Dealing with Missing Data

Challenges and Solutions

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Handling Missing Values is Easy!

Functions automatically exclude missing values:

```
## [...]
## Residual standard error: 2.305 on 69 degrees of freedom
## (25 observations deleted due to missingness)
## Multiple R-squared: 0.09255, Adjusted R-squared: 0.02679
## F-statistic: 1.407 on 5 and 69 DF, p-value: 0.2325
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1

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```

Imputation is super easy:

```
library("mice")
imp <- mice(mydata)</pre>
```

However ...

Complete case analysis is usually biased

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(Imputation) methods make certain assumptions, e.g.:

▶ missingness is M(C)AR

Complete case analysis is usually biased

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violation → bias

Imputation ???



Remind me, how did that imputation thing work again???

3

Imputation

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filling in missing values with (good) guesses

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Important:

Missing values → **uncertainty**This needs to be taken into account!!!

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This needs to be taken into account!!!

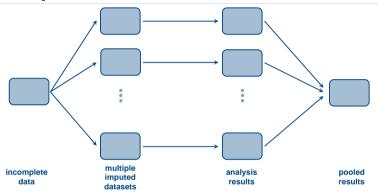
Donald Rubin (in the 1970s): Represent each missing value with **multiple imputed values**

Multiple Imputation

Note:

Imputation is not the only approach to handle missing values. (Also: maximum likelihood, inverse probability weighting, ...)

Multiple Imputation



- 1. Imputation: impute multiple times → multiple completed datasets
- 2. Analysis: analyse each of the datasets
- 3. Pooling: combine results, taking into account additional uncertainty

Imputation Step

Two main approaches

Joint Model Multiple Imputation

- ► the "original" approach
- ▶ often using a multivariate normal distribution

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Multiple Imputation with Chained Equations (MICE)

- also: Fully Conditional Specification (FCS)
- now often considered the gold standard

For each incomplete variable, specify a model using all other variables:

full conditionals

x_1	x_2	X_3	X_4	• • •
√	✓	NA	NA	
NA	\checkmark	\checkmark	NA	
\checkmark	NA	NA	\checkmark	
:				
:	:	:	:	

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\checkmark	✓	NA	NA	
NA	\checkmark	\checkmark	NA	
\checkmark	NA	NA	\checkmark	
:	:	:	:	
:	•	:	:	

$$x_1 \sim x_2 + x_3 + x_4 + \dots$$

 $x_2 \sim x_1 + x_3 + x_4 + \dots$
 $x_3 \sim x_1 + x_2 + x_4 + \dots$
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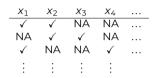
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:

For example:

- ▶ linear regression
- ▶ logistic regression
- ▶ ..

MICE is an iterative algorithm:

start with initial guess



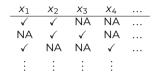
MICE is an iterative algorithm:

- start with initial guess
- update x_1 based on initial values of $x_2, x_3, x_4, ...$

x_1	x_2	<i>X</i> 3	X_4	
√	√	NA	NA	
NA	\checkmark	\checkmark	NA	
\checkmark	NA	NA	\checkmark	
÷	÷	:	:	

MICE is an iterative algorithm:

