



# ISE 5405 – OPTIMIZATION I

## *Semester Project – Part 1*

“On my honor, as a Hokie, I have neither given nor received  
unauthorized aid on this academic work”

### **Team Members**

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## PROBLEM 1

### Indices

$i$  – types of cables

### Index sets

$I$	Cable types	$I = \{1, 2, 3 \dots N_T\}$
$I_D$	Cable types that can be made on duplex machines	$I_D = I = \{1, \dots N_{D0} + N_{DR}\}$
$I_{D0}$	Cable types that can be made only on duplex machines	$I_{D0} = \{1, \dots N_{D0}\}$
$I_{DR}$	Cable types that can be made either on Duplex or Regular machines	$I_{DR} = I_R$
$I_R$	Cable types that can be made on regular machines	$I_R = I_{DR} = \{N_{D0} + 1, \dots, N_{D0} + N_{DR}\}$

### Parameters

$c_i$	cost to produce a yard of cable $i$ , $i \in I$
$s_i$	cost to outsource a yard of cable $i$ , $i \in I$
$p_i$	selling price of a yard of cable $i$ , $i \in I$
$Dm_i$	demand in yards for cable $i$ , $i \in I$
$D$	Total available Duplex machine hours = 32760
$R$	Total available Regular machine hours = 196560
$t_{di}$	hours/yard required for cable type $i$ on a Duplex machine, $i \in I$ (inverse of production rate)
$t_{ri}$	hours/yard required for cable type $i$ on a Regular machine, $i \in I$ (inverse of production rate)
$N_D$	Number of Duplex machines = 15
$N_{D0}$	Number of cable types that can be only made on Duplex machines = 4
$N_{DR}$	Number of cable types that can be only made on Regular machines = 11
$N_R$	Number of Regular machines = 90
$N_T$	Number of cable types = 15

### **Total available time**

Number of hours/day the machines operate = 24

Number of days/week the machines operate = 7

Number of weeks/quarter the machines operate = 13

### **Computed Parameters**

$Pr_i$	Profit for cable type i if produced in-house	$p_i - c_i$
$T_i$	Profit for cable type i if outsourced	$p_i - s_i$
D	$N_D \times (24)(7)(13)$	= 32760
R	$N_R \times (24)(7)(13)$	= 196560

### **Decision Variables**

$d_i$  yards of cable i to produce on a Duplex machine,  $i \in I$

$r_i$  yards of cable i to produce on a Regular machine,  $i \in I$

$o_i$  yards of cable i to outsource

### **Objective function**

Maximizing Profit

$$Max z = \sum_{i \in I_D} Pr_i d_i + \sum_{i \in I_R} Pr_i r_i + \sum_{i \in I} T_i o_i$$

### **Constraints**

#### **Time Constraints**

Production time of Duplex machine should be less than or equal to the available Duplex machine hours

$$\sum_{i \in I_D} (t_{di} d_i) \leq D$$

Production time of Regular machine should be less than or equal to the available Regular machine hours

$$\sum_{i \in I_R} (t_{ri} r_i) \leq R$$

### **Demand Constraints**

$$d_i + r_i \geq Dm_i ; \quad i \in I_R$$

Total demand should be met.

$$d_i + r_i + o_i \geq Dm_i ; \quad i \in I_{DO}$$

### **Non-negativity constraints**

$$d_i, r_i, o_i \geq 0 ; \quad i \in I$$

## **PROBLEM 2 - Sudoku Puzzle (9x9 matrix)**

### **Objective Function**

Max 0

### **Constraints**

For Columns

$$\sum_{i=1}^9 X_{ijk} = 1 \text{ for } j, k = 1 \text{ to } 9$$

For rows

$$\sum_{j=1}^9 X_{ijk} = 1 \text{ for } i, k = 1 \text{ to } 9$$

For 3x3 squares

$$\sum_{j=3p-2}^{3p} \sum_{i=3q-2}^{3q} X_{ijk} \text{ for } i, k = 1 \text{ to } 9 \text{ and } p, q = 1 \text{ to } 3 \text{ (only one } k \text{ in each submatrix)}$$

For  $\sum_{k=1}^9 X_{ijk} = 1 \text{ for } i, j = 1 \text{ to } 9$

$X_{ijk} = 1$  for all  $(i, j, k) \in G$  (all the known cells)

## **Sudoku Puzzle (4x4 matrix)**

### **Objective Function**

Max 0

### **Constraints**

For Columns

$$\sum_{i=1}^4 X_{ijk} = 1 \text{ for } j, k = 1 \text{ to } 4$$

For rows

$$\sum_{j=1}^4 X_{ijk} = 1 \text{ for } i, k = 1 \text{ to } 4$$

For 2x2 squares

$$\sum_{j=2p-1}^{2p} \sum_{i=2q-1}^{2q} X_{ijk} \text{ for } i, k = 1 \text{ to } 4 \text{ and } p, q = 1 \text{ to } 2 \text{ (only one } k \text{ in each submatrix)}$$

$$\text{For } \sum_{k=1}^4 X_{ijk} = 1 \text{ for } i, j = 1 \text{ to } 4$$

$$X_{ijk} = 1 \text{ for all } (i, j, k) \in G \text{ (all the known cells)}$$