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```

1 Basic

1.1 vimrc

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```
set nocompatible
set t_Co=256
set nu
set ai
set tabstop=4
set shiftwidth=4
set softtabstop=4
colorscheme torte
syntax on
filetype plugin indent on
```

1.2 default

```
#include<bits/stdc++.h>
using namespace std;
#define FI freopen("in.txt", "r", stdin)
#define F0 freopen("out.txt", "w", stdout)
#define IOS ios_base::sync_with_stdio(0);cin.tie(0)
#define pb push_back
#define mp make_pair
#define ff first
#define ss second
typedef long long LL;
const int MOD = 10000000007;
const double PI = acos(-1.0);
int dx[] = \{-1,0,1,0\};
int dy[] = \{0,1,0,-1\};
int main(){
    IOS;
    return 0;
}
```

1.3 FastInput

```
int readInt () {
  bool minus = false;
  int result = 0;
  char ch;
  ch = getchar();
  while (true) {
  if (ch == '-') break;
  if (ch >= '0' && ch <= '9') break;</pre>
    ch = getchar();
  if (ch == '-') minus = true; else result = ch-'0';
  while (true) {
     ch = getchar();
     if (ch < '0' || ch > '9') break;
    result = result*10 + (ch - '0');
  if (minus)
     return -result;
  else
     return result;
}
```

1.4 Int128

```
std::ostream::sentry s(dest);
    if (s) {
          _uint128_t tmp = value < 0 ? -value : value;
        char buffer[128];
        char* d = std::end(buffer);
             --d;
             *d = "0123456789"[tmp % 10];
             tmp \neq 10;
        } while (tmp != 0);
         if (value < 0) {
             --d;
             *d = '-';
        int len = std::end(buffer) - d;
        if (dest.rdbuf()->sputn(d, len) != len) {
             dest.setstate(std::ios_base::badbit);
    return dest;
}
__int128 parse(string& s) {
      int128 ret = 0;
    for (int i = 0; i < s.length(); i++)
if ('0' <= s[i] && s[i] <= '9')
             ret = 10 * ret + s[i] - '0';
    return ret;
}
int main()
{
    string s = "187821878218782187821878218782";
    _{-}int128 x = parse(s);
    \_int128 y = 1ULL << 63;
    __int128 z = 1ULL << 63;
    x *= 2;
    cout << x << endl;</pre>
    cout << y << endl;</pre>
    cout << y * z << endl;</pre>
```

2 Java

2.1 template

```
/* Compile: javac %
 * Run: java [Class name] */
import java.util.*;
import java.lang.*;
import java.math.*;
import java.io.*;
class Main {
  public static void main (String[] args) {
    System.out.print(1);
    System.out.print(2)
    System.out.println("Hello World");
    System.out.printf("%.2f", 0.12345);
    Scanner sc = new Scanner(System.in);
    System.out.println(sc.nextLine()); //gets()
    System.out.println(sc.next()); //scanf("%s")
    System.out.println(sc.nextInt())
    System.out.println(sc.nextDouble());
    while(sc.hasNext()) { //EOF
       int a = sc.nextInt()
       System.out.println(a);
    int[] a = {1,2,3};
int[][] b = {{1,2},{3,4,5}};
double[] c = new_double[90];
    System.out.print(b[0][1]);
    System.out.print(b[1][2]);
    int[] d = \{5,2,1,3,4\};
```

```
Integer[] e = \{6,3,4,1,2\};
    Arrays.sort(d);
    Arrays.sort(e, new MyCom());
    for(int i=0; i<d.length; i++) {</pre>
      System.out.print(d[i]);
    for(int i=0; i<e.length; i++) {</pre>
      System.out.print(e[i]);
    Set<String> s = new HashSet<String>(); //or TreeSet
s.add("123");
    s.add("234");
    System.out.println(s);
    System.out.println(s.contains("123"));
    Map<String, Integer> m = new TreeMap<String,</pre>
         Integer>();
    m.put("haha", 123);
m.put("hehe", 234);
    System.out.println(m);
    BigInteger b1 = new BigInteger("
         -1231237182379123712");
    BigInteger b2 = BigInteger.value0f(234);
    System.out.println(b1.add(b2));
    System.out.println(b1.mod(b2));
    int z = Integer.parseInt("-123");
    System.out.println(z);
    System.out.println(Math.PI);
    System.out.println(Math.sin(1));
  static class InputReader {
    public BufferedReader reader;
    public StringTokenizer tokenizer;
    public InputReader(InputStream stream) {
      reader = new BufferedReader(new InputStreamReader
           (stream), 32768);
      tokenizer = null;
    public String next() {
      while (tokenizer == null || !tokenizer.
          hasMoreTokens()) {
         try {
           tokenizer = new StringTokenizer(reader.
               readLine());
        } catch (IOException e) {
           throw new RuntimeException(e);
      return tokenizer.nextToken();
    public int nextInt() {
      return Integer.parseInt(next());
    public double nextDouble(){
      return Double.parseDouble( next() );
  static class MyCom implements Comparator<Integer> {
    public int compare(Integer i1, Integer i2) {
      return i2 - i1;
  }
}
```

3 Data Structure

3.1 Disjoint Set

```
struct DisjointSet{
   int p[N];
```

```
void init(int n){for(int i=1;i<=n;i++)p[i] = i;}</pre>
    int Find(int x){return x == p[x] ? x : p[x] = Find(
        p[x]); }
    void Union(int x,int y){p[Find(x)] = Find(y);}
};
```

3.2 Segment Tree

```
struct Node{
    int value, lazy;
    Node *lc,*rc;
    Node()\{value = 0; lc = rc = NULL; lazy=0\}
    void pull(){ value = lc->value+rc->value; }
    void push(){
        if(lc) lc->lazy=lazy;
        if(rc)rc->lazy=lazy;
        //value may should be update need [L,R];
        lazy=0;
    }
int v[N];
Node* build(int L,int R){
    Node *node = new Node();
    if(L == R){
        node \rightarrow value = v[L];
        return node;
    int mid = (L+R)>>1;
    node->lc = build(L,mid);
    node->rc = build(mid+1,R);
    node->pull();
    return node;
void modify(Node *node,int L,int R,int i,int d){
    if(L == R){
        node->value += d;
        return;
    int mid = (L+R)>>1;
    if(i<=mid)modify(node->lc,L,mid,i,d);
    else modify(node->rc,mid+1,R,i,d);
    node->pull();
int query(Node* node,int L,int R,int ql,int qr){
    if(ql > R || qr < L)return 0;
    if(ql <= L && R <= qr)return node->value;
    int mid = (L+R)>>1;
    return query(node->lc,L,mid,ql,qr)+query(node->rc,
        mid+1,R,ql,qr);
}
```

Binary Index Tree

```
int A[N+1]; // one-based
inline int lower_bit(int x){ return x&-x; }
int sum(int x){
    int s = 0;
    while(x > 0){
        s += A[x];
        x -= lower_bit(x);
    return s;
void add(int x,int d){
    while(x <= N){
        A[x] += d;
        x += lower_bit(x);
    }
}
int query(int a,int b){
    if(a > b) swap(a,b)
    return sum(b)-sum(a-1);
```

3.4 zkw Segment Tree.cpp

```
const int NUM = 100;
int M,A[NUM],T[NUM*4];
// 2
// 2
// 4 5 6 7
// x 1 2 x
// one-based
void Build(int N){
    while(M=1;M<N+2;M<<=1);
for(int i=1;i<=N;i++) T[M+i] = A[i];</pre>
     for(int i=M-1;i;i--) T[i] = T[i<-1]+T[i<<1|1];
}
// Single modify
void Modify(int x,int d){
    T[x+=M] = d;
     for(x>1;x;x>>=1) T[x] = T[x<<1]+T[x<<1|1];
// Range query
int Query(int L,int R){
    L = L+M-1;R = R+M+1;
     int ans = 0;
     for(;L^R^1;L>>=1,R>>=1){
         if(\simL&1) ans += T[\stackrel{\wedge}{L}^1];
         if( R&1) ans += T[R^1];
     return ans;
}
```

```
3.5 Treap
struct Treap {
    int key, pri , val ,sz , lazy;
Treap *l, *r;
Treap(int _key, int _val): key(_key) , val(_val)
         pri(rand()) , sz(1), lazy(0), l(NULL), r(NULL){
inline int Size(Treap* t)
    return t?t->sz:0;
inline void Pull(Treap* t)
{
    t\rightarrow sz = Size(t\rightarrow l) + Size(t\rightarrow r) + 1;
}
void Push(Treap* t)
    t->val += t->lazy;
    if (t->l)t->l->lazy += t->lazy;
    if (t->r)t->r->lazy += t->lazy;
    t \rightarrow lazy = 0;
Treap* Merge(Treap* a, Treap* b)
    if (!a | | !b) return a ? a : b;
    if (a->pri > b->pri) {
         a->r = Merge(a->r, b); Pull(a); return a;
    } else {
         b->l = Merge(a, b->r);Pull(b);return b;
void Split(Treap* t, int k, Treap*& a, Treap*& b)
    if (!t) a = b = NULL;
    else {
      if (t->key <= k) {
             a = t; Split(t->r, k, a->r, b); Pull(a);
         } else {
             b = t; Split(t->1, k, a, b->1); Pull(b);
         }
    }
Treap* Del(Treap* t, int k) //delete all key=k
```

3.6 monotonic-queue

