

```

from google.colab import drive
drive.mount('/content/drive')

Mounted at /content/drive

import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import plotly.express as px

from sklearn.preprocessing import MinMaxScaler

city_stats_df =
pd.read_csv('/content/drive/MyDrive/Project/Datasets/MSW_Waste_59_Citi
es.csv')
waste_df =
pd.read_csv('/content/drive/MyDrive/Project/Datasets/Waste_Management_
and_Recycling_India.csv')
new_pop_df =
pd.read_csv('/content/drive/MyDrive/Project/Datasets/cities_r2.csv')
# Your new population dataset
sdg_df =
pd.read_csv('/content/drive/MyDrive/Project/Datasets/Data_SDG_India_In
dex_2020-21.csv')
population_df =
pd.read_csv('/content/drive/MyDrive/Project/Datasets/Area_Population_D
ensity_and_Population_2011_Census.csv')

# Save raw datasets before preprocessing
waste_df.to_csv('/content/drive/MyDrive/Project/Dataset/backup_waste_r
aw.csv', index=False)
population_df.to_csv('/content/drive/MyDrive/Project/Dataset/backup_po
pulation_raw.csv', index=False)
city_stats_df.to_csv('/content/drive/MyDrive/Project/Dataset/backup_ci
ty_stats_raw.csv', index=False)
new_pop_df.to_csv('/content/drive/MyDrive/Project/Dataset/backup_new_p
op_raw.csv', index=False)
sdg_df.to_csv('/content/drive/MyDrive/Project/Dataset/backup_sdg_raw.c
sv', index=False)

# Optionally display heads to verify in notebook
print("Raw waste_df snapshot:")
print(waste_df.head())

```

Raw waste_df snapshot:

City/District	Waste Type	Waste Generated (Tons/Day)	Recycling Rate (%)
Mumbai	Plastic	6610	68
Mumbai	Organic	1181	56
Mumbai	E-Waste	8162	53
Mumbai	Construction	8929	56
Mumbai	Hazardous	5032	44

Population Density (People/km ²)	Municipal Efficiency Score (1-10)
11191	9
11191	5
11191	8
11191	5
11191	7

Disposal Method	Cost of Waste Management (₹/Ton)
Composting	3056
Composting	2778
Incineration	3390
Landfill	1498
Recycling	2221

Awareness Campaigns Count	Landfill Name	Landfill Location (Lat, Long)
14	Mumbai Landfill	22.4265, 77.4931
12	Mumbai Landfill	22.4265, 77.4931
13	Mumbai Landfill	22.4265, 77.4931
14	Mumbai Landfill	22.4265, 77.4931
16	Mumbai Landfill	22.4265, 77.4931

Landfill Capacity (Tons)	Year
45575	2019
45575	2019
45575	2019

```
3          45575  2019
4          45575  2019
```

```
print(new_pop_df.columns)
```

```
Index(['name_of_city', 'state_code', 'state_name', 'dist_code',
      'population_total', 'population_male', 'population_female',
      '0-6_population_total', '0-6_population_male', '0-6_population_female',
      'litrates_total', 'litrates_male', 'litrates_female',
      'sex_ratio',
      'child_sex_ratio', 'effective_literacy_rate_total',
      'effective_literacy_rate_male',
      'effective_literacy_rate_female',
      'location', 'total_graduates', 'male_graduates',
      'female_graduates'],
      dtype='object')
```

```
print(city_stats_df.columns)
```

```
Index(['City', 'Population_2001', 'Area_sq_km', 'Waste_TPD',
      'Waste_kg_per_capita_per_day'],
      dtype='object')
```

```
print(waste_df.columns)
```

```
Index(['City/District', 'Waste Type', 'Waste Generated (Tons/Day)',
      'Recycling Rate (%)', 'Population Density (People/km²)',
      'Municipal Efficiency Score (1-10)', 'Disposal Method',
      'Cost of Waste Management (₹/Ton)', 'Awareness Campaigns
Count',
      'Landfill Name', 'Landfill Location (Lat, Long)',
      'Landfill Capacity (Tons)', 'Year'],
      dtype='object')
```

```
print(population_df.columns)
```

```
Index(['District', 'Geographical Area (Sq.Kms)', 'Population Density',
      'Male',
      'Female', 'Total', 'Percentage Share to Total Population',
      'Rank'],
      dtype='object')
```

```
print(sdg_df.columns)
```

```
Index(['Category', 'State/UT', 'SDG 1', 'SDG 2', 'SDG 3', 'SDG 4',
      'SDG 5',
      'SDG 6', 'SDG 7', 'SDG 8', 'SDG 9', 'SDG 10', 'SDG 11', 'SDG
12',
```

```
'SDG 13', 'SDG 15', 'SDG 16', 'Composite Score', 'Rank'],  
dtype='object')
```

```
# Preprocessing for merging  
# Rename columns for consistency before merging  
city_stats_df.rename(columns={'City': 'City_Name'}, inplace=True)  
waste_df.rename(columns={'City/District': 'City_Name', 'Population  
Density (People/km²)': 'Population Density'}, inplace=True)  
population_df.rename(columns={  
    'District': 'City_Name',  
    'Total': 'Total_Population',  
    'Population Density (per sq.km)': 'Population Density',  
    'Geographical Area (Sq.Kms)': 'Geographical_Area'  
}, inplace=True)  
new_pop_df.rename(columns={  
    'name_of_city': 'City_Name',  
    'state_name': 'State',  
    'population_total': 'Total_Population'  
}, inplace=True)  
sdg_df.rename(columns={'State/UT': 'State'}, inplace=True)  
  
# Strip and standardize city/state names  
for df_ in [city_stats_df, waste_df, population_df, new_pop_df]:  
    df_['City_Name'] = df_['City_Name'].str.strip().str.title()  
sdg_df['State'] = sdg_df['State'].str.strip().str.title()  
  
# Manually map city to state (ensure full mapping)  
city_to_state = {  
    'Mumbai': 'Maharashtra', 'Delhi': 'Delhi', 'Bengaluru':  
    'Karnataka', 'Chennai': 'Tamil Nadu',  
    'Kolkata': 'West Bengal', 'Hyderabad': 'Telangana', 'Pune':  
    'Maharashtra', 'Ahmedabad': 'Gujarat',  
    'Jaipur': 'Rajasthan', 'Lucknow': 'Uttar Pradesh', 'Surat':  
    'Gujarat', 'Kanpur': 'Uttar Pradesh',  
    'Nagpur': 'Maharashtra', 'Patna': 'Bihar', 'Bhopal': 'Madhya  
Pradesh', 'Thiruvananthapuram': 'Kerala',  
    'Indore': 'Madhya Pradesh', 'Vadodara': 'Gujarat', 'Guwahati':  
    'Assam', 'Coimbatore': 'Tamil Nadu',  
    'Ranchi': 'Jharkhand', 'Amritsar': 'Punjab', 'Jodhpur':  
    'Rajasthan', 'Varanasi': 'Uttar Pradesh',  
    'Ludhiana': 'Punjab', 'Agra': 'Uttar Pradesh', 'Meerut': 'Uttar  
Pradesh', 'Nashik': 'Maharashtra',  
    'Rajkot': 'Gujarat', 'Madurai': 'Tamil Nadu', 'Jabalpur': 'Madhya  
Pradesh', 'Allahabad': 'Uttar Pradesh',  
    'Visakhapatnam': 'Andhra Pradesh', 'Gwalior': 'Madhya Pradesh'  
}  
waste_df['State'] = waste_df['City_Name'].map(city_to_state)
```

```

# Fix known city name typos before merging
waste_df['City_Name'] = waste_df['City_Name'].replace({
    'New Delhi': 'Delhi',
    'Thiruvananthapuram': 'Thiruvananthapuram',
    'Vishakhapatnam': 'Visakhapatnam',
    'Mysore': 'Mysuru'
})

# Merge datasets stepwise
merged_df = waste_df.merge(city_stats_df, on='City_Name', how='left')
merged_df = merged_df.merge(new_pop_df[['City_Name', 'State',
'Total_Population']], on=['City_Name', 'State'], how='left')
merged_df = merged_df.merge(sdg_df[['State', 'SDG 12', 'Composite
Score']], on='State', how='left')

# Fallback: use Population_2001 from city_stats_df if still missing
still_missing_pop = merged_df['Total_Population'].isna()
fallback_pop_map = city_stats_df.set_index('City_Name')
['Population_2001'].to_dict()
merged_df.loc[still_missing_pop, 'Total_Population'] =
merged_df.loc[still_missing_pop, 'City_Name'].map(fallback_pop_map)

manual_pop_map = {
    'Mumbai': 11978450,
    'Bengaluru': 6490131,
    'Thiruvananthapuram': 752490,
    'Visakhapatnam': 982904,
    'Jodhpur': 856034,
    'Gwalior': 826919
}
merged_df.loc[merged_df['City_Name'].isin(manual_pop_map.keys()),
'Population_2001'] = \
merged_df['City_Name'].map(manual_pop_map)

# Fill missing Geographical Area and Population Density from
city_stats_df
area_map = city_stats_df.set_index('City_Name')
['Area_sq_km'].to_dict()
pop_2001_map = city_stats_df.set_index('City_Name')
['Population_2001'].to_dict()

# Fill missing area
merged_df['Area_sq_km'] =
merged_df['Area_sq_km'].fillna(merged_df['City_Name'].map(area_map))

# Calculate population density where missing: population_2001 /
area_sq_km

