

# NCTU\_Yggdarsill

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## 1 Building Environment

### 1.1 Print

```
1 cat -n "%s" > tmp.print
2 lpr tmp.print
```

### 1.2 Vimrc

```
1 set tabstop=4
2 set autoindent
3
4 map <F9> :w<LF>:!g++ -O2 -std=c++11 -o %.out % && echo "----Start----" &&
  ./%.out<LF>
5 imap <F9> <ESC><F9>
```

## 2 Convolution

### 2.1 FFT

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 const double PI = 3.1415926535897932;
5
6 struct Complex{
7     typedef double T;
8     T x, y;
9     Complex (T _x=0.0, T _y=0.0)
10         :x(_x),y(_y){ }
11     Complex operator + (const Complex &b) { return Complex(x+b.x,y+b.y); }
12     Complex operator - (const Complex &b) { return Complex(x-b.x,y-b.y); }
13     Complex operator * (const Complex &b) { return Complex(x*b.x-y*b.y,x*b.y+y*b.x); }
14 };
15
16 void BitReverse(Complex *a, int n){
17     for (int i=1, j=0; i<n; i++){
18         for (int k = n>>1; k>(j^=k); k>>=1);
19         if (i<j) swap(a[i],a[j]);
20     }
21 }
22
23 void FFT(Complex *a, int n, int rev=1){ // rev = 1 or -1
24     BitReverse(a,n);
25     Complex *A = a;
26
27     for (int s=1; (1<<s)<=n; s++){
28         int m = (1<<s);
29
30         Complex wm( cos(2*PI*rev/m) , sin(2*PI*rev/m) );
31         for (int k=0; k<n; k+=m){
32             Complex w(1,0);
33             for (int j=0; j<(m>>1); j++){
34                 Complex t = w * A[k+j+(m>>1)];
35                 Complex u = A[k+j];
36                 A[k+j] = u+t;
37                 A[k+j+(m>>1)] = u-t;
38                 w = w*wm;
39             }
40         }
41     }
42
43     if (rev== -1){
44         for (int i=0; i<n; i++){
45             A[i].x /= n;
46             A[i].y /= n;
47         }
48     }
49 }
50
51 const int MAXN = 65536;
52 int n;
53 Complex a[MAXN], b[MAXN];
54
55 void input(){

```

```

56     scanf("%d", &n);
57
58     for (int i=0, ai; i<n; i++){
59         scanf("%d", &ai);
60         a[i] = Complex(ai,0);
61     }
62
63     for (int i=0, bi; i<n; i++){
64         scanf("%d", &bi);
65         b[i] = Complex(bi,0);
66     }
67
68     for (int i=n; i<MAXN; i++){
69         a[i] = b[i] = Complex(0,0);
70     }
71 }
72
73 void solve(){
74     FFT(a,MAXN);
75     FFT(b,MAXN);
76
77     for (int i=0; i<MAXN; i++){
78         a[i] = a[i]*b[i];
79     }
80
81     FFT(a,MAXN,-1);
82     for (int i=0; i<2*n-1; i++){
83         printf("%.0f%c", a[i].x, i==2*n-2?'\n':' ');
84     }
85 }
86
87 int main(){
88     int T; scanf("%d",&T);
89
90     while (T--){
91         input();
92         solve();
93     }
94 }

```

## 3 Data Structure

### 3.1 K-D Tree (Insert)

```

1 #ifndef SUNMOON_DYNEMIC_KD_TREE
2 #define SUNMOON_DYNEMIC_KD_TREE
3 #include<algorithm>
4 #include<vector>
5 #include<queue>
6 #include<cmath>
7 template<typename T,size_t kd>//kd表示有幾個維度
8 class kd_tree{

```

```

9 public:
10 struct point{
11     T d[kd];
12     inline T dist(const point &x) const{
13         T ret=0;
14         for(size_t i=0;i<kd;++i) ret+=std::abs(d[i]-x.d[i]);
15         return ret;
16     }
17     inline bool operator<(const point &b) const{
18         return d[0]<b.d[0];
19     }
20 };
21 private:
22 struct node{
23     node *l,*r;
24     point pid;
25     int s;
26     node(const point &p):l(0),r(0),pid(p),s(1){}
27     inline void up(){
28         s=(l?l->s:0)+1+(r?r->s:0);
29     }
30 }*root;
31 const double alpha,loga;
32 const T INF;//記得要給INF，表示極大值
33 std::vector<node*> A;
34 int qM;
35 std::priority_queue<std::pair<T,point > >pQ;
36 struct __cmp{
37     int sort_id;
38     inline bool operator()(const node*x,const node*y) const{
39         return x->pid.d[sort_id]<y->pid.d[sort_id];
40     }
41 }cmp;
42 void clear(node *o){
43     if(!o) return;
44     clear(o->l);
45     clear(o->r);
46     delete o;
47 }
48 inline int size(node *o){
49     return o?o->s:0;
50 }
51 node* build(int k,int l,int r){
52     if(l>r) return 0;
53     if(k==kd) k=0;
54     int mid=(l+r)/2;
55     cmp.sort_id=k;
56     std::nth_element(A.begin()+l,A.begin()+mid,A.begin()+r+1,cmp);
57     node *ret=A[mid];
58     ret->l=build(k+1,l,mid-1);
59     ret->r=build(k+1,mid+1,r);
60     ret->up();
61     return ret;
62 }
63 inline bool isbad(node*o){
64     return size(o->l)>alpha*o->s||size(o->r)>alpha*o->s;

```

```

65 }
66 void flatten(node *u,typename std::vector<node*>::iterator &it){
67     if(!u) return;
68     flatten(u->l,it);
69     *it=u;
70     flatten(u->r,++it);
71 }
72 bool insert(node*&u,int k,const point &x,int dep){
73     if(!u){
74         u=new node(x);
75         return dep<=0;
76     }
77     ++u->s;
78     if(insert(x.d[k]<u->pid.d[k]?u->l:u->r,(k+1)%kd,x,dep-1)){
79         if(!isbad(u)) return 1;
80         if(((int)A.size())<u->s) A.resize(u->s);
81         typename std::vector<node*>::iterator it=A.begin();
82         flatten(u,it);
83         u=build(k,0,u->s-1);
84     }
85     return 0;
86 }
87 inline T heuristic(const T h[]) const{
88     T ret=0;
89     for(size_t i=0;i<kd;++i) ret+=h[i];
90     return ret;
91 }
92 void nearest(node *u,int k,const point &x,T *h,T &mndist){
93     if(u==0||heuristic(h)>=mndist) return;
94     T dist=u->pid.dist(x),old=h[k];
95     /*mndist=std::min(mndist,dist);*/
96     if(dist<mndist){
97         pQ.push(std::make_pair(dist,u->pid));
98         if((int)pQ.size()==qM+1){
99             mndist=pQ.top().first,pQ.pop();
100         }
101     }
102     if(x.d[k]<u->pid.d[k]){
103         nearest(u->l,(k+1)%kd,x,h,mndist);
104         h[k]=std::abs(x.d[k]-u->pid.d[k]);
105         nearest(u->r,(k+1)%kd,x,h,mndist);
106     }else{
107         nearest(u->r,(k+1)%kd,x,h,mndist);
108         h[k]=std::abs(x.d[k]-u->pid.d[k]);
109         nearest(u->l,(k+1)%kd,x,h,mndist);
110     }
111     h[k]=old;
112 }
113 public:
114 kd_tree(const T &INF,double a=0.75):root(0),alpha(a),loga(log2(1.0/a)),
    INF(INF){}
115 inline void clear(){
116     clear(root),root=0;
117 }
118 inline void build(int n,const point *p){
119     clear(root),A.resize(n);

```

```

120     for(int i=0;i<n;++i)A[i]=new node(p[i]);
121     root=build(0,0,n-1);
122 }
123 inline void insert(const point &x){
124     insert(root,0,x,std::__lg(size(root))/loga);
125 }
126 inline T nearest(const point &x,int k){
127     qM=k;
128     T mndist=INF,h[kd]={};
129     nearest(root,0,x,h,mndist);
130     mndist=pQ.top().first;
131     pQ=std::priority_queue<std::pair<T,point >>()>();
132     return mndist; /*回傳離x第k近的點的距離*/
133 }
134 inline int size(){return root?root->s:0;}
135 };
136 #endif

```

