Course Project 1 Nondeterministic Finite Automata

CSE 30151 Spring 2020

Version of 2020/01/07 Due 2020/02/07 5:00pm

We've studied the theory of nondeterministic finite automata, and now it's time to implement them. The interesting challenge is that NFAs are nondeterministic, but real computers are deterministic – how do we simulate nondeterminism?

One option is backtracking: when two transitions are possible, try one, and if it fails, try the other. But this will lead to a $O(2^n)$ time algorithm (where n is the input length). The theory provides another option: convert the NFA to an equivalent DFA. That gives a O(n) algorithm, but the conversion could take $O(2^{|Q|})$ time and space (where |Q| is the number of states).

In this project, you'll implement a solution that runs in $O(|\delta|n)$ time, where $|\delta|$ is the number of transitions. You can write your implementation in C++ or Python (or another language with permission of the instructor).

Getting started

You should have been given access on GitHub to a repository called theory-project-team, with team replaced by your team's name. Please clone this repository to wherever you plan to work on the project:

```
git clone https://github.com/ND-CSE-30151-SP18/theory-project-team cd theory-project-team
```

If you're the first team member to do this, your repository is empty. In that case, run the commands:

```
git pull https://github.com/ND-CSE-30151-SP18/theory-project-skeleton git push
```

If one of your teammates already did this, there's no need for you to repeat it. Whenever we make an update to theory-project-skeleton, we'll send out an announcement, and

one of you will need to repeat the pull/push (resolving any merge conflicts if necessary) to get the update.

Now your directory should include the following files (among others):

```
bin.{linux,darwin}/
    nfa_path
    re_to_nfa
examples/
    sipser-n1.nfa
    sipser-n2.nfa
    sipser-n3.nfa
    sipser-n4.nfa
    cycle.nfa
tests/
    test-cp1.sh
cp1/
```

- The bin.linux and bin.darwin contain binaries for Linux and Mac, respectively. They contain reference implementations for the tools you will implement and tools used by the test scripts.
- The examples directory contains examples of NFAs that you will use for testing. See below for a description of the file format.
- The tests directory contains test scripts. The script tests/test-cp1.sh tests your code for correctness and speed. Your code needs to pass all tests in order to get full credit.
- Please place the programs that you write into the cp1/ subdirectory.

1 NFAs

Design a data structure for representing a NFA M, and write functions to read and write NFAs. (For all projects, the names of functions and the way that they are called are just suggestions; if you prefer a different style, that's fine.)

read_nfa(filename)

- filename: Name of file containing definition of NFA M
- \bullet Returns: The NFA M

```
write_nfa(M, filename)
```

- M: The NFA to write
- filename: Name of file to write to
- Effect: Writes definition of M to file

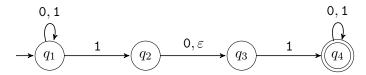
NFA file format The NFA definition should have the following format. It should begin with a four-line header:

- 1. A whitespace-separated list of states, Q.
- 2. A whitespace-separated list of input symbols, Σ . It should be disjoint from Q. Each symbol should be exactly one character long.
- 3. The start state, $s \in Q$.
- 4. A whitespace-separated list of accept states, $F \subseteq Q$.

The rest of the lines list the transitions, one transition per line. Each line has three fields, separated by whitespace:

- 1. The state $q \in Q$ that the transition leaves from.
- 2. The symbol $a \in \Sigma$ that the transition reads, or & for the empty string.
- 3. The state $r \in Q$ that the transition goes to.

For example, the following NFA (N_1 in the book):



would be specified by the file (examples/sipser-n1.nfa):

2 Matcher

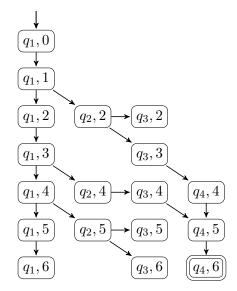
Write a function that tests whether a NFA M accepts a string w:

match(M, w)

- M: An NFA to run
- w: The string to run on
- Returns: A pair (flag, path), where
 - flag: True if M accepts w; false otherwise.
 - path: List of the transitions on an accepting path. If there is more than one, an arbitrary path is returned.

This function is required to be linear both in the length of w and the number of transitions in M.

Here's how to do this. Define a *configuration* of M on input string w to be a pair (q, i), where $q \in Q$ and $0 \le i \le |w|$. These configurations can be thought of as nodes in a graph. For example, if the NFA is N_1 above and w = 010110, then the graph of configurations would be:



This is similar to Sipser's Figure 1.29, but there are several differences here. The most important difference is that configuration $(q_4, 5)$ appears only once with two incoming edges, instead of appearing twice. In general, each configuration appears at most once in the graph. As a result, the graph has at most |Q||w| + 1 nodes and $|\delta||w|$ edges.

Then, deciding whether N_1 accepts w amounts to searching for a path from the start configuration (in this case, $(q_1,0)$) to an accept configuration (in this case, $(q_4,6)$). You can use any graph search algorithm; **breadth-first search** is probably the least hassle, but **depth-first search** corresponds to how the real Unix tools work. (One particular thing to watch out for is cycles of ε -transitions, as in cycle.nfa. Make sure your matcher doesn't hang when it encounters one.)

When you studied graph search algorithms, you may not have seen how to reconstruct the found path. Graph searches maintain a set that keeps track of which configurations have been visited (in your Data Structures notes, it was called marked). If you change this to a data structure that records, for each configuration, how you got to that configuration, then after the search finishes, you can use that information to reconstruct the path.

3 Putting it together

Package the above into a command-line tool called nfa_path:

nfa_path nfafile string

- *nfafile*: name of file defining an NFA M
- string: string to run M on
- Output:
 - If M accepts string, prints accept followed by an accepting path
 - Otherwise, prints reject

The path should be printed with one transition per line, in the same format as the NFA file format. For example:

```
$ nfa_path examples/sipser-m1.nfa 11
accept
q1 1 q2
q2 & q3
q3 1 q4
```

Test your program by running test-cp1.sh. This script runs nfa_path on several NFAs and several test strings, and it also produces a graph of the running time of nfa_path on NFAs of various sizes. The sizes are chosen so that the graph should look roughly linear, like this:

```
n= 32 *
n= 45 *
```

```
n= 55 * n= 64 * n= 71 * n= 78 * n= 84 * n= 90 * n= 95 * n=100 *
```

Submission instructions

Your code should build and run on studentnn.cse.nd.edu. The automatic tester will clone your repository, run make -C cp1, and then run tests/test-cp1.sh. You're advised to try all of the above steps and ensure that all tests pass.

To submit your work, please push your repository to Github and then create a new release with tag version cp1 (note that the tag version is not the same thing as the release title). If you are making a partial submission, then use tag version cp1-1 for part 1, cp1-2 for part 2, and so on.

Rubric

Part 1	
data structure	3
read_nfa	3
write_nfa	3
$\operatorname{Part} 2 (match)$	
correct algorithm	6
handling ε	3
reconstructing path	6
${ m Part} \ 3 \ ({ m nfa_path})$	
correctness	3
time complexity	3
Total	30