```
template <typename Item>
struct mqueue {
    deque<Item> data, aux;
    void push(Item& x)
    {
        data.push_back(x);
        while (!aux.empty() && aux.back() < x)</pre>
            aux.pop_back();
        aux.push_back(x);
    void pop()
    {
        if (data.front() == aux.front())
            aux.pop_front();
        data.pop_front();
    }
    int size()
    {
        return data.size();
    Item max()
    {
        return aux.front();
    }
};
```

4 Graph

4.1 BCC

```
int adj[9][9];
int visit[9], low[9], t = 0;
int stack[9], top = 0;
int contract[9];
void DFS(int i, int p)
    visit[i] = low[i] = ++t;
    stack[top++] = i; // push i
for (int j=0; j<9; ++j)
         if (adj[i][j]){
              if (!visit[j]) DFS(j, i);
                  tree edge
              if (!(j == p && adj[i][j] == 1))
                               // tree edge + back edge
                  low[i] = min(low[i], low[j]);
                                   // 形成BCC i點會是BCC裡
    if (visit[i] == low[i])
         面,最早拜訪的點
    {
         int_j;
         do {
              j = stack[--top];
                                     // pop j
              contract[j] = i;
         } while (i != j);
    }
}
```

4.2 SCC

```
vector<int> e[10000];int visit[10000], low[10000];bool
     instack[10000];int belong[10000];stack<int> s;
 int t;;int num; //number of SCC
void DFS(int u)
{
    visit[u] = low[u] = ++t; //進行標號
s.push(u); instack[u] = true;
     for (int i = 0; i < e[u].size(); i++) {
         int v = e[u][i];
         if (!visit[v])
             DFS(v); low[u] = min(low[u], low[v]); // 找
                   u 的最上層祖先
         if (instack[v]) low[u] = min(low[u], visit[v]);
               //還在stack中 用 visit的值
     if (visit[u] == low[u]){//SCC
         num++; int v = s.top(); s.pop();
         instack[v] = false; belong[v] = num;
         while (v != u) {
             v = s.top();
                            s.pop();
             belong[v] = num; instack[v] = false;
     }
int Tarjan(int n) //n:number of vertex 0-based
     t = 0, num = 0;
     memset(visit, 0, sizeof(visit));
     for (int i = 0; i < n; i++) e[i].clear();
for (int i = 0; i < n; i++)
         if (!visit[i]) DFS(i);
     return num:
}
```

4.3 SPFA

```
struct Edge {
    int v,cost;
    Edge(int _v=0,int _cost=0):v(_v),cost(_cost){}
vector<Edge> E[MAXN]; //MAXN:num of point
bool visited[MAXN];int cnt[MAXN];int dist[MAXN];
bool SPFA(int start , int n)
    memset(visited,0,sizeof(visited))
    for(int i=1;i<n;i++) dist[i]=INT_MAX;</pre>
    visited[start]=true,dist[start]=0;
    queue<int> que;
    while(!que.empty()) que.pop();
    que.push(start); cnt[start]=1;
    while(!que.empty()){
        int u=que.front();
        que.pop();
visited[u]=false;
        for(int i=0;i<E[u].size();i++){</pre>
             int v=E[u][i].v;
             if(dist[u]!=INT_MAX && dist[v]>dist[u]+E[u
                 ][i].cost){
                 dist[v]=dist[u]+E[u][i].cost;
                 if(!visited[v]) {
                     visited[v]=true;
                     que.push(v);
                     if(++cnt[v]>n) return false; //有負
                 }
```

```
}
}
return true; //正常
}
```

4.4 Dijkstra

```
int* Dijkstra(vector<VPII> E,int N,int S){
   bool *visit=new bool[N+1];for(int i=1;i<=N;i++)
        visit[i]=false;
   int *D=new int[N+1];for(int i=1;i<=N;i++)D[i]=INF;
   priority_queue<PII,VPII,greater<PII>> P;
   P.push(MP(0,S));D[S]=0;
   while(!P.empty()){
        int weight=P.top().ff,now=P.top().ss;P.pop();
        if(visit[now])continue;
        visit[now]=true;
        for(auto i:E[now]){
            int potential=D[now]+i.ff;
            if(!visit[i.ss] && potential < D[i.ss]){
                P.push(MP(D[i.ss]=potential,i.ss));
            }
        }
    }
   return D;
}</pre>
```

4.5 Floyd-Warshall

```
#include<bits/stdc++.h>
const int N = 500;
int dp[N][N];
void floyd_warshall()
{
    for (int k = 0; k < N; k++)
        for (int i = 0; i < N; i++)
        for (int j = 0; j < N; j++)
        if(dp[i][k]!=INT_MAX && dp[k][j]!=INT_MAX);
        dp[i][j] = min(dp[i][j], dp[i][k] + dp[k][j]);
}</pre>
```

4.6 Bipartite Match

```
#include <bits/stdc++.h>
using namespace std;
vector<int> g[10000];
bool check[10000];
int match[10000];
int num_left, num_right;
void init(int n)
    num_left = num_right = 0;
    for (int i = 0; i < n; i++)
        g[i].clear();
bool DFS(int u)
{
    for (int i = 0; i < g[u].size(); i++) {
        int v = g[ú][i];
        if (!check[v]) {
            check[v] = true;
if (match[v] == -1 || DFS(match[v]))
                 {
                     match[v] = u;
                     match[u] = v;
                     return true;
        }
    return false;
int Hungarian_DFS() //匈牙利算法
{
    int ans = 0;
```

```
memset(match, -1, sizeof(match));
    for (int i = 0; i < num_left; i++) { //只要對二分圖
         的一邊即可
        memset(check, 0, sizeof(check));
        if (DFS(i))
            ans++;
    return ans;
int Hungarian_BFS()
    int prev[10000];
    int ans = 0;
    memset(match, -1, sizeof(match));
    for (int i = 0; i < num_left; i++) {
        memset(check, 0, sizeof(check));
        if (match[i] == -1) {
            queue<int> q;
            q.push(i);
            prev[i] = -1;
            bool flag = false;
            while (!q.empty() && !flag) {
                 int u = q.front();
                 q.pop();
                 for (int j = 0; j < g[u].size() && !
                     flag; j++) {
int v = g[u][j];
                     if (!check[v]) {
                         check[v] = true;
                         if (match[v] != -1) {
                             q.push(match[v]);
                             prev[match[v]] = u;
                         } else {
                             flag = true;
                             int^{-}d = u, e = v;
                             while (d != -1) {
                                  int t = match[d];
                                 match[d] = e;
                                 match[e] = d;
                                 d = prev[d];
                                 e = t;
                             }
                         }
                     }
                 }
             if (match[i] != -1)
                 ans++;
        }
    return ans;
}
```

4.7 KM

```
#include <bits/stdc++.h>
using namespace std;
const int MAXN = 110;
int n;
int g[MAXN][MAXN], lx[MAXN], ly[MAXN];
int match[MAXN], slack[MAXN];
bool vsx[MAXN], vsy[MAXN];
bool find(int x)
{
    if(vsx[x]) return false;
    vsx[x] = 1;
    for (int i = 0; i < n; i++) {
         if (vsy[i])
             continue:
         int t = lx[x] + ly[i] - g[x][i];
         if (!t) {
             vsy[i] = 1;
             if (match[i] == -1 || find(match[i])) {
                  match[x] = i;
                  return true;
         } else
             slack[i] = min(slack[i], t);
    }
```

```
return false;
int km(bool MIN = false) //二分圖最大匹配
{
     if (MIN)
          for (int i = 0; i < n; i++)
               for (int j = 0; j < n; j++)
g[i][j] = -g[i][j];
     fill(lx, lx + n, INT_MAX);
     fill(ly, ly + n, 0);

for (int i = 0; i < n; i++)

for (int j = 0; j < n; j++)
               lx[i] = min(lx[i], g[i][j]);
     memset(match, -1, sizeof(match));
for (int i = 0; i < n; i++) {</pre>
          for (int j = 0; j < n; j++)
               fill(slack, slack + n, INT_MAX);
          while (true) {
               memset(vsx, 0, sizeof(vsx));
               memset(vsy, 0, sizeof(vsy));
               if (find(i))
                    break
               int d = INT_MAX;
               for (int j = 0; j < n; j++)
                    if (!vsy[j])
                         d = min(d, slack[j])
               for (int j = 0; j < n; j++) {
                    if (vsx[j])
                         lx[j] -= d;
                    if (vsy[j])
                         ly[j] += d;
                    else
                         slack[j] -= d;
               }
          }
     }
     int sum = 0;
     for (int i = 0; i < n; i++)
          sum += g[match[i]][i];
     if (MIN) {
          sum = -sum;
          for (int i = 0; i < n; i++)

for (int j = 0; j < n; j++)

g[i][j] = -g[i][j];
     return sum;
}
```

4.8 General-Match

```
#include <bits/stdc++.h>
using namespace std;
struct DisjointSet {
    int N;
    vector<int> p;
   DisjointSet(int n)
        : N(n)
        , p(vector<int>(N))
    {
        init();
    void init()
    {
        for (int i = 0; i < N; i++)
            p[i] = i;
    int find(int x)
        return p[x] == x ? x : p[x] = find(p[x]);
    void U(int a, int b)
        p[find(b)] = find(a);
   }
struct GMatch {
   int N:
    vector<vector<int> > vc;
    DisjointSet djs;
    vector<int> m, d, c1, c2, p, vis;
```