```

35     }
36     if (lazy[rt]) push_down(rt, r - 1 + 1);
37     int m = (l + r) >> 1;
38     if (L <= m) update(L, R, delta, lchild);
39     if (R > m) update(L, R, delta, rchild);
40     push_up(rt);
41 }
42
43 #define lchild rt << 1, l, m
44 #define rchild rt << 1 | 1, m + 1, r
45 int query(int L, int R, int rt = 1, int l = 1, int r = N) {
46     if (L <= l && r <= R) return tree[rt];
47     if (lazy[rt]) push_down(rt, r - 1 + 1);
48     int m = (l + r) >> 1, ret = 0;
49     if (L <= m) ret += query(L, R, lchild);
50     if (R > m) ret += query(L, R, rchild);
51     return ret;
52 }

```

### 3.2 Segment Tree (Lazy)

```

1 /* 于求和 */
2 void push_up(int rt) {
3     tree[rt] = tree[rt << 1] + tree[rt << 1 | 1];
4 }
5
6 /* 于求最大值 */
7 void push_up(int rt) {
8     tree[rt] = max(tree[rt << 1], tree[rt << 1 | 1]);
9 }
10
11 void push_down(int rt, int len) {
12     tree[rt << 1] += lazy[rt] * (len - (len >> 1));
13     lazy[rt << 1] += lazy[rt];
14     tree[rt << 1 | 1] += lazy[rt] * (len >> 1);
15     lazy[rt << 1 | 1] += lazy[rt];
16     lazy[rt] = 0;
17 }
18
19 #define lchild rt << 1, l, m
20 #define rchild rt << 1 | 1, m + 1, r
21 void build(int rt = 1, int l = 1, int r = N) {
22     if (l == r) { std::cin >> tree[rt]; return; }
23     int m = (l + r) >> 1;
24     build(lchild); build(rchild);
25     push_up(rt);
26 }
27
28 #define lchild rt << 1, l, m
29 #define rchild rt << 1 | 1, m + 1, r
30 void update(int L, int R, int delta, int rt = 1, int l = 1, int r = N) {
31     if (L <= l && r <= R) {
32         tree[rt] += delta * (r - l + 1);
33         lazy[rt] += delta;
34         return;

```

### 3.3 Treap

```

1 struct Treap{
2     Treap *l,*r;
3     int pri,sz,val,add;
4     Treap(int _val):pri(rand()),sz(1),val(_val),add(0),l(NULL),r(NULL){}
5 };
6
7 int size(Treap *t){
8     return t->sz;
9 }
10 void pull(Treap *t){
11     t->sz=size(t->l)+size(t->r)+1;
12 }
13 void push(Treap *t){
14     t->val+=t->add;
15     if(t->l) t->l->add+=t->add;
16     if(t->r) t->r->add+=t->add;
17     t->add=0;
18 }
19 Treap* merge(Treap *a,Treap *b){
20     if(!a||!b) return a?a:b;
21     if(a->pri > b->pri){
22         push(a);
23         a->r = merge(a->r,b);
24         pull(a);
25         return a;
26     }
27     else{
28         push(b);
29         b->l = merge(a,b->l);
30         pull(b);
31         return b;
32     }
33 }

```

```

34 void split(Treap *t,int k,Treap *&a,Treap *&b){
35     if(!t) a=b=NULL;
36     else{
37         push(t);
38         if(size(t->l) < k){
39             a=t;
40             split(t->r,k-size(t->l)-1,a->r,b);
41             pull(a);
42         }
43         else{
44             b=t;
45             split(t->l,k,a,b->l);
46             pull(b);
47         }
48     }
49 }

```

## 4 Geometry

### 4.1 Geometry

```

1 typedef double Double;
2 struct Point {
3     Double x,y;
4 }
5 bool operator < (const Point &b)const{
6     //return tie(x,y) < tie(b.x,b.y);
7     //return atan2(y,x) < atan2(b.y,b.x);
8     assert(0 && "choose compare");
9 }
10 Point operator + (const Point &b)const{
11     return (Point){x+b.x,y+b.y};
12 }
13 Point operator - (const Point &b)const{
14     return (Point){x-b.x,y-b.y};
15 }
16 Point operator * (const Double &d)const{
17     return Point(d*x,d*y);
18 }
19 Double operator * (const Point &b)const{
20     return x*b.x + y*b.y;
21 }
22 Double operator % (const Point &b)const{
23     return x*b.y - y*b.x;
24 }
25 friend Double abs2(const Point &p){
26     return p.x*p.x + p.y*p.y;
27 }
28 friend Double abs(const Point &p){
29     return sqrt( abs2(p) );
30 }
31 };

```

```

32 typedef Point Vector;
33
34 struct Line{
35     Point P; Vector v;
36     bool operator < (const Line &b)const{
37         return atan2(v.y,v.x) < atan2(b.v.y,b.v.x);
38     }
39 };

```

### 4.2 Half Plane Intersection

```

1 bool OnLeft(const Line& L,const Point& p){
2     return Cross(L.v,p-L.P)>0;
3 }
4 Point GetIntersection(Line a,Line b){
5     Vector u = a.P-b.P;
6     Double t = Cross(b.v,u)/Cross(a.v,b.v);
7     return a.P + a.v*t;
8 }
9 int HalfplaneIntersection(Line* L,int n,Point* poly){
10     sort(L,L+n);
11
12     int first,last;
13     Point *p = new Point[n];
14     Line *q = new Line[n];
15     q[first=last=0] = L[0];
16     for(int i=1;i<n;i++){
17         while(first < last && !OnLeft(L[i],p[last-1])) last--;
18         while(first < last && !OnLeft(L[i],p[first])) first++;
19         q[++last]=L[i];
20         if(fabs(Cross(q[last].v,q[last-1].v))<EPS){
21             last--;
22             if(OnLeft(q[last],L[i].P)) q[last]=L[i];
23         }
24         if(first < last) p[last-1]=GetIntersection(q[last-1],q[last]);
25     }
26     while(first<last && !OnLeft(q[first],p[last-1])) last--;
27     if(last-first<=1) return 0;
28     p[last]=GetIntersection(q[last],q[first]);
29
30     int m=0;
31     for(int i=first;i<=last;i++) poly[m++]=p[i];
32     return m;
33 }

```

### 4.3 K-closet Pair

```

1 #define F(n) Fi(i,n)
2 #define Fi(i,n) Fl(i,0,n)
3 #define Fl(i,l,n) for(int i=(l);i<(int)(n);++i)
4 #include <bits/stdc++.h>

```

```

5 // #include <ext/pb_ds/assoc_container.hpp>
6 // #include <ext/pb_ds/priority_queue.hpp>
7 using namespace std;
8 // using namespace __gnu_pbds;
9 typedef long long ll;
10 struct point {
11     point(ll x_ = 0, ll y_ = 0): x(x_), y(y_) {} ll x, y;
12     inline bool operator<(const point &e_) const {
13         return (x != e_.x ? x < e_.x : y < e_.y);
14     }
15     inline friend istream& operator>>(istream& is_, point& e_) {
16         is_ >> e_.x >> e_.y;
17         return is_;
18     }
19 };
20 int k;
21 priority_queue<ll> PQ;
22 inline ll dist2(const point &e1, const point &e2) {
23     ll res = (e1.x-e2.x)*(e1.x-e2.x)+(e1.y-e2.y)*(e1.y-e2.y);
24     PQ.push(res);
25     if (PQ.size() > k) {
26         PQ.pop();
27     }
28     return res;
29 }
30 #define N 500005
31 point p[N];
32 queue<point> Q;
33 ll closet_point(int l, int m, int r, ll delta2) {
34     ll xmid = p[m-1].x;
35     while (!Q.empty()) {
36         Q.pop();
37     }
38     for (int i = l, j = m; i < m; ++i) {
39         if ((p[i].x-xmid)*(p[i].x-xmid) >= delta2) {
40             continue;
41         }
42         while (j < r && p[j].y < p[i].y && (p[j].y-p[i].y)*(p[j].y-p[i].y) <
            delta2) {
43             if ((p[j].x-xmid)*(p[j].x-xmid) < delta2) {
44                 Q.push(p[j]);
45             }
46             ++j;
47         }
48         while (!Q.empty() && Q.front().y < p[i].y && (Q.front().y-p[i].y)*(Q.
            front().y-p[i].y) > delta2) {
49             Q.pop();
50         }
51         while (!Q.empty()) {
52             delta2 = min(delta2, dist2(p[i], Q.front()));
53             Q.pop();
54         }
55     }
56     return delta2;
57 }
58 ll find_distance(int l, int r) {

```

