

Problem 9.8 Equation 9.36 describes the most general **linearly** polarized wave on a string. Linear (or "plane") polarization (so called because the displacement is parallel to a fixed vector \hat{n}) results from the combination of horizontally and vertically polarized waves of the *same phase* (Eq. 9.39). If the two components are of equal amplitude, but *out of phase* by 90° (say, $\delta_v = 0$, $\delta_h = 90^\circ$), the result is a *circularly* polarized wave. In that case:

(a) At a fixed point z , show that the string moves in a circle about the z axis. Does it go *clockwise* or *counterclockwise*, as you look down the axis toward the origin? How would you construct a wave circling the *other way*? (In optics, the clockwise case is called **right circular polarization**, and the counterclockwise, **left circular polarization**.)

(b) Sketch the string at time $t = 0$.

(c) How would you shake the string in order to produce a circularly polarized wave?

Problem 9.9 Write down the (real) electric and magnetic fields for a monochromatic plane wave of amplitude E_0 , frequency ω , and phase angle zero that is (a) traveling in the negative x direction and polarized in the z direction; (b) traveling in the direction from the origin to the point $(1, 1, 1)$, with polarization parallel to the xz plane. In each case, sketch the wave, and give the explicit Cartesian components of \mathbf{k} and \hat{n} .

Problem 9.10 The intensity of sunlight hitting the earth is about 1300 W/m^2 . If sunlight strikes a perfect absorber, what pressure does it exert? How about a perfect reflector? What fraction of atmospheric pressure does this amount to?

Problem 9.11 In the complex notation there is a clever device for finding the time average of a product. Suppose $f(\mathbf{r}, t) = A \cos(\mathbf{k} \cdot \mathbf{r} - \omega t + \delta_a)$ and $g(\mathbf{r}, t) = B \cos(\mathbf{k} \cdot \mathbf{r} - \omega t + \delta_b)$. Show that $\langle fg \rangle = (1/2) \text{Re}(\tilde{f} \tilde{g}^*)$, where the star denotes complex conjugation. [Note that this only works if the two waves have the same \mathbf{k} and ω , but they need not have the same amplitude or phase.] For example

$$\langle u \rangle = \frac{1}{4} \text{Re}(\epsilon_0 \tilde{\mathbf{E}} \cdot \tilde{\mathbf{E}}^* + \frac{1}{\mu_0} \tilde{\mathbf{B}} \cdot \tilde{\mathbf{B}}^*) \quad \text{and} \quad \langle S \rangle = \frac{1}{2\mu_0} \text{Re}(\tilde{\mathbf{E}} \times \tilde{\mathbf{B}}^*).$$

Problem 9.12 Find all elements of the Maxwell stress tensor for a monochromatic plane wave traveling in the z direction and linearly polarized in the x direction (Eq. 9.48). Does your answer make sense? (Remember that $\hat{\mathbf{T}}$ represents the momentum flux density.) How is the momentum flux density related to the energy density, in this case?

Find all the Maxwell stress tensor for the wave of 9.9.