# Documentation of model building in Mobius

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# August 6, 2019

# Contents

1	Intr	roducti	ion	2
2	Bas	ic cond	cepts	2
	2.1	The m	odel	2
	2.2	The da	ataset	3
3	Mo	del str	ucture	4
	3.1	Index	sets and indexes	4
	3.2	Param	neter structure	4
	3.3	Input	structure	5
	3.4	Equat	ion batch structure	5
4	Mo	del bui	ilding	7
	4.1	Setting	g up a project and creating a model object	7
		4.1.1	A note on visualisation of model results	9
	4.2	Entity	registration, handles, and equation bodies	9
	4.3	Impler	menting an example mathematical model in Mobius	10
		4.3.1	Warning about value accesses inside conditionals	13
		4.3.2	What to do inside of or outside of equation bodies	14
	4.4	Advan	ded equation types	14
		4.4.1	Cumulation equations	14
		4.4.2	ODE equations and solvers	15
		4.4.3	Initial value equations	17
		4.4.4	Computed parameters (experimental feature)	18
	4.5	Advan	ced value accesses	19
		4.5.1	Special state values	19
		4.5.2	Explicit indexing and explicit iteration	19
		4.5.3	Predeclared indexes	21
		151	Branch iteration	22

	4.6	Debugging features	22
	4.7	Tips on model performance (speed)	23
	4.8	Determining the batch structure of advanced models	24
_		W	
5	App	olication building API	<b>2</b> 6
	5.1	Data types	27
	5.2	Procedures	27
6	Mo	del building API	<b>2</b> 9
	6.1	Registration procedures	29
	6.2	Equation body declaration	36

# 1 Introduction

This is documentation for model developers. Documentation for model users and framework developers will be provided in separate documents (eventually).

**Note 1.** It is recommended for any model developers to take a look at the tutorials and experiment with making changes to them before reading all of the documentation. The tutorials will also provide the information about how to compile the models into finished exes. After you have some experience, it is also a good idea to look at existing models (in the Modules folder of the github repository) for more advanced examples.

# 2 Basic concepts

#### 2.1 The model

The model object contains all immutable information about the model that will not change with each particular usage of the model. The model object contains lists of various model entities and information about these that are provided by the model developer in the model registration routine(s). The different model entities are presented in Table 1.

Index sets	Parameters, inputs and equation results can index over one
	or more index sets. For instance, you may want to evalute
	the same equations in multiple contexts, such as once per
	reach in a river, and in that case you want an index set for
	these reaches.
Parameter groups	Parameter groups are collections of parameters. A parame-
	ter group can vary with an index set, making each parameter
	have a separate value for each index in the index set. The
	parameter group can also be a child group of another pa-
	rameter group. In that case, each parameter in the group
	has a separate value for each pair of indexes from the index
	set of its group and the parent group. This can be chained
	to make parameters vary with as many index sets as one
	wants.
Parameters	Parameters are values used to tune the equations of the mod-
	ell. Parameters do not vary over time. Currently four dif-
	ferent types of parameters are supported: double precision
	floating point, unsigned integer, boolean and time.
Inputs	Inputs are forcings on the model that vary over time. An
	example of an input is a time series of daily air temperature
	that has been measured in the field. Inputs can also vary
	with index sets. For instance, one can have a separate air
	temperature series for each subcatchment area in the model.
Equations	The model has a set of equations that are executed in a
	specific order for every timestep of the model (see later de-
	scriptions of how the run order is determined). Each equa-
	tion can look up the value of various parameters, inputs,
	results of other equations (both from the current timestep
	and earlier) and produces a single output value every time it
	is evaluated. There are several types of equations. The main
	two are discrete timestep (or basic) equations and ordinary
	differential equations (ODE).
Solvers	Each solver contains a list ODE equations that it will solve
	over one timestep whenever it is run. The solver must be
	registered with additional information about e.g. which in-
	tegrator method it will use.

Table 1: The model entities

# 2.2 The dataset

The dataset contains information about a specific setup of a model. This includes all the indexes of each index set, as well as values for all the parameters and input series in the model. It will also contain the result series of each equation after the model is run. The typical way of setting up a dataset is by reading it in from a parameter file and an input file. The file formats for these are documented separately.

# 3 Model structure

#### 3.1 Index sets and indexes

Index sets is one of the fundamental concepts in the Mobius framework. Examples of index sets can for instance be "Reaches", or "Landscape units". Parameters, equation results and inputs can index over index sets, so that the same equation is evaluated for many indexes, and with different parameter values for each (combination of) indexes.

**Example 1.** The equation "Snow fall" depends on the input timeseries "Actual precipitation" and "Air temperature", and on the parameter "Canopy interception". Say that "Canopy interception" indexes over the index set "Landscape units". In this case, "Snow fall" will be evaluated once per index in the "Landscape units" index set, using the corresponding parameter value of "Canopy interception" for each index. If one of the inputs also index over "Reaches", then "Snow fall" will be evaluated once per reach-landscape unit pair. This generalizes to higher number of index sets.

Which index sets each model has is fixed, and determined by the model developer. However, which indexes each index set contains can usually be determined by the model user, for instance by configuring a parameter file. Some models do however require a fixed set of particular indexes for some of its index sets. For instance INCA-N only works with three particular soil boxes.

There are two types of index sets

- i Basic index sets. These have no additional structure except for the order of the indexes.
- ii Branched index sets. These contain additional connectivity information, and are typically used to encode river structures. Each index in a branched index set has a list of incoming branches, the branches being other indexes in the same index set.

#### 3.2 Parameter structure

Each parameter belongs to a parameter group, which again can belong to another parameter group and so on. Moreover, each parameter group can index over an index set. This means that each parameter can in practice be viewed as a multidimensional array of parameter values, where each dimension in the array is indexed by one of the model's index sets. It is possible for a parameter to index over the same index set multiple times. For instance, the PERSiST hydrology model [1] has a "Percolation matrix" parameter where both the row and column in the matrix is indexed by the soil box.

**Example 2.** A PERSiST "Percolation matrix", from a parameter file. (See separate documentation for a detailed description of the parameter file format).

```
"Percolation matrix":
0.2 0.8 0.0
1.0 0.5 0.5
0.0 0.0 1.0

0.1 0.9 0.0
1.0 0.6 0.4
0.0 0.0 1.0
```

The parameter indexes over "Landscape units" once (signifying what matrix you are looking at) and "Soils" twice (signifying which row and column). The percolation matrix is used to say something about what proportion of the water will flow between each soil box, but we will not go into detail about that here.

The parameter group and index set structure of the parameters are entirely fixed by the model (developer), and can not be configured in the parameter file. But one can usually configure which indexes each index set has and which values the parameter has for each (tuple of) index(es).

#### 3.3 Input structure

An input is a timeseries (usually of measured data or preprocessed data that is based on measured data). Inputs are used as forcings in many models. For instance, hydrological models often use precipitation timeseries to determine how much water enters the system at each day. Inputs can either be global for the system, or like parameters can index over one or more index sets. For instance, one may want to have a separate precipitation timeseries for each subcatchment (reach). Unlike with parameters, which index set each input indexes over is determined in the input file. This can sometimes change the equation structure of the model. For instance, if precipitation and air temperature does not depend on which subcatchment one are in, the framework may decide for some models that equations like "Precipitation falling as snow" should only be evaluated once globally instead of per subcatchment. This does however also depend on which parameters these equations reference. If "Precipitation falling as snow" references a parameter that indexes over the "Reaches" index set, that equation will still evaluate once per reach.

#### 3.4 Equation batch structure

During the main run of the model, the model will for each timestep evaluate all equations (sometimes called state variables) in a given order. Equations can also be evaluated for multiple indexes. For instance any equations having to do with flow or volume of a reach are typically evaluated for each index in a "Reaches" index set. Equations are sorted so that an equation is always evaluated after other equations that it uses the result values of. To facilitate this, the model builds an equation batch structure.

**Example 3.** The equation batch structure for the framework implementation of PERSiST. \*\*\*\* Result Structure \*\*\*\* [Reaches] [Landscape units] Snow melt Rainfall [Reaches] [Landscape units] [Soils] Percolation input Saturation excess input Input Water depth 1 Saturation excess Water depth 2 Evapotranspiration X3 Evapotranspiration X4 Evapotranspiration Water depth 3 Total runoff Drought runoff Percolation out Water depth 4 Runoff Runoff to reach Water depth [Reaches] [Landscape units] Snow fall Snow as water equivalent (Cumulative) Total runoff to reach Diffuse flow output [Reaches] (Cumulative) Total diffuse flow output Reach flow input

# (ODE) Reach flow (ODE) Reach volume

\_\_\_\_

Reach velocity Reach depth

Reach time constant

---- (SOLVER: Reach solver)

----

The model has an ordered list of batch groups, where each batch group has an ordered list of batches. Each batch group also has an ordered list of index sets that it indexes over. Each batch can either be a discrete batch or a solver batch. The model will evaluate each batch group at a time. Then for each combination of indexes in the index sets it evaluates each batch in the batch group in order. In discrete batches, each equation is evaluated in order. In solver batches, the ODE system will be integrated possibly evaluating each equation many times. In Example

3, the first three batch groups contain one batch each, while the last batch group contains three batches.