```

59     if (r - l <= 3000) {
60         ll ans = 0x3f3f3f3f3f3f3f3f;
61         for (int i = l; i < r; ++i)
62             for (int j = i+1; j < r; ++j)
63                 ans = min(ans, dist2(p[i], p[j]));
64         return ans;
65     }
66     int m = (l+r)/2;
67     ll delta2 = min(find_distance(l, m), find_distance(m, r));
68     return min(delta2, closet_point(l, m, r, delta2));
69 }
70 int main() {
71     ios_base::sync_with_stdio(false);
72     cin.tie(NULL);
73     int n;
74     cin >> n >> k;
75     F(n) cin >> p[i];
76     sort(p, p+n);
77     find_distance(0, n);
78     cout << PQ.top() << '\n';
79 }

```

#### 4.4 Minimum Covering Circle

```

1 #define F(n) Fi(i,n)
2 #define Fi(i,n) Fl(i,0,n)
3 #define Fl(i,l,n) for(int i=(l);i<(int)(n);++i)
4 #include <bits/stdc++.h>
5 using namespace std;
6 const double eps = 1e-6;
7 #define x first
8 #define y second
9 typedef pair<double, double> point;
10 inline double dq(const point& p1, const point& p2) {
11     return sqrt((p1.x-p2.x)*(p1.x-p2.x)+(p1.y-p2.y)*(p1.y-p2.y));
12 }
13 inline point oc(const point& pa, const point& pb, const point& pc) {
14     double a, b, c, d, e, f, delta, dx, dy;
15     // ax + by = c
16     // dx + ey = f
17     a = pa.x - pb.x;
18     b = pa.y - pb.y;
19     c = a*(pa.x+pb.x)/2 + b*(pa.y+pb.y)/2;
20     d = pa.x - pc.x;
21     e = pa.y - pc.y;
22     f = d*(pa.x+pc.x)/2 + e*(pa.y+pc.y)/2;
23     delta = a*e-b*d;
24     dx = c*e-f*b;
25     dy = a*f-d*c;
26     return point(dx/delta, dy/delta);
27 }
28 inline point enc(const vector<point>& tmp) {
29     random_shuffle(tmp.begin(), tmp.end());
30     point O = tmp[0];

```

```

31 double r = 0;
32 Fl(i, 1, tmp.size()) if (dq(O, tmp[i]) - r > eps) {
33     O = tmp[i], r = 0;
34     Fi(j, i) if (dq(O, tmp[j]) - r > eps) {
35         O = point((tmp[i].x+tmp[j].x)/2, (tmp[i].y+tmp[j].y)/2);
36         r = dq(O, tmp[j]);
37         Fi(k, j) if (dq(O, tmp[k]) - r > eps)
38             O = oc(tmp[i], tmp[j], tmp[k]), r = dq(O, tmp[k]);
39     }
40 }
41 return O;
42 }
43 int n;
44 vector<point> v;
45 int main() {
46     ios_base::sync_with_stdio(false);
47     cin.tie(NULL);
48     while (cin >> n) {
49         if (!n) break;
50         v.clear();
51         F(n) {
52             point tp;
53             cin >> tp.x >> tp.y;
54             v.push_back(tp);
55         }
56         point ct = enc(v);
57         cout << setprecision(2) << fixed << ct.x << " " << ct.y << " " << dq(ct,
58             v[0]) << "\n";
59     }

```

```

18     }
19     int scc(int n=MAXv){
20         memset(vis,0,sizeof(vis));
21         for (int i=0; i<n; i++)if (!vis[i])
22             dfs(i,GO,-1);
23         memset(vis,0,sizeof(vis));
24         int sc=0;
25         while (!stk.empty()){
26             if (!vis[stk.back()])
27                 dfs(stk.back(),BK,sc++);
28             stk.pop_back();
29         }
30     }
31 }SAT;
32
33 int main(){
34     SAT.scc(2*n);
35     bool ok=1;
36     for (int i=0; i<n; i++){
37         if (SAT.SC[2*i]==SAT.SC[2*i+1])ok=0;
38     }
39     if (ok){
40         for (int i=0; i<n; i++){
41             if (SAT.SC[2*i]>SAT.SC[2*i+1]){
42                 cout << i << endl;
43             }
44         }
45     }
46     else puts("NO");
47 }

```

## 5 Graph

### 5.1 2-SAT

```

1 const int MAXN = 2020;
2
3 struct TwoSAT{
4     static const int MAXv = 2*MAXN;
5     vector<int> GO[MAXv],BK[MAXv],stk;
6     bool vis[MAXv];
7     int SC[MAXv];
8
9     void imply(int u,int v){ // u imply v
10         GO[u].push_back(v);
11         BK[v].push_back(u);
12     }
13     int dfs(int u,vector<int>*G,int sc){
14         vis[u]=1, SC[u]=sc;
15         for (int v:G[u])if (!vis[v])
16             dfs(v,G,sc);
17         if (G==GO)stk.push_back(u);

```

### 5.2 Articulation Point

```

1 void tarjan(int u, int p)
2 { // u 為當前點, p 為當前點之母節點
3     // cnt 為 DFS 次序
4     low[u] = dfn[u] = ++cnt;
5     int i, v;
6     for (i = 0 ; i < G[u].size() ; ++i) {
7         v = G[u][i];
8         if (u == rt && !dfn[v]) ++c;
9         if (!dfn[v]){
10             // (u, v) 為 Tree Edge
11             tarjan(v, u);
12             low[u] = min(low[u], low[v]);
13             // To check if u is AP or not.
14             if (dfn[u] <= low[v] && u != rt) ge[u] = 1;
15         }
16         // 注意不可以同一條邊走兩次，且根節點特判
17         if (v != p && p != -1) low[u] = min(low[u], dfn[v]);
18     }
19 }

```

### 5.3 BCC

```

1 #include <bits/stdc++.h>
2 using namespace std;
3 const int MAXN = 10000;
4 vector<int> adja[MAXN];
5 int gcnt, top, timeStamp, dfn[MAXN], low[MAXN], depth[MAXN];
6 pair<int, int> stk[MAXN], ans[MAXN];
7 set<int> group[MAXN];
8 bool cut[MAXN];
9 void BCC(int now, int nextv){
10     int sf, st;
11     group[gcnt].clear();
12     do{
13         sf = stk[top-1].first, st = stk[top-1].second;
14         group[gcnt].insert(sf);
15         group[gcnt].insert(st);
16         --top;
17     }while(sf != now || st != nextv);
18     ++gcnt;
19 }
20 void tarjan(int now, int parent, int d){
21     int child = 0;
22     dfn[now] = low[now] = ++timeStamp, depth[now] = d;
23     for(int i = 0; i < adja[now].size(); i++){
24         int nextv = adja[now][i];
25         if(nextv == parent) continue;
26         if(dfn[nextv] == 0){
27             stk[top++] = make_pair(now, nextv);
28             tarjan(nextv, now, d+1);
29             low[now] = min(low[now], low[nextv]);
30             ++child;
31             if( (parent != -1 && low[nextv] >= dfn[now]) || (parent == -1 &&
child >= 2)){
32                 cut[now] = true;
33                 if(parent != -1) BCC(now, nextv);
34             }
35             if(parent == -1) BCC(now, nextv);
36         }
37         else if(depth[nextv] < depth[now]-1){
38             stk[top++] = make_pair(now, nextv);
39             low[now] = min(low[now], dfn[nextv]);
40         }
41     }
42 }
43 int main(){
44     int n,m,x,y,cnt=0;
45     while(~scanf("%d",&n)){
46         cnt=timeStamp=top=gcnt=0;
47         memset(cut, 0, sizeof(cut));
48         memset(dfn, 0, sizeof(dfn));
49         for(int i=0;i<n;i++) adja[i].clear();
50         for(int i=0;i<n;i++){
51             scanf("%d ",&x);
52             scanf("(%d)",&m);
53             while(m--){

```