```

```

merged_df['Population Density'] = merged_df['Population
Density'].fillna(
    merged_df['City_Name'].map(pop_2001_map) /
merged_df['City_Name'].map(area_map)
)

# Diagnostics: Print missing data counts
print("Missing Geographical Area:",
merged_df[merged_df['Area_sq_km'].isna()][['City_Name']].unique())
print("Missing Population Density:", merged_df[merged_df['Population
Density'].isna()][['City_Name']].unique())
print("Missing Total Population:",
merged_df[merged_df['Total_Population'].isna()][['City_Name']].unique())
print("Missing Waste Generated:", merged_df[merged_df['Waste Generated
(Tons/Day)'].isna()][['City_Name']].unique())
print("States with missing SDG 12:", merged_df[merged_df['SDG
12'].isna()][['State']].unique())

# Feature engineering
merged_df['Waste_per_capita'] = merged_df['Waste Generated
(Tons/Day)'] * 1000 / merged_df['Population_2001']
merged_df['Recycling_Efficiency'] = merged_df['Recycling Rate (%)'] /
100
merged_df['Circular_Score'] = (
    merged_df['Recycling Rate (%)'] +
    merged_df['Municipal Efficiency Score (1-10)'] * 10 +
    merged_df['SDG 12']
) / 3

# Normalize features for modeling
features_to_scale = ['Waste_per_capita', 'Recycling_Efficiency',
'Circular_Score', 'Population Density']
scaler = MinMaxScaler()
merged_df[features_to_scale] =
scaler.fit_transform(merged_df[features_to_scale])

# Preview final dataframe
print(merged_df.head())

Missing Geographical Area: ['Mumbai' 'Bengaluru' 'Thiruvananthapuram'
'Jodhpur' 'Visakhapatnam'
'Gwalior']
Missing Population Density: []
Missing Total Population: ['Mumbai' 'Bengaluru' 'Thiruvananthapuram'
'Jodhpur' 'Visakhapatnam'
'Gwalior']
Missing Waste Generated: []
States with missing SDG 12: []

```

City_Name \	Waste Type	Waste Generated (Tons/Day)	Recycling Rate (%)
0 Mumbai	Plastic	6610	68
1 Mumbai	Organic	1181	56
2 Mumbai	E-Waste	8162	53
3 Mumbai	Construction	8929	56
4 Mumbai	Hazardous	5032	44

Population Density Method \	Municipal Efficiency Score (1-10)	Disposal
0 Composting	0.408167	9
1 Composting	0.408167	5
2 Incineration	0.408167	8
3 Landfill	0.408167	5
4 Recycling	0.408167	7

Cost of Waste Management (₹/Ton)	Awareness Campaigns Count \
0 3056	14
1 2778	12
2 3390	13
3 1498	14
4 2221	16

Landfill Name ...	Population_2001	Area_sq_km	Waste_TPD \
0 Mumbai Landfill ...	11978450.0	NaN	NaN
1 Mumbai Landfill ...	11978450.0	NaN	NaN
2 Mumbai Landfill ...	11978450.0	NaN	NaN
3 Mumbai Landfill ...	11978450.0	NaN	NaN
4 Mumbai Landfill ...	11978450.0	NaN	NaN

Waste_kg_per_capita_per_day Score \	Total_Population	SDG 12	Composite
0 70	NaN	NaN	82
1 70	NaN	NaN	82
2 70	NaN	NaN	82
3 70	NaN	NaN	82

4		NaN	NaN	82
70				
	Waste_per_capita	Recycling_Efficiency	Circular_Score	
0	0.039189	0.690909	0.808824	
1	0.002015	0.472727	0.426471	
2	0.049817	0.418182	0.625000	
3	0.055069	0.472727	0.426471	
4	0.028384	0.254545	0.485294	

[5 rows x 24 columns]

... after all processing steps

Save the final cleaned and processed dataset to CSV

```
merged_df.to_csv('/content/drive/MyDrive/Project/Datasets/merged_final_dataset.csv', index=False)
print("Merged dataset saved successfully.")
```

Merged dataset saved successfully.

```
import matplotlib.pyplot as plt
import seaborn as sns
import plotly.express as px
```

1. Summary statistics

```
print("Summary statistics:")
print(merged_df.describe())
```

2. Distribution of Waste per Capita

```
plt.figure(figsize=(8,5))
sns.histplot(merged_df['Waste_per_capita'], bins=30, kde=True)
plt.title('Distribution of Waste per Capita (kg/day)')
plt.xlabel('Waste per Capita (kg/day)')
plt.ylabel('Frequency')
plt.show()
```

Summary statistics:

	Waste Generated (Tons/Day)	Recycling Rate (%)	Population
Density \			
count	850.000000	850.000000	
850.000000			
mean	5262.249412	57.076471	
0.514113			
std	2786.984735	16.129994	
0.305622			
min	511.000000	30.000000	
0.000000			
25%	2865.750000	43.000000	

0.257731		
50%	5283.000000	56.000000
0.472162		
75%	7757.250000	71.000000
0.772088		
max	9980.000000	85.000000
1.000000		

Municipal Efficiency Score (1-10)		Cost of Waste Management
(₹/Ton) \		
count	850.000000	
850.000000		
mean	7.400000	
2778.458824		
std	1.722162	
1276.325630		
min	5.000000	
503.000000		
25%	6.000000	
1647.500000		
50%	7.000000	
2853.000000		
75%	9.000000	
3855.000000		
max	10.000000	
4999.000000		

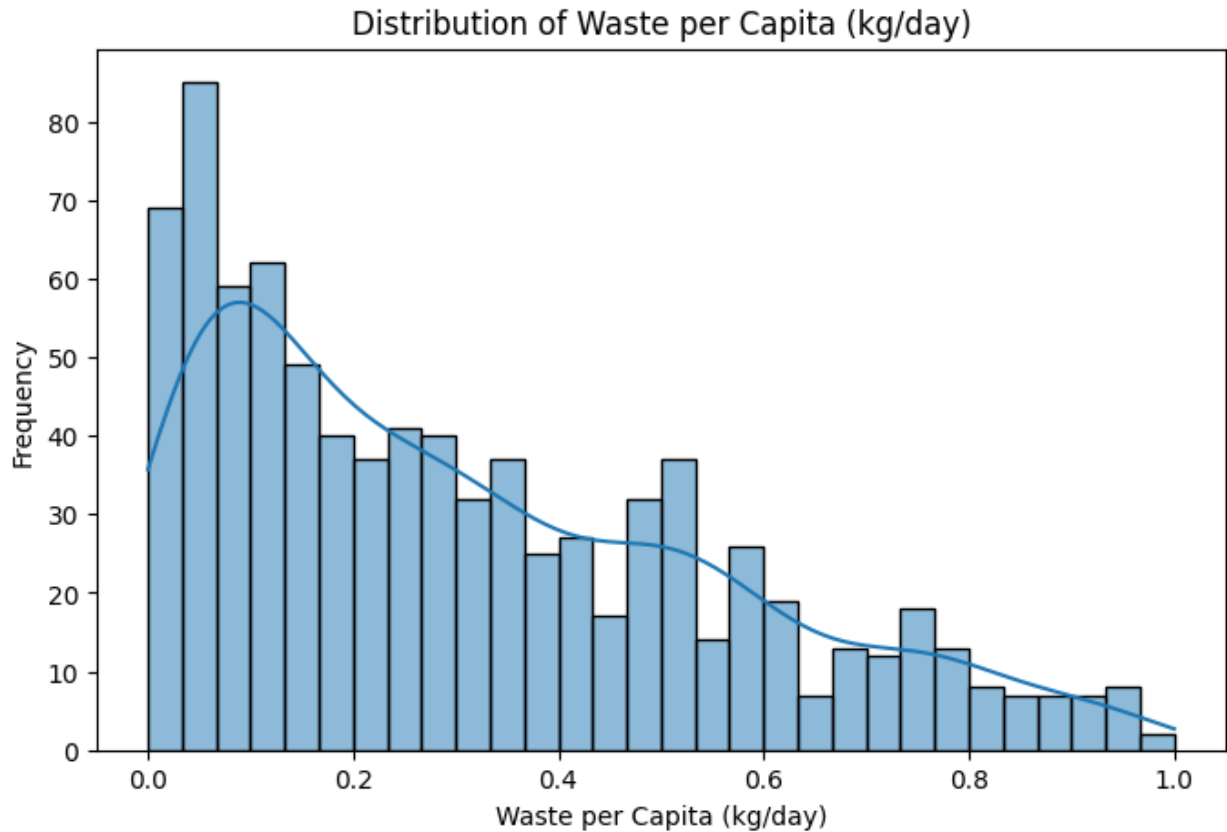
Awareness Campaigns Count		Landfill Capacity (Tons)
Year \		
count	850.000000	850.000000
850.000000		
mean	9.904706	58934.617647
2021.000000		
std	6.070772	19413.627292
1.415046		
min	0.000000	22690.000000
2019.000000		
25%	5.000000	45575.000000
2020.000000		
50%	10.000000	61038.500000
2021.000000		
75%	15.000000	71127.000000
2022.000000		
max	20.000000	98646.000000
2023.000000		

Population_2001	Area_sq_km	Waste_TPD
Waste_kg_per_capita_per_day \		
count	8.500000e+02	700.000000
700.000000		

