions

pure  
functions

# concepts

strict evaluation

recursion

1st class /  
higher-order  
functions      pure  
functions

concepts

strict evaluation

recursion

$$(\omega_{\mathbb{M}})^2 dV - \frac{1}{2} \omega^2 e^{\int_{\mathbb{M}} (\alpha^2 + g^2) dV} \psi^{-1} (\mathbb{C})$$

$$= \frac{d}{dx} \left( \frac{1}{x^2} \right) - \frac{2}{x^3} - \frac{1}{x^2} \left( \frac{d}{dx} \right) \frac{1}{x^2}$$

$$\frac{d^2w}{d\eta^2} = \frac{1}{V^2} \frac{d^2V}{d\eta^2} + \frac{2}{V^3} \left( \frac{dV}{d\eta} \right)^2$$

$$U = Mg h = Mg \rho A r \sin \theta \quad \frac{dU}{dr} = -\frac{1}{r^2} \frac{dr}{d\theta}$$

$$2 + \frac{1}{2} \left( \frac{v}{\mu} \right)^2 = \frac{1}{2} \prod_{i=1}^n \sqrt{1 - \frac{e_i^2}{\mu^2}} \prod_{i=1}^n v_i^2 \quad \frac{dv}{d\mu} = -\frac{1}{\mu^2} \left( \frac{v}{\mu} \right) \frac{d\omega}{d\mu} \Rightarrow \frac{d\omega}{d\mu} + \omega = \frac{v}{\mu^2}$$

$$N = \left( \frac{d\bar{x}}{dt} \right)_{t=T_1} = \frac{d\bar{x}}{dt} \Big|_{t=T_1}$$

$$\vec{S} = \vec{N} \quad R = \frac{I_3 - I_1}{I_1} w_1$$

$$\vec{F} = \frac{c}{r^2} \vec{r} \quad \text{L} = -\frac{\partial U}{\partial r} = \frac{c}{r^2}$$

$$-\vec{F} = \frac{C}{r^4}$$

$$k = \frac{1}{2} M \dot{x}^2 = \frac{1}{2} M \left[ m_0 \sin^2 \left( \frac{\pi t}{T} + \phi \right) \right]$$

$$\int_{-\infty}^{\tau} dt' = \frac{1}{T} \ln \left( \frac{e^{-\beta T}}{1 - e^{-\beta T}} \right)$$

$$\langle k \rangle = \frac{\sum k_i}{T} \quad \text{and} \quad \langle k^2 \rangle = \frac{\sum k_i^2}{T}$$

$$\int_{-\infty}^{\infty} e^{-t^2/2} dt = \sqrt{\pi}$$

$$t^{\frac{1}{2}} \cdot \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-\frac{(x-t)^2}{2}} dx = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-\frac{(x-t)^2}{2}} dx$$

# T-TORADO

10.  $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$

# Inception

# Michigan

$\langle U \rangle = \frac{1}{N} \sum_{i=1}^N U_i$

1000-1000

# Higher-order functions

# higher-order functions

functions that can  
either take other  
functions as  
arguments or return  
them as results

# extracting reusable code:

- extract via Template Method DP
- encapsulate verb via Command DP

```
public void addOrderFrom(ShoppingCart cart, String userName,  
                        Order order) throws SQLException {  
    setupDataInfrastructure();  
    try {  
        addOrder, userKeyBasedOn(userName));  
        addLineItemsFrom(cart, order.getOrderKey());  
        completeTransaction();  
    } catch (SQLException sqlx) {  
        rollbackTransaction();  
        throw sqlx;  
    } finally {  
        cleanUp();  
    }  
}
```



```
public void addOrderFrom(ShoppingCart cart, String userName,  
                        Order order) throws Exception {  
    setupDataInfrastructure();  
    try {  
        add(order, userKeyBasedOn(userName));  
        addLineItemsFrom(cart, order.getOrderKey());  
        completeTransaction();  
    } catch (Exception condition) {  
        rollbackTransaction();  
        throw condition;  
    } finally {  
        cleanUp();  
    }  
}
```



```
public void wrapInTransaction(Command c) throws Exception {
    setupDataInfrastructure();
    try {
        c.execute();
        completeTransaction();
    } catch (Exception condition) {
        rollbackTransaction();
        throw condition;
    } finally {
        cleanUp();
    }
}

public void addOrderFrom(final ShoppingCart cart,
    final String userName, final Order order) {
    wrapInTransaction(new Command() {
        public void execute() {
            add(order, userKeyBasedOn(userName));
            addLineItemsFrom(cart, order.getOrderKey());
        }
    });
}
```

# same “unit of work” code

```
public class OrderDbClosure {  
    def wrapInTransaction(command) {  
        setupDataInfrastructure()  
        try {  
            command()  
            completeTransaction()  
        } catch (RuntimeException ex) {  
            rollbackTransaction()  
            throw ex  
        } finally {  
            cleanUp()  
        }  
    }  
  
    def addOrderFrom(cart, userName, order) {  
        wrapInTransaction {  
            add order, userKeyBasedOn(userName)  
            addLineItemsFrom cart, order.orderKey  
        }  
    }  
}
```





```
def wrapInTransaction(command) {  
    setupDataInfrastructure()  
    try {  
        command()  
        completeTransaction()  
    } catch (Exception ex) {  
        rollbackTransaction()  
        throw ex  
    } finally {  
        cleanUp()  
    }  
}  
  
def addOrderFrom(cart, userName, order) {  
    wrapInTransaction {  
        add order, userKeyBasedOn(userName)  
        addLineItemsFrom cart, order.getOrderKey()  
    }  
}
```

```

def addOrderFrom(cart, userName, order) {
    wrapInTransaction {
        add order, userKeyBasedOn(userName)
        addLineItemsFrom cart, order.getOrderKey()
    }
}

```

What's so special about...

# closures

# minimal code to demonstrate closures

```
def makeCounter() {  
    def very_local_variable = 0  
    return { return very_local_variable += 1 }  
}  
  
c1 = makeCounter()  
c1()  
c1()  
c1()  
  
c2 = makeCounter()  
  
println "C1 = ${c1()}, C2 = ${c2()}"  
// output: C1 = 4, C2 = 1
```



```
def makeCounter() {  
    def very_local_variable = 0  
    return { very_local_variable += 1 }  
}
```

```
c1 = makeCounter()
```

```
c1()
```

```
c1()
```

```
c1()
```

```
c2 = makeCounter()
```

```
println "C1 = ${c1()}, C2 = ${c2()}"
```

```
closures » groovy MakeCounter.groovy  
C1 = 4, C2 = 1
```



# closest Java equivalent to closure code

```
class Counter {  
    public int varField;  
  
    Counter(int var) {  
        varField = var;  
    }  
  
    public static Counter makeCounter() {  
        return new Counter(0);  
    }  
  
    public int execute() {  
        return ++varField;  
    }  
}
```



```
public class Counter {  
    public int varField;  
  
    public Counter(int var) {  
        varField = var;  
    }  
  
    public static Counter makeCounter() {  
        return new Counter(0);  
    }  
  
    public int execute() {  
        return ++varField;  
    }  
}
```



Let the  
language  
manage state

# Languages handle

memory allocation

garbage collection

concurrency

state

tests → specification-based testing frameworks



time

$$\frac{\partial \theta^M T(\xi)}{\partial \theta} = \frac{\partial}{\partial \theta} \int_{R_n} T(x) f(x, \theta) dx = \int_{R_n} \frac{\partial}{\partial \theta} T(x) f(x, \theta) dx$$

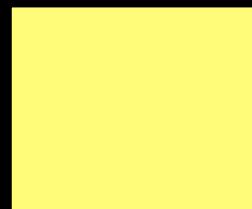
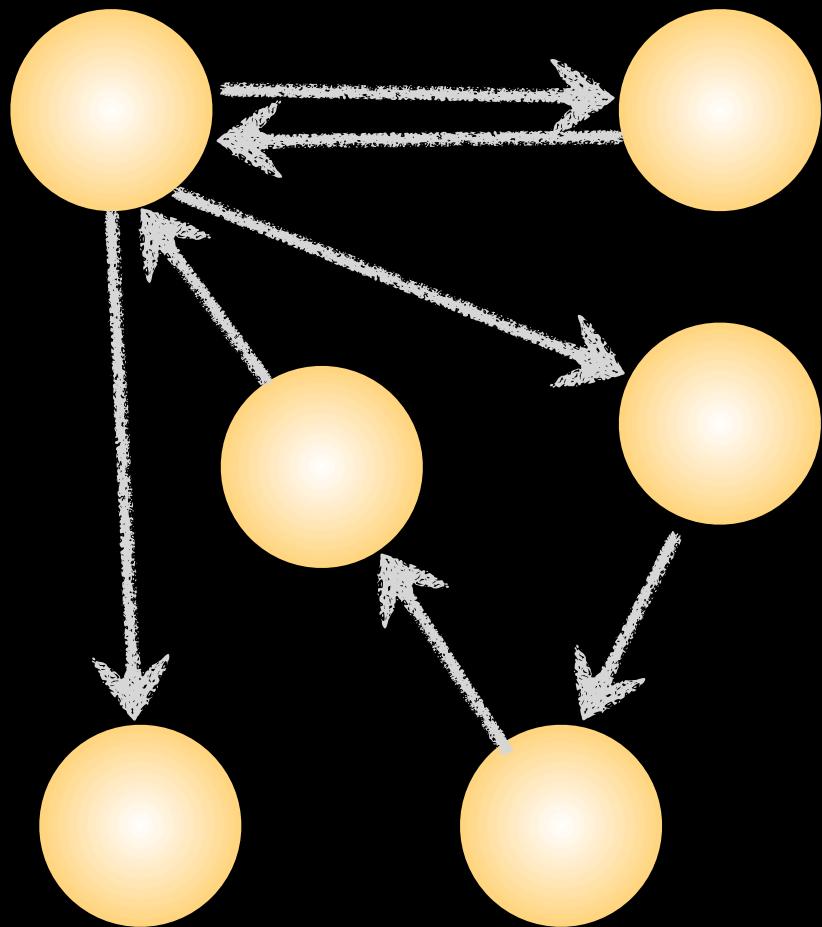
$$\int_{R_n} T(x) \cdot \frac{\partial}{\partial \theta} f(x, \theta) dx = M\left(T(\xi), \frac{\partial}{\partial \theta} \ln L(\xi, \theta)\right)$$

