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1 Basic

1.1 Tips

1. 把codebook 所有可能的算法掃一遍，可能會有靈感。
2. 可能要先枚舉某些部分，在套演算法
3. Size很小，考慮狀態壓縮dp

1.2 vimrc

```
set nocompatible
set ai ar sm rnu
set t_Co=256
set nu
set ai
set tabstop=4
set shiftwidth=4
set softtabstop=4
colorscheme darkblue
syntax on
filetype plugin indent on
se makeprg=g++\ \% -Wall\ -Wshadow\ -std=c++14\ -o\ %%.
out
map <F9> :w <CR> :make <CR>:!./%<.out<CR>
map <F10> :w <CR> :make <CR>:!./%<.out < %<.in<CR>
```

1.3 default

```
#include<bits/stdc++.h>

using namespace std;

#define FI freopen("in.txt", "r", stdin)
#define FO freopen("out.txt", "w", stdout)
#define IOS ios_base::sync_with_stdio(0);cin.tie(0)
#define pb push_back
#define mp make_pair
#define ff first
#define ss second

typedef long long LL;

const int MOD = 1000000007;
const double PI = acos(-1.0);

int dx[] = {-1,0,1,0};
int dy[] = {0,1,0,-1};

int main(){
    IOS;
    return 0;
}
```

1.4 FastInput

```
int readInt () {
    bool minus = false;
    int result = 0;
    char ch;
    ch = getchar();
    while (true) {
        if (ch == '-') break;
        if (ch >= '0' && ch <= '9') break;
        ch = getchar();
    }
    if (ch == '-') minus = true; else result = ch-'0';
    while (true) {
        ch = getchar();
        if (ch < '0' || ch > '9') break;
        result = result*10 + (ch - '0');
    }
    if (minus)
        return -result;
    else
```

```
    return result;
}
```

1.5 Int128

```
#include <bits/stdc++.h>
using namespace std;

std::ostream& operator<<(std::ostream& dest, __int128_t
    value)
{
    std::ostream::sentry s(dest);
    if (s) {
        __uint128_t tmp = value < 0 ? -value : value;
        char buffer[128];
        char* d = std::end(buffer);
        do {
            --d;
            *d = "0123456789"[tmp % 10];
            tmp /= 10;
        } while (tmp != 0);
        if (value < 0) {
            --d;
            *d = '-';
        }
        int len = std::end(buffer) - d;
        if (dest.rdbuf()->sputn(d, len) != len) {
            dest.setstate(std::ios_base::badbit);
        }
    }
    return dest;
}

__int128 parse(string& s)
{
    __int128 ret = 0;
    for (int i = 0; i < s.length(); i++)
        if ('0' <= s[i] && s[i] <= '9')
            ret = 10 * ret + s[i] - '0';
    return ret;
}

int main()
{
    string s = "18782187821878218782187821878218782";
    __int128 x = parse(s);
    __int128 y = 1ULL << 63;
    __int128 z = 1ULL << 63;
    x *= 2;
    cout << x << endl;
    cout << y << endl;
    cout << y * z << endl;
}
```

2 Java

2.1 template

```
/* Compile: javac %
 * Run: java [Class name] */
import java.util.*;
import java.lang.*;
import java.math.*;
import java.io.*;

class Main {
    public static void main (String[] args) {
        System.out.print(1);
        System.out.print(2);
        System.out.println("Hello World");
        System.out.printf("%.2f", 0.12345);

        Scanner sc = new Scanner(System.in);
        System.out.println(sc.nextLine()); //gets()
        System.out.println(sc.next()); //scanf("%s")
        System.out.println(sc.nextInt());
```

```
System.out.println(sc.nextDouble());
while(sc.hasNext()) { //EOF
    int a = sc.nextInt();
    System.out.println(a);
}

int[] a = {1,2,3};
int[][] b = {{1,2},{3,4,5}};
double[] c = new double[90];
System.out.print(b[0][1]);
System.out.print(b[1][2]);

int[] d = {5,2,1,3,4};
Integer[] e = {6,3,4,1,2};
Arrays.sort(d);
Arrays.sort(e, new MyCom());
for(int i=0; i<d.length; i++) {
    System.out.print(d[i]);
}
for(int i=0; i<e.length; i++) {
    System.out.print(e[i]);
}

Set<String> s = new HashSet<String>(); //or TreeSet
s.add("123");
s.add("234");
System.out.println(s);
System.out.println(s.contains("123"));
Map<String, Integer> m = new TreeMap<String,
    Integer>();
m.put("haha", 123);
m.put("hehe", 234);
System.out.println(m);

BigInteger b1 = new BigInteger("
    -1231237182379123712");
BigInteger b2 = BigInteger.valueOf(234);

System.out.println(b1.add(b2));
System.out.println(b1.mod(b2));

int z = Integer.parseInt("-123");
System.out.println(z);

System.out.println(Math.PI);
System.out.println(Math.sin(1));
}

static class InputReader {
    public BufferedReader reader;
    public StringTokenizer tokenizer;

    public InputReader(InputStream stream) {
        reader = new BufferedReader(new InputStreamReader
            (stream), 32768);
        tokenizer = null;
    }

    public String next() {
        while (tokenizer == null || !tokenizer.
            hasMoreTokens()) {
            try {
                tokenizer = new StringTokenizer(reader.
                    readLine());
            } catch (IOException e) {
                throw new RuntimeException(e);
            }
        }
        return tokenizer.nextToken();
    }

    public int nextInt() {
        return Integer.parseInt(next());
    }

    public double nextDouble(){
        return Double.parseDouble( next() );
    }
}

static class MyCom implements Comparator<Integer> {
    public int compare(Integer i1, Integer i2) {
        return i2 - i1;
    }
}
```

```
}
}
```

3 Data Structure

3.1 Disjoint Set

```
struct DS{
    vector<int> p;
    DS(int n){ for(int i=0;i<n;i++) p.push_back(i); }
    // zero-based
    int find(int x){ return x == p[x] ? x : p[x] = find(p[x]); } // Complexity : O(a(N))
    void join(int x,int y){ p[find(x)] = find(y); } // Complexity : O(a(N))
};
```

3.2 Segment Tree

```
/* HDU 1166 Partial Code */
struct ST{
    struct Node{
        int value,lazy;
        Node *lc,*rc;
        Node():lc(NULL),rc(NULL),lazy(0){}
        void pull(){ value = lc->value + rc->value; }
        void push(){
            if(!lazy) return;
            if(lc){ lc->lazy = lazy;lc->value += lazy; }
            if(rc){ rc->lazy = lazy;rc->value += lazy; }
            lazy = 0;
        }
    };
    vector<int> A;

    Node* build(int L,int R){
        Node *node = new Node();
        if(L == R){
            node->value = A[L];
            return node;
        }
        int mid = (L+R)>>1;
        node->lc = build(L,mid);
        node->rc = build(mid+1,R);
        node->pull();
        return node;
    }

    void modify(Node *node,int L,int R,int ql,int qr,
        int d){
        if(R < ql || qr < L) return;
        if(ql <= L && R <= qr){
            node->lazy += d;
            node->value += d;
            return;
        }
        node->push();
        int mid = (L+R)>>1;
        modify(node->lc,L,mid,ql,qr,d);
        modify(node->rc,mid+1,R,ql,qr,d);
        node->pull();
    }

    int query(Node* node,int L,int R,int ql,int qr){
        if(R < ql || qr < L) return 0;
        if(ql <= L && R <= qr) return node->value;
        node->push();
        int mid = (L+R)>>1;
        return query(node->lc,L,mid,ql,qr) + query(node->rc,mid+1,R,ql,qr);
    }
};
```

```
void delete_(Node* now){
    if(!now) return;
    delete_(now->lc);
    delete_(now->rc);
    delete now;
}
};
```

3.3 Binary Index Tree

```
/*
    can single update, range query sum
    can't insert, delete
*/
struct BIT{
    vector<int> val;

    inline int lsb(int x){ return x & -x; }

    int sum(int x){
        int s = 0;
        while(x > 0){
            s += val[x];
            x -= lower_bit(x);
        }
        return s;
    }

    void update(int x,int d){
        while(x <= A.size()){
            val[x] += d;
            x += lower_bit(x);
        }
    }

    int query(int a,int b){
        if(a > b) swap(a,b);
        return sum(b)-sum(a-1);
    }
};

struct BITRMQ{
    vector<int> val,LT,RT;

    BITRMQ(){}
    BITRMQ(int n,int v):val(n+1,v){
        LT.resize(n+1); RT.resize(n+1);
        for(int i=0;i<=n;i++) LT[i] = RT[i] = i;
    }

    inline int lsb(int x){ return x & -x; }

    int query(int a,int b){
        if(a >= SZ(LT) || b >= SZ(LT) || a < 1 || b < 1) while(1);
        int s = LLONG_MAX,i = a,x = a,y = b;

        while(x + lsb(x) <= b){
            if(s > val[RT[x]]){ s = val[RT[x]]; i = RT[x]; }
            x += lsb(x);
        }
        if(s > val[x]){ s = val[x]; i = x; }
        while(y != x){
            if(s > val[LT[y]]){ s = val[LT[y]]; i = LT[y]; }
            y -= lsb(y);
        }

        return i;
    }

    void _magic(int now,int x,int d,bool LR){
        vector<int> &T = LR ? LT : RT;
        if(T[now] != x){ if(val[T[now]] > d) T[now] = x; }
        else{
            int a = now,b = now;
            if(LR) a = now - lsb(now) + 1;
        }
    }
};
```

```

        else b = min(SZ(T)-1, now + lsb(now) - 1);
        if(a <= x-1){
            int s = query(a, x-1);
            if(val[s] < d) T[now] = s;
        }
        if(x+1 <= b){
            int s = query(x+1, b);
            if(val[s] < d) T[now] = s;
        }
    }
}

void update(int x, int d){
    val[x] = d;
    for(int now=x; now<=SZ(val); now+=lsb(now))
        _magic(now, x, d, true);
    for(int now=x; now>0; now-=lsb(now)) _magic(now, x, d, false);
}
};

```

3.4 zkw Segment Tree.cpp

```

const int NUM = 100;

int M, A[NUM], T[NUM*4];

// 1
// 2 3
// 4 5 6 7
// x 1 2 x
// one-based
void Build(int N){
    while(M=1; M<N+2; M<=1);
    for(int i=1; i<=N; i++) T[M+i] = A[i];
    for(int i=M-1; i--){ T[i] = T[i<<1]+T[i<<1|1]; }
}

// Single modify
void Modify(int x, int d){
    T[x+=M] = d;
    for(x>>1; x>>=1) T[x] = T[x<<1]+T[x<<1|1];
}

// Range query
int Query(int L, int R){
    L = L+M-1; R = R+M+1;
    int ans = 0;
    for(; L^R^1; L>>=1, R>>=1){
        if(~L&1) ans += T[L^1];
        if(R&1) ans += T[R^1];
    }
    return ans;
}

```

3.5 Treap

```

struct Treap {
    int key, pri, val, sz, lazy;
    Treap *l, *r;
    Treap(int _key, int _val): key(_key), val(_val),
        pri(rand()), sz(1), lazy(0), l(NULL), r(NULL){
    }
};

inline int Size(Treap* t)
{
    return t? t->sz:0;
}

inline void Pull(Treap* t)
{
    t->sz = Size(t->l) + Size(t->r) + 1;
}

void Push(Treap* t)
{
    t->val += t->lazy;
    if (t->l) t->l->lazy += t->lazy;
    if (t->r) t->r->lazy += t->lazy;
    t->lazy = 0;
}

```

```

Treap* Merge(Treap* a, Treap* b)
{
    if (!a || !b) return a ? a : b;
    if (a->pri > b->pri) {
        a->r = Merge(a->r, b); Pull(a); return a;
    } else {
        b->l = Merge(a, b->l); Pull(b); return b;
    }
}

void Split(Treap* t, int k, Treap*& a, Treap*& b)
{
    if (!t) a = b = NULL;
    else {
        if (t->key <= k) {
            a = t; Split(t->r, k, a->r, b); Pull(a);
        } else {
            b = t; Split(t->l, k, a, b->l); Pull(b);
        }
    }
}

Treap* Del(Treap* t, int k) //delete all key=k
{
    if (t->key == k) {return Merge(t->l, t->r);
    } else if (k < t->key) { t->l = Del(t->l, k);
        return t;
    } else { t->r = Del(t->r, k); return t;
    }
}

Treap* insert(Treap* t, int key, int val)
{
    Treap *tl, *tr;
    Split(t, key, tl, tr);
    Treap tmp(key, val);
    Treap *ans = &tmp;
    Merge(ans, tl); Merge(ans, tr);
    return ans;
}

```

3.6 monotonic-queue

```

template <typename Item>
struct mqueue {
    deque<Item> data, aux;
    void push(Item& x)
    {
        data.push_back(x);
        while (!aux.empty() && aux.back() < x)
            aux.pop_back();
        aux.push_back(x);
    }
    void pop()
    {
        if (data.front() == aux.front())
            aux.pop_front();
        data.pop_front();
    }
    int size()
    {
        return data.size();
    }
    Item max()
    {
        return aux.front();
    }
};

```

4 Graph

4.1 BCC

```

int adj[9][9];
int visit[9], low[9], t = 0;
int stack[9], top = 0;
int contract[9];
void DFS(int i, int p)
{