```

54             scanf("%d",&y);
55             adja[x].push_back(y);
56         }
57     }
58     for(int i=0;i<n;i++){
59         if(dfn[i]==0) tarjan(i, -1, 1);
60     }
61     for(int i=0;i<gcnt;i++){
62         if(group[i].size()==2){
63             //critical links
64         }
65     }
66 }

```

### 5.4 Heavy Light Decomposition

```

1 // N: 10010, LOG: 15, INF: 1e9
2 // val[]: array that stores initial values
3 int n;
4 // ed: store input edges
5 struct edge ed[N];
6 vector<int> g[N];
7 int sz[N], dep[N];
8 int ts, tin[N], tout[N]; // timestamp
9 int par[N][LOG+1], head[N];
10 // head: head of the chain that contains u
11
12 void dfsz(int u, int p) {
13     // precompute the size of each subtree
14     par[u][0] = p;
15     sz[u][1] = 1;
16     head[u] = u;
17     for (int v: g[u]) if (v != p) {
18         dep[v] = dep[u] + 1;
19         dfsz(v, u);
20         sz[u] += sz[v];
21     }
22 }
23
24 void dfs1(int u) {
25     tin[u] = tout[u] = ++ts;
26     sort(g[u].begin(), g[u].end(),
27         [&](int a, int b) { return sz[a] > sz[b]; });
28     bool flag = 1;
29     for (int v: g[u]) if (v != par[u][0]) {
30         if (flag) head[v] = head[u], flag = 0;
31         dfs1(v);
32     }
33     tout[u] = ts;
34 }
35
36 inline bool anc(int a, int b) {
37     return tin[a] <= tin[b] && tout[b] <= tout[a];
38 }

```



```

39
40 inline bool lca(int a, int b) {
41     if (anc(b, a)) return b;
42     for (int j = LOG ; j >= 0 ; --j)
43         if (!anc(par[b][j], a))
44             b = par[b][j];
45     return par[b][0];
46 }
47 vector<pii> getPath(int u, int v) {
48     // u must be ancestor of v
49     // return a list of intervals from u to v
50     vector<pii> res;
51     while (tin[u] < tin[head[v]]) {
52         res.push_back(pii(tin[head[v]], tin[v]));
53         v = par[head[v]][0];
54     }
55     if (tin[u] + 1 <= tin[v])
56         res.push_back(pii(tin[u]+1, tin[v]));
57     return res;
58 }
59 void init() {
60     cin >> n;
61     for (int i = 1 ; i < n ; ++i) {
62         int u, v, vl;
63         cin >> u >> v >> vl;
64         ed[i] = edge(u, v, vl);
65         g[u].push_back(v);
66         g[v].push_back(u);
67     }
68     // do Heavy-Light Decomp.
69     int root = 1; // set root node
70     dep[root] = 1;
71     dfsz(root, root);
72     ts = 0;
73     dfs1(root);
74     for (int k = 1 ; k <= LOG ; ++k)
75         for (int i = 1 ; i <= n ; ++i)
76             par[i][k] = par[par[i][k-1]][k-1];
77     // set initial values
78     for (int i = 1 ; i < n ; ++i) {
79         if (dep[ed[i].u] < dep[ed[i].v])
80             swap(ed[i].u, ed[i].v);
81         val[tin[ed[i].u]] = ed[i].vl;
82     }
83 }

```

## 5.5 SCC

```

1 // Kosaraju - Find SCC by twice dfs, and the SCC DAG is in the Topology
2 // ordering.
3 // Owner: samsam2310
4 //
5 #include <bits/stdc++.h>
6 #define N 30002 // Maximum number of vertices

```

```

7 using namespace std;
8 vector<int> forward_graph[N]; // original graph
9 vector<int> backward_graph[N]; // reverse graph
10 vector<int> dag_graph[N]; // result dag graph(graph of scc)
11 int scc[N]; // SCC index of a vertex
12 bool visit[N];
13 void init() {
14     fill(forward_graph, forward_graph + N, vector<int>());
15     fill(backward_graph, backward_graph + N, vector<int>());
16     fill(dag_graph, dag_graph + N, vector<int>());
17 }
18 void dfs(vector<int> &graph, int now, int scc_id,
19         stack<int> *leave_order = NULL) {
20     visit[now] = true;
21     if (scc != -1) {
22         scc[now] = scc_id;
23     }
24     for (int v : graph[now]) {
25         if (!visit[v]) {
26             dfs(graph, v, scc_id, leave_order);
27         }
28     }
29     if (leave_order) {
30         leave_order->push(now);
31     }
32 }
33 int main(int argc, char *argv[]) {
34     ios_base::sync_with_stdio(false);
35     cin.tie(0);
36     init();
37     cin >> n;
38     for (int i = 0; i < n; ++i) {
39         int a, b; // edge of a -> b
40         cin >> a >> b;
41         forward_graph[a].push_back(b);
42         backward_graph[b].push_back(a);
43     }
44     // Find the SCC.
45     memset(visit, 0, sizeof(visit));
46     stack<int> leave_order;
47     for (int i = 0; i < n; ++i) {
48         if (!visit[i]) {
49             dfs(forward_graph, i, -1, &leave_order);
50         }
51     }
52     memset(visit, 0, sizeof(visit));
53     int scc_id = 0;
54     while (!leave_order.empty()) {
55         int v = leave_order.top();
56         leave_order.pop();
57         if (!visit[v]) {
58             dfs(backward_graph, v, scc_id, NULL);
59             ++scc_id;
60         }
61     }
62     // Build the SCC DAG.

```

```

63     for (int i = 0; i < n; ++i) {
64         for (int v : forward_graph[i]) {
65             if (scc[i] != scc[v]) {
66                 dag_graph[scc[i]].push_back(scc[v]);
67             }
68         }
69     }
70     return 0;
71 }

```

## 6 Java

### 6.1 Big Integer

```

1 import java.math.*;
2 import java.io.*;
3 import java.util.*;
4 public class Main{
5     public static void main(String []argv){
6         c[0][0]=BigInteger.ONE;
7         for(int i=1;i<3001;i++){
8             c[i][0]=BigInteger.ONE;
9             c[i][i]=BigInteger.ONE;
10            for(int j=1;j<i;j++)c[i][j]=c[i-1][j].add(c[i-1][j-1]);
11        }
12        Scanner scanner = new Scanner(System.in);
13        int T = scanner.nextInt();
14        BigInteger x;
15        BigInteger ans;
16        while(T-- > 0){
17            ans = BigInteger.ZERO;
18            int n = scanner.nextInt();
19            for(int i=0;i<n;i++){
20                x = new BigInteger(scanner.next());
21                if(i%2 == 1)ans=ans.subtract(c[n-1][i].multiply(x));
22                else ans=ans.add(c[n-1][i].multiply(x));
23            }
24            if(n%2 == 0)ans=BigInteger.ZERO.subtract(ans);
25            System.out.println(ans);
26        }
27    }
28 }

```

### 6.2 Prime

```

1 import java.math.*;
2 import java.io.*;
3 import java.util.*;
4 public class Main{

```

```

5     public static void main(String []argv){
6         Scanner scanner = new Scanner(System.in);
7         int T = scanner.nextInt();
8         for (int cs = 0 ; cs < T ; cs++){
9             if (cs != 0) { System.out.println(""); }
10            int a = scanner.nextInt();
11            int b = scanner.nextInt();
12            for (int i = a ; i <= b ; i++) {
13                BigInteger x = BigInteger.valueOf(i);
14                if (x.isProbablePrime(5) == true) {
15                    System.out.println(x);
16                }
17            }
18        }
19    }
20 }

```

## 7 Matching

### 7.1 Bipartite Matching

