

By looking at the figure it is clear that the value at node A is the sum of the values of its children. The index of node A is at $2^{h+1} - 1$ which is the same as its right child. The left child of A has index $2^h - 1$. Let S be the array then

$$S[2^{h+1} - 1] = S[2^h - 1] + S[2^{h+1} - 1]$$

For node B it is the same except we shift the indices by 2^{h+1} to the right. Therefore for nodes at level $h + 1$ we have

$$S[k + 2^{h+1} - 1] = S[k + 2^h - 1] + S[k + 2^{h+1} - 1]$$

where k starts with 0 and is incremented by 2^{h+1} . The above is performed for

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forall  $k = 0, k < n$  multiples of  $2^{h+1}$  do
  |  $S[k + 2^{h+1} - 1] = S[k + 2^h - 1] + S[k + 2^{h+1} - 1]$ 
end

```

all values of h .

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for  $h = 0$  to  $\log n - 1$  do
  | for  $k = 0, k < n$  multiples of  $2^{h+1}$  do
    |  $S[k + 2^{h+1} - 1] = S[k + 2^h - 1] + S[k + 2^{h+1} - 1]$ 
    end
  end

```

Now, multiples of 2^{h+1} can be write as $\alpha 2^{h+1}$ with $\alpha = 0, \dots, d - 1$ with $d = \frac{n}{2^{h+1}}$.

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for  $d = \frac{n}{2}$  to 1 do
  | for  $\alpha = 0$  to  $d - 1$  do
    |  $S[(2\alpha + 2)s - 1] += S[(2\alpha + 1)s - 1]$ 
    |  $\alpha = \alpha + 1$ 
    end
  |  $s = 2 * s$ 
  |  $d = d/2$ 
end

```