```

```

visit[i] = low[i] = ++t;
stack[top++] = i; // push i
for (int j=0; j<9; ++j)
    if (adj[i][j]){
        if (!visit[j]) DFS(j, i); // tree edge
        if (!(j == p && adj[i][j] == 1)) // tree edge + back edge
            low[i] = min(low[i], low[j]);
    }

if (visit[i] == low[i]) // 形成BCC i點會是BCC裡
                        // 面，最早拜訪的點。
{
    int j;
    do {
        j = stack[--top]; // pop j
        contract[j] = i;
    } while (i != j);
}

void tarjan()
{
    memset(visit, 0, sizeof(visit));
    t = 0;

    for (int i=0; i<9; ++i)
        if (!visit[i])
            DFS(i, i);
}

```

4.2 SCC

```

vector<int> e[10000]; int visit[10000], low[10000]; bool
instack[10000]; int belong[10000]; stack<int> s;
int t; int num; //number of SCC
void DFS(int u)
{
    visit[u] = low[u] = ++t; //進行標號
    s.push(u); instack[u] = true;
    for (int i = 0; i < e[u].size(); i++) {
        int v = e[u][i];
        if (!visit[v]) {
            DFS(v); low[u] = min(low[u], low[v]); // 找
            // u 的最上層祖先
        }
        if (instack[v]) low[u] = min(low[u], visit[v]);
        //還在stack中 用 visit的值
    }
    if (visit[u] == low[u]){//SCC
        num++; int v = s.top(); s.pop();
        instack[v] = false; belong[v] = num;
        while (v != u) {
            v = s.top(); s.pop();
            belong[v] = num; instack[v] = false;
        }
    }
}

int Tarjan(int n) //n:number of vertex 0-based
{
    t = 0, num = 0;
    memset(visit, 0, sizeof(visit));
    for (int i = 0; i < n; i++) e[i].clear();
    for (int i = 0; i < n; i++)
        if (!visit[i]) DFS(i);
    return num;
}

```

4.3 SPFA

```

struct Edge {
    int v, cost;
    Edge(int _v=0, int _cost=0):v(_v), cost(_cost){}
};
vector<Edge> E[MAXN]; //MAXN:num of point
bool visited[MAXN]; int cnt[MAXN]; int dist[MAXN];
bool SPFA(int start, int n)

```

```

{
    memset(visited, 0, sizeof(visited));
    for (int i=1; i<n; i++) dist[i]=INT_MAX;
    visited[start]=true; dist[start]=0;
    queue<int> que;
    while(!que.empty()) que.pop();
    que.push(start); cnt[start]=1;
    while(!que.empty()){
        int u=que.front();
        que.pop();
        visited[u]=false;
        for (int i=0; i<E[u].size(); i++){
            int v=E[u][i].v;
            if (dist[u]!=INT_MAX && dist[v]>dist[u]+E[u][i].cost){
                dist[v]=dist[u]+E[u][i].cost;
                if (!visited[v]) {
                    visited[v]=true;
                    que.push(v);
                    if (++cnt[v]>n) return false; //有負
                    //環
                }
            }
        }
    }
    return true; //正常
}

```

4.4 Dijkstra

```

int* Dijkstra(vector<VPPI> E, int N, int S){
    bool *visit=new bool[N+1]; for (int i=1; i<=N; i++)
        visit[i]=false;
    int *D=new int[N+1]; for (int i=1; i<=N; i++) D[i]=INF;
    priority_queue<PII, VPPI, greater<PII>> P;
    P.push(MP(0, S)); D[S]=0;
    while(!P.empty()){
        int weight=P.top().ff, now=P.top().ss; P.pop();
        if (visit[now]) continue;
        visit[now]=true;
        for (auto i:E[now]){
            int potential=D[now]+i.ff;
            if (!visit[i.ss] && potential < D[i.ss]){
                P.push(MP(D[i.ss]=potential, i.ss));
            }
        }
    }
    return D;
}

```

4.5 Floyd-Warshall

```

#include<bits/stdc++.h>
const int N = 500;
int dp[N][N];
void floyd_warshall()
{
    for (int k = 0; k < N; k++)
        for (int i = 0; i < N; i++)
            for (int j = 0; j < N; j++)
                if (dp[i][k]!=INT_MAX && dp[k][j]!=INT_MAX)
                    dp[i][j] = min(dp[i][j], dp[i][k] + dp[k][j]);
}

```

4.6 Bipartite Match

```

#include <bits/stdc++.h>
using namespace std;
vector<int> g[10000];
bool check[10000];
int match[10000];
int num_left, num_right;
void init(int n)
{
    num_left = num_right = 0;
    for (int i = 0; i < n; i++)

```

```

        g[i].clear();
    }
    bool DFS(int u)
    {
        for (int i = 0; i < g[u].size(); i++) {
            int v = g[u][i];
            if (!check[v]) {
                check[v] = true;
                if (match[v] == -1 || DFS(match[v]))
                    /
                    {
                        match[v] = u;
                        match[u] = v;
                        return true;
                    }
            }
        }
        return false;
    }
    int Hungarian_DFS() //匈牙利算法
    {
        int ans = 0;
        memset(match, -1, sizeof(match));
        for (int i = 0; i < num_left; i++) { //只要對二分圖
            的一邊即可
            memset(check, 0, sizeof(check));
            if (DFS(i))
                ans++;
        }
        return ans;
    }
    int Hungarian_BFS()
    {
        int prev[10000];
        int ans = 0;
        memset(match, -1, sizeof(match));
        for (int i = 0; i < num_left; i++) {
            memset(check, 0, sizeof(check));
            if (match[i] == -1) {
                queue<int> q;
                q.push(i);
                prev[i] = -1;
                bool flag = false;
                while (!q.empty() && !flag) {
                    int u = q.front();
                    q.pop();
                    for (int j = 0; j < g[u].size() && !
                        flag; j++) {
                        int v = g[u][j];
                        if (!check[v]) {
                            check[v] = true;
                            if (match[v] != -1) {
                                q.push(match[v]);
                                prev[match[v]] = u;
                            } else {
                                flag = true;
                                int d = u, e = v;
                                while (d != -1) {
                                    int t = match[d];
                                    match[d] = e;
                                    match[e] = d;
                                    d = prev[d];
                                    e = t;
                                }
                            }
                        }
                    }
                }
                if (match[i] != -1)
                    ans++;
            }
        }
        return ans;
    }
}

```

4.7 KM-Match

```

#include <bits/stdc++.h>
using namespace std;
const int MAXN = 110;

```

```

int n;
int g[MAXN][MAXN], lx[MAXN], ly[MAXN];
int match[MAXN], slack[MAXN];
bool vsx[MAXN], vsy[MAXN];

bool find(int x)
{
    if(vsx[x]) return false;
    vsx[x] = 1;
    for (int i = 0; i < n; i++) {
        if (vsy[i])
            continue;
        int t = lx[x] + ly[i] - g[x][i];
        if (!t) {
            vsy[i] = 1;
            if (match[i] == -1 || find(match[i])) {
                match[x] = i;
                return true;
            }
        } else
            slack[i] = min(slack[i], t);
    }
    return false;
}

int km(bool MIN = false) //二分圖最大匹配
{
    if (MIN)
        for (int i = 0; i < n; i++)
            for (int j = 0; j < n; j++)
                g[i][j] = -g[i][j];
    fill(lx, lx + n, INT_MAX);
    fill(ly, ly + n, 0);
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            lx[i] = min(lx[i], g[i][j]);
    memset(match, -1, sizeof(match));
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++)
            fill(slack, slack + n, INT_MAX);
        while (true) {
            memset(vsx, 0, sizeof(vsx));
            memset(vsy, 0, sizeof(vsy));
            if (find(i))
                break;
            int d = INT_MAX;
            for (int j = 0; j < n; j++)
                if (!vsy[j])
                    d = min(d, slack[j]);
            for (int j = 0; j < n; j++) {
                if (vsx[j])
                    lx[j] -= d;
                if (vsy[j])
                    ly[j] += d;
                else
                    slack[j] -= d;
            }
        }
    }
    int sum = 0;
    for (int i = 0; i < n; i++)
        sum += g[match[i]][i];
    if (MIN) {
        sum = -sum;
        for (int i = 0; i < n; i++)
            for (int j = 0; j < n; j++)
                g[i][j] = -g[i][j];
    }
    return sum;
}

```

4.8 General-Match

```

#include <bits/stdc++.h>
using namespace std;
struct DisjointSet {
    int N;
    vector<int> p;
    DisjointSet(int n)
        : N(n)
        , p(vector<int>(N))
    {
    }
}

```

```

{
    init();
}
void init()
{
    for (int i = 0; i < N; i++)
        p[i] = i;
}
int find(int x)
{
    return p[x] == x ? x : p[x] = find(p[x]);
}
void U(int a, int b)
{
    p[find(b)] = find(a);
}
};
struct GMatch {
    int N;
    vector<vector<int>> > vc;
    DisjointSet djs;
    vector<int> m, d, c1, c2, p, vis;
    queue<int> q;
    int ts;
    GMatch(int n)
        : N(n)
        , vc(vector<vector<int>>(N + 1))
        , djs(DisjointSet(N))
        , ts(0)
    {}
}
void add(int a, int b)
{
    vc[a].push_back(b);
    vc[b].push_back(a);
}
void path(int x, int r)
{
    if (x == r)
        return;
    if (d[x] == 0) {
        int i = p[x], j = p[p[x]];
        path(j, r);
        m[i] = j, m[j] = i;
    }
    else if (d[x] == 1) {
        int i = c1[x], j = c2[x];
        path(i, m[x]);
        path(j, r);
        m[i] = j, m[j] = i;
    }
}
void blossom(int x, int y, int bi)
{
    for (int i = djs.find(x); i != bi; i = djs.find(p[i])) {
        djs.U(bi, i);
        if (d[i] == 1)
            c1[i] = x, c2[i] = y, q.push(i);
    }
}
int lca(int x, int y, int r)
{
    ts++;
    vis[r] = ts;
    for (int i = djs.find(x); i != r; i = djs.find(p[i]))
        vis[i] = ts;
    int b;
    for (b = djs.find(y); vis[b] != ts; b = djs.find(p[b]))
        ;
    return b;
}
bool Match(int x)
{
    djs.init();
    d = vector<int>(N + 1, -1);
    d[x] = 0;
    q = queue<int>();
    q.push(x);
    while (!q.empty()) {

```

```

        int u = q.front();
        q.pop();
        for (int v : vc[u]) {
            if (m[v] != v && djs.find(u) != djs.find(v)) {
                if (d[v] == -1) {
                    if (m[v] == -1) {
                        path(u, x);
                        m[u] = v, m[v] = u;
                        return true;
                    }
                    else {
                        p[v] = u, p[m[v]] = v;
                        d[v] = 1, d[m[v]] = 0;
                        q.push(m[v]);
                    }
                }
                else {
                    if (d[djs.find(v)] == 0) {
                        int bi = lca(u, v, x);
                        blossom(u, v, bi);
                        blossom(v, u, bi);
                    }
                }
            }
        }
    }
    return false;
}
int Solve()
{
    m = c1 = c2 = d = p = vis = vector<int>(N + 1, -1);
    int ans = 0;
    for (int i = 0; i < N; i++) {
        if (m[i] == -1) {
            if (Match(i))
                ans++;
            else
                m[i] = i;
        }
    }
    return ans;
}
};

```

4.9 General-Weighted-Match

```

#include <iostream>
#include <cstdio>
#include <algorithm>
#include <vector>
using namespace std;

typedef long long s64;

const int INF = 2147483647;

const int MaxN = 400;
const int MaxM = 79800;

template <class T>
inline void tension(T &a, const T &b){
    if (b < a)
        a = b;
}
template <class T>
inline void relax(T &a, const T &b){
    if (b > a)
        a = b;
}
template <class T>
inline int size(const T &a){
    return (int)a.size();
}

inline int getint(){
    char c;
    while (c = getchar(), '0' > c || c > '9');
```



```

int res = c - '0';
while (c = getchar(), '0' <= c && c <= '9')
    res = res * 10 + c - '0';
return res;
}

const int MaxNX = MaxN + MaxN;

struct edge{
    int v, u, w;

    edge(){}
    edge(const int &_v, const int &_u, const int &_w)
        : v(_v), u(_u), w(_w){}
};

int n, m;
edge mat[MaxNX + 1][MaxNX + 1];

int n_matches;
s64 tot_weight;
int mate[MaxNX + 1];
int lab[MaxNX + 1];

int q_n, q[MaxN];
int fa[MaxNX + 1], col[MaxNX + 1];
int slackv[MaxNX + 1];

int n_x;
int bel[MaxNX + 1], blofrom[MaxNX + 1][MaxN + 1];
vector<int> bloch[MaxNX + 1];

inline int e_delta(const edge &e){ // does not work
    inside blossoms
    return lab[e.v] + lab[e.u] - mat[e.v][e.u].w * 2;
}

inline void update_slackv(int v, int x){
    if (!slackv[x] || e_delta(mat[v][x]) < e_delta(mat[
        slackv[x]][x]))
        slackv[x] = v;
}

inline void calc_slackv(int x){
    slackv[x] = 0;
    for (int v = 1; v <= n; v++){
        if (mat[v][x].w > 0 && bel[v] != x && col[bel[v]]
            == 0)
            update_slackv(v, x);
    }
}

inline void q_push(int x){
    if (x <= n) q[q_n++] = x;
    else{
        for (int i = 0; i < size(bloch[x]); i++){
            q_push(bloch[x][i]);
        }
    }
}

inline void set_mate(int xv, int xu){
    mate[xv] = mat[xv][xu].u;
    if (xv > n){
        edge e = mat[xv][xu];
        int xr = blofrom[xv][e.v];
        int pr = find(bloch[xv].begin(), bloch[xv].end(),
            xr) - bloch[xv].begin();
        if (pr % 2 == 1){
            reverse(bloch[xv].begin() + 1, bloch[xv].end());
            pr = size(bloch[xv]) - pr;
        }
        for (int i = 0; i < pr; i++){
            set_mate(bloch[xv][i], bloch[xv][i ^ 1]);
        }
        set_mate(xr, xu);
        rotate(bloch[xv].begin(), bloch[xv].begin() + pr,
            bloch[xv].end());
    }
}

inline void set_bel(int x, int b){
    bel[x] = b;
    if (x > n){
        for (int i = 0; i < size(bloch[x]); i++){
            set_bel(bloch[x][i], b);
        }
    }
}

