NCTU electron Codebook

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1 .vimrc

```
set nu
set sw=4
set ts=4
set st=4
set bs=2
set cul
set ai
set ls=2
map \langle F5 \rangle gT
imap < F5 > < ESC > gT
map < F6 > gt
imap < F6 > < ESC > gt
imap {<CR> {<CR> END> CR>} <UP> END>
au FileType cpp map <F9> <ESC>:w<CR>:!g++<Space>-Wall<Space>%&&./a.
    out < CR>
au FileType cpp imap <F9> <ESC>:w<CR>:!g++<Space>-Wall<Space>%&&./a.
    out < CR>
set encoding=UTF-8
```

2 AC Actomaton

```
#include <iostream>
#include <queue>
#include <cstring>
#include <cstdio>

using namespace std;

struct AC_Automaton {
    static const int MAX.N = 1e6+10;
    static const int MAX.CHILD = 52;

    int n;
    int fail [MAX.N];
    int trie [MAX.N] [MAX.CHILD];

    void clean (int target) {
        for (int i = 0; i < MAX.CHILD; ++i) {
            trie [target][i] = -1;
        }
    }
    void reset () {</pre>
```

```
clean (0);
    n = 1;
void add(char* s) {
    int p = 0;
    while (*s) {
        int id = get_id(s[0]);
        if (\text{trie}[p][id] = -1) {
            clean(n);
            trie[p][id] = n++;
        p = trie[p][id];
        ++s;
void construct() {
    queue<int> que;
    fail[0] = 0;
    for (int i = 0; i < MAX_CHILD; ++i) {
        if (trie [0][i] != -1) {
            fail[trie[0][i]] = 0;
            que.push(trie[0][i]);
        else {
            trie[0][i] = 0;
    while (que.size()) {
        int now = que.front();
        que.pop();
        for (int i = 0; i < MAX\_CHILD; ++i) {
            int target = trie[now][i];
            if (target != -1) {
                que.push(target);
                 fail [target] = trie [fail [now]][i];
                 trie [now][i] = trie [fail [now]][i];
```

```
int solve() {
        int ans = fail[n-1];
        while (ans > n/2-1) ans = fail [ans];
        return ans;
    }
    int get_id(const char& ch) {
        if (ch \le z') && ch \ge a') return ch-a';
        else return ch-'A'+26;
} ac;
char input [1000010];
int main () {
    int tcase;
    scanf("%d", &tcase);
    while (tcase --) {
        ac.reset();
        scanf("%s", input);
        ac.add(input);
        ac.construct();
        printf("%d\n", ac.solve());
```

3 Combinatoion

```
const long long MOD = 1e9+7;
const int MAX = 1e5+1;

typedef long long T;
T inverse(T mod, T b) { /* return b^(-1) mod a */
   T k[2][2], n[2][2], u1, u2;

k[0][0] = k[1][1] = 1;
k[0][1] = k[1][0] = 0;

u1 = mod, u2 = b;

while (u2) {
   T div = u1/u2;
   T remind = u1%u2;

   n[0][0] = k[1][0];
   n[0][1] = k[1][1];
```

```
n[1][0] = k[0][0] - k[1][0] * div;
        n[1][1] = k[0][1] - k[1][1] * div;
        for (T i = 0; i < 2; ++i)
            for (T j = 0; j < 2; ++j) {
                k[i][j] = n[i][j];
        u1 = u2;
        u2 = remind;
    if (k[0][1] < 0) k[0][1] += mod;
    return k[0][1];
T C(T n, T m, T mod)  {
    if (m < 0) return 0;
    if (n < m) return 0;
    T \text{ ans} = 1;
    T base = \min(n-m, m);
    for (T i = 0; i < base; ++i)
        ans = ans *(n-i)%mod;
    T inv = 1;
    for (T i = 1; i \le base; ++i) {
        inv = inv * i \mod;
    return ans*inverse (mod, inv)%mod;
```

4 Decomposition

```
static class Decomposition {
    Map<BigInteger , Integer> prime;
    Random random;

    Decomposition(String x) {
        prime = new HashMap<>();
        random = new Random();
        BigInteger in = new BigInteger(x);
        int twos = 0;
        while (!in.testBit(0)) {
```

```
in = in.shiftRight(1);
        twos++;
    if (twos > 0) prime.put(BigInteger.valueOf(2), twos);
    peel(in);
void peel(BigInteger x){
    System.out.println("peel "+x);
    if (x.equals (BigInteger .ONE)) return;
    if (x.isProbablePrime (100)) {
        Integer temp = prime.put(x, 1);
        if (temp!=null) prime.put(x, temp+1);
        return;
    BigInteger a, b, c, next;
        a = b = new BigInteger(x.bitLength()+5, random).mod(x);
        c = new BigInteger(x.bitLength()+5, random).mod(x);
        if(c.equals(BigInteger.ZERO)) c = BigInteger.ONE;
        do{
            a = f(a, c, x);
            b = f(f(b, c, x), c, x);
            next = x.gcd(a.subtract(b).abs());
        } while (next.equals (BigInteger .ONE));
    } while (next.equals(x));
    peel(next);
    peel(x.divide(next));
BigInteger f(BigInteger x, BigInteger c, BigInteger n) {
    return x.multiply(x).add(c).mod(n):
```

5 Double LCA

```
/* build: O(VlogV), query: O(logV) */
#include <iostream>
#include <vector>
#include <cstdio>
#define MAX 50010

using namespace std;
```

```
| \text{int a} [\text{MAX}] [160]; /* 160 = \log 2 (\text{MAX}/2) */
 int parent[MAX], tin[MAX], tout[MAX];
 int num, root, timestamp;
bool visit [MAX];
 vector < int > adj [MAX];
 int log2(int n) {
     int i = 0;
     while ((1 << i) <= n) ++i;
     return i - 1;
 /* when x == y, it's be true */
 bool ancestor(int x, int y) {
     return (tin[x] \le tin[y]) && (tout[x] >= tout[y]);
 void dfs(int x, int px) {
     tin[x] = timestamp++;
     visit[x] = true;
     a[x][0] = px;
     for (int i = 1; i < log2(num); ++i) {
         a[x][i] = a[a[x][i-1]][i-1];
     for (int i = 0; i < adj[x].size(); ++i) {
         int target = adj[x][i];
         if (!visit[target]) {
             parent[target] = x;
             dfs(target, x);
     tout[x] = timestamp++;
 int lca(int x, int y) {
     if (ancestor(x, y)) return x;
     if (ancestor(y, x)) return y;
     for (int i = log 2 (num); i >= 0; --i) {
         if (!ancestor(a[x][i], y)) {
             x = a[x][i];
     return a[x][0];
int main () {
```

```
timestamp = 0;

/* init */
for (int i = 0; i < num; ++i) {
    parent[i] = i;
    visit[i] = false;
    adj[i].clear();
}

for (int i = 0; i < num-1; ++i) {
    int x, y;
    scanf("%d%d", &x, &y);
    adj[x].push_back(y);
    adj[y].push_back(x);
}

dfs(0, 0);
cin >> x >> y;
cout << lca(x, y);
}</pre>
```

