

Bleichenbacher RSA Signature Forgery (2006)

oalieno



PKCS

PKCS

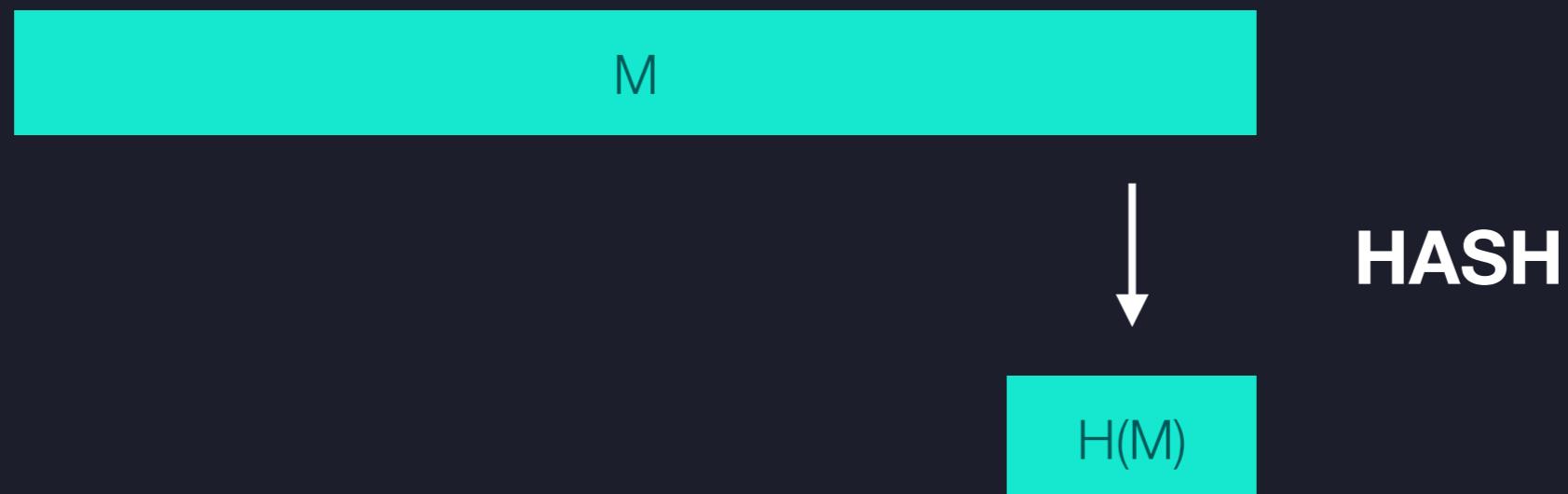
- PKCS (Public Key Cryptography Standards) 是公鑰密碼標準
- 制定了一系列從 PKCS#1 到 PKCS#15 的標準
- 其中 PKCS#1 是 RSA Cryptography Standard