```

```

inline void augment(int xv, int xu){
    while (true){
        int xnu = bel[mate[xv]];
        set_mate(xv, xu);
        if (!xnu) return;
        set_mate(xnu, bel[fa[xnu]]);
        xv = bel[fa[xnu]], xu = xnu;
    }
}

inline int get_lca(int xv, int xu){
    static bool book[MaxNX + 1];
    for (int x = 1; x <= n_x; x++){
        book[x] = false;
        while (xv || xu){
            if (xv){
                if (book[xv]) return xv;
                book[xv] = true;
                xv = bel[mate[xv]];
                if (xv)xv = bel[fa[xv]];
            }
            if (xu){
                if (book[xu]) return xu;
                book[xu] = true;
                xu = bel[mate[xu]];
                if (xu)xu = bel[fa[xu]];
            }
            swap(xv, xu);
        }
    }
    return 0;
}

inline void add_blossom(int xv, int xa, int xu){
    int b = n + 1;
    while (b <= n_x && bel[b]b++){
        if (b > n_x)n_x++;
        lab[b] = 0;
        col[b] = 0;
        mate[b] = mate[xa];
        bloch[b].clear();
        bloch[b].push_back(xa);
        for (int x = xv; x != xa; x = bel[fa[bel[mate[x]]]])
            bloch[b].push_back(x), bloch[b].push_back(bel[mate[
                x]]), q_push(bel[mate[x]]);
        reverse(bloch[b].begin() + 1, bloch[b].end());
        for (int x = xu; x != xa; x = bel[fa[bel[mate[x]]]])
            bloch[b].push_back(x), bloch[b].push_back(bel[mate[
                x]]), q_push(bel[mate[x]]);
        set_bel(b, b);
        for (int x = 1; x <= n_x; x++){
            mat[b][x].w = mat[x][b].w = 0;
            blofrom[b][x] = 0;
        }
        for (int i = 0; i < size(bloch[b]); i++){
            int xs = bloch[b][i];
            for (int x = 1; x <= n_x; x++){
                if (mat[b][x].w == 0 || e_delta(mat[xs][x]) <
                    e_delta(mat[b][x]))
                    mat[b][x] = mat[xs][x], mat[x][b] = mat[x][xs];
                for (int x = 1; x <= n_x; x++){
                    if (blofrom[xs][x])
                        blofrom[b][x] = xs;
                }
            }
            calc_slackv(b);
        }
    }

    inline void expand_blossom1(int b){ // lab[b] == 1
        for (int i = 0; i < size(bloch[b]); i++){
            set_bel(bloch[b][i], bloch[b][i]);
        }
        int xr = blofrom[b][mat[b][fa[b]].v];
        int pr = find(bloch[b].begin(), bloch[b].end(), xr) -
            bloch[b].begin();
        if (pr % 2 == 1){
            reverse(bloch[b].begin() + 1, bloch[b].end());
            pr = size(bloch[b]) - pr;
        }
        for (int i = 0; i < pr; i += 2){
            int xs = bloch[b][i], xns = bloch[b][i + 1];
            fa[xs] = mat[xns][xs].v;
            col[xs] = 1, col[xns] = 0;
            slackv[xs] = 0, calc_slackv(xns);
            q_push(xns);
        }
        col[xr] = 1; fa[xr] = fa[b];
        for (int i = pr + 1; i < size(bloch[b]); i++){
            int xs = bloch[b][i];
            col[xs] = -1;
            calc_slackv(xs);
        }
        bel[b] = 0;
    }
}

```



```

}
inline void expand_blossom_final(int b){ // at the
    final stage
    for (int i = 0; i < size(bloch[b]); i++){
        if (bloch[b][i] > n && lab[bloch[b][i]] == 0)
            expand_blossom_final(bloch[b][i]);
        else set_bel(bloch[b][i], bloch[b][i]);
    }
    bel[b] = 0;
}

inline bool on_found_edge(const edge &e){
    int xv = bel[e.v], xu = bel[e.u];
    if (col[xu] == -1){
        int nv = bel[mate[xu]];
        fa[xu] = e.v;
        col[xu] = 1, col[nv] = 0;
        slackv[xu] = slackv[nv] = 0;
        q_push(nv);
    } else if (col[xu] == 0){
        int xa = get_lca(xv, xu);
        if (!xa){
            augment(xv, xu), augment(xu, xv);
            for (int b = n + 1; b <= n_x; b++){
                if (bel[b] == b && lab[b] == 0)
                    expand_blossom_final(b);
            }
            return true;
        } else add_blossom(xv, xa, xu);
    }
    return false;
}

bool match()
{
    for (int x = 1; x <= n_x; x++){
        col[x] = -1, slackv[x] = 0;
        q_n = 0;
        for (int x = 1; x <= n_x; x++){
            if (bel[x] == x && !mate[x])
                fa[x] = 0, col[x] = 0, slackv[x] = 0, q_push(x);
        }
        if (q_n == 0)
            return false;
        while (true){
            for (int i = 0; i < q_n; i++){
                int v = q[i];
                for (int u = 1; u <= n; u++){
                    if (mat[v][u].w > 0 && bel[v] != bel[u]){
                        int d = e_delta(mat[v][u]);
                        if (d == 0){
                            if (on_found_edge(mat[v][u]))
                                return true;
                        } else if (col[bel[u]] == -1 || col[bel[u]] == 0)
                            update_slackv(v, bel[u]);
                    }
                }
            }
            int d = INF;
            for (int v = 1; v <= n; v++){
                if (col[bel[v]] == 0)
                    tension(d, lab[v]);
            }
            for (int b = n + 1; b <= n_x; b++){
                if (bel[b] == b && col[b] == 1)
                    tension(d, lab[b] / 2);
            }
            for (int x = 1; x <= n_x; x++){
                if (bel[x] == x && slackv[x]){
                    if (col[x] == -1)
                        tension(d, e_delta(mat[slackv[x]][x]));
                    else if (col[x] == 0)
                        tension(d, e_delta(mat[slackv[x]][x]) / 2);
                }
            }
            for (int v = 1; v <= n; v++){
                if (col[bel[v]] == 0)
                    lab[v] -= d;
                else if (col[bel[v]] == 1)
                    lab[v] += d;
            }
            for (int b = n + 1; b <= n_x; b++){
                if (bel[b] == b){
                    if (col[bel[b]] == 0)
                        lab[b] += d * 2;
                }
            }
        }
    }
}

```

```

        else if (col[bel[b]] == 1)
            lab[b] -= d * 2;
    }
    q_n = 0;
    for (int v = 1; v <= n; v++){
        if (lab[v] == 0) // all unmatched vertices'
            labels are zero! cheers!
            return false;
        for (int x = 1; x <= n_x; x++){
            if (bel[x] == x && slackv[x] && bel[slackv[x]] !=
                x && e_delta(mat[slackv[x]][x]) == 0){
                if (on_found_edge(mat[slackv[x]][x]))
                    return true;
            }
        }
        for (int b = n + 1; b <= n_x; b++){
            if (bel[b] == b && col[b] == 1 && lab[b] == 0)
                expand_blossom1(b);
        }
        return false;
    }
}

void calc_max_weight_match()
{
    for (int v = 1; v <= n; v++)
        mate[v] = 0;
    n_x = n;
    n_matches = 0;
    tot_weight = 0;
    bel[0] = 0;
    for (int v = 1; v <= n; v++)
        bel[v] = v, bloch[v].clear();
    for (int v = 1; v <= n; v++)
        for (int u = 1; u <= n; u++){
            blofrom[v][u] = v == u ? v : 0;
        }
    int w_max = 0;
    for (int v = 1; v <= n; v++)
        for (int u = 1; u <= n; u++){
            relax(w_max, mat[v][u].w);
        }
    for (int v = 1; v <= n; v++)
        lab[v] = w_max;
    while (match())
        n_matches++;
    for (int v = 1; v <= n; v++)
        if (mate[v] && mate[v] < v)
            tot_weight += mat[v][mate[v]].w;
}

int main(){
    n = getint(), m = getint();
    for (int v = 1; v <= n; v++)
        for (int u = 1; u <= n; u++){
            mat[v][u] = edge(v, u, 0);
        }
    for (int i = 0; i < m; i++){
        int v = getint(), u = getint(), w = getint();
        mat[v][u].w = mat[u][v].w = w;
    }
    calc_max_weight_match();
    printf("%lld\n", tot_weight);
    for (int v = 1; v <= n; v++)
        printf("%d ", mate[v]);
    printf("\n");
    return 0;
}

```

4.10 Directed-MST

```

const int MAXN = 1010;
int pre[MAXN], min_dist[MAXN];
struct Edge {
    int from, to, cost;
    Edge() {}
    Edge(int _from, int _to, int _cost)
        : from(_from)
        , to(_to)
        , cost(_cost)
    {}
};
vector<Edge> E;
int solve(int n, int m, int root)
{

```

```

int ans = 0;
while (true) {
    fill(min_dist, min_dist + MAXN, INT_MAX);
    for (int i = 0; i < E.size(); i++) {
        int u = E[i].from, v = E[i].to, cost = E[i].cost;
        if (cost < min_dist[v] && v != u) {
            min_dist[v] = cost;
            pre[v] = u;
        }
    }
    for (int i = 1; i <= n; i++)
        if (min_dist[i] == INT_MAX && i != root)
            return -1;
    int cnt_node = 1, id[MAXN], vis[MAXN];
    memset(id, -1, sizeof(id));
    memset(vis, 0, sizeof(vis));
    min_dist[root] = 0;
    for (int i = 1; i <= n; i++) {
        ans += min_dist[i];
        int v = i;
        while (vis[v] != i && id[v] == -1 && v != root) {
            vis[v] = i;
            v = pre[v];
        }
        if (id[v] == -1 && v != root) {
            for (int u = v; u != v; u = pre[u])
                id[u] = cnt_node;
            cnt_node++;
        }
    }
    if (cnt_node == 1)
        break;
    for (int i = 1; i <= n; i++)
        if (id[i] == -1)
            id[i] = cnt_node++;
    for (int i = 0; i < E.size(); i++) {
        int v = E[i].to;
        E[i].from = id[E[i].from];
        E[i].to = id[E[i].to];
        if (E[i].from != E[i].to)
            E[i].cost -= min_dist[v];
    }
    n = cnt_node - 1;
    root = id[root];
}
return ans;
}

```

4.11 LCA

```

/*
多個點的LCA => DFS走訪順序中min 和 max 的LCA
*/
#include <bits/stdc++.h>
using namespace std;
const int MAXN = 1000;
vector<int> tree[MAXN];
int depth[MAXN];
int father[MAXN][20];
void init()
{
    memset(depth, 0, sizeof(depth));
    memset(father, -1, sizeof(father));
}
void dfs(int u)
{
    for (int i = 0; i < tree[u].size(); i++) {
        int v = tree[u][i];
        if (!depth[v]) {
            depth[v] = depth[u] + 1;
            father[v][0] = u;
            dfs(v);
        }
    }
}
void build()
{
    for (int i = 1; (1 << i) < MAXN; i++) {

```

```

        for (int j = 0; j < MAXN; j++) {
            if (father[j][i - 1] != -1) {
                father[j][i] = father[father[j][i - 1]][i - 1];
            }
        }
    }
}
int lca(int u, int v)
{
    if (depth[u] < depth[v]) swap(u, v);
    for (int i = log2(MAXN - 1); i >= 0; i--)
    {
        if (father[u][i] != -1 && depth[father[u][i]] >= depth[v])
            u = father[u][i];
    }
    if (u == v) return v;
    for (int i = log2(MAXN - 1); i >= 0; i--)
    {
        if (father[u][i] != father[v][i])
            u = father[u][i], v = father[v][i];
    }
    return father[u][0];
}

