NCTU_Yggdarsill

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Building Environment

1.1 C++11

1.2 Default

```
1 #define F(n) Fi(i,n)
2 #define Fi(i,n) Fl(i,0,n)
3 #define Fl(i,l,n) for(int i=(l);i<(int)(n);++i)
4 #include <bits/stdc++.h>
5 #include <bits/extc++.h>
6 // #include <ext/pb_ds/assoc_container.hpp>
7 // #include <ext/pb_ds/priority_queue.hpp>
8 using namespace std;
9 using namespace __gnu_pbds;
10 const double PI = acos(-1);
11 main() {
12  ios_base::sync_with_stdio(false);
13  cin.tie(NULL);
```

```
14 cout << fixed << setprecision(7) << PI << endl;
15 }
```

1.3 Preferences

```
1 {
2    "color_scheme": "Packages/Color Scheme - Default/Monokai Bright.tmTheme",
3    // "font_face": "Courier New", // Uncomment if defaults is proportional.
4    "font_size": 18
5 }
```

1.4 Print File

```
import sublime, sublime_plugin
import os

class print_file(sublime_plugin.TextCommand):

def run(self, edit):
    os.system('cat -n "%s" > tmp.print; lpr tmp.print' % self.view.file_name
    ())
self.view.show_popup("JIZZ!!")
```

1.5 Vimrc

2 Convolution

2.1 FFT

```
1 #ifndef SUNMOON_FFT
2 #define SUNMOON_FFT
3 #include<vector>
4 #include<complex>
5 #include<algorithm>
6 template<typename T, typename VT=std::vector<std::complex<T>>>
7 struct FFT{
8 const T pi;
```

```
FFT(const T pi=acos((T)-1)):pi(pi){}
     inline unsigned int bit reverse (unsigned int a, int len) {
       a = ((a\&0x55555555U) << 1) | ((a\&0xAAAAAAAAU) >> 1);
12
       a = ((a\&0x33333333U) << 2) | ((a\&0xCCCCCCCU) >> 2);
13
       a = ((a\&0x0F0F0F0FU) << 4) | ((a\&0xF0F0F0F0U) >> 4);
14
       a = ((a\&0x00FF00FFU) << 8) | ((a\&0xFF00FF00U) >> 8);
       a = ((a\&0x0000FFFFU) << 16) | ((a\&0xFFFF0000U) >> 16);
16
       return a>>(32-len);
17
18
     inline void fft(bool is inv, VT &in, VT &out, int N) {
       int bitlen=std:: lg(N), num=is inv?-1:1;
19
       for(int i=0;i<N;++i)out[bit reverse(i,bitlen)]=in[i];</pre>
21
       for(int step=2;step<=N;step<<=1){</pre>
         const int mh=step>>1;
23
         for (int i=0; i < mh; ++i) {</pre>
24
            std::complex<T> wi=exp(std::complex<T>(0,i*num*pi/mh));
            for(int j=i;j<N;j+=step){</pre>
26
              int k=j+mh;
27
              std::complex<T> u=out[j],t=wi*out[k];
28
              out[i]=u+t;
              out [k]=u-t;
29
       if (is inv) for (int i=0; i<N; ++i) out[i] /=N;</pre>
34 }
35 };
36 #endif
```

3 Geometry

3.1 Geometry

```
1 const double eps = 1e-10;
 2 const double INF = 1.0/0.0;
 3 const double SIDE = 10000;
 4 const double PI = acos(-1.0);
 5 \text{ const int MAXN} = 500000 + 10;
 6 struct PT{
      double x, y;
 8
       PT(){}
       PT (double x, double y):x(x), y(y) {}
       PT operator + (const PT& p)const{
           return PT(x+p.x,y+p.y);
12
13
       PT operator - (const PT& p)const{
14
           return PT(x-p.x,y-p.y);
15
16
       PT operator * (double c)const{
17
           return PT(x*c,y*c);
18
19
       PT operator / (double c)const{
```

```
return PT(x/c,y/c);
21
     PT rot(double a) const{return PT(x*cos(a)-y*sin(a),x*sin(a)+y*cos(a));}
23
      double operator *(const PT& p)const{
24
           return x*p.x+y*p.y;
25
26
      double operator ^(const PT& p)const{
27
           return x*p.y-y*p.x;
28
29
      bool operator == (const PT& p) const{
           return fabs(x-p.x)<eps&&fabs(y-p.y)<eps;
    double len2()const{return x*x+y*y;}
32
     double len()const{return sqrt(len2());}
34 }poi[MAXN], stk[MAXN];
35 struct LINE{
      PT a,b;
36
37
      double angle;
38
      LINE(){}
      LINE(PT a, PT b):a(a),b(b),angle(atan2(b.y-a.y, b.x-a.x)){}
40 }line[MAXN],deq[MAXN];
41 int top;
42 inline int ori(const PT& p1, const PT& p2, const PT& p3) {
      double a=(p2-p1)^(p3-p1);
      if (a>-eps&&a<eps) return 0;
44
45
      return a>0 ? 1:-1;
46 }
47 inline bool btw(const PT& p1,const PT& p2,const PT& p3) {
       return (p2-p1) * (p3-p1) < eps;
49 }
50 //segment intersection
51 inline bool intersection(const PT& p1,const PT& p2,const PT& p3,const PT& p4)
52
      int a123=ori(p1,p2,p3);
53
      int a124=ori(p1,p2,p4);
54
      int a341=ori(p3,p4,p1);
55
      int a342=ori(p3,p4,p2);
56
      if (a123==0&&a124==0) return btw(p1,p3,p4) | |btw(p2,p3,p4) | |btw(p3,p1,p2) | |
      btw(p4,p1,p2);
57
      return a123*a124 <= 0 && a341*a342 <= 0;
58 }
59 inline PT intersectionPoint(const PT& p1,const PT& p2,const PT& p3,const PT&
       p4){
60
      double a123=(p2-p1)^(p3-p1);
61
       double a124=(p2-p1)^(p4-p1);
62
       return (p4*a123-p3*a124) / (a123-a124);
63 }
64 //line intersection
65 inline PT intersectionPoint(const LINE& 11,const LINE& 12) {
66
      PT p1=11.a,p2=11.b,p3=12.a,p4=12.b;
67
      double a123=(p2-p1)^(p3-p1);
68
       double a124=(p2-p1)^(p4-p1);
69
       return (p4*a123-p3*a124)/(a123-a124);
70 }
71 PT foot(const LINE& 1, const PT& p) {
72 PT m(l.b.y-l.a.y, l.a.x-l.b.x);
```

```
73 return p+m*(l.a-p ^ l.b-p)/((l.b-l.a).len2());
 74 }
 75 PT mirror(const LINE& l,const PT& p) {
 76 PT m(l.b.y-l.a.y,l.a.x-l.b.x);
 77 return p+m*(l.a-p ^ l.b-p)/((l.b-l.a).len2())*2;
 78 }
 79 //segment-point distance
 80 inline double sp dis(PT a, PT 11, PT 12) {
       if((a-11)*(12-11)<0) return (11-a).len();
 82 else if((a-12)*(11-12)<0) return (12-a).len();
 83
        return fabs(11-a^12-a)/((12-11).len());
 84 }
 8.5
 86 struct cir{
        point c;
        double r:
 89 }0[10];
 90 double out ang(cir a,cir b) { //a.c+(b.c-a.c).unit().rot(ang)*b.r
        return acos((a.r-b.r)/(a.c-b.c).len());
 92 }
 93 double in ang(cir a,cir b) {
        return acos((a.r+b.r)/(a.c-b.c).len());
 94
 95 }
 96 int main() {
 97 double tmp, sum;
 98 if(fabs(o[i].r-o[j].r)<(o[j].c-o[i].c).len()){
 99
      tmp = out ang(o[i],o[j]);
100
     sum = ang add(cl,tmp);
101
        pi=o[i].c+point(o[i].r*cos(sum),o[i].r*sin(sum));
102
        pj=o[j].c+point(o[j].r*cos(sum),o[j].r*sin(sum));
       sum = ang add(cl,-tmp);
104
        pi=o[i].c+point(o[i].r*cos(sum),o[i].r*sin(sum));
105
       pj=o[j].c+point(o[j].r*cos(sum),o[j].r*sin(sum));
106
107
      if(o[i].r+o[j].r<(o[j].c-o[i].c).len()){</pre>
108
      tmp = in ang(o[i],o[j]);
109
      sum = ang add(cl,tmp);
110
      pi=o[i].c+point(o[i].r*cos(sum),o[i].r*sin(sum));
111
       pj=o[j].c-point(o[j].r*cos(sum),o[j].r*sin(sum));
112
       sum = ang add(cl,-tmp);
113
        pi=o[i].c+point(o[i].r*cos(sum),o[i].r*sin(sum));
114
        pj=o[j].c-point(o[j].r*cos(sum),o[j].r*sin(sum));
115
116 }
1117
118 inline double dist(const PT& p1, const PT& p2) {
119
        return sqrt((p2-p1)*(p2-p1));
120 }
121 inline double tri(const PT& p1, const PT& p2, const PT& p3) {
122
        return fabs((p2-p1)^(p3-p1));
123 }
124 inline double getPerimeter(){
125
       double res=0.0;
126
       poi[top++]=poi[0];
       for (int i=0;i<top-1;i++) res+=dist(poi[i],poi[i+1]);</pre>
128
        return res;
```

```
129 }
130 inline double getarea(){
        double res=0.0;
        for (int i=1;i<top-1;i++) res+=tri(poi[0],poi[i],poi[i+1]);</pre>
        return 0.5*res;
134 }
136 //convex hull
137 inline bool cmp convex(const PT &a, const PT &b) {
138
        if(a.x!=b.x)return a.x<b.x;</pre>
139
        return a.y<b.y;</pre>
140 }
141 inline void convex hull(PT a[], int &n){
142
        top=0;
143
        sort(a,a+n,cmp convex);
144
        for (int i=0; i < n; i++) {</pre>
145
             while (top>=2&&ori(stk[top-2],stk[top-1],a[i])>=0)top--;
146
            stk[top++]=a[i];
147
148
        for (int i=n-2, t=top+1; i>=0; i--) {
149
            while (top \ge t\& \& ori(stk[top-2], stk[top-1], a[i]) \ge 0) top--;
             stk[top++]=a[i];
        }
        top--;
        for (int i=0;i<top;i++)poi[i]=stk[i];</pre>
154 }
155 //half plane intersection
156 inline bool cmp half plane(const LINE &a,const LINE &b){
        if(fabs(a.angle-b.angle)<eps)return ori(a.a,a.b,b.a)<0;</pre>
158
        return a.angle > b.angle;
159 }
160 inline void half plane intersection (LINE a[], int &n) {
        int m=1,front=0,rear=1;
        sort(a,a+n,cmp half plane);
163
        for(int i=1;i<n;i++){</pre>
164
             if(fabs(a[i].angle-a[m-1].angle)>eps)a[m++]=a[i];
166
        deq[0]=a[0], deq[1]=a[1];
167
        for(int i=2;i<m;i++){</pre>
168
            while (front<rear&&ori(a[i].a,a[i].b,intersectionPoint(deq[rear],deq[</pre>
        rear-1]))<0)rear--;
169
            while(front<rear&&ori(a[i].a,a[i].b,intersectionPoint(deg[front],deg[</pre>
        front+1]))<0)front++;
            deq[++rear]=a[i];
171
      while (front<rear&&ori(deq[front].a, deq[front].b, intersectionPoint(deq[rear
        ], deg[rear-1]))<0)rear--;
173
        while (front < rear & & ori (deg[rear].a, deg[rear].b, intersection Point (deg[front
        ], deq[front+1]))<0) front++;
174
        if (front==rear) return;
175
176
        top=0;
177
        for(int i=front;i<rear;i++)poi[top++]=intersectionPoint(deg[i],deg[i+1]);</pre>
178
        if (rear>front+1)poi[top++]=intersectionPoint(deq[front], deq[rear]);
179 }
180
```

```
181
182
183
184 //smallest cover rectangle
185 double ans1, ans2;
186 void rotating calipers(){
187
         ans1=ans2=INF;
188
        int j=1, k=1, l=1;
189
         poi[top]=poi[0];
190
         for (int i=0; i < top; i++) {</pre>
191
             while(tri(poi[i],poi[i+1],poi[j])<tri(poi[i],poi[i+1],poi[j+1])) j=(j</pre>
         +1)%top;
192
             while (((poi[i+1]-poi[i])*(poi[k+1]-poi[k]))>eps)k=(k+1)%top;
193
             if(i==0) l=(k+1) %top;
194
             while (((poi[i+1]-poi[i])*(poi[l+1]-poi[l]))<-eps)l=(l+1)%top;</pre>
195
             double tmp1 = tri(poi[i],poi[i+1],poi[j])/dist(poi[i],poi[i+1]);
196
             double tmp2 = (((poi[k]-poi[i])*(poi[i+1]-poi[i]))-((poi[l]-poi[i])*(
         poi[i+1]-poi[i])))/dist(poi[i],poi[i+1]);
197
             if ((tmp1+tmp2) *2.0<ans1) ans1=(tmp1+tmp2) *2.0;
198
             if (tmp1*tmp2<ans2) ans2=tmp1*tmp2;</pre>
199
200 }
201 int main() {
202
        int n.m;
203
         while (~scanf ("%d", &n) &&n) {
204
             for (int i=0;i<n;i++) scanf ("%lf%lf", &poi[i].x, &poi[i].y);</pre>
205
             convex hull (poi, n);
206
             rotating calipers();
207
             printf("%.2f %.2f\n",ans2,ans1);
208
209 }
210
211 inline bool online (const LINE &L, const PT &p) {
         return ori(p, L.a, L.b) == 0 & & btw(p, L.a, L.b);
213 }
214 inline bool on convex(const PT& p) {
215
         for (int i=0; i < top; i++)</pre>
216
             if(p==poi[i])return 1;
217
         poi[top]=poi[0];
218
         for(int i=0;i<top;i++) {</pre>
 219
             line[i].a=poi[i];
             line[i].b=poi[i+1];
         for(int i=0;i<top;i++)</pre>
             if (online(line[i],p))return 1;
 224
         return 0;
 225 }
226 //originally in long long, should be modified
227 bool in simple polygon(PT b[], int k) {
228 bool flag=false;
229
      for(int j=0;j<k;j++){</pre>
         if(((p-b[j])^{p-b[(j+1)%k])) ==0\&\&(p-b[j])*(p-b[(j+1)%k])<=0){
           flag=true;
232
           break;
233
234
         if((b[j].y<p.y)^(b[(j+1)%k].y<p.y)){
```

```
235    long long xss=(b[j]-p)^(b[(j+1)%k]-p);
236    if((xss<0)^(b[j].y<b[(j+1)%k].y)){
237       flag^=1;
238    }
239    }
240    }
241    return flag;
242 }</pre>
```