**Note 2.** The only time a batch group can have more than one batch is if it contains both a solver batch and one or more discrete batches (or possibly another solver batch using a different integrator). Two discrete batches next to each other that index over the same index sets will always be merged.

**Example 4.** Pseudocode for how the model evaluates the batch structure in Example 3.

```
for every timestep:
       for every reach R:
              for every landscape unit LU:
                     evaluate "Snow melt" and "Rainfall" for this LU in this R.
       for every reach R:
              for every landscape unit LU:
                     for every soil box S:
                             evaluate "Percolation input" to "Water depth" for this S
                                  in this LU in this R
       for every reach R:
              for every landscape unit LU:
                     evaluate "Snow fall" to "Diffuse flow output" for this LU in
                         this R
       for every reach R:
              evaluate "Total diffuse flow output" and "Reach flow input"
              run a solver that integrates the ODE system containing the equations "
                  Reach time constant" to "Reach volume" (possibly evaluating them
                  many times)
              evaluate "Reach velocity" and "Reach depth"
```

At the end of a model run, one can extract a timeseries of each of these equations for any combination of indexes that they index over. For instance one can look at the timeseries for "Snow melt" in {"Langtjern", "Forest"}, or the timeseries for "Water depth" in {"Langtjern", "Peatland", "Organic soil layer"} (given that these were indexes provided for this particular dataset).

Unlike parameters, equations can never index over one index set more than once. We will go through how the index set dependencies of an equation are determined and how it is placed in a batch structure later.

# 4 Model building

# 4.1 Setting up a project and creating a model object

We refer to the quick start guide on the front page of the github repository as well as the tutorials on how to quickly get a project started.

Usually you will have one header (.h) file with the procedures you use to build your model, and one source file (.cpp) with the main function of the C++ program, where you do all application-level operations such as creating and destroying model and dataset objects or reading in parameter values from files, running the model and so on.

```
Example 5. Example of a main.cpp
#define MOBIUS_PRINT_TIMING_INFO 1
#include "../mobius.h" //NOTE: This path is relative to the location of this file
#include "mymodel.h"
int main()
{
       const char *InputFile = "mytestinputs.dat";
       const char *ParFile = "mytestparameters.dat";
       mobius_model *Model = BeginModelDefinition();
       AddTestModel(Model);
       ReadInputDependenciesFromFile(Model, InputFile);
       EndModelDefinition(Model);
       PrintResultStrucuture(Model);
       mobius_data_set *DataSet = GenerateDataSet(Model);
       ReadParametersFromFile(DataSet, ParFile);
       ReadInputsFromFile(DataSet, InputFile);
       RunModel(DataSet);
       u64 Timesteps = GetTimesteps(DataSet);
       PrintResultSeries(DataSet, "AX", {}, Timesteps);
}
```

# Example 7. mytestparameters.dat parameters: "Timesteps": 10 "Start date": 2019-02-22 "A": 5.0

```
Example 8. mytestinputs.dat

timesteps:
10

inputs:
"X":
1 2 3 4 5 6 7 8 9 10
```

Example 5 shows a main function that you can usually keep unchanged throughout model development. The only thing you may want to change in it is the debug printout (PrintResultSeries) at the end, to print out different result series. Your main model development will happen inside mymodel.h (which you can name anything you like). You will also have to update your parameter and input files as the model requirements change. The parameter file can be autogenerated, something that is explained in the tutorials.

Note that the "Timesteps" and "Start date" parameters are automatically registered with every new model, so you don't have to register them.

#### 4.1.1 A note on visualisation of model results

During model development it can be pretty unsatisfactory to just look at the numbers printed out by PrintResultSeries in order to determine if the model performs as expected. It can be a good idea to set up an MobiView (or python wrapper) - compatible model application early. We will not provide an in-depth description of how to do that in this document, but it should not be too difficult to follow the example of existing model applications. See also some notes about this on the front page of the Mobius github repository.

#### 4.2 Entity registration, handles, and equation bodies

The mobius\_model object contains lists of various model entities (see Table 1 for an explanaition) and information about these. It is the model developer's job to register all the entities and provide the needed information for each one.

```
Example 9. Example of entity registration.
auto X = RegisterInput(Model, "X");
auto A = RegisterParameterDouble(Model, System, "A", Dimensionless, 1.0);
```

The input "X" is tied to the model and is given the name "X". The parameter (of type double) is tied to the Model, the parameter group System, given the name "A", the unit Dimensionless, and the default value 1.0. A full model building API describing all the registration functions is given in Section 6.1.

Each registration function returns a handle. In Example 9, the handles are X and A (declared with auto to signify that we don't care about their exact type). Handles are "tickets" one can use to talk about an entity one has already registered. If you provide the handle A in the context of extracting a parameter value, the model will know that you are talking about the parameter "A" that you registered earlier.

Every equation in the model also receives an equation body, and inside the equation body one can extract the values of registered parameters, inputs and equations by referring to them by their handle.

**Example 10.** The equation "AX" references the value of the parameter "A" and the input "X" by using the handles returned from the registration of those entities.

**Note 3.** If you are confused by the syntax of declaring an equation body because it does not look like valid C++, don't worry. **EQUATION** is a macro that expands to declaring a C++11 lambda that is then stored in the Model object. The macro is needed to hide some of the underlying functionality, like what object the PARAMETER and INPUT accessors read their values from, so that the model builder does not have to type too much repetitive code all the time.

#### 4.3 Implementing an example mathematical model in Mobius

The SimplyP model [2] uses the following very simple snow module.

Symbol	Type	Units	Name	Default	Min	Max
$D_{snow,0}$	parameter	mm	Initial snow depth	0.0	0.0	10000.0
$f_{DDSM}$	parameter	$mm d^{-1} \circ C^{-1}$	Degree-day factor for snowmelt	2.74	1.6	6
Pptn	input timeseries	$mm d^{-1}$	Precipitation			
$T_{air}$	input timeseries	$^{\circ}C$	Air temperature			
$P_{snow}$	state variable	$mm d^{-1}$	Precipitation falling as snow			
$P_{rain}$	state variable	$mm  d^{-1}$	Precipitation falling as rain			
$P_{melt}$	state variable	$mm d^{-1}$	Snow melt			
$D_{snow}$	state variable	mm	Snow depth (water equivalents)			
P	state variable	$mm d^{-1}$	Hydrological input to soil			

Table 2: SimplyP snow parameters and state variables

The state variables at a given timestep t are given by the following equations

$$P_{snow,t} = \begin{cases} 0 & \text{if } T_{air,t} > 0 \\ Pptn_t & \text{otherwise.} \end{cases}$$

$$P_{rain,t} = \begin{cases} 0 & \text{if } T_{air,t} <= 0 \\ Pptn_t & \text{otherwise.} \end{cases}$$

$$P_{melt,t} = \min(D_{snow,t-1}, \max(0, f_{DDSM}T_{air,t}))$$

$$D_{snow,t} = D_{snow,t-1} + P_{snow,t} - P_{melt,t}$$

$$P_t = P_{rain,t} + P_{melt,t}$$

Say that one also wants a different initial snow depth and degree-day factor for each reach (subcatchment). First one has to register all of the model entities.

**Example 11.** Registration of model entities for the SimplyP snow module. = RegisterUnit(Model, "mm"); auto MmPerDegreePerDay = RegisterUnit(Model, "mm/°C/day"); auto MmPerDay = RegisterUnit(Model, "mm/day"); auto Reach = RegisterIndexSetBranched(Model, "Reaches"); auto Snow = RegisterParameterGroup(Model, "Snow", Reach); auto InitialSnowDepth = RegisterParameterDouble(Model, Snow, "Initial\_snow\_depth" , Mm, 0.0, 0.0, 10000.0); auto DegreeDayFactorSnowmelt = RegisterParameterDouble(Model, Snow, "Degree-dayu factor\_for\_snowmelt", MmPerDegreePerDay, 2.74, 1.6, 6.0); auto Precipitation = RegisterInput(Model, "Precipitation"); auto AirTemperature = RegisterInput(Model, "Air temperature"); auto PrecipitationFallingAsSnow = RegisterEquation(Model, "Precipitation\_falling\_as\_ snow", MmPerDay); auto PrecipitationFallingAsRain = RegisterEquation(Model, "Precipitation\_falling\_as\_ rain", MmPerDay); auto PotentialDailySnowmelt = RegisterEquation(Model, "Potentialudailyusnowmelt", MmPerDay); = RegisterEquation(Model, "Snow⊔melt", MmPerDay); auto SnowMelt = RegisterEquation(Model, "Snow\_depth", Mm); auto SnowDepth auto HydrologicalInputToSoilBox = RegisterEquation(Model, "Hydrological\_input\_to\_soil □box", MmPerDay); SetInitialValue(Model, SnowDepth, InitialSnowDepth);

