

Notre Dame University

Computer Science Department

CSC 311 Theory of Computation

Homework 1

For each of the following languages over $\Sigma = \{0, 1\}$ build the DFA that recognizes it. Each exercise is worth 10 pts.

1. $L = \{w \in \{0, 1\}^* : w \text{ begins with a 1 and ends with a 0}\}.$
2. $L = \{w \in \{0, 1\}^* : w \text{ contains at least two 1's}\}.$ Note: Not necessarily consecutive.
3. $L = \{w \in \{0, 1\}^* : w \text{ contains the substring 0110}\}.$
4. $L = \{w \in \{0, 1\}^* : |w| \geq 1 \text{ and every odd position of } w \text{ is a 1}\}.$
5. $L = \{w \in \{0, 1\}^* : \text{every 1 in } w \text{ is preceded and followed by a 0}\}.$ Note: ϵ is accepted.
6. $L = \{w \in \{0, 1\}^* : w \text{ does not contain 001 as substring}\}.$
7. $L = \{w \in \{0, 1\}^* : w \text{ contains at least one occurrence of two consecutive 1's not followed immediately by a 0}\}.$
Examples: 111, 011 accepted whereas 1101 is not.
8. $L = \{w \in \{0, 1\}^* : w \text{ contains at least two occurrences of a 1 not followed immediately by a 0}\}.$
9. $L = \{w \in \{0, 1\}^* : \text{the number of 1's in } w \text{ is divisible by 3}\}.$
10. $L = \{w \in \{0, 1\}^* : \text{the number of 0's in } w \text{ is not divisible by 2}\}.$