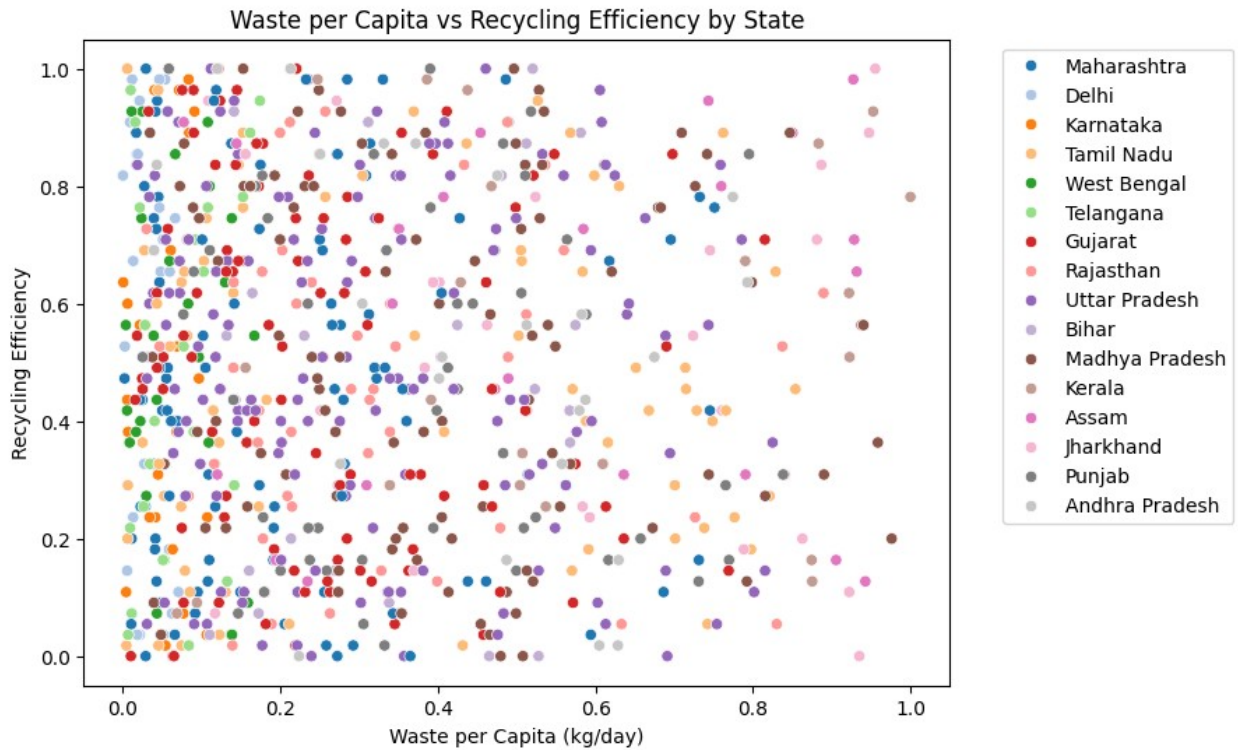
mean	2.394508e+06	229.071429	975.357143
0.396429			
std	2.555171e+06	259.234585	1188.270892
0.130620			
min	7.524900e+05	52.000000	166.000000
0.190000			
25%	9.668620e+05	110.750000	408.000000
0.265000			
50%	1.336336e+06	171.500000	520.500000
0.395000			
75%	2.538473e+06	241.000000	1025.000000
0.512500			
max	1.197845e+07	1483.000000	5922.000000
0.620000			

	Total_Population	SDG 12	Composite Score	Waste_per_capita
\				
count	7.000000e+02	850.000000	850.000000	850.000000
mean	2.125940e+06	72.294118	65.441176	0.308621
std	1.905892e+06	11.381409	5.945330	0.247007
min	8.098950e+05	50.000000	52.000000	0.000000
25%	9.734138e+05	66.000000	60.000000	0.098794
50%	1.382456e+06	78.000000	68.000000	0.250968
75%	2.459994e+06	79.000000	70.000000	0.484880
max	1.030645e+07	89.000000	75.000000	1.000000

	Recycling_Efficiency	Circular_Score
count	850.000000	850.000000
mean	0.492299	0.539490
std	0.293273	0.191454
min	0.000000	0.000000
25%	0.236364	0.404412
50%	0.472727	0.536765
75%	0.745455	0.676471
max	1.000000	1.000000

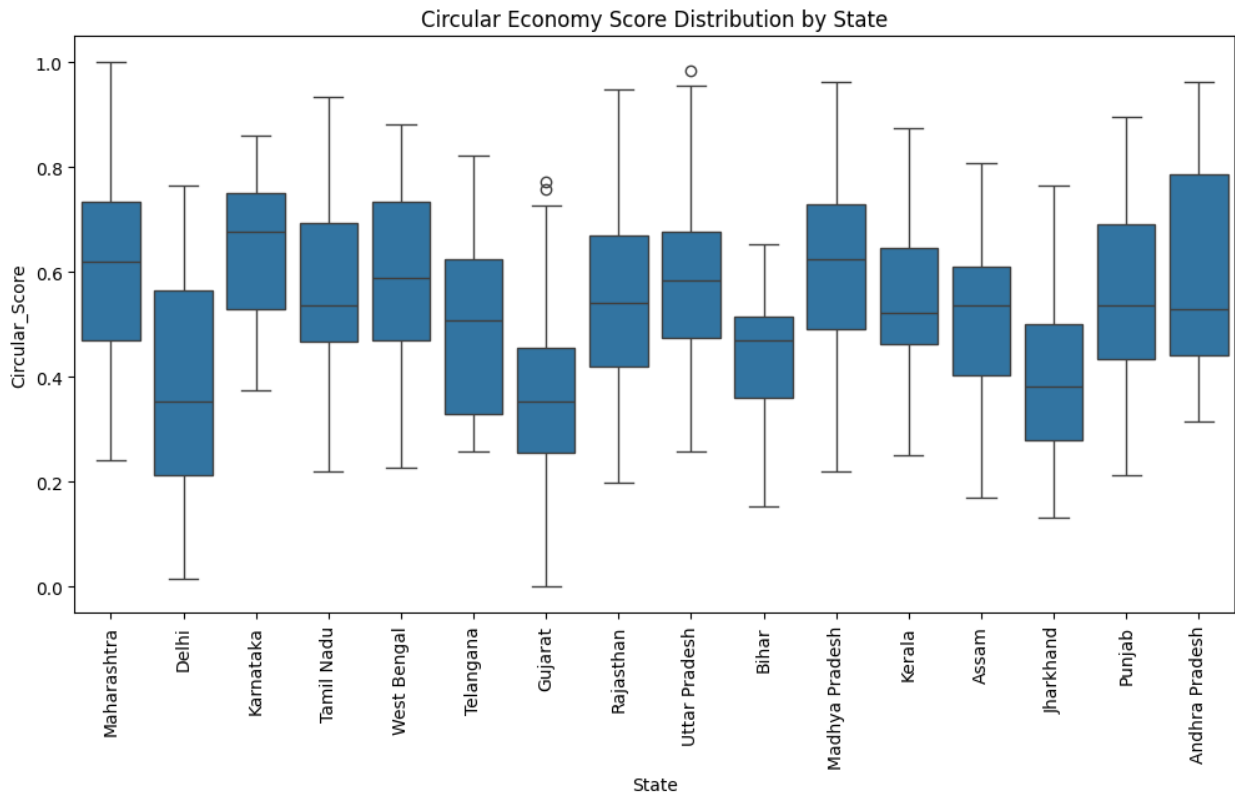


```
# 3. Scatter plot: Waste per Capita vs Recycling Efficiency (colored by State)
plt.figure(figsize=(8,6))
sns.scatterplot(data=merged_df, x='Waste_per_capita',
y='Recycling_Efficiency', hue='State', palette='tab20')
plt.title('Waste per Capita vs Recycling Efficiency by State')
plt.xlabel('Waste per Capita (kg/day)')
plt.ylabel('Recycling Efficiency')
plt.legend(bbox_to_anchor=(1.05, 1), loc='upper left')
plt.show()
```



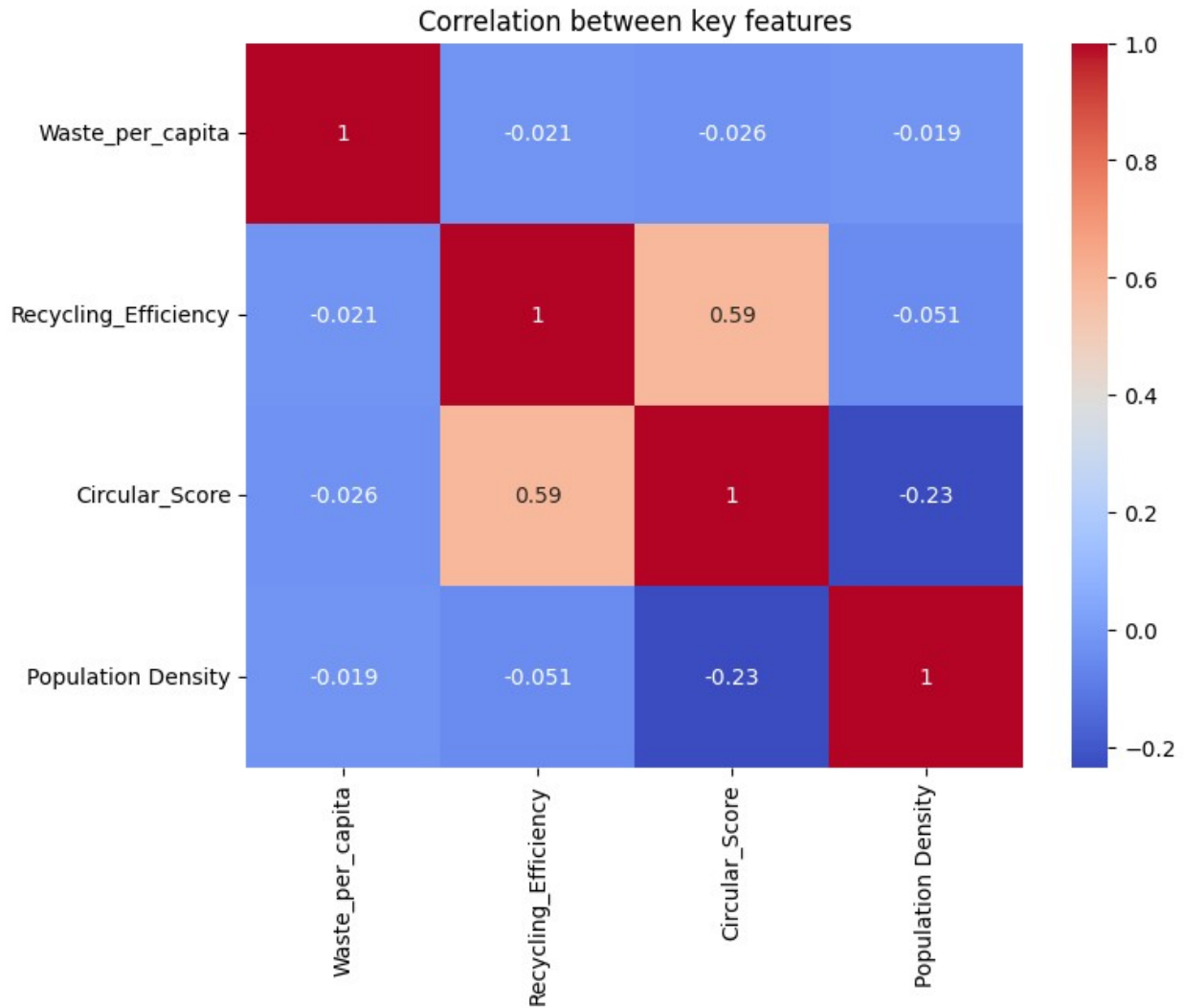
4. Boxplot of Circular Score by State

```
plt.figure(figsize=(12,6))
sns.boxplot(data=merged_df, x='State', y='Circular_Score')
plt.xticks(rotation=90)
plt.title('Circular Economy Score Distribution by State')
plt.show()
```