```
queue<int> q;
int ts:
GMatch(int n)
    : N(n)
    , vc(vector<vector<int> >(N + 1))
    , djs(DisjointSet(N))
     ts(0)
void add(int a, int b)
    vc[a].push_back(b);
    vc[b].push_back(a);
void path(int x, int r)
    if(x == r)
        return;
    if (d[x] == 0) {
        int i = p[x], j = p[p[x]];
        path(j, r);
        m[i] = j, m[j] = i;
    } else if (d[x] == 1) {
        int i = c1[x], j = c2[x];
        path(i, m[x]);
        path(j, r);
m[i] = j, m[j] = i;
    }
void blossom(int x, int y, int bi)
    for (int i = djs.find(x); i != bi; i = djs.find
        (p[i])) {
        djs.U(bi, i);
        if (d[i] == 1)
            c1[i] = x, c2[i] = y, q.push(i);
int lca(int x, int y, int r)
    ts++
    vis[r] = ts;
    for (int i = djs.find(x); i != r; i = djs.find(
        p[i]))
        vis[i] = ts;
    int b:
    for (b = djs.find(y); vis[b] != ts; b = djs.
        find(p\lceil b\rceil)
    return b;
bool Match(int x)
    djs.init();
    d = vector < int > (N + 1, -1);
    d[x] = 0;
    q = queue<int>();
    q.push(x);
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        for (int v : vc[u]) {
            if (m[v] != v \&\& djs.find(u) != djs.
                 find(v)) {
                 if (d[v] == -1) {
                     if (m[v] == -1) {
                         path(u, x);
                         m[u] = v, m[v] = u;
                         return true;
                     } else {
                         p[v] = u, p[m[v]] = v;
                         d[v] = 1, d[m[v]] = 0;
                         q.push(m[v]);
                     }
                } else {
                     if (d[djs.find(v)] == 0) {
                         int bi = lca(u, v, x);
                         blossom(u, v, bi);
                         blossom(v, u, bi);
```

```
}
                 }
             }
         return false;
     int Solve()
         m = c1 = c2 = d = p = vis = vector < int > (N + 1,
              -1);
         int ans = 0;
         for (int i = 0; i < N; i++) {
             if (m[i] == -1) {
                  if (Match(i))
                      ans++;
                 else
                      m[i] = i;
         }
         return ans;
    }
|};
```

4.9 Directed-MST

```
const int MAXN = 1010;
int pre[MAXN], min_dist[MAXN];
struct Edge {
    int from, to, cost;
    Edge() {}
    Edge(int _from, int _to, int _cost)
        : from(_from)
        , to(_to)
        , cost(_cost)
vector<Edge> E;
int solve(int n, int m, int root)
    int ans = 0:
    while (true) {
        fill(min_dist, min_dist + MAXN, INT_MAX);
for (int i = 0; i < E.size(); i++) {</pre>
            int u = E[i].from, v = E[i].to, cost = E[i]
                 ].cost;
            if (cost < min_dist[v] && v != u) {</pre>
                 min_dist[v] = cost;
                 pre[v] = u;
        for (int i = 1; i <= n; i++)
            if (min_dist[i] == INT_MAX && i != root)
                 return -1;
        ans += min_dist[i];
            int v = i;
            while (vis[v] != i && id[v] == -1 && v !=
                 root) {
                 vis[v] = i;
                 v = pre[v];
             if (id[v] == -1 && v != root) {
                 for (int u = v; u != v; u = pre[u])
                     id[u] = cnt_node;
                 cnt_node++;
        if (cnt_node == 1)
        break;
for (int i = 1; i <= n; i++)
   if (id[i] == -1)</pre>
                 id[i] = cntnode++;
        for (int i = 0; i < E.size(); i++) {
            int v = E[i].to;
```

4.10 LCA

```
#include <bits/stdc++.h>
using namespace std;
const int MAXN = 1000;
vector<int> tree[MAXN];
int depth[MAXN]
int father[MAXN][20];
void init()
     memset(depth, 0, sizeof(depth));
    memset(father, -1, sizeof(father));
void dfs(int u)
     for (int i = 0; i < tree[u].size(); i++) {</pre>
         int v = tree[u][i];
         if (!depth[v]) {
              depth[v] = depth[u] + 1;
              father[v][0] = u;
              dfs(v);
         }
    }
void build()
    for (int i = 1; (1 << i) < MAXN; i++) {
    for (int j = 0; j < MAXN; j++) {
        if (father[j][i - 1] != -1) {</pre>
                   father[j][i] = father[father[j][i -
                        1]][i - 1];
              }
         }
    }
int lca(int u,int v)
     if(depth[u]<depth[v]) swap(u,v);</pre>
     for(int i =log2(MAXN-1);i>=0;i--)
          if( father[u][i]!=-1 && depth[father[u][i]]>=
              depth[v]) u=father[u][i];
     if(u==v) return v;
     for(int i=log2(MAXN-1);i>=0;i--)
         if(father[u][i]!=father[v][i])
              u=father[u][i],v=father[v][i];
    return father[u][0];
```

4.11 MST-kruskal

```
#include<bits/stdc++.h>
using namespace std;
const int N=20005;
struct Edge{
   int u,v,cost;
   Edge(int _u=0,int _v=0,int _cost=0){
        u=_u,v=_v,cost=_cost;
   }
   bool operator < (const Edge & a) const{
        return cost<a.cost;
   }
};
vector<Edge> E;
```

```
int ds[N];
void Init (int n){
    E.clear();
    for(int i=0;i<n;i++) ds[i]=i;</pre>
int Find(int x){
    return (ds[x]==x)?x:(ds[x]=Find(ds[x]));
int kruskal(int n) //point_number;
    sort(E.begin(),E.end());
    int ans=0;
    int num=1;
    for( auto &e : E ){
         int u=e.u,v=e.v
        u=Find(u);v=Find(v);
        if(u!=v){
             ds[u]=v;
             num++:
             ans+=e.cost;
         if(num==n) break;
    return ans;
}
```

4.12 Manhattan-Mst

```
#include <bits/stdc++.h>
using namespace std;
const int N = 100100;
struct Point {
    int x, y, id;
Point(int _x, int _y, int _id)
    : x(_x)
    , y(_y)
      id(_id)
    bool operator<(const Point& p) const</pre>
        return (x != p.x) ? x < p.x : y < p.y;
};
struct BIT {
    int min_val, pos;
    void init()
    {
        min_val = INT_MAX;
        pos = -1;
} bit[N];
struct Edge {
    int u, v, d;
Edge() {}
    Edge(int _u, int _v, int _d)
    : u(_u)
    , v(_v)
      d(_d)
    bool operator<(const Edge& e) const
        return d < e.d;</pre>
vector<Point> p;
vector<Edge> E;
int ds[N]; //disjoint set for kruskal
void add_edge(int u, int v, int d)
    E.push_back(Edge(u, v, d));
int find(int x)
{
    return ds[x] = (x == ds[x] ? x : find(ds[x]));
```

```
int dist(int i, int j)
     return abs(p[i].x - p[j].x) + abs(p[i].y - p[j].y);
inline int lowbit(int x)
{
    return x & (-x);
void update(int x, int val, int pos)
     for (int i = x; i >= 1; i -= lowbit(i)) {
         if (val < bit[i].min_val)</pre>
             bit[i].min_val = val, bit[i].pos = pos;
int query(int x, int m)
     int min_val = INT_MAX, pos = -1;
     for (int i = x; i <= m; i += lowbit(i)) {</pre>
         if (bit[i].min_val < min_val) {</pre>
             min_val = bit[i].min_val, pos = bit[i].pos;
     return pos;
int Manhattan_MST(vector<Point>& P)
     int n = P.size();
     for (int dir = 0; dir < 4; dir++) {</pre>
         if (dir == 1 || dir == 3) {
              for (int i = 0; i < n; i++)
                  swap(P[i].x, P[i].y);
         } else if (dir == 2) {
    for (int i = 0; i < n; i++)</pre>
                  P[i].x = -P[i].x;
         }
         int T[N], hs[N];
         sort(P.begin(), P.end());
for (int i = 0; i < n; i++) { //discretize</pre>
             T[i] = hs[i] = p[i].y - p[i].x;
         sort(hs, hs + n);
         int m = unique(hs, hs + n) - hs;
         for (int i = 1; i <= m; i++)
         bit[i].init();
for (int i = n - 1; i >= 0; i--) {
              int pos = lower_bound(hs, hs + m, T[i]) -
                  hs + 1; //Bit is 1-based
              int w = query(pos, m);
              if (w != -1)
                  add_edge(p[i].id, p[w].id, dist(i, w));
             update(pos, p[i].x + p[i].y, i);
     sort(E.begin(), E.end());
     int ans = 0;
     int p = 1;
     for (int i = 0; i < n; i++)
         ds[i] = i;
    for (int i = 0; i < (int)E.size() && p <= n; i++) {
  int fa = find(E[i].u);</pre>
         int fb = find(E[i].v);
         if (fa != fb) {
             p++
             ds[fa] = fb;
             ans += E[i].d;
         }
     return ans;
}
4.13 Flow-Dinic
```

```
#include <bits/stdc++.h>
#define pb push_back
#define SZ(x) (int)x.size()
using namespace std;
struct Dinic {
    struct Edge {
```