6 Flow (Dinics)

```
import java.io.*;
import java.util.*;
public class Main{
  static ArrayList<ArrayList<Edge>> list;
  static Edge [][] matrix;
  static int start, finish;
  static int findFlow(){
    int[] height = new int[list.size()];
    Arrays. fill (height, -1);
    Queue<Integer > queue = new ArrayDeque<Integer >();
    height[start] = 0;
    queue.add(start);
    while (!queue.isEmpty()) {
      int now = queue.poll();
      for (Edge e : list.get(now)) {
        int next = e.v;
        if(e.cap = 0) continue;
        if (height [next] != -1) continue;
        height[next] = height[now]+1;
        queue.add(next);
```

```
if (height [finish] = -1) return 0;
 int result = 0, flow;
  while ((flow = trace(start, Integer.MAX_VALUE, height)) != 0)
 result += flow;
  return result:
static int trace (int now, int flow, int [] height) {
  if (now == finish) 
    return flow;
 int result = 0;
  for (Edge e : list.get(now)){
   if(e.cap = 0) continue;
    int next = e.v;
    if (height [now]+1 != height [next]) continue;
    result = trace(next, Math.min(flow, e.cap), height);
    if(result != 0){
      matrix [now] [next].cap -= result;
      matrix [next] [now].cap += result;
      break;
  return result;
static class Edge{
 int u, v, cap;
  public Edge(int u, int v, int cap, Edge[][] matrix){
    this.u = u;
    this.v = v:
    this.cap = cap;
    matrix[u][v] = this;
```

7 Geometry

```
#include <bits/stdc++.h>
using namespace std;
```

```
#define EPS 1e-10
#define LEFT_TOP POS(1000, 1000)
#define NO_INTERSECT POS(-1234, -1234)
#define PARALLEL POS(-1001, -1001)
#define COLINE POS(1234, 1234)
const double PI = acos(-1.0);
typedef double T;
class POS {
public:
   T x, y;
   POS(const T\& x = 0, const T\& y = 0) : x(x), y(y)  {}
    POS(const\ POS\&\ x) : x(x.x), y(x.y)  {}
    bool operator == (const POS rhs) const {
        return x = rhs.x & y = rhs.y;
    }
    POS& operator+=(const POS& rhs) {
        x += rhs.x;
        v += rhs.v;
        return *this;
    POS operator -() {
        POS tmp(-x, -y);
        return tmp;
    }
    double dist (const POS rhs) const {
        T \text{ tmp}_x = x-rhs.x, \text{ tmp}_y = y-rhs.y;
        return sqrt(tmp_x*tmp_x+tmp_y*tmp_y);
    }
    friend ostream& operator << (ostream& out, const POS& pos) {
        out \ll pos.x \ll " " \ll pos.y;
        return out;
};
POS const operator+(const POS& lhs, const POS& rhs) {
    return POS(lhs) += rhs;
POS const operator - (const POS& lhs, const POS& rhs) {
    POS tmp = rhs:
    tmp = -tmp;
```

```
return POS(lhs) += (tmp);
bool cmp_convex(const POS& lhs, const POS& rhs) {
    return (lhs.x < rhs.x) | ((lhs.x = rhs.x)&&(lhs.y < rhs.y));
inline T cross (const POS& o, const POS& a, const POS& b) {
    double value = (a.x-o.x)*(b.v-o.y) - (a.v-o.y)*(b.x-o.x);
    if (fabs(value) < EPS) return 0;
    return value:
void convex_hull(POS* points, POS* need, int& n) {
    sort(points, points+n, cmp_convex);
    int index = 0;
   for (int i = 0; i < n; ++i) {
        while (index \geq 2 && cross (need [index -2], need [index -1],
   points[i]) \le 0 index --;
        need[index++] = points[i];
   int half_point = index + 1;
   for (int i = n-2; i >= 0; —i) {
        while (index >= half-point && cross (need [index -2], need [index
   -1], points[i]) \leq 0 index --;
       need[index++] = points[i];
   \} /* be careful that start point will appear in first and last in
    need arrav */
   n = index;
class LINE {
public:
   POS start, end, vec;
   double angle;
   LINE() {}
   LINE(const T& st_x, const T& st_y, const T& ed_x, const T& ed_y)
        start(st_x, st_y), end(ed_x, ed_y), vec(end - start), angle(
   atan2(vec.x, vec.y)) {}
   LINE(const POS& start, const POS& end):
        start(start), end(end), vec(end - start), angle(atan2(vec.x,
   vec.y)) {}
   LINE(const POS& end) : /* start point is origin */
        start (0, 0), end (end), vec (end), angle (atan2 (vec.x, vec.y))
   {}
```

```
LINE(const T a, const T b, const T c): /* given line by ax+by+c
= 0 * /
    start(0, 0), end(0, 0), vec(-b, a)
     if (a == 0) {
         start.y = end.y = -c/b;
         end.x = -b;
     else if (b = 0) {
         start.x = end.x = -c/a;
         end.y = a;
     else if (c = 0) {
         end.x = -b; end.y = a;
     else {
         start.y = -c/b; end.x = -c/a;
         \operatorname{vec.x} = -c/a; \operatorname{vec.y} = c/b;
     angle = atan2(vec.x, vec.y);
}
LINE build_orthogonal(const POS point) const {
    T c = -(vec.x*point.x + vec.y*point.y);
    return LINE(vec.x, vec.y, c);
}
T length2() const { /* square */
    T x = start.x - end.x, y = start.y - end.y;
    return x*x + y*y;
}
void modify (T x, T y) {
     this \rightarrow end.x += x;
     this \rightarrow end.y += y;
     this \rightarrow vec.x += x;
     this \rightarrow vec. y += y;
bool on_line(const POS& a) const {
     if (vec.x == 0) {
         if (start.x != a.x) return false;
         return true;
     if (vec. y == 0) {
         if (start.y!= a.y) return false;
         return true;
```

```
return fabs(( (a.x-start.x)/vec.x*vec.y + start.y) - a.y) <
   EPS:
    bool operator/(const LINE& rhs) const { /* to see if this line
   parallel to LINE rhs */
        return (vec.x*rhs.vec.y == vec.y*rhs.vec.x);
    bool operator == (const LINE& rhs) const { /* to see if they are
   same line */
        return (*this/rhs) && (rhs.on_line(start));
   POS intersect (const LINE& rhs) const {
        if (*this=rhs) return COLINE; /* return co-line */
        if (*this/rhs) return PARALLEL; /* return parallel */
        double A1 = vec.y, B1 = -vec.x, C1 = end.x*start.y - start.x*
        double A2 = rhs.vec.y, B2 = -rhs.vec.x, C2 = rhs.end.x*rhs.
   start.y - rhs.start.x*rhs.end.y;
        return POS( (B2*C1-B1*C2)/(A2*B1-A1*B2), (A1*C2-A2*C1)/(A2*B1
   -A1*B2)); /* sometimes has -0 */
    double dist (const POS& a) const {
        return fabs (vec.y*a.x - vec.x*a.y + vec.x*start.y - vec.y*
   start.x)/sqrt(vec.y*vec.y+vec.x*vec.x);
    double dist (const LINE& rhs) const {
       POS intersect_point = intersect(rhs);
        if (intersect_point == PARALLEL) {
            return dist(rhs.start);
        return 0;
    friend ostream& operator << (ostream& out, const LINE& line) {
        out << line.start << "-->" << line.end << " vec: " << line.
   vec;
        return out;
class LINESEG : public LINE {
public:
```