3.2 MinimumCoveringCircle

```
1 inline point oc(const point& pa, const point& pb, const point& pc) {
    double a, b, c, d, e, f, delta, dx, dy;
   // ax + bv = c
   // dx + ey = f
    a = pa.x - pb.x;
    b = pa.y - pb.y;
    c = a*(pa.x+pb.x)/2 + b*(pa.y+pb.y)/2;
    d = pa.x - pc.x;
    e = pa.y - pc.y;
   f = d*(pa.x+pc.x)/2 + e*(pa.y+pc.y)/2;
    delta = a*e-b*d;
    dx = c*e-f*b;
13
    dy = a*f-d*c;
14
    return point (dx/delta, dy/delta);
15 }
16 inline point enc(const point& a, const point& b, const point& c) {
    vector<point> tmp;
    tmp.clear();tmp.push back(a);tmp.push back(b);tmp.push back(c);
    point O = tmp[0];
   double r = 0;
   Fl(i, 1, 3) if (dq(0, tmp[i]) - r > eps) {
22
      0 = tmp[i], r = 0;
     Fi(j, i) if (dq(0, tmp[j]) - r > eps) {
24
       0 = point((tmp[i].x+tmp[j].x)/2, (tmp[i].y+tmp[j].y)/2);
25
        r = dq(0, tmp[j]);
26
        Fi(k, j) if (dq(0, tmp[k]) - r > eps)
27
          O = oc(tmp[i], tmp[j], tmp[k]), r = dq(O, tmp[k]);
28
29
    return 0;
31 }
```

4 GNU Black Magic

4.1 Black Magic

```
1 #include<ext/rope>
2 using namespace std;
```

```
3 using namespace gnu cxx;
 4 \text{ const int MAXN} = 50000 + 10;
 5 crope ro, l[MAXN], tmp;
 6 char str[200+10];
 7 main(){
       int T, op, p, c, d=0, cnt=1, v;
       scanf("%d",&T);
10
       while (T--) {
           scanf("%d", &op);
12
           if (op==1) {
                scanf("%d%s", &p, str);
14
               p-=d;
15
                ro.insert(p,str);
16
               l[cnt++]=ro;
17
18
           else if(op==2){
19
                scanf ("%d%d", &p, &c);
20
                p-=d, c-=d;
               ro.erase(p-1,c);
                l[cnt++]=ro;
23
24
           else{
25
                scanf("%d%d%d",&v,&p,&c);
26
                p-=d, v-=d, c-=d;
27
                tmp=l[v].substr(p-1,c);
28
                d+=count(tmp.begin(),tmp.end(),'c');
29
                cout<<tmp<<endl;
32 }
33 #include <bits / extc++.h>
34 using namespace std;
35 using namespace gnu pbds;
36 gnu pbds::priority queue<int> h1,h2;
37 typedef tree<int, null type, less<int>, rb tree tag,
       tree order statistics node update> set t;
38
39 int main() {
       printf("heap:\n");
41
       for (int i=1;i<=10;i+=2)h1.push(i);
42
       for(int i=2;i<=10;i+=2)h2.push(i);</pre>
43
44
       printf("%d\n", h1.top());
45
       printf("%d\n", h2.top());
46
       h1.join(h2);
47
       printf("%d\n",h1.size());
48
       printf("%d\n",h2.size());
49
       printf("%d\n",h1.top());
50
51
       printf("\ntree:\n");
52
       set t s;
53
       for(int i=0;i<5;i++)s.insert(10*i);</pre>
54
       printf("%d\n", *s.find by order(0));
55
       printf("%d\n",*s.find by order(3));
56
       printf("%d\n", s.find by order(5) == s.end());
57
```

```
58     printf("%d\n",s.order_of_key(0));
59     printf("%d\n",s.order_of_key(30));
60     printf("%d\n",s.order_of_key(35));
61     printf("%d\n",s.order_of_key(100));
62     return 0;
63 }
```

4.2 GNU Bitwise Operation

```
1 int builtin ffs (unsigned int x)
2 int builtin ffsl (unsigned long)
3 int builtin ffsll (unsigned long long)
4 // 返回右起第一個1的位置
5 // Returns one plus the index of the least significant 1-bit of x, or if x is
       zero, returns zero.
6
7 int builtin clz (unsigned int x)
8 int builtin clzl (unsigned long)
9 int builtin clzll (unsigned long long)
10 // 返回左起第一個1之前0的個數
11 // Returns the number of leading 0-bits in x, starting at the most
      significant bit position. If x is 0, the result is undefined.
13 int builtin ctz (unsigned int x)
14 int builtin ctzl (unsigned long)
15 int builtin ctzll (unsigned long long)
16 // 返回右起第一個1之後的0的個數
17 // Returns the number of trailing 0-bits in x, starting at the least
      significant bit position. If x is 0, the result is undefined.
19 int builtin popcount (unsigned int x)
20 int builtin popcountl (unsigned long)
21 int builtin popcountll (unsigned long long)
22 // 返回1的個數
23 // Returns the number of 1-bits in x.
25 int builtin parity (unsigned int x)
26 int builtin parityl (unsigned long)
27 int builtin parityll (unsigned long long)
28 // 返回1的個數的奇偶性(1的個數 mod 2的值)
29 // Returns the parity of x, i.e. the number of 1-bits in x modulo 2.
```

5 Graph

5.1 BCC

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int MAXN = 10000;
```

```
4 vector <int> adja[MAXN];
 5 int gcnt, top, timeStamp, dfn[MAXN], low[MAXN], depth[MAXN];
 6 pair<int, int> stk[MAXN],ans[MAXN];
 7 set <int> group[MAXN];
8 bool cut[MAXN];
9 void BCC(int now, int nextv) {
      int sf, st;
       group[gcnt].clear();
12
       do{
13
           sf = stk[top-1].first, st = stk[top-1].second;
14
           group[gcnt].insert(sf);
           group[gcnt].insert(st);
           --top;
16
17
       }while(sf != now || st != nextv);
18
       ++gcnt;
19 }
20 void tarjan(int now, int parent, int d) {
      int child = 0;
       dfn[now] = low[now] = ++timeStamp, depth[now] = d;
       for (int i = 0; i < adja[now].size(); i++) {
24
           int nextv = adja[now][i];
           if(nextv == parent) continue;
26
           if(dfn[nextv] == 0){
27
               stk[top++] = make pair(now, nextv);
28
               tarjan(nextv, now, d+1);
29
               low[now] = min(low[now], low[nextv]);
               ++child;
               if ((parent !=-1 \&\& low[nextv] >= dfn[now]) || (parent :=-1 \&\&
       child >= 2)){
                   cut[now] = true;
                   if (parent != -1) BCC (now, nextv);
34
               if(parent == -1) BCC(now, nextv);
36
37
           else if(depth[nextv] < depth[now]-1){</pre>
38
               stk[top++] = make pair(now, nextv);
39
               low[now] = min(low[now], dfn[nextv]);
40
41
42 }
43 int main() {
      int n, m, x, y, cnt=0;
45
       while (~scanf ("%d", &n)) {
46
           cnt=timeStamp=top=gcnt=0;
47
           memset(cut, 0, sizeof(cut));
48
           memset(dfn, 0, sizeof(dfn));
49
           for(int i=0;i<n;i++)adja[i].clear();</pre>
50
           for(int i=0;i<n;i++) {</pre>
51
               scanf("%d ",&x);
52
               scanf("(%d)",&m);
53
               while (m--) {
54
                   scanf("%d",&v);
55
                   adja[x].push back(y);
56
               }
57
58
           for (int i=0; i < n; i++)</pre>
```