```

4.12 MST-kruskal

```

#include <bits/stdc++.h>
using namespace std;
const int N = 20005;
struct Edge {
    int u, v, cost;
    Edge(int _u = 0, int _v = 0, int _cost = 0) {
        u = _u, v = _v, cost = _cost;
    }
    bool operator < (const Edge & a) const {
        return cost < a.cost;
    }
};
vector<Edge> E;
int ds[N];
void Init (int n) {
    E.clear();
    for (int i = 0; i < n; i++) ds[i] = i;
}
int Find(int x) {
    return (ds[x] == x) ? x : (ds[x] = Find(ds[x]));
}
int kruskal(int n) //point_number;
{
    sort(E.begin(), E.end());
    int ans = 0;
    int num = 1;
    for (auto &e : E) {
        int u = e.u, v = e.v;
        u = Find(u), v = Find(v);
        if (u != v) {
            ds[u] = v;
            num++;
            ans += e.cost;
        }
        if (num == n) break;
    }
    return ans;
}

```

4.13 Manhattan-Mst

```

#include <bits/stdc++.h>
using namespace std;
const int N = 100100;
struct Point {
    int x, y, id;
    Point(int _x, int _y, int _id)
        : x(_x)
        , y(_y)
        , id(_id)

```

```

{
}
bool operator<(const Point& p) const
{
    return (x != p.x) ? x < p.x : y < p.y;
}
};

struct BIT {
    int min_val, pos;
    void init()
    {
        min_val = INT_MAX;
        pos = -1;
    }
} bit[N];
struct Edge {
    int u, v, d;
    Edge() {}
    Edge(int _u, int _v, int _d)
        : u(_u)
        , v(_v)
        , d(_d)
    {}
    bool operator<(const Edge& e) const
    {
        return d < e.d;
    }
};
vector<Point> p;
vector<Edge> E;
int ds[N]; //disjoint set for kruskal

void add_edge(int u, int v, int d)
{
    E.push_back(Edge(u, v, d));
}
int find(int x)
{
    return ds[x] = (x == ds[x] ? x : find(ds[x]));
}
int dist(int i, int j)
{
    return abs(p[i].x - p[j].x) + abs(p[i].y - p[j].y);
}
inline int lowbit(int x)
{
    return x & (-x);
}
void update(int x, int val, int pos)
{
    for (int i = x; i >= 1; i -= lowbit(i)) {
        if (val < bit[i].min_val)
            bit[i].min_val = val, bit[i].pos = pos;
    }
}
int query(int x, int m)
{
    int min_val = INT_MAX, pos = -1;
    for (int i = x; i >= 1; i -= lowbit(i)) {
        if (bit[i].min_val < min_val) {
            min_val = bit[i].min_val, pos = bit[i].pos;
        }
    }
    return pos;
}
int Manhattan_MST(vector<Point>& P)
{
    int n = P.size();
    for (int dir = 0; dir < 4; dir++) {
        if (dir == 1 || dir == 3) {
            for (int i = 0; i < n; i++)
                swap(P[i].x, P[i].y);
        } else if (dir == 2) {
            for (int i = 0; i < n; i++)
                P[i].x = -P[i].x;
        }

        int T[N], hs[N];
        sort(P.begin(), P.end());
        for (int i = 0; i < n; i++) { //discretize

```

```

            T[i] = hs[i] = p[i].y - p[i].x;
        }
        sort(hs, hs + n);
        int m = unique(hs, hs + n) - hs;
        for (int i = 1; i <= m; i++)
            bit[i].init();
        for (int i = n - 1; i >= 0; i--) {
            int pos = lower_bound(hs, hs + m, T[i]) -
                hs + 1; //Bit is 1-based
            int w = query(pos, m);
            if (w != -1)
                add_edge(p[i].id, p[w].id, dist(i, w));
            update(pos, p[i].x + p[i].y, i);
        }
    }
    sort(E.begin(), E.end());
    int ans = 0;
    int p = 1;
    for (int i = 0; i < n; i++)
        ds[i] = i;
    for (int i = 0; i < (int)E.size() && p <= n; i++) {
        int fa = find(E[i].u);
        int fb = find(E[i].v);
        if (fa != fb) {
            p++;
            ds[fa] = fb;
            ans += E[i].d;
        }
    }
    return ans;
}
}

```

4.14 Flow-Dinic

```

#include <bits/stdc++.h>
#define pb push_back
#define SZ(x) (int)x.size()
using namespace std;
struct Dinic {
    struct Edge {
        int v, f, re;
        Edge(int v, int f, int re)
            : v(v)
            , f(f)
            , re(re)
        {}
    };
    vector<vector<Edge>> E;
    vector<int> level;
    int N, s, t;
    Dinic(int N, int s, int t)
        : N(N)
        , s(s)
        , t(t)
    {}
    E.resize(N + 1);
    void AddEdge(int u, int v, int c)
    {
        E[u].pb({ v, c, SZ(E[v]) });
        E[v].pb({ u, 0, SZ(E[u]) - 1 });
    }
    bool BFS()
    {
        level.clear();
        for (int i = 0; i <= N; i++)
            level.pb(-1);
        queue<int> Q;
        Q.push(s);
        level[s] = 0;
        while (!Q.empty()) {
            int now = Q.front();
            Q.pop();
            for (auto i : E[now]) {
                if (i.f > 0 && level[i.v] == -1) {
                    level[i.v] = level[now] + 1;
                    Q.push(i.v);
                }
            }
        }
    }
}

```

```

    }
    return level[t] != -1;
}
int DFS(int now, int nf)
{
    if (now == t)
        return nf;
    int ans = 0;
    for (auto& i : E[now]) {
        if (i.f > 0 && level[i.v] == level[now] + 1) {
            int tf = DFS(i.v, min(nf, i.f));
            ans += tf;
            nf -= tf;
            i.f -= tf;
            E[i.v][i.re].f += tf;
            if (nf == 0)
                return ans;
        }
    }
    if (!ans)
        level[now] = -1;
    return ans;
}
int Flow()
{
    int ans = 0;
    while (BFS())
        ans += DFS(s, INT_MAX);
    return ans;
}
};

```

4.15 Flow-MinCost

```

#include <bits/stdc++.h>
using namespace std;
const int N = 1000;
struct Edge {
    int v; //連的點
    int cap; //容量
    int cost;
    int next; //下一條邊的
} e[N * N];
int id;
int p[N];
int pre[N];
int path[N];
int dist[N]; //dist;

void init() //初始化
{
    memset(e, 0, sizeof(e));
    memset(p, -1, sizeof(p));
    id = 0;
}

void add(int u, int v, int cap, int cost)
{
    e[id].v = v, e[id].cap = cap, e[id].cost = cost, e[id].next = p[u], p[u] = id++;
    e[id].v = u, e[id].cap = 0, e[id].cost = -cost, e[id].next = p[v], p[v] = id++;
}

bool SPFA(int s, int t)
{
    memset(pre, -1, sizeof(pre));
    fill(dist, dist + N, INT_MAX);
    bool vis[N] = {};
    dist[s] = 0;
    queue<int> q;
    q.push(s);
    vis[s] = true;
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        vis[u] = false;
        for (int i = p[u]; i != -1; i = e[i].next) {
            int v = e[i].v;
            if (e[i].cap > 0 && dist[u] + e[i].cost < dist[v]) {

```

```

                dist[v] = dist[u] + e[i].cost;
                pre[v] = u; //路徑
                path[v] = i; //邊的編號
                if (!vis[v])
                    vis[v] = true, q.push(v);
            }
        }
    }
    if (pre[t] == -1)
        return false;
    return true;
}

int MinCostFlow(int s, int t)
{
    int cost = 0;
    int flow = 0;
    while (SPFA(s, t)) {
        int f = INT_MAX;
        for (int u = t; u != s; u = pre[u])
            f = min(f, e[path[u]].cap);
        flow += f;
        cost += dist[t] * f;
        for (int u = t; u != s; u = pre[u]) {
            e[path[u]].cap -= f;
            e[path[u]^1].cap += f;
        }
    }
    return cost; //cost
}

```

4.16 HeavyLight-Decomposition

```

#include <bits/stdc++.h>
using namespace std;
const int MAXN = 3000;
int size[MAXN], pre[MAXN], son[MAXN], dep[MAXN];
vector<int> E[MAXN];
struct Node { // segmnet tree with lazy tag;
    Node * l, * r;
    int v, lazy;
}*root;
//1-based;
int dfs(int x, int fa)
{
    size[x] = 1;
    int max_v = INT_MIN;
    dep[x] = dep[fa] + 1;
    pre[x] = fa;
    for (auto &v : E[x]) {
        size[x] += dfs(v, x);
        if (size[v] > max_v) {
            max_v = size[v];
            son[x] = v;
        }
    }
    return size[x];
}

int no, pos[MAXN], top[MAXN];
int repos(int x, int fa, int tp) {
    pos[x] = ++no;
    top[x] = tp;
    if (son[x]) repos(son[x], x, tp);
    for (auto &v : E[x]) {
        if (v != son[x] && v != fa) repos(v, x, v);
    }
}

// 1-based segment tree
void update_seg(Node* root, int l, int r, int ql, int qr, int v) {
    ;
}

void query_seg(Node* root, int l, int r, int ql, int qr) {
    ;
}

void update(int x, int y, int v)
{
    while (top[x] != top[y]) {
        if (dep[x] < dep[y]) swap(x, y);
        update_seg(root, 1, MAXN, pos[top[x]], pos[x], v);
        x = pre[top[x]];
    }
}

```

```

    }
    update_seg(root,1,MAXN,min(pos[x],pos[y]),max(pos[x],pos[y]),v);
}
//query from x to y
void query(int x ,int y){
    int ans;
    while(top[x]!=top[y]){
        if(dep[x]<dep[y]) swap(x,y);
        ans+=query_seg(root,1,MAXN,pos[top[x]],pos[x]);
        x=pre[top[x]];
    }
    ans+=query_seg(root,1,MAXN,min(pos[x],pos[y]),max(pos[x],pos[y]));
}
}

```

4.17 Maximal-Clique

```

/*
 * compute maximal cliques
 * lmaximum clique=
 * lcomp(G)'s maximum independent setl
 * comp(G) Complete Graph's Edge - G's Edge
 */
#include <bits/stdc++.h>
using namespace std;
typedef unsigned long long ull;

ull adj[64];
vector<ull> cliques; // if ith bit is 1 then i is in
                    // that maximal clique

void BronKerbosch(ull R, ull P, ull X)
{
    if (P == 0 && X == 0) {
        cliques.push_back(R);
    }
    /*
     * Returns the number of trailing 0-bits in x,
     * starting at the least significant bit position
     *
     * If x is 0, the result is undefined.
     */
    int p = __builtin_ctzll(P | X);
    ull Q = P & ~adj[p];
    while (Q) {
        int i = __builtin_ctzll(Q);
        BronKerbosch(R | (1ULL << i), P & adj[i], X & adj[i]);
        Q&=~(1ULL<<i) ; P&=~(1ULL<<i); X|=(1ULL<<i);
    }
}

```

4.18 2SAT

```

#include <bits/stdc++.h>
using namespace std;

const int MAXN = 2010;
const int VN = MAXN * 2;
const int EN = 4000010;
#define False(a) a * 2
#define True(a) a * 2 + 1
class Graph {
public:
    void init()
    {
        size = 0;
        memset(head, -1, sizeof(head));
    }
}
/*
1) 如果給出A和B的限制關係，A和B必須一起選，(A and B) || (!A and !B) == true 那麼選A必須選B，建邊<i',j>和<j,i>還有<i',j'>和<j',i'>
2) 如果給出A和B的限制關係，選A不能選B，那麼(A && !B) || (!A && B) == true,建邊<i,j'>和<j,i'>

```

3) 如果必須選A,那麼A==true,建邊<i',i>
4) 如果A一定不能選，那麼!A==true.建邊<i,i'>

```

*/
void addEdge(int u, int v)
{
    E[size].v = v;
    E[size].next = head[u];
    head[u] = size++;
}

public:
    int size;
    int head[VN];
    struct Edge {
        int v, next;
    } E[EN];
} g;

class Two_Sat {
public:
    bool check(const Graph& g, const int n)
    {
        scc(g, n);
        for (int i = 0; i < n; ++i)
            if (belong[i * 2] == belong[i * 2 + 1])
                return false;
        return true;
    }

private:
    void tarjan(const Graph& g, const int u)
    {
        int v;
        DFN[u] = low[u] = ++idx;
        sta[top++] = u;
        inStack[u] = true;

        for (int e = g.head[u]; e != -1; e = g.E[e].next) {
            v = g.E[e].v;
            if (DFN[v] == -1) {
                tarjan(g, v);
                low[u] = min(low[u], low[v]);
            } else if (inStack[v]) {
                low[u] = min(low[u], DFN[v]);
            }
        }
        if (low[u] == DFN[u]) {
            ++bcnt;
            do {
                v = sta[--top];
                inStack[v] = false;
                belong[v] = bcnt;
            } while (u != v);
        }
    }

    void scc(const Graph& g, const int n)
    {
        top = idx = bcnt = 0;
        memset(DFN, -1, sizeof(DFN));
        memset(inStack, 0, sizeof(inStack));
        for (int i = 0; i < 2 * n; ++i) {
            if (DFN[i] == -1)
                tarjan(g, i);
        }
    }

private:
    int top, idx, bcnt;
    int sta[VN];
    int DFN[VN];
    int low[VN];
    int belong[VN];
    bool inStack[VN];
} sat;