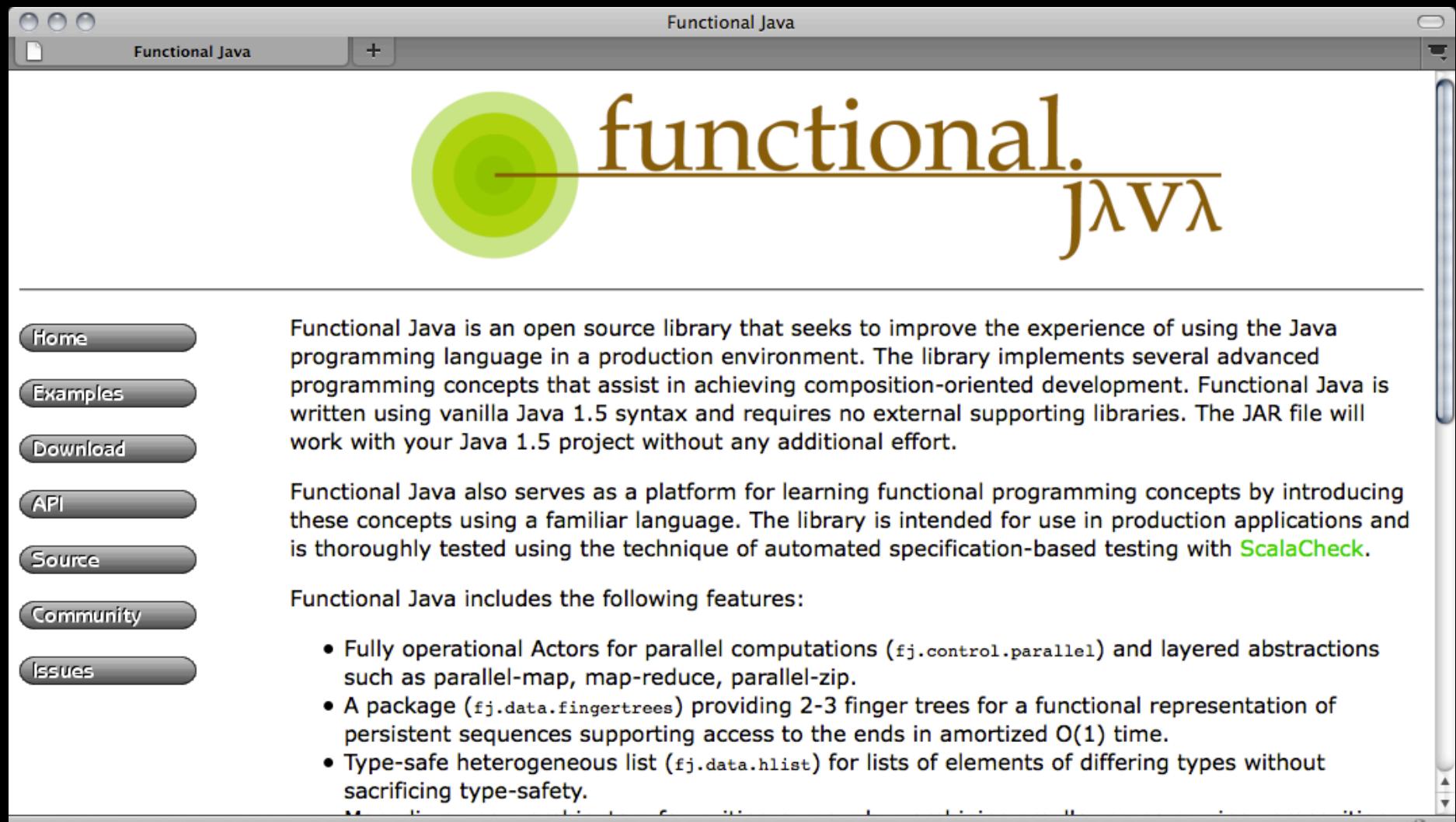
**1st-class  
functions**

$$\int_{R_n} T(x) \cdot \left( \frac{\partial}{\partial \theta} \ln L(x, \theta) \right) \cdot f(x, \theta) dx = \int_{R_n} T(x) \left[ \frac{\partial}{\partial \theta} \ln L(x, \theta) \right] f(x, \theta) dx$$

# 1st-class functions

functions can  
appear anywhere  
other language  
constructs can  
appear





- Fully operational Actors for parallel computations (`fj.control.parallel`) and layered abstractions such as parallel-map, map-reduce, parallel-zip.
  - A package (`fj.data.fingertrees`) providing 2-3 finger trees for a functional representation of persistent sequences supporting access to the ends in amortized O(1) time.
  - Type-safe heterogeneous list (`fj.data.hlist`) for lists of elements of differing types without sacrificing type-safety.

# NumberClassifier using Functional Java

```
package com.nealford.conf.ft.numberclassifier;

import fj.F;
import fj.data.List;
import static fj.data.List.range;
import static fj.function.Integers.add;

import static java.lang.Math.round;
import static java.lang.Math.sqrt;

public class FNumberClassifier {
```

```
    public boolean isFactor(int number, int potential_factor) {
        return number % potential_factor == 0;
    }

    public List<Integer> factorsOf(final int number) {
        return range(1, number+1)
            .filter(new F<Integer, Boolean>() {
                public Boolean f(final Integer i) {
                    return isFactor(number, i);
                }
            });
    }

    public int sum(List<Integer> factors) {
        return factors.foldLeft(fj.function.Integers.add, 0);
    }

    public boolean isPerfect(int number) {
        return sum(factorsOf(number)) - number == number;
    }

    public boolean isAbundant(int number) {
        return sum(factorsOf(number)) - number > number;
    }

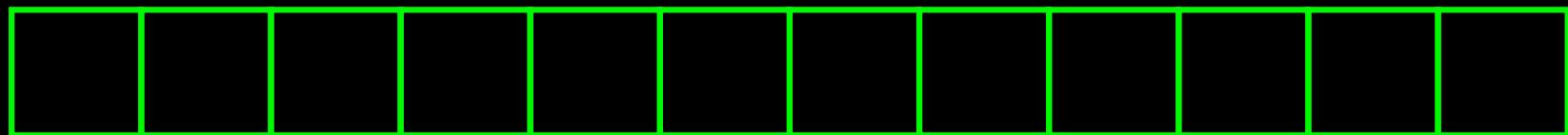
    public boolean isDeficient(int number) {
        return sum(factorsOf(number)) - number < number;
    }
```



```
public class FNumberClassifier {  
  
    public boolean isFactor(int number, int potential_factor) {  
        return number % potential_factor == 0;  
    }  
  
    public List<Integer> factorsOf(final int number) {  
        return range(1, number+1).filter(new F<Integer, Boolean>() {  
            public Boolean f(final Integer i) {  
                return isFactor(number, i);  
            }  
        });  
    }  
  
    public int sum(List<Integer> factors) {  
        return factors.foldLeft(fj.function.Integers.add, 0);  
    }  
  
    public boolean isPerfect(int number) {  
        return sum(factorsOf(number)) - number == number;  
    }  
  
    public boolean isAbundant(int number) {  
        return sum(factorsOf(number)) - number > number;  
    }  
  
    public boolean isDeficient(int number) {  
        return sum(factorsOf(number)) - number < number;  
    }  
}
```

```
public int sum(List<Integer> factors) {  
    return factors.foldLeft(add, 0);  
}  
  
public int sum(List<Integer> factors) {  
    return factors.foldLeft(fj.function.Integers.add, 0);  
}
```

fold



```

public int sum(List<Integer> factors) {
    return factors.foldLeft(add, 0);
}

public int sum(List<Integer> factors) {
    return factors.foldLeft(fj.function.Integers.add, 0);
}

```

```

public int sum(List<Integer> factors) {
    return factors.foldLeft(fj.function.Integers.add, 0);
}

public boolean isPerfect(int number) {
    return sum(factorsOf(number)) - number =
}

public boolean isAbundant(int number) {
    return sum(factorsOf(number)) - number >
}

```

add F<Integer, F<Integer, Integer>>  
multiply F<Integer, F<Integer, Integer>>  
power F<Integer, F<Integer, Integer>>  
remainder F<Integer, F<Integer, Integer>>  
subtract F<Integer, F<Integer, Integer>>  
abs F<Integer, Integer>>

(defn sum-factors [number]  
 (reduce + (factors number)))



think about results,  
 not steps

```
public List<Integer> factorsOf(final int number) {  
    return range(1, number + 1)  
        .filter(new F<Integer, Boolean>() {  
            public Boolean f(final Integer i) {  
                return isFactor(number, i);  
            }  
        });  
}
```

12

1 2 3 4 5 6 7 8 9 10 11 12

```
public boolean isFactor(int number, int potential_factor) {  
    return number % potential_factor == 0;  
}  
  
public List<Integer> factorsOf(final int number) {  
    return range(1, number + 1)  
        .filter(new F<Integer, Boolean>() {  
            public Boolean f(final Integer i) {  
                return isFactor(number, i);  
            }  
        });  
}  
  
public int sum(List<Integer> factors) {  
    return factors.stream().reduce(0, (j, f) -> f + j);  
}
```

think about results,  
not steps

academia  
alert!