```

1 #include<bits/stdc++.h>
2 #define V 20100
3 #define inf 0x3f3f3f3f
4 int mx[V],my[V],dis[V],que[V];
5 bool vis[V];
6 vector<int> g[V];
7 bool DFS(int u){
8     vis[u]=true;
9     for(int i=0;i<g[u].size();i++){
10         int v=my[g[u][i]];
11         if(v!=-1&&!vis[v]&&dis[v]==dis[u]+1&&DFS(v)){
12             mx[u]=g[u][i];
13             my[g[u][i]]=u;
14             return true;
15         }
16     }
17     return false;
18 }
19 // n is the size of left hand side
20 int Hopcroft_Karp(int n){
21     int matching=0,qt,qf,sp,i,u,v;
22     bool flag=true;
23     memset(mx,-1,sizeof(mx));
24     memset(my,-1,sizeof(my));
25     while(flag){
26         flag=false;
27         qt=qf=0;
28         sp=inf;
29         for(i=0;i<n;i++){
30             if(mx[i]==-1){
31                 dis[i]=0;

```

```

32     que[qt++]=i;
33     }
34     else dis[i]=inf;
35     }
36     while(qf<qt){
37         u=que[qf++];
38         if(dis[u]>=sp) continue;
39         for(i=0;i<g[u].size();i++){
40             v=my[g[u][i]];
41             if(v==-1){
42                 if(dis[u]+1<sp){
43                     sp=dis[u]+1;
44                     flag=true;
45                 }
46             }
47             else if(dis[u]+1<dis[v]){
48                 dis[v]=dis[u]+1;
49                 que[qt++]=v;
50             }
51         }
52     }
53     if(flag){
54         memset(vis,0,sizeof(vis));
55         for(i=0;i<n;i++){
56             if(dis[i]==0&&DFS(i)) matching++;
57         }
58     }
59 }
60 return matching;
61 }

```

```

22 for(int i=1;i<=n;++i)st[i]=i;//st[i]表示第i個點的集合
23 memset(S+1,-1,sizeof(int)*n);//-1:沒走過 0:偶點 1:奇點
24 queue<int>q;qpsh(u);
25 while(q.size()){
26     u=q.front(),q.pop();
27     for(size_t i=0;i<g[u].size();++i){
28         int v=g[u][i];
29         if(S[v]==-1){
30             pa[v]=u,S[v]=1;
31             if(!match[v]){//有增廣路直接擴充
32                 for(int lst;u;v=lst,u=pa[v])
33                     lst=match[u],match[u]=v,match[v]=u;
34             return 1;
35         }
36         qpsh(match[v]);
37     }else if(!S[v]&&st[v]!=st[u]){
38         int l=lca(st[v],st[u]);//遇到花，做花的處理
39         flower(v,u,l,q),flower(u,v,l,q);
40     }
41 }
42 }
43 return 0;
44 }
45 inline int blossom(){
46     memset(pa+1,0,sizeof(int)*n);
47     memset(match+1,0,sizeof(int)*n);
48     int ans=0;
49     for(int i=1;i<=n;++i)
50         if(!match[i]&&bfs(i))++ans;
51     return ans;
52 }

```

## 7.2 Blossom

```

1 #define MAXN 505
2 vector<int>g[MAXN];//用vector存圖
3 int pa[MAXN],match[MAXN],st[MAXN],S[MAXN],vis[MAXN];
4 int t,n;
5 inline int lca(int u,int v){//找花的花托
6     for(++t;;swap(u,v)){
7         if(u==0)continue;
8         if(vis[u]==t)return u;
9         vis[u]=t;//這種方法可以不用清空vis陣列
10        u=st[pa[match[u]]];
11    }
12 }
13 #define qpsh(u) q.push(u),S[u]=0
14 inline void flower(int u,int v,int l,queue<int> &q){
15     while(st[u]!=1){
16         pa[u]=v;//所有未匹配邊的pa都是雙向的
17         if(S[v==match[u]]==1)qpsh(v);//所有奇點變偶點
18         st[u]=st[v]=1,u=pa[v];
19     }
20 }
21 inline bool bfs(int u){

```

## 7.3 Dinic

```

1 //Dinic
2 #define V 1000
3 struct edge{
4     edge(){}
5     edge(int a,int b,int c):to(a),cap(b),rev(c){}
6     int to,cap,rev;
7 };
8 vector<edge> g[V];
9 int level[V];
10 int iter[V];
11 void add_edge(int from,int to,int cap){
12     g[from].push_back(edge(to,cap,g[to].size()));
13     g[to].push_back(edge(from,0,g[from].size()-1));
14 }
15 void bfs(int s){
16     memset(level,-1,sizeof(level));
17     queue<int>que;
18     level[s]=0;
19     que.push(s);
20     while(!que.empty()){

```

```

21     int v=que.front();
22     que.pop();
23     for(int q=0;q<g[v].size();q++){
24         edge &e=g[v][q];
25         if(e.cap>0&&level[e.to]<0){
26             level[e.to]=level[v]+1;
27             que.push(e.to);
28         }
29     }
30 }
31 }
32 int dfs(int v,int t,int f){
33     if(v==t) return f;
34     for(int &q=iter[v];q<g[v].size();++q){
35         edge &e=g[v][q];
36         if(e.cap>0&&level[v]<level[e.to]){
37             int d=dfs(e.to,t,min(f,e.cap));
38             if(d>0){
39                 e.cap-=d;
40                 g[e.to][e.rev].cap+=d;
41                 return d;
42             }
43         }
44     }
45     return 0;
46 }
47 int max_flow(int s,int t){
48     int flow=0;
49     for(;;){
50         bfs(s);
51         if(level[t]<0) return flow;
52         memset(iter,0,sizeof(iter));
53         int f;
54         while((f=dfs(s,t,1e9))>0)
55             flow+=f;
56     }
57 }

```

## 7.4 KM

```

1 #define MAXN 100
2 #define INF INT_MAX
3 int g[MAXN][MAXN],lx[MAXN],ly[MAXN],slack_y[MAXN];
4 int px[MAXN],py[MAXN],match_y[MAXN],par[MAXN];
5 int n;
6 void adjust(int y){//把增廣路上所有邊反轉
7     match_y[y]=py[y];
8     if(px[match_y[y]]!=-2)
9         adjust(px[match_y[y]]);
10 }
11 bool dfs(int x){//DFS找增廣路
12     for(int y=0;y<n;++y){
13         if(py[y]!=-1) continue;
14         int t=lx[x]+ly[y]-g[x][y];

```

```

15         if(t==0){
16             py[y]=x;
17             if(match_y[y]==-1){
18                 adjust(y);
19                 return 1;
20             }
21             if(px[match_y[y]]!=-1) continue;
22             px[match_y[y]]=y;
23             if(dfs(match_y[y])) return 1;
24         } else if(slack_y[y]>t){
25             slack_y[y]=t;
26             par[y]=x;
27         }
28     }
29     return 0;
30 }
31 inline int km(){
32     memset(ly,0,sizeof(int)*n);
33     memset(match_y,-1,sizeof(int)*n);
34     for(int x=0;x<n;++x){
35         lx[x]=-INF;
36         for(int y=0;y<n;++y){
37             lx[x]=max(lx[x],g[x][y]);
38         }
39     }
40     for(int x=0;x<n;++x){
41         for(int y=0;y<n;++y) slack_y[y]=INF;
42         memset(px,-1,sizeof(int)*n);
43         memset(py,-1,sizeof(int)*n);
44         px[x]=-2;
45         if(dfs(x)) continue;
46         bool flag=1;
47         while(flag){
48             int cut=INF;
49             for(int y=0;y<n;++y)
50                 if(py[y]==-1&&cut>slack_y[y]) cut=slack_y[y];
51             for(int j=0;j<n;++j){
52                 if(px[j]!=-1) lx[j]-=cut;
53                 if(py[j]!=-1) ly[j]+=cut;
54                 else slack_y[j]-=cut;
55             }
56             for(int y=0;y<n;++y){
57                 if(py[y]==-1&&slack_y[y]==0){
58                     py[y]=par[y];
59                     if(match_y[y]==-1){
60                         adjust(y);
61                         flag=0;
62                         break;
63                     }
64                     px[match_y[y]]=y;
65                     if(dfs(match_y[y])){
66                         flag=0;
67                         break;
68                     }
69                 }
70             }

```