```

4.19 Stable-Marriage

□定婚姻是□合数学里面的一个□□。

□□大概是这样的：有一个社团里有 n 个女生和 n 个男生，每位女生按照她的偏□程度将男生排序，同时每位男生也按照自己的偏□程度将女生排序。然后将这 n 个女生和 n 个男生配成完备婚姻。

如果存在两位女生 A 和 B ，两位男生 a 和 b ，使得 A 和 a □婚， B 和 b □婚，但是 A 更偏□ b 而不是 a ， b 更偏□ A 而不是 B ，□这个婚姻就是不□定的， A 和 b 可能背着别人相伴而走，因□他□都□□，与当前配偶比起□他□更偏□各自的新伴侣。如果完备婚姻不是不□定的，□称其是□定的。通过□明，可以得到每一个 n 女 n 男的社团，都存在□定婚姻的□□。但是这种情况只在异性的社团中存在。也就是□在同性的社团里面，□定婚姻的存在性将不再被保□。

Gale - Shapley 算法

while 存在男人 m 是自由的且还没对每个女人都求过婚
选□这个男人 m

令 w 是 m 的优先表中还没求过婚的最高排名的女人

if w 是自由的

(m, w) 变成□会状□

else w 当前与 m_1 □会

if w 更偏□ m_1 而不□ m

m 保持自由

else w 更偏□ m 而不□ m_1

(m, w) 变成□会状□

m_1 变成自由

endif

endif

endwhile

```
#include <iostream>
#include <queue>
#include <algorithm>
#include <cstdio>
#include <string.h>
using namespace std;
int gg[30][30], mm[30][30];
int a[30], n, ggpre[30], mmpre[30];
queue<int>my;
void stable_marriage()
{
    int i;
    memset(ggpre, 0, sizeof(ggpre)); //gg优先选□.
    memset(mmpre, -1, sizeof(mmpre)); //mm优先选□.
    int pm, pf;
    while (!my.empty())
    {
        pm = my.front();
        my.pop();
        pf = gg[pm][ggpre[pm]];
        ggpre[pm]++;
        if (mmpre[pf] < 0) mmpre[pf] = pm; //pf是自由的
        // (pm, pf) 变成□会状□
        else if (mm[pf][mmpre[pf]] < mm[pf][pm]) //pf更
            喜欢pm1, pm保持自由.
        {
            my.push(pm);
        }
        else //pf更喜欢pm, 而
            不是pm1, (pm, pf) 变成□会状□.
        {
            my.push(mmpre[pf]);
            mmpre[pf] = pm;
        }
    }
    for (i = 0; i < 26; i++)
        if (mmpre[i] > -1) ggpre[mmpre[i]] = i;
    for (i = 0; i < n; i++)
        printf("%c %c\n", a[i] + 'a', ggpre[a[i]] + 'A');
    puts("");
}
int main()
{
    int i, j, t;
    scanf("%d", &t);
    while (t--)
    {
        scanf("%d", &n);
        char temp, str[30];
        while (!my.empty())
            my.pop();
        for (i = 0; i < n; i++)
        {
```

```
scanf("%c", &temp);
a[i] = temp - 'a';
my.push(temp - 'a');
}
sort(a, a + n);
for (i = 0; i < n; i++)
    scanf("%c", &temp);
for (i = 0; i < n; i++)
{
    scanf("%s", str);
    for (j = 0; j < n; j++)
        gg[str[0] - 'a'][j] = str[j + 2] - 'A';
}
for (i = 0; i < n; i++)
{
    scanf("%s", str);
    for (j = 0; j < n; j++)
        mm[str[0] - 'A'][str[j + 2] - 'a'] = j;
}
stable_marriage();
}
return 0;
}
```

4.20 Euler-Circuit

```
#define eid w
void _EulerCircuit(int x){
    for(int i=0;i<(int)vc[x].size();i++){
        Edge e = vc[x][i];
        if(vis[e.eid]) continue;
        vis[e.eid] = 1;
        _EulerCircuit(e.to);
        eulercircuit.push_back(e.eid);
    }
}
bool EulerCircuit(){ // undirected
    if(!Connected()) return false;
    vis = vector<int>(M+1, 0);
    for(int i=0;i<N;i++){
        if(vc[i].size()&1)
            return false;
        //sort
        sort(vc[i].begin(), vc[i].end());
    }
    eulercircuit.clear();
    _EulerCircuit(0);
    //sort
    reverse(eulercircuit.begin(), eulercircuit.end());
    return true;
}
```

5 String Theory

5.1 KMP

```
// Complexity : O(T+P)
void predo(string pattern, int dp[]){
    dp[0] = 0;
    for(int i=1; i<pattern.size(); i++){
        dp[i] = dp[i-1];
        while(dp[i] > 0 && pattern[dp[i]] != pattern[i])
            dp[i] = dp[dp[i]-1];
        if(pattern[dp[i]] == pattern[i]) dp[i]++;
    }
}
void KMP(string text, string pattern){
    int dp[pattern.size()]; predo(pattern, dp);
    for(int i=0, match=0; i<text.size(); i++){
        while(match > 0 && pattern[match] != text[i])
            match = dp[match-1];
        if(pattern[match] == text[i]) match++;
        if(match == pattern.size()){
            // do something with i-pattern.size()+1
            match = dp[match-1];
        }
    }
}
```



```

    }
}
}

```

5.2 Z

```

void ZAlgorithm(string word,string pattern){
    int Z[word.size()+pattern.size()];
    string S = pattern+word;
    Z[0] = 0;
    for(int i=1,best=0;i<S.size();i++){
        if(best+Z[best] <= i)Z[i] = 0;
        else Z[i] = min(Z[i-best],best+Z[best]-i);
        while(S[i+Z[i]] == S[Z[i]])Z[i]++;
        if(i+Z[i] > best+Z[best])best = i;
    }
    for(int i=pattern.size();i<S.size();i++){
        if(Z[i] >= pattern.size())cout << i-pattern.
            size() << " ";
    }
}

```

5.3 Trie

```

const int MAXCHAR = 26;
const char CHAR = 'a';

struct Trie{
    struct Node{
        int N;
        Node* child[MAXCHAR];
        Node():N(-1){ for(int i=0;i<MAXCHAR;i++) child[i] =
            NULL; }
    };
    Node* root;

    Trie(){ root = new Node; }
    ~Trie(){ release(root); }

    void insert(string text, int id){
        Node* now = root;
        for(int i=0;i<SZ(text);i++){
            int c = text[i] - CHAR;
            if(now->child[c] == NULL) now->child[c] = new
                Node;
            now = now->child[c];
        }
        now->N = id;
    }

    void release(Node* now){
        for(int i=0;i<MAXCHAR;i++) if(now->child[i])
            release(now->child[i]);
        delete now;
    }
};

```

5.4 AC automaton

```

const int MAXCHAR = 26;
const char CHAR = 'a';

struct Node{
    Node* child[MAXCHAR];
    Node* fail;
    int N;
    Node():N(-1),fail(NULL){for(int i=0;i<MAXCHAR;i++)
        child[i] = NULL;}
};

struct AC{
    Node* root;
    AC(){root = new Node;}
    void word(string s,int index){
        Node* now = root;

```

```

        for(int i=0;i<s.size();i++){
            int c = s[i] - CHAR;
            if(now->child[c] == NULL)now->child[c] =
                new Node;
            now = now->child[c];
        }
        if(now->N == -1)now->N = index;
    }
    void predo(){
        root->fail = NULL;
        Node* p;
        queue<Node*> Q;
        Q.push(root);
        while(!Q.empty()){
            Node* now = Q.front();Q.pop();
            for(int i=0;i<MAXCHAR;i++){
                if(!now->child[i])continue;
                Q.push(now->child[i]);
                p = now->fail;
                while(p != NULL && p->child[i] == NULL)
                    p = p->fail;
                if(p == NULL)now->child[i]->fail = root;
                else now->child[i]->fail = p->child[i];
            }
        }
    }
    void match(string text){
        Node* now = root;
        for(int i=0;i<text.size();i++){
            int c = text[i] - CHAR;
            while(now != root && now->child[c] == NULL)
                now = now->fail;
            if(now->child[c])now = now->child[c];
            if(now->N != -1)cout << "Got you" << endl;
        }
    }
    void release(Node* now = root){
        for(int i=0;i<MAXCHAR;i++)if(now->child[i])
            release(now->child[i]);
        delete now;
    }
};

```

5.5 Suffix Array

```

int SA[MAXNUM],H[MAXNUM];
void SuffixArray(string text){
    int N = text.size(),A = 128;
    int SA2[MAXNUM],rank[MAXNUM],rank2[MAXNUM],radix[
        MAXNUM];
    for(int i=0;i<A;i++)radix[i] = 0;
    for(int i=0;i<N;i++)radix[rank[i]] = text[i]++;
    for(int i=0;i<A;i++)radix[i] += radix[i-1];
    for(int i=N-1;i>=0;i--)SA[--radix[text[i]]] = i;

    for(int power=1;power<N;power<=<=1){
        for(int i=0;i<A;i++)radix[i] = 0;
        for(int i=0;i<N;i++)radix[rank[i]]++;
        for(int i=0;i<A;i++)radix[i] += radix[i-1];

        int now = 0;
        for(int i=N-power;i<N;i++)SA2[now++] = i;
        for(int i=0;i<N;i++){
            if(SA[i]-power >= 0)SA2[now++] = SA[i]-
                power;
        }

        for(int i=N-1;i>=0;i--)SA[--radix[rank[SA2[i]
            ]]] = SA2[i];

        rank2[SA[0]] = now = 0;
        for (int i=1;i<N;i++){
            if (!(rank[SA[i-1]] == rank[SA[i]] && SA[i
                -1]+power < N && SA[i]+power < N &&
                rank[SA[i-1]+power] == rank[SA[i]+power
                ]))now++;
            rank2[SA[i]] = now;
        }
        swap(rank,rank2);
    }
}

```



```

    if(now == N-1)break;
    A = now+1;
}
for(int i=0;i<N;i++)rank[SA[i]] = i;
for(int i=0,k=0;i<N;i++,k?k--:0){
    if(rank[i] == 0){H[rank[i]] = 0;continue;}
    int j = SA[rank[i]-1];
    while(i+k < N && j+k < N && text[i+k] == text[j+k])k++;
    H[rank[i]] = k;
}
}
}

```

6 Geometry

6.1 Point

```

#include <bits/stdc++.h>
using namespace std;
const double EPS = 1e-6;
int dcmp(double x)
{
    if (fabs(x) < EPS)
        return 0;
    else
        return x < 0 ? -1 : 1;
}
struct Point {
    double x, y;
    Point() { x = 0, y = 0; }
    Point(double _x, double _y)
    {
        x = _x;
        y = _y;
    }
    Point operator+(const Point& b)
    {
        return Point(x + b.x, y + b.y);
    }
    Point operator-(const Point& b) const
    {
        return Point(x - b.x, y - b.y);
    }
    Point operator*(double p)
    {
        return Point(x * p, y * p);
    }
    Point operator/(double p)
    {
        return Point(x / p, y / p);
    }
    double operator^(const Point& b) const
    {
        return x * b.y - y * b.x;
    }
    bool operator<(const Point& b)
    {
        return x < b.x || (x == b.x && y < b.y);
    }
    bool operator==(const Point& b)
    {
        return dcmp(x - b.x) == 0 && dcmp(y - b.y) == 0;
    }
};
typedef Point Vector;
double dot(Vector v1, Vector v2)
{
    return v1.x * v2.x + v1.y * v2.y;
}
double cross(Point& o, Point& a, Point& b) //OA X OB
{
    return (a.x - o.x) * (b.y - o.y) - (a.y - o.y) * (b.x - o.x);
}
double cross(Vector a, Vector b)
{
    return a.x * b.y - a.y * b.x;
}

```

```

}
double length(Vector v)
{
    return sqrt(v.x * v.x + v.y * v.y); //return sqrt(dot(v,v));
}
double length(Point a, Point b)
{
    return length(a - b);
}
double angle(const Vector& a, const Vector& b) { return acos(dot(a, b) / length(a) / length(b)); }
double Triarea(const Point& p1, const Point& p2, const Point& p3)
{
    return fabs(cross(p2 - p1, p3 - p1)) / 2;
}
Vector Rotate(const Vector& a, double rad)
{ //radian 0~2pi //counterclockwise
    return Vector(a.x * cos(rad) - a.y * sin(rad), a.x * sin(rad) + a.y * cos(rad)); //旋轉矩陣
}
Vector Normal(const Vector& a)
{ //向量的單位法線
    double L = length(a);
    return Vector(-a.y / L, a.x / L);
}
struct Line {
    Point p1, p2;
};
typedef Line Segment;
Point GetLineIntersection(Point p, Vector v, Point q, Vector w) //點斜式交點 p+vt1 q+wt2
{
    Vector u = p - q;
    double t = cross(w, u) / cross(v, w); //t1
    return p + v * t; //p+vt1
}
Point GetLineProjection(Point p, Point a, Point b)
{
    Vector v = b - a;
    return a + v * (dot(v, p - a) / dot(v, v));
}
typedef Line Segment;
bool SegmentProperIntersection(Point a1, Point a2, Point b1, Point b2)
{
    int c1 = cross(b1 - a1, b2 - a1), c2 = cross(b1 - a2, b2 - a2);
    int c3 = cross(a1 - b1, a2 - b1), c4 = cross(a1 - b2, a2 - b2);
    return dcmp(c1) * dcmp(c2) < 0 && dcmp(c3) * dcmp(c4) < 0;
}
bool SegmentProperIntersection(Segment s1, Segment s2)
{
    return SegmentProperIntersection(s1.p1, s1.p2, s2.p1, s2.p2);
}
bool Onsegment(Point p, Point a1, Point a2)
{
    return dcmp(cross(p - a2, a1 - a2)) == 0 && dcmp(dot(a1 - p, a2 - p)) <= 0;
}
bool SegmentIntersection(Point a1, Point a2, Point b1, Point b2)
{
    if (cross(a2 - a1, b2 - b1) == 0)
        return false;
    if (Onsegment(a1, b1, b2) || Onsegment(a2, b1, b2) || Onsegment(b1, a1, a2) || Onsegment(b2, a1, a2))
        return true;
    if (SegmentProperIntersection(a1, a2, b1, b2))
        return true;
    return false;
}
bool SegmentIntersection(Line& l1, Line& l2)
{
    return SegmentIntersection(l1.p1, l1.p2, l2.p1, l2.p2);
}