5. Correlation heatmap for key features

```
plt.figure(figsize=(8,6))  
corr = merged_df[['Waste_per_capita', 'Recycling_Efficiency',  
'Circular_Score', 'Population_Density']].corr()  
sns.heatmap(corr, annot=True, cmap='coolwarm')  
plt.title('Correlation between key features')  
plt.show()
```



6. Interactive Plotly scatter: Waste per Capita vs Circular Score colored by SDG 12

```
fig = px.scatter(
    merged_df,
    x='Waste_per_capita',
    y='Circular_Score',
    color='SDG 12',
    hover_name='City_Name',
    title='Waste per Capita vs Circular Economy Score by SDG 12'
)
fig.show()
```

```
import tensorflow as tf
from tensorflow.keras import Input
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import LSTM, Dense, Dropout
from sklearn.preprocessing import MinMaxScaler
```

```

import numpy as np

cities = merged_df['City_Name'].unique()
results = {}

for city in cities:
    city_data = merged_df[merged_df['City_Name'] ==
city].sort_values(by='Year')
    if city_data['Year'].nunique() < 5:
        print(f"⚠ Not enough data to forecast for {city}")
        continue

    time_series = city_data[['Year', 'Waste Generated
(Tons/Day)']].dropna()
    if len(time_series) < 4: # at least window size + 1 data points
        print(f"⚠ Not enough data points for {city}")
        continue

    scaler = MinMaxScaler()
    waste_scaled = scaler.fit_transform(time_series[['Waste Generated
(Tons/Day)']])

    def create_sequences(data, window_size=3):
        X, y = [], []
        for i in range(len(data) - window_size):
            X.append(data[i:i+window_size])
            y.append(data[i+window_size])
        return np.array(X), np.array(y)

    X, y = create_sequences(waste_scaled, window_size=3)
    X = X.reshape((X.shape[0], X.shape[1], 1))

    model = Sequential([
        Input(shape=(X.shape[1], 1)), # <-- Add Input layer explicitly
here
        LSTM(64, activation='relu'),
        Dropout(0.2),
        Dense(1)
    ])
    model.compile(optimizer='adam', loss='mse')
    model.fit(X, y, epochs=100, verbose=0)

    last_sequence = waste_scaled[-3:].reshape((1, 3, 1))
    next_prediction = model.predict(last_sequence)
    next_tpd = scaler.inverse_transform(next_prediction)[0][0]

    results[city] = next_tpd
    print(f"⚠ Forecasted Waste for {city} (next year): {next_tpd:.2f}
Tons/Day")

```

```
# Optional: convert results dict to DataFrame for saving or analysis
import pandas as pd
forecast_df = pd.DataFrame(list(results.items()),
columns=['City_Name', 'Forecasted_Waste_TonsPerDay'])
```

```
1/1 _____ 0s 274ms/step
[] Forecasted Waste for Mumbai (next year): 6061.08 Tons/Day
1/1 _____ 0s 183ms/step
[] Forecasted Waste for Delhi (next year): 5556.22 Tons/Day
1/1 _____ 0s 294ms/step
[] Forecasted Waste for Bengaluru (next year): 4719.50 Tons/Day
1/1 _____ 0s 177ms/step
[] Forecasted Waste for Chennai (next year): 4512.31 Tons/Day
```

WARNING:tensorflow:5 out of the last 5 calls to <function TensorFlowTrainer.make_predict_function.<locals>.one_step_on_data_distributed at 0x780264067ce0> triggered tf.function retracing. Tracing is expensive and the excessive number of tracings could be due to (1) creating @tf.function repeatedly in a loop, (2) passing tensors with different shapes, (3) passing Python objects instead of tensors. For (1), please define your @tf.function outside of the loop. For (2), @tf.function has reduce_retracing=True option that can avoid unnecessary retracing. For (3), please refer to https://www.tensorflow.org/guide/function#controlling_retracing and https://www.tensorflow.org/api_docs/python/tf/function for more details.

```
1/1 _____ 0s 209ms/step
[] Forecasted Waste for Kolkata (next year): 4047.00 Tons/Day
```

WARNING:tensorflow:6 out of the last 6 calls to <function TensorFlowTrainer.make_predict_function.<locals>.one_step_on_data_distributed at 0x780260433a60> triggered tf.function retracing. Tracing is expensive and the excessive number of tracings could be due to (1) creating @tf.function repeatedly in a loop, (2) passing tensors with different shapes, (3) passing Python objects instead of tensors. For (1), please define your @tf.function outside of the loop. For (2), @tf.function has reduce_retracing=True option that can avoid unnecessary retracing. For (3), please refer to https://www.tensorflow.org/guide/function#controlling_retracing and https://www.tensorflow.org/api_docs/python/tf/function for more details.

```
1/1 _____ 0s 196ms/step
[] Forecasted Waste for Hyderabad (next year): 3579.45 Tons/Day
1/1 _____ 0s 185ms/step
[] Forecasted Waste for Pune (next year): 5819.08 Tons/Day
1/1 _____ 0s 268ms/step
[] Forecasted Waste for Ahmedabad (next year): 4958.43 Tons/Day
1/1 _____ 0s 172ms/step
```


□ Forecasted Waste for Jaipur (next year): 5233.23 Tons/Day
1/1 _____ 0s 196ms/step

□ Forecasted Waste for Lucknow (next year): 5555.64 Tons/Day
1/1 _____ 0s 175ms/step

□ Forecasted Waste for Surat (next year): 5803.92 Tons/Day
1/1 _____ 0s 174ms/step

□ Forecasted Waste for Kanpur (next year): 5005.38 Tons/Day
1/1 _____ 0s 182ms/step

□ Forecasted Waste for Nagpur (next year): 4669.88 Tons/Day
1/1 _____ 0s 204ms/step

□ Forecasted Waste for Patna (next year): 4496.56 Tons/Day
1/1 _____ 0s 197ms/step

□ Forecasted Waste for Bhopal (next year): 5612.57 Tons/Day
1/1 _____ 0s 262ms/step

□ Forecasted Waste for Thiruvananthapuram (next year): 3841.90 Tons/Day
1/1 _____ 0s 176ms/step

□ Forecasted Waste for Indore (next year): 4557.53 Tons/Day
1/1 _____ 0s 198ms/step

□ Forecasted Waste for Vadodara (next year): 5984.08 Tons/Day
1/1 _____ 0s 168ms/step

□ Forecasted Waste for Guwahati (next year): 4982.79 Tons/Day
1/1 _____ 0s 201ms/step

□ Forecasted Waste for Coimbatore (next year): 5278.44 Tons/Day
1/1 _____ 0s 180ms/step

□ Forecasted Waste for Ranchi (next year): 4551.01 Tons/Day
1/1 _____ 0s 185ms/step

□ Forecasted Waste for Amritsar (next year): 5056.85 Tons/Day
1/1 _____ 0s 181ms/step

□ Forecasted Waste for Jodhpur (next year): 3397.81 Tons/Day
1/1 _____ 0s 173ms/step

□ Forecasted Waste for Varanasi (next year): 4042.34 Tons/Day
1/1 _____ 0s 172ms/step

□ Forecasted Waste for Ludhiana (next year): 3623.85 Tons/Day
1/1 _____ 0s 192ms/step

□ Forecasted Waste for Agra (next year): 5122.79 Tons/Day
1/1 _____ 0s 181ms/step

□ Forecasted Waste for Meerut (next year): 3929.37 Tons/Day
1/1 _____ 0s 264ms/step

□ Forecasted Waste for Nashik (next year): 4979.12 Tons/Day
1/1 _____ 0s 170ms/step

□ Forecasted Waste for Rajkot (next year): 5012.54 Tons/Day
1/1 _____ 0s 178ms/step

□ Forecasted Waste for Madurai (next year): 2276.50 Tons/Day
1/1 _____ 0s 172ms/step

□ Forecasted Waste for Jabalpur (next year): 5631.14 Tons/Day
1/1 _____ 0s 186ms/step

□ Forecasted Waste for Allahabad (next year): 5778.92 Tons/Day
1/1 _____ 0s 186ms/step

```
□ Forecasted Waste for Visakhapatnam (next year): 5474.69 Tons/Day  
1/1 _____ 0s 190ms/step  
□ Forecasted Waste for Gwalior (next year): 5837.37 Tons/Day
```

```
ce_features = [  
    'Recycling Rate (%)',  
    'Municipal Efficiency Score (1-10)',  
    'Awareness Campaigns Count',  
    'Waste_TPD', # from your dataset  
    'SDG 12',  
    'Waste_per_capita'  
]  
  
import pandas as pd  
import numpy as np  
from sklearn.preprocessing import StandardScaler  
from sklearn.cluster import KMeans  
from sklearn.metrics import silhouette_score, silhouette_samples  
from tensorflow.keras.models import Model  
from tensorflow.keras.layers import Input, Dense  
import matplotlib.pyplot as plt  
import seaborn as sns  
  
# Drop duplicates so each city only once  
ce_df = merged_df.drop_duplicates(subset='City_Name')  
  
# Filter CE feature columns and drop rows with missing values  
ce_data = ce_df[ce_features].dropna()  
  
# Save city names corresponding to filtered rows  
city_names = ce_df.loc[ce_data.index, 'City_Name'].values  
  
# --- 2. Scale the features ---  
scaler = StandardScaler()  
X_scaled = scaler.fit_transform(ce_data)  
  
# --- 3. Build Autoencoder for Dimensionality Reduction ---  
input_dim = X_scaled.shape[1]  
encoding_dim = 2 # compress to 2D for visualization  
  
input_layer = Input(shape=(input_dim,))  
encoded = Dense(5, activation='relu')(input_layer)  
encoded = Dense(encoding_dim, activation='relu')(encoded)  
decoded = Dense(5, activation='relu')(encoded)  
decoded = Dense(input_dim, activation='linear')(decoded)  
  
autoencoder = Model(inputs=input_layer, outputs=decoded)  
encoder = Model(inputs=input_layer, outputs=encoded)
```

```

autoencoder.compile(optimizer='adam', loss='mse')

# Train autoencoder
autoencoder.fit(X_scaled, X_scaled, epochs=100, batch_size=8,
verbose=0)

# --- 4. Extract encoded features ---
X_encoded = encoder.predict(X_scaled)

# --- 5. Cluster in encoded space ---
n_clusters = 3
kmeans = KMeans(n_clusters=n_clusters, random_state=42)
clusters = kmeans.fit_predict(X_encoded)

# --- 6. Silhouette score ---
silhouette_avg = silhouette_score(X_encoded, clusters)
print(f" Silhouette Score (Overall Clustering Quality):
{silhouette_avg:.2f}")

# Prepare DataFrame with embeddings and cluster info
encoded_df = pd.DataFrame(X_encoded, columns=['Dim1', 'Dim2'])
encoded_df['Cluster'] = clusters
encoded_df['City'] = city_names
encoded_df['Silhouette'] = silhouette_samples(X_encoded, clusters)

# --- 7. Visualization ---
plt.figure(figsize=(12, 10))
palette = sns.color_palette("Set1", n_colors=n_clusters)

sns.scatterplot(
    data=encoded_df,
    x='Dim1',
    y='Dim2',
    hue='Cluster',
    palette=palette,
    s=150,
    alpha=0.8,
    edgecolor='black'
)

# Plot cluster centers
centers = kmeans.cluster_centers_
plt.scatter(
    centers[:, 0], centers[:, 1],
    c='black', s=250, marker='X', label='Cluster Centers'
)

# Annotate city names with small offset
for i, row in encoded_df.iterrows():
    plt.text(row['Dim1'] + 0.03, row['Dim2'] + 0.03, row['City'],