```
int v, f, re;
Edge(int v, int f, int re)
                                                                int cap; //容量
                                                                int cost;
            : v(v)
                                                                int next; //下一條邊的
            , f(f)
                                                            } e[N * N];
            , re(re)
                                                            int id;
                                                            int p[N];
        }
                                                            int pre[N]
    };
                                                            int path[N];
    vector<vector<Edge> > E;
                                                            int dist[N]; //dist;
    vector<int> level;
    int N, s, t;
Dinic(int N, int s, int t)
                                                            void init() //初始化
                                                            {
        : N(N)
                                                                memset(e, 0, sizeof(e));
        , s(s)
                                                                memset(p, -1, sizeof(p));
                                                                id = 0;
        , t(t)
                                                            void add(int u, int v, int cap, int cost)
        E.resize(N + 1);
    void AddEdge(int u, int v, int c)
                                                                e[id].v = v, e[id].cap = cap, e[id].cost = cost, e[
                                                                     id].next = p[u], p[u] = id++
                                                                 e[id].v = u, e[id].cap = 0, e[id].cost = -cost, e[
        E[u].pb({v, c, SZ(E[v])});
        E[v].pb({u, 0, SZ(E[u]) - 1});
                                                                     id].next = p[v], p[v] = id++;
    bool BFS()
                                                            bool SPFA(int s, int t)
                                                                memset(pre, -1, sizeof(pre));
fill(dist, dist + N, INT_MAX);
        level.clear();
        for (int i = 0; i \leftarrow N; i++)
            level.pb(-1);
                                                                bool vis[N]={};
        queue<int> Q;
                                                                dist[s] = 0;
        Q.push(s);
                                                                queue<int> q;
                                                                q.push(s);
        level[s] = 0;
        while (!Q.empty()) {
                                                                vis[s]=true;
            int now = Q.front();
                                                                while (!q.empty()) {
                                                                    int u = q.front();
            Q.pop();
             for (auto i : E[now]) {
                                                                     q.pop();
                 if (i.f > 0 && level[i.v] == -1) {
                                                                     vis[u]=false;
                     level[i.v] = level[now] + 1;
                                                                     for (int i = p[u]; i != -1; i = e[i].next) {
                                                                         Q.push(i.v);
                 }
            }
                                                                             dist[v] = dist[u] + e[i].cost;
        }
        return level[t] != -1;
                                                                             pre[v] = u; //路徑
                                                                             path[v] = i; //邊的編號
    int DFS(int now, int nf)
                                                                             if(!vis[v])
                                                                             vis[v]=true,q.push(v);
        if (now == t)
                                                                         }
            return nf;
                                                                    }
        int ans = 0;
        for (auto& i : E[now]) {
                                                                if (pre[t] == -1)
                                                                     return false;
            if (i.f > 0 \&\& level[i.v] == level[now] +
                 1) {
                                                                return true;
                 int tf = DFS(i.v, min(nf, i.f));
                                                            int MinCostFlow(int s, int t)
                 ans += tf;
                nf -= tf;
i.f -= tf;
                                                                int cost = 0;
                E[i.v][i.re].f += tf;
                                                                int flow = 0;
                                                                while (SPFA(s, t)) {
                 if (nf == 0)
                                                                     int f = INT_MAX;
                     return ans;
            }
                                                                     for (int u = t; u != s; u = pre[u])
                                                                         f = min(f, e[path[u]].cap);
        if (!ans)
                                                                     flow+=f;
             level[now] = -1;
                                                                     cost+=dist[t]*f;
                                                                     for(int u=t;u!=s;u=pre[u]){
        return ans;
                                                                         e[path[u]].cap-=f;
    int Flow()
                                                                         e[path[u]^1].cap+=f;
        int ans = 0;
        while (BFS())
                                                                return cost; //cost
            ans += DFS(s, INT_MAX);
                                                            }
        return ans;
    }
};
                                                                     HeavyLight-Decomposition
```

4.14 Flow-MinCost

```
#include <bits/stdc++.h>
using namespace std;
const int N = 1000;
struct Edge {
   int v; //連的點
```

```
#include <bits/stdc++.h>
using namespace std;
const int MAXN = 3000;
int size[MAXN], pre[MAXN], son[MAXN], dep[MAXN];
vector<int> E[MAXN];
struct Node{ // segmnet tree with lazy tag;
    Node * 1 ,* r;
    int v,lazy;
```

```
}*root;
//1-based;
int dfs(int x, int fa)
    size[x] = 1;
int max_v = INT_MIN;
    dep[x] = dep[fa] + 1;
    pre[x]=fa;
    for(auto &v:E[x]){
        size[x] += dfs(v, x);
        if (size[v] > max_v) {
            \max_{v} = \text{size}[v];
             son[x] = v;
    }
    return size[x];
int no,pos[MAXN],top[MAXN];
int repos(int x ,int fa,int tp){
    pos[x]=++no;
    top[x]=tp;
    if(son[x]) repos(son[x],x,tp);
    for(auto &v:E[x]){
        if(v!=son[x] \& v!=fa) repos(v,x,v);
// 1-based segment tree
void update_seg(Node* root,int l,int r ,int ql,int qr ,
    int v){
void query_seg(Node* root,int l,int r ,int ql,int qr){
void update(int x, int y,int v)
    while(top[x]!=top[y]){
        if(dep[x]<dep[y]) swap(x,y);</pre>
        update_seg(root,1,MAXN,pos[top[x]],pos[x],v);
        x=pre[top[x]];
    update_seg(root,1,MAXN,min(pos[x],pos[y]),max(pos[x
        ],pos[y]),v);
//query from x to y
void query(int x ,int y){
    int ans:
    while(top[x]!=top[y]){
        if(dep[x]<dep[y]) swap(x,y);</pre>
        ans+=query_seg(root,1,MAXN,pos[top[x]],pos[x]);
        x=pre[top[x]];
    ans+=query_seg(root,1,MAXN,min(pos[x],pos[y]),max(
        pos[x],pos[y]));
}
```

4.16 Maximal-Clique

5 String Theory

5.1 KMP

```
// Complexity : O(T+P)
void predo(string pattern,int dp[]){
    dp[0] = 0;
    for(int i=1;i<pattern.size();i++){</pre>
        dp[i] = dp[i-1];
        if(pattern[dp[i]] == pattern[i]) dp[i]++;
    }
void KMP(string text,string pattern){
    int dp[pattern.size()];predo(pattern,dp);
    for(int i=0,match=0;i<text.size();i++){
   while(match > 0 && pattern[match] != text[i])
            match = dp[match-1];
        if(pattern[match] == text[i]) match++;
        if(match == pattern.size()){
            // do something with i-pattern.size()+1
            match = dp[match-1];
        }
    }
}
```

5.2 Z

5.3 Trie

```
const int MAXCHAR = 10;
const char CHAR = '0';

struct Node{
   Node* child[MAXCHAR];
   int N;
   Node():N(0){for(int i=0;i<MAXCHAR;i++)child[i] =
        NULL;}
};
Node* root = new Node;
void word(string s){</pre>
```

```
Node* now = root;
for(int i=0;i<s.size();i++){
    int c = s[i] - CHAR;
    if(now->child[c] == NULL)now->child[c] = new
        Node;
    now = now->child[c];
}
now->N++;
}
void release(Node* now = root){
    for(int i=0;i<MAXCHAR;i++)if(now->child[i])release(
        now->child[i]);
    delete now;
}
```

5.4 AC automaton

```
const int MAXCHAR = 26;
const char CHAR = 'a';
struct Node{
    Node* child[MAXCHAR];
Node* fail;
    int N:
    Node():N(-1),fail(NULL){for(int i=0;i<MAXCHAR;i++)
         child[i] = NULL;}
};
struct AC{
    Node* root;
    AC(){root = new Node;}
    void word(string s,int index){
         Node* now = root;
         for(int i=0;i<s.size();i++){</pre>
             int c = s[i] - CHAR;
             if(now->child[c] == NULL)now->child[c] =
                 new Node;
             now = now->child[c];
         if(now->N == -1)now->N = index;
     void predo(){
         root->fail = NULL;
         Node* p;
         queue<Node*> Q;
         Q.push(root);
         while(!Q.empty()){
             Node* now = Q.front();Q.pop();
             for(int i=0;i<MAXCHAR;i++){</pre>
                  if(!now->child[i])continue;
                 Q.push(now->child[i]);
                 p = now->fail;
                 while(p != NULL && p->child[i] == NULL)
                      p = p \rightarrow fail;
                  if(p == NULL)now->child[i]->fail = root
                 else now->child[i]->fail = p->child[i];
             }
         }
     void match(string text){
         Node* now = root;
         for(int i=0;i<text.size();i++){</pre>
             int c = text[i] - CHAR;
             while(now != root && now->child[c] == NULL)
                  now = now->fail;
             if(now->child[c])now = now->child[c];
             if(now->N != -1)cout << "Got you" << endl;</pre>
     void release(Node* now = root){
         for(int i=0;i<MAXCHAR;i++)if(now->child[i])
             release(now->child[i]);
         delete now;
    }
};
```

5.5 Suffix Array