```

```

}
double distance(Point& a, Point& b)
{
    return sqrt(length(b - a));
}
double distance(Point& p, Line &L) //Line => p1,p2
{
    Vector v1 = p - L.p1, v2 = L.p2 - L.p1;
    return fabs(cross(v1, v2)) / length(v2); //面積/底=
        高(距離)
}
double distance(Point& p, Segment& s) //Point to
    Segment
{
    Vector v = s.p2 - s.p1;
    if (dcmp(length(v)) == 0)
        return length(p - s.p1); //線段退化成點
    Vector v1 = p - s.p1;
    Vector v2 = p - s.p2;
    if (dcmp(dot(v1, v)) < 0)
        return length(v1); //點投影不在線上
    if (dcmp(dot(v2, v)) > 0)
        return length(v2); //點投影不在線上
    return fabs(cross(v, v1)) / length(v);
}
double distance(Segment& s1, Segment& s2) //線段到線段
{
    if (SegmentIntersection(s1, s2))
        return 0;
    double d = 1e9;
    d = min(d, distance(s1.p1, s2)); //點到線段距離取最
        短
    d = min(d, distance(s1.p2, s2));
    d = min(d, distance(s2.p1, s1));
    d = min(d, distance(s2.p2, s1));
    return d;
}
double ldistance(Line& l1, Line& l2) //線段到線段距離
{
    Vector v1 = l1.p2 - l1.p1;
    Vector v2 = l2.p2 - l2.p1;
    if (cross(v1, v2) != 0)
        return 0;
    return distance(l1.p1, l2); //點到線段距離
}
void ConvexHull(vector<Point>& P, vector<Point>& res)
{
    sort(P.begin(), P.end());
    int cnt = P.size();
    res.resize(cnt+1);
    int m = 0;
    for (int i = 0; i < cnt; i++) {
        while (m > 1 && cross(res[m - 1] - res[m - 2],
            P[i] - res[m - 2]) <= 0)
            m--;
        res.at(m) = P[i];
        m++;
    }
    int k = m;
    for (int i = cnt - 2; i >= 0; i--) {
        while (m > k && cross(res[m - 1] - res[m - 2],
            P[i] - res[m - 2]) <= 0)
            m--;
        res.at(m) = P[i];
        m++;
    }
    if (cnt > 1)
        m--;
    res.resize(m);
}
double ConvexHullWidth(vector<Point>& p)
{
    double ans = 1e18;
    int num = p.size();
    for (int i = 0, j = 0; i < num; i++) {
        Line s;
        s.p1 = p[i];
        s.p2 = p[(i + 1) % num];
        while (distance(p[(j + 1) % num], s) >=
            distance(p[j], s))
            j = (j + 1) % num;
        ans = min(ans, distance(p[j], s));
    }
}

```

```

}
return ans;
}
double PolygonArea(Point* p, int n)
{
    double area = 0;
    for (int i = 0; i < n; ++i)
        area += cross(p[i], p[(i + 1) % n]);
    return fabs(area) / 2;
}
//半平面交
typedef vector<Point> Polygon;
Polygon halfplane_intersection(Polygon& p, Line& line)
{
    Polygon q;
    Point p1 = line.p1, p2 = line.p2;
    int n = p.size();
    for (int i = 0; i < n; i++) {
        double c = cross(p1, p2, p[i]);
        double d = cross(p1, p2, p[(i + 1) % n]);
        if (dcmp(c) >= 0)
            q.push_back(p[i]);
        if (dcmp(c * d) < 0)
            q.push_back(GetLineIntersection(p1, p2, p[i],
                p[(i + 1) % n]));
    }
    return q;
}

```

6.2 Convexhull

```

void ConvexHull(vector<Point>& P, vector<Point>& res)
{
    sort(P.begin(), P.end());
    int cnt = P.size();
    res.resize(cnt+1);
    int m = 0;
    for (int i = 0; i < cnt; i++) {
        while (m > 1 && cross(res[m - 1] - res[m - 2],
            P[i] - res[m - 2]) <= 0)
            m--;
        res.at(m) = P[i];
        m++;
    }
    int k = m;
    for (int i = cnt - 2; i >= 0; i--) {
        while (m > k && cross(res[m - 1] - res[m - 2],
            P[i] - res[m - 2]) <= 0)
            m--;
        res.at(m) = P[i];
        m++;
    }
    if (cnt > 1)
        m--;
    res.resize(m);
}
double ConvexHullWidth(vector<Point>& p)
{
    double ans = 1e18;
    int num = p.size();
    for (int i = 0, j = 0; i < num; i++) {
        Line s;
        s.p1 = p[i];
        s.p2 = p[(i + 1) % num];
        while (distance(p[(j + 1) % num], s) >=
            distance(p[j], s))
            j = (j + 1) % num;
        ans = min(ans, distance(p[j], s));
    }
    return ans;
}
#define next(i) (((i) + 1) % N)
double diameter(vector<Point>& v)
{
    const int N = v.size();
    if (N == 1)
        return 0;
}

```

```

double maxd = 0;
Point a, b;
for (int i = 0, j = 1; i < N; i++) {
    while (dcmp(cross(v[next(i)] - v[i], v[j] - v[i]
        ]) - cross(v[next(i)] - v[i], v[next(j)] -
        v[i])) < 0) {
        j = next(j);
    }
    double d = length(v[i], v[j]);
    if (d > maxd) {
        maxd = d;
        a = v[i];
        b = v[j];
    }
    d = length(v[next(i)], v[next(j)]);
    if (d > maxd) {
        maxd = d;
        a = v[next(i)];
        b = v[next(j)];
    }
}
// a, b is the point pair form the diameter
return maxd;
}

```

6.3 rotating-caliper

```

#include "Point.cpp"
void rotating_caliper(vector<Point> P)
{
    sort(P.begin(), P.end());
    int l = 0, u = 0;
    Point L[10000], U[10000];
    int cnt = P.size();
    for (int i = 0; i < cnt; i++) {
        while (l >= 2 && cross(L[l - 2] - L[l - 1], L[l
            - 1] - P[i]) <= 0)
            l--;
        while (u >= 2 && cross(U[u - 2] - U[u - 1], U[u
            - 1] - P[i]) >= 0)
            u--;
        L[l++] = P[i];
        U[u++] = P[i];
    }
    if (u >= 2) L[l] = U[u - 2];
    for (int i = 0, j = u - 1; i < l && j > 0; i++) {
        //compute L[i] and U[j];
        if (cross(L[i + 1] - L[i], U[j - 1] - U[j]) <= 0) i++;
        else j--;
    }
}

```

6.4 closet-pair

```

#include "Point.cpp"
bool cmpy(const Point& i, const Point& j) { return i.y
    < j.y; }
vector<Point> p;
double DnC(int L, int R, vector<Point>& p) // 區間
{
    if (L >= R)
        return 1e-9;
    if (L + 1 == R) {
        return length(p[L], p[R]);
    }
    int M = (L + R) >> 1;
    double d = min(DnC(L, M, p), DnC(M + 1, R, p));
    if (dcmp(d) == 0)
        return 0;
    int N = 0;
    Point t[10000];
    for (int i = M; i >= L && p[M].x - p[i].x < d; --i)
    {
        t[N++] = p[i];
    }
    for (int i = M + 1; i <= R && p[i].x - p[M].x < d;
        ++i) {

```

```

        t[N++] = p[i];
    }
    sort(t, t + N, cmpy);
    for (int i = 0; i < N; i++) {
        for (int j = 1; j <= 3; j++) {
            d = min(d, length(t[i], t[i + j]));
        }
    }
    return d;
}
double closet_pair(vector<Point>& p)
{
    sort(p.begin(), p.end());
    return DnC(0, p.size(), p);
}

```

6.5 Minimum-Cover-Circle

```

const double eps = 1e-7;
struct Point{
    double x, y;
    Point(){}
    Point(double x, double y):x(x), y(y){}
};
Point Circumcenter(Point a, Point b, Point c){
    double a1 = b.x - a.x, b1 = b.y - a.y, c1 = (a1*a1
        + b1*b1)/2;
    double a2 = c.x - a.x, b2 = c.y - a.y, c2 = (a2*a2
        + b2*b2)/2;
    double d = a1 * b2 - a2 * b1;
    return Point(a.x + (c1*b2 - c2*b1)/d, a.y + (a1*c2 -
        a2*c1)/d);
}
double Distance(Point A, Point B){
    return sqrt((A.x-B.x)*(A.x-B.x)+(A.y-B.y)*(A.y-B.y)
        );
}
// Expected Complexity : O(N)
pair<Point, double> MinimumCoverCircle(vector<Point> P){
    random_shuffle(P.begin(), P.end());
    Point center = P[0];
    double R = 0.0;
    for (int i = 1; i < P.size(); i++) if (Distance(center, P[i]
        ]) + eps > R) {
        center = P[i]; R = 0.0;
    }
    for (int j = 0; j < i; j++) if (Distance(center, P[j]) + eps >
        R) {
        center.x = (P[i].x + P[j].x) / 2.0;
        center.y = (P[i].y + P[j].y) / 2.0;
        R = Distance(center, P[j]);
        for (int k = 0; k < j; k++) if (Distance(center, P[k]) + eps
            > R) {
            center = Circumcenter(P[i], P[j], P[k]);
            R = Distance(center, P[k]);
        }
    }
    return make_pair(center, R);
}

```

6.6 Max-Triangle

```

#include "Point.cpp"
double max_triangle(vector<Point>& points){
    vector<Point> p = ConvexHull(points); // 最大三角形
    // 點一定在凸包上
    int n = p.size();
    p.push_back(p[0]);
    double ans = 0;
    for (int i = 0; i < n; ++i)
    {
        int j = (i + 1) % n;
        int k = (j + 1) % n;

```

```

//當Area(P[i], p[j], p[k+1]) <= Area(p[i], p[j], p[k]) 時停止旋轉
//即Cross(p[j]-p[i], p[k+1]-p[i]) - Cross(p[j]-p[i], p[k]-p[i]) <= 0
//根據Cross(A,B) - Cross(A,C) = Cross(A,B-C)
//化簡得Cross(p[j]-p[i], p[k+1] - p[k]) <= 0
while(k!=i && Cross(p[j]-p[i], p[k+1]-p[k]) > 0)
    k = (k+1) % n;
if(k==i) continue;
int kk = (k+1) % n;
while(j!=kk && k!=i)
{
    ans = max(ans, Cross(p[j]-p[i], p[k]-p[i]));
    while(k!=i && Cross(p[j]-p[i], p[k+1]-p[k]) > 0)
        k = (k+1) % n;
    j = (j+1) % n;
}
return ans*0.5;
}
}

```

6.7 Halfplane

```

//半平面交
typedef vector<Point> Polygon;
Polygon halfplane_intersection(Polygon& p, Line& line)
{
    Polygon q;
    Point p1 = line.p1, p2 = line.p2;
    int n = p.size();
    for (int i = 0; i < n; i++) {
        double c = cross(p1, p2, p[i]);
        double d = cross(p1, p2, p[(i + 1) % n]);
        if (dcmp(c) >= 0)
            q.push_back(p[i]);
        if (dcmp(c * d) < 0)
            q.push_back(GetLineIntersection(p1, p2, p[i], p[(i + 1) % n]));
    }
    return q;
}

```

7 Sort

7.1 Heap Sort

```

void heap_sort(int* arr, int len)
{
    heapify(arr, len/2-1, len);
    max_heap(arr, len);
}
void heapify(int* ptr, int now, int last)
{
    if(now >= last/2 || now < 0) return;
    sub_heapify(ptr, now, last);
    heapify(ptr, now-1, last);
}
void sub_heapify(int* ptr, int now, int last)
{
    if(now*2+2 < last && !(ptr[now] >= ptr[now*2+1] && ptr[now] >= ptr[now*2+2])) {
        int max = (ptr[now*2+1] > ptr[now*2+2]) ? now*2+1 : now*2+2;
        swap(ptr, now, max, 1);
        if(max < last/2) sub_heapify(ptr, max, last);
    }
    else if(now*2+1 < last && ptr[now] < ptr[now*2+1]){
        swap(ptr, now, now*2+1, 1);
        if(now*2+1 < last/2)sub_heapify(ptr, now*2+1, last);
    }
}
void max_heap(int* ptr, int len)