```
if(dfn[i]==0)tarjan(i, -1, 1);
for(int i=0;i<gcnt;i++){
    if(group[i].size()==2){
        //critical links
    }
}
</pre>
```

5.2 MST Directed

```
1 #include<cstdio>
2 #include<vector>
3 #include<algorithm>
4 #define N 100100
5 using namespace std;
6 struct edge{
7 edge(){}
8 edge(int f,int d):f(f),d(d){}
9 int f;
10 int d;
    bool operator<(const edge &rhs)const{return d<rhs.d;}</pre>
12 };
13 struct node{
14 int sz, v, now;
15 node *1, *r;
void pull() \{sz=1+(1?1->sz:0)+(r?r->sz:0);\}
17 }pq[N];
18 int pa[N], sub[N], stk[N], top;
19 bool vis[N], instk[N];
20 vector<edge> rg[N];
21 void init(int n) {
22 for (int i=0; i<n; i++) {
23 pa[i]=i;
    sub[i]=0;
    pq[i].l=pq[i].r=NULL;
26
    pq[i].sz=1;
      pq[i].v=i;
27
28
      pg[i].now=0;
29 }
30 }
31 int find(int x){
32 if(pa[x]==x) return x;
33 int y=find(pa[x]);
34 if(pa[x]!=y) sub[x]+=sub[pa[x]],pa[x]=y;
35 return pa[x];
36 }
37 inline int get sub(int x){
38 if(x==find(x)) return sub[x];
39 else return sub[x]+sub[pa[x]];
40 }
41 inline int get cost(const node& a) {
42 return rg[a.v][a.now].d-get sub(a.v);
43 }
```

```
44 bool cmp(const node& a, const node& b) {
45 return get cost(a) < get cost(b);
47 node* merge(node *a, node *b) {
48 if(!a||!b) return a?a:b;
49 if (cmp(*b, *a)) swap(a,b);
a \rightarrow r = merge(a \rightarrow r, b);
if ((a->1?a->1->sz:0)<(a->r?a->r->sz:0)) swap(a->1,a->r);
52 a.pull();
53 return a;
54 }
55 int min cost arborescence (int r, int n) {
56 vis[r]=true;
57 int res=0;
58 for(int i=0;i<n;i++){
    if(!vis[i]){
60
   top=0;
61
    int u=i;
        while(!vis[u]){
62
63
64
65
66 }
67 }
68 int main() {
69 int n,m,r,x,y,w;
70 scanf("%d%d%d", &n, &m, &r);
71 for(int i=0;i<m;i++){
    scanf("%d%d%d",&x,&y,&w);
73
     rg[y].push back(edge(x,w));
74
      sort()
75 }
76 }
```

5.3 SCC

```
1 #include <cstdlib>
2 #include <iostream>
3 #include <vector>
4 #include <queue>
5 #define N 300002
6 using namespace std;
7 vector<int>go[N],back[N],tree[N];
8 int hu[N],ST[N],st=0,scc[N],scCo[N],scmx[N];
9 bool wed[N];
10 int DFS go(int now) {
11 //cout<<now<<" DFS ";
      wed[now]=true;
13
      for(int i=0;i<go[now].size();i++){</pre>
14
          if(!wed[qo[now][i]])
15
               DFS go(go[now][i]);
16
17
      ST[st++]=now;
18
       return 0;
```

```
19 }
20 int DFS back(int now, int id) {
21
       wed[now]=true;
       scc[now]=id;
23
       int sum=1;
24
       if(now==0)sum=0;
25
       for(int i=0;i<back[now].size();i++){</pre>
26
           if(!wed[back[now][i]])
27
                sum+=DFS back(back[now][i],id);
28
29
       return sum;
30 }
31 int DFS tree(int now)
32 {
       if (scmx[now]!=0) return scmx[now];
34
       int mx=0,tmp;
35
       for(int i=0;i<tree[now].size();i++){</pre>
36
           tmp=DFS tree(tree[now][i]);
37
           mx=(mx>tmp)? mx:tmp;
38
39
       scmx[now] = mx + scCo[now];
40
       return mx+scCo[now];
41 }
42 int main(int argc,char *argv[])
43 {
44
       ios base::sync with stdio(false);
45
       int n, k;
46
       char c;
47
       cin>>n>>k>>hu[1];
48
       go[0].push back(1);
49
       back[1].push back(0);
       for(int i=2;i<=n;i++) {</pre>
51
           cin>>hu[i];
52
           if (hu[i]>=hu[i-1]) {
53
                go[i].push back(i-1);
54
                back[i-1].push back(i);
55
56
           if (hu[i-1]>=hu[i]) {
57
                go[i-1].push back(i);
               back[i].push back(i-1);
58
59
           go[0].push back(i);
61
           back[i].push back(0);
62
63
       for (int i=1;i<=n;i++) {</pre>
64
           cin>>c;
65
           if (c=='T') {
66
                go[i].push back(0);
67
                back[0].push back(i);
68
69
       for(int i=0;i<=n;i++)</pre>
71
           if(!wed[i])DFS go(i);
72
       //cout<<endl;
73
       fill((bool*)wed,(bool*)wed+N,false);
74
       int tsc=0;
```

```
// for(int i=0;i<st;i++)cout<<ST[i]<<" HH ";
76
       // cout<<endl;
77
      while(st!=0)
78
           if(!wed[ST[--st]]){
79
               scCo[tsc]=DFS back(ST[st],tsc);
80
               tsc++;
81
       // for(int i=0;i<N;i++)</pre>
              while(!back[i].empty())back[i].pop back();
83
84
       for (int i=0;i<=n;i++)</pre>
85
           for(int j=0;j<go[i].size();j++){</pre>
86
               if(scc[i]!=scc[go[i][j]]){
87
                   tree[scc[i]].push back(scc[go[i][j]]);
88
89
       // for (int i=0;i<=n;i++) cout<<scc[i]<<" BB ";
91
      // cout<<endl;
     // for(int i=0;i<tsc;i++)cout<<scCo[i]<<" GG ";
      cout<<DFS tree(scc[k])<<endl;</pre>
93
      //system("pause");
95
       return 0;
96 }
```

6 Matching

6.1 Bipartite Matching

```
1 #include <bits/stdc++.h>
2 #define V 20100
3 #define inf 0x3f3f3f3f
4 int mx[V],my[V],dis[V],que[V];
5 bool vis[V];
6 vector<int> q[V];
7 bool DFS(int u) {
8 vis[u]=true;
9 for(int i=0;i<g[u].size();i++){</pre>
      int v=mv[q[u][i]];
     if (v==-1||!vis[v]&&dis[v]==dis[u]+1&&DFS(v)) {
11
        mx[u]=g[u][i];
13
        my[g[u][i]]=u;
14
        return true;
15
16 }
17 return false;
18 }
19 // n is the size of left hand side
20 int Hopcroft Karp(int n) {
int matching=0,qt,qf,sp,i,u,v;
22 bool flag=true;
23 memset(mx, -1, sizeof(mx));
   memset(my,-1,sizeof(my));
    while(flag) {
```

```
flag=false;
26
27
       qt=qf=0;
28
       sp=inf;
29
       for (i=0; i < n; i++) {</pre>
        if(mx[i] == -1){
           dis[i]=0;
            que [qt++]=i;
34
         else dis[i]=inf;
35
36
       while(qf<qt){</pre>
         u=que[qf++];
38
         if(dis[u]>=sp) continue;
39
         for (i=0; i < g[u].size(); i++) {</pre>
40
           v=my[q[u][i]];
41
           if(v==-1){
42
              if (dis[u]+1<sp) {
43
                sp=dis[u]+1;
44
                flag=true;
45
46
47
            else if(dis[u]+1<dis[v]){</pre>
48
              dis[v]=dis[u]+1;
49
              que [qt++]=v;
51
       if(flag){
54
         memset(vis, 0, sizeof(vis));
55
         for(i=0;i<n;i++){
56
            if (dis[i] == 0 & & DFS(i)) matching++;
57
58
59
60
     return matching;
61 }
```

6.2 Blossom

```
1 int V;
2 bool adj[MAXN][MAXN];
3 int w[MAXN][MAXN];
4 int p[MAXN];
5 int m[MAXN];
6 int d[MAXN];
7 int c1[MAXN], c2[MAXN];
8 int q[MAXN], *qf, *qb;
9 int pp[MAXN];
10 int f(int x) {return x == pp[x] ? x : (pp[x] = f(pp[x]));}
11 void u(int x, int y) \{pp[x] = y;\}
12 int v[MAXN];
13 void path(int r, int x) {
      if (r == x) return;
15
      if (d[x] == 0) {
```

```
16
           path(r, p[p[x]]);
17
           int i = p[x], j = p[p[x]];
18
           m[i] = j; m[j] = i;
19
20
      else if (d[x] == 1){
           path(m[x], c1[x]);
22
           path(r, c2[x]);
23
           int i = c1[x], j = c2[x];
24
           m[i] = j; m[j] = i;
25
26 }
27 int lca(int x, int y, int r) {
      int i = f(x), j = f(y);
29
      while (i != j && v[i] != 2 && v[j] != 1) {
          v[i] = 1; v[j] = 2;
           if (i != r) i = f(p[i]);
           if (j != r) j = f(p[j]);
34
      int b = i, z = j; if (v[j] == 1) swap(b, z);
      for (i = b; i != z; i = f(p[i])) v[i] = -1;
36
      v[z] = -1;
37
       return b;
38 }
39 void contract one side(int x, int y, int b) {
       for (int i = f(x); i != b; i = f(p[i])) {
41
           u(i, b);
42
           if (d[i] == 1) c1[i] = x, c2[i] = y, *qb++ = i;
43
44 }
45 bool BFS(int r) {
      for (int i=0; i<V; ++i) pp[i] = i;
47
      memset(v, -1, sizeof(v));
48
      memset(d, -1, sizeof(d));
49
      d[r] = 0;
       qf = qb = q;
51
       *qb++ = r;
52
       while (qf < qb)</pre>
53
           for (int x=*qf++, y=0; y<V; ++y)</pre>
54
               if (adj[x][y] \&\& m[y] != y \&\& f(x) != f(y))
55
                   if (d[y] == -1)
56
                       if (m[y] == -1) {
57
                            path(r, x);
58
                            m[x] = y; m[y] = x;
59
                            return true;
60
61
                        else{
62
                            p[y] = x; p[m[y]] = y;
63
                            d[y] = 1; d[m[y]] = 0;
64
                            *qb++ = m[y];
65
66
                   else
67
                        if (d[f(y)] == 0) {
68
                            int b = lca(x, y, r);
69
                            contract one side(x, y, b);
                            contract one side(y, x, b);
```

