## Hypothesis Testing pt. 3 More Types of Hypothesis Tests

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## Hypothesis Test - Single Proportion

$$H_0: p = p_0$$

Under the null hypothesis we have:

$$Z:=rac{\hat{
ho}-
ho_0}{\sqrt{rac{
ho_0(1-
ho_0)}{n}}}\sim extsf{N(0,1)}$$

use qnorm() with value of Z

#### **Conditions:**

- Random Sample
- $ightharpoonup n imes p_0 \ge 10$
- ►  $n \times (1 p_0) \ge 10$

### Hypothesis Test – Difference of Proportions

$$H_0$$
:  $p_1 - p_2 = 0$ 

If  $p_1 = p_2$ , then both are estimating the same thing.

Let 
$$\hat{p}_{pool} = \frac{x_1 + x_2}{n_1 + n_2} = \frac{n_1 \hat{p}_1 + n_2 \hat{p}_2}{n_1 + n_2}$$

If we are simulating what the null hypothesis looks like, then

$$Z := \frac{(\hat{\rho}_1 - \hat{\rho}_2) - 0}{\sqrt{\frac{\hat{\rho}_{pool}(1 - \hat{\rho}_{pool})}{n_1} + \frac{\hat{\rho}_{pool}(1 - \hat{\rho}_{pool})}{n_2}}} = \frac{(\hat{\rho}_1 - \hat{\rho}_2)}{\sqrt{\hat{\rho}_{pool}(1 - \hat{\rho}_{pool})(\frac{1}{n_1} + \frac{1}{n_2})}} \sim \mathbf{N(0,1)}$$

use qnorm() with value of Z

#### **Conditions:**

- Random Samples
- $ightharpoonup n_1 imes \widehat{p}_1 \geq 10$  and  $n_1 imes (1 \widehat{p}_1) \geq 10$
- $ightharpoonup n_1 imes \widehat{p}_2 \geq 10$  and  $n_1 imes (1 \widehat{p}_2) \geq 10$

#### Hypothesis Test – Single Mean

 $H_0$ :  $\mu = \mu_0$ 

The CLT says that  $\bar{x} \sim N(\mu, \frac{\sigma}{\sqrt{n}})$ 

If we are simulating what the null hypothesis looks like  $o ar x \sim \mathsf{N}(\mu_0,\,rac{\sigma}{\sqrt{n}})$ 

Think back to standardizing. If we standardize a Normal distribution it becomes a Standard Normal distribution N(0,1). So...

$$Z:=rac{ar{x}-\mu_0}{\sigma/\sqrt{n}}\sim extsf{N(0,1)}$$

If we define Z in this way, then we know it follows a Standard Normal distribution and we have a way to calculate p-values.

use qnorm() function with value of Z

## Hypothesis Test – Single Mean

H<sub>0</sub>: 
$$\mu = \mu_0$$

Issue: We probably don't know  $\sigma$ 

$$T:=rac{ar{x}-\mu_0}{s/\sqrt{n}}\sim \mathbf{t(df=n-1)}$$

use qt() function with value of T and df

# Hypothesis Test – Single Mean

 $H_0$ :  $\mu = \mu_0$ 

#### **Conditions:**

- ► Random Sample
- ▶ Normal population **OR**  $n \ge 30$

If  $\sigma$  is known:

$$Z:=rac{ar{x}-\mu_0}{\sigma/\sqrt{n}}\sim extsf{N(0,1)}$$

▶ use qnorm() function with value of Z

If  $\sigma$  is not known:

$$T:=rac{ar{x}-\mu_0}{s/\sqrt{n}}\sim \mathsf{t}(\mathsf{df}=\mathsf{n-1})$$

use qt() function with value of T and df

## Hypothesis Test – Difference of Means

$$H_0$$
:  $\mu_1 - \mu_2 = \mu_0 = 0$ 

#### **Conditions:**

- ► Random Sample
- Normal population **OR**  $n_1 \ge 30$  and  $n_2 \ge 30$

If  $\sigma$  is known:

$$Z:=rac{ar{x}_1-ar{x}_2}{\sqrt{rac{\sigma^2}{n_1}+rac{\sigma^2}{n_2}}}\sim extsf{N(0,1)}$$

use qnorm() function with value of Z

If  $\sigma$  is not known:

$$T := \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}} \sim \mathbf{t}(\mathsf{df} = \mathsf{min}(n_1, n_2) - 1)$$

use qt() function with value of T and df