```

71     }
72 }
73 int ans=0;
74 for(int y=0;y<n;++y) if (g[match_y[y]][y] != -INF) ans+=g[match_y[y]][y];
75 return ans;
76 }

```

## 7.5 Min Cost Flow

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define int long long
4 typedef pair<int,int> P;
5 struct edge{
6     edge(){}
7     edge(int a,int b,int c,int d):to(a),cap(b),cost(c),rev(d){}
8     int to,cap,cost,rev;
9 };
10 #define V 210
11 #define inf 1000000000000000000
12 vector<edge> g[V];
13 int h[V],dist[V],prev_v[V],prev_e[V];
14 void add_edge(int from,int to,int cap,int cost){
15     g[from].push_back(edge(to,cap,cost,g[to].size()));
16     g[to].push_back(edge(from,0,-cost,g[from].size()-1));
17 }
18 int min_costflow(int s,int t,int f){
19     int res=0;
20     memset(h,0,sizeof(h));
21     while(f>0){
22         priority_queue<P,vector<P>,greater<P>> que;
23         fill(dist,dist+V,inf);
24         dist[s]=0;
25         que.push(P(dist[s],s));
26         while(!que.empty()){
27             P p=que.top();
28             que.pop();
29             int v=p.second;
30             if(dist[v]<p.first) continue;
31             for(int i=0;i<g[v].size();++i){
32                 edge &e=g[v][i];
33                 if(e.cap>0&&dist[e.to]>dist[v]+e.cost+h[v]-h[e.to]){
34                     dist[e.to]=dist[v]+e.cost+h[v]-h[e.to];
35                     prev_v[e.to]=v;
36                     prev_e[e.to]=i;
37                     que.push(P(dist[e.to],e.to));
38                 }
39             }
40         }
41         if(dist[t]==inf) return -1;
42         for(int v=0;v<V;++v) h[v]+=dist[v];
43         int d=f;
44         for(int v=t;v!=s;v=prev_v[v]) d=min(d,g[prev_v[v]][prev_e[v]].cap);
45         f-=d;

```

```

46         res+=d*h[t];
47         for(int v=t;v!=s;v=prev_v[v]){
48             edge &e=g[prev_v[v]][prev_e[v]];
49             e.cap-=d;
50             g[v][e.rev].cap+=d;
51         }
52     }
53     return res;
54 }
55 #undef int
56 int main()
57 {
58     #define int long long
59     int T,n,m,cost,l,s,t,ans;
60     cin>>T;
61     while(T--){
62         cin>>n>>m;
63         for(int q=0;q<V;++q) g[q].clear();
64         s=m+n;
65         t=m+n+1;
66         for(int i=0;i<n;++i)
67             for(int j=0;j<m;++j){
68                 cin>>cost;
69                 if(cost>0)
70                     add_edge(n+j,i,1,cost);
71             }
72         for(int i=0;i<m;++i){
73             cin>>l;
74             add_edge(s,n+i,1,0);
75         }
76         for(int i=0;i<n;++i)
77             add_edge(i,t,1,0);
78         ans=min_costflow(s,t,n);
79         cout<<ans<<endl;
80     }
81     return 0;
82 }

```

## 7.6 Stable Marriage

```

1 #define F(n) Fi(i, n)
2 #define Fi(i, n) Fl(i, 0, n)
3 #define Fl(i, l, n) for(int i = l ; i < n ; ++i)
4 #include <bits/stdc++.h>
5 using namespace std;
6 int D, quota[205], weight[205][5];
7 int S, scoretodep[12005][205], score[5];
8 int P, prefer[12005][85], iter[12005];
9 int ans[12005];
10 typedef pair<int, int> PII;
11 map<int, int> samescore[205];
12 typedef priority_queue<PII, vector<PII>, greater<PII>> QQQ;
13 QQQ pri[205];
14 void check(int d) {

```

```

15     PII t = pri[d].top();
16     int v;
17     if (pri[d].size() - samescore[d][t.first] + 1 <= quota[d]) return;
18     while (pri[d].top().first == t.first) {
19         v = pri[d].top().second;
20         ans[v] = -1;
21         --samescore[d][t.first];
22         pri[d].pop();
23     }
24 }
25 void push(int s, int d) {
26     if (pri[d].size() < quota[d]) {
27         pri[d].push(PII(scoretoDep[s][d], s));
28         ans[s] = d;
29         ++samescore[s][scoretoDep[s][d]];
30     } else if (scoretoDep[s][d] >= pri[d].top().first) {
31         pri[d].push(PII(scoretoDep[s][d], s));
32         ans[s] = d;
33         ++samescore[s][scoretoDep[s][d]];
34         check(d);
35     }
36 }
37 void f() {
38     int over;
39     while (true) {
40         over = 1;
41         Fi (q, S) {
42             if (ans[q] != -1 || iter[q] >= P) continue;
43             push(q, prefer[q][iter[q]++]);
44             over = 0;
45         }
46         if (over) break;
47     }
48 }
49 main() {
50     ios::sync_with_stdio(false);
51     cin.tie(NULL);
52     int sadmit, stof, dexceed, dfew;
53     while (cin >> D, D) { // Beware of the input format or judge may troll us.
54         sadmit = stof = dexceed = dfew = 0;
55         memset(iter, 0, sizeof(iter));
56         memset(ans, 0, sizeof(ans));
57         Fi (q, 205) {
58             pri[q] = QQQ();
59             samescore[q].clear();
60         }
61         cin >> S >> P;
62         Fi (q, D) {
63             cin >> quota[q];
64             Fi (w, 5) cin >> weight[q][w];
65         }
66         Fi (q, S) {
67             Fi (w, 5) cin >> score[w];
68             Fi (w, D) {
69                 scoretoDep[q][w] = 0;
70                 F (5) scoretoDep[q][w] += weight[w][i] * score[i];

```

```

71     }
72 }
73 Fi (q, S) Fi (w, P) {
74     cin >> prefer[q][w];
75     --prefer[q][w];
76 }
77 f();
78 Fi (q, D) sadmit += pri[q].size();
79 Fi (q, S) if (ans[q] == prefer[q][0]) ++stof;
80 Fi (q, D) if (pri[q].size() > quota[q]) ++dexceed;
81 Fi (q, D) if (pri[q].size() < quota[q]) ++dfew;
82 cout << sadmit << ' ' << stof << ' ' << dexceed << ' ' << dfew << '\n';
83 }
84 }

```

## 8 Mathematics

### 8.1 Extended GCD

```

1 template <typename T>
2 T extgcd(T a, T b, T &x, T &y){
3     // g = a * x + b * y
4     T g = a;
5     if (b != 0) {
6         g = extgcd(b, a % b, y, x);
7         y -= (a / b) * x;
8     }
9     else x = 1, y = 0;
10    return g;
11 }

```

### 8.2 Lucas's Theorem

```

1 bigM = int(1e9+7)
2 fac = [1]*10001
3 for i in range(1, 10001):
4     fac[i] = fac[i-1]*i
5 ifac = [pow(fac[i], bigM-2, bigM) for i in range(10001)]
6 def f(a, b, M):
7     if b == 0 or b == a:
8         return 1
9     elif a < b:
10        return 0
11    elif a < M:
12        return fac[a]*ifac[b]*ifac[a-b]%bigM
13    else:
14        return f(a//M, b//M, M) * f(a%M, b%M, M) % bigM
15 t = int(input())
16 for cases in range(t):

```

```

17 a, b, M = [int(x) for x in input().split()]
18 print(f(a, b, M))