```
72
        return false;
 73 }
 74 int match result(){
        int res=0;
 76
        memset(m,-1,sizeof(m));
        for(int i=0;i<V;i++){</pre>
 78
            if(m[i] == -1){
 79
                 if(BFS(i))res++;
 80
                 else m[i]=i;
 81
 82
 83
        return res;
 84 }
 85 int num[10000 + 10], top;
 86 int main() {
 87
        int T, Case=0, n;
 88
        scanf("%d",&T);
 89
        while (T--) {
 90
            scanf("%d", &n);
 91
            V = (1 << n);
 92
            top=0;
 93
            for (int i=0; i < V; i++) {</pre>
 94
                 for(int j=i+1;j<V;j++){</pre>
 95
                     scanf("%d", &w[i][j]);
 96
                     num[top++]=w[i][j];
 97
 98
 99
            sort(num, num+top);
            top = (unique(num, num+top) -num);
            int l=0, r=top-1, mid;
            while(r>1) {
                 mid=(1+r+1)/2;
104
                 memset(adj,false,sizeof(adj));
                 for(int i=0;i<V;i++){</pre>
106
                     for(int j=i+1;j<V;j++) {</pre>
                          if (w[i][j]>=num[mid])adj[i][j]=adj[j][i]=true;
108
109
                 int res=match result();
                 if(res==V/2)l=mid;
                 else r=mid-1;
114
             printf("Case %d: %d\n",++Case,num[1]);
115
116 }
```

6.3 Dinic

```
1 //Dinic
2 #define V 1000
3 struct edge{
4    edge(){}
5    edge(int a,int b,int c):to(a),cap(b),rev(c){}
6    int to,cap,rev;
```

```
7 };
 8 vector<edge> g[V];
9 int level[V];
10 int iter[V];
11 void add edge(int from,int to,int cap) {
       g[from].push back(edge(to,cap,g[to].size()));
13
       q[to].push back(edge(from, 0, q[from].size()-1));
14 }
15 void bfs(int s){
       memset(level, -1, sizeof(level));
       queue<int>que;
18
     level[s]=0;
19
       que.push(s);
       while(!que.empty()){
21
          int v=que.front();
22
           que.pop();
           for(int q=0;q<g[v].size();q++){</pre>
24
               edge &e=q[v][q];
               if (e.cap>0&&level[e.to]<0) {
26
                   level[e.to]=level[v]+1;
                    que.push(e.to);
28
29
31 }
32 int dfs(int v,int t,int f) {
      if (v==t) return f;
34
       for(int &q=iter[v];q<q[v].size();++q){</pre>
           edge &e=q[v][q];
36
           if (e.cap>0&&level[v]<level[e.to]) {</pre>
               int d=dfs(e.to,t,min(f,e.cap));
38
               if(d>0){
39
                   e.cap-=d;
                   g[e.to][e.rev].cap+=d;
40
41
                   return d;
42
43
44
45
       return 0;
46 }
47 int max flow(int s, int t) {
     int flow=0;
49
       for(;;){
           bfs(s);
51
           if(level[t]<0)return flow;</pre>
52
           memset(iter, 0, sizeof(iter));
53
           int f;
54
           while((f=dfs(s,t,1e9))>0)
55
                 flow+=f;
56
57 }
```

6.4 General Weighted Matching

```
1 #include <iostream>
 2 #include <cstdio>
 3 #include <algorithm>
 4 #include <vector>
 5 using namespace std;
 7 typedef long long s64;
 9 const int INF = 2147483647;
11 const int MaxN = 400;
12 const int MaxM = 79800;
14 template <class T>
15 inline void tension (T &a, const T &b)
16 {
17 if (b < a)
18
      a = b;
19 }
20 template <class T>
21 inline void relax(T &a, const T &b)
22 {
23 if (b > a)
24
      a = b;
25 }
26 template <class T>
27 inline int size(const T &a)
28 {
29 return (int)a.size();
30 }
32 inline int getint()
33 {
34 char c;
35 while (c = getchar(), '0' > c \mid \mid c > '9');
36
37 int res = c - '0';
38 while (c = getchar(), '0' <= c && c <= '9')
    res = res * 10 + c - '0';
40 return res;
41 }
42
43 const int MaxNX = MaxN + MaxN;
44
45 struct edge
46 {
47 int v, u, w;
48
49 edge(){}
50 edge (const int & v, const int & u, const int & w)
      : v(v), u(u), w(w){}
52 };
53
55 edge mat[MaxNX + 1][MaxNX + 1];
56
```

```
57 int n matches;
 58 s64 tot weight;
 59 int mate[MaxNX + 1];
 60 int lab[MaxNX + 1];
 62 int q n, q[MaxN];
 63 int fa[MaxNX + 1], col[MaxNX + 1];
 64 int slackv[MaxNX + 1];
 66 int n x;
 67 int bel[MaxNX + 1], blofrom[MaxNX + 1][MaxN + 1];
 68 vector<int> bloch[MaxNX + 1];
 70 inline int e delta(const edge &e) // does not work inside blossoms
 71 {
 72     return lab[e.v] + lab[e.u] - mat[e.v][e.u].w * 2;
 73 }
 74 inline void update slackv(int v, int x)
 76 if (!slackv[x] | | e delta(mat[v][x]) < e delta(mat[slackv[x]][x]))
        slackv[x] = v;
 78 }
 79 inline void calc slackv(int x)
 slackv[x] = 0;
 82 for (int v = 1; v \le n; v++)
     if (mat[v][x].w > 0 \&\& bel[v] != x \&\& col[bel[v]] == 0)
 84
          update slackv(v, x);
 85 }
 87 inline void q push(int x)
 88 {
 89 if (x \le n)
 90 q[q n++] = x;
 91 else
      for (int i = 0; i < size(bloch[x]); i++)
          q push(bloch[x][i]);
 95 }
 96 }
 97 inline void set mate(int xv, int xu)
 99 mate[xv] = mat[xv][xu].u;
100 if (xv > n)
101 {
102
      edge e = mat[xv][xu];
103
     int xr = blofrom[xv][e.v];
104
       int pr = find(bloch[xv].begin(), bloch[xv].end(), xr) - bloch[xv].begin()
105
       if (pr % 2 == 1)
106
107
       reverse(bloch[xv].begin() + 1, bloch[xv].end());
108
         pr = size(bloch[xv]) - pr;
109
        for (int i = 0; i < pr; i++)
```

```
set mate(bloch[xv][i], bloch[xv][i ^ 1]);
113
       set mate(xr, xu);
114
115
       rotate(bloch[xv].begin(), bloch[xv].begin() + pr, bloch[xv].end());
116 }
117 }
118 inline void set bel(int x, int b)
120 bel[x] = b;
121 if (x > n)
122 {
       for (int i = 0; i < size(bloch[x]); i++)
124
         set bel(bloch[x][i], b);
125
126 }
127
128 inline void augment(int xv, int xu)
130 while (true)
131 {
      int xnu = bel[mate[xv]];
     set mate(xv, xu);
134
     if (!xnu)
135
        return;
       set mate(xnu, bel[fa[xnu]]);
       xv = bel[fa[xnu]], xu = xnu;
138 }
139 }
140 inline int get lca(int xv, int xu)
141 {
142 static bool book[MaxNX + 1];
143 for (int x = 1; x \le n x; x++)
      book[x] = false;
145
    while (xv || xu)
146
147
      if (xv)
148
     {
149
       if (book[xv])
         return xv;
       book[xv] = true;
       xv = bel[mate[xv]];
        if (xv)
154
           xv = bel[fa[xv]];
155
156
       swap(xv, xu);
157 }
158
    return 0;
159 }
161 inline void add blossom(int xv, int xa, int xu)
163 int b = n + 1;
164 while (b <= n x && bel[b])
     b++;
166 if (b > n x)
167
       n x++;
```

```
169
     lab[b] = 0;
170
     col[b] = 0;
171
172
     mate[b] = mate[xa];
173
174
     bloch[b].clear();
175
     bloch[b].push back(xa);
176
     for (int x = xv; x != xa; x = bel[fa[bel[mate[x]]]])
177
       bloch[b].push back(x), bloch[b].push back(bel[mate[x]]), q push(bel[mate[
       x]]);
     reverse(bloch[b].begin() + 1, bloch[b].end());
     for (int x = xu; x != xa; x = bel[fa[bel[mate[x]]]])
       bloch[b].push back(x), bloch[b].push back(bel[mate[x]]), q push(bel[mate[
       x]]);
181
182
     set bel(b, b);
183
184 for (int x = 1; x \le n x; x++)
185 {
186
       mat[b][x].w = mat[x][b].w = 0;
187
     blofrom[b][x] = 0;
188 }
190 {
191
     int xs = bloch[b][i];
192
     for (int x = 1; x \le n x; x++)
193
     if (mat[b][x].w == 0 \mid \mid e delta(mat[xs][x]) < e delta(mat[b][x]))
194
           mat[b][x] = mat[xs][x], mat[x][b] = mat[x][xs];
195
      for (int x = 1; x \le n x; x++)
196
        if (blofrom[xs][x])
197
           blofrom[b][x] = xs;
198 }
199 calc slackv(b);
200 }
201 inline void expand_blossom1(int b) // lab[b] == 1
202 {
203 for (int i = 0; i < size(bloch[b]); i++)
204
       set bel(bloch[b][i], bloch[b][i]);
206
     int xr = blofrom[b] [mat[b] [fa[b]].v];
     int pr = find(bloch[b].begin(), bloch[b].end(), xr) - bloch[b].begin();
208
     if (pr % 2 == 1)
209 {
210
      reverse(bloch[b].begin() + 1, bloch[b].end());
       pr = size(bloch[b]) - pr;
212
214 for (int i = 0; i < pr; i += 2)
215 {
216
     int xs = bloch[b][i], xns = bloch[b][i + 1];
     fa[xs] = mat[xns][xs].v;
218
     col[xs] = 1, col[xns] = 0;
219
      slackv[xs] = 0, calc slackv(xns);
       q push (xns);
```

```
col[xr] = 1;
223 fa[xr] = fa[b];
    for (int i = pr + 1; i < size(bloch[b]); i++)</pre>
226
       int xs = bloch[b][i];
       col[xs] = -1;
       calc slackv(xs);
229
231
     bel[b] = 0;
232 }
233 inline void expand blossom final(int b) // at the final stage
234 {
235
     for (int i = 0; i < size(bloch[b]); i++)</pre>
236
       if (bloch[b][i] > n && lab[bloch[b][i]] == 0)
238
         expand blossom final(bloch[b][i]);
239
240
         set bel(bloch[b][i], bloch[b][i]);
241
242
     bel[b] = 0;
243 }
244
245 inline bool on found edge (const edge &e)
246 {
     int xv = bel[e.v], xu = bel[e.u];
248
     if (col[xu] == -1)
249 {
       int nv = bel[mate[xu]];
       fa[xu] = e.v;
       col[xu] = 1, col[nv] = 0;
       slackv[xu] = slackv[nv] = 0;
254
       q push (nv);
255
256
     else if (col[xu] == 0)
258
       int xa = get lca(xv, xu);
259
       if (!xa)
260
         augment(xv, xu), augment(xu, xv);
         for (int b = n + 1; b \le n \times b + +)
          if (bel[b] == b && lab[b] == 0)
264
              expand blossom final(b);
         return true;
266
       else
268
          add blossom(xv, xa, xu);
269
     return false;
271 }
272
273 bool match()
274 {
275 for (int x = 1; x \le n_x; x++)
276
       col[x] = -1, slackv[x] = 0;
277
```