};

```
LINESEG() : LINE(POS(0, 0))  {}
LINESEG(const LINE& input) : LINE(input) {}
LINESEG(const POS& start, const POS& end) : LINE(start, end) {}
bool on_lineseg(const POS& a) const {
    if (!on_line(a)) return false;
    bool first, second;
    if (\text{vec.} x \ge 0) first = (\text{a.} x \ge \text{start.} x) \& \& (\text{a.} x \le \text{end.} x);
    else first = (a.x \le start.x)&&(a.x \ge end.x);
    if (\text{vec.y} \ge 0) second = (\text{a.y} \ge \text{start.y}) \&\& (\text{a.y} \le \text{end.y});
    else second = (a.y \le start.y) & (a.y \ge end.y);
    return first&&second;
bool operator == (const LINESEG& rhs) const {
    return ( (rhs.start = start && rhs.end = end) ||
           (rhs.start = end \&\& rhs.end = start));
bool operator == (const LINE& rhs) const {
    return this -> LINE :: operator == (rhs);
T dot(const LINESEG& rhs) const {
    return vec.x*rhs.vec.x + vec.y*rhs.vec.y;
}
T cross (const LINESEG& rhs) const {
    return vec.x*rhs.vec.y - vec.y*rhs.vec.x;
bool clockwise (const LINE& a) const { /* to see if LINE a is in b
's clockwise way */
    return cross(a) > 0;
double dist (const POS& a) const {
    double ortho_dist = this->LINE::dist(a);
    LINE ortho_line = build_orthogonal(a);
    POS intersect_point = this->LINE::intersect(ortho_line);
    if (on_lineseg(intersect_point)) return ortho_dist;
    else return min(a.dist(this->start), a.dist(this->end));
double dist(const LINE& line) const {
    POS intersect_point = this->LINE::intersect(line);
    if (intersect_point == COLINE) return 0;
    if (intersect_point == PARALLEL) return dist(line.start);
```

```
if (on_lineseg(intersect_point)) return 0;
        return min(line.dist(start), line.dist(end));
    double dist (const LINESEG& line) const {
        return min( min(dist(line.start), dist(line.end)),
                    min(line.dist(start), line.dist(end)));
   POS intersect (const LINESEG& rhs) const {
       LINE alb1(start, rhs.start);
       LINE a1b2(start, rhs.end);
       LINE bla1(rhs.start, start);
       LINE b1a2(rhs.start, end);
       POS tmp(this->LINE::intersect(rhs));
        if (tmp == COLINE) {
            if ((start=rhs.start) && (!rhs.on_lineseg(end)) && (!
   on_lineseg(rhs.end)) ) return start;
            if ((start=rhs.end) && (!rhs.on_lineseg(end)) && (!
   on_lineseg(rhs.start)) ) return start;
            if ((end=rhs.start) && (!rhs.on_lineseg(start)) && (!
   on_lineseg(rhs.end)) ) return end;
            if ((end=rhs.end) && (!rhs.on_lineseg(start)) && (!
   on_lineseg(rhs.start)) ) return end;
            if (on_lineseg(rhs.start) || on_lineseg(rhs.end) || rhs.
   on_lineseg(start) || rhs.on_lineseg(end)) return COLINE;
            return NO_INTERSECT;
        bool intersected = ((cross(a1b1)*cross(a1b2)<0) \&\& (rhs.
   cross(b1a1)*rhs.cross(b1a2)<0);
        if (!intersected) return NO_INTERSECT;
        if (!on_lineseg(tmp) || !rhs.on_lineseg(tmp)) return
   NO_INTERSECT;
        return tmp;
inline bool cmp_half_plane(const LINE &a, const LINE &b){
    if (fabs (a.angle-b.angle) < EPS) return cross (a.start, a.end, b.
   start) < 0:
    return a.angle > b.angle;
void half_plane_intersection(LINE* a, LINE* need, POS* answer, int &n
   ) {
```