```

```

{
    if(len <= 1) return;
    swap(ptr, 0, len-1, 2);
    sub_heapify(ptr, 0, len-1);
    max_heap(ptr, len-1);
}

```

7.2 Merge Sort

```

void Merge(int* N,int L,int M){
    int tmp[L],p=0; int a,b;
    for(a=0,b=M;a<M && b<L;){
        if(N[a] < N[b]){ tmp[p++]=N[a]; a++; }
        else{ tmp[p++]=N[b]; b++;}
    }
    if(a == M)for(int i=b;i<L;i++)tmp[p++]=N[i];
    else for(int i=a;i<M;i++)tmp[p++]=N[i];
    for(int i=0;i<L;i++)N[i]=tmp[i];
}
void MergeSort(int* N,int L){
    int M=L/2;
    if(L == 1)return;
    MergeSort(N,M);
    MergeSort(N+M,L-M);
    Merge(N,L,M);
}

```

7.3 Radix Sort

```

int maxbit(int data[], int n) //輔助函数，求數據的最大位數
{
    int maxData = data[0]; //最大數
    //先求出最大數，再求其位數，这样有原先依次每个數判斷其位數，稍微優化點。
    for (int i = 1; i < n; ++i) {
        if (maxData < data[i]) maxData = data[i];
    }
    int d = 1; int p = 10;
    while (maxData >= p){
        p *= 10;
        ++d;
    }
    return d;
}
/* int d = 1; //保存最大的位數
int p = 10;
for(int i = 0; i < n; ++i){
    while(data[i] >= p){
        p *= 10;
        ++d;
    }
}
return d;*/
}
void radixsort(int data[], int n) //基數排序
{
    int d = maxbit(data, n);
    int *tmp = new int[n];
    int *count = new int[10]; //計數器
    int i, j, k;
    int radix = 1;
    for(i = 1; i <= d; i++) { //進行d次排序
        for(j = 0; j < 10; j++) count[j] = 0; //每次分配前清空計數器
        for(j = 0; j < n; j++){
            k = (data[j] / radix) % 10; //統計每個桶中的記錄數
            count[k]++;
        }
        for(j = 1; j < 10; j++) count[j] = count[j] + count[j-1]; //將tmp中的位置依次分配每個桶
        for(j = n-1; j >= 0; j--) { //將所有桶中記錄依次收集到tmp中
            k = (data[j] / radix) % 10;
            tmp[count[k]-1] = data[j];
            count[k]--;
        }
    }
}

```

```

    for(j = 0; j < n; j++) //將臨時數組的內容複製到
        data中
        data[j] = tmp[j];
    radix = radix * 10;
}
delete []tmp;
delete []count;
}

```

7.4 Shell Sort

```

void shell_sort(int* ptr, int len)
{
    int gap = len / 2;
    while(gap){
        for(int i = gap; i < len; ++i, gap /= 2) {
            for(int j = i; j >= gap; j-=gap){
                if(ptr[j] > ptr[j-gap]) swap(ptr, j, j-
                    gap, gap);
                else break;
            }
        }
    }
}

```

8 Math

8.1 LIS

```

#include <bits/stdc++.h>
using namespace std;
template <typename E>
struct Node {
    E value;
    E* pointer;
};

template <class E>
struct node_ptr_less {
    bool operator()(E* & node1,
        E* & node2) const
    {
        return node1->value < node2->value;
    }
};

template <typename E>
std::vector<E> lis(const std::vector<E> & n)
{
    typedef E* NodePtr;

    std::vector<NodePtr> pileTops;
    // sort into piles
    for (typename std::vector<E>::const_iterator it = n
        .begin(); it != n.end(); it++) {
        NodePtr node(new Node<E>());
        node->value = *it;
        typename std::vector<NodePtr>::iterator j = std
            ::lower_bound(pileTops.begin(), pileTops.
                end(), node, node_ptr_less<E>());
        if (j != pileTops.begin())
            node->pointer = *(j - 1);
        if (j != pileTops.end())
            *j = node;
        else
            pileTops.push_back(node);
    }
    // extract LIS from piles
    std::vector<E> result;
    for (NodePtr node = pileTops.back(); node !=
        nullptr; node = node->pointer)
        result.push_back(node->value);
    std::reverse(result.begin(), result.end());
    return result;
}

int LIS(vector<int> & v)
{
}

```

```

vector<int> ans;
for (auto& i : v) {
    auto it = lower_bound(ans.begin(), ans.end(), i
        );
    if (ans.size() == 0 || i >= ans.back())
        ans.push_back(i);
    else {
        *it = i;
    }
}
return ans.size();
}

```

8.2 Extended Euclidean

```

int ExGCD(int A, int B, int& X, int& Y, int s0 = 1, int s1 =
    0, int t0 = 0, int t1 = 1){
    if(A%B == 0){
        X = s1;
        Y = t1;
        return B;
    }
    s0 -= s1*(A/B);
    t0 -= t1*(A/B);
    return ExGCD(B, A%B, X, Y, s1, s0, t1, t0);
}

```

8.3 Prime

```

// Complexity : O(NlogN)
void BuildPrime(bool prime[], int N){
    for(int i=2; i<N; i++) prime[i] = true;
    for(int i=2; i<N; i++){
        if(prime[i]) for(int j=i*i; j<N; j+=i) prime[j] =
            false;
    }
}

// Complexity : O(N)
void BuildPrime(vector<int> primelist, bool prime[], int
    N){
    for(int m=2; m<N; m++){
        if(prime[m] == true) primelist.push_back(m);
        for(auto i:primelist){
            if(m*i >= N) break;
            prime[m*i] = false;
            if(m%i == 0) break;
        }
    }
}

void ExBuildPrime(int first[], bool prime[], int N){
    for(int i=2; i<N; i++){
        prime[i] = true;
        first[i] = 1;
    }
    for(int i=2; i<N; i++){
        if(prime[i]) for(int j=i*i; j<N; j+=i){
            prime[j] = false;
            if(first[j] == 1) first[j] = i;
        }
    }
}

```

8.4 Factor Decomposition

```

vector<pair<int, int>> FactorDecomposition(int x){
    vector<pair<int, int>> ans;
    while(x > 1){
        int p, e = 0;
        if(prime[x] == true) p = x; else p = first[x];
        while(x%p == 0){x/=p; e++;}
        ans.push_back(make_pair(p, e));
    }
    return ans;
}

```

8.5 Module Inverse

```
int inverse(int A,int M,int X = 1,int Y = 0){
    if(A%M == 0){
        if(Y < 0)Y+=M;
        return Y;
    }
    X-=Y*(A/M);
    return inverse(M,A%M,Y,X);
}

inline int inverse(int A,int M){
    return ExPower(A,M-2,M);
}
```

8.6 Phi

```
int Phi(int x){
    vector<pair<int,int>> FD = FactorDecomposition(x);
    int ans = 1;
    for(auto i:FD){
        ans *= i.first-1;
        ans *= Power(i.first,i.second-1);
    }
    return ans;
}

void BuildPhi(int phi[],int N){
    for(int i=1;i<=N;i++) phi[i] = i;
    for(int i=1;i<=N;i++) for(x=i*2;x<=N;x+=i) phi[x]
        -= phi[i];
}

void BuildPhi(int phi[],int N){
    bool prime[N+1];for(int i=2;i<=N;i++) prime[i] =
        true;
    vector<int> primelist;
    phi[1] = 1;
    for(int m=2;m<=N;m++){
        if(prime[m] == true){
            phi[m] = m-1;
            primelist.push_back(m);
        }
        for(auto i:primelist){
            if(m*i > N) break;
            prime[m*i] = false;
            if(m%i == 0){
                int now = m,power = 1;
                while(now%i == 0){ now /= i;power *= i;
                }
                phi[m*i] = phi[now]*power*(i-1);
                break;
            }
            else phi[m*i] = phi[m]*(i-1);
        }
    }
}
```

8.7 Miller Rabin

```
int ExMultiply(int a,int b,int n){
    a %= n;b %= n;
    int r = 0;
    while(b){
        if(b&1)r = ((a+r >= n)? a+r-n : a+r);
        a = ((a+a >= n)? a+a-n : a+a);
        b >>= 1;
    }
    return r;
}

int ExExPower(int a,int d,int n){
    if(d == 0)return 1;
    int k = ExExPower(a,d/2,n);
    if(d%2)return ExMultiply(ExMultiply(k,k,n),a,n);
    return ExMultiply(k,k,n);
}
```

```
}

bool MillerRabin(int n,int a){
    if(__gcd(n,a) == n)return true;
    if(__gcd(n,a) != 1)return false;
    // a^(d*2^r)
    int d = n-1, r = 0;
    while(d%2 == 0){ d /= 2;r++; }
    // a^d = ? (mod n)
    int remain = ExExPower(a,d,n);
    if(remain == 1 || remain == n-1)return true;
    while(r--){
        remain = ExMultiply(remain,remain,n);
        if(remain == n-1)return true;
    }
    return false;
}

bool IsPrime(int n){
    int a[7] =
        {2,325,9375,28178,450775,9780504,1795265022};
    for(int i=0;i<7;i++)if(!MillerRabin(n,a[i]))return
        false;
    return true;
}
```

8.8 Pollard-Rho

```
#include <bits/stdc++.h>
using namespace std;
//don't use __gcd for negative number
int gcd(int a, int b)
{
    if (a < 0)
        return gcd(-a, b);
    return b ? gcd(b, a % b) : a;
}
//super fast
int ExMultiply(int a, int b, int n)
{
    if (a == 0)
        return 0;
    return ((a & 1) * b % n + (ExMultiply(a >> 1, b, n)
        << 1) % n) % n;
}

int FastPow(int a, int b, int n)
{
    a %= n;
    int ans = 1;
    int d = a;
    while (b) {
        if (b & 1)
            ans = ExMultiply(ans, d, n);
        d = ExMultiply(d, d, n);
        b >>= 1;
    }
    return ans;
}

bool MillerRabin(int n, int a)
{
    if (n == a)
        return true;
    //even
    if (gcd(n, a) == n)
        return true;
    if (gcd(n, a) != 1)
        return false;
    // a^(d*2^r)
    int d = n - 1, r = 0;
    while (!(d & 1)) {
        d >>= 1;
        r++;
    }
    // a^d = ? (mod n)
    int remain = FastPow(a, d, n);
    if (remain == 1 || remain == n - 1)
        return true;
    while (r--){
        remain = ExMultiply(remain, remain, n);
    }
}
```



```

        if (remain == n - 1)
            return true;
    }
    return false;
}
bool IsPrime(int n)
{
    if (n == 2)
        return true;
    if (!(n & 1))
        return false;
    int a[7] = { 2, 325, 9375, 28178, 450775, 9780504,
        1795265022 };
    for (int i = 0; i < 7; i++) {
        if (!MillerRabin(n, a[i]))
            return false;
    }
    return true;
}
int PollardRho(int n, int c)
{
    int x = rand() % n, y = x, k = 2;
    for (int i = 2;; i++) {
        x = (ExMultiply(x, x, n) + c) % n;
        int d = gcd(x - y, n);
        if (d != 1 && d != n)
            return d;
        if (y == x)
            return n;
        if (i == k) {
            y = x;
            k <<= 1;
        }
    }
}
vector<int> Fac;
void fac(int n)
{
    if (IsPrime(n)) {
        Fac.push_back(n);
        return;
    }
    int p = n;
    while (p >= n)
        p = PollardRho(p, rand() % (n - 1) + 1);
    fac(p);
    fac(n / p);
}

```

8.9 Chinese-Remainder-Theorem

```

#include <bits/stdc++.h>
using namespace std;
int inverse(int A, int M)
{
    return A == 1 ? 1 : inverse(M % A, M) * (M - M / A)
        % M;
}
/*
 * chinese remainder theorem
 * check all m[i] are pairwise coprime
 * if x = a1(mod p) and x=a2(mod p) if a1!=a2
 * then no solution
 * return first positive answer
 * next answer is answer+M
 */
int CRT(vector<int> a, vector<int> m)
{
    if (a.size() != m.size())
        return -1;
    int M = 1;
    for (int i = 0; i < m.size(); i++) {
        M *= m[i];
    }
    int res = 0;
    for (int i = 0; i < a.size(); i++) {
        res = (res + a[i] * (M / m[i]) * inverse(M / m[i], m[i])) % M;
    }
}

```

```

return (res+M)%M;
}

```

8.10 Lucas-Theorem

```

#include <bits/stdc++.h>
using namespace std;
const int p = 5; //prime<10^5
int fac[p + 1];
void build_fac(int p)
{
    fac[0] = 1;
    for (int i = 1; i <= p; i++)
        fac[i] = fac[i - 1] * i % p;
}
//mod inverse
int inv(int a, int p)
{
}
//called after build_fac
int Lucas(int n, int m, int p)
{
    if (m == 0)
        return 1;
    if (m > n)
        return 0;
    if (n < m)
        return fac[n] * inv(fac[m] * fac[n - m] % p, p)
            % p;
    else
        return Lucas(n / p, m / p, p) * Lucas(n % p, m
            % p, p) % p;
}