ASN.1

- ASN.1 是高階的抽象標準
- 具體的實作編碼規則有 : BER, CER, DER, PER, XER

PKCS#1 1.5 Signature

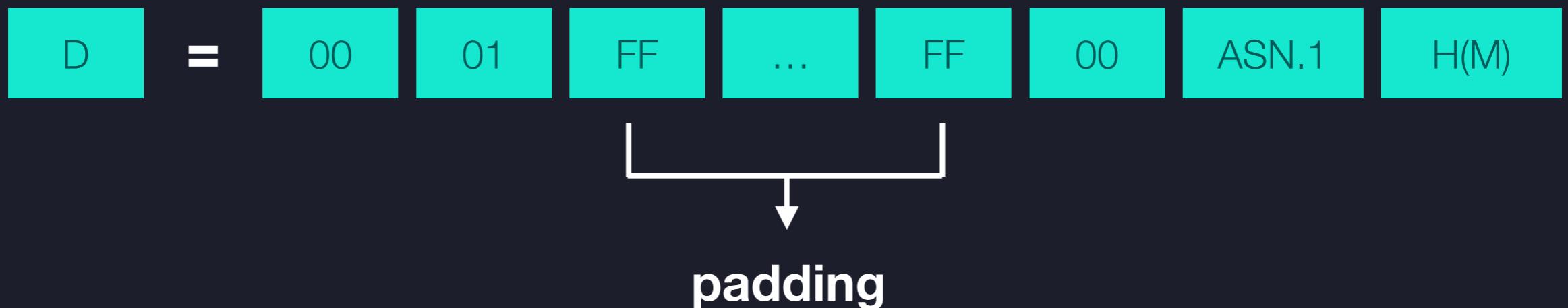
<https://tools.ietf.org/html/rfc2313>



PKCS#1 1.5 Signature

<https://tools.ietf.org/html/rfc2313>

- ASN.1 是編碼數據的格式，這裡紀錄了使用的 hash 演算法



PKCS#1 1.5 Signature

<https://tools.ietf.org/html/rfc2313>

$$D^d \% n = S$$

Sign

Step 3 : RSA encryption

PKCS#1 1.5 Signature

<https://tools.ietf.org/html/rfc2313>

$$s^e \% n = d$$

Verify

Step 1 : RSA decryption

PKCS#1 1.5 Signature

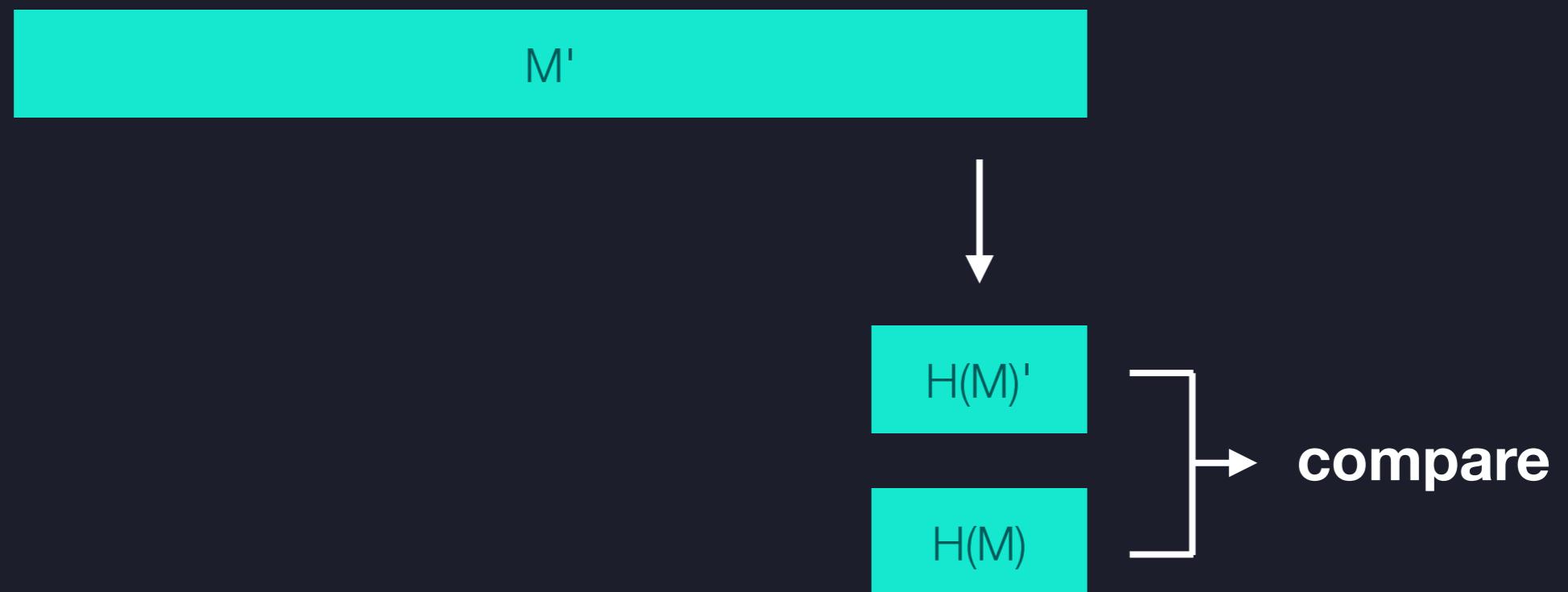
<https://tools.ietf.org/html/rfc2313>

- 需要 parse 這個格式取出 $H(M)$
- 這個標準沒有說要怎麼 parse
- 如果 e 太小且沒有正確的 parse，就有機會偽造簽章



PKCS#1 1.5 Signature

<https://tools.ietf.org/html/rfc2313>



Bleichenbacher RSA Signature Forgery (2006)

Bleichenbacher RSA Signature Forgery (2006)

<https://mailarchive.ietf.org/arch/msg/openpgp/5rnE9ZRN1AokBVj3VqbIGP63QE>

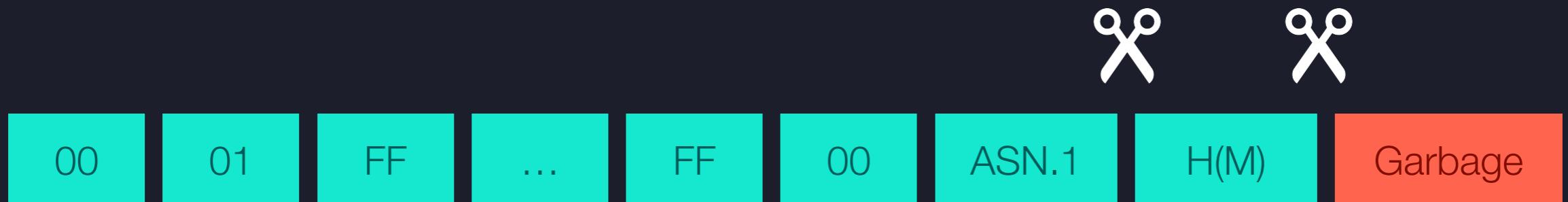
- 又稱作 BB06
- 針對 PKCS#1 1.5 (RFC 2313)
- RSA 簽章偽造



Bleichenbacher RSA Signature Forgery (2006)

<https://mailarchive.ietf.org/arch/msg/openpgp/5rnE9ZRN1AokBVj3VqbIGP63QE>

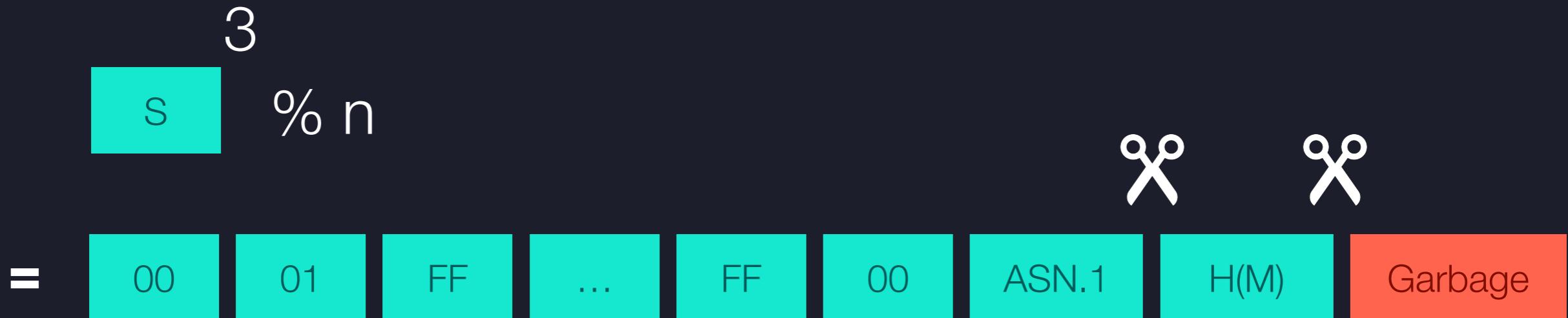
- 實作缺陷：可以有多餘的字元在後面
- parse 的時候直接取出後面固定長度的 $H(M)$
- 沒有檢查後面還有沒有東西



Bleichenbacher RSA Signature Forgery (2006)