};

```
int m = 1, front = 0, rear = 1;
    sort(a, a+n, cmp_half_plane);
    for (int i = 1; i < n; ++i)
        if (fabs(a[i].angle-a[m-1].angle) > EPS) a[m++] = a[i];
    need[0] = a[0], need[1] = a[1];
    for (int i = 2; i < m; ++i){
        while (front < rear&&cross(a[i].start, a[i].end, need[rear].
    intersect (need [rear -1]) < 0) rear --;
        while (front < rear&&cross(a[i].start, a[i].end, need[front].
    intersect (need [front+1]) < 0) front++;
        need[++rear] = a[i];
    while (front < rear&&cross (need [front].start, need [front].end, need [
    rear ]. intersect (need [rear -1]))<0) rear --;
    while (front < rear && cross (need [rear]. start, need [rear].end, need [
   front ]. intersect (need [front +1]))<0) front ++;
    if (front=rear) return;
    n = 0;
    for (int i=front; i<rear; ++i) answer[n++] = need[i].intersect(
   need[i+1]:
    if (rear>front+1) answer [n++] = need [front].intersect (need [rear]);
void rotating_calipers(int& ans, POS* need, int& n) {
    --n:
    if (n == 2)  {
        ans = need[0]. dist(need[1]);
        return;
    }
    int now = 2;
    for (int i = 0; i < n; ++i) {
        LINE target (need [i], need [i+1]);
        double pre = target.dist(need[now]);
        for (; now != i; now = (now+1)\%(n)) {
            double tmp = target.dist(need[now]);
            if (tmp < pre) break;
            pre = tmp;
        now = (now-1+n)\%n;
        ans = max(ans, max(need[i].dist(need[now]), need[i+1].dist(
   need [now])));
class POLYGON {
public:
```

```
vector < POS> point;
vector <LINESEG> line;
void add_points(const POS& x) {
    point.push_back(x);
void add_points(const int& x, const int& y) {
    point.push_back(POS(x,y));
void build_line() {
    if (line.size() != 0) return; /* if it has build */
    for (int i = 1; i < point.size(); ++i) {
        line.push_back(LINESEG(point [i], point [i-1]);
    line.push_back(LINESEG(point [0], point [point.size()-1]);
double area() {
    double ans = 0;
    vector <LINESEG> tmp;
    for (int i = 0; i < point.size(); ++i) {
        tmp.push_back(LINESEG(point[i]));
    tmp.push_back(LINESEG(point [0]));
    for (int i = 1; i < tmp. size(); ++i) {
        ans += tmp[i-1].cross(tmp[i]);
    return 0.5 * fabs (ans);
bool in_polygon(const POS& a, const POS& left_top = LEFT_TOP) {
    for (int i = 0; i < point.size(); ++i) {
        if (a == point[i]) return true; /* a is polygon's point
*/
    build_line();
    for (int i = 0; i < line.size(); ++i) {
        if (line[i].on_line(a)) {
            return true; /* a is on polygon's line */
```

```
POS endpoint(left_top); /* should be modified according to
   problem */
       LINESEG ray(a, endpoint);
        bool touch_endpoint = false;
        do {
            touch_endpoint = false;
            for (int i = 0; i < point.size(); ++i) {
                if (ray.on_lineseg(point[i])) {
                    touch_endpoint = true;
                    break;
            if (touch_endpoint) ray.modify(-1, 0); /* should be
   modified according to problem */
        } while (touch_endpoint);
        int times = 0;
        for (int i = 0; i < line.size(); ++i) {
            POS tmp(ray.intersect(line[i]));
            if (tmp == NO_INTERSECT || tmp == PARALLEL) {
                continue;
            ++times;
        return (times&1);
};
int main() {
    return 0;
```

8 Simple Tabulation Hash

```
import java.util.*;
class HashTable{
    long[] key;
    Main.Entry[] content;
    SimpleTabulationHash hash;

HashTable(long universeSize, int sizeBit){
        key = new long[1<<sizeBit];
        content = new Main.Entry[1<<sizeBit];
        Arrays.fill(key, -1);</pre>
```

```
hash = new SimpleTabulationHash(universeSize, sizeBit);
    //returns index if found, -1 if not
    int contains Key (long x) {
        int hashValue = hash.hashCode(x);
        for (int i=hashValue;; i++){
            if(i = key.length) i = 0;
            if(key[i] = -1) return -1;
            if(key[i] == x) return i;
    void put(long x, Main.Entry entry){
        int hashValue = hash.hashCode(x);
        for (int i=hashValue;; i++){
            if(i = key.length) i = 0;
            if(key[i] == -1)
                \text{key}[i] = x;
                content[i] = entry;
                return;
   Main. Entry get (long x) {
        return content [contains(x)];
class SimpleTabulationHash {
    final static int bit = 16, mask = (1 << bit) -1;
   int C;
    int[][] table;
    SimpleTabulationHash(long universeSize, int tableBit) { // table
   size is givin in 2<sup>n</sup>
        C = 0:
        while (universe Size > 0) {
            universeSize >>= bit;
            C++:
        table = new int[C][mask+1];
       // System.err.println("C = "+C);
        Random random = new Random();
        int cutmask = (1 << tableBit) -1;
```

```
//System.err.println("tablebit: "+tableBit+", cutmask : "+
cutmask);
    for(int i=0;i<C;i++){
        for(int j=0;j<=mask;j++) table[i][j] = random.nextInt()&
cutmask;
    }
}

int hashCode(long x) {
    int result = 0;
    for(int i=0;i<C;i++){
        result ^= table[i][(int)(x&mask)];
        x >>= bit;
    }
    return result;
}
```

9 IDA*

```
int search (STATE& now, int g, int bound) {
    int f = g + now. heuri;
    if (f > bound) return f;
    if (is_goal(now)) return FOUND;
    int min = INF;
    for next in successors (now):
        int t = search(state, g+cost(now, next), bound);
        if (t == FOUND) return FOUND;
        if (t < min) min = t;
    return min;
void IDAStar() {
   STATE init (input);
    int bound = init.heuri;
    while (bound <= MAXI) ·
        int t = search(init, 0, bound);
        if (t == FOUND) return FOUND;
        if (t == INF) return NOT_FOUND;
        bound = t;
```

