

Sortings

longest substring : no duplicates ✓

function fun(s,n)

{

head=0

✓ map={}

✓ res=0

→ for(tail=0;tail<n;tail++)

{

↓ key=s[tail]

while(key in map and map[key]>0)

{

✓ 1. res=max(res,tail-head)

✓ 2. map[s[head]]=map[s[head]]-1

✓ 3. head++

}

if key in map

{

map[key]++

}

else

{

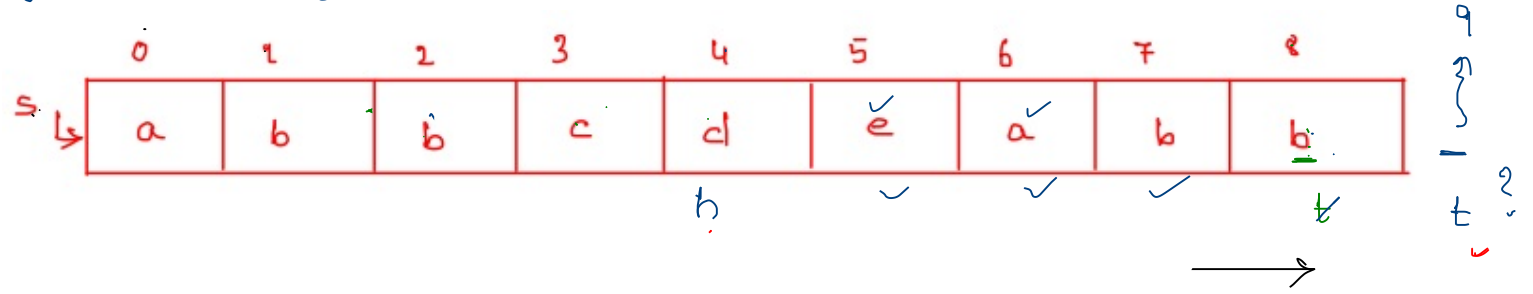
map[key]=1

}

}

✓ return max(res,tail-head) 5 ✓

}



map

key	value
d	1
e	1
a	1
b	1

key = d
res = 5
5 ✓
5 ✓
2 ✓
b ✓ ✓

completion ✓

map[key]>0)

1, 2, ...

≥ 1

map[key]>=1

By-default, we consider as inc. order, \therefore - strictly no duplicates.
non-decreasing order.

✓ 1) Bubble sort \therefore -

Ex :-

i/p

	0	1	2	3	4	5
a \hookrightarrow	9	7	6	4	2	1

$n=6$

\hookrightarrow 2 4 4 5 6 9 9 . . .

o/p

	0	1	2	3	4	5
a \hookrightarrow	1	2	4	6	7	9

\uparrow order

* *

idea : works by repeatedly swapping the adjacent elements if they are not in the proper
order

6, 7, 9 ✓ ↪ ↑ order

7, 6, 9 ✗

~~7~~ ~~6~~ 9
— —
↺
swap

6 7 9 ✓
 └─┘
no swap

$n=6$

	0	1	2	3	4	5
a →	9	7	6	4	2	1

✓ every pass will start from index-0 (beg)
 → everytime adjacent elements only compared.

Pass-1:-

$i=0$ i/p : $\begin{matrix} j \\ \text{9} \end{matrix}$ $\begin{matrix} j \\ \text{7} \end{matrix}$ $\begin{matrix} j \\ \text{6} \end{matrix}$ $\begin{matrix} j \\ \text{4} \end{matrix}$ $\begin{matrix} j \\ \text{2} \end{matrix}$ $\begin{matrix} j \\ \text{1} \end{matrix}$?

$\begin{matrix} 7 \\ \text{---} \\ 6 \\ \text{---} \\ 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 9 \\ \text{---} \\ 7 \\ \text{---} \\ 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 6 \\ \text{---} \\ 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 1 \\ \text{---} \\ 9 \end{matrix}$

final o/p of P_1 : 7 6 4 2 1 9

$i=0, j=0$ to 4

$i=1, j=0$ to 3

$i=2, j=0$ to 2

$i=1$
 Pass2:-

$\begin{matrix} 7 \\ \text{---} \\ 6 \\ \text{---} \\ 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 6 \\ \text{---} \\ 7 \\ \text{---} \\ 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 4 \\ \text{---} \\ 7 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 2 \\ \text{---} \\ 7 \\ \text{---} \\ 1 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 1 \\ \text{---} \\ 7 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 9 \end{matrix}$

o/p of P_2 : 6 4 2 1 7 9

$i=2$
 Pass3:-

$\begin{matrix} 6 \\ \text{---} \\ 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 7 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 4 \\ \text{---} \\ 2 \\ \text{---} \\ 1 \\ \text{---} \\ 6 \\ \text{---} \\ 7 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 2 \\ \text{---} \\ 1 \\ \text{---} \\ 6 \\ \text{---} \\ 7 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 1 \\ \text{---} \\ 6 \\ \text{---} \\ 7 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 7 \\ \text{---} \\ 9 \end{matrix}$ $\begin{matrix} 9 \end{matrix}$