```
int SA[MAXNUM],H[MAXNUM];
void SuffixArray(string text){
     int N = text.size(),A = 128;
    int SA2[MAXNUM],rank[MAXNUM],rank2[MAXNUM],radix[
         : [MUNXAM
     for(int i=0;i<A;i++)radix[i] = 0;</pre>
     for(int i=0;i<N;i++)radix[rank[i] = text[i]]++;</pre>
     for(int i=0;i<A;i++)radix[i] += radix[i-1];</pre>
     for(int i=N-1;i>=0;i--)SA[--radix[text[i]]] = i;
     for(int power=1;power<N;power<<=1){</pre>
         for(int i=0;i<A;i++)radix[i] = 0;</pre>
         for(int i=0;i<N;i++)radix[rank[i]]++;</pre>
         for(int i=0;i<A;i++)radix[i] += radix[i-1];</pre>
         int now = 0;
         for(int i=N-power;i<N;i++)SA2[now++] = i;
for(int i=0;i<N;i++){</pre>
              if(SA[i]-power >= 0)SA2[now++] = SA[i]-
         for(int i=N-1;i>=0;i--)SA[--radix[rank[SA2[i
              ]]]] = SA2[i];
         rank2[SA[0]] = now = 0;
         for (int i=1;i<N;i++){</pre>
             if (!(rank[SA[i-1]] == rank[SA[i]] && SA[i
                  -1]+power < N && SA[i]+power < N &&
                  rank[SA[i-1]+power] == rank[SA[i]+power
                  1))now++
             rank2[SA[i]] = now;
         swap(rank, rank2);
         if(now == N-1)break;
         A = now+1;
     for(int i=0;i<N;i++)rank[SA[i]] = i;
    for(int i=0,k=0;i<N;i++,k?k--:0){
   if(rank[i] == 0){H[rank[i]] = 0;continue;}</pre>
         int j = SA[rank[i]-1];
         while(i+k < N && j+k < N && text[i+k] == text[j
              +k])k++;
         H[rank[i]] = k;
    }
}
```

6 Geometry

6.1 Point

```
#include<bits/stdc++.h>
using namespace std;
const double EPS =1e-6;
int dcmp(double x)
    if (fabs(x) < EPS)
        return 0;
    else
        return x < 0 ? -1 : 1;
struct Point {
    double x, y;
Point() { x = 0, y = 0; }
    Point(double _x, double _y)
        X = _X;
        y = _y;
    Point operator+(const Point& b)
        return Point(x + b.x, y + b.y);
    Point operator-(const Point& b) const
        return Point(x - b.x, y - b.y);
    Point operator*(double p)
```

```
{
        return Point(x * p, y * p);
    Point operator/(double p)
    {
        return Point(x / p, y / p);
    double operator ^ (const Point & b) const {
        return x*b.y-y*b.x;
    bool operator<(const Point& b)</pre>
        return x < b.x | | (x == b.x \&\& y < b.y);
    bool operator==(const Point& b)
        return dcmp(x - b.x) == 0 \&\& dcmp(y - b.y) ==
            0;
typedef Point Vector;
double dot(Vector v1, Vector v2)
    return v1.x * v2.x + v1.y * v2.y;
double cross(Point& o, Point& a, Point& b) //OA X OB
    return (a.x - o.x) * (b.y - o.y) - (a.y - o.y) * (b.y - o.y)
        .x - o.x);
double cross(Vector a, Vector b)
    return a.x * b.y - a.y * b.x;
double length(Vector v)
    return sqrt(v.x * v.x + v.y * v.y); //return sqrt(
        dot(v,v));
double length(Point a ,Point b){
    return length(a-b);
double angle(const Vector& a, const Vector& b) { return
     acos(dot(a, b) / length(a) / length(b)); }
double Triarea(const Point& p1, const Point& p2, const
    Point& p3)
    return fabs(cross(p2 - p1, p3 - p1)) / 2;
Vector Rotate(const Vector& a, double rad){ //radian
    0~2pi //counterclockwise{
    return Vector(a.x * cos(rad) - a.y * sin(rad), a.x*
         sin(rad) + a.y * cos(rad)); //旋轉矩陣
Vector Normal(const Vector& a)
{ //向量的單位法線
    double L = length(a);
    return Vector(-a.y / L, a.x / L);
struct Line {
    Point p1, p2;
typedef Line Segment;
Point GetLineIntersection(Point p, Vector v, Point q,
    Vector w) //點斜式交點 p+vt1 q+wt2
   Vector u = p - q;
double t = cross(w, u) / cross(v, w); //t1
return p + v * t; //p+vt1
Point GetLineProjection(Point p, Point a, Point b)
{
    Vector v = b - a;
return a + v * (dot(v, p - a) / dot(v, v));
typedef Line Segment;
bool Onsegment(Point p, Point a1, Point a2) //點在線上
                                  //端點在兩側
    return dcmp(cross(a1 - p, a2 - p)) == 0 && dcmp(dot
        (a1 - p, a2 - p)) < 0;
```

```
bool SegmentProperIntersection(Point a1, Point a2,
    Point b1, Point b2)
{
    // 規範相交:交點不能是線段的交點
    double c1 = cross(a2 - a1, b1 - a1), c2 = cross(a2)
         - a1, b2 - a1);
    double c3 = cross(b2 - b1, a1 - b1), c4 = cross(b2)
         - b1, a2 - b1)
    return dcmp(c1) * dcmp(c2) < 0 && dcmp(c3) * dcmp(</pre>
bool SegmentProperIntersection(Segment s1, Segment s2)
    return SegmentProperIntersection(s1.p1, s1.p2, s2.
         p1, s2.p2);
bool SegmentInterSection(Point a1, Point a2, Point b1,
    Point b2) // 非規範相交
{
    if (Onsegment(a1, b1, b2) || Onsegment(a2, b1, b2)
         II Onsegment(b1, a1, a2) II Onsegment(b2, a1,
         a2))
         return true;
    if (SegmentProperIntersection(a1, a2, b1, b2))
         return true; //規範相交
    return false;
bool SegmentInterSection(Line& 11, Line& 12)
{
    return SegmentInterSection(l1.p1, l1.p2, l2.p1, l2.
         p2):
double distance(Point& a, Point& b)
    return sqrt(length(b - a));
double distance(Point& p, Point& p1, Point& p2) //Line
     => p1,p2
{
    Vector v1 = p - p1, v2 = p2 - p1;
return fabs(cross(v1, v2)) / length(v2); //面積/底=
         高(距離)
double distance(Point& p, Segment& s) //Point to
    Segment
    Vector v = s.p2 - s.p1;
    if (dcmp(length(v)) == 0)
         return length(p - s.p1); //線段退化成點
    Vector v1 = p - s.p1;
Vector v2 = p - s.p2;
    if (dcmp(dot(v1, v)) < 0)
    return length(v1); // 點投影不在線上
if (dcmp(dot(v2, v)) > 0)
        return length(v2); // 點投影不在線上
    return fabs(cross(v, v1)) / length(v);
double distance(Segment& s1, Segment& s2) //線段到線段
    if (SegmentInterSection(s1, s2))
         return 0;
    double d = 1e9;
d = min(d, distance(s1.p1, s2)); //點到線段距離取最
    d = min(d, distance(s1.p2, s2));
d = min(d, distance(s2.p1, s1));
d = min(d, distance(s2.p2, s1));
double ldistance(Line& l1, Line& l2) //線段到線段距離
    Vector v1 = l1.p2 - l1.p1;
Vector v2 = l2.p2 - l2.p1;
    if (cross(v1, v2) != 0)
         return 0;
    return distance(l1.p1, l2); //點到線段距離
int ConvexHull(vector<Point>& P, Point* res)
{ //凸包Andrew's Monotone Chain
    sort(P.begin(), P.end()); //先x 後 y
```

```
auto last = unique(P.begin(), P.end()); //非重複的
        點數量
    P.erase(last, P.end());
    int cnt = P.size();
    int m = 0;
    for (int i = 0; i < cnt; i++) {</pre>
        while (m > 1 \&\& cross(res[m - 1] - res[m - 2],
            P[i] - res[m - 2]) <= 0
        res[m++] = P[i];
    int k = m;
    for (int i = cnt - 2; i >= 0; i--) {
        while (m > k \&\& cross(res[m - 1] - res[m - 2],
            P[i] - res[m - 2]) <= 0)
        res[m++] = P[i];
    if (cnt > 1) //頭尾 1個點不用--
        m--;
    return m; //凸包點數
double PolygonArea(Point* p, int n)
    double area = 0;
    for (int i = 0; i < n; ++i)
area += cross(p[i], p[(i + 1) % n]);
    return fabs(area) / 2;
//半平面交
typedef vector<Point> Polygon;
Polygon halfplane_intersection(Polygon& p, Line& line)
{
    Point p1 = line.p1, p2 = line.p2;
    int n = p.size();
    for (int_i = 0; i < n; i++) {
        double c = cross(p1, p2, p[i]);
        double d = cross(p1, p2, p[(i + 1) % n]);
        if (dcmp(c) >= 0)
            q.push_back(p[i]);
        if (dcmp(c * d) < 0)
            q.push_back(GetLineIntersection(p1, p2, p[i
                ], p[(i + 1) % n]);
    return q;
}
```

6.2 rotating-caliper

```
#include "Point.cpp"
void rotating_caliper(vector<Point> P)
     sort(P.begin(), P.end());
     int l = 0, u = 0;
    Point L[10000], U[10000];
     int cnt = P.size();
     for (int i = 0; i < cnt; i++) {
   while (l >= 2 && cross(L[l - 2], L[l - 1], P[i
               ]) <= 0)
         while (u \ge 2 \& cross(U[1 - 2], U[1 - 1], P[i])
              ]) >= 0)
              u--;
         L[l++] = P[i];
         U[u++] = P[i];
     if(u>=2) L[1]=U[u-2];
     for(int i=0, j=u-1; i < l && j>0;){
    //compute L[i] and U[j];
         if(cross(L[i+1]-L[i],U[j-1]-U[j])<0) i++;
         else j--;
    }
}
```

6.3 closet-pair