Note that we also use the SetInitialValue procedure to tell the model that "Snow depth" should have initial value "Initial snow depth". The value of "Initial snow depth" is not determined at this point, but it will be determined before one runs the model (typically by reading a parameter file), and the framework will remember that it should set this value as the initial value of "Snow depth" before the run starts. We have also added the state variable "Potential daily snowmelt" as a partial calculation used in "Snow melt", however that is not strictly necessary. Next one provides the equation bodies.

```
Example 12. Equation bodies for the SimplyP snow module.
EQUATION (Model, PrecipitationFallingAsSnow,
       double precip = INPUT(Precipitation);
       if(INPUT(AirTemperature) <= 0) { return precip; }</pre>
       else { return 0.0; }
EQUATION(Model, PrecipitationFallingAsRain,
       double precip = INPUT(Precipitation);
       if(INPUT(AirTemperature) > 0) { return precip; }
       else { return 0.0; }
)
EQUATION (Model, Potential Daily Snowmelt,
       return Max(0.0, PARAMETER(DegreeDayFactorSnowmelt) * INPUT(AirTemperature));
EQUATION (Model, SnowMelt,
       return Min(LAST_RESULT(SnowDepth), RESULT(PotentialDailySnowmelt));
EQUATION (Model, SnowDepth,
       return LAST_RESULT(SnowDepth) + RESULT(PrecipitationFallingAsSnow) - RESULT(
           SnowMelt);
)
EQUATION(Model, HydrologicalInputToSoilBox,
       return RESULT(SnowMelt) + RESULT(PrecipitationFallingAsRain);
```

In Example 16 we see that RESULT refers to the value of another equation from the current timestep, while LAST\_RESULT refers to the value from the previous timestep. Looking at the model result structure that is printed using the PrintResultStructure procedure, we see the following.

```
Example 13. Batch structure for the SimplyP snow module.

[]

----
Precipitation falling as snow
Precipitation falling as rain
----
[Reaches]

----
Potential daily snowmelt
Snow melt
Snow depth
Hydrological input to soil box
-----
```

The framework automatically determined that "Potential daily snowmelt" has to index over "Reaches" since it references the parameter "Degree-day factor for snowmelt", which we declared to be part of the "Snow" group, which indexes over "Reaches". Next, "Snow melt" does not reference any parameters, but it does reference "Potential daily snowmelt", and so it too has to

index over "Reaches". "Snow depth" inherits a "Reaches" dependency both from "Snow melt" and from its intial value parameter "Initial snow depth".

Even if we had declared the equations in a different order, the framework would have been able to put them in an order that makes sense. Every equation will be evaluated after any other equation that it accesses the current-timestep result of (i.e. using the RESULT accessor). Previous-timestep result accesses (LAST\_RESULT) do not have any impact on evaluation order. In this case, the equations "Snow depth" and "Hydrological input to soil box" do not depend on (the current-day value of) each other, and so they could have been placed by the framework in any order respective to one another.

In this example we used an input file that does not declare any index set dependencies for "Air temperature" or "Precipitation". If we had instead used an input file where these two timeseries are given per index in "Reaches", we would get the following batch structure.

**Example 14.** Batch structure for the SimplyP snow module if the user provided precipitation and air temperature timeseries per reach.

```
[Reaches]
----
Precipitation falling as snow
Precipitation falling as rain
Potential daily snowmelt
Snow melt
Snow depth
Hydrological input to soil box
----
```

Because of the dynamic batch structure, it can change if you start adding other equations later. For instance, the framework may decide to interleave new equations between the existing ones, or move some of the existing ones to a later batch, but correctness is always preserved.

#### 4.3.1 Warning about value accesses inside conditionals

You may have noticed that in the "Precipitation falling as snow" example we extracted the value of precipitation outside the if conditional.

This has to do with a limiting factor of the implementation of the framework. It is related to how it registers what equations depend on what other entities. When the model is finalized, the framework evaluates each equation once in a certain state to determine what entities it referenced. Since the equation may go down either branch (but not both) of the conditional if during this registration phase, it may miss value accesses that happened in the other branch. You can however access a value inside a conditional if you access it inside both branches.

#### **Example 16.** WRONG. DO NOT DO THIS! Extracting values inside conditionals.

```
EQUATION(Model, PrecipitationFallingAsSnow,
         if(INPUT(AirTemperature) <= 0) { return INPUT(Precipitation); }
         else { return 0.0; }
)</pre>
```

The general rule is that if you access an entity value at any point in the equation body, you have to make sure that this entity value is accessed regardless of the state of any other values.

**Note 4.** This means that you also have to make sure that an equation does not (potentially) return before it has accessed all the values it could access!

#### 4.3.2 What to do inside of or outside of equation bodies

Generally you should try to limit what kind of expressions you use inside equation bodies. Things to do inside EQUATION bodies:

- i Access values using PARAMETER, INPUT, RESULT, LAST\_RESULT, or any of the more advanced accesses described in Section 4.5.
- ii Simple control flow like for or if (but remember the warning about accesses inside conditionals above!!).
- iii Calling functions (that don't have side effects) that do mathematical computations on values, like exp, pow, sin etc.
- iv Always returning a value of type double (if you do not do this, you will get a compilation error).
- v You can refer to variables that are declared outside the equation body, but you should generally limit this to the entity handles you get from entity registration. Any variable you reference inside the equation body will be copied (by value) using the rules of C++11 lambda captures.

Things to do outside equation bodies, in the registration code.

- i Registering entities using the registration procedures.
- ii Registering additional relationships between model entities, such as with the SetInitialValue procedure, or SetSolver (explained later).

Remember that you always have to register an entity before you refer to it inside an equation body.

# 4.4 Advanced equation types

#### 4.4.1 Cumulation equations

Cumulation equations allow you to sum up the result of another equation over a given index set. Cumulation equations are unique in that you don't provide a body for them. Instead, the framework infers the body of the equation from the data provided in the registration.

**Example 17.** Declaring a cumulative equation that sum up the value of the DiffuseFlowOutput of each landscape unit, determining the total diffuse flow output of the subcatchment.

```
auto TotalDiffuseFlowOutput = RegisterEquationCumulative(Model, "Total⊔diffuse⊔flow∪
    output", DiffuseFlowOutput, LandscapeUnits);
//NOTE: Don't provide an equation body for TotalDiffuseFlowOutput!
```

A cumulative equation will get the same unit as the equation it cumulates. It will also get the same index set dependencies *except* for the index set it cumulates over. In Example 17, if "Diffuse flow output" indexes over "Reaches" and "Landscape units", then "Total diffuse flow output" indexes over "Reaches" only.

#### 4.4.2 ODE equations and solvers

A solver is a model entity of its own. A solver is registered with an integration method and some configuration values to the integration method. One can then add an equation to the solver batch using SetSolver (see example below). All equations with the same solver will be treated as one batch. This means that the solver inherits all the index set dependencies of all the equations in the solver. All the equations will then be evaluated for all of these indexes regardless of whether they had all the index sets as dependencies individually. The solver can (and usually will) evaluate the entire set of equations more than one time per timestep (and index combination). For instance it is not uncommon that a solver evaluates all the equations for 10 or more sub-timesteps per timestep. Moreover, some integration methods (like higher-order Runge-Kutta methods) require multiple evaluations per sub-timestep.

In the next example we have a predator-prey system subject to the Lotka-Volterra equations

$$\dot{x} = \alpha x - \beta xy$$
$$\dot{y} = \delta xy - \gamma y$$

Where x is the prey population, y is the predator population and  $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\delta$  are parameters. This can be implemented as follows

**Example 18.** Implementing the Lotka-Volterra system in Mobius. Parameter and unit registration is omitted.

```
auto LVSolver = RegisterSolver(Model, "Lotka-Volterrausolver", 0.1, IncaDascru); //It
     is not important what you name the solver.
auto Predation = RegisterEquation(Model, "Predation", Individuals);
SetSolver(Model, Predation, LVSolver);
auto PredatorGrowth = RegisterEquation(Model, "Predator growth", Individuals);
SetSolver(Model, PredatorGrowth, LVSolver);
auto PreyPopulation = RegisterEquationODE(Model, "Preypopulation", Individuals);
SetSolver(Model, PreyPopulation, LVSolver);
SetInitialValue(Model, PreyPopulation, InitialPreyPopulation); //
    InitialPreyPopulation is a parameter
auto PredatorPopulation = RegisterEquationODE(Model, "Predator population",
    Individuals);
SetSolver(Model, PredatorPopulation, LVSolver);
SetInitialValue(Model, PredatorPopulation, InitialPredatorPopulation); //
    InitialPredatorPopulation is a parameter
EQUATION (Model, Predation,
       return PARAMETER(PredationBaseRate) * RESULT(PreyPopulation) * RESULT(
           PredatorPopulation); //PredationBaseRate is beta
)
EQUATION (Model, PredatorGrowth,
       return PARAMETER(PredatorBaseGrowhtRate) * RESULT(PreyPopulation) * RESULT(
           PredatorPopulation); //PredatorBaseGrowthRate is delta
EQUATION (Model, PreyPopulation,
       return PARAMETER(PreyBirthRate) * RESULT(PreyPopulation) - RESULT(Predation);
            //PreyBirthRate is alpha
)
EQUATION (Model, Predator Population,
       return -PARAMETER(PredatorDeathRate) * RESULT(PredatorPopulation) + RESULT(
           PredatorGrowth); //PredatorDeathRate is gamma
```

There are a couple of things to note from Example 18.