# currying

given:  $f:(X \times Y) \rightarrow Z$

then:  $\text{curry}(f): X \rightarrow (Y \rightarrow Z)$

currying transforms a multi-argument function so that it can be called as a chain of single-argument functions



# partial application

partial application fixes a number of arguments to a function, producing another function of smaller arity

# currying & partial application

```
def product = { x, y ->
    return x * y
}

def quadrade = product.curry(4)
def octate = product.curry(8)

println "4x4: ${quadrade.call(4)}"
println "5x8: ${octate(5)}"

// curry composition
def composite = { f, g, x -> return f(g(x))}
def thirtyTwoer = composite.curry(quadrade, octate)

println "composition of curried functions yields ${thirtyTwoer(2)}"

def volume = {h, w, l -> h * w * l}
def area = volume.curry(1)
def lengthPA = volume.curry(1, 1)
def lengthC = volume.curry(1).curry(1)

println "The volume of the 2x3x4 rectangle is ${volume(2, 3, 4)}"
println "The area of the 3x4 square is ${area(3, 4)}"
println "The length of the 6 line is ${lengthPA(6)}"
println "The length of the 6 line via curried function is ${lengthC(6)}"
```



```
def product = { x, y ->
    return x * y
}
```

return a version that always multiplies by 4

```
def quadrature = product.curry(4)
```



```
def quadrature_ = { y ->
    return 4 * y
}
```



```
def product = { x, y ->
    return x * y
}

def quadrate = product.curry(4)
def octate = product.curry(8)

println "4x4: ${quadrate.call(4)}"
println "5x8: ${octate(5)}"
```

# Currying vs partial application

```
def volume = {h, w, l -> h * w * l}
```



partial application

# Currying vs partial application

partial application

```
def volume = {h, w, l -> h * w * l}  
def area = volume.curry(1)  
def lengthPA = volume.curry(1, 1)  
def lengthC = volume.curry(1).curry(1)
```

currying

# function reuse

```
def adder = { x, y -> x + y}  
def inc = adder.curry(1)
```

```
def composite = { f, g, x -> return f(g(x))}  
def thirtyTwoer = composite.curry(quadrat, octate)
```

new, different  
tools

# currying (& recursion)

```
object CurryTest extends Application {  
  
  def filter(xs: List[Int], p: Int => Boolean): List[Int] =  
    if (xs.isEmpty) xs  
    else if (p(xs.head)) xs.head :: filter(xs.tail, p)  
    else filter(xs.tail, p)  
  
  def dividesBy(n: Int)(x: Int) = ((x % n) == 0)  
  
  val nums = List(1, 2, 3, 4, 5, 6, 7, 8)  
  println(filter(nums, dividesBy(2)))  
  println(filter(nums, dividesBy(3)))  
}
```



# Currying

```
object CurryTest extends Application {  
  
  def filter(xs: List[Int], p: Int => Boolean): List[Int] =  
    if (xs.isEmpty) xs  
    else if (p(xs.head)) xs.head :: filter(xs.tail, p)  
    else filter(xs.tail, p)  
  
  def dividesBy(n: Int)(x: Int) = ((x % n) == 0)  
  
  val nums = List(1, 2, 3, 4, 5, 6, 7, 8)  
  println(filter(nums, dividesBy(2)))  
  println(filter(nums, dividesBy(3)))  
}
```



# pure functions

# pure functions

no memory or  
i/o side effects

# purity

if the result isn't used, it can be removed

a particular invocation with a set of parameters returns a constant value

enables memoization

execution order can change

parallel execution

$$\frac{1}{\zeta + (\zeta^3)^{1/2}} \cdot \left( \frac{w(k+2)}{1+w^2} \right)^2 \cdot \beta^k R$$

recursion

$$w(k+1) = \sqrt{\zeta^3 - 4\zeta + \frac{9}{4}\zeta^2} - \frac{w^2 - 2\zeta}{1-w^2}$$

$$\frac{1}{\zeta + (\zeta^3)^{1/2}} \cdot \left( \frac{w(k+2)}{1+w^2} \right)^2 \cdot \beta^k R$$

# iteration & recursion

```
def perfectNumbers = [6, 28, 496, 8128]
```

```
def iterateList(listOfNums) {  
    listOfNums.each { n ->  
        println "${n}"  
    }  
}
```

```
iterateList(perfectNumbers)
```

```
def recurseList(listOfNums) {  
    if (listOfNums.size == 0) return;  
    println "${listOfNums.head()}"  
    recurseList(listOfNums.tail())  
}
```

```
recurseList(perfectNumbers)
```



# iterate a List

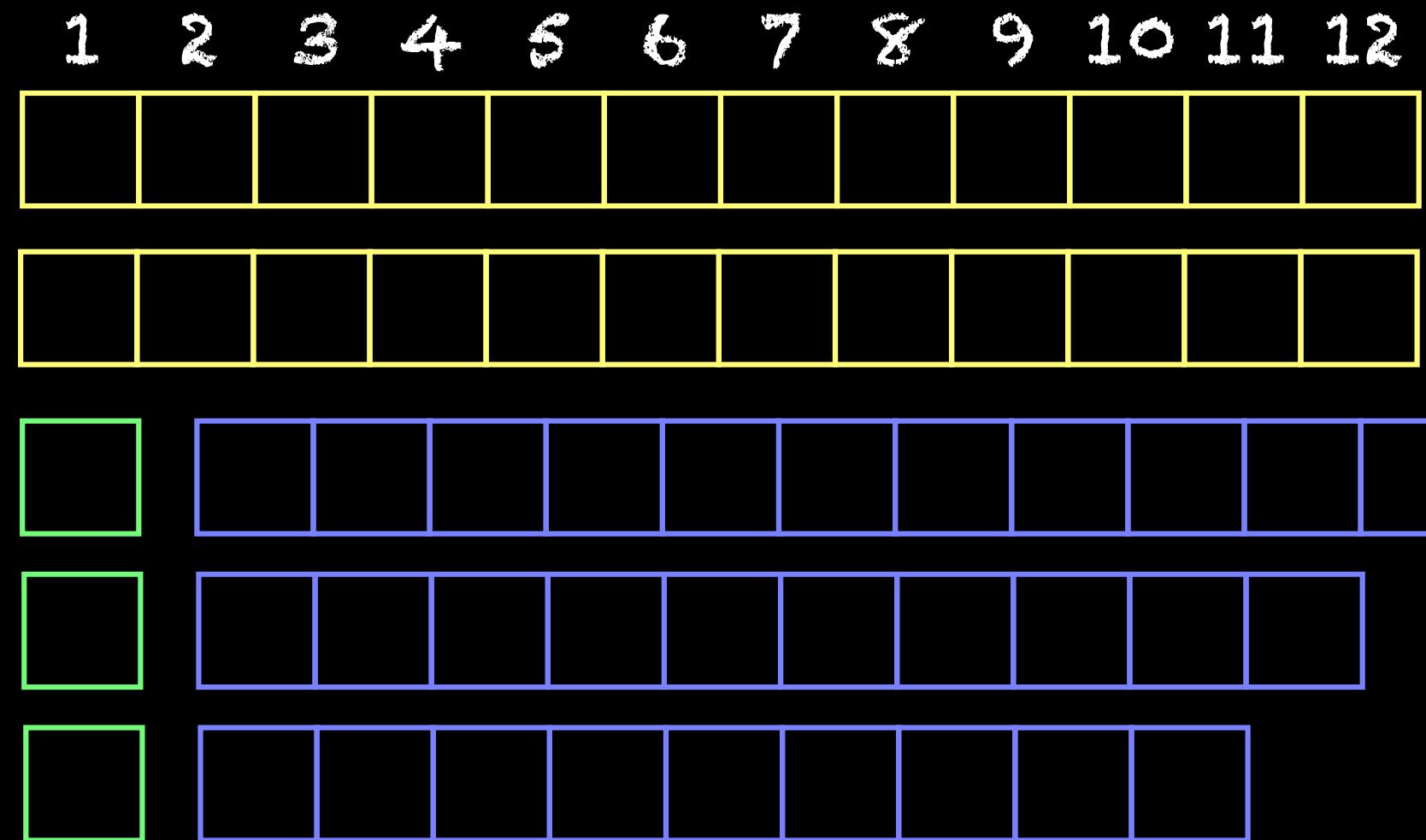
```
def perfectNumbers = [6, 28, 496, 8128]
```

```
def iterateList(listOfNums) {  
    listOfNums.each { n ->  
        println "${n}"  
    }  
}
```

```
iterateList(perfectNumbers)
```



