



a) Rezolvați circuitul aplicând Kierhoff.

b) BiCoulul puterilor.

a) $N=4, L=6$

~~#1~~ : $N-1 = 3$ noduri (arbori)

~~#2~~ : $L-N+1 = 6-4+1 = 3$ laturi (coarbori)

(S₁): $-I_5 + I_{g6} + I_3 = 0 \Rightarrow I_3 - I_5 = 6 \Rightarrow \boxed{I_3 = 6 + I_5}$

(S₂): $I_5 - I_2 - I_4 = 0 \Rightarrow I_1 - I_2 = 0 \Rightarrow \boxed{I_1 = I_2}$

(S₃): $-I_4 - I_1 + I_5 = 0$

(B₁): $U_{g6} + I_3 R_3 - E_1 = 0 \Rightarrow U_{g6} = 8I_3 - 3I_3 = 5I_3 \Rightarrow \boxed{U_{g6} = 5I_3}$

(B₂): $-I_4 R_4 + E_1 + I_2 R_2 + E_2 = 0$

(B₃): $I_5 R_5 - U_{g6} + E_1 + R_2 I_2 + E_2 = 0 \quad (-)$

$-I_4 R_4 + I_5 R_5 + U_{g6} = 0 \Rightarrow -2I_4 - 3I_5 + 5I_3 = 0$

$-2I_4 - 3I_5 + 30 + 5I_5 = 0$

$-2I_4 = -30 - 2I_5 \Rightarrow$

$$\Rightarrow \boxed{I_4 = +15 + I_5}$$

$$I_1 = I_5 - I_4 = I_5 - 15 - I_5 = -15 \Rightarrow \boxed{I_1 = -15 A}$$

$$I_1 = I_2 \Rightarrow \boxed{I_2 = -15 A}$$

$$\left. \begin{aligned} -I_4 R_4 + E_1 + I_2 R_2 + E_2 &= 0 \\ E_2 &= 3U_4 = 3I_4 R_4 \end{aligned} \right\} \Rightarrow 2I_4 R_4 + 3I_3 + 5I_2 = 0$$

$$\Rightarrow 4I_4 + 3I_3 = 75 \Rightarrow 4(15 + I_5) + 3(-6 + I_5) = 75 \Rightarrow$$

$$\Rightarrow 60 + 4I_5 - 18 + 3I_5 = 75 \Rightarrow 42 + 7I_5 = 75 \Rightarrow$$

$$\Rightarrow \cancel{4I_5 = -3} \Rightarrow \underline{I_5 = -\frac{3}{7} A} \quad \boxed{I_5 = 33 A}$$

$$I_4 = 15 + I_5 = \cancel{15 - \frac{3}{7}} = \frac{102}{7} A \Rightarrow$$

$$\Rightarrow \underline{I_4 = \frac{102}{7} A} \quad \boxed{I_4 = 48 A}$$

$$I_3 = 6 + I_5 = 6 - \frac{3}{7} = \frac{39}{7} A \Rightarrow \underline{I_3 = \frac{39}{7} A}$$

$$U_{ge} = 8I_3 = 8 \cdot \frac{39}{7} = \frac{194}{7} V \quad E_2 = 3I_4 R_4 = 6 \cdot \frac{102}{7} A =$$

$$E_1 = 3I_3 = 3 \cdot \frac{39}{7} = \frac{117}{7} V = \frac{612}{7} A$$

$$b) P_g = E_2 I_2 + U_{g6} I_{g6} + E_1 I_1$$

$$P_c = R_2 I_2^2 + R_3 I_3^2 + R_4 I_4^2 + R_5 I_5^2$$

$$\begin{aligned} P_g &= \frac{612}{7} \cdot (-15) + \frac{194}{7} \cdot 6 + \frac{114}{7} \cdot (-15) = \\ &= (-15) \left(\frac{612}{7} + \frac{114}{7} \right) + \frac{1164}{7} = \frac{729}{7} \cdot (-15) + \frac{1164}{7} = \\ &= \frac{-10935}{7} + \frac{1164}{7} = \end{aligned}$$

$$a) I_3 = -6 + I_5 = -6 + 30 = 24 \text{ A} \Rightarrow \boxed{I_3 = 24 \text{ A}}$$

$$U_{g6} = 5 I_3 = 5 \cdot 24 = 120 \text{ V} \Rightarrow \boxed{U_{g6} = 120 \text{ V}}$$

$$E_1 = 3 I_3 = 3 \cdot 24 = 72 \text{ V} \Rightarrow \boxed{E_1 = 72 \text{ V}}$$

$$E_2 = 3 U_4 = 3 I_4 R_4 = 3 \cdot 2 \cdot 48 = 288 \text{ V} \Rightarrow \boxed{E_2 = 288 \text{ V}}$$

$$\begin{array}{r} 729 \cdot \\ 15 \\ \hline 3645 \\ 729 \\ \hline 10935 \end{array}$$