10 inverse

```
long long inverse (long long b, long long mod=MOD) {
    long long k[2][2], n[2][2], u1, u2;
   k[0][0] = k[1][1] = 1;
   k[0][1] = k[1][0] = 0;
   u1 = mod, u2 = b;
    while (u2) {
        long long div = u1/u2;
        long long remind = u1\%u2;
        n[0][0] = k[1][0];
        n[0][1] = k[1][1];
        n[1][0] = k[0][0] - k[1][0] * div;
        n[1][1] = k[0][1] - k[1][1] * div;
        for (int i = 0; i < 2; ++i) {
            for (int j = 0; j < 2; ++j) {
                k[i][j] = n[i][j];
        u1 = u2;
        u2 = remind;
    while (k[0][1] < 0) k[0][1] += mod;
    if (((k[0][1]*(b%mod))%mod+mod)%mod!=1ll) printf("%lld^-1 doesn't
    exist under mod %11d \n", b, mod);
    return k[0][1];
```

11 Karatsuba (FFFT)

```
static class Karatsuba{
  int maxHeight;
  long[][][] buffer; //h1, l1, m1, h2, l2, m2, hh, ll, mm
  Karatsuba(int maxHeight){
    this.maxHeight = maxHeight;
```

```
buffer = new long [maxHeight][9][];
    for (int i=6; i < maxHeight; i++){
         for (int j=0; j<6; j++) buffer [i][j] = \text{new long}[(1<< i)>>1];
         for (int j=6; j<9; j++) buffer [i][j] = new long[1<<i];
void multiply(long[] a, long[] b, long[] result, int depth){
    int size = 1 < depth, mid = size >>1;
    if (depth \le 5)
         Arrays. fill (result, 0);
         for (int i=0; i < a. length; i++){
             for (int j=0; j< b. length; j++) result [i+j] += a[i]*b[j];
         return;
    for (int i = 0; i < mid; i++)
         buffer [depth][0][i] = a[i+mid];
         buffer [depth][1][i] = a[i];
         buffer [depth][2][i] = a[i+mid] + a[i];
         buffer [depth][3][i] = b[i+mid];
         buffer [depth][4][i] = b[i];
         buffer [depth][5][i] = b[i+mid] + b[i];
    multiply (buffer [depth][0], buffer [depth][3], buffer [depth
[6], depth -1);
    multiply (buffer [depth] [1], buffer [depth] [4], buffer [depth
[7], depth -1;
    multiply (buffer [depth] [2], buffer [depth] [5], buffer [depth
[8], depth -1);
    Arrays. fill (result, 0);
    for (int i=0; i < size; i++){
         result [i+size] += buffer [depth][6][i];
         result [i] += buffer [depth][7][i];
         result [i+mid] += buffer [depth][8][i] - buffer [depth][6][i
| - buffer [depth] [7] [i];
```

12 KM

```
#include <iostream>
#include <cstdio>
#include <algorithm>
```

```
#include <cstring>
#define MAX 404
#define INF 0x7ffffffff
using namespace std;
int num; // total num of node
int path [MAX] [MAX];
bool visit_x [MAX], visit_y [MAX];
int parent [MAX], weight_x [MAX], weight_y [MAX];
bool find (int i) {
     visit_x[i] = true;
    for (int j = 0; j < num; ++j) {
         if (visit_y[j]) continue;
         if (weight_x[i] + weight_y[j] = path[i][j]) {
             visit_y[j] = true;
             if (parent[j] = -1 \mid find(parent[j])) {
                 parent[j] = i;
                 return true;
     return false;
int weighted_hangarian() {
     /* remember to initial weight_x (max weight of node's edge)*/
    /* initialize */
     for (int i = 0; i < num; ++i) {
         weight_v[i] = 0;
         parent[i] = -1;
    for (int i = 0; i < num; ++i) {
         while (1) {
             memset(visit_x, false, sizeof(visit_x));
             memset(visit_v, false, sizeof(visit_v));
             if (find(i)) break;
             int lack = INF;
             for (int j = 0; j < num; ++j) {
                 if (visit_x[j]) 
                     for (int k = 0; k < num; ++k) {
                         if (!visit_v[k]) {
                             lack = min(lack, weight_x[j] + weight_y[k]
      - path[j][k]);
```

```
}
}
}

}

if (lack == INF) break;
// renew label
for (int j = 0; j < num; ++j) {
    if (visit_x[j]) weight_x[j] -= lack;
    if (visit_y[j]) weight_y[j] += lack;
}

int ans = 0;
for (int i = 0; i < num; ++i) {
    ans += weight_x[i];
    ans += weight_y[i];
}
return ans;
}
</pre>
```

13 Linear Prime

```
#include <cstdio>
#include <cmath>
#include <vector>
using namespace std;
#define N (10000000+5)
bool killed [N] = \{0\};
int kill [N] = \{0\};
int prime [N];
long long numOfPrime=0;
void makeTable(){
    long long limit;
    for (long long i=2; i < N; i++)
        if(kill[i]==0){
            prime[numOfPrime++] = i;
            limit = i:
        else{
            limit = kill[i];
```

14 Mod Combine

```
int modCombine(int x, int a, int y, int b) \{//\text{ans mod } x = a, \text{ans mod } y = b;

int ans = x * (x^{(-1)}) \pmod{y} * b + y * (y^{(-1)}) \pmod{x} * a;

ans %=(x*y);

return ans;
}
```