# List perspective



# recurse a List

```
def recurseList(listOfNums) {  
    if (listOfNums.size == 0) return;  
    println "${listOfNums.head()}"  
    recurseList(listOfNums.tail())  
}
```

```
recurseList(perfectNumbers)
```



# iterative & recursive filtering



```
def filter(list, criteria) {  
    def new_list = []  
    list.each { i ->  
        if (criteria(i))  
            new_list << i  
    }  
    return new_list  
}  
  
modBy2 = { n -> n % 2 == 0}  
  
l = filter(1..20, modBy2)  
  
def filter(list, p) {  
    if (list.size() == 0) return list  
    if (p(list.head()))  
        [] + list.head() + filter(list.tail(), p)  
    else filter(list.tail(), p)  
}  
  
filter(1..20, {n-> n % 2 == 0}).each {i-> println "${i}"}
```

# iterative filtering

```
def filter(list, criteria) {  
    def new_list = []  
    list.each { i ->  
        if (criteria(i))  
            new_list << i  
    }  
    return new_list  
}
```

```
modBy2 = { n -> n % 2 == 0}
```

```
l = filter(1..20, modBy2)
```



# recursive filtering

```
def filter(list, p) {  
    if (list.size() == 0) return list  
    if (p(list.head()))  
        return [] + list.head() + filter(list.tail(), p)  
    else return filter(list.tail(), p)  
}
```



# functional vs imperative

```
def filter(list, p) {  
    if (list.size() == 0) return list  
    if (p(list.head()))  
        return [] + list.head() + filter(list.tail(), p)  
    else return filter(list.tail(), p)  
}
```

who's minding  
the state?

```
def filter(list, criteria) {  
    def new_list = []  
    list.each { i ->  
        if (criteria(i))  
            new_list << i  
    }  
    return new_list  
}
```

# recursive filtering

```
object CurryTest extends Application {  
  
  def filter(xs: List[Int], p: Int => Boolean): List[Int] =  
    if (xs.isEmpty) xs  
    else if (p(xs.head)) xs.head :: filter(xs.tail, p)  
    else filter(xs.tail, p)  
  
  def dividesBy(n: Int)(x: Int) = ((x % n) == 0)  
  
  val nums = List(1, 2, 3, 4, 5, 6, 7, 8)  
  println(filter(nums, dividesBy(2)))  
  println(filter(nums, dividesBy(3)))  
}
```

think about results,  
not steps

<http://www.scala-lang.org/node/135>



think about results,  
not steps

what about things you want to control?

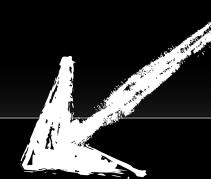
performance?

new, different  
tools

# imperative number classifier

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...  
  
    private void calculateFactors() {  
        for (int i = 2; i < sqrt(_number) + 1; i++)  
            if (isFactor(i))  
                addFactor(i);  
    }  
  
    private void addFactor(int factor) {  
        _factors.add(factor);  
        _factors.add(_number / factor);  
    }  
}
```

optimized!



# optimized functional classifier

```
public List<Integer> factorsOfOptimized(final int number) {  
    final List<Integer> factors = range(1, (int) round(sqrt(number) + 1))  
        .filter(new F<Integer, Boolean>() {  
            public Boolean f(final Integer i) {  
                return isFactor(number, i);  
            }  
        });  
    return factors.append(factors.map(new F<Integer, Integer>() {  
        public Integer f(final Integer i) {  
            return number / i;  
        }  
    }))  
        .nub();  
}
```

# optimized factors

```
public List<Integer> factorsOfOptimized(final int number) {  
    final List<Integer> factors = range(1, (int) round(sqrt(number) + 1))  
        .filter(new F<Integer, Boolean>() {  
            public Boolean f(final Integer i) {  
                return isFactor(number, i);  
            }  
        });  
    return factors.append(factors.map(new F<Integer, Integer>() {  
        public Integer f(final Integer i) {  
            return number / i;  
        }  
    }));  
}
```

think about results,  
not steps



special thanks to Michal Karwanski for optimizations to my optimizations

# post-imperative

Google challenged college grads to write code for 100 CPU computers...

...they failed

<http://broadcast.oreilly.com/2008/11/warning-x-x-1-may-be-hazardous.html>

ingrained imperativity

learn MapReduce

<http://code.google.com/edu/submissions/mapreduce-minilecture/listing.html>

sound familiar?

# Languages handle

garbage collection

concurrency

state

tests

iteration

...

time



$$\mathcal{F}(u, v, w) = \int \int \int_{-\infty}^{+\infty} f(x, y, z) \cdot \exp(2\pi i(ux + vy + wz)) \, dx \, dy \, dz$$
$$(u, v, w) = \int \int \int_{-\infty}^{+\infty} f(x, y, z) \cdot \exp(2\pi i(ux + vy + wz)) \, dx \, dy \, dz$$
$$u, v, w) = \int \int \int_{-\infty}^{+\infty} f(x, y, z) \cdot \exp(2\pi i(ux + vy + wz)) \, dx \, dy \, dz$$
$$, v, w) = \int \int \int_{-\infty}^{+\infty} f(x, y, z) \cdot \exp(2\pi i(ux + vy + wz)) \, dx \, dy \, dz$$
$$, w) = \int \int \int_{-\infty}^{+\infty} f(x, y, z) \cdot \exp(2\pi i(ux + vy + wz)) \, dx \, dy \, dz$$

**strict evaluation**

academia  
alert!



# strict evaluation

all elements  
pre-evaluated

divByZero

```
print length([2+1, 3*2, 1/0, 5-4])
```

=4



# non-strict evaluation

elements evaluated  
as needed



Laziness



# Lazy List

```
class LazyList {  
    private head, tail  
  
    LazyList(head, tail) {  
        this.head = head;  
        this.tail = tail  
    }  
  
    def LazyList getTail() { tail ? tail() : null }  
  
    def List getHead(n) {  
        def valuesFromHead = [];  
        def current = this  
        n.times {  
            valuesFromHead << current.head  
            current = current.tail  
        }  
        valuesFromHead  
    }  
  
    def LazyList filter(Closure p) {  
        if (p(head))  
            p.owner.prepend(head, { getTail().filter(p) })  
        else  
            getTail().filter(p)  
    }  
}
```



# Laziness

```
class LazyList {  
    private head, tail  
  
    LazyList(head, tail) {  
        this.head = head;  
        this.tail = tail  
    }  
  
    private head, tail  
    def List getHead(n) {  
        L  
        def valuesFromHead = [];  
        def current = this  
        n.times {  
            valuesFromHead << current.head  
            current = current.tail  
        }  
        valuesFromHead  
    }  
    def LazyList filter(Closure p) {  
        if (p(head))  
            p.owner.prepend(head, { getTail().filter(p) })  
        else  
            getTail().filter(p)  
    }  
}
```

# Lazy list in



```
def prepend(val, closure) { new LazyList(val, closure) }

def integers(n) { prepend(n, { integers(n + 1) }) }

@Test
public void lazy_list_acts_like_a_list() {
    def naturalNumbers = integers(1)
    assertEquals('1 2 3 4 5 6 7 8 9 10',
                naturalNumbers.getHead(10).join(' '))
    def evenNumbers = naturalNumbers.filter { it % 2 == 0 }
    assertEquals('2 4 6 8 10 12 14 16 18 20',
                evenNumbers.getHead(10).join(' '))
}
```



# Laziness

```
def prepend(val, closure) { new LazyList(val, closure) }

def integers(n) { prepend(n, { integers(n + 1) }) }

@Test
public void lazy_list_acts_like_a_list() {
    def naturalNumbers = integers(1)
    assertEquals('1 2 3 4 5 6 7 8 9 10',
                naturalNumbers.getHead(10).join(' '))
    def evenNumbers = naturalNumbers.filter { it % 2 == 0 }
    assertEquals('2 4 6 8 10 12 14 16 18 20',
                evenNumbers.getHead(10).join(' '))
}
```

# nomenclature



foldLeft()

inject()

filter()

findAll()

# Tersest NumberClassifier



```
class NumberClassifier {  
    static def factorsOf(number) {  
        (1..number).findAll { i -> number % i == 0 }  
    }  
  
    static def isPerfect(number) {  
        factorsOf(number).inject(0, {i, j -> i + j}) == 2 * number  
    }  
  
    static def nextPerfectNumberFrom(n) {  
        while (! isPerfect(++n)) ;  
        n  
    }  
}
```



# perfect #'s

```
class NumberClassifier {  
    static def factorsOf(number) {  
        (1..number).findAll { i -> number % i == 0 }  
    }  
  
    static def isPerfect(number) {  
        factorsOf(number).inject(0, {i, j -> i + j}) == 2 * number  
    }  
  
    static def nextPerfectNumberFrom(n) {  
        while (! isPerfect(++n)) ;  
        n  
    }  
}
```



# ∞ perfect # sequence

```
import static com.nealford.ft.allaboutlists.NumberClassifier.nextPerfectNumberFrom

def prepend(val, closure) { new LazyList(val, closure) }

def perfectNumbers(n) { prepend(n,
    { perfectNumbers(nextPerfectNumberFrom(n)) }) };

@Test
public void infinite_perfect_number_sequence() {
    def perfectNumbers =
        perfectNumbers(nextPerfectNumberFrom(1))
    assertEquals([6, 28, 496], perfectNumbers.getHead(3))
}
```

# ∞ Sequence

