

$$-\frac{d}{dx} \left( k(x) \frac{du(x)}{dx} \right) = 100x$$

$$u(2) = 0$$

$$\frac{du(0)}{dx} + u(0) = 20$$

$$\Omega = \langle 0, 2 \rangle \ni x \longmapsto u(x) \in \mathbb{R}$$

$$k(x) = \begin{cases} 1 & \text{dla } x \in \langle 0, 1 \rangle \\ 2x & \text{dla } x \in (1, 2) \end{cases}$$

$$-\left[ k(x) u'(x) \right]' = 100x \quad | \cdot v(x), v \in V, V = \{ f \in H^1 : f(2) = 0 \}$$

$$-v(x) \left[ k(x) u'(x) \right]' = 100x v(x) \quad | \int_{\Omega} dx$$

$$-\int_0^2 v(x) \left[ k(x) u'(x) \right]' dx = \int_0^2 100x v(x) dx$$

$$\left| \begin{array}{ll} a = v(x) & a' = v'(x) \\ b' = \left[ k(x) u'(x) \right]' & b = k(x) u'(x) \end{array} \right|$$

$$-\left( \left[ v(x) k(x) u'(x) \right]_0^2 - \int_0^2 k(x) v'(x) u'(x) dx \right) = \int_0^2 100x v(x) dx$$

$$-\left( \overbrace{v(2)k(2)u'(2)}^0 - v(0) \overbrace{k(0)}^1 \overbrace{u'(0)}^{20-u(0)} - \int_0^2 k(x) v'(x) u'(x) dx \right) = \int_0^2 100x v(x) dx$$

$$v(0)(20 - u(0)) + \int_0^2 k(x) v'(x) u'(x) dx = \int_0^2 100x v(x) dx$$

$$20v(0) - u(0)v(0) + \int_0^2 k(x) v'(x) u'(x) dx = \int_0^2 100x v(x) dx \quad | -20v(0)$$

$$-u(0)v(0) + \int_0^2 k(x) v'(x) u'(x) dx = -20v(0) + \int_0^2 100x v(x) dx$$

$$\underbrace{\hspace{15em}}_{B(u,v)} \quad \underbrace{\hspace{15em}}_{L(v)}$$

$$B(u,v) = L(v)$$