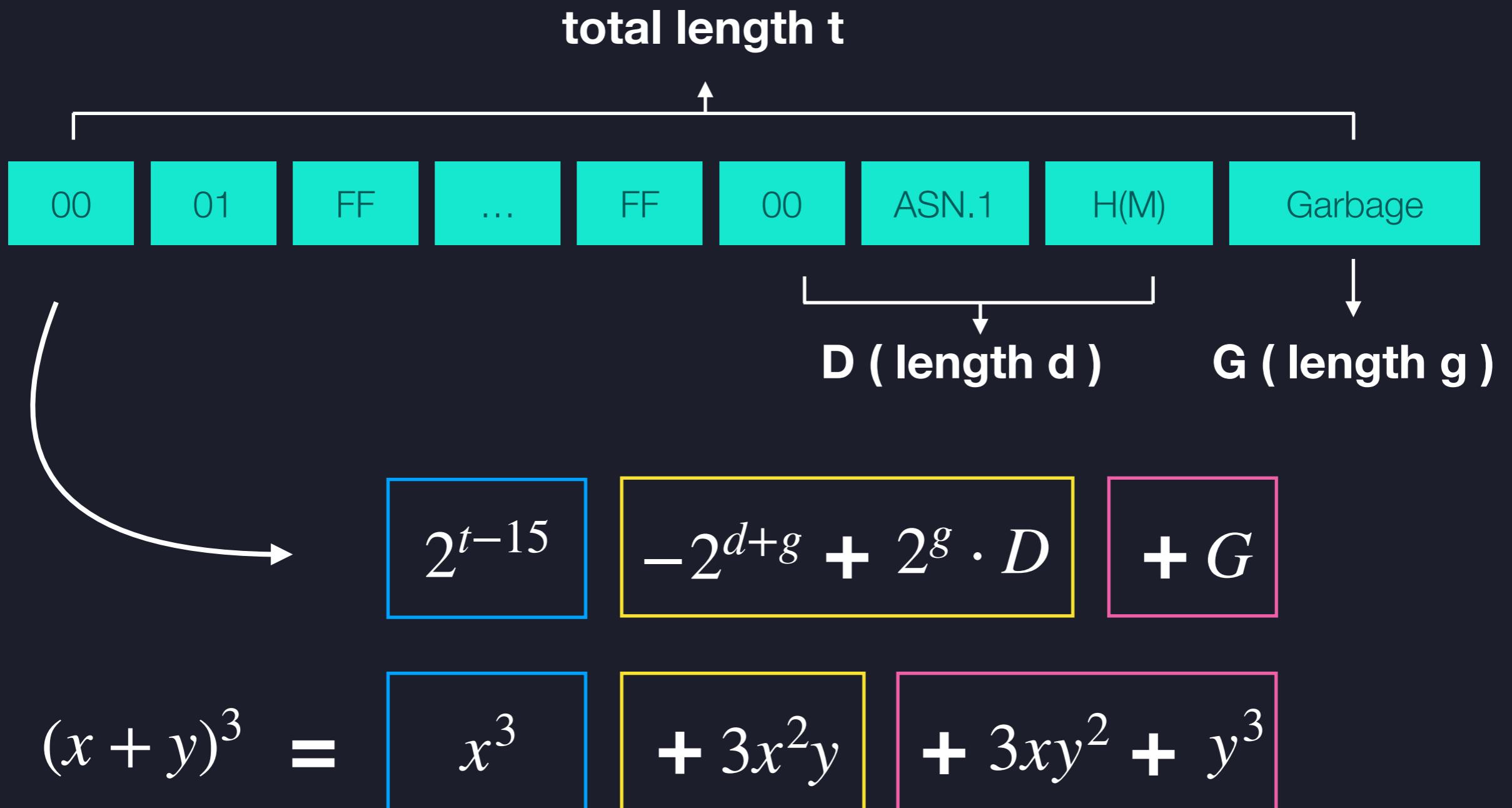
<https://mailarchive.ietf.org/arch/msg/openpgp/5rnE9ZRN1AokBVj3VqbIGP63QE>

- 在 $e = 3$ 的情況下可以 forge signature
- 嘗試構造 ED 讓 ED 的三次方不超過 n 且滿足以下格式



Bleichenbacher RSA Signature Forgery (2006)

<https://mailarchive.ietf.org/arch/msg/openpgp/5rnE9ZRN1AokBVj3VqbIGP63QE>



Bleichenbacher RSA Signature Forgery (2006)

<https://mailarchive.ietf.org/arch/msg/openpgp/5rnE9ZRN1AokBVj3VqbIGP63QE>

$$x = 2^{\frac{t-15}{3}}$$

$$y = \frac{(D - 2^d) \cdot 2^g}{3 \cdot 2^{\frac{2(t-15)}{3}}}$$

Bleichenbacher RSA Signature Forgery (2006)

<https://mailarchive.ietf.org/arch/msg/openpgp/5rnE9ZRN1AokBVj3VqbIGP63QE>

- 假設
 - Key 長度為 3072 bit
 - Garbage 長度為 2072 bit
 - 使用 SHA-1 的話，D 的長度是 288 bit
- 最後 $ED = x + y$ 就是我們構造出的合法簽章

$$x = 2^{1019}$$

$$y = \frac{(D - 2^{288}) \cdot 2^{34}}{3}$$

RSA Signature Forgery in python-rsa (2016)

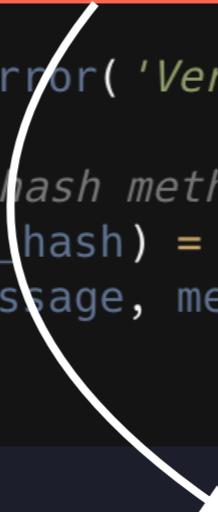
CVE-2016-1494

RSA Signature Forgery in python-rsa (2016)