- start with initial guess
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- ▶ update x_2 based on new x_1 and initial values of $x_3, x_4, ...$
- ▶ ..



MICE is an iterative algorithm:

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- ▶ update x_2 based on new x_1 and initial values of $x_3, x_4, ...$
- **.**...
- update x_1 again, based on updated $x_2, x_3, x_4, ...$
- ▶ ..

x_1	<i>X</i> ₂	<i>X</i> 3	<i>X</i> ₄	
\checkmark	✓	NA	NA	
NA	\checkmark	\checkmark	NA	
\checkmark	NA	NA	\checkmark	
÷	:	:	:	

MICE makes assumptions

- **▶ missingness** is M(C)AR
- ▶ the incomplete variable has a certain conditional distribution (e.g. normal)
- ► all associations are linear
- compatibility and congeniality

Missing Completely At Random (MCAR) Missing At Random (MAR) Missing Not At Random (MNAR)

Missing Completely At Random (MCAR)

$$p(R \mid X_{obs}, X_{mis}) = p(R)$$

Missingness is independent of all data.

questionnaire got lost in mail

Missing At Random (MAR)

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Missingness depends only on observed data.

overweight participants are less likely to report their chocolate consumption (and we know their weight)

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Missing Not At Random (MNAR)

$$p(R \mid X_{obs}, X_{mis}) \neq p(R \mid X_{obs})$$

Missingness depends (also) on unobserved data.

overweight participants are less likely to report their weight

MICE makes assumptions

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In case of MNAR: MICE → bias

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For example:

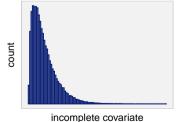
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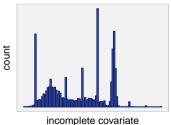
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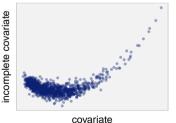
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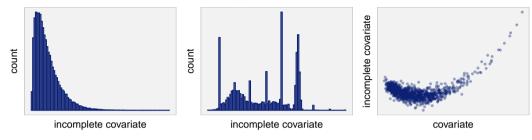
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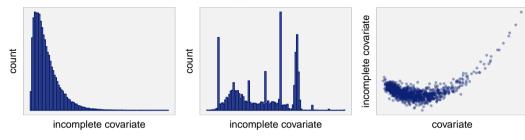








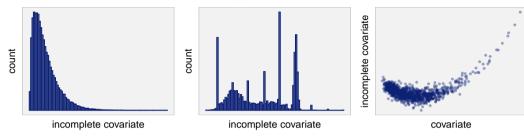
- misspecification of the residual distribution
- ► misspecification of the association structure



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- misspecification of the association structure

Partial solutions:

- Predictive Mean Matching
- ► Passive imputation



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- ▶ misspecification of the association structure

Partial solutions:

- Predictive Mean Matching
- Passive imputation

But...

- can get tedious
- requires knowledge (about data & methods)
- users often inexperienced and/or lazy

MICE makes assumptions

(Imputation) methods make certain assumptions, e.g.:

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Model misspecification → bias

MICE makes assumptions

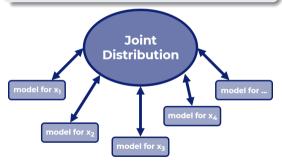
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Compatibility & Congeniality

Compatibility

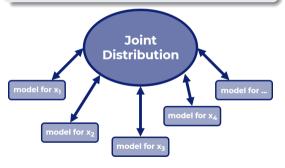
A **joint distribution** exists, that has the full conditionals (imputation models) as its conditional distributions.



Compatibility & Congeniality

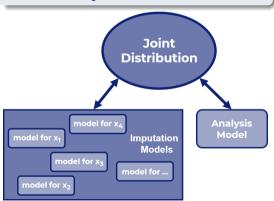
Compatibility

