

✓ 1. Types of Data: Qualitative and Quantitative

- **Qualitative (Categorical):** Non-numeric data representing categories or labels.
 - **Examples:** Colors of cars (red, blue, green), types of cuisine (Italian, Chinese).
 - **Quantitative (Numerical):** Numeric data representing measurable quantities.
 - **Examples:** Height (in cm), test scores (out of 100).
 - **Scales of Measurement:**
 - **Nominal:** Categories without a meaningful order (e.g., types of fruits: apple, banana).
 - **Ordinal:** Categories with a meaningful order, but no consistent difference between ranks (e.g., satisfaction levels: poor, good, excellent).
 - **Interval:** Numeric scales with equal intervals but no true zero (e.g., temperature in Celsius).
 - **Ratio:** Numeric scales with a true zero, allowing ratios to be meaningful (e.g., weight in kg).
-

2. Measures of Central Tendency

- **Mean:** Average value. Use when data is symmetric and without extreme outliers.
 - **Example:** Average test score.
 - **Median:** Middle value when data is sorted. Use when data has outliers.
 - **Example:** Median income in a region.
 - **Mode:** Most frequently occurring value. Use for categorical data or to identify peaks in numerical data.
 - **Example:** Most common shoe size.
-

3. Concept of Dispersion

- **Dispersion:** Indicates the spread of data points.
 - **Variance:** Average of squared deviations from the mean.
 - **Standard Deviation:** Square root of variance; shows spread in the same units as the data.
 - **Example:** In a dataset of exam scores, a high standard deviation indicates widely varying scores.
-

4. Box Plot

- **Definition:** A graphical summary using five-number summary (minimum, Q1, median, Q3, maximum).

- **Insights:** Identifies the spread, central tendency, and outliers.
-

5. Random Sampling

- Ensures every individual in the population has an equal chance of selection.
 - **Role:** Reduces bias and enables generalization to the population.
-

6. Skewness

- **Concept:** Measures data asymmetry.
 - **Positive Skew:** Tail on the right (e.g., income data with a few very high incomes).
 - **Negative Skew:** Tail on the left (e.g., exam scores where most scored high).
 - **Impact:** Skewness affects the choice of central tendency (e.g., median over mean in skewed data).
-

7. Interquartile Range (IQR)

- **Definition:** Difference between Q3 (75th percentile) and Q1 (25th percentile).
 - **Use:** Identifies outliers using the rule: values below $(Q1 - 1.5 \times IQR)$ or above $(Q3 + 1.5 \times IQR)$.
-

8. Binomial Distribution

- **Conditions:**
 - Fixed number of trials.
 - Each trial has two outcomes (success/failure).
 - Constant probability of success.
 - **Example:** Flipping a coin 10 times to count heads.
-

9. Normal Distribution and Empirical Rule

- **Properties:** Symmetrical, bell-shaped curve with mean = median = mode.
 - **Empirical Rule:**
 - 68% of data within 1 standard deviation.
 - 95% within 2 standard deviations.
 - 99.7% within 3 standard deviations.
-

10. Poisson Process

- **Example:** Number of customer arrivals at a store per hour.
 - **Calculation:** If the average is 5 arrivals/hour, the probability of 7 arrivals: $[P(X = 7) = \frac{\lambda^7 e^{-\lambda}}{7!}, \lambda = 5]$
-

11. Random Variables

- **Definition:** Variables whose outcomes are determined by chance.
 - **Discrete:** Countable outcomes (e.g., number of heads in 10 coin flips).
 - **Continuous:** Infinite outcomes (e.g., time taken to run a race).
-

12. Covariance and Correlation

- **Example Dataset:** $[X = [2, 4, 6], Y = [3, 6, 9]]$
- **Covariance:**
$$\text{Cov}(X, Y) = \frac{\sum{(X_i - \bar{X})(Y_i - \bar{Y})}}{n-1}$$
- **Correlation:** Standardized measure ((-1) to (1)) indicating strength and direction of relationship.
$$\text{Correlation} = \frac{\text{Cov}(X, Y)}{\sigma_X \cdot \sigma_Y}$$
- **Interpretation:** A positive value indicates a direct relationship, and a negative value indicates an inverse relationship.

Double-click (or enter) to edit