15 Range Tree 2D, kth number

```
#include <cstdio>
#include <cmath>
#include <algorithm>

using namespace std;

struct COORDINATE {
    int x, y;
};

bool cmp(const COORDINATE& x, const COORDINATE& y) {
    return x.x < y.x;
}

/* x: data, y: index */
struct RangeTree2D {</pre>
```

```
COORDINATE **container;
bool **is_left;
int **left, **right, *input, length, rank, capacity;
void init(int *input, int length) {
    this->input = input;
    this -> length = length;
    rank = 1;
    while ((1 << rank++) < length);
    capacity = 1 << (rank-1);
    container = new COORDINATE*[rank], left = new int*[rank],
right = new int * [rank];
    is_left = new bool*[rank];
    for (int i = 0; i < rank; ++i) {
        container [i] = new COORDINATE [capacity];
        left[i] = new int[capacity];
        right[i] = new int[capacity];
        is_left[i] = new bool[capacity];
    for (int i = 0; i < capacity; ++i) {
        container [0][i].x = i>=length?0:input[i];
        container [0][i].y = i;
    sort (container [0], container [0] + length, cmp);
    build (rank-1, 0, capacity-1);
void build(int height, int start, int finish) {
    if (height == 0) return;
    if (start == finish) {
        build (height -1, start, finish);
        container [height] [start] = container [height-1] [start];
        return:
    int middle = start + (1 << (height -1));
    build (height -1, start, middle -1);
    build (height -1, middle, finish);
    int now = start, l_index = start, r_index = middle;
    while (now <= finish) {
        left[height][now] = l_index;
        right [height] [now] = r_index;
        if (l_index < middle && (r_index > finish || container [
height - 1 [l_index]. v \le container[height - 1][r_index]. <math>v) {
             container[height][now] = container[height-1][l_index]
];
```

```
is_left [height][now] = true;
                ++l_iindex;
            else {
                container [height] [now] = container [height -1] [r_index
   ];
                is_left [height][now] = false;
                ++r_index;
            ++now;
    /* 0-base index, k 1-base */
    int query(int start, int finish, int k) {
        return query (rank-1, start, finish, k);
    int query (int height, int start, int finish, int k) {
        if (height == 0) return container [height] [start].x;
        int left_size = left[height][finish] - left[height][start];
        if (is_left [height] [finish]) ++left_size;
        int right_size = finish-start+1-left_size;
        if (left_size >= k) return query(height-1, left[height][start
   ], min(left[height][finish], left[height][start]+left_size -1), k)
        else return query(height-1, right[height][start], min(right[
   height [ finish ], right [ height ] [ start] + right_size -1), k-left_size)
};
int input[100005];
int main () {
    int n, m;
    scanf("%d%d", &n, &m);
    for (int i = 0; i < n; ++i) {
        scanf("%d", &input[i]);
    RangeTree2D range;
    range.init(input, n);
    for (int i = 0; i < m; ++i) {
        int a, b, k;
        scanf("%d%d%d", &a, &b, &k);
        printf("%d \setminus n", range.query(a-1, b-1, k));
    return 0;
```

```
}
/* Pass POJ 2104 */
```

16 Range Tree 2D, rectangle

```
struct POS {
    int x, y, value, cost, segid;
   POS() {}
   POS(int x, int y, int value, int cost):x(x), y(y), value(value),
   cost(cost) {}
  bool operator < (const POS &rhs) const {
    return this -> v < rhs.v;
} pos[100005];
struct SegmentTree{
    unordered_map<int, int> trans;
  int rank, capacity, length;
 POS *input;
    int *tree;
    SegmentTree() {}
  void init(POS* input, int length){
        trans.clear();
    this -> input = input;
    this->length = length;
    rank = 1:
    while ((1 << rank++) < length);
    capacity = 1 < (rank - 1);
    tree = new int [capacity << 1];
    build (1, capacity, capacity <<1);
  ~SegmentTree(){
        delete [] tree;
  int build(int index, int left, int right){
    if(index >= left)
      tree[index] = getInput(index);
            trans[tree[index]] = index;
            return tree[index]:
    int middle = (left+right) >> 1;
    int left_value = build(lc(index), left, middle);
```

```
int right_value = build(rc(index), middle, right);
  return tree[index] = max(left_value, right_value);
  void update(int origin_value, int value) {
      int index = trans[origin_value];
      tree[index] = value;
      maintain (index >>1);
void maintain(int index){
      tree[index] = max(tree[lc(index)], tree[rc(index)]);
  if(index == 1) return;
      maintain (index >>1);
int query(int start, int finish){
  return query(1, capacity, capacity <<1, capacity+start, capacity+
 finish+1):
int query(int index, int left, int right, int start, int finish){
  if (left = start && right = finish) return tree[index];
  int middle = (left+right) >> 1;
  if (finish <= middle) return query(lc(index), left, middle, start,
  if (start >= middle) return query (rc(index), middle, right, start,
  finish);
  int left_value = query(lc(index), left, middle, start, middle);
  int right_value = query(rc(index), middle, right, middle, finish)
  return max(left_value, right_value);
int getInput(int index){
  index -= capacity;
  if (index < length) return input [index]. value;
  return 0:
int lc(int x){
  return x << 1;
int rc(int x){
  return (x << 1)+1:
```

```
bool cmp(const POS& x, const POS& v) {
    return x.x==y.x? x.y<y.y: x.x<y.x;
struct rangeTree2D {
    unordered_map<int, int> trans;
   POS **container, *input;
    SegmentTree *seg;
    int rank, capacity, length;
    int *idx:
    void init(POS* input, int length) {
        trans.clear();
        sort (input, input+length, cmp);
        for (int i = 0; i < length; ++i) this->trans[input[i].value]
   = i;
        this -> input = input;
        this -> length = length;
        rank = 1:
        while ((1 << rank++) < length);
        capacity = 1 < (rank - 1);
        container = new POS*[rank];
        seg = new SegmentTree[capacity <<1];</pre>
        idx = new int[length];
        POS tmp(input[length-1].x+1, input[length-1].y+1, 0, 0);
        for (int i = 0; i < rank; ++i) {
            container [i] = new POS [capacity];
        for (int i = 0; i < length; ++i) {
            container [0][i] = input[i];
            idx[i] = input[i].x;
        for (int i = length; i < capacity; ++i) container [0][i] = tmp
        sort (idx, idx+length);
        // build
        int segid = 0;
        for (int height = 0; height < rank - 1; ++ height) {
            for (int i = 0; i < capacity; i += (2 < height)) {
                merge (container [height]+i, container [height]+i+(1<<
   height),
                       container [height]+i+(1<<height), container [
   height]+i+(2<< height),
                       container [height+1]+i);
                container [height +1][i]. segid = segid;
                seg [segid++].init (container [height+1]+i, (2<<height))
```

```
void decrease(int value) {
    int index = trans[value];
    container [0][index]. value = 0;
    maintain (1, (index >> 1) << 1, value);
int range_query(int left, int right, int bottum, int top) {
    left = lower_bound(idx, idx+length, left)-idx;
    right = upper_bound(idx, idx+length, right)-idx;
    POS _bottum(0, bottum, 0, 0), _top(0, top, 0, 0);
    int ans = range_query(rank-1, 0, left, right, _bottum, _top);
    if (ans != 0) decrease (ans);
    if (ans = 0) return 0;
    return container [0][trans[ans]].cost;
void maintain(int height, int start, int value) {
    if (height == rank) return;
    int myId = container[height][start].segid;
    seg[mvId].update(value, 0);
    maintain(height+1, (start>>(height+1))<<(height+1), value);
int range_query(int height, int start, int left, int right, const
POS& bottum, const POS& top) {
    if (\text{start} > = \text{right} \mid | \text{start} + (1 < \text{height}) < = \text{left}) \text{ return } 0;
    if (start >= left \&\& start + (1 << height) <= right) {
         int st = lower_bound(container[height]+start, container[
height]+start+(1<<height), bottum)-container[height]-start;
        int ed = upper_bound(container[height]+start, container[
height | + start + (1 << height), top) - container [height] - start;
        --ed:
         if (ed < st) return 0:
         if (height == 0) return container [0] [start]. value;
         int myId = container[height][start].segid;
        return seg[myId].query(st, ed);
    --height;
    return max(range_query(height, start, left, right, bottum,
top),
             range_query(height, start+(1<<height), left, right,
bottum, top));
```