```

```
fontsize=9, weight='bold')

plt.title("□ City Clusters based on Circular Economy Indicators",
fontsize=18, weight='bold')
plt.xlabel("Latent Dimension 1", fontsize=14)
plt.ylabel("Latent Dimension 2", fontsize=14)
plt.legend(title='Cluster', fontsize=12, title_fontsize=14)
plt.grid(True, linestyle='--', alpha=0.5)
plt.tight_layout()
plt.show()
```

1/1 ————— 0s 75ms/step

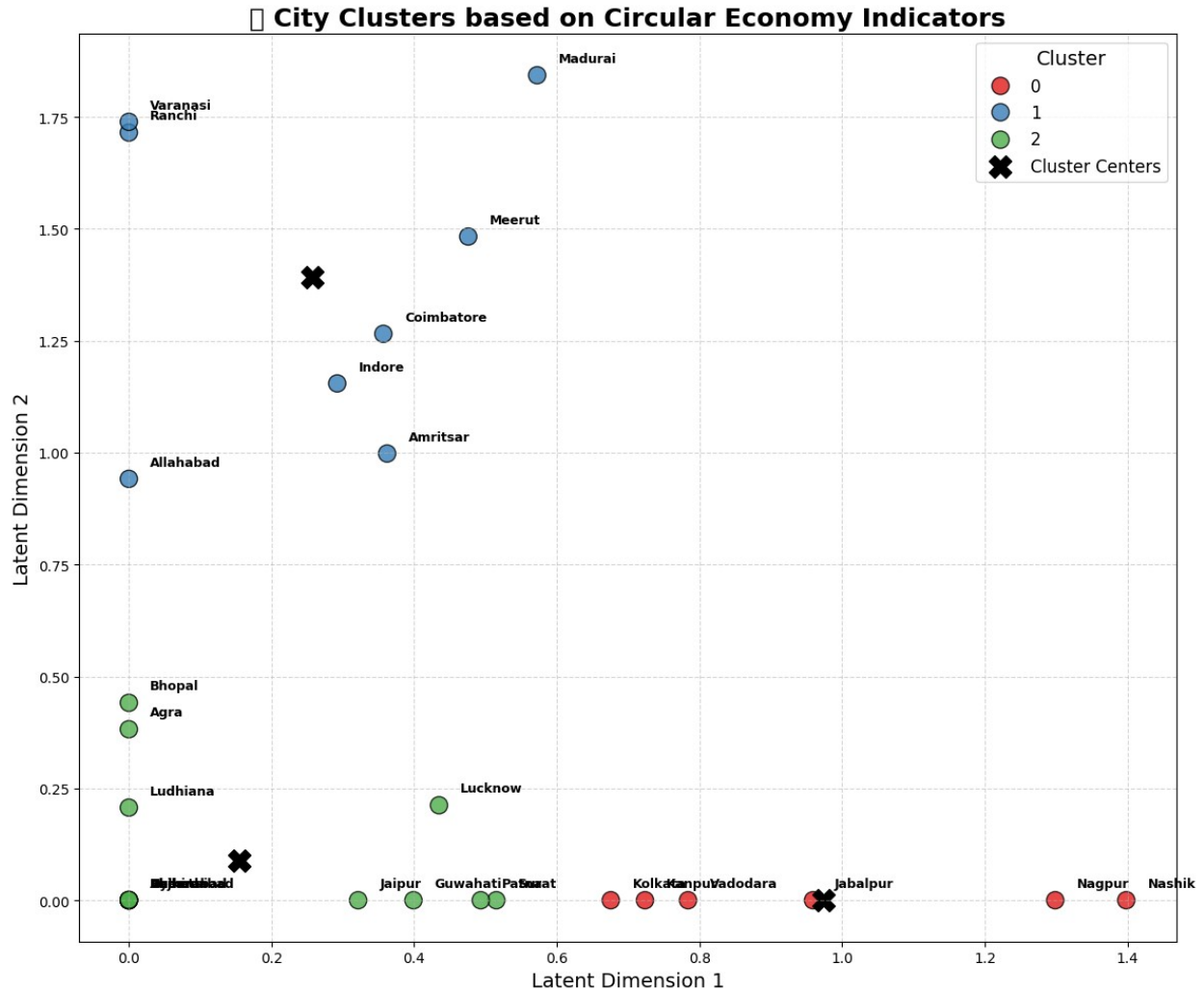
□ Silhouette Score (Overall Clustering Quality): 0.56

/tmp/ipython-input-19-1480003489.py:93: UserWarning:

Glyph 128260 (\N{ANTICLOCKWISE DOWNWARDS AND UPWARDS OPEN CIRCLE
ARROWS}) missing from font(s) DejaVu Sans.

/usr/local/lib/python3.11/dist-packages/IPython/core/pylabtools.py:151
: UserWarning:

Glyph 128260 (\N{ANTICLOCKWISE DOWNWARDS AND UPWARDS OPEN CIRCLE
ARROWS}) missing from font(s) DejaVu Sans.



```
# === 8. Silhouette Distribution Plot ===
plt.figure(figsize=(8, 5))
sns.histplot(encoded_df['Silhouette'], bins=10, kde=True,
color='skyblue')
plt.axvline(silhouette_avg, color='red', linestyle='--', label=f"Avg =
{silhouette_avg:.2f}")
plt.title("\n Silhouette Score Distribution")
plt.xlabel("Silhouette Score")
plt.ylabel("Number of Cities")
plt.legend()
plt.tight_layout()
plt.show()

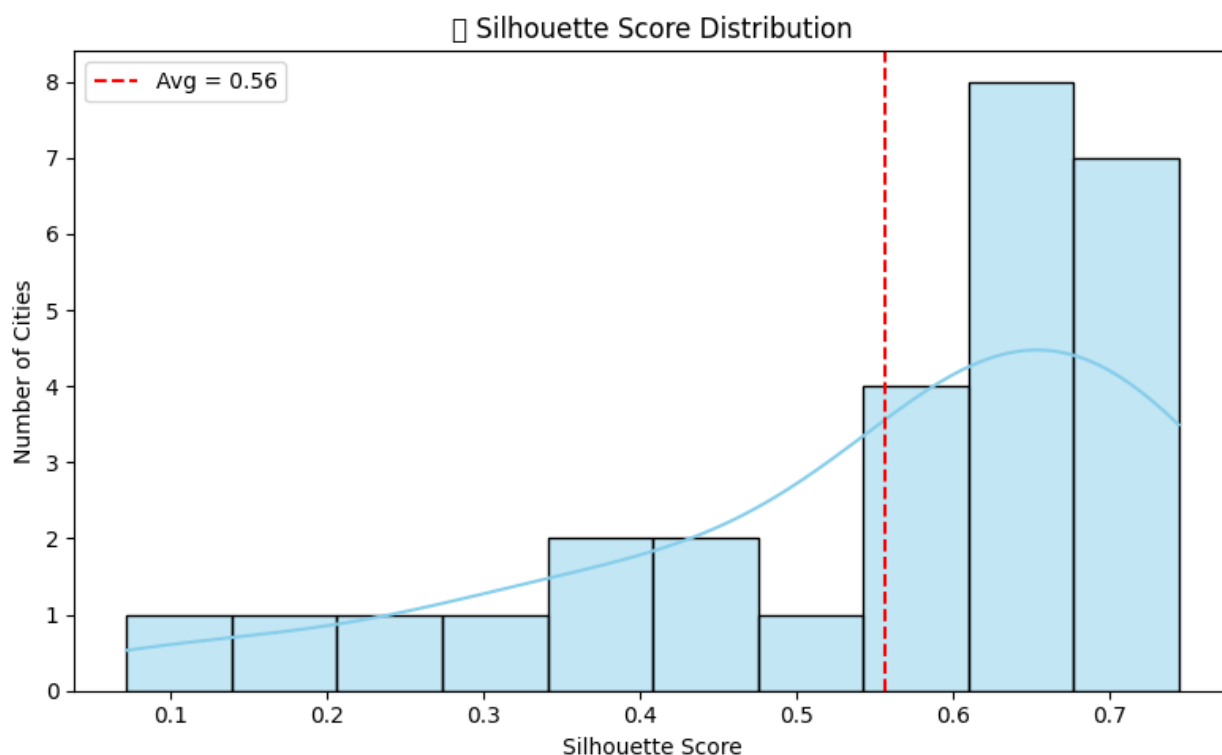
# === 9. Cluster-wise City Summary ===
cluster_summary = encoded_df.groupby('Cluster')['City'].apply(list)
for c, cities in cluster_summary.items():
    print(f"\n Cluster {c} ({len(cities)} cities):")
    print(", ".join(cities))
```

```
merged_df.to_csv("your_merged_ce_data.csv", index=False)
print(" Saved: your_merged_ce_data.csv")

# === 10. Save cluster results ===
encoded_df.to_csv("city_clusters_autoencoder.csv", index=False)

/tmp/ipython-input-20-1075552831.py:9: UserWarning:
Glyph 128207 (\N{STRAIGHT RULER}) missing from font(s) DejaVu Sans.

/usr/local/lib/python3.11/dist-packages/IPython/core/pylabtools.py:151
: UserWarning:
Glyph 128207 (\N{STRAIGHT RULER}) missing from font(s) DejaVu Sans.
```



```
 Cluster 0 (6 cities):
Kolkata, Kanpur, Nagpur, Vadodara, Nashik, Jabalpur

 Cluster 1 (8 cities):
Indore, Coimbatore, Ranchi, Amritsar, Varanasi, Meerut, Madurai,
Allahabad

 Cluster 2 (14 cities):
```