```
| 278 \quad q \quad n = 0;
     for (int x = 1; x \le n_x; x++)
279
280
      if (bel[x] == x && !mate[x])
281
          fa[x] = 0, col[x] = 0, slackv[x] = 0, q push(x);
282
      if (q n == 0)
283
       return false;
284
285
      while (true)
286
287
        for (int i = 0; i < q n; i++)
288
289
         int v = q[i];
290
          for (int u = 1; u <= n; u++)
291
            if (mat[v][u].w > 0 && bel[v] != bel[u])
292
293
              int d = e delta(mat[v][u]);
294
              if (d == 0)
295
296
                if (on found edge(mat[v][u]))
297
                  return true;
298
299
              else if (col[bel[u]] == -1 || col[bel[u]] == 0)
300
                update slackv(v, bel[u]);
301
        }
304
        int d = INF;
        for (int v = 1; v \le n; v++)
306
         if (col[bel[v]] == 0)
307
            tension(d, lab[v]);
308
        for (int b = n + 1; b \le n \times b + +)
309
        if (bel[b] == b && col[b] == 1)
310
            tension(d, lab[b] / 2);
311
        for (int x = 1; x \le n x; x++)
312
          if (bel[x] == x \&\& slackv[x])
313
314
            if (col[x] == -1)
315
              tension(d, e delta(mat[slackv[x]][x]));
316
            else if (col[x] == 0)
317
              tension(d, e delta(mat[slackv[x]][x]) / 2);
318
319
320
        for (int v = 1; v \le n; v++)
321
         if (col[bel[v]] == 0)
323
           lab[v] -= d;
324
          else if (col[bel[v]] == 1)
325
            lab[v] += d;
326
327
        for (int b = n + 1; b \le n \times (b++)
328
          if (bel[b] == b)
329
330
            if (col[bel[b]] == 0)
             lab[b] += d * 2;
            else if (col[bel[b]] == 1)
             lab[b] -= d * 2;
```

```
334
         }
336
        q n = 0;
       for (int v = 1; v \le n; v++)
338
         if (lab[v] == 0) // all unmatched vertices' labels are zero! cheers!
339
            return false;
340
        for (int x = 1; x \le n x; x++)
341
         if (bel[x] == x \&\& slackv[x] \&\& bel[slackv[x]] != x \&\& e delta(mat[
        slackv[x]][x] == 0
342
            if (on found edge(mat[slackv[x]][x]))
343
344
              return true;
345
346
        for (int b = n + 1; b \le n \times (b++)
347
          if (bel[b] == b && col[b] == 1 && lab[b] == 0)
348
            expand blossom1(b);
349
     return false;
351 }
353 void calc max weight match()
354 {
355
     for (int v = 1; v \le n; v++)
356
        mate[v] = 0;
358 n x = n;
359
     n \text{ matches} = 0;
     tot weight = 0;
361
362 \text{ bel}[0] = 0;
    for (int v = 1; v \le n; v++)
364
      bel[v] = v, bloch[v].clear();
365 for (int v = 1; v \le n; v++)
366
      for (int u = 1; u <= n; u++)
367
         blofrom[v][u] = v == u ? v : 0;
368
369 int w \max = 0;
    for (int v = 1; v \le n; v++)
371
        for (int u = 1; u <= n; u++)
372
         relax(w max, mat[v][u].w);
     for (int v = 1; v <= n; v++)
374
       lab[v] = w max;
375
376
     while (match())
       n matches++;
378
379
     for (int v = 1; v \le n; v++)
       if (mate[v] && mate[v] < v)</pre>
381
          tot weight += mat[v][mate[v]].w;
382
384 int main()
385 {
386
     n = getint(), m = getint();
387
388
     for (int v = 1; v \le n; v++)
```

```
389
        for (int u = 1; u <= n; u++)
          mat[v][u] = edge(v, u, 0);
391
392
      for (int i = 0; i < m; i++)
393
394
       int v = getint(), u = getint(), w = getint();
395
        mat[v][u].w = mat[u][v].w = w;
396
397
398
      calc max weight match();
399
400
      printf("%lld\n", tot weight);
401
     for (int v = 1; v \le n; v++)
402
       printf("%d ", mate[v]);
403
     printf("\n");
404
405
     return 0;
406 }
```

6.5 KM

```
1 #define MAXN 100
2 #define INF INT MAX
3 int g[MAXN][MAXN], lx[MAXN], ly[MAXN], slack y[MAXN];
4 int px[MAXN],py[MAXN],match y[MAXN],par[MAXN];
5 int n;
6 void adjust(int y){//把增廣路上所有邊反轉
7 match y[y]=py[y];
8 if (px[match y[y]]!=-2)
9
      adjust(px[match y[y]]);
10 }
11 bool dfs(int x){//DFS找增廣路
12 for (int y=0; y< n; ++y) {
     if (py[y]!=-1) continue;
      int t=lx[x]+ly[y]-q[x][y];
15
     if(t==0){
16
       py[y]=x;
17
       if(match y[y] == -1) {
18
        adiust(v);
19
          return 1;
21
        if (px[match y[y]]!=-1) continue;
22
        px[match y[y]]=y;
        if(dfs(match y[y]))return 1;
24
      }else if(slack y[y]>t){
        slack y[y]=t;
26
        par[y]=x;
27
28
29 return 0;
30 }
31 inline int km() {
32 memset(ly,0,sizeof(int)*n);
33 memset(match y,-1,sizeof(int)*n);
```

```
for (int x=0; x<n; ++x) {</pre>
       lx[x] = -INF;
36
       for (int y=0; y<n; ++y) {</pre>
         lx[x]=max(lx[x],g[x][y]);
38
39
     for (int x=0; x<n; ++x) {
41
       for(int y=0;y<n;++y)slack y[y]=INF;</pre>
42
       memset(px,-1, sizeof(int)*n);
43
       memset(py,-1, sizeof(int)*n);
44
       px[x]=-2;
45
       if (dfs(x)) continue;
46
       bool flag=1;
47
       while (flag) {
48
        int cut=INF;
49
         for (int y=0; y< n; ++y)
           if(py[y]==-1&&cut>slack y[y])cut=slack y[y];
51
         for(int j=0;j<n;++j){</pre>
           if(px[j]!=-1)lx[j]-=cut;
           if (py[j]!=-1)ly[j]+=cut;
54
           else slack y[j]-=cut;
55
56
         for (int y=0; y<n; ++y) {</pre>
57
           if(py[y] == -1&&slack y[y] == 0) {
58
              py[y]=par[y];
59
             if(match y[y] == -1){
60
                adjust(y);
61
                flag=0;
62
                break:
63
64
              px[match y[y]]=y;
65
             if(dfs(match y[y])){
66
                flag=0;
67
                break;
68
69
71
72
74
     for (int y=0; y<n; ++y) if (g[match y[y]][y]!=-INF) ans+=g[match y[y]][y];
75
     return ans;
76 }
```

6.6 MinCostFlow

```
1 #define maxnode (1000+10)
2 #define maxedge (40000+10)
3 #define INF 1023456789
4 #include<bits/stdc++.h>
5 using namespace std;
6 int node, src, dest, nedge;
7 int head[maxnode], point[maxedge], nxt[maxedge], flow[maxedge], capa[maxedge], wt[maxedge];
```

```
8 int dist[maxnode], in[maxnode], from[maxnode], mf[maxnode];
9 //set number of node, source, and destination (one base)
10 void init(int node, int src, int dest) {
      node = node;
12
      src = src;
13
      dest = dest;
14
     nedge = 0;
15
      memset(point, -1, sizeof(point));
      for (int i = 1; i <= node; i++) head[i] = -1;</pre>
16
17
      nedge = 0;
18 }
19 void add edge (int u, int v, int c1, int w) {
       point[nedge] = v, capa[nedge] = c1, flow[nedge] = 0, nxt[nedge] = head[u
       ], wt[nedge]=w, head[u] = (nedge++);
       point[nedge] = u, capa[nedge] = 0, flow[nedge] = 0, nxt[nedge] = head[v],
        wt[nedge] = -w, head[v] = (nedge++);
22 }
23 int sp(int &left) {
24 for(int i=1;i<=node;i++) dist[i]=INF;</pre>
    queue<int> que;
    que.push(src);
    in[src]=1;
    mf[src]=left;
    dist[srcl=0;
    while(!que.empty()){
     int u=que.front();
     que.pop();
      in[u]=0;
      if(dist[u]>=dist[dest]) continue;
      for(int v=head[u];v!=-1;v=nxt[v]){
36
        if(flow[v]==capa[v]) continue;
        if (dist[u]+wt[v]<dist[point[v]]) {</pre>
38
          dist[point[v]]=dist[u]+wt[v];
39
           from[point[v]]=v;
40
           mf[point[v]]=min(mf[u],capa[v]-flow[v]);
41
           if(!in[point[v]]){
            in[point[v]]=1;
42
43
             que.push(point[v]);
44
45
46
47
48
    left-=mf[dest];
49
    if (dist[dest] < INF) {</pre>
50
       for(int u=dest;u!=src;u=point[from[u]^1]){
51
         flow[from[u]]+=mf[dest];
52
         flow[from[u]^1]-=mf[dest];
53
54
    return dist[dest];
56 }
57 int min cost flow() {
int res=0, tmp, maxflow=2;
    while (maxflow&& (tmp=sp(maxflow)) < INF) res+=tmp;</pre>
60
    return res;
61 }
```

```
62 int main() {
63 int n, m, x, y, z;
64 while (scanf ("%d%d", &n, &m) == 2) {
     init(n,1,n);
66
     for(int i=0;i<m;i++){</pre>
67
      scanf("%d%d%d",&x,&y,&z);
68
      add edge(x, y, 1, z);
69
        add edge(y,x,1,z); //undirected
71
      printf("%d\n", min cost flow());
72 }
73 return 0;
74 }
```

6.7 Stable Marriage