A **joint distribution** exists, that has the full conditionals (imputation models) as its conditional distributions.



Congeniality

The imputation model is compatible with the **analysis model**.



MICE is based on the idea of

Gibbs sampling

Exploits the fact that a joint distribution is fully determined by its full conditional distributions.



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Gibbs sampling

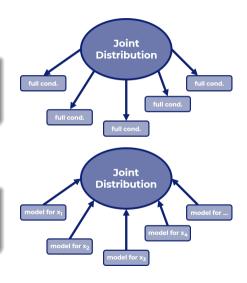
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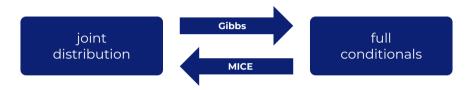
In MICE

Imputation models are specified directly

→ no guarantee that a corresponding joint distribution exists







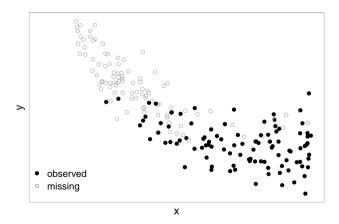
Is this a problem?

- often not
- but it can be when
 - imputation/analysis models contradict each other
 - ▶ different assumptions are made during analysis and imputation
 - ▶ the **outcome cannot easily be included** in the imputation models

Example 1: Contradicting Models

Analysis model with a quadratic association:

$$y = \beta_0 + \beta_1 x + \beta_2 x^2 + \dots$$

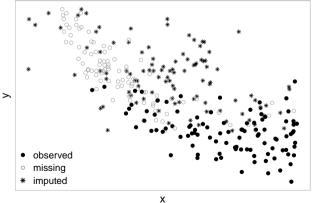


Example 1: Contradicting Models

Imputation model for x (when using MICE naively):

$$x = \theta_{10} + \theta_{11}y + \dots,$$

i.e., a **linear relation** between x and y is assumed.

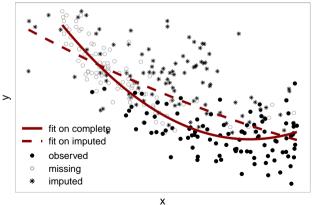


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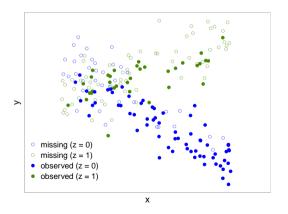


Example 2: Contradicting Models

Analysis model with interaction term:

$$y = \beta_0 + \beta_x x + \beta_z z + \beta_{xz} xz + \dots,$$

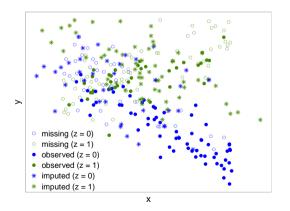
i.e., y again has a **non-linear relationship** with x



Example 2: Contradicting Models

Imputation model for *x* (when using MICE naively):

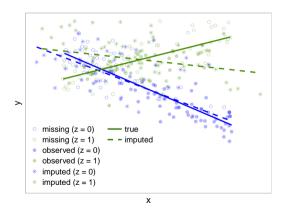
$$x = \theta_{10} + \theta_{11}y + \theta_{12}z + \dots,$$



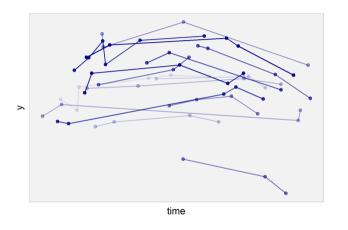
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Example 3: Longitudinal / Multi-level Data



id	time	У	Х
1	0.34	0.12	\checkmark
1	0.65	-0.04	\checkmark
1	0.68	0.30	\checkmark
1	1.97	0.44	\checkmark
1	2.38	0.48	\checkmark
1	3.09	0.46	\checkmark
2	$\bar{2}.\bar{1}\bar{1}$	0.43	$\bar{N}\bar{A}$
2	3.72	0.46	NA
2	3.82	0.46	NA
2	4.13	0.29	NA
:	:		- -

Example 3: Longitudinal / Multi-level Data

Imputation in long format

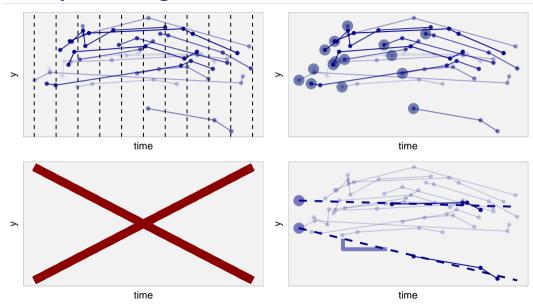
- rows are treated as independent
- imputations in baseline covariates will vary over time
- ⇒ bias

Can we use data in **wide format** (one row per subject)?

- can be very inefficient
- not always possible

id	time	У	X
1	0.34	0.12	√
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	<u> </u>	•	<u> </u>

Example 3: Longitudinal / Multi-level Data



Lack of compatibility / congeniality can become a **problem for MICE** in settings with

- ► Non-linear associations
 - ► non-linear effects
 - ▶ interaction terms
 - **▶** ...
- complex outcomes
 - multi-level settings
 - ▶ time-to-event outcomes
 - **.**..

What can we do in these settings?

Remember, the **problem** is



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⇒ Solution: Start with the joint distribution!

Remember, the **problem** is



⇒ Solution: Start with the joint distribution!