<https://blog.filippo.io/bleichenbacher-06-signature-forgery-in-python-rsa/>

- 實作缺陷：padding bytes 可以是任意字元

```
...  
# If we can't find the signature marker, verification failed.  
if clearsig[0:2] != b('\x00\x01'):  
    raise VerificationError('Verification failed')  
  
# Find the 00 separator between the padding and the payload  
try:  
    sep_idx = clearsig.index(b('\x00'), 2)  
except ValueError:  
    raise VerificationError('Verification failed')  
  
# Get the hash and the hash method  
(method_name, signature_hash) = _find_method_hash(clearsig[sep_idx+1:])  
message_hash = _hash(message, method_name)  
...
```

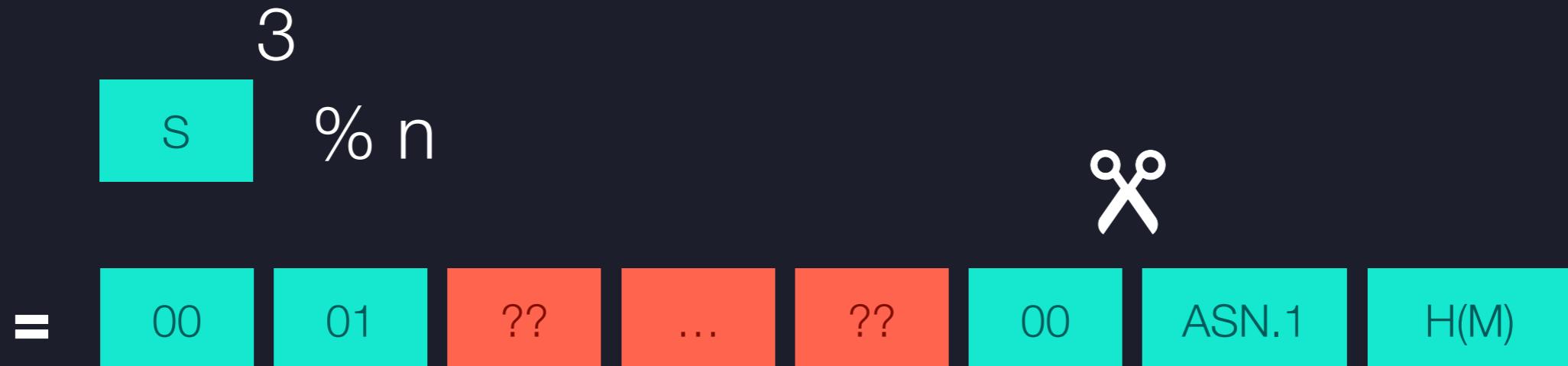


直接取第二個 0x00 沒有檢查中間的 padding bytes

RSA Signature Forgery in python-rsa (2016)

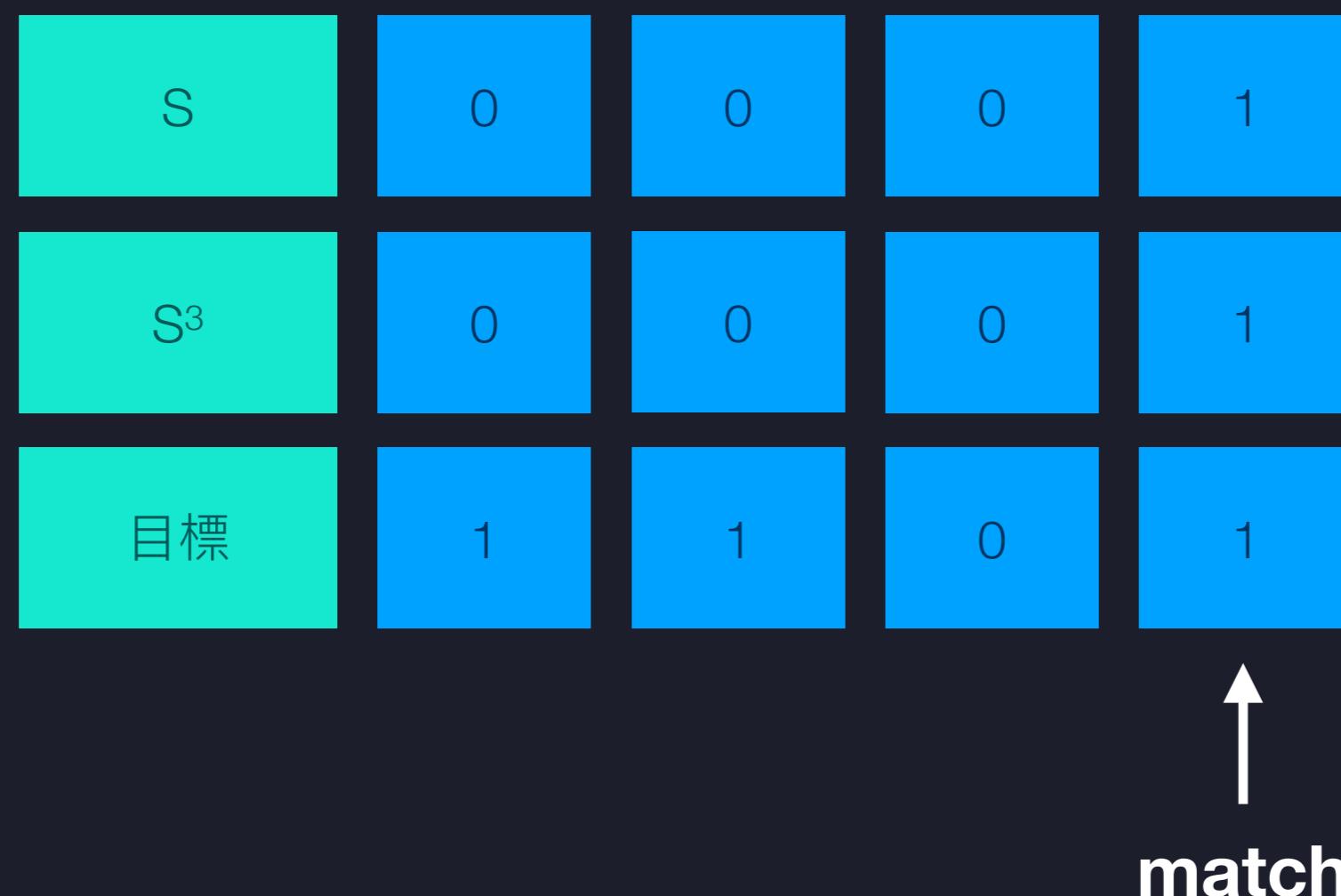
<https://blog.filippo.io/bleichenbacher-06-signature-forgery-in-python-rsa/>