```
1 #define F(n) Fi(i, n)
2 #define Fi(i, n) Fl(i, 0, n)
3 #define Fl(i, l, n) for (int i = l; i < n; ++i)
4 #include <bits/stdc++.h>
5 using namespace std;
6 int D, quota[205], weight[205][5];
7 int S, scoretodep[12005][205], score[5];
8 int P, prefer[12005][85], iter[12005];
9 int ans[12005];
10 typedef pair<int, int> PII;
11 map<int, int> samescore[205];
12 typedef priority queue<PII, vector<PII>, greater<PII>> QQQ;
13 QQQ pri[205];
14 void check(int d) {
15 PII t = pri[d].top();
if (pri[d].size() - samescore[d][t.first] + 1 <= quota[d]) return;
while (pri[d].top().first == t.first) {
19
    v = pri[d].top().second;
    ans[v] = -1;
21
     --samescore[d][t.first];
      pri[d].pop();
23 }
24 }
25 void push(int s, int d) {
26 if (pri[d].size() < quota[d]) {
      pri[d].push(PII(scoretodep[s][d], s));
28
     ans[s] = d;
29
     ++samescore[s][scoretodep[s][d]];
30 } else if (scoretodep[s][d] >= pri[d].top().first) {
    pri[d].push(PII(scoretodep[s][d], s));
32
      ans[s] = d;
      ++samescore[s][scoretodep[s][d]];
34
      check(d);
35 }
36 }
37 void f() {
38 int over;
```

```
39 while (true) {
    over = 1;
41
    Fi (a, S) {
      if (ans[q] != -1 || iter[q] >= P) continue;
      push(q, prefer[q][iter[q]++]);
44
       over = 0:
45
46
    if (over) break;
47 }
48 }
49 main() {
50 ios::sync with stdio(false);
51 cin.tie(NULL);
52 int sadmit, stof, dexceed, dfew;
53 while (cin >> D, D) { // Beware of the input format or judge may troll us.
    sadmit = stof = dexceed = dfew = 0;
55
    memset(iter, 0, sizeof(iter));
56
   memset(ans, 0, sizeof(ans));
57
    Fi (q, 205) {
58
    pri[q] = QQQ();
59
       samescore[q].clear();
60
61
    cin >> S >> P;
    Fi (q, D) {
62
    cin >> quota[q];
       Fi (w, 5) cin >> weight[q][w];
64
65
66
    Fi (q, S) {
67
       Fi (w, 5) cin >> score[w];
68
        Fi (w, D) {
69
          scoretodep[q][w] = 0;
          F (5) scoretodep[q][w] += weight[w][i] * score[i];
72
73
      Fi (q, S) Fi (w, P) {
74
        cin >> prefer[q][w];
75
       --prefer[q][w];
76
     f();
78
      Fi (q, D) sadmit += pri[q].size();
79
      Fi (q, S) if (ans[q] == prefer[q][0]) ++stof;
      Fi (q, D) if (pri[q].size() > quota[q]) ++dexceed;
81
      Fi (q, D) if (pri[q].size() < quota[q]) ++dfew;</pre>
      cout << sadmit << ' ' << stof << ' ' << dexceed << ' ' << dfew << '\n';
82
83
84 }
```

7 Mathematics

7.1 Extgcd

```
1 long long extgcd(long long a,long long b,long long &x,long long &y) {
```

```
long long d=a;
 3
       if(b!=0){
 4
           d=extgcd(b,a%b,y,x);
 5
           v = (a/b) *x;
 6
 7
       else x=1, y=0;
 8
       return d;
 9 }
10 int main() {
11
       int T;
       long long a,b,m,GCD,x,y;
13
       while(~scanf("%d",&T))
14
           while (T--) {
15
               scanf("%lld%lld%lld", &m, &a, &b);
16
               GCD=extgcd(a,m,x,y);
17
               if(GCD!=1)printf("No inverse, gcd(a,m)=%lld\n",GCD);
18
               else{
19
                    b = ((-b*x)%m+m)%m;
                    printf("%lld %lld\n", (x%m+m)%m,b);
21
22
23 }
```

7.2 Miller-Rabin

```
1 inline long long mod mul(long long a, long long b, long long m) {
     a%=m,b%=m;
    long long y=(long long)((double)a*b/m+0.5);/* fast for m < 2^58 */
    long long r=(a*b-y*m)%m;
     return r<0?r+m:r;</pre>
 6 }
 7 template<typename T>
 8 inline T pow(T a, T b, T mod) {//a^b%mod
 9 T ans=1;
     for(;b;a=mod mul(a,a,mod),b>>=1)
       if (b&1) ans=mod mul(ans,a,mod);
12
     return ans;
13 }
14 int sprp[3]={2,7,61};//int範圍可解
15 int llsprp[7]={2,325,9375,28178,450775,9780504,1795265022};//至少unsigned
       long long範圍
16 template<typename T>
17 inline bool isprime (T n, int *sprp, int num) {
18 if (n==2) return 1;
19 if (n<2||n%2==0) return 0;
20 int t=0;
21 T u=n-1:
22 for (; u%2==0; ++t) u>>=1;
23 for(int i=0;i<num;++i){</pre>
24
     T a=sprp[i]%n;
25
     if (a==0||a==1||a==n-1) continue;
26
     T x=pow(a,u,n);
27
      if (x==1 | x==n-1) continue;
28
       for(int j=0; j<t;++j){</pre>
```

8 String

8.1 AC Automaton

```
1 #ifndef SUNMOON AHO CORASICK AUTOMATON
 2 #define SUNMOON AHO CORASICK AUTOMATON
 3 #include<queue>
 4 #include<vector>
 5 template<char L='a',char R='z'>
 6 class ac automaton{
    private:
       struct joe{
9
         int next[R-L+1], fail, efl, ed, cnt dp, vis;
         joe():ed(0),cnt dp(0),vis(0)
11
           for (int i=0;i<=R-L;++i)next[i]=0;</pre>
13
      };
14
    public:
      std::vector<joe> S;
16
      std::vector<int> q;
17
      int qs,qe,vt;
18
       ac automaton():S(1), qs(0), qe(0), vt(0){}
19
      inline void clear(){
         q.clear();
21
         S.resize(1);
         for(int i=0;i<=R-L;++i)S[0].next[i]=0;</pre>
         S[0].cnt dp=S[0].vis=qs=qe=vt=0;
24
      inline void insert(const char *s){
26
         int o=0:
27
         for(int i=0,id;s[i];++i){
28
          id=s[i]-L;
29
           if(!S[o].next[id]){
             S.push back(joe());
             S[o].next[id]=S.size()-1;
32
           o=S[o].next[id];
34
         ++S[o].ed;
36
37
       inline void build fail() {
38
         S[0].fail=S[0].efl=-1;
```

```
39
        q.clear();
40
        q.push back(0);
41
        ++ae;
42
        while (qs!=qe) {
43
          int pa=q[qs++],id,t;
44
          for (int i=0;i<=R-L;++i) {</pre>
45
            t=S[pal.next[i];
46
            if(!t)continue;
47
            id=S[pa].fail;
48
            while(~id&&!S[id].next[i])id=S[id].fail;
49
            S[t].fail=~id?S[id].next[i]:0;
            S[t].efl=S[S[t].fail].ed?S[t].fail:S[S[t].fail].efl;
51
            q.push back(t);
            ++qe;
53
54
55
56
      /*DP出每個前綴在字串s出現的次數並傳回所有字串被s匹配成功的次數O(N+M)*/
57
      inline int match 0(const char *s){
58
        int ans=0,id,p=0,i;
59
        for(i=0;s[i];++i){
60
          id=s[i]-L;
61
          while (!S[p].next[id]&&p)p=S[p].fail;
62
          if(!S[p].next[id])continue;
63
          p=S[p].next[id];
          ++S[p].cnt dp;/*匹配成功則它所有後綴都可以被匹配(DP計算)*/
64
65
66
        for(i=qe-1;i>=0;--i){
67
          ans+=S[q[i]].cnt dp*S[q[i]].ed;
68
          if(~S[q[i]].fail)S[S[q[i]].fail].cnt dp+=S[q[i]].cnt dp;
69
        }
        return ans;
71
      /*多串匹配走efl邊並傳回所有字串被s匹配成功的次數O(N*M^1.5)*/
73
      inline int match 1(const char *s)const{
74
        int ans=0,id,p=0,t;
75
        for(int i=0;s[i];++i){
76
          id=s[i]-L;
          while (!S[p].next[id] &&p) p=S[p].fail;
78
          if(!S[p].next[id])continue;
79
          p=S[p].next[id];
8.0
          if(S[p].ed) ans+=S[p].ed;
          for(t=S[p].efl;~t;t=S[t].efl){
81
            ans+=S[t].ed;/*因為都走efl邊所以保證匹配成功*/
82
83
          }
84
        }
85
        return ans;
86
      /* 枚舉 (s的子字串\capA)的所有相異字串各恰一次並傳回次數\circ(N*M^(1/3))*/
87
88
      inline int match 2(const char *s){
89
        int ans=0,id,p=0,t;
90
        ++vt;
        /*把戳記vt+=1,只要vt沒溢位,所有S[p].vis==vt就會變成false
91
92
        這種利用vt的方法可以O(1)歸零vis陣列*/
93
        for(int i=0;s[i];++i){
94
          id=s[i]-L;
```

```
95
            while (!S[p].next[id] &&p) p=S[p].fail;
 96
            if(!S[p].next[id])continue;
 97
            p=S[p].next[id];
 98
            if(S[p].ed&&S[p].vis!=vt){
 99
              S[p].vis=vt;
              ans+=S[p].ed;
102
            for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[t].efl){
103
              S[t].vis=vt;
              ans+=S[t].ed;/*因為都走efl邊所以保證匹配成功*/
104
105
106
107
          return ans;
108
        /*把AC自動機變成真的自動機*/
109
110
        inline void evolution(){
111
          for (qs=1;qs!=qe;) {
112
            int p=q[qs++];
113
            for (int i=0; i<=R-L; ++i)</pre>
114
              if(S[p].next[i] == 0)S[p].next[i] = S[S[p].fail].next[i];
115
116
117 };
1118 #endif
```

8.2 Suffix Array

```
1 //should initialize s and n first
2 #define N 301000
3 using namespace std;
4 char s[N]; //string=s, suffix array=sar, longest common prefix=lcp
5 int rk[2][N],id[2][N];
6 int n,p;
7 int cnt[N];
8 int len[N],od[N],sar[N];
9 inline int sr(int i, int t) { //rank of shifted position
10 return i+t<n?rk[p][i+t]:-1;</pre>
11 }
12 inline bool check same(int i, int j, int t) {
13 return rk[p][i]==rk[p][j]&&sr(i,t)==sr(j,t);
14 }
15 bool cmp(int i, int j) {
16    return s[i] < s[j];</pre>
17 }
18 void sa() { //length of array s
19 int i,t,now,pre;
20 memset(cnt,0,sizeof(cnt));
21 for (i=0; i<n; i++) {
      id[p][i]=i;
23
      rk[p][i]=s[i];
24
      cnt[s[i]]++;
26
    for(i=1;i<128;i++) cnt[i]+=cnt[i-1];
    sort(id[p],id[p]+n,cmp);
```