New problem:

What is the multivariate distribution of multiple variables of different types?

Remember, the **problem** is



→ Solution: Start with the joint distribution!

New problem:

What is the multivariate distribution of multiple variables of different types?

🙁 Usually, the joint distribution is not of any known form.

Joint Model Imputation

Multivariate Normal Model

Approximate the joint distribution by a known multivariate (usually normal) distribution

- ▶ this is **Joint Model** Multiple Imputation
- ② assures compatibility & congeniality
- (2) can't handle non-linear associations

Joint Model Imputation

Multivariate Normal Model

Approximate the joint distribution by a known multivariate (usually normal) distribution

- ▶ this is Joint Model Multiple Imputation
- 3 assures compatibility & congeniality
- (2) can't handle non-linear associations

Sequential Factorization

Factorize the joint distribution into (a sequence of) conditional distributions.

- (2) assures compatibility & congeniality
- © can handle non-linear associations

Sequential Factorization

A **joint distribution** p(y,x) can be written as the product of conditional distributions:

$$p(y,x) = p(y \mid x) p(x)$$

(or alternatively $p(y,x) = p(x \mid y) p(y)$)

Sequential Factorization

A **joint distribution** p(y, x) can be written as the product of conditional distributions:

$$p(y,x) = p(y \mid x) p(x)$$

(or alternatively $p(y, x) = p(x \mid y) p(y)$)

This can be extended for more variables:

$$p(y, x_1, ..., x_p) = p(y \mid x_1, ..., x_p) p(x_1 \mid x_2, ..., x_p) p(x_2 \mid x_3, ..., x_p) ... p(x_p)$$

Joint Distribution

$$p(y, X, \theta) = \underbrace{p(y \mid X, \theta)}_{\text{analysis}} \underbrace{p(X \mid \theta)}_{\text{piors}} \underbrace{p(\theta)}_{\text{part}}$$

 θ contains regr. coefficients, variance parameters, ...

Joint Distribution

$$p(y, X, \theta) = \underbrace{p(y \mid X, \theta)}_{\text{analysis}} \underbrace{p(X \mid \theta)}_{\text{position}} \underbrace{p(\theta)}_{\text{priors}}$$

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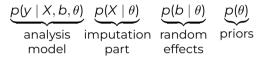
Imputation part

$$p(\overbrace{x_1, \dots, x_p, X_{compl.}} \mid \theta) = p(x_1 \mid X_{compl.}, \theta)$$

$$p(x_2 \mid X_{compl.}, x_1, \theta)$$

$$p(x_3 \mid X_{compl.}, x_1, x_2, \theta)$$

Extension for a Multi-level Setting



Extension for a Multi-level Setting

Extension for a Time-to-Event Outcome

$$\underbrace{p(T,D\mid X,\theta)}_{\text{analysis}} \underbrace{p(X\mid \theta)}_{\text{imputation priors}} \underbrace{p(\theta)}_{\text{part}}$$

Extension for a Multi-level Setting

$$\underbrace{p(y \mid X, b, \theta)}_{\text{analysis}} \underbrace{p(X \mid \theta)}_{\text{position}} \underbrace{p(b \mid \theta)}_{\text{random}} \underbrace{p(\theta)}_{\text{priors}}$$

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Extension for a Time-to-Event Outcome

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Extension for a Multivariate Outcome

$$\underbrace{p(y_1,y_2\mid X,\theta)}_{\text{analysis}} \underbrace{p(X\mid \theta)}_{\text{imputation priors}} \underbrace{p(\theta)}_{\text{port}}$$

MICE vs Sequential Factorization

Imputation in MICE