- 在 $e = 3$ 的情況下可以 forge signature
- 嘗試構造 ED 讓 ED 的三次方不超過 n 且滿足以下格式
 - ED^3 的後綴是 ASN.1 + $H(M)$
 - ED^3 的前綴是 \x00\x01



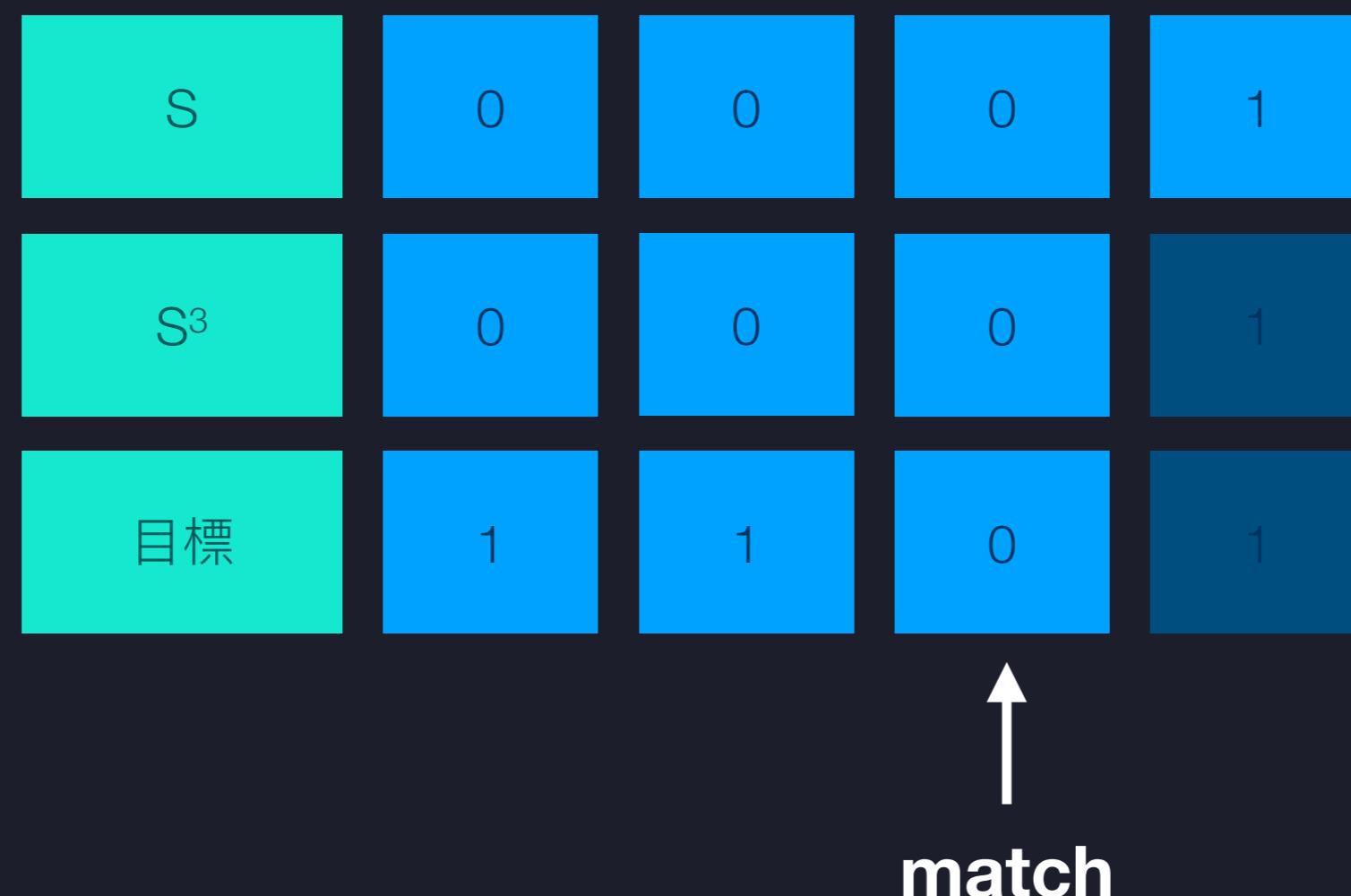
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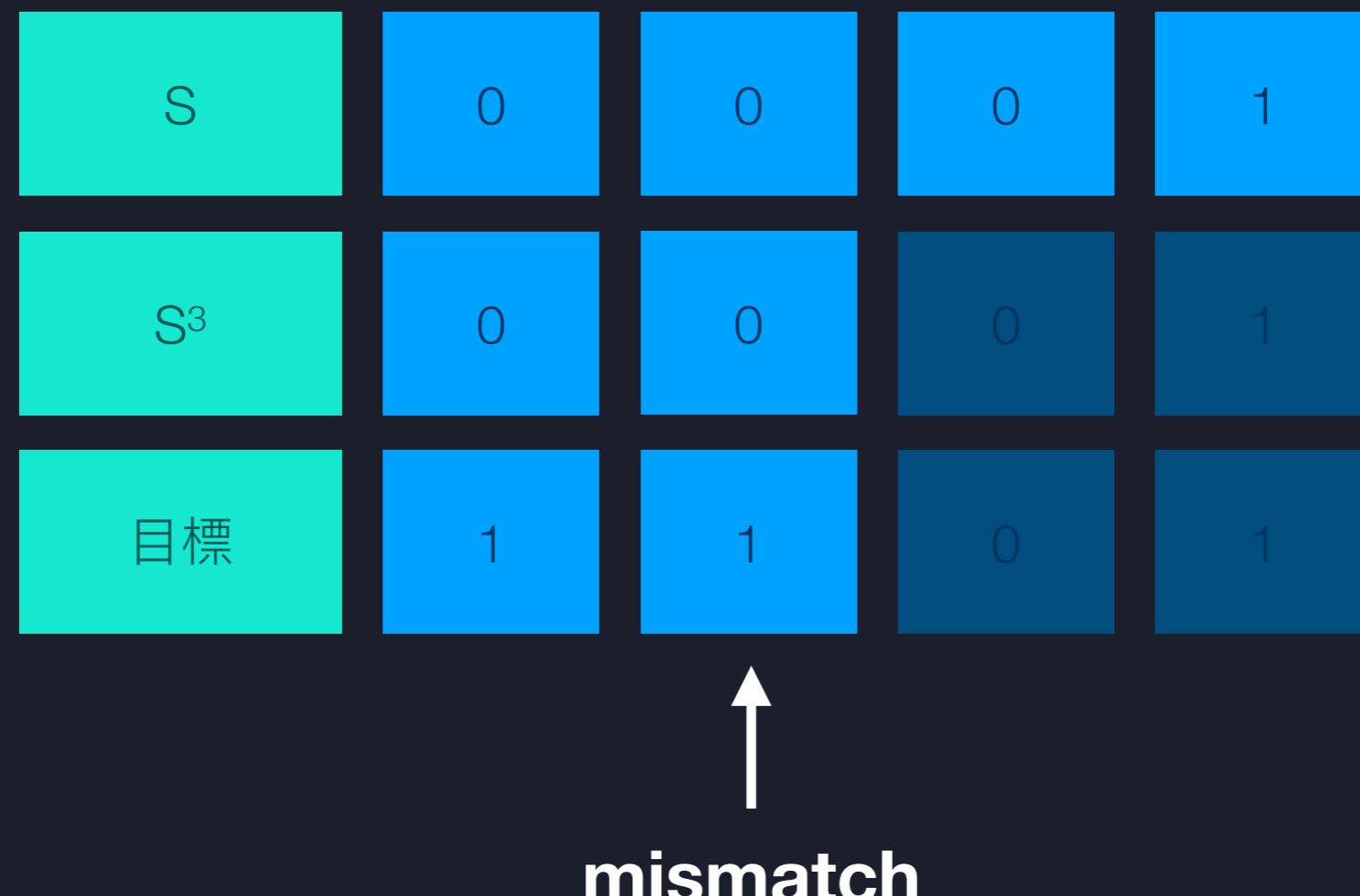