```
import static com.nealford.ft.allaboutlists.NumberClassifier.nextPerfectNumberFrom  
  
def prepend(val, closure) { new LazyList(val, closure) }  
  
def perfectNumbers(n) { prepend(n,  
  { perfectNumbers(nextPerfectNumberFrom(n)) }) };  
  
@Test  
public void infinite_perfect_number_sequence() {  
  def perfectNumbers =  
    perfectNumbers(nextPerfectNumberFrom(1))  
  assertEquals([6, 28, 496], perfectNumbers.getHead(3))  
}
```

new, different  
tools

# CONCURRENCY

$$\oint \mathcal{D} dA = \int_V \rho dV = Q$$

$$\oint \mathcal{E} dl = - \frac{d}{dt} \int_A \mathcal{B} dA$$

$$\oint \mathcal{B} dA = 0$$

$$\oint \mathcal{H} dl = \int_A \mathcal{J} dA + \frac{d}{dt} \int_A \mathcal{D} dA$$

<http://www.infoq.com/presentations/Simple-Made-Easy>

# Simple Made Easy

Rich Hickey



STATE

You're Doing It Wrong



# variables

assume 1 thread of control, 1 timeline

not atomic

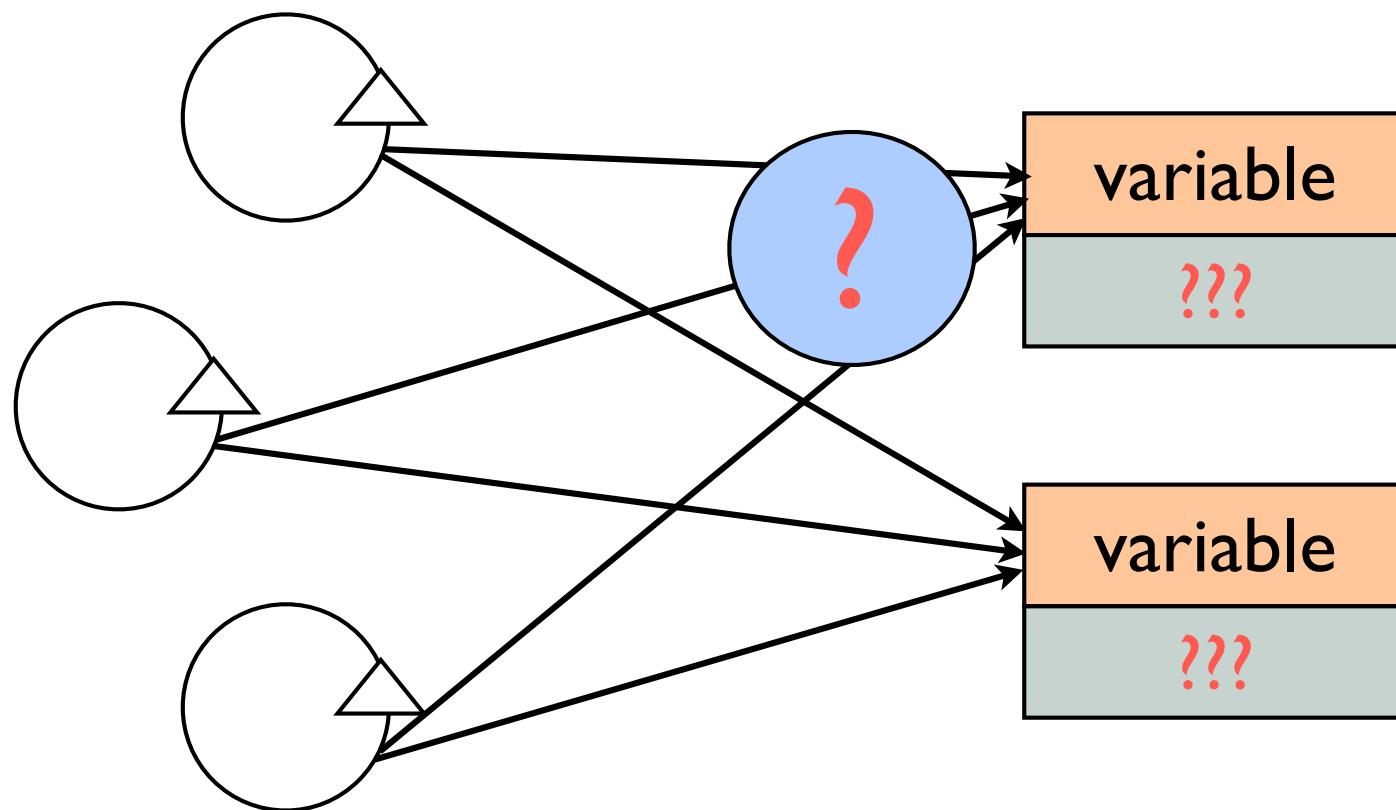


non-composable

subtle visibility rules

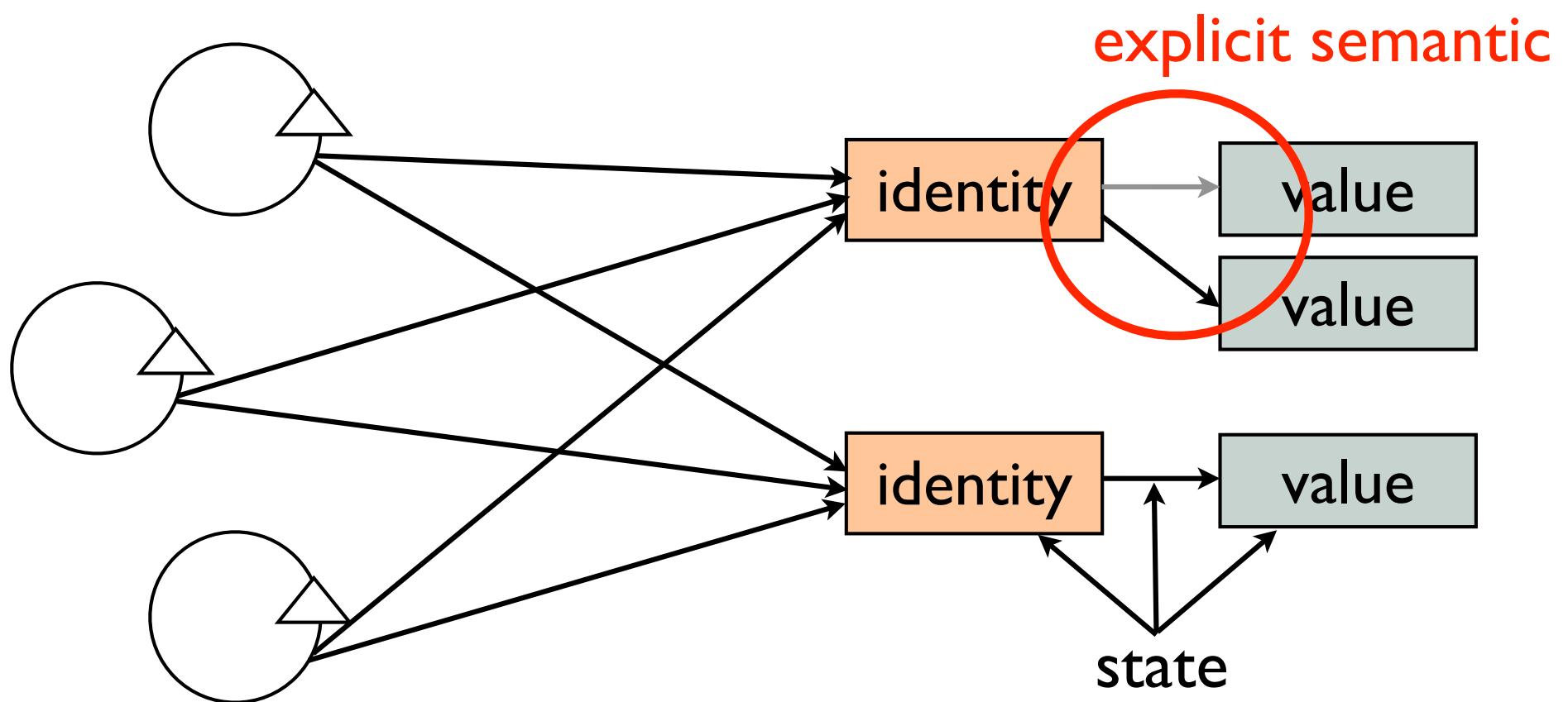
with concurrency: lock & pray

# Life w/ variables





# identity



# identity, state, ≠ time

term	meaning
value	immutable data in a persistent data structure
identity	series of causally related values over time
state	identity at a point in time
time	relative: before/simultaneous/after ordering of causal values

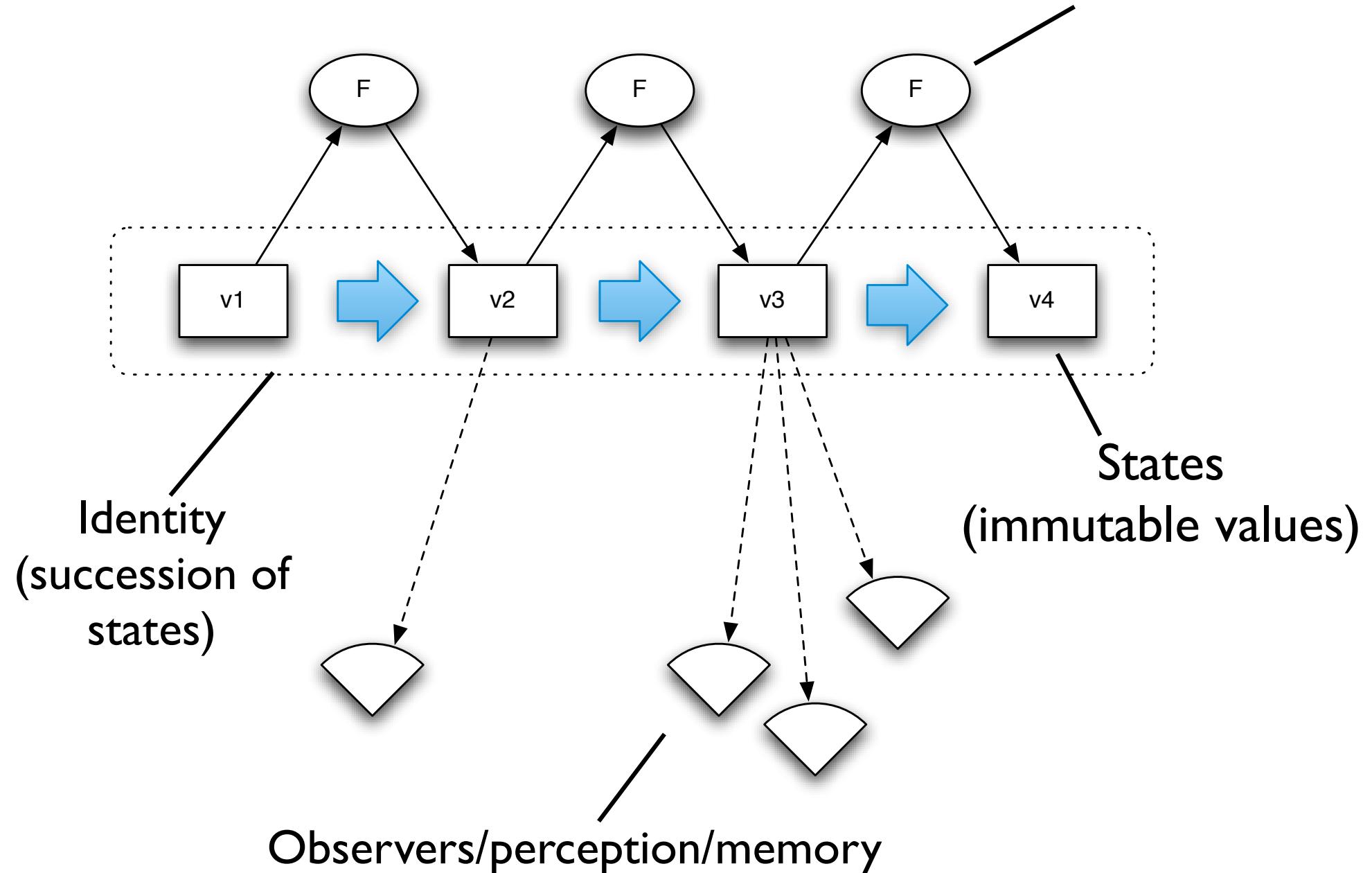


Clojure



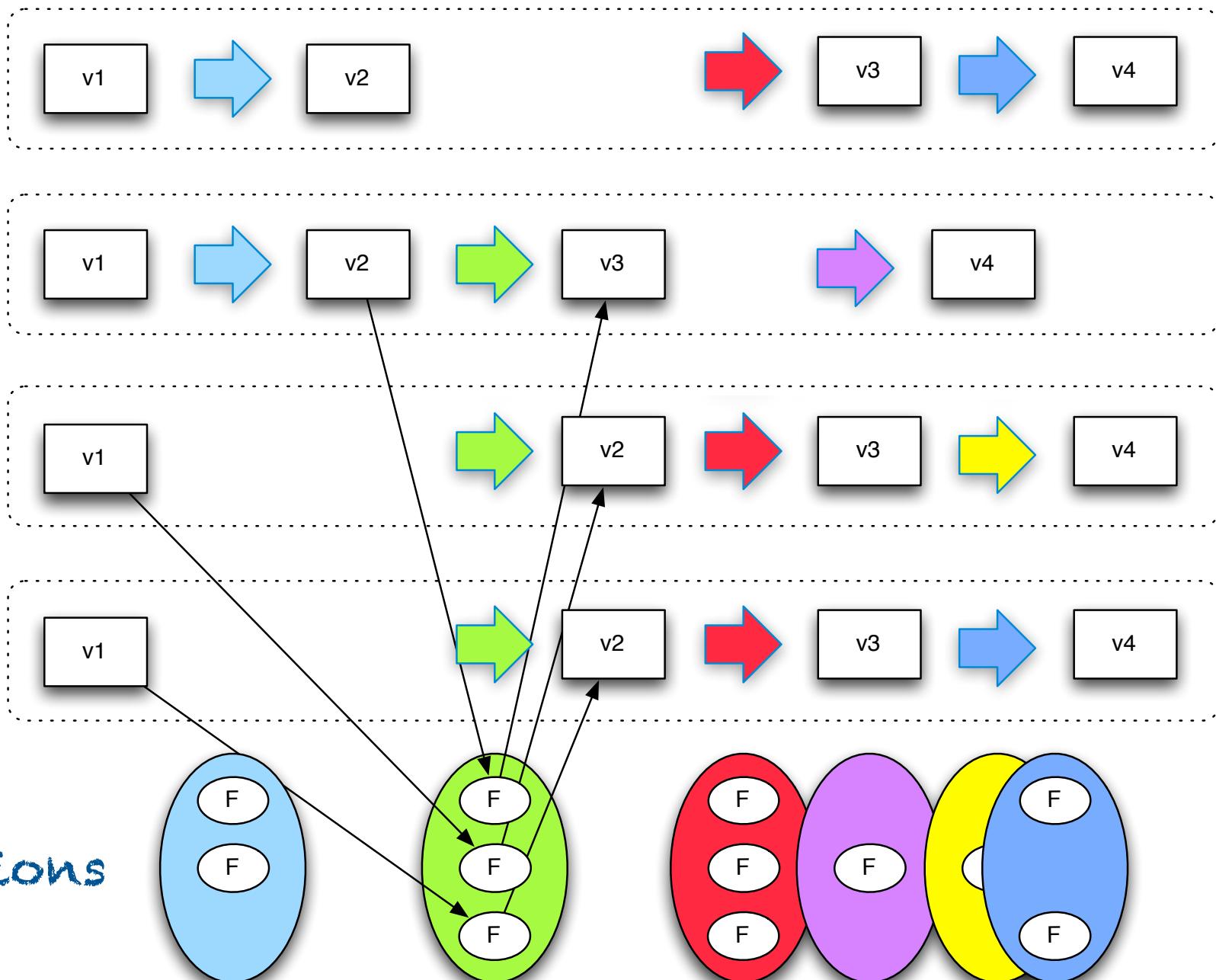
# Clojure time model

Process events  
(pure functions)





# Clojure's Software Transactional Memory



$$\frac{\delta_{ijt} = (v_{ijt} / \sum_{i=1}^n v_{ijt}) \times 100 - (r_{ijt} / \sum_{i=1}^n r_{ijt}) \times 100}{\sigma(\delta_{ij})}$$

actors

# PerfectNumber