Delhi, Chennai, Hyderabad, Pune, Ahmedabad, Jaipur, Lucknow, Surat, Patna, Bhopal, Guwahati, Ludhiana, Agra, Rajkot

□ Saved: your_merged_ce_data.csv

Load cluster labels from saved CSV (from Phase 4)

```
cluster_df = pd.read_csv("city_clusters_autoencoder.csv")
```

Confirm the column names in cluster_df

```
print(cluster_df.columns)
```

```
Index(['Dim1', 'Dim2', 'Cluster', 'City', 'Silhouette'],  
      dtype='object')
```

```
import pandas as pd
```

Load your original merged CE dataset (adjust file path)

```
merged_df = pd.read_csv("your_merged_ce_data.csv")
```

Load clustering results from autoencoder step (adjust file path)

```
cluster_df = pd.read_csv("city_clusters_autoencoder.csv") # Has  
'City', 'Cluster', etc.
```

Merge cluster info with original CE dataset on city names

```
merged = pd.merge(  
    merged_df,  
    cluster_df[['City', 'Cluster']],  
    left_on='City_Name',  
    right_on='City',  
    how='inner'  
)
```

*# If after merge you see duplicate cluster columns (Cluster_x,
Cluster_y),*

keep 'Cluster_y' as final 'Cluster' and drop the rest

```
if 'Cluster_y' in merged.columns and 'Cluster_x' in merged.columns:  
    merged['Cluster'] = merged['Cluster_y']  
    merged.drop(columns=['Cluster_x', 'Cluster_y'], inplace=True)
```

Define CE action mapping based on cluster label

```
action_map = {  
    0: 'Rethink',  
    1: 'Redesign',  
    2: 'Reuse'  
}
```

Map cluster to CE Action

```
merged['CE_Action'] = merged['Cluster'].map(action_map)
```

Show sample output

```
print(merged[['City_Name', 'Cluster', 'CE_Action']].head(10))
```

```

# Save final dataframe with CE action recommendations
merged.to_csv("ce_action_recommendations.csv", index=False)
print("✅ Saved: ce_action_recommendations.csv")

   City_Name  Cluster CE_Action
0    Delhi      0    Rethink
1    Delhi      0    Rethink
2    Delhi      0    Rethink
3    Delhi      0    Rethink
4    Delhi      0    Rethink
5    Delhi      0    Rethink
6    Delhi      0    Rethink
7    Delhi      0    Rethink
8    Delhi      0    Rethink
9    Delhi      0    Rethink
✅ Saved: ce_action_recommendations.csv

import matplotlib.pyplot as plt
import seaborn as sns

# If 'Dim1' and 'Dim2' are missing, merge from cluster_df
if 'Dim1' not in merged.columns or 'Dim2' not in merged.columns:
    merged = merged.merge(
        cluster_df[['City', 'Dim1', 'Dim2']],
        left_on='City_Name',
        right_on='City',
        how='left'
    )

plt.figure(figsize=(12, 10))

# Use a distinct color palette for the CE_Action categories
palette = sns.color_palette("Set2", n_colors=3)

sns.scatterplot(
    data=merged,
    x='Dim1',
    y='Dim2',
    hue='CE_Action',
    palette=palette,
    s=150,
    edgecolor='black',
    alpha=0.8
)

# Annotate city names slightly offset
for i, row in merged.iterrows():
    plt.text(row['Dim1'] + 0.03, row['Dim2'] + 0.03, row['City_Name'],
            fontsize=9, weight='bold')

```



```
plt.title("Circular Economy Action Recommendations by City",
          fontsize=18, weight='bold')
plt.xlabel("Latent Dimension 1", fontsize=14)
plt.ylabel("Latent Dimension 2", fontsize=14)
plt.legend(title='CE Action', fontsize=12, title_fontsize=14)
plt.grid(True, linestyle='--', alpha=0.5)
plt.tight_layout()
plt.show()
```

/tmp/ipython-input-49-1996795105.py:38: UserWarning:

Glyph 128260 (\N{ANTICLOCKWISE DOWNWARDS AND UPWARDS OPEN CIRCLE
ARROWS}) missing from font(s) DejaVu Sans.

/usr/local/lib/python3.11/dist-packages/IPython/core/pylabtools.py:151
: UserWarning:

Glyph 128260 (\N{ANTICLOCKWISE DOWNWARDS AND UPWARDS OPEN CIRCLE
ARROWS}) missing from font(s) DejaVu Sans.


```

    'Circular_Score'
]

X = merged[features].copy()
y = merged['CE_Action']

# Encode target
le = LabelEncoder()
y_encoded = le.fit_transform(y) # Rethink:0, Redesign:1, Reuse:2

# Train-test split
X_train, X_test, y_train, y_test = train_test_split(X, y_encoded,
test_size=0.2, random_state=42, stratify=y_encoded)

# Scale features
scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)

import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Dropout, BatchNormalization
from sklearn.metrics import classification_report, accuracy_score

models = []
names = ['MLP_1layer', 'MLP_2layer', 'Dropout_MLP', 'BatchNorm_MLP',
'WideDeep_MLP']
histories = []
scores = []

for name in names:
    model = Sequential()
    model.add(Dense(64, input_shape=(X_train_scaled.shape[1],),
activation='relu'))

    if name == 'MLP_2layer':
        model.add(Dense(32, activation='relu'))

    elif name == 'Dropout_MLP':
        model.add(Dropout(0.3))
        model.add(Dense(32, activation='relu'))

    elif name == 'BatchNorm_MLP':
        model.add(BatchNormalization())
        model.add(Dense(32, activation='relu'))

    elif name == 'WideDeep_MLP':
        model.add(Dense(128, activation='relu'))
        model.add(Dense(64, activation='relu'))

    model.add(Dense(3, activation='softmax'))

```

```
model.compile(optimizer='adam',
loss='sparse_categorical_crossentropy', metrics=['accuracy'])
```

```
history = model.fit(X_train_scaled, y_train, epochs=100,
batch_size=8, verbose=0, validation_split=0.2)
```

```
y_pred = model.predict(X_test_scaled)
y_pred_labels = y_pred.argmax(axis=1)
```

```
acc = accuracy_score(y_test, y_pred_labels)
scores.append(acc)
models.append(model)
histories.append(history)
```

```
print(f"\n Model: {name}")
print(f"Accuracy: {acc:.4f}")
print(classification_report(y_test, y_pred_labels,
target_names=le.classes_))
```

```
/usr/local/lib/python3.11/dist-packages/keras/src/layers/core/
dense.py:87: UserWarning:
```

Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead.

5/5 ————— 0s 15ms/step

Model: MLP_1layer
Accuracy: 0.9143

	precision	recall	f1-score	support
Redesign	0.80	0.91	0.85	35
Rethink	0.95	0.91	0.93	85
Reuse	1.00	0.95	0.97	20
accuracy			0.91	140
macro avg	0.92	0.92	0.92	140
weighted avg	0.92	0.91	0.92	140

```
/usr/local/lib/python3.11/dist-packages/keras/src/layers/core/
dense.py:87: UserWarning:
```

Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead.

5/5 ————— 0s 15ms/step

□ Model: MLP_2layer

Accuracy: 0.9143

	precision	recall	f1-score	support
Redesign	0.85	0.94	0.89	35
Rethink	0.96	0.89	0.93	85
Reuse	0.86	0.95	0.90	20
accuracy			0.91	140
macro avg	0.89	0.93	0.91	140
weighted avg	0.92	0.91	0.91	140

/usr/local/lib/python3.11/dist-packages/keras/src/layers/core/dense.py:87: UserWarning:

Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead.

5/5 ————— 0s 14ms/step

□ Model: Dropout_MLP

Accuracy: 0.9786

	precision	recall	f1-score	support
Redesign	0.95	1.00	0.97	35
Rethink	0.99	0.98	0.98	85
Reuse	1.00	0.95	0.97	20
accuracy			0.98	140
macro avg	0.98	0.98	0.98	140
weighted avg	0.98	0.98	0.98	140

/usr/local/lib/python3.11/dist-packages/keras/src/layers/core/dense.py:87: UserWarning:

Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead.

5/5 ————— 0s 19ms/step

□ Model: BatchNorm_MLP

Accuracy: 0.8714

	precision	recall	f1-score	support
--	-----------	--------	----------	---------

Redesign	0.82	0.91	0.86	35
Rethink	0.94	0.85	0.89	85
Reuse	0.75	0.90	0.82	20
accuracy			0.87	140
macro avg	0.84	0.89	0.86	140
weighted avg	0.88	0.87	0.87	140

```
/usr/local/lib/python3.11/dist-packages/keras/src/layers/core/dense.py:87: UserWarning:
```

Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead.