```
#include "Point.cpp"
bool cmpy(const Point& i, const Point& j) { return i.y
    < j.y;
vector<Point> p;
double DnC(int L, int R, vector<Point>& p) // 區間
    if (L >= R)
        return 1e-9;
    if (L + 1 == R) {
        return length(p[L], p[R]);
    int M = (L + R) >> 1;
    double d = min(DnC(L, M, p), DnC(M + 1, R, p));
    if (dcmp(d) == 0)
        return 0;
    int N = 0;
    Point t[10000];
    for (int i = M; i >= L \&\& p[M].x - p[i].x < d; --i)
        t[N++] = p[i];
    for (int i = M + 1; i \le L && p[i].x - p[M].x < d;
         ++i) {
        t[N++] = p[i];
    sort(t, t + N, cmpy)
    for (int i = 0; i < N; i++) {
    for (int j = 1; j <= 3; j++) {
             d = min(d, length(t[i], t[i + j]));
    return d;
double closet_pair(vector<Point>& p)
    sort(p.begin(),p.end());
    return DnC(0,p.size(),p);
```

6.4 Minimum-Cover-Circle

```
const double eps = 1e-7;
struct Point{
            double x,y;
            Point(){}
            Point(double x, double y):x(x),y(y){}
};
Point Circumcenter(Point a,Point b,Point c){
            double a1 = b.x - a.x, b1 = b.y - a.y, c1 = (a1*a1)
                        + b1*b1)/2;
            double a2 = c.x - a.x, b2 = c.y - a.y, c2 = (a2*a2)
            + b2*b2)/2;
double d = a1 * b2 - a2 * b1;
            return Point(a.x + (c1*b2 - c2*b1)/d,a.y + (a1*c2 - c2*b1)/d
                           a2*c1)/d);
}
double Distance(Point A, Point B){
            return sqrt((A.x-B.x)*(A.x-B.x)+(A.y-B.y)*(A.y-B.y)
                        );
}
// Expected Complexity : O(N)
pair<Point,double> MinimumCoverCircle(vector<Point> P){
      random_shuffle(P.begin(),P.end());
            Point center = P[0];
            double R = 0.0;
            for(int i=1;i<P.size();i++) if(Distance(center,P[i</pre>
                        ])+eps > R){
            center = P[i];R = 0.0;
            for(int j=0;j<i;j++) if(Distance(center,P[j])+eps >
                           R){
                 center.x=(P[i].x+P[j].x)/2.0;
center.y=(P[i].y+P[j].y)/2.0;
R = Distance(center,P[j]);
                  for(int k=0;k<j;k++) if(Distance(center,P[k])+eps</pre>
                                 > R){
                        center = Circumcenter(P[i],P[j],P[k]);
```

```
R = Distance(center,P[k]);
}

return make_pair(center,R);
}
```

7 Sort

7.1 Heap Sort

```
void heap_sort(int* arr, int len)
    heapify(arr, len/2-1, len);
    max_heap(arr, len);
void heapify(int* ptr, int now, int last)
    if(now >= last/2 || now < 0) return;</pre>
    sub_heapify(ptr, now, last);
    heapify(ptr, now-1, last);
void sub_heapify(int* ptr, int now, int last)
    if(now*2+2 < last && !(ptr[now] >= ptr[now*2+1] &&
         ptr[now] >= ptr[now*2+2])) {
         int max = (ptr[now*2+1] > ptr[now*2+2]) ? now
             *2+1 : now*2+2;
        swap(ptr, now, max, 1);
        if(max < last/2) sub_heapify(ptr, max, last);</pre>
    else if(now*2+1 < last && ptr[now] < ptr[now*2+1]){
        swap(ptr, now, now*2+1, 1);
if(now*2+1 < last/2)sub_heapify(ptr, now*2+1,</pre>
             last);
void max_heap(int* ptr, int len)
{
    if(len <= 1) return;</pre>
    swap(ptr, 0, len-1, 2);
    sub_heapify(ptr, 0, len-1);
    max_heap(ptr, len-1);
}
```

7.2 Merge Sort

```
void Merge(int* N,int L,int M){
   int tmp[L],p=0; int a,b;
   for(a=0,b=M;a<M && b<L;){
      if(N[a] < N[b]){ tmp[p++]=N[a]; a++; }
      else{ tmp[p++]=N[b]; b++;}
   }
   if(a == M)for(int i=b;i<L;i++)tmp[p++]=N[i];
   else for(int i=a;i<M;i++)tmp[p++]=N[i];
   for(int i=0;i<L;i++)N[i]=tmp[i];
}
void MergeSort(int* N,int L){
   int M=L/2;
   if(L == 1)return;
   MergeSort(N,M);
   MergeSort(N+M,L-M);
   Merge(N,L,M);
}</pre>
```

7.3 Radix Sort

```
if (maxData < data[i]) maxData = data[i];</pre>
    int d = 1; int p = 10;
    while (maxData >= p){
        p *= 10;
        ++d;
    }
    return d;
          int d = 1; //保存最大的位數
          int p = 10;
          for(int i = 0; i < n; ++i){
          while(data[i] >= p){
           p *= 10;
           ++d;
          return d;*/
void radixsort(int data[], int n) //基數排序
{
    int d = maxbit(data, n);
    int *tmp = new int[n];
    int *count = new int[10]; //計數器
    int i, j, k;
    int radix = 1;
    for(i = 1; i <= d; i++) { //進行d次排序
for(j = 0; j < 10; j++) count[j] = 0; //每次分
            配前清空計數器
        for(j = 0; j < n; j++){
k = (data[j] / radix) % 10; //統計每個桶中
            count[k]++;
        for(j = 1; j < 10; j++) count[j] = count[j - 1]
             + count[j]; //將tmp中的位置依次分配□每個
        for(j = n - 1; j >= 0; j--) { //將所有桶中記錄
            依次收集到tmp中
            k = (data[j] / radix) % 10;
            tmp[count[k] - 1] = data[j];
            count[k]--;
        for(j = 0; j < n; j++) //將臨時數組的內容複製到
            data中
            data[j] = tmp[j];
        radix = radix * 10;
    delete []tmp;
    delete ∏count;
}
```

7.4 Shell Sort

8 Math

8.1 LIS

```
#include <bits/stdc++.h>
using namespace std;
template <typename E>
struct Node {
    E value;
```

```
E* pointer;
};
template <class E>
struct node_ptr_less {
    bool operator()(E*& node1,
        E*& node2) const
        return node1->value < node2->value;
    }
template <typename E>
std::vector<E> lis(const std::vector<E>& n)
    typedef E* NodePtr;
    std::vector<NodePtr> pileTops;
    // sort into piles
    for (typename std::vector<E>::const_iterator it = n
        .begin(); it != n.end(); it++) {
        NodePtr node(new Node<E>());
        node->value = *it;
        typename std::vector<NodePtr>::iterator j = std
            ::lower_bound(pileTops.begin(), pileTops.
            end(), node, node_ptr_less<E>());
        if (j != pileTops.begin())
            node->pointer = *(j -
        if (j != pileTops.end())
            *j = node;
        else
            pileTops.push_back(node);
    // extract LIS from piles
    std::vector<E> result;
    for (NodePtr node = pileTops.back(); node !=
        nullptr; node = node->pointer)
        result.push_back(node->value)
    std::reverse(result.begin(), result.end());
    return result;
int LIS(vector<int>& v)
    vector<int> ans;
    for (auto& i : v) {
        auto it = lower_bound(ans.begin(), ans.end(), i
        if (ans.size() == 0 || i >= ans.back())
            ans.push_back(i);
        else {
            *it = i;
        }
    return ans.size();
```

8.2 Extended Euclidean

```
int ExGCD(int A,int B,int& X,int& Y,int s0 = 1,int s1 =
    0,int t0 = 0,int t1 = 1){
    if(A%B == 0){
        X = s1;
        Y = t1;
        return B;
    }
    s0-=s1*(A/B);
    t0-=t1*(A/B);
    return ExGCD(B,A%B,X,Y,s1,s0,t1,t0);
}
```

8.3 Prime

```
}
// Complexity : O(N)
void BuildPrime(vector<int> primelist,bool prime[],int
     for(int m=2;m<N;m++){</pre>
         if(prime[m] == true) primelist.push_back(m);
         for(auto i:primelist){
              if(m*i >= N) break;
              prime[m*i] = false;
              if(m%i == 0) break;
         }
    }
}
void ExBuildPrime(int first[],bool prime[],int N){
    for(int i=2;i<N;i++){
    prime[i] = true;</pre>
         first[i] = 1;
     for(int i=2;i<N;i++){</pre>
         if(prime[i]) for(int j=i*i;j<N;j+=i){
    prime[j] = false;</pre>
              if(first[j] == 1) first[j] = i;
    }
}
```

8.4 Factor Decomposition

```
vector<pair<int,int>> FactorDecomposition(int x){
   vector<pair<int,int>> ans;
   while(x > 1){
        int p,e = 0;
        if(prime[x] == true)p = x;else p = first[x];
        while(x%p == 0){x/=p;e++;}
        ans.push_back(make_pair(p,e));
   }
   return ans;
}
```

8.5 Module Inverse

```
int inverse(int A,int M,int X = 1,int Y = 0){
   if(A%M == 0){
     if(Y < 0)Y+=M;
     return Y;
   }
   X-=Y*(A/M);
   return inverse(M,A%M,Y,X);
}
inline int inverse(int A,int M){
   return ExPower(A,M-2,M);
}</pre>
```

8.6 Phi