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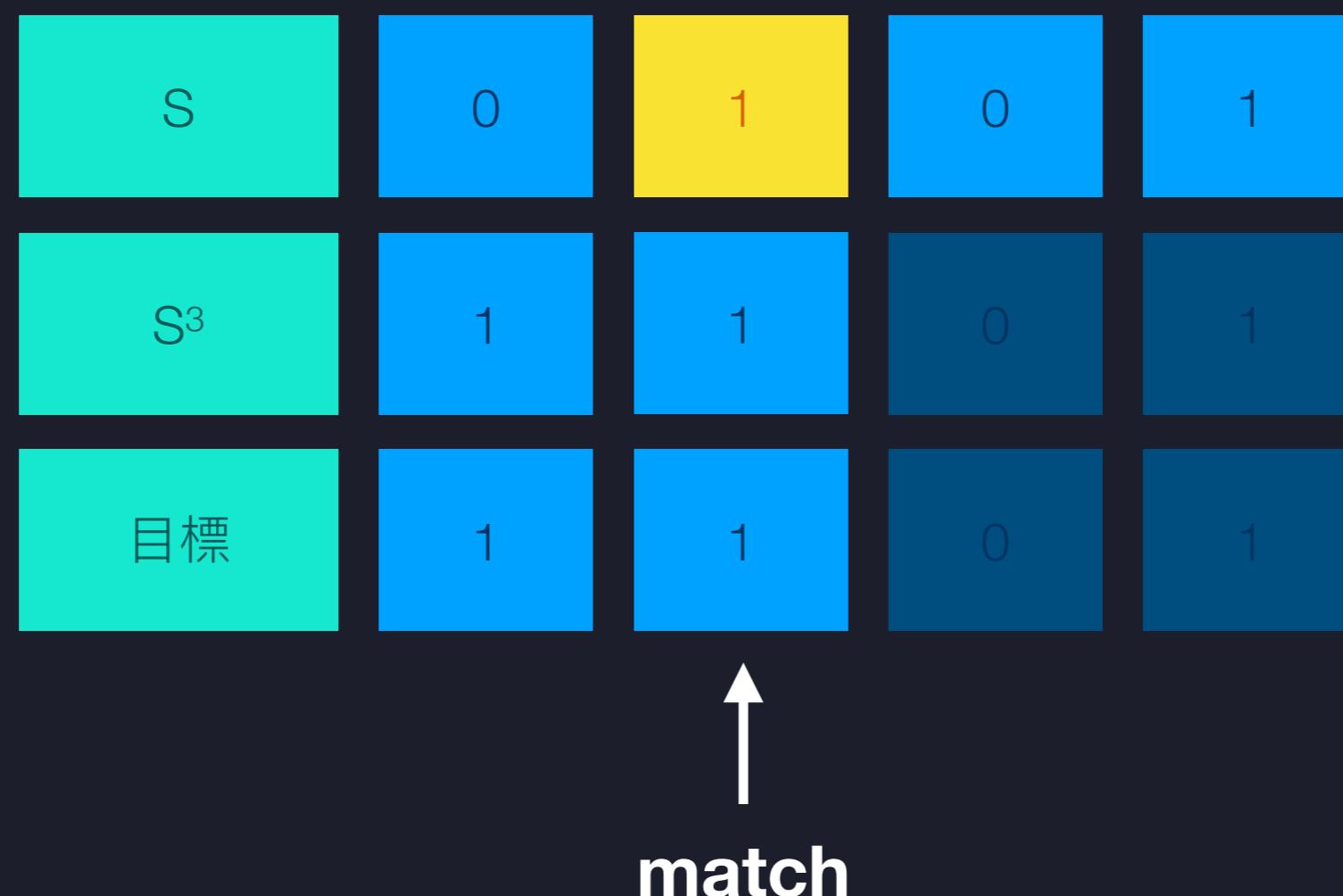
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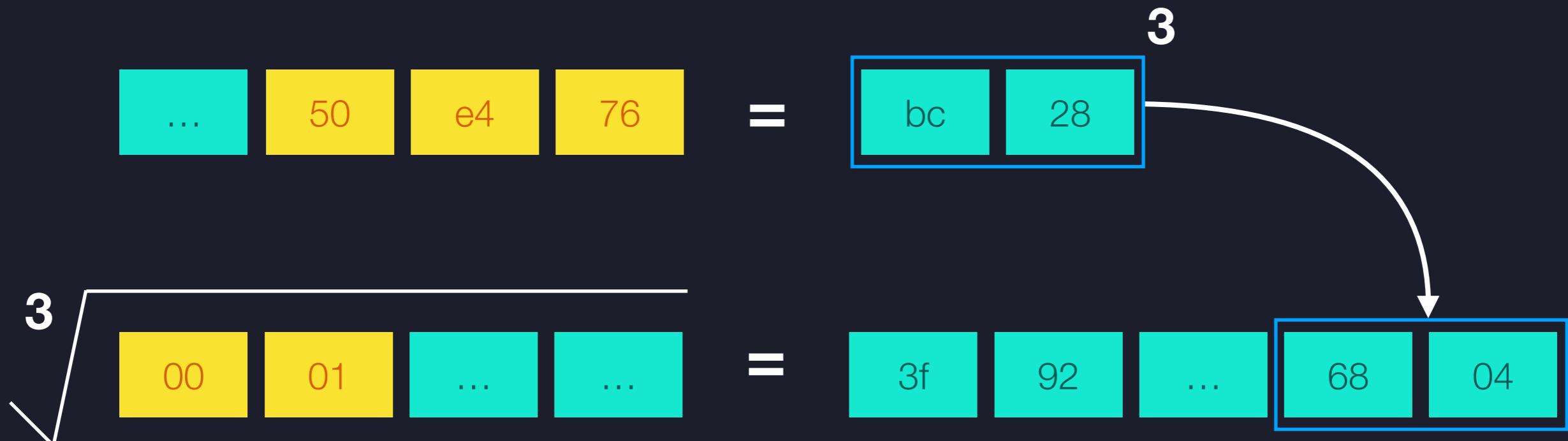
S	0	1	0	1
S^3	1	1	0	1
目標	1	1	0	1