5/5 ————— 0s 24ms/step

□ Model: WideDeep_MLP

Accuracy: 0.9357

	precision	recall	f1-score	support
Redesign	0.87	0.97	0.92	35
Rethink	0.97	0.92	0.95	85
Reuse	0.90	0.95	0.93	20
accuracy			0.94	140
macro avg	0.92	0.95	0.93	140
weighted avg	0.94	0.94	0.94	140

```
best_idx = scores.index(max(scores))
best_model = models[best_idx]
print(f"\n□ Best Model: {names[best_idx]} with Accuracy:
{scores[best_idx]:.4f}")
```

□ Best Model: Dropout_MLP with Accuracy: 0.9786

```
from sklearn.metrics import f1_score, confusion_matrix, roc_auc_score
from sklearn.preprocessing import label_binarize
import seaborn as sns
import matplotlib.pyplot as plt
```

```
# Get the trained Dropout_MLP model (assuming it's at index 2)
dropout_model = models[names.index('Dropout_MLP')]
```

```
# Predict
```

```
y_pred_probs = dropout_model.predict(X_test_scaled)
```

```

y_pred_labels = y_pred_probs.argmax(axis=1)

# === F1 Score ===
f1_macro = f1_score(y_test, y_pred_labels, average='macro')
print(f" F1 Score (macro): {f1_macro:.4f}")

# === Confusion Matrix ===
cm = confusion_matrix(y_test, y_pred_labels)

plt.figure(figsize=(6, 5))
sns.heatmap(cm, annot=True, fmt='d', cmap='Blues',
            xticklabels=le.classes_, yticklabels=le.classes_)
plt.title(" Confusion Matrix: Dropout_MLP")
plt.xlabel("Predicted Label")
plt.ylabel("True Label")
plt.tight_layout()
plt.show()

# === ROC-AUC (One-vs-Rest) ===
# Binarize y_test for multi-class ROC
y_test_bin = label_binarize(y_test, classes=[0, 1, 2])

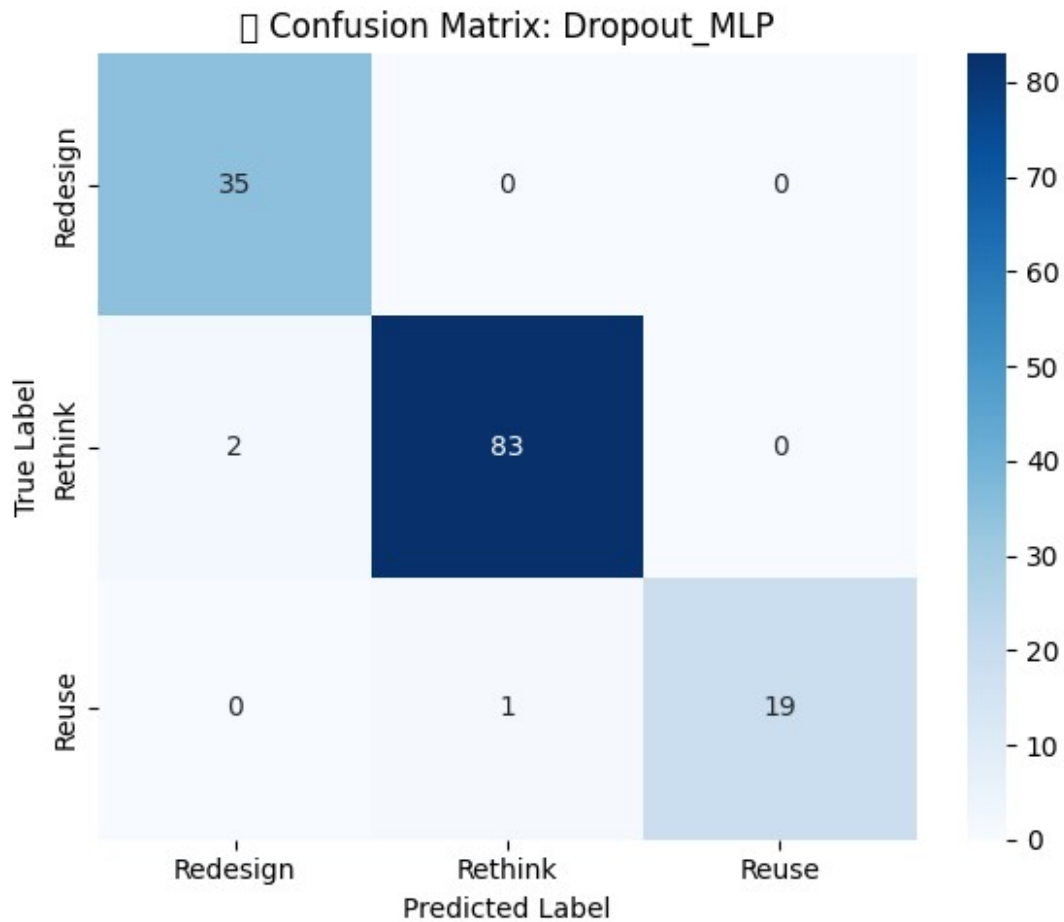
try:
    auc_ovr = roc_auc_score(y_test_bin, y_pred_probs,
multi_class='ovr')
    print(f" ROC-AUC (OvR): {auc_ovr:.4f}")
except ValueError:
    print("⚠ ROC-AUC could not be computed due to class imbalance or
missing classes in y_test.")

5/5 ————— 0s 5ms/step
 F1 Score (macro): 0.9763

/tmp/ipython-input-41-3134291662.py:26: UserWarning:
Glyph 128269 (\N{LEFT-POINTING MAGNIFYING GLASS}) missing from font(s)
DejaVu Sans.

/usr/local/lib/python3.11/dist-packages/IPython/core/pylabtools.py:151
: UserWarning:
Glyph 128269 (\N{LEFT-POINTING MAGNIFYING GLASS}) missing from font(s)
DejaVu Sans.

```



ROC-AUC (OvR): 0.9994

```
import shap
```

```
# Use SHAP KernelExplainer
```

```
explainer = shap.Explainer(best_model.predict, X_test_scaled)
shap_values = explainer(X_test_scaled[:50]) # Use a subset for speed
```

```
# SHAP summary plot
```

```
shap.summary_plot(shap_values, X_test.iloc[:50],
feature_names=features)
```

```
80/80 ██████████ 0s 1ms/step
80/80 ██████████ 0s 3ms/step
80/80 ██████████ 0s 2ms/step
80/80 ██████████ 0s 1ms/step
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80/80 ██████████ 0s 1ms/step
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80/80 ██████████ 0s 1ms/step
80/80 ██████████ 0s 1ms/step
80/80 ██████████ 0s 2ms/step
```


80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	3ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	3ms/step
80/80	=====	0s	4ms/step
80/80	=====	0s	5ms/step
80/80	=====	0s	4ms/step
80/80	=====	0s	3ms/step
79/79	=====	1s	7ms/step
79/79	=====	0s	5ms/step
79/79	=====	0s	3ms/step
79/79	=====	0s	3ms/step
79/79	=====	0s	2ms/step
79/79	=====	0s	3ms/step
79/79	=====	0s	2ms/step
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79/79	=====	0s	2ms/step
79/79	=====	0s	2ms/step
79/79	=====	0s	3ms/step
79/79	=====	0s	2ms/step
79/79	=====	0s	2ms/step
79/79	=====	0s	3ms/step
79/79	=====	0s	2ms/step
43/43	=====	0s	3ms/step

PermutationExplainer explainer: 4%|| | 2/50 [00:00<?, ?it/s]

81/81	=====	0s	2ms/step
81/81	=====	1s	5ms/step
81/81	=====	0s	5ms/step
81/81	=====	0s	3ms/step
81/81	=====	0s	5ms/step
81/81	=====	1s	5ms/step
81/81	=====	0s	5ms/step
81/81	=====	0s	2ms/step
81/81	=====	0s	4ms/step
81/81	=====	0s	2ms/step
81/81	=====	0s	5ms/step
81/81	=====	0s	2ms/step
81/81	=====	0s	2ms/step
81/81	=====	0s	1ms/step
81/81	=====	0s	1ms/step
81/81	=====	0s	1ms/step
81/81	=====	0s	1ms/step

81/81 _____ 0s 1ms/step
43/43 _____ 0s 2ms/step

PermutationExplainer explainer: 8%|██████████ | 4/50 [00:29<04:08, 5.40s/it]

79/79 _____ 0s 1ms/step
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79/79 _____ 0s 1ms/step
79/79 _____ 0s 1ms/step
79/79 _____ 0s 1ms/step
79/79 _____ 0s 1ms/step
79/79 _____ 0s 1ms/step
79/79 _____ 0s 1ms/step
79/79 _____ 0s 1ms/step
79/79 _____ 0s 1ms/step
43/43 _____ 0s 2ms/step

PermutationExplainer explainer: 10%|██████████ | 5/50 [00:33<03:41, 4.92s/it]

78/78 _____ 0s 1ms/step
78/78 _____ 0s 1ms/step
78/78 _____ 0s 1ms/step
78/78 _____ 0s 1ms/step
78/78 _____ 0s 1ms/step
78/78 _____ 0s 1ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 2ms/step
78/78 _____ 0s 1ms/step
78/78 _____ 0s 1ms/step
78/78 _____ 0s 1ms/step
43/43 _____ 0s 1ms/step

PermutationExplainer explainer: 12% | 6/50 [00:39<03:45, 5.13s/it]

80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
43/43	=====	0s	1ms/step

PermutationExplainer explainer: 14% | 7/50 [00:43<03:20, 4.66s/it]

79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	2ms/step
44/44	=====	0s	2ms/step

PermutationExplainer explainer: 16% | 8/50 [00:47<03:07, 4.47s/it]

80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	2ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
44/44	=====	0s	2ms/step

PermutationExplainer explainer: 18%|██████████| 9/50 [00:52<03:14, 4.74s/it]

79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
43/43	=====	0s	1ms/step

PermutationExplainer explainer: 20%|██████████| 10/50 [00:56<03:01, 4.53s/it]

81/81	=====	0s	1ms/step
81/81	=====	0s	1ms/step
81/81	=====	0s	1ms/step
81/81	=====	0s	1ms/step

81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	2ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
81/81	0s	2ms/step
81/81	0s	1ms/step
81/81	0s	1ms/step
44/44	0s	1ms/step

```
PermutationExplainer explainer: 44%|██████████ | 22/50 [01:52<02:07, 4.56s/it]
```