- i You can put both regular and ODE equations on a solver. The regular equations will serve as partial computations that can be used by the ODE equations. In the example, it is a little excessive to factor out Predation and PredatorGrowth as their own equations, but one can easily imagine more complicated examples where a big computation can be reused by many ODE equations.
- ii Instead of returning the value of its state variable, an ODE equation has to return the time-derivative of its state variable. The integrator will then integrate the equation system to calculate the actual values of the ODE state variables.
- iii The integration of the ODE equations starts every timestep at the end-of-timestep value from the previous timestep, and then integrates the system over one timestep.

For each time the solver evaluates its batch (i.e. typically many times per timestep), the regular equations are evaluated in order before the ODE equations. Within an ODE-system, a reference

to a RESULT from the current solver batch will give you the intermediate sub-timestep value that the integrator is currently at. The RESULT of an ODE equation will refer to the (integrated) value of the state variable, not the value returned by the ODE equation, which was the time-derivative of the state variable.

If you refer to the RESULT value of a solver batch equation from an equation belonging to a different batch (i.e. it was not put on the same solver or any solver at all), you will get the end-of timestep value of that state variable. This is also the value that will be stored in the result timeseries that you can extract after a model run.

**Note 5.** While for regular equations the framework sorts them so that an equation is evaluated after another equation if it uses the value of the other equation, this is not the case if the other equation is an ODE equation. In that case the only requirement is that the referencing equation is put in the same batch (if it was registered with the same solver) or a batch later than the ODE equation. This is again because the ODE equation does not return a state value, but a derivative. All the state variables of the ODEs within a batch are advanced "simultaneously" during the integration step. See more about this in Section 4.8.

Which integration methods are available is subject to expansion. It is better that you look for them yourself in the source code, such as in mobius\_solver.h or boost\_solvers.h. Usually, IncaDascru (an adaptive 4th order Runge-Kutta) performs pretty well unless the ODE system is stiff. In case of a stiff system, you could use an implicit solver like BoostRosenbrock4, but it is significantly slower and should only be used if absolutely needed.

#### 4.4.3 Initial value equations

Initial value equations are special equations that are not evaluated during the main model run. Instead they are evaluated once (sometimes over multiple indexes) at the start of the model run to determine the initial value of another state variable. This is useful, because sometimes you don't want the initial value of a state variable to be given by a parameter, but by a computation depending on several parameters or initial values of other state variables.

```
Example 19. An initial value equation referencing parameters.
auto SoilVolume = RegisterEquation(Model, "Soil_volume", M3);
auto InitialSoilVolume = RegisterEquationInitialValue(Model, "Initial_soil_volume", M3);
SetInitialValue(Model, SoilVolume, InitialSoilVolume);

EQUATION(Model, InitialSoilVolume, return PARAMETER(CatchmentArea) * 1e6 * PARAMETER(InitialSoilDepth);
)//...
```

Initial value equations can also reference the result of other equations. What this means in practice is that they access the initial value of the other equation, whether that is given by a parameter or another initial value equation. Every equation is always given the initial value of 0 unless an initial value is explicitly specified. When you reference the initial value of another equation, you reference the handle of the equation itself, not the handle of the initial value equation (The initial value equation does not have any storage of its own for the value it generates, it just generates a value that is stored for the equation it is computing the initial value for).

**Example 20.** Another initial value equation that references the initial value computed in Example 19.

There are a couple of things to be aware of when referencing RESULTs inside an initial value equation.

- i Initial value equations have their own evaluation order *inside the solver batches of the equations they generate initial values for*. What this means is that if you have two initial value equations where their "parent" equations are in the same batch, you can let the initial value equations have a different dependency order than the parent equations.
- ii You can not reference the RESULT of an equation that is in a later batch. You can also not reference the RESULT of an equation that comes in a previous batch *unless* you use explicit indexing. This is an implementation limitation. If this is something that causes big problems for users, this is something we could try to improve. Note that this is again something you just have to be aware of while building the model, since the batch structure may not be apparent until a large part of the model has come together. You will usually not get error messages if you reference results that are not "available", but you may get a 0 or a result that is misindexed.

#### 4.4.4 Computed parameters (experimental feature)

If you have a value in the model that you know can be computed based on other parameters and will not change during model run, you can have this value as a computed parameter. Register it as a parameter in the usual way, then call ParameterIsComputedBy.

```
Example 21.

auto SoilMass = RegisterParameterDouble(Model, Land, "Soil_mass", KgPerKm2, 1e6);
ParameterIsComputedBy(Model, SoilMass, SoilMassComputation, true);
```

In the above example SoilMassComputation is an initial value equation. This initial value equation can only refer to the value of other parameters in its equation body, never the value of other equations or inputs. The last boolean argument to the ParameterIsComputedBy call, if true, says that this parameter should never be exposed in parameter files (or be editable in GUIs).

The step to compute parameters is executed right before the step that initializes the initial values of all equations. The initial value equation for the parameter is evaluated once for each instance of the parameter regardless of what index set dependencies the equation itself has. Right now it is not safe for this equation to depend on the value of other computed parameters since we don't sort the computations in order of dependencies for these.

#### 4.5 Advanced value accesses

#### 4.5.1 Special state values

The framework lets you access a few additional variables that tell you something about the state the equation is called under. These are.

- i CURRENT\_INDEX(IndexSetHandle) This will return an index\_t which tells you the current index of the index set corresponding to the provided IndexSetHandle. An index\_t is a small struct that contains information about what index set and what index it belongs to. In addition to providing the value of the current index, CURRENT\_INDEX forces the equation to depend on this index set, i.e. it will be evaluated for each index in the index set (otherwise, if it was not evaluated for each index in the index set, it would not make sense to ask what was the current index of that index set during evaluation).
- ii INDEX\_COUNT(IndexSetHandle) This will return an index\_ that is always guaranteed to be one larger than the largest index in the index set corresponding to the provided IndexSetHandle. Registers no dependencies.
- iii FIRST\_INDEX(IndexSetHandle) Gives you an index\_t corresponding to the first index of that index set. Registers no dependencies.
- iv INDEX\_NUMBER(IndexSetHandle, Number) Gives you an index\_t corresponding to the index of that number. However, be careful when using this that the index is smaller than INDEX\_COUNT(IndexSetHandle). Also, it is probably better to use a predeclared index, which guarantees you that what you are referring to has the right index name (see Section 4.5.3 below). Registers no dependencies.
- v CURRENT\_DAY\_OF\_YEAR() Returns an unsigned integer telling you which day of year it is (in the current model state). January 1st is always day 1. For instance, if the model "Start date" is 1999-1-15, then during the first timestep, the current day of year will be 15.
- vi DAYS\_THIS\_YEAR() Returns an unsigned integer that is either 365 (in a normal year) or 366 (in a leap year).

Note 6. The index\_t structure only contains numeric info about what index set handle it belongs to and the number of the index. However, instead of specifying these directly, it is better to use one of the wrapper macros that allow you to get an index of a specific index set. There are also a couple of overloaded operators that allow you to do size comparisons or increment index\_t's.

#### 4.5.2 Explicit indexing and explicit iteration

The most common case is that you don't have to use any explicit for loops. Instead the batch structure takes care of the for loops for you, evaluating every equation for all combination of indexes it depends on. Moreover, if you want to sum up the result of an equation, you can always use a cumulation equation. There may however be situations where you want to do something more complicated.

**Example 22.** A simplified version of the percolation output function in PERSiST.

In Example 22 we are in one of PERSiST's soil layers, and we want to iterate over every soil layer below this one (in this case, the indexes have been declared in order from top to bottom, so "below" is the same as after in the list of indexes), to see how much of the runoff from this soil layer is distributed to the other soil layers. To do this we iterate from CURRENT\_INDEX(SoilBoxes)+1 to INDEX\_COUNT(SoilBoxes). We then look up the maximum infiltration to the other soil box by calling PARAMETER(Infiltration, OtherSoil). We are looking up the value of the parameter Infiltration, but instead of looking up the value for the current index of SoilBoxes using PARAMETER(Infiltration), we provide an explicit index for the other soil box.