```
for (t=1; t<n; t<<=1) {</pre>
29
           //least significant bit is already sorted
       for(i=n-1;i>=0;i--){
                now=id[p][i]-t;
32
         if(now>=0) id[p^1][--cnt[rk[p][now]]]=now;
34
       for (i=n-t; i < n; i++) {</pre>
35
                id[p^1][--cnt[rk[p][i]]]=i;
36
37
       memset(cnt,0,sizeof(cnt));
38
       now=id[p^1][0];
39
       rk[p^1][now]=0;
40
       cnt[0]++;
41
       for (i=1; i<n; i++) {</pre>
42
        pre=now;
43
         now=id[p^1][i];
44
         if(check same(pre,now,t)){
45
           rk[p^1][now]=rk[p^1][pre];
46
47
         else{
           rk[p^1][now]=rk[p^1][pre]+1;
48
49
         cnt[rk[p^1][now]]++;
       p^{=1};
53
       if(rk[p][now]==n-1) break;
54
       for (i=1;i<n;i++) cnt[i]+=cnt[i-1];</pre>
55
56
     memcpy(sar,id[p],sizeof(sar));
57 }
58 void lcp() {
59
       int i,l,pre;
60
       for(i=0;i<n;i++) od[sar[i]]=i;</pre>
61
       for (i=0; i<n; i++) {</pre>
62
           if(i) l=len[od[i-1]]?len[od[i-1]]-1:0;
63
           else 1=0;
           if (od[i]) {
64
65
                pre=sar[od[i]-1];
                while (pre+l<n&&i+l<n&&s[pre+l] ==s[i+l]) l++;
66
67
                len[od[i]]=1;
68
69
           else len[0]=0;
70
71 }
```

8.3 Suffix Automaton

```
1 #include<bits/stdc++.h>
2 #define C 96
3 #define N 200100
4 using namespace std;
5 struct SAM{
6 struct node{
7 node *nxt[C],*pre;
```

```
int len;
      vector<int> pos;
    node mem[N*2], *root, *ed;
12
    int top;
13
    SAM(){
14
      top = 0;
15
      root = new node(0);
16
      ed = root;
17 }
18
    node *new node(int 1) {
     for(int i=0;i<C;i++) mem[top].nxt[i]=NULL;</pre>
20
      mem[top].pre=NULL;
      mem[top].len=l;
      mem[top].pos.clear();
23
      return mem+(top++);
24 }
25   node *split node(int l, node *p) {
    for(int i=0;i<C;i++) mem[top].nxt[i]=p->nxt[i];
26
27
      mem[top].pre = p->pre;
28
    mem[top].len = 1;
29
    mem[top].pos.assign()
    p->pre = mem+top;
      return mem+(top++);
32 }
    void push(char c) {
     node *nw = new node(ed->len+1),*ptr=ed->pre;
34
      ed->nxt[c] = nw;
36
      nw->pos.push back(ed->len);
37
      for(;ptr;ptr=ptr->pre) {
38
       if(ptr->nxt[c]){
39
          if (ptr->nxt[c]->len==ptr->len+1) {
40
            nw->pre = ptr->nxt[c];
41
42
          else{
43
            node *tmp=ptr->nxt[c];
            nw->pre = split node(ptr->len+1, tmp);
44
45
            while(ptr && ptr->nxt[c]==tmp) {
46
              ptr->nxt[c] = nw->pre;
47
               ptr = ptr->pre;
48
            }
49
50
          break:
51
52
        else{
53
           ptr->nxt[c] = nw;
54
55
      if(!nw->pre) nw->pre = root;
56
57
       ed = ed->nxt[c];
58
59
    void init(){
60
     while(top){
61
        mem[--top].pos.clear();
62
63
       root = new node(0);
```

```
ed = root;
64
65
   }
    void push(char *s){
66
67
      for (int i=0; s[i]; i++) push (s[i]-32);
68
   long long count(){
69
     long long ans=0;
71
      for (int i=1; i < top; i++) {</pre>
72
        ans+=mem[i].len-mem[i].pre->len;
73
      }
74
      return ans;
75
76 }sam;
77 char S[N];
78 int main() {
79 int T;
80 scanf("%d",&T);
81 while (T--) {
82
     scanf("%s",S);
83
      sam.build(S);
      printf("%lld\n", sam.count());
84
85 }
86 return 0;
87 }
```

8.4 Z Algorithm

```
1 void Zalg(char *s, int *z, int n) {
z [0] = n;
3 for(int L=0, R=0, i=1; i<n; i++) {</pre>
     if(i<=R && z[i-L]<=R-i) z[i]=z[i-L];
5
      else {
       L=i;
6
7
       if(i>R) R=i;
8
       while (R < n \&\& s[R-L] == s[R]) R++;
9
        z[i] = (R--)-L;
11 }
12 }
```

9 Struct

9.1 Splay Tree

```
1 #include<cstdio>
2 #include<string>
3 using namespace std;
4 struct node{
5 node *ch[2],*par;
```

```
6 long long sum;
 7 int val, sz, add;
8 node(){}
    node(int x): par(NULL), val(x), sum(x), add(0), sz(1) {ch[0]=ch[1]=NULL;}
10 bool dir(){return !par||par->ch[1]==this;}
void pull();
12 void push();
13 }pool[100100];
14 inline long long qsum(node *x) {
return x?1LL*x->add*x->sz+x->sum:0;
17 inline int qsz(node *x) {return x?x->sz:0;}
18 void node::pull() {
19    sum=val+qsum(ch[0])+qsum(ch[1]);
sz=1+qsz(ch[0])+qsz(ch[1]);
21 }
22 void node::push() {
23 if(add){
24 val+=add;
   sum+=add*sz;
    if(ch[0]) ch[0]->add+=add;
27
    if (ch[1]) ch[1]->add+=add;
28
    add=0:
29 }
30 }
31 inline void con(node *p, node *c, bool d) {
32 p->ch[d]=c;
33 if(c) c->par=p;
34 }
35 void splay (node *x) {
x \rightarrow push();
37 while (x->par) {
38
    node *p=x->par,*g=p->par;
    bool d=x->dir(),pd=p->dir();;
39
40
    con(p,x->ch[d^1],d);
41
      con(x,p,d^1);
42
     if(q){
43
    if(g->par) con(g->par,x,g->dir());
44
        else x->par=NULL;
45
        if(d^pd){
46
          con(q,x->ch[d],pd);
47
          con(x,q,pd^1);
48
49
        else{
50
          con(q,p->ch[pd^1],pd);
51
          con(p,g,pd^1);
52
53
        g->pull();
54
      else x->par=NULL;
56
      p->pull();
57
      x - > pull();
58 }
59 }
60 void check tree (node *t, int d) {
61 if(!t) return;
```

```
check tree(t->ch[0],d+1);
 63 for(int i=0;i<d;i++) printf("\t");</pre>
     printf("%d\n",t->val);
     check tree(t->ch[1],d+1);
 66 }
 67 void split (node *t, int k, node *&a, node *&b) {
     if(!k){
 69
       a=NULL; b=t; return;
 71 int rod;
 72 while ( k != (rod=qsz(t->ch[0])+1) ) {
 73
     t->push();
 74
     if (k>rod) k-=rod, t=t->ch[1];
 75
      else t=t->ch[0];
 76 }
 77 splay(t);
 78 a=t;
 79 a->push();
 80 b=a->ch[1];
 81 a->ch[1]=NULL;
     a->pull();
 83
    if(b) b->par=NULL;
84 }
 85 node* merge(node *a, node *b) {
    if(!a) return b;
    while(a->ch[1]){
 87
 88
       a->push();
 89
       a=a->ch[1];
 90 }
 91 splay(a);
 92 con(a,b,1);
 93 a->pull();
 94
     return a;
 95 }
 96 int main() {
 97 int n,q,x;
 98 node *root=NULL, *a, *b, *c;
 99 scanf("%d%d",&n,&q);
100 for(int i=0;i<n;i++){
      scanf("%d",&x);
       node *tmp=new (pool+i) node(x);
       root=merge(root,tmp);
104 }
105 for (int i=0; i<q; i++) {
106
     char tp;
      int x, v, z;
108
      scanf(" %c%d%d", &tp, &x, &y);
109
     split(root,x-1,a,b);
     split(b,y-x+1,b,c);
111
      if(tp=='C'){
       scanf("%d",&z);
113
         b->add+=z;
114
115
       else printf("%lld\n",qsum(b));
116
       root=merge(a, merge(b,c));
117
```

```
118 return 0;
119 }
```

9.2 Treap

```
1 struct Treap{
2 Treap *1,*r;
3 int pri,sz,val,add;
 4 Treap(int val):pri(rand()),sz(1),val( val),add(0),l(NULL),r(NULL){}
5 };
7 int size(Treap *t) {
8 return t?t->sz:0;
9 }
10 void pull(Treap *t) {
11 t->sz=size(t->1)+size(t->r)+1;
13 void push (Treap *t) {
14 t->val+=t->add;
15 if(t->1) t->1->add+=t->add;
if (t->r) t->r->add+=t->add;
17 t->add=0;
18 }
19 Treap* merge(Treap *a, Treap *b) {
20 if(!a||!b) return a?a:b;
21 if(a->pri > b->pri){
22 push(a);
   a->r = merge(a->r,b);
24
   pull(a);
    return a;
26 }
27 else{
28
   push(b);
   b->1 = merge(a,b->1);
    pull(b);
    return b;
32 }
33 }
34 void split (Treap *t, int k, Treap *&a, Treap *&b) {
35 if(!t) a=b=NULL;
36 else{
   push(t);
38
    if(size(t->1) < k){
39
40
       split(t->r,k-size(t->l)-1,a->r,b);
     pull(a);
41
42
   }
43
    else{
44
    b=t;
45
    split(t->1,k,a,b->1);
46
        pull(b);
47
48 }
49 }
```

10 Tree

10.1 Heavy Light Decomposition

```
1 //with set value && guery sum, 1-based with n points
2 //remove vis in DFS, add it back if something weird happen (I don't think it
       's required)
3 using namespace std;
4 int sz[N], top[N], up[N], dep[N];
5 int lightval[N]; //value on light edge
6 struct node{
7 node(){}
    node(int 1,int r):val(1),l(1),r(r),lc(NULL),rc(NULL){}
10 node *lc, *rc;
11 int sum;
12 int val;
   int qsum() {return val>=0?val*(r-1):sum;}
   void push() {
15
     if (val>=0) {
16
      sum=val*(r-1);
      lc->val=rc->val=val;
17
18
        val=-1;
19
20 }
21
    void pull() {
       sum=lc->qsum()+rc->qsum();
23
24 };
25 node* tr[N];
26 node* build(int l,int r) {
27   node *now=new node(1,r);
28 if(r-1>1){
      now->lc=build(l,(l+r)/2);
29
      now->rc=build((l+r)/2,r);
   return now;
33 }
34 //partial
35 int qry(node* now, int l, int r) {
36 if(1>=r) return 0;
   if(l==now->l&&r==now->r){
38
      return now->qsum();
39
40 int m = (now - > 1 + now - > r) / 2;
41 now->push();
42
   if(l>=m) {
43
      return qry(now->rc,1,r);
44
45 else if(r<=m){
```