83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	1ms/step
83/83	0s	2ms/step
83/83	0s	2ms/step
83/83	0s	2ms/step
83/83	0s	2ms/step
83/83	0s	2ms/step
83/83	0s	2ms/step
83/83	0s	2ms/step
44/44	0s	2ms/step

```
PermutationExplainer explainer: 46%|██████████| 23/50 [01:58<02:11, 4.86s/it]
```

79/79	0s 2ms/step
79/79	0s 2ms/step
79/79	0s 1ms/step
79/79	0s 1ms/step

79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
79/79	=====	0s	1ms/step
44/44	=====	0s	1ms/step

```
PermutationExplainer explainer: 48%|██████████ | 24/50 [02:02<02:02, 4.72s/it]
```

80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
43/43	=====	0s	1ms/step

```
PermutationExplainer explainer: 50%|██████████| 25/50 [02:06<01:51, 4.46s/it]
```

[illegible]

79/79	0s	1ms/step
79/79	0s	1ms/step
79/79	0s	1ms/step
79/79	0s	1ms/step
79/79	0s	1ms/step
79/79	0s	1ms/step
79/79	0s	2ms/step
79/79	0s	1ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	2ms/step
79/79	0s	1ms/step
43/43	0s	1ms/step

```
PermutationExplainer explainer: 70%|██████████ | 35/50 [02:52<01:11, 4.75s/it]
```

80/80	0s	2ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	2ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
80/80	0s	1ms/step
44/44	0s	1ms/step

```
PermutationExplainer explainer: 72%|██████████| 36/50 [02:56<01:03, 4.57s/it]
```

80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step
80/80	=====	0s	1ms/step

79/79	0s 2ms/step
79/79	0s 2ms/step
79/79	0s 1ms/step
79/79	0s 1ms/step
79/79	0s 1ms/step
79/79	0s 1ms/step
44/44	0s 2ms/step

```
PermutationExplainer explainer: 82%|██████████ | 41/50 [03:19<00:42, 4.72s/it]
```

78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	2ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	2ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	2ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
78/78	0s	1ms/step
43/43	0s	2ms/step

```
PermutationExplainer explainer: 84%|██████████ | 42/50 [03:23<00:35, 4.50s/it]
```

[illegible]

PermutationExplainer explainer: 90%|██████████ | 45/50 [03:38<00:23, 4.69s/it]

80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
80/80	██████████	0s	1ms/step
44/44	██████████	0s	2ms/step

PermutationExplainer explainer: 92%|██████████ | 46/50 [03:42<00:18, 4.55s/it]

79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	2ms/step
79/79	██████████	0s	1ms/step
79/79	██████████	0s	1ms/step
79/79	██████████	0s	1ms/step
79/79	██████████	0s	1ms/step
79/79	██████████	0s	1ms/step
79/79	██████████	0s	1ms/step
79/79	██████████	0s	1ms/step
79/79	██████████	0s	1ms/step
43/43	██████████	0s	1ms/step

PermutationExplainer explainer: 94%|██████████ | 47/50 [03:47<00:14, 4.79s/it]

```
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
44/44 _____ 0s 1ms/step
```

PermutationExplainer explainer: 96%|██████████| 48/50 [03:51<00:09, 4.54s/it]

```
81/81 _____ 0s 1ms/step
81/81 _____ 0s 2ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 2ms/step
81/81 _____ 0s 1ms/step
81/81 _____ 0s 1ms/step
44/44 _____ 0s 2ms/step
```

PermutationExplainer explainer: 98%|██████████| 49/50 [03:55<00:04, 4.44s/it]

```
79/79 _____ 0s 2ms/step
79/79 _____ 0s 2ms/step
79/79 _____ 0s 2ms/step
79/79 _____ 0s 2ms/step
```

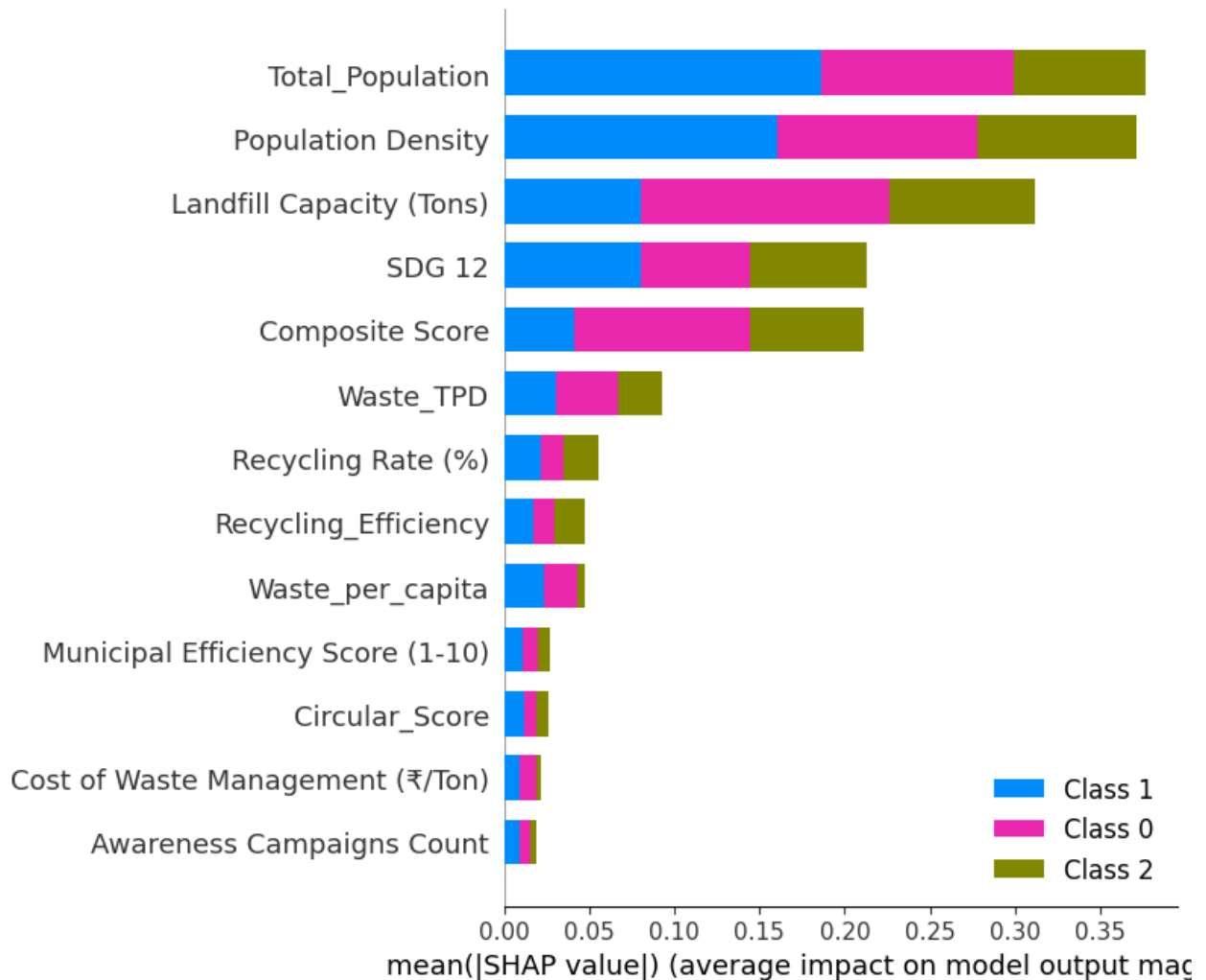
```
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
43/43 ██████████ 0s 2ms/step
```

```
PermutationExplainer explainer: 100%|██████████| 50/50 [04:01<00:00, 4.72s/it]
```

```
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 1ms/step
79/79 ██████████ 0s 2ms/step
79/79 ██████████ 0s 1ms/step
44/44 ██████████ 0s 2ms/step
```

```
PermutationExplainer explainer: 5lit [04:07, 5.04s/it]
/tmp/ipython-input-43-4008263907.py:8: FutureWarning:
```

The NumPy global RNG was seeded by calling ``np.random.seed``. In a future version this function will no longer use the global RNG. Pass ``rng`` explicitly to opt-in to the new behaviour and silence this warning.



```
import matplotlib.pyplot as plt

# Get the training history for Dropout_MLP (index 2)
history = histories[names.index('Dropout_MLP')]

# Plot training & validation accuracy
plt.figure(figsize=(12, 5))

# --- Accuracy Plot ---
plt.subplot(1, 2, 1)
plt.plot(history.history['accuracy'], label='Train Accuracy',
linewidth=2)
plt.plot(history.history['val_accuracy'], label='Val Accuracy',
linewidth=2, linestyle='--')
plt.title('□ Dropout_MLP - Accuracy over Epochs', fontsize=14)
plt.xlabel('Epochs')
plt.ylabel('Accuracy')
plt.legend()
```



```
plt.grid(True)

# --- Loss Plot ---
plt.subplot(1, 2, 2)
plt.plot(history.history['loss'], label='Train Loss', linewidth=2)
plt.plot(history.history['val_loss'], label='Val Loss', linewidth=2,
linestyle='--')
plt.title('□ Dropout_MLP - Loss over Epochs', fontsize=14)
plt.xlabel('Epochs')
plt.ylabel('Loss')
plt.legend()
plt.grid(True)

plt.tight_layout()
plt.show()
```

/tmp/ipython-input-44-1472516604.py:29: UserWarning:

Glyph 128200 (\N{CHART WITH UPWARDS TREND}) missing from font(s)
DejaVu Sans.

/tmp/ipython-input-44-1472516604.py:29: UserWarning:

Glyph 128201 (\N{CHART WITH DOWNWARDS TREND}) missing from font(s)
DejaVu Sans.

/usr/local/lib/python3.11/dist-packages/IPython/core/pylabtools.py:151
: UserWarning:

Glyph 128200 (\N{CHART WITH UPWARDS TREND}) missing from font(s)
DejaVu Sans.

/usr/local/lib/python3.11/dist-packages/IPython/core/pylabtools.py:151
: UserWarning:

Glyph 128201 (\N{CHART WITH DOWNWARDS TREND}) missing from font(s)
DejaVu Sans.