There are a few prerequisites for allowing you to do this

- i The parameter Infiltration has to depend on the index set SoilBoxes.
- ii Moreover, SoilBoxes has to be the immediate index set dependency for Infiltration. This means that Infiltration is in a parameter group that indexes over SoilBoxes directly (as opposed to only having a parent group that indexes over SoilBoxes).

Even if you explicitly index only one index set, the parameter can have more than one index set dependency. I.e. its parameter group can be a member of another parameter group which itself has an index set dependency. When you explicitly index only the immediate index set dependency, the index of the higher level index sets is as usual inferred to be the current index of these index sets in the execution state. Moreover, the call will register a dependency for PercolationOut on the higher level index set(s) that were automatically inferred, but not on SoilBoxes. (Though, PercolationOut does get a dependency on SoilBoxes any way from the call to CURRENT\_INDEX(SoilBoxes)).

**Example 23.** Equation A refers to PARAMETER(B, IX) in its equation body. Parameter B has the dependencies {"Reaches", "Landscape units"}, where "Landscape units" is the immediate dependency, and "Reaches" is a dependency of the parent group of the immediate group. The index IX will refer to an index of "Landscape units". The framework determines that A has to index over "Reaches".

You can also provide more than one explicit index.

Example 24. Equation A refers to PARAMETER(B, IX, IY) in its equation body. Parameter B has the dependencies {"Reaches", "Landscape units", "Soils"}, where "Soils" is the immediate dependency, "Landscape units" is a dependency of the parent group of the immediate group, and "Reaches" is again a dependency of a parent of that group. The index IX will refer to an index of "Landscape units", IY of "Soils". The framework determines that A has to index over "Reaches".

Example 24 also generalizes to higher numbers of explicit indexes. If you only want to explicitly index one of the higher index sets and let the framework infer the index of the immediate one, you can do the following.

```
Example 25. Explicitly indexing a higher index only.

PARAMETER(PercolationMatrix, OtherSoil, CURRENT_INDEX(SoilBoxes))
```

Explicit indexing of INPUTs is currently not available.

Explicit indexing of RESULT and LAST\_RESULT follows some of the same rules as explicit indexing of parameters, however here you have to be much more careful. For one thing, during model development, you can not be sure in which order the index set dependencies of an equation will be in, or even which index set dependencies it will have. This is after all determined by the framework at runtime. You therefore have to check that you guessed the correct order of the dependencies by looking at the equation batch structure (which could change if you for instance change the dependencies of some parameters).

Note 7. You should generally be careful with explicit indexing of RESULTs inside equations that are in a solver batch. If you explicitly index a result from the same batch you will either get just the end-of-timestep value (if you indexed an already evaluated index) or a 0 (if you for some reason explicitly indexed the currently evaluated index). This is because the sub-timestep values of the ODE system are not stored out to the main result storage and are discarded after (or during) integration. To give an example, while an expression like RESULT(WaterDepth, CURRENT\_INDEX(Soils)) would give the same value as RESULT(WaterDepth) outside a solver (albeit slower), it would give a 0 inside a solver (if WaterDepth is also evaluated in the solver). Of course, there should not be any reason to use such an expression in the first place. Explicit indexing of parameters is ok, but see the notes on performance under Section 4.7.

#### 4.5.3 Predeclared indexes

In some cases you may not want the indexes of an index set to be user defined, instead you want the model to determine the indexes. In that case you can call RequireIndex one or more times to tell the model what indexes you want in the index set. This call will also return to you an index\_t value that you can use to explicitly refer to this index inside EQUATIONs.

Example 26. Explicit indexing using predeclared indexes for the index set with handle Soils.

The order of these indexes in the index set will be the order they were declared in using RequireIndex.

#### 4.5.4 Branch iteration

If you have a branched index set, you may want to use the special connectivity information that is carried by its indexes. You can do this using branch iteration, which iterates over all the branch inputs to the current index of this index set.

**Example 27.** Iterating over all the branch inputs to the current index of the branched index set with handle Reach. Here we sum up the result of ReachFlow coming in from each branch.

The FOREACH\_INPUT expression is a macro that expands to an iteration over the branches. The index\_t of each branch that is iterated over is given by \*Input.

#### 4.6 Debugging features

Apart from using full C++ debugging techniques, there are a few framework features that may help you to better debug unexpected model behaviour. We have already covered using PrintResultStructure(Model) to show you the equation batch structure, which is something you should have turned on at all times during model development. You can also use PrintParameterStorageStructure(DataSet) and PrintInputStorageStructure(DataSet) to show you the index set dependencies of each parameter and input timeseries.

There are also five flags that you can turn on that will make the model store and print out additional debug information during the model run. These have to be declared above your #include "mobius.h"

```
Example 28. Declaring the debug flags.

#define MOBIUS_TIMESTEP_VERBOSITY 1

#define MOBIUS_TEST_FOR_NAN 1

#define MOBIUS_PRINT_TIMING_INFO 1

#define MOBIUS_EQUATION_PROFILING 1

#define MOBIUS_INDEX_BOUNDS_TESTS 1

#include "../../mobius.h"
```

You can turn the debug flags either on or off by setting them to 1 or 0 respectively (or turn them off by removing them entirely).

i MOBIUS\_TIMESTEP\_VERBOSITY. This has 3 levels. If it is set to 1 it will print out the number of the timestep for every timestep. If it is set to 2, it will also print out every time it changes the state of an index set during the iteration. If it is set to 3 it will also print out every time

it finishes the evaluation of an equation (or an integration in the case of a solver), along with the value. This can give you a full sense of the model evaluation like it is described in Example 4 (You should probably turn down the number of timesteps if you want to test the model in this mode).

- ii MOBIUS\_TEST\_FOR\_NAN. If turned on, this will test every result value to see if it was an inf or nan. In the case of such a value, it will halt the model execution and print out the current timestep, the state of the index sets, and the state of all the parameter, input and result dependencies of the equation that produced the illegal value. This will make the model run a little slower even if it does not encounter an illegal value. The nan test will not work correctly if you compile with the -ffast-math flag. The -ffast-math flag may make the model run a little faster, but the underlying floating point architecture will no longer make nans detectable, which can interfer both with this safeguard and other safeguards you may put in.
- iii MOBIUS\_PRINT\_TIMING\_INFO. If turned on, this will time and print out how long it took to run the model (both in milliseconds and processor instructions). This only gives very coarse information, but can be useful to detect if something weird happened (does the model suddenly run much slower after you added a new equation?).
- iv MOBIUS\_EQUATION\_PROFILING. This will give you very fine-grained information about how many processor ticks every equation evaluation took on average, and how many times each equation was evaluated. Note that the time to evaluate an equation is not always the same as the time to produce a result value since a solver may evaluate an equation many times to produce a result value for it. See Section 4.7 about tips on how to improve the speed of the model. Having this flag turned on will make the framework itself a little slower.
- v MOBIUS\_INDEX\_BOUNDS\_TESTS. This should probably be turned on as often as possible during model development. It will catch if during explicit indexing you provided an <code>index\_t</code> that was out of bounds for this index set. It will also give you an error if you use it to index a different index set than it was created from. Having this flag turned on will make the model run a little slower.

#### 4.7 Tips on model performance (speed)

This section will contain a few general tips on how to make the model run as fast as possible.

One important thing you can do is to turn on the MOBIUS\_EQUATION\_PROFILING flag (see the previous section) to see which individual equations are slow. You should then weigh the importance of improving the speed of an equation by the number of times it is evaluated. Equations with many index set dependencies are evaluated more often than equations with few index set dependencies, and equations in solvers are evaluated many more times than equations that are not on solvers.

The following things are common causes of slow equations:

i Calling transcendental functions from the C++ (C) standard math library, like exp, pow or sin. The standard implementation of these is often slow because they have to satisfy a large range of criteria. If you know that you only need implementations that are correct in a short value range (i.e.  $[0,2\pi)$ ) or need a smaller precisional correctness (say only 4 digits), then you may be able to find implementations that are much faster. You could also look into implementing that yourself, but this is a big topic of its own, and will not be covered here. Of course, it may often not be worth it going into the trouble of replacing the implementation of these. ii Explicit indexing (e.g. calling RESULT(Handle, Index)) is always slower than implicit indexing (e.g. RESULT(Handle)). This is because the model keeps all the values you need for implicitly indexed values in a quick buffer that it updates for you using a heavily optimized system. On the other hand, if you explicitly index a value, the model has to first determine where that value is stored using an index calculation, and then go back to main storage to retrieve it (risking cache misses).