};

17 Scan (JAVA)

```
import java.io.*;
import java.util.*;
public class Scan{
  BufferedReader buffer;
  StringTokenizer tok;
  Scan(){
    buffer = new BufferedReader(new InputStreamReader(System.in));
  boolean hasNext(){
    while (tok=null | !tok.hasMoreElements()) {
      try {
        tok = new StringTokenizer(buffer.readLine());
      }catch(Exception e){
        return false:
    return true;
  String next(){
    if (hasNext()) return tok.nextToken();
    return null;
  String nextLine() {
    if (hasNext()) return tok.nextToken("\n");
    return null:
  int nextInt(){
    return Integer.parseInt(next());
  long nextLong(){
    return Long.parseLong(next());
  double nextDouble(){
```

return Double.parseDouble(next()); }

18 Segment Tree

```
struct SegmentTree{
 int rank, capacity, length;
 int *input, *tree;
    SegmentTree() {}
 void init(int* input, int length){
    this -> input = input;
    this->length = length;
   rank = 1:
    while ((1 << rank++) < length);
    capacity = 1 << (rank - 1);
   tree = new int [capacity << 1];
    build (1, capacity, capacity <<1);
  ~SegmentTree(){
        delete [] tree;
 int build(int index, int left, int right){
   if(index >= left)
      return tree[index] = getInput(index);
   int middle = (left+right) >> 1;
   int left_value = build(lc(index), left, middle);
   int right_value = build(rc(index), middle, right);
    return tree[index] = max(left_value, right_value);
 int query (int start, int finish) {
   return query(1, capacity, capacity<<1, capacity+start, capacity+
   finish+1);
 int query (int index, int left, int right, int start, int finish) {
   if(left == start && right == finish) return tree[index];
   int middle = (left+right) >> 1;
    if (finish <= middle) return query(lc(index), left, middle, start,
    finish);
```

```
if(start >= middle) return query(rc(index), middle, right, start,
    finish);
int left_value = query(lc(index), left, middle, start, middle);
int right_value = query(rc(index), middle, right, middle, finish)
;
    return max(left_value, right_value);
}

int getInput(int index){
    index == capacity;
    if(index < length) return input[index];
    return 0;
}

int lc(int x){
    return x<<1;
}

int rc(int x){
    return (x<<1)+1;
}
</pre>
```

19 Splay Tree

```
public class SplayTree{
   Node root;
   int size;

   SplayTree(){
      root = null;
      size = 0;
   }

   public boolean containsKey(int target){
      return splay(target);
   }

   public void add(int target){
      // System.out.println("add "+target);
      if(root == null){
        root = new Node(null, target);
        return;
      }
      Node now = root;
```

```
while (true) {
    if (now.key == target) break;
    if (target < now.key) {</pre>
      if(now.lchild = null)
        now.lchild = new Node(now, target);
        break:
      }else now = now.lchild;
    }else{
      if (now.rchild = null) 
        now.rchild = new Node(now, target);
        break:
      } else now = now.rchild;
  splay(target);
public void delete(int target){
    System.out.println("delete "+target);
  if (!containsKey(target)) return;
  Node l = root.lchild;
  Node r = root.rchild;
  if(l = null){
    root = r;
  }else l.parent = null;
  if(r = null){
    root = 1;
  }else r.parent = null;
  if (root=null | root.key != target) return;
  Node lMax = l;
  while (lMax.rchild != null) lMax = lMax.rchild;
  splay (lMax.key);
  lMax.rchild = r:
private boolean splay(int target){
    System.out.println("splay "+target);
  while (true) {
    if (root == null) return false;
    if(root.key == target) return true;
    if (target < root.key){</pre>
      if (root.lchild = null) return false;
      Node l = root.lchild;
      if(l.key == target){
        root = 1;
        rightRoatation(1);
        return true;
```

```
if (target < l. kev) {
        if (1.1child == null) return false;
        Node a = l.lchild;
        root = a;
        rightRoatation(1);
        rightRoatation(a);
      }else{
        if (l.rchild = null) return false;
        Node b = l.rchild;
        root = b:
        leftRoatation(b);
        rightRoatation(b);
    }else{
      if (root.rchild == null) return false;
      Node r = root.rchild;
      if(r.key == target){
        root = r;
        leftRoatation(r);
        return true;
      if (target>r.key) {
        if (r.rchild == null) return false;
        Node d = r.rchild;
        root = d;
        leftRoatation(r);
        leftRoatation(d);
      }else{
        if (r.lchild == null) return false;
        Node c = r.lchild;
        root = c:
        rightRoatation(c);
        leftRoatation(c);
void print(Node now){
 if (now = null) 
    System.out.print("-1");
    return:
 System.out.print(now.key+"");
  print (now.lchild);
  print(now.rchild);
```

```
void rightRoatation(Node x){
 Node r = x.parent.parent;
 Node p = x.parent;
 Node b = x.rchild;
 x.rchild = p;
  if (p != null) p.parent = x;
  if(p != null) p.lchild = b;
 if(b != null) b.parent = p;
 x.parent = r;
 if(r != null) r.lchild = x;
void leftRoatation(Node x){
 Node r = x.parent.parent;
 Node p = x.parent;
 Node b = x.lchild;
 x.lchild = p;
  if (p != null) p.parent = x;
 if(p != null) p.rchild = b;
 if (b != null) b.parent = p;
 x.parent = r;
  if(r != null) r.rchild = x;
class Node{
 Node parent, lchild, rchild;
 int key;
 Node(Node parent, int key){
    this.parent = parent;
   lchild = rchild = null;
    this.key = key;
```