$$0101^3 = 111\textcolor{yellow}{1}101$$

RSA Signature Forgery in python-rsa (2016)

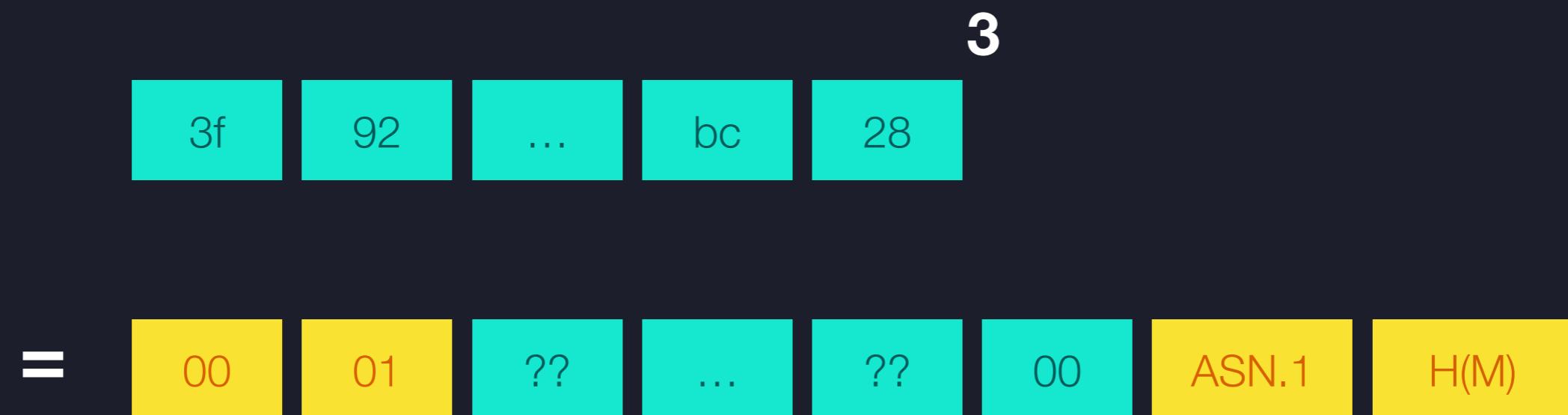
<https://blog.filippo.io/bleichenbacher-06-signature-forgery-in-python-rsa/>

- 要讓 ED³ 的前綴是 \x00\x01 只要把 \x00\x01... 開三次方
- 最後再把開完三次方的值的後綴換成前面算出來的後綴
- 就可以成功自己構造合法簽章了



RSA Signature Forgery in python-rsa (2016)

<https://blog.filippo.io/bleichenbacher-06-signature-forgery-in-python-rsa/>



A Decade After Bleichenbacher '06, RSA Signature Forgery Still Works (2019)



A Decade After Bleichenbacher '06, RSA Signature Forgery Still Works (2019)

<https://i.blackhat.com/USA-19/Wednesday/us-19-Chau-A-Decade-After-Bleichenbacher-06-RSA-Signature-Forgery-Still-Works.pdf>