Pass4:-

$i=3$ 2 1 4 6 7 9

Pass5:-

$i=4$ 1 2 4 6 7 9 ✓

$i=5 \times$

$n=6$ ✓

	0	1	2	3	4	5
a →	9	7	6	4	2	1

 ✓

o/p of

✓ P_1 : 7 6 4 2 1 (9) ✓
↑

✓ P_2 : 6 4 2 1 (7) (9)
↑

✓ P_3 : 4 2 1 (6) (7) (9)
↑

✓ P_4 : 2 1 (4) (6) (7) (9)

✓ P_5 : 1 (2) (4) (6) (7) (9) ✓
←————→

P_6 ?

out of 6 elements, if 5 elements in the correct position of final sorted list

which means 6th element automatically in its correct position

so we can say here 5 passes are enough when $n=6$

so we can say $n-1$ passes are enough

```

function bubbleSort(arr,n)
{
    for(i=0;i<=n-2;i++) // runs for n-1 times, because we need n-1 passes
    {
        for(j=0;j<=n-i-2;j++) // j loop is responsible for with in the pass what happening?
        {
            if(arr[j]>arr[j+1]) // out of order
            {
                temp=arr[j]
                arr[j]=arr[j+1]
                arr[j+1]=temp
            }
        }
    }
}

```

including when $n=6$

$i=0$, $j=0$ to <u>4</u> ✓	$6-0-2=4$
$i=1$, $j=0$ to <u>3</u>	$6-1-2=3$
$i=2$, $j=0$ to <u>2</u>	$6-2-2=2$
	\vdots
	$\leq n-i-2$


```
function bubbleSort(arr,n)
{
    for(i=0;i<=n-2;i++) // runs for n-1 times, because we need n-1 passes
    {
        for(j=0;j<n-i-1;j++) // j loop is responsible for within the pass what happening?
        {
            if(arr[j]>arr[j+1]) // out of order
            {
                temp=arr[j]
                arr[j]=arr[j+1]
                arr[j+1]=temp
            }
        }
    }
}
```

function bubbleSort(arr,n)

```
{
  for(i=0;i<n-1;i++)
  {
    → for(j=0;j<=n-i-2;j++)
    {
      if(arr[j]>arr[j+1])
      {
        temp=arr[j]
        arr[j]=arr[j+1]
        arr[j+1]=temp
      }
    }
  }
}
```

$n=6$ ✓

5
passes

		# of comp's	# of Swaps	
P ₁	i=0 j=0 1 2 3 4 5	5	✓ ✓ ✓ ✓ ✓	5
P ₂	i=1	4		4
P ₃	i=2	3		3
P ₄	i=3	2		2
P ₅	i=4	1		1

$n=6$, total comp's : $1+2+3+4+5$
 , total swaps : $1+2+3+4+5$

in general : $1+2+3+\dots+n-1 = \frac{n(n-1)}{2}$ } total # of comp's
 same as swaps
 $n \rightarrow \text{replace : } n-1$

$$1+2+3+\dots+n-1+n = \frac{n(n+1)}{2}$$

$\therefore O(n^2)$ ✓

i/p

	0	1	2	3	4	5	$n=6$
$a \rightarrow$	1	2	3	4	5	6	

✓

```
function bubbleSort(arr,n)
{
    for(i=0;i<n-1;i++)
    {
        for(j=0;j<=n-i-2;j++)
        {
            if(arr[j]>arr[j+1])
            {
                temp=arr[j]
                arr[j]=arr[j+1]
                arr[j+1]=temp
            }
        }
    }
}
```

total comp's = 15
total swaps = 0 ✓

in general -

$$\frac{\frac{n(n-1)}{2}}{0}$$

T.C:
 $O(n^2)$ ✓

```

function modifiedBubbleSort(arr,n)
{
    for(i=0;i<n-1;i++) // pass=1
    {
        flag=0
        for(j=0;j<=n-i-2;j++) // sorted
        {
            if(arr[j]>arr[j+1])
            {
                temp=arr[j]
                arr[j]=arr[j+1]
                arr[j+1]=temp
                flag=1
            }
        }
        if(flag==0) // swap not happened
        {
            break
        }
    }
}

```

\rightarrow i/p : already \uparrow order : Tc: $O(n)$
 \rightarrow i/p : o/w : $O(n^2)$

selection sort

↳ next class (Friday)

$n=6$

	0	1	2	3	4	5
a ↪	9	7	6	4	2	1

```
function selectionSort(arr[], n)
{
    for( i=0;i<n-1;i++)
    {
        min_index=i;
        for(j=i+1;j<n;j++)
        {
            if(arr[j]<arr[min_index])
            {
                min_index=j;
            }
        }
        if(min_index!=i)
        {
            temp=arr[min_index];
            arr[min_index]=arr[i];
            arr[i]=temp;
        }
    }
}
```