```

8.11 FFT

```

const int MAXN = 262144;
const double PI = acos(-1.0);
const complex<double> I(0, 1);
complex<double> omega[MAXN+1];

void pre_FFT(){
    for(int i=0; i<=MAXN; i++)omega[i] = exp(i * 2 * PI
        / MAXN * I);
}

void FFT(int n, complex<double> a[], bool inv=false){
    int basic = MAXN / n;
    int theta = basic;
    for(int m = n; m >= 2; m >>= 1) {
        int mh = m >> 1;
        for(int i = 0; i < mh; i++) {
            complex<double> w = omega[inv ? MAXN-(i*
                theta%MAXN) : i*theta%MAXN];
            for(int j = i; j < n; j += m) {
                int k = j + mh;
                complex<double> x = a[j] - a[k];
                a[j] += a[k];
                a[k] = w * x;
            }
        }
        theta = (theta * 2) % MAXN;
    }
    int i = 0;
    for(int j = 1; j < n - 1; j++) {
        for(int k = n >> 1; k > (i ^= k); k >>= 1);
        if(j < i) swap(a[i], a[j]);
    }
    if(inv)for(i = 0; i < n; i++)a[i] /= n;
}

```

8.12 Fraction


```

struct fraction_positive{
    int p,q;
    fraction_positive(){
    fraction_positive(int p,int q):p(p),q(q){}
    void reduction(){
        int G = __gcd(p,q);
        p /= G;
        q /= G;
    }
    bool operator==(const fraction_positive& B) const {
        return (p == B.p && q == B.q);
    }
    bool operator!=(const fraction_positive& B) const {
        return (p != B.p || q != B.q);
    }
    bool operator>(const fraction_positive& B) const {
        return (p*B.q > B.p*q);
    }
    bool operator>=(const fraction_positive& B) const {
        return (p*B.q >= B.p*q);
    }
    bool operator<(const fraction_positive& B) const {
        return (p*B.q < B.p*q);
    }
    bool operator<=(const fraction_positive& B) const {
        return (p*B.q <= B.p*q);
    }
    fraction_positive operator+(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.q+B.p*q;
        F.q = q*B.q;
        F.reduction();
        return F;
    }
    fraction_positive operator-(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.q-B.p*q;
        F.q = q*B.q;
        F.reduction();
        return F;
    }
    fraction_positive operator*(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.p;
        F.q = q*B.q;
        F.reduction();
        return F;
    }
    fraction_positive operator/(const fraction_positive
        & B) const {
        fraction_positive F;
        F.p = p*B.q;
        F.q = q*B.p;
        F.reduction();
        return F;
    }
    fraction_positive operator*(int x) const {
        fraction_positive F = *this;
        F.p *= x;
        F.reduction();
        return F;
    }
    fraction_positive operator/(int x) const {
        fraction_positive F = *this;
        F.q *= x;
        F.reduction();
        return F;
    }
};

struct fraction{
    fraction_positive N;
    bool sign,broken; //0 positive 1 negative
    fraction():broken(false){}
    fraction(int p,int q,bool sign):sign(sign){
        if(q == 0){broken = true;cout << "====divide by
            zero====" << endl;}
        else{N.p = p;N.q = q;N.reduction();}
    }
};

```

```

bool operator==(const fraction& B) const {
    return (N == B.N && sign == B.sign);
}
bool operator!=(const fraction& B) const {
    return (N != B.N || sign != B.sign);
}
bool operator>(const fraction& B) const {
    return (!sign && B.sign) || (!sign && N > B.N)
        || (sign && N < B.N);
}
bool operator>=(const fraction& B) const {
    return (!sign && B.sign) || (!sign && N >= B.N)
        || (sign && N <= B.N);
}
bool operator<(const fraction& B) const {
    return !(*this >= B);
}
bool operator<=(const fraction& B) const {
    return !(*this > B);
}
fraction operator+(const fraction& B) const {
    fraction F;
    if(broken || B.broken){F.broken = true;return F;
    }
    if(sign^B.sign){
        const fraction_positive& big = (N > B.N ? N
            : B.N);
        const fraction_positive& small = (N <= B.N
            ? N : B.N);
        F.N = big - small;
        F.sign = (N > B.N ? sign : B.sign);
    }
    else{
        F.N = N+B.N;
        F.sign = sign;
    }
    return F;
}
fraction operator-(const fraction& B) const {
    fraction F = B;
    if(broken || B.broken){F.broken = true;return F;
    }
    F.sign = !F.sign;
    return (*this+F);
}
fraction operator*(const fraction& B) const {
    fraction F;
    if(broken || B.broken){F.broken = true;return F;
    }
    F.N = N*B.N;
    F.sign = sign^B.sign;
    return F;
}
fraction operator/(const fraction& B) const {
    fraction F;
    if(broken || B.broken || B.N.p == 0){F.broken =
        true;return F;}
    F.N = N/B.N;
    F.sign = sign^B.sign;
    return F;
}
fraction operator*(int x) const {
    fraction F = *this;
    if(broken){F.broken = true;return F;}
    F.N = F.N*abs(x);
    if(x < 0)F.sign = !F.sign;
    return F;
}
fraction operator/(int x) const {
    fraction F = *this;
    if(x == 0){F.broken = true;return F;}
    F.N = F.N/abs(x);
    if(x < 0)F.sign = !F.sign;
    return F;
}
friend istream& operator>>(istream& in,fraction& B)
{
    int x;
    char c;
    B.sign = false;
    in >> x;if(x < 0){B.sign = true;x = -x;}
    B.N.p = x;
};

```

```

    in >> c >> x; if(x == 0){B.broken = true; return
        in;}
    B.N.q = x;
    B.N.reduction();
    return in;
}
friend ostream& operator<<(ostream& out, const
    fraction& B){
    if(B.broken){return out << "NaN";}
    if(B.sign)out << '-';
    return out << B.N.p << '/' << B.N.q;
}
};

```

8.13 Matrix

```

#include <bits/stdc++.h>
using namespace std;
const double EPS = 1e-9;

template <typename T>
class Matrix {
public:
    Matrix()
        : wrong(false)
    {
    }
    Matrix(int _rows, int _cols)
        : wrong(false)
    {
        rows = _rows;
        cols = _cols;
        data.resize(_rows);
        for (int i = 0; i < _rows; i++)
            data[i].resize(_cols);
    }
    Matrix(T** _data, int _rows, int _cols)
        : wrong(false)
    {
        rows = _rows;
        cols = _cols;
        data.resize(_rows);
        for (int i = 0; i < _rows; i++)
            data[i].resize(_cols);
        for (int i = 0; i < _rows; i++)
            for (int j = 0; j < _cols; j++)
                data[i][j] = _data[i][j];
    }
    Matrix(const Matrix& N)
    {
        wrong = N.wrong;
        rows = N.rows;
        cols = N.cols;
        data.resize(rows);
        for (int i = 0; i < rows; i++)
            data[i].resize(cols);
        for (int i = 0; i < rows; i++)
            for (int j = 0; j < cols; j++)
                data[i][j] = N.data[i][j];
    }
    T& at(int a, int b)
    {
        return data[a][b];
    }
    Matrix operator+(const Matrix& N)
    {
        cout << (*this) << endl
            << N << endl;
        Matrix tmp = Matrix(*this);
        if (rows != N.rows || cols != N.cols)
            tmp.wrong = true;
        else
            for (int i = 0; i < rows; i++)
                for (int j = 0; j < cols; j++)
                    tmp.data[i][j] += N.data[i][j];
        return tmp;
    }
    Matrix operator-(const Matrix& N)
    {
        Matrix tmp = Matrix(*this);

```

```

        if (rows != N.rows || cols != N.cols)
            tmp.wrong = true;
        else
            for (int i = 0; i < rows; i++)
                for (int j = 0; j < cols; j++)
                    tmp.data[i][j] -= N.data[i][j];
        return tmp;
    }
    Matrix operator*(const Matrix& N)
    {
        Matrix tmp = Matrix(rows, N.cols);
        if (cols != N.rows)
            tmp.wrong = true;
        else
            for (int i = 0; i < tmp.rows; i++)
                for (int j = 0; j < tmp.cols; j++) {
                    tmp.data[i][j] = 0;
                    for (int k = 0; k < cols; k++)
                        tmp.data[i][j] += data[i][k] *
                            N.data[k][j];
                }
        return tmp;
    }
    Matrix operator*(int c)
    {
        Matrix tmp = Matrix(*this);
        for (int i = 0; i < rows; i++)
            for (int j = 0; j < cols; j++)
                tmp.data[i][j] *= c;
        return tmp;
    }
    Matrix operator=(const Matrix& N)
    {
        wrong = N.wrong;
        rows = N.rows;
        cols = N.cols;
        data = new T*[rows];
        for (int i = 0; i < rows; i++)
            data[i] = new T[cols];
        for (int i = 0; i < rows; i++)
            for (int j = 0; j < cols; j++)
                data[i][j] = N.data[i][j];
        return (*this);
    }
    Matrix transpose(void)
    {
        Matrix tmp = Matrix(*this);
        //int fuck = tmp.rows; tmp.rows = tmp.cols; tmp.
        cols = fuck;
        swap(tmp.rows, tmp.cols);
        tmp.data = new T*[tmp.rows];
        for (int i = 0; i < tmp.rows; i++)
            tmp.data[i] = new T[tmp.cols];
        for (int i = 0; i < rows; i++)
            for (int j = 0; j < cols; j++)
                tmp.data[j][i] = data[i][j];
        return tmp;
    }
    void Identity()
    { // rows==cols
        for (int i = 0; i < rows; i++) {
            at(i, i) = 1;
        }
    }
    Matrix pow(int rhs) const
    {
        if (rows != cols)
            return Matrix();
        Matrix res(rows, rows), p(*this);
        res.Identity();
        while (rhs) {
            if (rhs & 1)
                res = res * p;
            p = p * p;
            rhs >>= 1;
        }
        return res;
    }
    T det()
    {
        int ans = 1;
        for (int i = 0; i < rows; i++) {

```

```

        for (int j = i + 1; j < rows; j++) {
            int a = i, b = j;
            while (at(b, i)) {
                int q = at(a, i) / at(b, i);
                for (int k = 0; k < rows; k++) {
                    at(a, k) = at(a, k) - at(b, k)
                        * q;
                }
                swap(a, b);
            }
            if (a != i) {
                swap(data[i], data[j]);
                ans = -ans;
            }
        }
        if (fabs(at(i, i)) < EPS)
            return 0;
        else
            ans *= at(i, i);
    }
    return ans;
}
// r:non-free number l:l[i] is true if i-th
// variable is non-free
Matrix GuassElimination(int& r, vector<bool>& l,
    int flag = 0)
{
    l = vector<bool>(cols);
    r = 0;
    Matrix res(*this);
    for (int i = 0; i < res.cols - flag; i++) {
        for (int j = r; j < res.rows; j++) {
            if (fabs(res.at(j, i)) > EPS) {
                swap(res.data[r], res.data[j]);
                break;
            }
        }
        if (fabs(res.at(r, i)) < EPS) {
            continue;
        }
        for (int j = 0; j < res.rows; j++) {
            if (j != r && fabs(res.at(j, i)) > EPS)
            {
                double tmp = (double)res.at(j, i) /
                    (double)res.at(r, i);
                for (int k = 0; k < res.cols; k++)
                {
                    res.at(j, k) -= tmp * res.at(r,
                        k);
                }
            }
        }
        r++;
        l[i] = true;
    }
    return res;
}
vector<double> Solve(vector<double> a)
{
    if (rows != cols)
        return vector<double>();
    vector<double> res(rows);
    Matrix t(rows, cols + 1);
    for (int i = 0; i < rows; i++) {
        for (int j = 0; j < cols; j++)
            t.at(i, j) = at(i, j);
        t.at(i, rows) = a[i];
    }
    int r = 0;
    vector<bool> l;
    t = t.GuassElimination(r, l, 1);
    if (r != rows)
        return vector<double>();
    for (int i = 0; i < cols; i++) {
        if (l[i])
            for (int j = 0; j < rows; j++) {
                if (fabs(t.at(j, i)) > EPS)
                    res[i] = t.at(j, cols) / t.at(j
                        , i);
            }
    }
    return res;
}

```

```

}
Matrix Inverse()
{
    if (rows != cols)
        return Matrix();
    Matrix t(rows, rows * 2);
    for (int i = 0; i < rows; i++) {
        for (int j = 0; j < cols; j++)
            t.at(i, j) = at(i, j);
        t.at(i, i + rows) = 1;
    }
    int r = 0;
    vector<bool> l;
    t = t.GuassElimination(r, l, rows);
    if (r != rows)
        return Matrix();
    for (int i = 0; i < cols; i++) {
        if (l[i])
            for (int j = 0; j < rows; j++) {
                if (fabs(t.at(j, i)) > EPS) {
                    for (int k = 0; k < cols; k++)
                        t.at(j, cols + k) /= t.at(j
                            , i);
                }
            }
    }
    Matrix res(rows, cols);
    for (int i = 0; i < rows; i++)
        for (int j = 0; j < cols; j++)
            res.at(i, j) = t.at(i, j + cols);
    return res;
}

vector<vector<T>> data;
int rows, cols;
bool wrong;
};

```