```
int Phi(int x){
    vector<pair<int,int>> FD = FactorDecomposition(x);
    int ans = 1;
    for(auto i:FD){
        ans *= i.first-1;
        ans *= Power(i.first,i.second-1);
    }
    return ans;
}

void BuildPhi(int phi[],int N){
    for(int i=1;i<=N;i++) phi[i] = i;
    for(int i=1;i<=N;i++) for(x=i*2;x<=N;x+=i) phi[x]
        -= phi[i];
}

void BuildPhi(int phi[],int N){</pre>
```

```
bool prime[N+1];for(int i=2;i<=N;i++) prime[i] =</pre>
         true;
    vector<int> primelist;
    phi[1] = 1;
    for(int m=2;m<=N;m++){</pre>
        if(prime[m] == true){
             phi[m] = m-1;
             primelist.push_back(m);
         for(auto i:primelist){
             if(m*i > N) break;
             prime[m*i] = false;
             if(m\%i == 0){
                 int now = m, power = 1;
                 while(now%i == 0){ now /= i;power *= i;
                 phi[m*i] = phi[now]*power*(i-1);
                 break;
             else phi[m*i] = phi[m]*(i-1);
        }
    }
}
```

8.7 Miller Rabin

```
int ExMultiply(int a,int b,int n){
    a %= n;b %= n;
    int r = 0;
    while(b){
        if(b\&1)r = ((a+r >= n)? a+r-n : a+r);
        a = ((a+a >= n)? a+a-n : a+a);
    return r;
}
int ExExPower(int a,int d,int n){
    if(d == 0)return 1;
    int k = ExExPower(a,d/2,n);
    if(d%2)return ExMultiply(ExMultiply(k,k,n),a,n);
    return ExMultiply(k,k,n);
}
bool MillerRabin(int n,int a){
    if(__gcd(n,a) == n)return true;
    if(__gcd(n,a) != 1)return false;
    // a^(d*2^r)
    int d = n-1, r = 0;
    while(d\%2 == 0){ d /= 2; r++; }
    // a^d = ? \pmod{n}
    int remain = ExExPower(a,d,n);
    if(remain == 1 || remain == n-1)return true;
    while(r--){
        remain = ExMultiply(remain, remain, n);
        if(remain == n-1)return true;
    return false;
}
bool IsPrime(int n){
    int a[7] =
        {2,325,9375,28178,450775,9780504,1795265022};
    for(int i=0;i<7;i++)if(!MillerRabin(n,a[i]))return</pre>
        false;
    return true;
}
```

8.8 Pollard-Rho

```
#include <bits/stdc++.h>
using namespace std;
//don't use __gcd for negative number
int gcd(int a, int b)
{
   if (a < 0)
       return gcd(-a, b);
   return b ? gcd(b, a % b) : a;</pre>
```

```
//super fast
int ExMultiply(int a, int b, int n)
    if (a == 0)
        return 0;
    return ((a & 1) * b % n + (ExMultiply(a >> 1, b, n)
          << 1) % n) % n;
int FastPow(int a, int b, int n)
    a \% = n;
    int ans = 1;
    int d = a;
    while (b) {
        if (b & 1)
            ans = ExMultiply(ans, d, n);
        d = ExMultiply(d, d, n);
        b >>= 1;
    return ans;
}
bool MillerRabin(int n, int a)
{
    if (n == a)
        return true;
    //even
    if (gcd(n, a) == n)
        return true;
    if (gcd(n, a) != 1)
        return false;
    // a^(d*2^r)
    int d = n - 1,
    while (!(d & 1)) {
        d >>= 1;
        r++;
    // a^d = ? \pmod{n}
    int remain = FastPow(a, d, n);
    if (remain == 1 | | remain == n - 1)
        return true;
    while (r--) {
        remain = ExMultiply(remain, remain, n);
        if (remain == n - 1)
             return true;
    return false;
bool IsPrime(int n)
    if (n == 2)
        return true;
    if (!(n & 1))
    return false;
int a[7] = { 2, 325, 9375, 28178, 450775, 9780504,
        1795265022 };
    for (int i = 0; i < 7; i++)
        if (!MillerRabin(n, a[i]))
             return false;
    return true;
int PollardRho(int n, int c)
    int x = rand() % n, y = x, k = 2;
    for (int i = 2;; i++) {
        x = (ExMultiply(x, x, n) + c) % n;
int d = gcd(x - y, n);
        if (d != 1 && d != n)
             return d;
        if (y == x)
             return n;
        if (i == k) {
             y = x;
             k <<= 1;
        }
    }
vector<int> Fac;
void fac(int n)
```

```
if (IsPrime(n)) {
    Fac.push_back(n);
    return;
}
int p = n;
while (p >= n)
    p = PollardRho(p, rand() % (n - 1) + 1);
fac(p);
fac(n / p);
}
```

8.9 Chinese-Remainder-Theorem

```
#include <bits/stdc++.h>
using namespace std;
int inverse(int A, int M)
     return A == 1 ? 1 : inverse(M % A, M) * (M - M / A)
          % M;
}
 * chinese remainder theorem
 * check all m[i] are pairwise coprime
 * if x = a1 \pmod{p} and x=a2 \pmod{p} if a1!=a2
 * then no solution
 * return first positive answer
 * next answer is answer+M
 */
int CRT(vector<int> a, vector<int> m)
    if (a.size() != m.size())
         return -1;
     int M = 1;
     for (int i = 0; i < m.size(); i++) {</pre>
         M *= m[i];
    int res = 0;
    for (int i = 0; i < a.size(); i++) {
    res = (res + a[i] * (M / m[i]) * inverse(M / m[i], m[i])) % M;</pre>
    return (res+M)%M;
}
```

8.10 Lucas-Theorem

```
#include <bits/stdc++.h>
using namespace std;
const int p = 5; //prime<10^5
int fac[p + 1];
void build_fac(int p)
     fac[0] = 1;
    for (int i = 1; i <= p; i++)
fac[i] = fac[i - 1] * i % p;
//mod inverse
int inv(int a, int p)
//called after build_fac
int Lucas(int n, int m, int p)
{
    if (m == 0)
         return 1;
    if (m > n)
         return 0:
    if (n < m)
         return fac[n] * inv(fac[m] * fac[n - m] % p, p)
               % p;
         return Lucas(n / p, m / p, p) * Lucas(n % p, m
              % p, p) % p;
}
```

8.11 FFT

```
const int MAXN = 262144;
const double PI = acos(-1.0);
const complex<double> I(0, 1);
complex<double> omega[MAXN+1];
void pre_FFT(){
    for(int i=0; i<=MAXN; i++)omega[i] = exp(i * 2 * PI
          / MAXN * I);
}
void FFT(int n, complex<double> a[], bool inv=false){
    int basic = MAXN / n;
    int theta = basic;
    for(int m = n; m >= 2; m >>= 1) {
         int mh = m >> 1;
         for(int i = 0; i < mh; i++) {</pre>
             complex<double> w = omega[inv ? MAXN-(i*
    theta%MAXN) : i*theta%MAXN];
             for(int j = i; j < n; j += m) {
  int k = j + mh;</pre>
                  complex<double> x = a[j] - a[k];
                  a[j] += a[k];
                  a[k] = w * x;
         theta = (theta * 2) % MAXN;
    int i = 0;
    for(int j = 1; j < n - 1; j++) {
         for(int k = n >> 1; k > (i ^= k); k >>= 1);
         if(j < i) swap(a[i], a[j]);
    if(inv)for(i = 0; i < n; i++)a[i] /= n;
```

8.12 Fraction

```
struct fraction_positive{
    int p,q;
    fraction_positive(){}
    fraction_positive(int p,int q):p(p),q(q){}
    void reduction(){
        int G = \__gcd(p,q);
        p /= G;
        q /= G;
    bool operator==(const fraction_positive& B) const {
        return (p == B.p && q == B.q);
    bool operator!=(const fraction_positive& B) const {
        return (p != B.p || q != B.q);
    bool operator>(const fraction_positive& B) const {
        return (p*B.q > B.p*q);
    bool operator>=(const fraction_positive& B) const {
        return (p*B.q >= B.p*q);
    bool operator<(const fraction_positive& B) const {</pre>
        return (p*B.q < B.p*q);</pre>
    bool operator<=(const fraction_positive& B) const {</pre>
        return (p*B.q <= B.p*q);</pre>
    fraction_positive operator+(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.q+B.p*q;
        F.q = q*B.q;
        F.reduction();
        return F;
    fraction_positive operator-(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.q-B.p*q;
```

```
F.q = q*B.q;
F.reduction();
        return F;
    fraction_positive operator*(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.p;
        F.q = q*B.q
        F.reduction();
        return F;
    fraction_positive operator/(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.q;
        F.q = q*B.p
        F.reduction();
        return F;
    fraction_positive operator*(int x) const {
        fraction_positive F = *this;
        F.p *= x
        F.reduction();
        return F;
    fraction_positive operator/(int x) const {
        fraction_positive F = *this;
        F.q *= x;
        F.reduction();
        return F;
    }
};
struct fraction{
    fraction_positive N;
    bool sign,broken;//0 positive 1 negative
    fraction():broken(false){}
    fraction(int p,int q,bool sign):sign(sign){
   if(q == 0){broken = true;cout << "===divide by</pre>
             zero===" << endl;}
        else{N.p = p;N.q = q;N.reduction();}
    bool operator==(const fraction& B) const {
        return (N == B.N && sign == B.sign);
    bool operator!=(const fraction& B) const {
        return (N != B.N || sign != B.sign);
    bool operator>(const fraction& B) const {
        return (!sign && B.sign) || (!sign && N > B.N)
             | (sign && N < B.N);</pre>
    bool operator>=(const fraction& B) const {
        return (!sign && B.sign) || (!sign && N >= B.N
             ) || (sign && N <= B.N);
    bool operator<(const fraction& B) const {
   return !(*this >= B);
    bool operator<=(const fraction& B) const {</pre>
        return !(*this > B);
    fraction operator+(const fraction& B) const {
        fraction F;
        if(broken | | B.broken){F.broken = true; return F
        if(sign^B.sign){
             const fraction_positive& big = (N > B.N ? N
                  : B.N);
             const fraction_positive& small = (N <= B.N</pre>
                 ? N : B.N);
             F.N = big - small;
             F.sign = (N > B.N ? sign : B.sign);
        else{
             F.N = N+B.N;
             F.sign = sign;
        return F;
    fraction operator-(const fraction& B) const {
```