Since equations on solvers are much more expensive than equations outside solvers, you may sometimes want to see if you can factor a calculation made in a solver equation out to a separate equation that can be evaluated before the solver is run.

```
Example 29. Instead of doing the reach flow in one calculation,
EQUATION (Model, ReachFlow,
                                //ReachFlow is an ODE equation
       double reachflowinput = 0.0;
       FOREACH_INPUT(Reach,
               reachflowinput += RESULT(ReachFlow, *Input);
       )
       reachflowinput += RESULT(TotalDiffuseFlowOutput);
       return ( reachflowinput - RESULT(ReachFlow) ) / ( RESULT(ReachTimeConstant) *
            (1.0 - PARAMETER(B)));
separate out the expensive bit that uses explicit indexing (and don't run the expensive bit on
the solver).
EQUATION (Model, ReachFlowInput,
                                        //ReachFlowInput should not run on the solver
       double upstreamflow = 0.0;
       FOREACH_INPUT(Reach,
               upstreamflow += RESULT(ReachFlow, *Input);
       )
       return upstreamflow + RESULT(TotalDiffuseFlowOutput);
                                      //ReachFlow should still run on the solver
EQUATION (Model, ReachFlow,
       return (RESULT(ReachFlowInput) - RESULT(ReachFlow) ) / ( RESULT(
           ReachTimeConstant) * (1.0 - PARAMETER(B)));
```

Cumulation equations are also always faster than explicit for loops, because the framework can use some tricks to determine how to look up the indexes of values accessed by a cumulation equation. Only use explicit for loops if you have to.

#### 4.8 Determining the batch structure of advanced models

**Note 8.** This section is very technical, and so you could probably skip it until your model does something completely unexpected and you have to figure out why.

Every equation has three types of dependencies that are important to model structure.

i Index set dependencies are the index sets that the equation should index over (i.e. be evaluated for every combination of indexes of). Again, remember that unlike for parameters, index sets can only appear once in the dependency list of an equation.

- ii Direct result dependencies are other equations of which this equation references the RESULT of (using implicit indexing: RESULT(Handle)).
- iii Cross index result dependencies are other equations of which this equation references the RESULT of using explicit indexing (e.g. RESULT(Handle, Index)).

When processing information about equation dependencies during model finalization (in the EndModelDefinition procedure), every equation gets its index set dependencies and result dependencies using the following rules:

- i A cumulation equation has the equation it cumulates as a direct result dependency (this is an exception to the description of direct result dependencies above). It also gets all the index set dependencies of the equation it cumulates *minus* the index set it cumulates over.
- ii An equation gets all the index set dependencies of all the parameters and inputs it references. If the reference uses explicit indexing, it will not get a dependency for the index sets that are explicitly indexed. It will also get a dependency on index sets it calls CURRENT\_INDEX or FOREACH\_INDEX on.
- iii An equation gets all the index set dependencies of its initial value parameter or initial value equation if it has one.
- iv An equation gets all the index set dependencies of all the other equations it references the RESULT or LAST\_RESULT of. The same rules for explicit indexing hold as for parameters. Note that this creates a large directed dependency graph between equations, where index set dependencies propagate down all the paths of the graph. Thus an equation can inherit an index set dependency not only from an equation it directly accesses the result of, but also one that was accessed by that equation and so on.

The list of equations (excluding initial value equations) are processed into a batch structure obeying the following rules:

- i All equations that were put on a solver have to belong to the same solver batch, and no other equations can belong to this batch. The index set dependencies of the batch is the union of the index set dependencies of all its equations. Similarly, the direct result (or cross-index) dependencies of a solver are the union of all the direct (or cross-index) result dependencies of its equations.
- ii Non-ode equations in a solver are sorted in order so that a given non-ode-equation comes after any other non-ode equations that it has a direct result dependency on. ODE equations are placed after the non-ode equations in any order (in practice the order they were declared in).
- iii Solver batches have to be placed after any equations (not belonging to itself) that it has a direct result dependency on, and in the same batch group as or after any it has a cross-index result dependency on.
- iv If two non-solver equations that have the same index set dependencies are placed next to each other, they are merged into a batch.
- v A non-solver equation has to be placed after any other equation it has a direct result dependency on. It has to be placed in the same batch group as or after any equation it has a cross-index result dependency on.

vi If a solver batch is next to one or more non-solver batches (or different solver batches) with the same index set dependencies, they form a batch group.

The rules above do not determine a unique structure. To improve the run speed of the model, the framework will also try to move batches and equations around (without breaking the rules) so that there are as few batches and batch groups as possible in the structure. I.e. it will prefer to place equations with the same index set dependencies next to each other. The algorithm we use is not guaranteed to find the most optimal structure (indeed, we are not even sure if such an algorithm would be polynomial or not), but it does produce pretty good results for the particular models we have built so far. The reason that such an minimalization of the amount of batch groups is a good idea is that there is some overhead associated with every time the model running code starts evaluating a new batch group.

During model creation you may accidentally specify equations that have direct result dependencies on each other in a circular way. This means that there is no possible way for the framework to place them in an order where each equation has access to all the result values it needs. The framework will detect this and print an error. Here ODE equations are exceptional in that any equation in the same solver can have a direct dependency on the result of an ODE equation regardless of circular dependencies.

This can sometimes be tricky if a solver is involved. Equation A can not depend on any equation in solver batch B if any equation at all in B (even those that A does not depend on) has a dependency on A. Just remember that the framework can never sort A into the middle of B as it has to evaluate all of B in one go.

For each batch, the order of evaluating the initial value of each equation (either by reading it from a parameter, setting it to a constant, or evaluating an initial value equation) is given its own evaluation order based on the dependencies of the initial value equations.

**Note 9.** The description given here does not give all the implementation details. To get a complete understanding you probably have to look up the implementation of the EndModelDefinition function in mobius\_model.cpp.

# 5 Application building API

We logically separate application building from model building. By application building we mean the process of building a program that can allocate a new model, allocate a dataset for it, put values in the dataset, choose how and when to run the model using the given parameters and inputs, extract result values and process them, and so on. By model building we mean the process of filling a given model object with information about the model structure, such as what parameters and equations it has, and what the equation bodies are. It is recommended to separate out the model building to its own procedure, because then the model can be reused by different applications.

# 5.1 Data types

#### 5.2 Procedures

# BeginModelDefinition

Application building procedure.

#### **Arguments:**

const char \*Name (optional) The name of the model.
const char \*Version (optional) The version of the model.

#### Returns:

A mobius\_model\* pointer to a newly created model object.

#### Description:

Heap-allocates a new model object. The model object can be freed using delete.

# ReadInputDependenciesFromFile

Application building procedure

#### Arguments:

mobius\_model \*Model Pointer to the model object.

const char \*Filename Name of an input file (of the .dat format).

#### Description:

If you wish to use an input file you have to let the model read the input dependencies before calling <code>EndModelDefinition</code> so that it can properly determine the model structure. This has to happen after the inputs are registered. You then have to read the actual input values into a dataset using <code>ReadInputsFromFile</code> after finalizing the model. The current procedure also registers any additional timeseries that are present in the input file.

#### EndModelDefinition

Application building procedure.

#### Arguments:

mobius\_model \*Model Pointer to the model object.

#### Description:

Finalizes the model object. You can no longer call model building procedures on it, and you should not try to make any further changes to it in general. This procedure generates the final equation batch structure of the model according to the rules given in Section 4.8.

#### GenerateDataSet

Application building procedure

#### **Arguments:**

mobius\_model \*Model Pointer to the model object.

#### Returns:

A mobius\_data\_set\* pointer to a newly created dataset object.

#### Description:

Heap-allocates a new dataset. The dataset can be freed using delete. You can have multiple datasets per model. You have to keep the model object alive as long as you want to use the dataset (i.e. don't delete the model before you are finished with the dataset). You can only generate a dataset from a model that has been finalized using EndModelDefinition.

# ReadParametersFromFile

Application building procedure

Arguments:

mobius\_data\_set \*DataSet

Pointer to the dataset object.

const char \*Filename The name of the parameter file (of the .dat format)

#### Description:

Reads the indexes of each index set and the values of all the parameters from a parameter file into the dataset.

# ReadInputsFromFile

Application building procedure

**Arguments:** 

mobius\_data\_set \*DataSet
const char \*Filename

Pointer to the dataset object.

The name of the input file (of the .dat format)

Description:

Reads the input timeseries from the file into the dataset. This can only be called if all the index sets registered in the model has been given indexes in the dataset (either by calling ReadParametersFromFile or by calling SetIndexes).

#### RunModel

Application building procedure

Arguments:

mobius\_data\_set \*DataSet

Pointer to the dataset object.

#### Description:

Attempts to run the model (that the dataset was generated from) with the parameter and input values given in this dataset. The start date is read from the "Start date" parameter, and the number of timesteps is read from the "Timesteps" parameter. All result timeseries are stored in the dataset.

There are a few more procedures that we will try to document soon.

#### CopyDataSet

Application building procedure

**Arguments:** 

mobius\_data\_set \*DataSet

Pointer to a dataset object.

bool CopyResults = false

Whether or not results series should be copied.