- 整個格式固定是 n 這麼長
- 用 Symbolic Execution 去找到可以任意亂塞的部分有多長

<u>Name - Version</u>	<u>Overly lenient</u>	<u>Practical exploit under small e</u>
axTLS - 2.1.3	YES	YES
BearSSL - 0.4	No	-
BoringSSL - 3112	No	-
Dropbear SSH - 2017.75	No	-
GnuTLS - 3.5.12	No	-
LibreSSL - 2.5.4	No	-
libtomcrypt - 1.16	YES	YES
MatrixSSL - 3.9.1 (Certificate)	YES	No
MatrixSSL - 3.9.1 (CRL)	YES	No
mbedTLS - 2.4.2	YES	No
OpenSSH - 7.7	No	-
OpenSSL - 1.0.2l	No	-
Openswan - 2.6.50 *	YES	YES
PuTTY - 0.7	No	-
strongSwan - 5.6.3 *	YES	YES
wolfSSL - 3.11.0	No	-

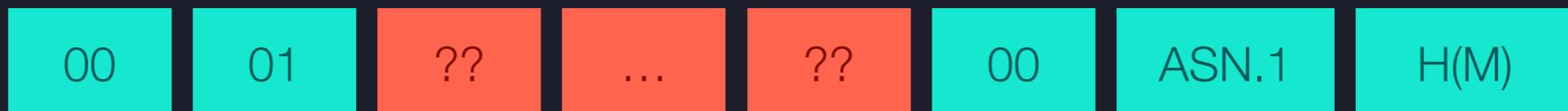
A Decade After Bleichenbacher '06, RSA Signature Forgery Still Works (2019)

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Openswan 2.6.50

CVE-2018-15836

- 實作缺陷 : padding bytes 可以是任意字元



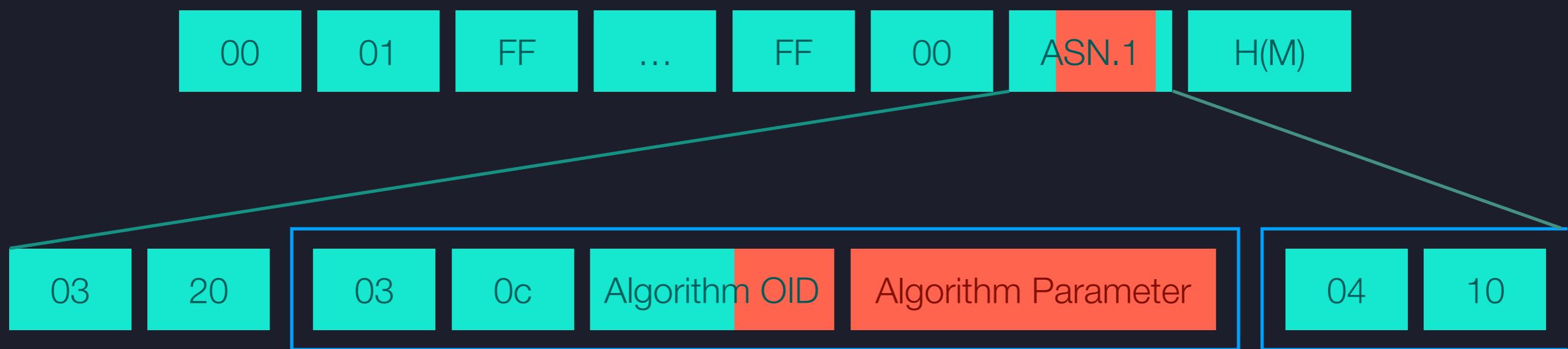
A Decade After Bleichenbacher '06, RSA Signature Forgery Still Works (2019)

<https://i.blackhat.com/USA-19/Wednesday/us-19-Chau-A-Decade-After-Bleichenbacher-06-RSA-Signature-Forgery-Still-Works.pdf>

strongSwan 5.6.3

CVE-2018-16152

- 實作缺陷：
 - Algorithm Parameter 可以是任意字元
 - Algorithm OID 後面可以有多餘的字元



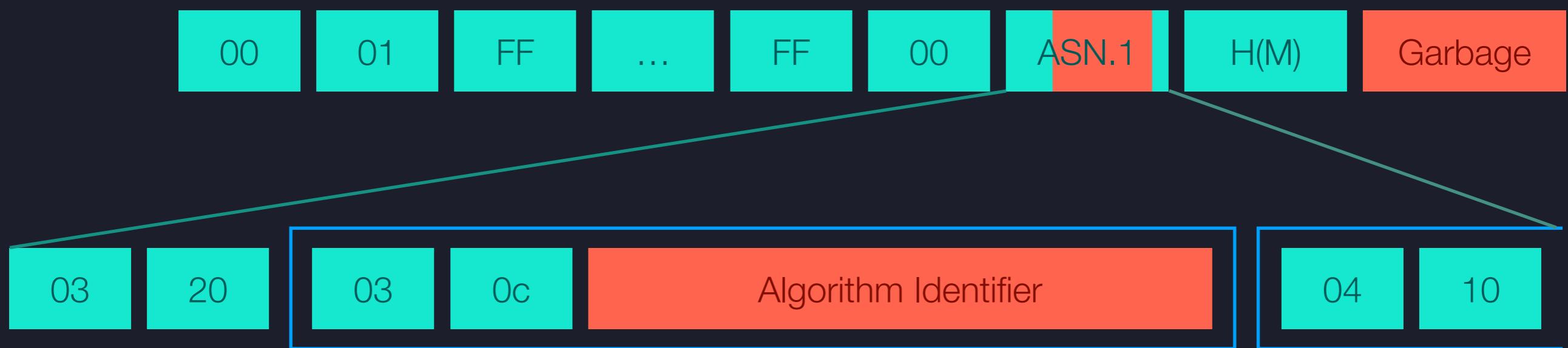
A Decade After Bleichenbacher '06, RSA Signature Forgery Still Works (2019)

<https://i.blackhat.com/USA-19/Wednesday/us-19-Chau-A-Decade-After-Bleichenbacher-06-RSA-Signature-Forgery-Still-Works.pdf>

axTLS 2.1.3

CVE-2018-16150

- 實作缺陷：
 - 可以有多餘的字元在後面
 - Algorithm Identifier 可以是任意字元



Defense against RSA Signature Forgery

How to defense?

- 用其他的簽章演算法，比如說 ECDSA
- 用更大的 e ，比如 65537
- parsing based → comparison based