```
fraction F = B;
         if(broken || B.broken){F.broken = true; return F
         F.sign = !F.sign;
         return (*this+F);
    fraction operator*(const fraction& B) const {
         fraction F;
         if(broken | | B.broken){F.broken = true; return F
         F.N = N*B.N;
         F.sign = sign^B.sign;
         return F;
    fraction operator/(const fraction& B) const {
         fraction F;
         if(broken | | B.broken | | B.N.p == 0){F.broken =
               true; return F;}
         F.N = N/B.N;
         F.sign = sign^B.sign;
         return F;
    fraction operator*(int x) const {
   fraction F = *this;
         if(broken){F.broken = true;return F;}
         F.N = F.N*abs(x);
         if(x < 0)F.sign = !F.sign;
         return F;
    fraction operator/(int x) const {
    fraction F = *this;
         if(x == 0){F.broken = true;return F;}
         F.N = F.N/abs(x);
         if(x < 0)F.sign = !F.sign;</pre>
         return F;
    friend istream& operator>>(istream& in,fraction& B)
         {
         int x;
         char c;
         B.sign = false;
         in \Rightarrow x; if(x < 0){B.sign = true;x = -x;}
         B.N.p = x;
         in >> c >> x; if(x == 0)\{B.broken = true; return
             in;}
         B.N.q = x;
         B.N.reduction();
         return in;
    friend ostream& operator<<(ostream& out,const</pre>
         fraction& B){
         if(B.broken){return out << "NaN";}</pre>
         if(B.sign)out << '-'</pre>
         return out << B.N.p << '/' << B.N.q;</pre>
    }
};
```

8.13 Matrix

```
#include <bits/stdc++.h>
using namespace std;
const double EPS = 1e-9;
template <typename T>
class Matrix {
public:
    Matrix()
        : wrong(false)
    Matrix(int _rows, int _cols)
         : wrong(false)
         rows = _{rows};
         cols = _cols;
data = new T*[rows];
         for (int i = 0; i < rows; i++)
             data[i] = new T[cols];
    Matrix(T** _data, int _rows, int _cols)
```

```
: wrong(false)
{
     rows = _rows;
     cols = _cols;
data = new T*[rows];
     for (int i = 0; i < rows; i++)
          data[i] = new T[cols];
     for (int i = 0; i < rows; i++)
    for (int j = 0; j < cols; j++)</pre>
               data[i][j] = _data[i][j];
Matrix(const Matrix& N)
     wrong = N.wrong;
     rows = N.rows;
     cols = N.cols;
     data = new T*[rows];
for (int i = 0; i < rows; i++)</pre>
          data[i] = new T[cols];
     for (int i = 0; i < rows; i++)
for (int j = 0; j < cols; j++)
data[i][j] = N.data[i][j];
~Matrix()
{
     delete data;
T& at(int a, int b)
{
     return data[a][b];
Matrix operator+(const Matrix& N)
{
     cout << (*this) << endl</pre>
            << N << endl;
     Matrix tmp = Matrix(*this);
     if (rows != N.rows || cols != N.cols)
          tmp.wrong = true;
     else
          for (int i = 0; i < rows; i++)
               for (int j = 0; j < cols; j++)
                    tmp.data[i][j] += N.data[i][j];
     return tmp;
Matrix operator-(const Matrix& N)
     Matrix tmp = Matrix(*this);
     if (rows != N.rows || cols != N.cols)
          tmp.wrong = true;
     else
          for (int i = 0; i < rows; i++)
               for (int j = 0; j < cols; j++)
                    tmp.data[i][j] -= N.data[i][j];
     return tmp;
Matrix operator*(const Matrix& N)
     Matrix tmp = Matrix(rows, N.cols);
if (cols != N.rows)
          tmp.wrong = true;
     else
          for (int i = 0; i < tmp.rows; i++)</pre>
               for (int j = 0; j < tmp.cols; j++) {
   tmp.data[i][j] = 0;
   for (int k = 0; k < cols; k++)
        tmp.data[i][j] += data[i][k] *</pre>
                               N.data[k][j];
     return tmp;
Matrix operator*(int c)
     Matrix tmp = Matrix(*this);
     for (int i = 0; i < rows; i++)
for (int j = 0; j < cols; j++)
tmp.data[i][j] *= c;
     return tmp;
Matrix operator=(const Matrix& N)
     wrong = N.wrong;
     rows = N.rows;
```

```
cols = N.cols;
     data = new T*[rows];
     for (int i = 0; i < rows; i++)
          data[i] = new T[cols];
     for (int i = 0; i < rows; i++)
          for (int j = 0; j < cols; j++)
    data[i][j] = N.data[i][j];</pre>
     return (*this);
Matrix transpose(void)
    Matrix tmp = Matrix(*this);
     //int fuck = tmp.rows; tmp.rows = tmp.cols;tmp.
          cols = fuck;
     swap(tmp.rows, tmp.cols);
     delete tmp.data;
     tmp.data = new T*[tmp.rows];
for (int i = 0; i < tmp.rows; i++)</pre>
         tmp.data[i] = new T[tmp.cols];
     for (int i = 0; i < rows; i++)
for (int j = 0; j < cols; j++)
tmp.data[j][i] = data[i][j];
     return tmp;
void Identity()
{ // rows==cols
     for (int i = 0; i < rows; i++) {</pre>
         at(i, i) = 1;
Matrix pow(int rhs) const
     if (rows != cols)
          return Matrix();
    Matrix res(rows, rows), p(*this);
     res.Identity();
     while (rhs) {
          if (rhs & 1)
              res = res * p;
         p = p * p;
         rhs >>= 1;
     return res;
T det()
     int ans = 1;
     for (int i = 0; i < rows; i++) {</pre>
          for (int j = i + 1; j < rows; j++) {
  int a = i, b = j;</pre>
               while (at(b, i)) {
                   int q = at(a, i) / at(b, i);
for (int k = 0; k < rows; k++) {</pre>
                        at(a, k) = at(a, k) - at(b, k)
* q;
                   swap(a, b);
               if (a != i) {
                   swap(data[i], data[j]);
                   ans = -ans;
          if (fabs(at(i, i)) < EPS)</pre>
              return 0;
          else
              ans *= at(i, i);
     return ans;
// r:non-free number l:l[i] is true if i-th
     variable is non-free
Matrix GuassElimination(int& r, vector<bool>& l,
     int flag = 0
     l = vector<bool>(cols);
     r = 0;
    Matrix res(*this);
     for (int i = 0; i < res.cols - flag; <math>i++) {
          for (int j = r; j < res.rows; j++) {</pre>
              if (fabs(res.at(j, i)) > EPS) {
    swap(res.data[r], res.data[j]);
```

```
int rows, cols;
                    break:
              }
                                                                       bool wrong;
                                                                 };
          if (fabs(res.at(r, i)) < EPS) {</pre>
               continue;
          for (int j = 0; j < res.rows; j++) {
   if (j != r && fabs(res.at(j, i)) > EPS)
                    double tmp = (double)res.at(j, i) /
                          (double)res.at(r, i);
                    for (int k = 0; k < res.cols; k++)
                        res.at(j, k) -= tmp * res.at(r,
                               k);
              }
          }
          r++;
          l[i] = true;
     return res;
vector<double> Solve(vector<double> a)
{
     if (rows != cols)
          return vector<double>();
     vector<double> res(rows);
    Matrix t(rows, cols + 1);

for (int i = 0; i < rows; i++) {

    for (int j = 0; j < cols; j++)

        t.at(i, j) = at(i, j);
          t.at(i, rows) = a[i];
     int r = 0;
     vector<bool> 1;
     t = t.GuassElimination(r, l, 1);
     if (r != rows)
          return vector<double>();
     for (int i = 0; i < cols; i++) {
          if (l[i])
               for (int j = 0; j < rows; j++) {</pre>
                    if (fabs(t.at(j, i)) > EPS)
                        res[i] = t.at(j, cols) / t.at(j
                              , i);
              }
     return res;
Matrix Inverse()
     if (rows != cols)
    return Matrix();
Matrix t(rows, rows * 2);
     for (int i = 0; i < rows; i++) {
    for (int j = 0; j < cols; j++)
              t.at(i, j) = at(i, j);
          t.at(i, i + rows) = 1;
     int r = 0;
     vector<bool> 1;
     t = t.GuassElimination(r, l, rows);
     if (r != rows)
          return Matrix();
     for (int i = 0; i < cols; i++) {</pre>
          if (l[i])
               for (int j = 0; j < rows; j++) {
                    if (fabs(t.at(j, i)) > EPS) {
    for (int k = 0; k < cols; k++)</pre>
                             }
              }
     Matrix res(rows, cols);
     for (int i = 0; i < rows; i++)
         for (int j = 0; j < cols; j++)
    res.at(i, j) = t.at(i, j + cols);</pre>
     return res;
```

T** data;