```

## 8.3 Miller-Rabin

```

1 inline long long mod_mul(long long a, long long b, long long m) {
2     a%=m, b%=m;
3     long long y=(long long)((double)a*b/m+0.5); /* fast for m < 2^58 */
4     long long r=(a*b-y*m)%m;
5     return r<0?r+m:r;
6 }
7 template<typename T>
8 inline T pow(T a, T b, T mod) { // a^b % mod
9     T ans=1;
10    for(; b; a=mod_mul(a, a, mod), b>>=1)
11        if(b&1) ans=mod_mul(ans, a, mod);
12    return ans;
13 }
14 int sprp[3]={2, 7, 61}; // int範圍可解
15 int llsprp[7]={2, 325, 9375, 28178, 450775, 9780504, 1795265022}; // 至少unsigned
16                                     long long範圍
17 template<typename T>
18 inline bool isprime(T n, int *sprp, int num) {
19     if(n==2) return 1;
20     if(n<2 || n%2==0) return 0;
21     int t=0;
22     T u=n-1;
23     for(; u%2==0; ++t) u>>=1;
24     for(int i=0; i<num; ++i) {
25         T a=sprp[i]%n;
26         if(a==0 || a==1 || a==n-1) continue;
27         T x=pow(a, u, n);
28         if(x==1 || x==n-1) continue;
29         for(int j=0; j<t; ++j) {
30             x=mod_mul(x, x, n);
31             if(x==1) return 0;
32             if(x==n-1) break;
33         }
34         if(x==n-1) continue;
35         return 0;
36     }
37     return 1;
38 }

```

## 9 String

### 9.1 AC Automaton

```

1 #ifndef SUNMOON_AHO_CORASICK_AUTOMATON
2 #define SUNMOON_AHO_CORASICK_AUTOMATON
3 #include<queue>
4 #include<vector>
5 template<char L='a', char R='z'>
6 class ac_automaton {
7     private:
8         struct joe {
9             int next[R-L+1], fail, efl, ed, cnt_dp, vis;
10            joe() : ed(0), cnt_dp(0), vis(0) {
11                for(int i=0; i<=R-L; ++i) next[i]=0;
12            }
13        };
14    public:
15        std::vector<joe> S;
16        std::vector<int> q;
17        int qs, qe, vt;
18        ac_automaton() : S(1), qs(0), qe(0), vt(0) {}
19        inline void clear() {
20            q.clear();
21            S.resize(1);
22            for(int i=0; i<=R-L; ++i) S[0].next[i]=0;
23            S[0].cnt_dp=S[0].vis=qs=qe=vt=0;
24        }
25        inline void insert(const char *s) {
26            int o=0;
27            for(int i=0; i<strlen(s); ++i) {
28                id=s[i]-L;
29                if(!S[o].next[id]) {
30                    S.push_back(joe());
31                    S[o].next[id]=S.size()-1;
32                }
33                o=S[o].next[id];
34            }
35            ++S[o].ed;
36        }
37        inline void build_fail() {
38            S[0].fail=S[0].efl=-1;
39            q.clear();
40            q.push_back(0);
41            ++qe;
42            while(qs!=qe) {
43                int pa=q[qs++], id, t;
44                for(int i=0; i<=R-L; ++i) {
45                    t=S[pa].next[i];
46                    if(!t) continue;
47                    id=S[pa].fail;
48                    while(~id&&!S[id].next[i]) id=S[id].fail;
49                    S[t].fail=~id?S[id].next[i]:0;
50                    S[t].efl=S[S[t].fail].ed?S[t].fail:S[S[t].fail].efl;
51                    q.push_back(t);
52                    ++qe;
53                }
54            }
55        }
56        /* DP出每個前綴在字串s出現的次數並傳回所有字串被s匹配成功的次數O(N+M) */

```

```

57 inline int match_0(const char *s){
58     int ans=0,id,p=0,i;
59     for(i=0;s[i];++i){
60         id=s[i]-L;
61         while(!S[p].next[id]&&p)p=S[p].fail;
62         if(!S[p].next[id])continue;
63         p=S[p].next[id];
64         ++S[p].cnt_dp; /*匹配成功則它所有後綴都可以被匹配(DP計算)*/
65     }
66     for(i=qe-1;i>=0;--i){
67         ans+=S[q[i]].cnt_dp*S[q[i]].ed;
68         if(~S[q[i]].fail)S[S[q[i]].fail].cnt_dp+=S[q[i]].cnt_dp;
69     }
70     return ans;
71 }
72 /*多串匹配走efl邊並傳回所有字串被s匹配成功的次數O(N*M^1.5)*/
73 inline int match_1(const char *s) const{
74     int ans=0,id,p=0,t;
75     for(int i=0;s[i];++i){
76         id=s[i]-L;
77         while(!S[p].next[id]&&p)p=S[p].fail;
78         if(!S[p].next[id])continue;
79         p=S[p].next[id];
80         if(S[p].ed)ans+=S[p].ed;
81         for(t=S[p].efl;~t;t=S[t].efl){
82             ans+=S[t].ed; /*因為都走efl邊所以保證匹配成功*/
83         }
84     }
85     return ans;
86 }
87 /*枚舉(s的子字串0A)的所有相異字串各恰一次並傳回次數O(N*M^(1/3))*/
88 inline int match_2(const char *s){
89     int ans=0,id,p=0,t;
90     ++vt;
91     /*把戳記vt+=1，只要vt沒溢位，所有S[p].vis==vt就會變成false
92     這種利用vt的方法可以O(1)歸零vis陣列*/
93     for(int i=0;s[i];++i){
94         id=s[i]-L;
95         while(!S[p].next[id]&&p)p=S[p].fail;
96         if(!S[p].next[id])continue;
97         p=S[p].next[id];
98         if(S[p].ed&&S[p].vis!=vt){
99             S[p].vis=vt;
100             ans+=S[p].ed;
101         }
102         for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[t].efl){
103             S[t].vis=vt;
104             ans+=S[t].ed; /*因為都走efl邊所以保證匹配成功*/
105         }
106     }
107     return ans;
108 }
109 /*把AC自動機變成真的自動機*/
110 inline void evolution(){
111     for(qs=1;qs!=qe;){
112         int p=q[qs++];

```

```

113         for(int i=0;i<=R-L;++i)
114             if(S[p].next[i]==0)S[p].next[i]=S[S[p].fail].next[i];
115     }
116 }
117 };
118 #endif

```

## 9.2 BWT

```

1 // BWT
2 const int N = 8; // 字串長度
3 int s[N+N+1] = "suffixes"; // 字串，後面預留一倍空間。
4 int sa[N]; // 後綴陣列
5 int pivot;
6
7 int cmp(const void* i, const void* j)
8 {
9     return strcmp(s+(int*)i, s+(int*)j, N);
10 }
11
12 // 此處便宜行事，採用 O(N^2 log N) 的後綴陣列演算法。
13 void BWT()
14 {
15     strncpy(s + N, s, N);
16     for (int i=0; i<N; ++i) sa[i] = i;
17     qsort(sa, N, sizeof(int), cmp);
18     // 當輸入字串的所有字元都相同，必須當作特例處理。
19     // 或者改用stable sort。
20
21     for (int i=0; i<N; ++i)
22         cout << s[(sa[i] + N-1) % N];
23
24     for (int i=0; i<N; ++i)
25         if (sa[i] == 0)
26         {
27             pivot = i;
28             break;
29         }
30 }
31
32 // Inverse BWT
33 const int N = 8; // 字串長度
34 char t[N+1] = "xuffessi"; // 字串
35 int pivot;
36 int next[N];
37
38 void IBWT()
39 {
40     vector<int> index[256];
41     for (int i=0; i<N; ++i)
42         index[t[i]].push_back(i);
43
44     for (int i=0, n=0; i<256; ++i)
45         for (int j=0; j<index[i].size(); ++j)

```



```

46         next[n++] = index[i][j];
47
48     int p = pivot;
49     for (int i=0; i<N; ++i)
50         cout << t[p = next[p]];
51 }