```
import scala.actors.Actor._

object NumberClassifier extends Application {
  def isPerfect(candidate: Int) =
  {
    val RANGE = 1000000
    val numberOfPartitions = (candidate.toDouble / RANGE).ceil.toInt

    val caller = self

    for (i <- 0 until numberOfPartitions) {
      val lower = i * RANGE + 1;
      val upper = candidate min (i + 1) * RANGE

      actor {
        var partialSum = 0
        for(j <- lower to upper)
          if (candidate % j == 0) partialSum += j

        caller ! partialSum
      }
    }

    var responseExpected = numberOfPartitions
    var sum = 0
    while(responseExpected > 0) {
      receive {
        case partialSum : Int =>
          responseExpected -= 1
          sum += partialSum
      }
    }

    sum == 2 * candidate
  }

  println("6 is perfect? " + isPerfect(6))
  println("496 is perfect? " + isPerfect(496))
  println("33550336 is perfect? " + isPerfect(33550336))
  println("33550337 is perfect? " + isPerfect(33550337))
}
}
```



```

def isPerfect(candidate: Int) =
{
  val RANGE = 1000000
  val numberOfPartitions = (candidate.toDouble / RANGE).ceil.toInt

  val caller = self

  for (i <- 0 until numberOfPartitions) {
    val lower = i * RANGE + 1;
    val upper = candidate min (i + 1) * RANGE

    actor {
      var partialSum = 0
      for(j <- lower to upper)
        if (candidate % j == 0) partialSum += j

      caller ! partialSum
    }
  }

  var responseExpected = numberOfPartitions
  var sum = 0
  while(responseExpected > 0) {
    receive {
      case partialSum : Int =>
        responseExpected -= 1
        sum += partialSum
    }
  }

  sum == 2 * candidate
}

```

new, different  
tools



Thinking  
functionally



# immutability over state transitions

<http://www.ibm.com/developerworks/java/library/j-jtp02183/index.html>

# **immutable ...**

simple to construct & test

**automatically thread safe**

do not need a copy constructor

does not need an implementation of clone

make good Map keys & Set elements

no need for defensive copying

has “failure atomicity”

# immutable !

ensure the class cannot be overridden

make fields final

all state set in constructor

no mutating methods

defensively copy mutable object fields

Let the  
language  
manage scope  
as much as possible