```
return qry(now->lc,l,r);
 46
 47 }
 48 else return qry(now->lc,l,m)+qry(now->rc,m,r);
 50 void set0 (node *now, int l, int r) {
 51 if(l>=r) return;
 52 if (l==now->l&&r==now->r) {
     now->val=0;
 54
      return;
 55
 56
     int m = (now - > 1 + now - > r) / 2;
    now->push();
 58
    if(1>=m){
 59
      set0(now->rc,1,r);
 60 }
 61 else if (r<=m) {
     set0(now->lc,l,r);
 63 }
 64 else{
 65
       set0(now->lc,1,m);
 66
       set0(now->rc,m,r);
 67 }
 68 now->pull();
 69 }
 70 vector<int> g[N];
 71 void DFS (int u, int p, int d) {
 72 dep[u]=d;
 73 sz[u]=1;
 74 for(int i=0;i<q[u].size();i++){
    int v=g[u][i];
     if(v==p) continue;
     DFS(v,u,d+1);
 78
       sz[u] += sz[v];
 79 }
 80 }
 81 void decom(int u, int p, bool istop) {
 82 bool ed=true;
 if (istop) top[u]=u,up[u]=p,lightval[u]=1;
 84 else top[u]=top[p],up[u]=up[p];
 85 for(int i=0;i<g[u].size();i++){
     int v=g[u][i];
     if(v==p) continue;
 88
     if(sz[v]>=sz[u]-sz[v]){
 89
     decom(v,u,false);
 90
         ed=false;
 91
 92
       else decom(v,u,true);
 93 }
 94 if (ed) {
 95
       tr[top[u]]=build(dep[top[u]],dep[u]);
 96 }
 97 }
 98 //global
 99 int qry(int u, int v) {
100 int res=0;
101 while (top[u]!=top[v]) {
```

```
if (dep[top[u]]>dep[top[v]]) swap(u,v);
      res+=qry(tr[top[v]],dep[top[v]],dep[v]);
104
      res+=lightval[top[v]];
      v=up[top[v]];
106 }
if (dep[u]>dep[v]) swap(u,v);
108 res+=qry(tr[top[v]],dep[u],dep[v]);
109 return res;
110 }
111 void set0(int u,int v){
112 while (top[u]!=top[v]) {
     if (dep[top[u]]>dep[top[v]]) swap(u,v);
114
     set0(tr[top[v]],dep[top[v]],dep[v]);
115
      lightval[top[v]]=0;
116
      v=up[top[v]];
117 }
118 if (dep[u]>dep[v]) swap(u,v);
119 set0(tr[top[v]],dep[u],dep[v]);
120 }
121 int main() {
122 DFS(1,0,0);
123 decom(1,0,true);
124 }
```

10.2 KDtree Insert

```
1 #include < algorithm >
 2 #include<cmath>
 3 #include<cstdio>
 4 #include<queue>
 5 #include<cstdlib>
 6 #include<vector>
 7 #define MAXN 50100
8 using namespace std;
 9 inline long long sq(long long x) {return x*x;}
10 const double alpha=0.75;
11 int W, H, rx[MAXN], ry[MAXN];
12 namespace KDTree{
13 struct Point {
14
     int x, y;
15
      int index;
     long long distance(const Point &b)const{
16
17
        return sq(x-b.x) + sq(y-b.y);
18
19
      bool operator==(const Point& rhs){return index==rhs.index;}
    };
21 struct qnode{
22
      Point p;
23
      long long dis;
24
      gnode(){}
25
       qnode(Point p,long long dis){
26
       p = p;
        dis = dis;
27
28
```

```
bool operator <(const qnode &b)const{</pre>
29
        if(dis != b.dis)return dis < b.dis;</pre>
        else return p.index < b.p.index;</pre>
33 };
34 priority queue<qnode>q;
   inline bool cmpX(const Point &a, const Point &b) {
      return a.x < b.x || (a.x == b.x \&\& a.y < b.y) || (a.x == b.x \&\& a.y == b.
      y && a.index < b.index);
37 }
38
   inline bool cmpY(const Point &a, const Point &b) {
      return a.y < b.y || (a.y == b.y \&\& a.x < b.x) || (a.y == b.y \&\& a.x == b.
      x && a.index < b.index);
40 }
41 bool cmp (const Point &a, const Point &b, bool div) {
      return div?cmpY(a,b):cmpX(a,b);
43 }
44 struct Node{
    Point e:
    Node *lc, *rc;
    int size;
47
48
   bool div;
49
    inline void pull() {
       size = 1 + lc->size + rc->size;
51
52
      inline bool isBad(){
53
        return lc->size > alpha*size || rc->size > alpha*size;
54
55
    }pool[MAXN],*tail,*root,*recycle[MAXN],*null;
56
    int rc cnt;
57 void init(){
    tail = pool;
58
   null = tail++;
60
   null->lc = null->rc = null;
61
    null->size = 0;
62
    rc cnt = 0;
     root = null;
63
64 }
65 Node *newNode(Point e) {
66
    Node *p;
67
    if(rc cnt)p = recycle[--rc cnt];
68
    else p = tail++;
69
    p->e = e;
   p->lc = p->rc = null;
71
      p->size = 1;
72
      return p;
73 }
74 Node *build(Point *a, int l, int r, bool div) {
75 if (1 >= r) return null;
76
    int mid = (1+r)/2;
    nth element(a+l,a+mid,a+r,div?cmpY:cmpX);
78
    Node *p = newNode(a[mid]);
79
      p->div = div;
80
    p->lc = build(a,l,mid,!div);
81
      p->rc = build(a,mid+1,r,!div);
82
      p->pull();
```

```
83
        return p;
84
 85
     void getTree(Node *p, vector<Point>& v) {
 86
       if(p==null) return;
 87
       getTree(p->lc,v);
       v.push back(p->e);
 88
 89
       recycle[rc cnt++]=p;
 90
       getTree(p->rc,v);
 91
 92
     Node *rebuild(vector<Point>& v,int l,int r,bool div) {
 93
       if(l>=r) return null;
 94
       int mid = (1+r)/2;
 95
       nth element(v.begin()+l,v.begin()+mid,v.begin()+r,div?cmpY:cmpX);
 96
       Node *p = newNode(v[mid]);
 97
       p->div = div;
 98
       p->lc = rebuild(v,l,mid,!div);
 99
       p->rc = rebuild(v,mid+1,r,!div);
       p->pull();
       return p;
     void rebuild(Node *&p) {
104
       vector<Point> v;
       getTree(p,v);
106
       p = rebuild(v, 0, v.size(), p->div);
108
     Node **insert(Node *&p, Point a, bool div) {
109
       if (p==null) {
         p = newNode(a);
111
         p->div = div;
         return &null;
113
114
       else{
115
116
         if (cmp(a,p->e,div)) res=insert(p->lc,a,!div);
         else res=insert(p->rc,a,!div);
118
         p->pull();
119
         if(p->isBad()) res=&p;
          return res;
122
123
     void insert(Point e) {
124
       Node **p = insert(root, e, 0);
125
        if(*p!=null) rebuild(*p);
126
127
     Node **get min(Node *&p, bool div) {
128
       if (p->div==div) {
129
         if (p->lc!=null) return get min(p->lc,div);
          else return &p;
132
       else{
         Node **res=&p, **tmp;
134
         if(p->lc!=null){
            tmp = get min(p->lc,div);
136
            if (cmp((*tmp)->e,(*res)->e,div)) res=tmp;
138
         if(p->rc!=null){
```

```
139
             tmp = get min(p->rc,div);
140
             if (cmp((*tmp)->e,(*res)->e,div)) res=tmp;
141
142
           return res;
143
144
145
      void del (Node *&p) {
146
        Node **nxt;
147
       if(p->rc!=null){
148
          nxt = get min(p->rc,p->div);
149
          p->e = (*nxt)->e;
150
           del(*nxt);
151
152
        else if(p->lc!=null){
153
          nxt = qet min(p->lc,p->div);
154
          p - > e = (*nxt) - > e;
155
          del(*nxt);
156
          p->rc = p->lc;
157
           p->lc = null;
158
159
        else{
160
           recycle[rc cnt++]=p;
           p=null;
162
163
164
      void del(Node *&p, Point d) {
165
       if(p->e==d){
166
           del(p);
167
168
        else if (cmp(d, p\rightarrow e, p\rightarrow div)) del(p\rightarrow lc, d);
169
        else del(p->rc,d);
170
171
      void search(Point p, Node *t, bool div, int m) {
172
       if(!t)return;
       if (cmp(p,t->e,div)) {
173
174
           search(p,t->lc,!div,m);
175
          if(q.size() < m){}
176
             q.push(qnode(t->e,p.distance(t->e)));
177
             search(p,t->rc,!div,m);
178
179
           else {
180
             if (p.distance(t->e) <= q.top().dis) {</pre>
181
               q.push(qnode(t->e,p.distance(t->e)));
182
               q.pop();
183
184
             if(!div){
185
               if(sq(t->e.x-p.x) \le q.top().dis)
186
                 search(p,t->rc,!div,m);
187
188
             else {
189
               if(sq(t->e.y-p.y) \le q.top().dis)
190
                 search (p, t->rc, !div, m);
191
192
193
194
         else {
```

```
195
         search(p,t->rc,!div,m);
196
         if(q.size() < m){
197
           q.push(qnode(t->e,p.distance(t->e)));
198
            search(p,t->lc,!div,m);
199
         else {
            if (p.distance(t->e) <= q.top().dis) {</pre>
202
              q.push(gnode(t->e,p.distance(t->e)));
             q.pop();
204
            if(!div){
206
             if(sq(t->e.x-p.x) \le q.top().dis)
                search(p,t->lc,!div,m);
208
209
           else {
             if(sq(t->e.y-p.y) \le q.top().dis)
                search(p,t->lc,!div,m);
212
213
214
       }
215
216
     void search(Point p,int m) {
217
       while(!q.empty())q.pop();
218
       search (p, root, 0, m);
219 }
void getRange(Node *p,vector<Point>& v,int x1,int x2,int y1,int y2) {
       if(p==null) return;
222
       if(x1 \le p-e.x \&\& p-e.x \le x \le y1 \le p-e.y \&\& p-e.y \le y \le y2) v.push back(p-e
       if (p-)div ? y1 <= p-)e.y : x1 <= p-)e.x) getRange <math>(p-)1c, v, x1, x2, y1, y2);
224
       if(p->div ? y2>=p->e.y : x2>=p->e.x) getRange(p->rc,v,x1,x2,y1,y2);
225
226 void solve(Point p) {
       del(root,p);
228
       insert(p);
229 }
230 };
231 KDTree::Point p[MAXN];
232 int main() {
233 KDTree::init();
234 KDTree::root = KDTree::build(p,0,n,0);
235 while(q--){
236
      KDTree::Point tmp,p1,p2;
      scanf("%d%d",&tmp.x,&tmp.y);
238
       search(tmp,2);
239
       p1=KDTree::q.top().p;
240
       KDTree::q.pop();
241
       p2=KDTree::q.top().p;
242
       KDTree::q.pop();
243 }
244 return 0;
245 }
```