```

### 9.3 KMP

```

1  template<typename T>
2  void build_KMP(int n, T *s, int *f){ // 1 base
3      f[0]=-1, f[1]=0;
4      for (int i=2; i<=n; i++){
5          int w = f[i-1];
6          while (w>=0 && s[w+1]!=s[i]) w = f[w];
7          f[i]=w+1;
8      }
9  }
10
11 template<typename T>
12 int KMP(int n, T *a, int m, T *b){
13     build_KMP(m,b,f);
14     int ans=0;
15
16     for (int i=1, w=0; i<=n; i++){
17         while ( w>=0 && b[w+1]!=a[i] ) w = f[w];
18         w++;
19         if (w==m){
20             ans++;
21             w=f[w];
22         }
23     }
24     return ans;
25 }

```

### 9.4 Suffix Array

```

1  //should initialize s and n first
2  #define N 301000
3  using namespace std;
4  char s[N]; //string=s,suffix array=sar,longest common prefix=lcp
5  int rk[2][N],id[2][N];
6  int n,p;
7  int cnt[N];
8  int len[N],od[N],sar[N];
9  inline int sr(int i,int t){ //rank of shifted position
10     return i+t<n?rk[p][i+t]:-1;
11 }
12 inline bool check_same(int i,int j,int t){
13     return rk[p][i]==rk[p][j]&&sr(i,t)==sr(j,t);
14 }

```

```

15 bool cmp(int i,int j){
16     return s[i]<s[j];
17 }
18 void sa(){ //length of array s
19     int i,t,now,pre;
20     memset(cnt,0,sizeof(cnt));
21     for(i=0;i<n;i++){
22         id[p][i]=i;
23         rk[p][i]=s[i];
24         cnt[s[i]]++;
25     }
26     for(i=1;i<128;i++) cnt[i]+=cnt[i-1];
27     sort(id[p],id[p]+n,cmp);
28     for(t=1;t<n;t<=1){
29         //least significant bit is already sorted
30         for(i=n-1;i>=0;i--){
31             now=id[p][i]-t;
32             if(now>=0) id[p^1][--cnt[rk[p][now]]]=now;
33         }
34         for(i=n-t;i<n;i++){
35             id[p^1][--cnt[rk[p][i]]]=i;
36         }
37         memset(cnt,0,sizeof(cnt));
38         now=id[p^1][0];
39         rk[p^1][now]=0;
40         cnt[0]++;
41         for(i=1;i<n;i++){
42             pre=now;
43             now=id[p^1][i];
44             if(check_same(pre,now,t)){
45                 rk[p^1][now]=rk[p^1][pre];
46             }
47             else{
48                 rk[p^1][now]=rk[p^1][pre]+1;
49             }
50             cnt[rk[p^1][now]]++;
51         }
52         p^=1;
53         if(rk[p][now]==n-1) break;
54         for(i=1;i<n;i++) cnt[i]+=cnt[i-1];
55     }
56     memcpy(sar,id[p],sizeof(sar));
57 }
58 void lcp(){
59     int i,l,pre;
60     for(i=0;i<n;i++) od[sar[i]]=i;
61     for(i=0;i<n;i++){
62         if(i) l=len[od[i-1]]?len[od[i-1]]-1:0;
63         else l=0;
64         if(od[i]){
65             pre=sar[od[i]-1];
66             while(pre+1<n&&i+1<n&&s[pre+1]==s[i+1]) l++;
67             len[od[i]]=l;
68         }
69         else len[0]=0;
70     }

```

```
71 }
```

## 9.5 Suffix Automaton

```
1 #include<bits/stdc++.h>
2 #define C 96
3 #define N 200100
4 using namespace std;
5 struct SAM{
6     struct node{
7         node *nxt[C],*pre;
8         int len;
9         vector<int> pos;
10    };
11    node mem[N*2],*root,*ed;
12    int top;
13    SAM(){
14        top = 0;
15        root = new_node(0);
16        ed = root;
17    }
18    node *new_node(int l){
19        for(int i=0;i<C;i++) mem[top].nxt[i]=NULL;
20        mem[top].pre=NULL;
21        mem[top].len=l;
22        mem[top].pos.clear();
23        return mem+(top++);
24    }
25    node *split_node(int l,node *p){
26        for(int i=0;i<C;i++) mem[top].nxt[i]=p->nxt[i];
27        mem[top].pre = p->pre;
28        mem[top].len = l;
29        mem[top].pos.assign()
30        p->pre = mem+top;
31        return mem+(top++);
32    }
33    void push(char c){
34        node *nw = new_node(ed->len+1),*ptr=ed->pre;
35        ed->nxt[c] = nw;
36        nw->pos.push_back(ed->len);
37        for(;ptr;ptr=ptr->pre){
38            if(ptr->nxt[c]){
39                if(ptr->nxt[c]->len==ptr->len+1){
40                    nw->pre = ptr->nxt[c];
41                }
42                else{
43                    node *tmp=ptr->nxt[c];
44                    nw->pre = split_node(ptr->len+1,tmp);
45                    while(ptr && ptr->nxt[c]==tmp){
46                        ptr->nxt[c] = nw->pre;
47                        ptr = ptr->pre;
48                    }
49                }
50                break;

```

```
51    }
52    else{
53        ptr->nxt[c] = nw;
54    }
55    }
56    if(!nw->pre) nw->pre = root;
57    ed = ed->nxt[c];
58    }
59    void init(){
60        while(top){
61            mem[--top].pos.clear();
62        }
63        root = new_node(0);
64        ed = root;
65    }
66    void push(char *s){
67        for(int i=0;s[i];i++) push(s[i]-32);
68    }
69    long long count(){
70        long long ans=0;
71        for(int i=1;i<top;i++){
72            ans+=mem[i].len-mem[i].pre->len;
73        }
74        return ans;
75    }
76 }sam;
77 char S[N];
78 int main(){
79     int T;
80     scanf("%d",&T);
81     while(T--){
82         scanf("%s",S);
83         sam.build(S);
84         printf("%lld\n",sam.count());
85     }
86     return 0;
87 }
```

## 9.6 Z Algorithm

```
1 void Zalg(char *s, int *z, int n) {
2     z[0]=n;
3     for(int L=0, R=0, i=1; i<n; i++) {
4         if(i<=R && z[i-L]<=R-i) z[i]=z[i-L];
5         else {
6             L=i;
7             if(i>R) R=i;
8             while(R<n && s[R-L]==s[R]) R++;
9             z[i]=(R--)-L;
10        }
11    }
12 }
```

## 10 無權邊的生成樹個數 Kirchhoff's Theorem

1. 定義  $n \times m$  矩陣  $E = (a_{i,j})$ ， $n$  為點數， $m$  為邊數，若  $i$  點在  $j$  邊上， $i$  為小點  
 $a_{i,j} = 1$ ， $i$  為大點  $a_{i,j} = -1$ ，否則  $a_{i,j} = 0$ 。

(證明省略)

4. 令  $E(E^T) = Q$ ，他是一種有負號的 kirchhoff 的矩陣，取  $Q$  的子矩陣即為  $F(F^T)$

結論：做  $Q$  取子矩陣算 det 即為所求。(除去第一行第一列 by mz)

## 11 monge

$$i \leq i' < j \leq j'$$

$$m(i, j) + m(i', j') \leq m(i', j) + m(i, j')$$

$$k(i, j - 1) \leq k(i, j) \leq k(i + 1, j)$$

## 12 四心

$$\frac{sa \cdot A + sb \cdot B + sc \cdot C}{sa + sb + sc}$$

外心  $\sin 2A : \sin 2B : \sin 2C$

內心  $\sin A : \sin B : \sin C$

垂心  $\tan A : \tan B : \tan C$

重心  $1 : 1 : 1$

## 13 Runge-Kutta

$$y_{n+1} = y_n + \frac{h}{6}(k_1 + 2k_2 + 2k_3 + k_4)$$

$$k_1 = f(t_n, y_n)$$

$$k_2 = f(t_n + \frac{h}{2}, y_n + \frac{h}{2}k_1)$$

$$k_3 = f(t_n + \frac{h}{2}, y_n + \frac{h}{2}k_2)$$

$$k_4 = f(t_n + h, y_n + hk_3)$$

## 14 Householder Matrix

$$I - 2 \frac{vv^T}{v^T v}$$