Returns:

A mobius\_data\_set \* pointer to a copy of the dataset.

#### **Description:**

Creates a new mobius\_data\_set and copies all index set structure, parameter and input values from the provided dataset. If CopyResults == true, result series are also copied if present. This does not copy the mobius\_model object, instead the new dataset will refer to the same model object as the old one.

#### SetIndexes

Application building procedure

#### **Arguments:**

mobius\_data\_set \*DataSet Pointer to a dataset object.

token\_string IndexSetName The name of one of the index sets in the model.

const std::vector<token\_string> A list of index names

&Indexes

#### **Description:**

Sets the indexes for the given index set in the dataset. Can only be done for an index set that has not received indexes in any way already.

#### SetParameterValue

Application building procedure

#### **Arguments:**

\*>& Indexes

mobius\_data\_set \*DataSet Pointer to a dataset object.

const char \*Name The name of a parameter in the model.

const std::vector<const char A list of index names, each index corresponding to

one of the index sets the parameter indexes over.

These have to be in the right order.

 $\boldsymbol{x}$  Value The value you want to set the parameter to. Here

x is either double, u64, bool or const char \* (the latter one for date values). The type has to match

the registered type of the parameter.

#### **Description:**

Sets the (indexed) parameter to the provided value. Example: SetParameterValue(DataSet, "Degree-day factor", {"Forest"}, 0.33);

#### GetParameterX

Application building procedure

# Arguments:

mobius\_data\_set \*DataSet Pointer to a dataset object.

const char \*Name The name of a parameter in the model.

const std::vector<const char

A list of index names, each index corresponding to

one of the index sets the parameter indexes over.

The of the finder bets the parameter may

These have to be in the right order.

#### Returns:

Returns an x value, where x is either double, u64 or bool.

#### **Description:**

Examples:double flow = GetParameterDouble(DataSet, "Reach flow",

{"First"});u64 Timesteps = GetParameterUInt(DataSet, "Timesteps", {});

# 6 Model building API

#### 6.1 Registration procedures

The registration procedures can only be called on a mobius\_model object that has not been finalized using EndModelDefinition.

#### RegisterUnit

Registration procedure

#### **Arguments:**

mobius\_model \*Model Pointer to the model object.

const char \*Name (optional) The name of the unit.

#### Returns:

A unit\_h handle to the newly registered unit.

#### Description:

Register a new unit with the model. If the name is omitted, it is assumed to be "dimensionless".

# RegisterIndexSet

Registration procedure

#### **Arguments:**

mobius\_model \*Model Pointer to the model object.

const char \*Name The full name of the index set.

#### Returns:

An index\_set\_h handle to the newly registered index set.

#### **Description:**

Register a new (basic) index set with the model.

# RegisterIndexSetBranched

Registration procedure

#### **Arguments:**

mobius\_model \*Model Pointer to the model object.

const char \*Name The full name of the index set.

#### Returns:

An index\_set\_h handle to the newly registered index set.

#### Description:

Register a new branched index set with the model.

#### RequireIndex

Registration procedure

#### Arguments:

mobius\_model \*Model Pointer to the model object.
index\_set\_h IndexSet Handle to an index set.
const char \*Name The name of the index.

#### Returns:

An index\_t giving the number of the new index in the index set.

#### Description:

Require the index set to have this index. If an index set has one or more required indexes, it can only have those indexes and not user-defined ones. Can only be called on basic index sets, not branched index sets.

# RegisterParameterGroup

Registration procedure

**Arguments:** 

mobius\_model \*Model Pointer to the model object.

const char \*Name The full name of the parameter group.

index\_set\_h IndexSet (optional) Handle to an index set that the group

should index over.

Returns:

An parameter\_group\_h handle to the newly registered parameter group.

Description:

Register a new parameter group with the model.

# SetParentGroup

Registration procedure

**Arguments:** 

mobius\_model \*Model Pointer to the model object.

parameter\_group\_h Child A handle to the child group.

parameter\_group\_h Parent A handle to the parent group.

Returns:

void

Description:

Set Parent to be the parent group of Child. Every parameter in Child will index both over the index set of Child and the index set of Parent.

# RegisterInput

Registration procedure

Arguments:

mobius\_model \*Model Pointer to the model object.

const char \*Name The full name of the input.

unit\_h Unit (optional) A unit for the input.

Returns:

An input\_h handle to the newly registered input timeseries.

Description:

Register a new input timeseries with the model.

RegisterParameterDouble	Registration procedure			
Arguments:				
mobius_model *Model	Pointer to the model object.			
parameter_group_h ParameterGroup	Handle to the parameter group that the parameter			
	should be put in.			
const char *Name	The full name of the parameter.			
unit_h Unit	Handle to the unit of the parameter.			
double Default	The default value of the parameter.			
double Min	(optional) The minimum value of the parameter.			
double Max	(optional) The maximum value of the parameter.			
const char *Description	(optional) A long-form description of the parameter.			
Returns:				
A parameter_double_h handle to the newly registered parameter.				
Description:				

Register a new parameter of type double with the model.

RegisterParameterUInt	Registration procedure	
Arguments:		
mobius_model *Model	Pointer to the model object.	
parameter_group_h ParameterGroup	Handle to the parameter group that the parameter	
	should be put in.	
const char *Name	The full name of the parameter.	
unit_h Unit	Handle to the unit of the parameter.	
u64 Default	The default value of the parameter.	
u64 Min	(optional) The minimum value of the parameter.	
u64 Max	(optional) The maximum value of the parameter.	
const char *Description	(optional) A long-form description of the parameter.	
Returns:		
A parameter_uint_h handle to the newly registered parameter.		
Description:		
Register a new parameter of type uint with the model.		

RegisterParameterBool	Registration procedure		
Arguments:			
mobius_model *Model	Pointer to the model object		
parameter_group_h ParameterGroup	Handle to the parameter group that the parameter		
	should be put in		
const char *Name	The full name of the parameter		
bool Default	The default value of the parameter		
const char *Description	(optional) A long-form description of the parameter		
Returns:			
A parameter_bool_h handle to the newly registered parameter.			
Description:			
Register a new parameter of type bool with the model			

RegisterParameterDate Registration procedure			
Arguments:			
mobius_model *Model	Pointer to the model object.		
parameter_group_h ParameterGroup	Handle to the parameter group that the parameter		
	should be put in.		
const char *Name	The full name of the parameter.		
const char *Default	The default value of the parameter. Must be on the		
	format "y-m-d".		
const char *Min	(optional) The minimum value of the parameter.		
	Must be on the form "y-m-d".		
const char *Max	(optional) The maximum value of the parameter.		
	Must be on the form "y-m-d".		
const char *Description	(optional) A long-form description of the parameter.		
Returns:			
A parameter_time_h handle to the newly registered parameter.			
Description:			
Register a new parameter of type date(time) with the model.			

RegisterEquation	Registration procedure		
Arguments:			
mobius_model *Model	Pointer to the model object.		
const char *Name	The full name of the equation.		
unit_h Unit	Handle to the unit of the equation.		
Returns:			
A equation_h handle to the newly registered equation.			
Description:			
Register a new equation with the model. The is is a basic equation. The equation			
body has to be provided separately using the EQUATION macro.			

RegisterEquationODE	Registration procedure		
Arguments:			
mobius_model *Model	Pointer to the model object.		
const char *Name	The full name of the equation.		
unit_h Unit	Handle to the unit of the equation.		
Returns:			
A equation_h handle to the newly registered equation.			
Description:			
Register a new equation of type ODE with the model. The equation body has to be			
provided separately using the EQUATION macro.			

# RegisterEquationInitialValue

Registration procedure

**Arguments:** 

mobius\_model \*Model Pointer to the model object.

const char \*Name The full name of the equation.

unit\_h Unit Handle to the unit of the equation.

#### Returns:

A equation\_h handle to the newly registered equation.

#### Description:

Register a new initial value equation with the model. The equation body has to be provided separately using the EQUATION macro.

# RegisterEquationCumulative

Registration procedure

**Arguments:** 

mobius\_model \*Model Pointer to the model object.

const char \*Name The full name of the equation.

(can not be an initial value equation).

index\_set\_h CumulatesOver Handle to the index set that should be cumulated

over.

parameter\_double\_h Weight (optional) A weight parameter for the cumulation.

#### Returns:

A equation h handle to the newly registered equation.

#### Description:

Register a new initial value equation with the model. No equation body should be provided. If a weight is provided it has to index over the CumulatesOver index set. For the purpose of the cumulation, the weight is scaled so that it sums to 1.

# SetInitialValue

Registration procedure

Arguments:

mobius\_model \*Model Pointer to the model object.

equation\_h Equation The equation to set the initial value for.

double Value A constant value to set as the initial value.

Returns:

void.

#### Description:

Set the initial value of an equation to be a constant.

