

Day 6

1. $3! = 6$

2. Choose 1 out of 5
 ${}^5C_1 = 5$

3. $3! = 6$

4. ${}^4C_2 = \frac{4!}{(4-2)!2!} = 6$

5. $P(4) = \frac{1}{2}$

6. $P(4) = \frac{1}{6}$

7. $\boxed{3} \boxed{2} = 3 \times 2 = 6$

8. $T = 7$

$$A = 3$$

$$P(A) = \frac{3}{7}$$

9. $4 \times 3 \times 2 \times 1 = 24$

10. $T = 5$

$$G = 2 \quad P(G) = \frac{2}{5}$$

11. ${}^4P_3 = 4 \times 3 \times 2 = 24$

12. ${}^7C_3 = \frac{7!}{(7-3)!3!} = 35$ ways

13.

$$T = 52$$

$$k = 4$$

$$P(k) = \frac{4}{52} = \frac{1}{13}$$

14.

$$5! = 120$$

15

$$T = 10$$

$$B = 4$$

$$P(B) = \frac{4}{10} = \frac{2}{5}$$

16

$$T = 4$$

$$4P_3 = 4 \times 3 \times 2 = 24$$

17.

Even on die = 2, 4, 6

$$P = \frac{3}{6} = \frac{1}{2}$$

18.

$${}^4C_2 = \frac{4!}{2!2!} = 2 \times 3 = 6$$

19.

$$T = 52$$

$$\text{head} = 13$$

$$P(\text{head}) = \frac{13}{52} = \frac{1}{4}$$

20

$$(n-1)! = (4-1)! \\ = 3! = 6!!$$

21

$$\frac{4!}{3! \cdot 1!} = \frac{24}{6 \cdot 1} = 4$$

$$2 \times 3 \times 4 \times 5 = 48$$

22

$$\text{total} = 12$$

$${}^{12}C_2 = \frac{12!}{10!2!} = \frac{12 \times 11 \times 10!}{2 \times 1 \times 10!} = 66$$

$${}^8C_2 = \frac{8!}{3!5!} = \frac{8 \times 7}{2 \times 1} = 10$$

$$P(6) = \frac{10}{66} = \frac{5}{33}$$

23. $5! = 120$

$$4! = 24$$

$$4! \times 2 = 24 \times 2 = 48$$

$$120 - 48 = 72 \text{ ways}$$

24. Case 1: 2W, 2M

$${}^8C_2 \times {}^{10}C_2 = \frac{8 \times 7 \times 6!}{6! \times 1} \times \frac{10 \times 9 \times 8!}{8! \times 2 \times 1}$$

$$= 98 \times 45$$

$$= 4410$$

Case 2 = 3W, 1M

$${}^8C_3 \times {}^{10}C_1 = \frac{8 \times 7 \times 6 \times 5!}{5! \times 3 \times 2} \times 10$$

$$= 56 \times 10 = 560$$

Case 3 = 4W

$${}^8C_4 = \frac{8 \times 7 \times 6 \times 5 \times 4!}{4! \times 4 \times 3 \times 2}$$

$$= 70$$

$$4410 + 560 + 70 = 5040$$

25. Sum of 7 = (1,6) (2,5) (3,4) (4,3) (5,2) (6,1)

Sum of 1 = 6

total = 36

$$P(7) = \frac{6}{36} = \frac{1}{6}$$