20 Suffix Array

```
import java.io.*;
import java.util.*;
```

```
class SuffixArray {
    Entry[] entries;
    int[] rank;
    int length;
    Suffix Array (CharSequence S) {
        length = S.length();
        rank = new int[length];
        entries = new Entry[length];
        int[] temp = new int[length];
        int counter:
        for (int i=0; i< length; i++)
             entries [i] = new Entry(i);
             entries [i]. a = S. charAt(i) - 'a';
        Arrays.parallelSort(entries);
        rank[entries[0].index] = temp[0] = counter = 0;
        for (int i=1; i < length; i++)
             if (entries [i]. a != entries [i-1].a) counter++;
            rank [entries [i].index] = temp[i] = counter;
        int step = 1;
        while (step < length) {
            for (int i=0; i < length; i++)
                 entries [i]. a = temp[i];
                 entries[i].b = rank[(entries[i].index+step)%length];
             countingSort (entries);
            rank[entries[0].index] = temp[0] = counter = 0;
            for (int i=1; i < length; i++){
                 if (entries [i].a! = entries [i-1].a || entries [i].b!=
   entries [i-1].b) counter++;
                 rank [entries [i].index] = temp[i] = counter;
             step \ll 1;
    }
    void countingSort(Entry[] input){
        int[] counter = new int[length];
        Entry [] temp = new Entry [length];
        for (int i=0; i < length; i++) counter [input [i].b]++;
        for (int i=1; i < length; i++) counter [i] += counter [i-1];
        for (int i=length -1; i > 0; i - -) temp[--counter[input[i].b]] =
   input[i]:
        Arrays. fill (counter, 0);
```

```
for (int i=0; i < length; i++) counter [temp[i].a]++;
     for (int i=1; i < length; i++) counter [i] += counter [i-1];
     for (int i=length-1; i>=0; i--) input [--counter[temp[i].a]] =
temp[i];
class Entry implements Comparable<Entry>{
    int a, b, index;
    Entry(int index){
         this.index = index;
    void assign(Entry rhs){
         a = rhs.a;
         b = rhs.b;
     @Override
     public int compareTo(Entry rhs){
         return a - rhs.a;
```

21 Treap

```
inline int size (Treap *target) {
    if (!target) return 0;
    return target -> size;
inline void pull(Treap *target) {
    target \rightarrow size = size(target \rightarrow lc) + size(target \rightarrow rc) + 1;
void reverseIt(Treap *target) {
    if (!(target->reverse)) return;
    Treap *lc = target ->lc;
    target -> lc = target -> rc;
    target \rightarrow rc = lc;
    target -> reverse = false;
    if (target -> lc) (target -> lc -> reverse) ^= true;
    if (target ->rc) (target ->rc->reverse) ^= true;
Treap* merge(Treap *lhs, Treap *rhs) {
    if (!lhs | !rhs) return lhs? lhs: rhs;
    if (lhs->priority > rhs->priority) {
         reverseIt(lhs):
         lhs \rightarrow rc = merge(lhs \rightarrow rc, rhs);
         pull(lhs);
         return lhs;
    else {
         reverseIt (rhs);
         rhs \rightarrow lc = merge(lhs, rhs \rightarrow lc);
         pull(rhs):
         return rhs;
void split (Treap *target, Treap *&lhs, Treap *&rhs, int k) {
    if (!target) lhs = rhs = NULL;
    else if (k > target \rightarrow key) {
         lhs = target;
         split (target -> rc, lhs -> rc, rhs, k);
         pull(lhs);
    }
    else {
         rhs = target;
         split (target -> lc, lhs, rhs -> lc, k);
         pull(rhs):
```

```
Treap* insert (Treap *target, int key, int value) {
    Treap *lhs, *rhs;
    split (target, lhs, rhs, key);
    return merge (merge (lhs, new Treap (key, value)), rhs);
/* split by size */
void splitSize(Treap *target, Treap *&lhs, Treap *& rhs, int k) {
    if (!target) lhs = rhs = NULL:
    else {
        reverseIt (target):
        if (size(target->lc) < k) {
            lhs = target;
             splitSize(target->rc, lhs->rc, rhs, k-size(target->lc)-1)
            pull(lhs);
        else {
             rhs = target;
             splitSize(target->lc, lhs, rhs->lc, k);
             pull(rhs);
/* do lazv tag */
Treap* reverseIt (Treap *target, int lp, int rp) {
    Treap *A, *B, *C, *D;
    splitSize (target, A, B, lp-1);
    splitSize(B, C, D, rp-lp+1);
    C->reverse ^= true;
    return merge (merge (A, C), D);
/* delete singal key */
Treap* del(Treap *target, int key) {
    if (target->key == key) return merge(target->lc, target->rc);
    else if (target->kev > kev) target->lc = del(target->lc, key);
    else target ->rc = del(target ->rc, key);
    pull(target);
    return target;
T findK(Treap *target, int k) {
    if (size(target \rightarrow lc)+1 == k) return target \rightarrow key;
```

```
else if (size(target->lc) < k) return findK(target->rc, k-size(
    target->lc)-1);
    else return findK(target->lc, k);

/* find the kth's value */
T1 findK(Treap *target, int k) {
    reverseIt(target);
    if (size(target->lc)+1 == k) return target->value;
    else if (size(target->lc) < k) return findK(target->rc, k-size(
    target->lc)-1);
    else return findK(target->lc, k);
}

int main () {
    return 0;
}

/* pass POJ2761, CF gym 100488 pL */
```

22 Z Algorithm

```
void z_algorithm(string& input) {
    int z[1000005];
    memset(z, 0, sizeof(z));
    z[0] = input.size();
    int L = 0, R = 1;
    for (int i = 1; i < input.size(); ++i) {
        if (R <= i || z[i-L] >= R-i) {
            int x = ((i>=R)? i: R);
            while (x < input.size() && input[x] == input[x-i]) x++;
            z[i] = x-i;
            if (i < x) {
                L = i;
                R = x;
            }
        }
        else {
            z[i] = z[i-L];
        }
}</pre>
```