

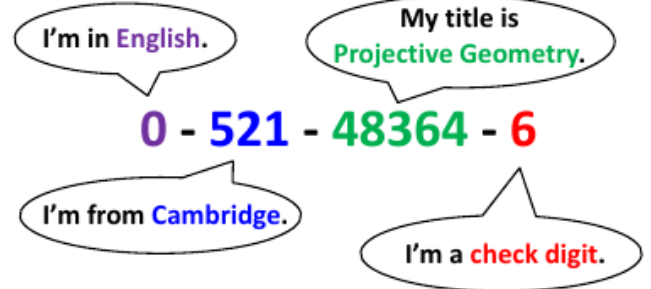
ISBN Numbers

ISBN (International Standard Book Number):

- A 10-digit or 13-digit number that identifies a book for purposes of commerce and supply chains
- The last digit of the ISBN is a check digit used to detect transcription errors.
- This last digit is sometimes an X (representing the number 10).

An ISBN has 4 parts:

- group/country identifier: 0 or 1 for English, 2 for French, 3 for German, 4 for Japanese, 8 for Indian
- publisher identifier
- title identifier
- check digit



10-Digit ISBN:

The sum of the digits multiplied by 1-10 respectively should add to a multiple of 11.

$$\text{Last digit} = 1 \times 1^{\text{st}} \text{ digit} + 2 \times 2^{\text{nd}} \text{ digit} + 3 \times 3^{\text{rd}} \text{ digit} + 4 \times 4^{\text{th}} \text{ digit} + 5 \times 5^{\text{th}} \text{ digit} + 6 \times 6^{\text{th}} \text{ digit} + 7 \times 7^{\text{th}} \text{ digit} + 8 \times 8^{\text{th}} \text{ digit} + 9 \times 9^{\text{th}} \text{ digit} \pmod{11}$$

- ISBN: 3-540-56489-6

$$\begin{aligned} \text{Last Digit} &= 1 \times 3 + 2 \times 5 + 3 \times 4 + 4 \times 0 + 5 \times 5 + 6 \times 6 + 7 \times 4 + 8 \times 8 + 9 \times 9 \pmod{11} \\ &= 3 + 10 + 12 + 0 + 25 + 36 + 28 + 64 + 81 \pmod{11} \\ &= 259 \pmod{11} \\ &= 6 \end{aligned}$$

- ISBN: 1st nine digits are _____

$$\begin{aligned} \text{Last digit} &= 1 \times \underline{\hspace{1cm}} + 2 \times \underline{\hspace{1cm}} + 3 \times \underline{\hspace{1cm}} + 4 \times \underline{\hspace{1cm}} + 5 \times \underline{\hspace{1cm}} \\ &\quad + 6 \times \underline{\hspace{1cm}} + 7 \times \underline{\hspace{1cm}} + 8 \times \underline{\hspace{1cm}} + 9 \times \underline{\hspace{1cm}} \pmod{11} \\ &= \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \\ &\quad \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}} + \underline{\hspace{1cm}} \pmod{11} \\ &= \underline{\hspace{2cm}} \pmod{11} = \underline{\hspace{1cm}} \end{aligned}$$

- ISBN: 1st nine digits are _____

$$\begin{aligned}
 \text{Last digit} &= 1 \times \underline{\quad} + 2 \times \underline{\quad} + 3 \times \underline{\quad} + 4 \times \underline{\quad} + 5 \times \underline{\quad} \\
 &\quad + 6 \times \underline{\quad} + 7 \times \underline{\quad} + 8 \times \underline{\quad} + 9 \times \underline{\quad} \pmod{11} \\
 &= \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \\
 &\quad \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} \pmod{11} \\
 &= \underline{\quad} \pmod{11} = \underline{\quad}
 \end{aligned}$$

Question: How many 10-digit ISBNs are there?

Books published since January 2007 are required to have 13-digit ISBNs.

For a 13-digit ISBN, the last digit is found as follows:

Let

$a = 1^{\text{st}} \text{ digit} + 3^{\text{rd}} \text{ digit} + 5^{\text{th}} \text{ digit} + 7^{\text{th}} \text{ digit} + 9^{\text{th}} \text{ digit} + 11^{\text{th}} \text{ digit},$

$b = 2^{\text{nd}} \text{ digit} + 4^{\text{th}} \text{ digit} + 6^{\text{th}} \text{ digit} + 8^{\text{th}} \text{ digit} + 10^{\text{th}} \text{ digit} + 12^{\text{th}} \text{ digit},$

$c = a + (3 \times b),$ and

$d = c \pmod{10}.$

Then last digit = $10 - d.$

Let's try it:

1st 12 digits _____

$$a = \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = \underline{\quad},$$

$$b = \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = \underline{\quad},$$

$$c = \underline{\quad} + (3 \times \underline{\quad}) = \underline{\quad}, \text{ and}$$

$$d = \underline{\quad} \pmod{10} = \underline{\quad}.$$

$$\text{Then last digit} = 10 - \underline{\quad} = \underline{\quad}.$$