```
@Immutable  
class Client {  
    String name, city, state, zip  
    List<String> streets  
}
```



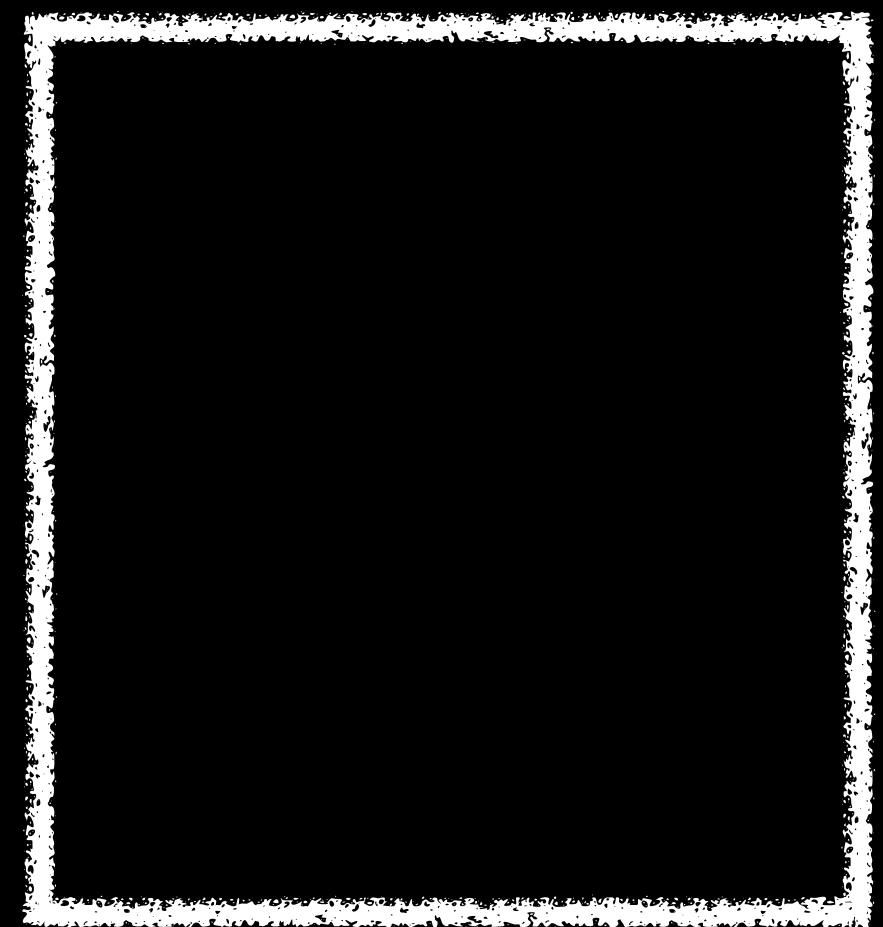
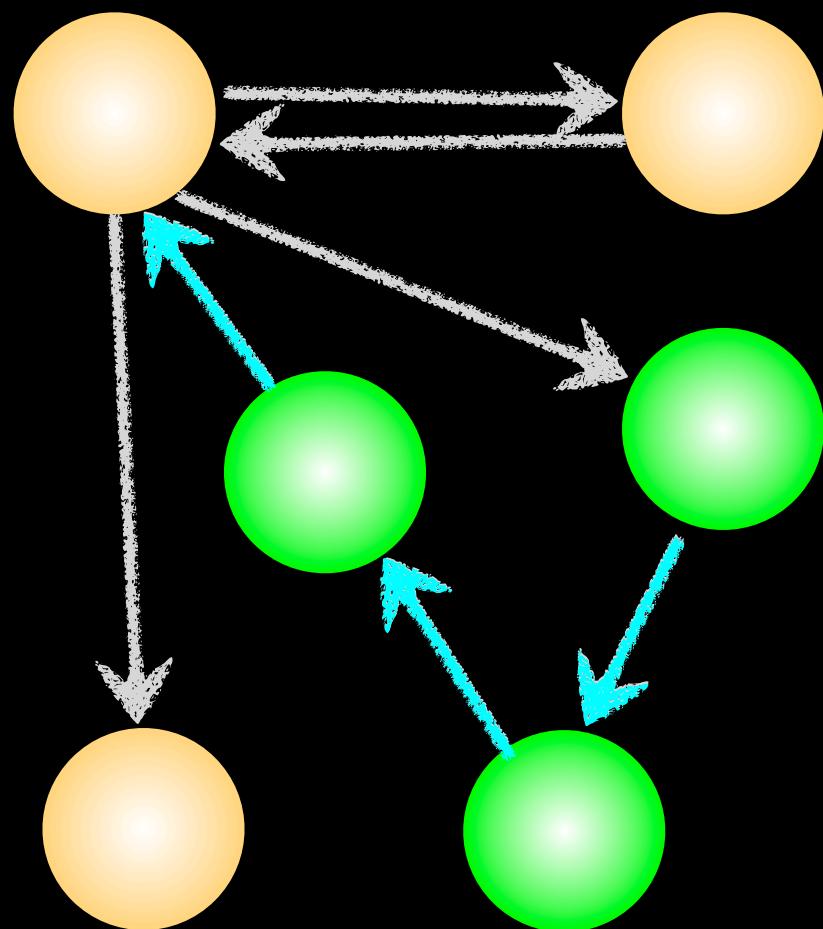
# @Immutable

properties have private, final backing fields  
updates result in `ReadOnlyPropertyException`  
map & tuple style constructors generated  
default `equals`, `hashCode`, `toString` methods  
defensive copies of mutable references  
Arrays & cloneables use `clone()`  
collections wrapped in immutable wrappers  
updates result in `UnsupportedOperationException`

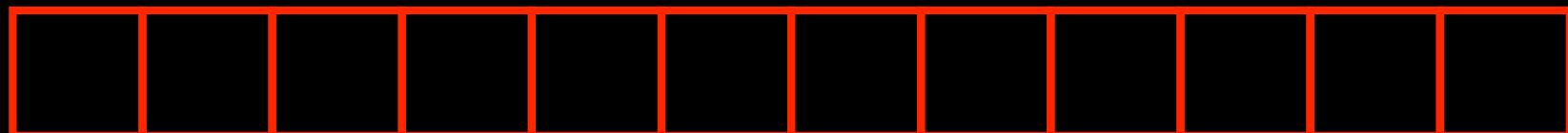
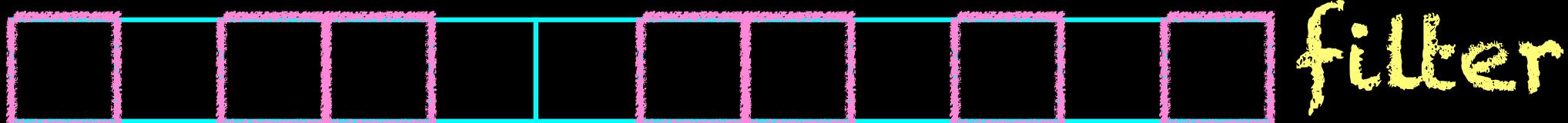
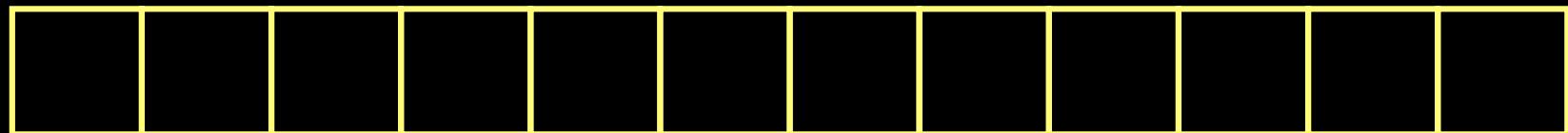
results  
over  
steps

composition  
over  
structure

# structural reuse



# functional reuse

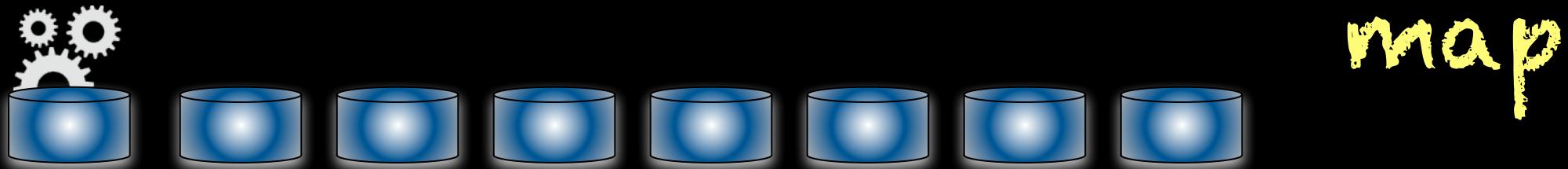
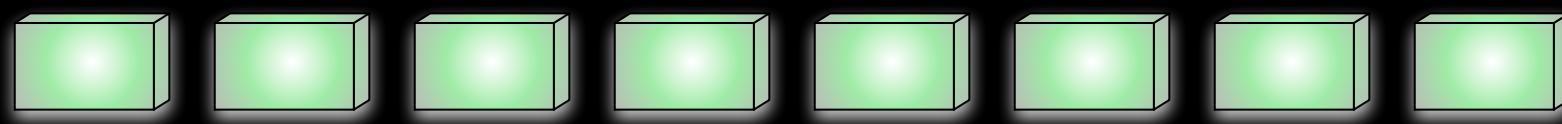
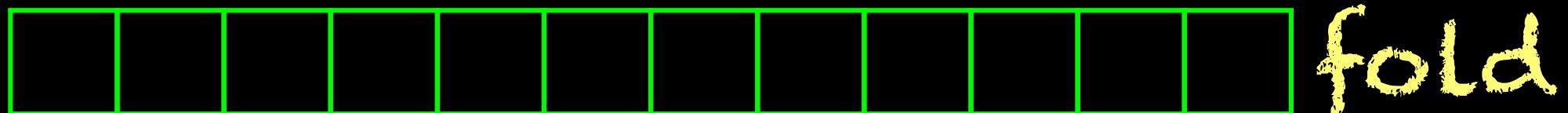
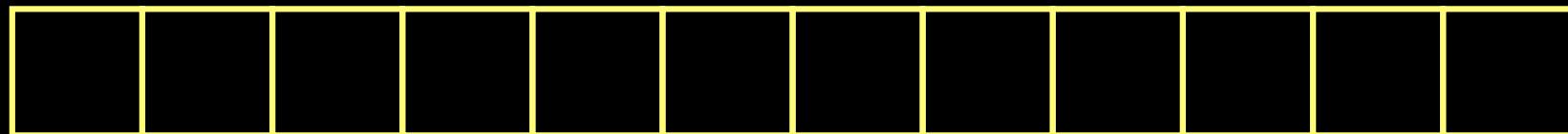


fold

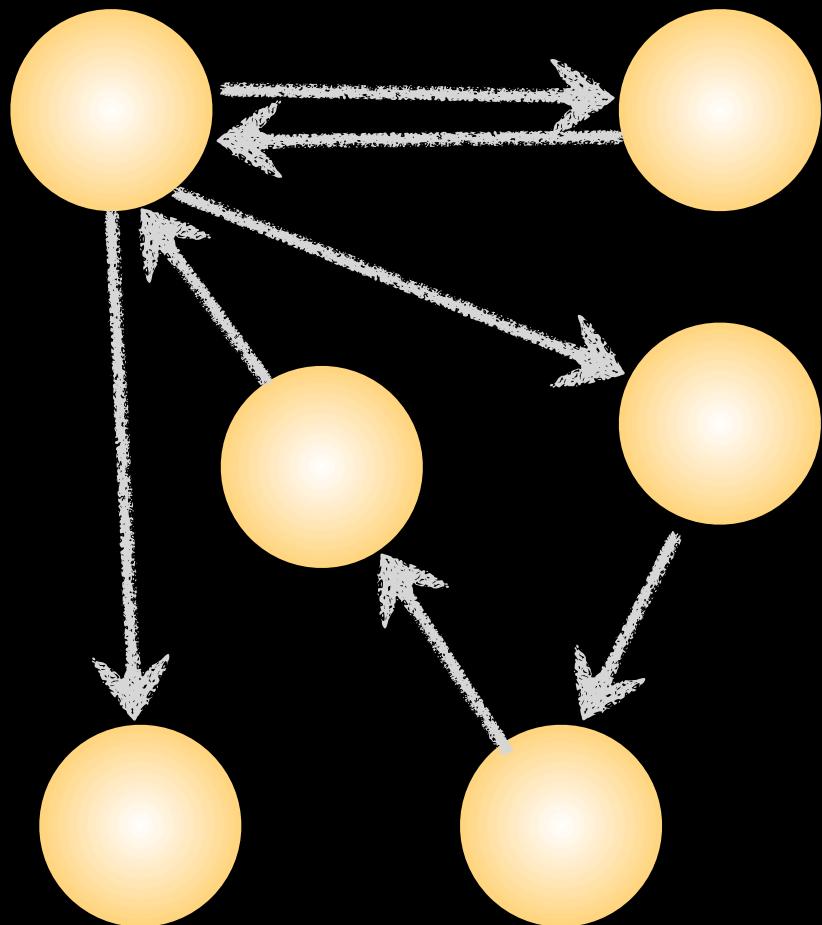
filter

map

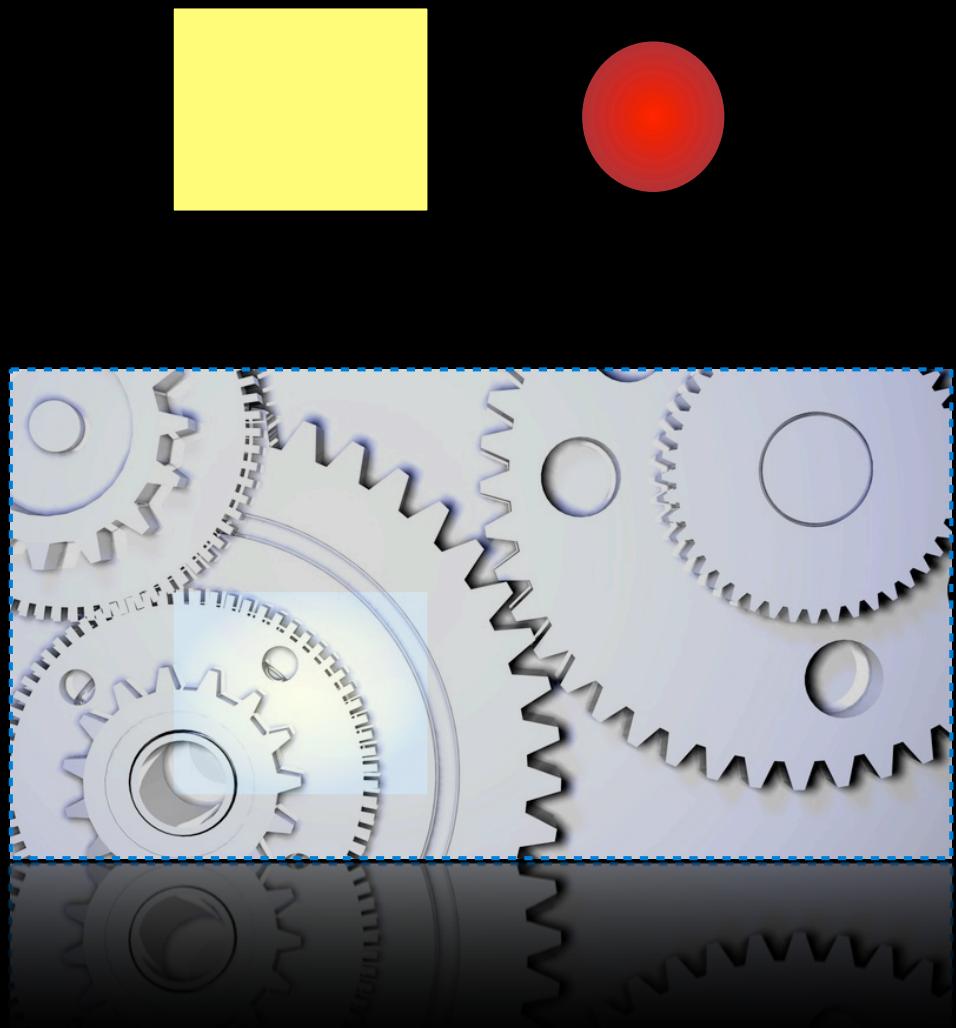
# functional reuse



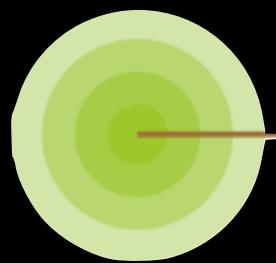
map



# composition



declarative  
over  
imperative



functional.  
j $\lambda$ v $\lambda$



paradigm  
over  
tool



Clojure

Scala

# summary

$$E=mc^2$$

# functional thinking

new ways of thinking

cede control to languages & runtimes

immediately beneficial beginning steps

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# Functional thinking: Thinking functionally, Part 1

## Learning to think like a functional programmer

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**Summary:** Functional programming has generated a recent surge of interest with claims of fewer bugs and greater productivity. But many developers have tried and failed to understand what makes functional languages compelling for some types of jobs. Learning the syntax of a new language is easy, but learning to *think* in a different way is hard. In the first installment of his *Functional thinking* column series, Neal Ford introduces some functional programming concepts and discusses how to use them in both Java™ and Groovy.

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Let's say for a moment that you are a lumberjack. You have the best axe in the forest, which makes you the most productive lumberjack in the camp. Then one day, someone shows up and extols the virtues of a new tree-cutting paradigm, the *chainsaw*. The sales guy is persuasive, so you buy a chainsaw, but you don't know how it works. You try hefting it and swinging at the tree with great force, which is how your other tree-cutting paradigm works. You quickly conclude that this newfangled chainsaw thing is just a fad, and you go back to chopping down trees with your axe. Then, someone comes by and shows you how to crank the chainsaw.

You can probably relate to this story, but with *functional programming* instead of a *chainsaw*. The problem with a completely new programming paradigm isn't learning a new language. After all, language syntax is just details. The tricky part is to learn to *think* in a different way. That's where I come in — chainsaw cracker and

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## About this series

This series aims to reorient your perspective toward a functional mindset, helping you look at common problems in new ways and find ways to improve your day-to-day coding. It explores functional programming concepts, frameworks that allow functional programming within the Java language, functional programming languages that run on the JVM, and some future-leaning directions of language design. The series is geared toward developers who know Java and how its abstractions work but have little or no experience using a functional language.

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