

DEPARTMENT OF MATHEMATICS, I.I.T. GUWAHATI

MA 473: Computational Finance Labs – V and VI February 19, 2019

1. Consider the following American put option problem:

$$\left\{ \begin{array}{l} \frac{\partial V}{\partial t} + \frac{1}{2}\sigma^2 S^2 \frac{\partial^2 V}{\partial S^2} + (r - \delta)S \frac{\partial V}{\partial S} - rV = 0, \quad (0, \infty) \times (0, T], \quad T > 0 \\ \text{with suitable initial and boundary and free boundary conditions.} \end{array} \right.$$

- (a) Solve the transformed PDE $y_\tau = y_{xx}$ of the above IBVP by using the Backward-Time and Central Space (BTCS) Scheme and the Crank-Nicolson finite difference scheme.
- (b) Plot $V(S, t)$ for $T = 1$, $K = 10$, $r = 0.25$, $\sigma = 0.6$, $\delta = 0.2$, and the payoff.
- (c) Solve the problem by using δx and $\delta \tau$, and $\delta x/2$ and $\delta \tau/2$ and calculate the error between these two numerical solution. Plot the error.
- (d) Also calculate the error mentioned above for different values of $\delta x/2$ and $\delta t/2$ and plot N *versus* the maximum absolute error.

2. Consider the following American call option problem:

$$\left\{ \begin{array}{l} \frac{\partial V}{\partial t} + \frac{1}{2}\sigma^2 S^2 \frac{\partial^2 V}{\partial S^2} + (r - \delta)S \frac{\partial V}{\partial S} - rV = 0, \quad (0, \infty) \times (0, T], \quad T > 0 \\ \text{with suitable initial and boundary and free boundary conditions.} \end{array} \right.$$

- (a) Solve the transformed PDE $y_\tau = y_{xx}$ of the above IBVP by using the Backward-Time and Central Space (BTCS) Scheme and the Crank-Nicolson finite difference scheme.
 - (b) Plot $V(S, t)$ for $T = 1$, $K = 10$, $r = 0.06$, $\sigma = 0.3$, $\delta = 0.25$, and the payoff.
 - (c) Solve the problem by using δx and $\delta \tau$, and $\delta x/2$ and $\delta \tau/2$ and calculate the error between these two numerical solution. Plot the error.
 - (d) Also calculate the error mentioned above for different values of $\delta x/2$ and $\delta t/2$ and plot N *versus* the maximum absolute error.
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