#### SetInitialValue

Registration procedure

**Arguments:** 

mobius\_model \*Model Pointer to the model object.

equation\_h Equation The equation to set the initial value for.

parameter\_double\_h InitialValue A handle to a parameter of type double.

Returns:

void.

# Description:

Set the initial value of an equation to be determined by a parameter.

SetInitialValue	Registration procedure		
Arguments:			
mobius_model *Model	Pointer to the model object.		
equation_h Equation	The equation to set the initial value for.		
equation_h InitialValueEq	A handle to an initial value equation.		
Returns:			
void.			
Description:			
Set the initial value of an equation to be computed by an initial value equation.			

ResetEveryTimestep	Registration procedure
Arguments:	
mobius_model *Model	Pointer to the model object.
equation h Equation	Handle to an ODE equation.
Returns:	
void.	
Description:	
Tell the model that instead of start	ing the ODE state variable at the end value from
the previous timestep, it should sta	rt at 0 each timestep. This is primarily used if you
want to integrate some variable over	er each timestep, such as when you compute mean
values.	

RegisterSolver	Registration procedure	
Arguments:		
mobius_model *Model	Pointer to the model object.	
const char *Name	Name of the solver batch (for internal reference).	
double h	The suggested sub-timestep length of the solver (in the range 0 to 1).	
mobius_solver_setup_function	One of the integrator setup functions provided by	
*SetupFunction	mobius_solvers.h or boost_solvers.h, or others.	
double RelErr	(only available for some choices of SetupFunction)	
	The relative error tolerance of the solver.	
double AbsErr	(only available for some choices of SetupFunction)	
	The absolute error tolerance of the solver.	
Returns:		
A solver_h handle to the newly registered solver.		
Description:		
Register a new solver batch with the model. You may have to look at the source code		
to determine which solvers accept error tolerances.		

SetSolver	Registration procedure	
Arguments:		
mobius_model *Model	Pointer to the model object.	
equation h Equation	Handle to the equation to put in the solver batch.	
solver_h	The solver batch to put the equation in.	
Returns:		
void.		
Description:		
Put an equation in a solver batch. Can only be done with basic or ODE equations.		

GetXHandle	Registration procedure	
Arguments:		
mobius_model *Model	Pointer to the model object.	
const char *Name	The name of an already registered X.	
Returns:		
A $x_h$ handle.		
Description:		
X is either Equation, Input, ParameterGroup, ParameterDouble, ParameterUInt, Pa-		
rameterBool, ParameterTime, IndexSet, or Solver. Is useful if you want to modularize		
different parts of your model into several different registration procedures, but need		
one module to access some of the	ne handles of another one.	

# 6.2 Equation body declaration

There are a lot of advanced rules governing the use cases of the macros in this section, and so we recommend that you read the documentation above (that means at least all of Section 4, which describes the details. All the equation bodies of the registered equations have to be declared before calling EndModelDefinition on the model object.

```
EQUATION
                                                                       Equation macro
Arguments:
mobius_model *Model
                                     Pointer to the model object.
equation_h Equation
                                     A handle to the equation to declare the body for.
Decl
                                     The code for the equation body.
Description:
EQUATION (Model, Handle, Decl) expands to
SetEquation(Model, Handle,
         [=](value_set_accessor *ValueSet__) -> double {
                  Decl
         }
);
where Decl stands for possibly multiple lines of code of an equation body. These lines
of code always have to return a double. The value_set_accessor is an object that
can be used by other macros (such as PARAMETER or RESULT) inside the Decl to extract
values.
```

The following macros are only available inside the Decl of an EQUATION. This is because they

expand to something that refer to the value\_set\_accessor that is given as an argument in the lambda inside the expansion of the EQUATION macro.

PARAMETER	Equation macro
Arguments:	
parameter_ $x$ _h ParameterHandle	Handle to a parameter that you wish to extract the value of, where x is either double, uint or bool.
index_t Indexes	(optional, varargs) One or more indexes to explicitly index.

#### Returns:

Either a double, a u64 or a bool depending on what type of handle was passed in.

# Description:

Returns the value of the parameter, depending on the current state of the index sets. This is a macro that expands to an expression which either extracts a value from the <code>value\_set\_accessor</code> or registers a dependency of the surrounding <code>Equation</code> on this parameter, depending on the context of the evaluation.

INPUT	Equation macro	
Arguments:		
input_h InputHandle	Handle to an input that you wish to extract the value	
	of.	
Returns:		
A double.		
Description:		
Returns the current timestep value of the input timeseries, depending on the cur-		
rent state of the index sets. This is a macro that expands to an expression which		
either extracts a value from the value_set_accessor or registers a dependency of the		

surrounding Equation on this input, depending on the context of the evaluation.

RESULT	Equation macro	
Arguments:		
equation_h EquationHandle	Handle to an equation that you wish to extract the value of.	
index_t Indexes	(optional, varargs) One or more indexes to explicitly	
	index.	
Returns:		
A double.		
Description:		
Returns the value of the current timestep result of the equation, depending on the		
current state of the index sets. This is a macro that expands to an expression which		
either extracts a value from the value_set_accessor or registers a dependency of the		
surrounding Equation on this equation, depending on the context of the evaluation.		

LAST_RESULT	Equation macro
Arguments:	-
equation_h EquationHandle	Handle to an equation that you wish to extract the previous-timestep value of.
index_t Indexes	(optional, varargs) One or more indexes to explicitly index.
Returns:	
A double	

# A double.

# **Description:**

Returns the value of the previous timestep result of the equation, depending on the current state of the index sets. This is a macro that expands to an expression which either extracts a value from the value\_set\_accessor or registers a (last-result) dependency of the surrounding Equation on this equation, depending on the context of the evaluation.

EARLIER_RESULT	Equation macro
Arguments:	
equation_h EquationHandle	Handle to an equation that you wish to extract an earlier-timestep value of.
u64 StepBack	How many timesteps back you want to go.
index_t Indexes	(optional, varargs) One or more indexes to explicitly index.
Returns:	

# A double.

#### **Description:**

Looks up the result of the equation value for the current timestep minus StepBack number of timesteps. So if StepBack=0 you get the current result, if StepBack=1 you get the last result and so on. This registers the same dependencies as a LAST\_RESULT lookup.

CURRENT_DAY_OF_YEAR	Equation macro
Arguments:	
None.	
Returns:	
A u64.	
Description:	
Returns the current day of the year in the context of the simulation	on. January 1st
corresponds to a current day of year of 1. This is a macro that expands	to an expression
that extracts the value from the value_set_accessor.	

#### DAYS\_THIS\_YEAR

Equation macro

Arguments:

None.

Returns:

A u64.

## Description:

Returns the amount of days this year in the context of the simulation. Is either 365 (in a common year) or 366 (in a leap year). This is a macro that expands to an expression that extracts the value from the value\_set\_accessor.

#### INDEX COUNT

Equation macro

**Arguments:** 

index\_set\_h IndexSet

Handle to an index set.

Returns:

A size\_t.

#### Description:

Returns the amount of indexes in this index set. This is a macro that expands to an expression that extracts the value from the value\_set\_accessor.

#### CURRENT\_INDEX

Equation macro

Arguments:

index\_set\_h IndexSet

Handle to an index set.

#### Returns:

A index\_t.

#### Description:

Returns the current (numeric) index of the given index set. This is a macro that expands to an expression that either extracts the value from the value\_set\_accessor or registers a dependency of the surrounding Equation on this index set, depending on the contex of the evaluation.

# FOREACH\_INPUT

Equation macro

Arguments:

index\_set\_h IndexSet

Handle to a branched index set.

Def The code to put inside of the for loop.

Description:

Expands to something that looks like

```
for(<every index in that is a branch input to CURRENT_INDEX(IndexSet)>)
{
          Def
```

}

Inside Def you can refer to the index of the iterated branch by \*Input. Note that FOREACH\_INPUT calls CURRENT\_INDEX(IndexSet), and thus registers an index set dependency.

INPUT_COUNT		Equation macro
Arguments:		
index set h IndexSet	Handle to a branched index set	

#### Returns:

A size\_t.

#### Description:

Returns the amount of branch input indexes to the current index in the index set. This is a macro that expands to an expression that either extracts the value from the value\_set\_accessor or registers a dependency of the surrounding Equation on this index set, depending on the contex of the evaluation.

# References

- [1] M. N. Futter, M. A. Erlandsson, D. Butterfield, P. G. Whitehead, S. K. Oni, and A. J. Wade. PERSiST: a flexible rainfall-runoff modelling toolkit for use with the INCA family of models. *Hydrol. Earth Syst. Sci.*, 18:855–873, 2014.
- [2] L. A. Jackson-Blake, J. E. Sample, A. J. Wade, R. C. Helliwell, and R. A. Skeffington. Are our dynamic water quality models too complex? a comparison of a new parsimonious phosphorous model, SimplyP, and INCA-P. *Water Resources Research*, 53:5382–5399, 2017.