```
p(x_1 | y, X_{compl.}, x_2, x_3, x_4, ..., \theta)

p(x_2 | y, X_{compl.}, x_1, x_3, x_4, ..., \theta)

p(x_3 | y, X_{compl.}, x_1, x_2, x_4, ..., \theta)

...
```

Sequential Factorization

$$p(y \mid X_{compl.}, x_1, x_2, x_3, \dots, \theta)$$

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...
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Sequential Factorization

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p(\mathbf{y} \mid \mathbf{X}_{compl.}, \mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3, \dots, \theta)
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p(x_3 \mid X_{compl.}, x_1, x_2, \theta)
...
```

No issues with

- complex outcomes, e.g.:
 - multi-level
 - survival
- non-linear effects
- congeniality
- compatibility

MICE vs Sequential Factorization

Imputation in MICE

$$p(x_1 | y, X_{compl.}, x_2, x_3, x_4, ..., \theta)$$

 $p(x_2 | y, X_{compl.}, x_1, x_3, x_4, ..., \theta)$
 $p(x_3 | y, X_{compl.}, x_1, x_2, x_4, ..., \theta)$
...

Sequential Factorization

$$p(y \mid X_{compl.}, x_1, x_2, x_3, \dots, \theta)$$

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$$p(x_3 \mid X_{compl.}, x_1, x_2, \theta)$$
...

Analysis model part of specification

- parameters of interest directly available
- no need for pooling
- simultaneous analysis and imputation

Joint Analysis and Imputation in 🕟

Sequential Factorization is implemented in the R package JointAl



Joint Analysis and Imputation in 🕟

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Bayesian analysis of incomplete data using

- (generalized) linear regression
- (generalized) linear mixed models
- ordinal (mixed) models

- parametric (Weibull) time-to-event models
- Cox proportional hazards models



Joint Analysis and Imputation in 🕟

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Bayesian analysis of incomplete data using

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- ▶ on CRAN: https://CRAN.R-project.org/package=JointAl
- ▶ webpage: https://nerler.github.io/JointAl/
- ► GitHub: https://github.com/NErler/JointAl



Joint Analysis and Imputation in ®

	standard regression		mixed model	
type	outcome	covariate	outcome	covariate
normal	✓	√	√	√
lognormal	(soon)	\checkmark	(soon)	\checkmark
Gamma	✓	\checkmark	\checkmark	\checkmark
beta	(soon)	\checkmark	(soon)	(soon)
binomial	✓	✓	\checkmark	\checkmark
poisson	\checkmark	(soon)	\checkmark	\checkmark
ordinal	\checkmark	\checkmark	\checkmark	\checkmark
multinomial	(soon)	\checkmark	(soon)	(soon)

Available soon:

- ▶ Joint models (of longitudinal & time-to-event data)
- ► Multivariate models

Requirements:

- ► (https://cran.r-project.org/)
- ► JAGS (Just Another Gibbs Sampler; https://sourceforge.net/projects/mcmc-jags/files/JAGS/4.x/)

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Installation:

```
install.packages("JointAI")
```

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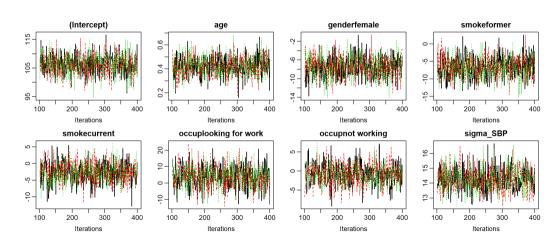
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Usage:

traceplot(res)



summary(res)

```
##
   Linear model fitted with JointAI
##
## Call:
## lm imp(formula = SBP ~ age + gender + smoke + occup, data = NHANES,
##
      n.iter = 300)
##
## Posterior summary:
##
                         Mean
                                 SD 2.5% 97.5% tail-prob. GR-crit
                      106.222 3.3979
                                     99.461 112.961
                                                      0.0000
## (Intercept)
                                                                1.00
## age
                       0.427 0.0798
                                      0.278 0.583 0.0000 1.00
## genderfemale
                       -7.450 2.2718 -11.755 -3.072 0.0000 1.00
## smokeformer
                      -6.692 3.0297 -12.342 -0.885 0.0267 1.03
## smokecurrent
                      -2.658 3.0229 -8.450 3.313 0.3711 1.01
                                     -9.487 16.087 0.5044 1.01
## occuplooking for work 3.817 6.4037
## occupnot working
                       -0.869 2.6858 -6.110 4.256
                                                    0.7511 1.02
##
## Posterior summary of residual std. deviation:
##
            Mean
                   SD 2.5% 97.5% GR-crit
## sigma_SBP 14.3 0.753 12.8 15.8 0.999
##
##
## MCMC settings
## [...]
```

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- The incomplete variable has a certain conditional distribution
- all associations are linear
- compatibility and congeniality

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 extension to MNAR using pattern mixture model

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- ⇒ semi-parametric methods

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- JointAl aims to facilitate correct handling of missing values by
 - assuring compatibility & congeniality
 - simultaneous analysis & imputation
 - especially for complex settings
- ▶ There is no magical solution that will always work in all settings.

Thank you for your attention.

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zafung