



# CASAL2 User Manual

S. Rasmussen, I. Doonan, A. Dunn, C. Marsh, K.  
Large, S. Mormede

NIWA Technical Report 139  
ISSN 1174-2631  
2016

CASAL2 User Manual (modified 2016-09-03) for use with  
casal2\_v2016-09-03



Citation: S. Rasmussen, I. Doonan, A. Dunn, C. Marsh, K. Large, S. Mormede (2016). CASAL2  
User Manual, v2016-09-03. National Institute of Water & Atmospheric Research Ltd. NIWA  
*Technical Report 139*. 171 p.



## Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	Where to get CASAL2 . . . . .	1
1.2	System requirements . . . . .	1
1.3	Necessary files . . . . .	1
1.4	Getting help . . . . .	2
1.5	Technical details . . . . .	2
<b>2</b>	<b>Model overview</b>	<b>3</b>
2.1	Introduction . . . . .	3
2.2	The population section . . . . .	4
2.3	The estimation section . . . . .	4
2.4	The observation section . . . . .	5
2.5	The report section . . . . .	5
<b>3</b>	<b>Running CASAL2</b>	<b>7</b>
3.1	Using CASAL2 . . . . .	7
3.2	The input configuration file . . . . .	7
3.3	Redirecting standard output . . . . .	8
3.4	Command line arguments . . . . .	8
3.5	Constructing a CASAL2 input configuration files . . . . .	9
3.5.1	Commands . . . . .	9
3.5.2	Subcommands . . . . .	10
3.5.3	The command-block format . . . . .	11
3.5.4	Commenting out lines . . . . .	11
3.5.5	Determining parameter names . . . . .	11
3.6	Single stepping CASAL2 . . . . .	12
3.7	CASAL2 exit status values . . . . .	12
<b>4</b>	<b>The population section</b>	<b>13</b>
4.1	Introduction . . . . .	13
4.2	Population structure . . . . .	13
4.3	The state object and the partition . . . . .	15
4.4	Time sequences . . . . .	16
4.4.1	Initialisation . . . . .	17
4.5	Model run years . . . . .	19
4.6	Projection years . . . . .	19
4.7	Population processes . . . . .	20
4.7.1	Recruitment . . . . .	20
4.7.2	Ageing . . . . .	22
4.7.3	Mortality . . . . .	22
4.7.3.1	Constant mortality rate . . . . .	23

4.7.3.2	Event and biomass-event mortality . . . . .	23
4.7.3.3	Instantaneous mortality . . . . .	24
4.7.3.4	Hollings mortality rate . . . . .	25
4.7.4	Transition By Category . . . . .	26
4.7.4.1	Annual transition by category . . . . .	27
4.7.5	Tag Release events . . . . .	27
4.7.6	Tag Loss . . . . .	27
4.8	Derived quantities . . . . .	28
4.9	Age-length relationship . . . . .	29
4.10	Weightless model . . . . .	30
4.11	Maturity, in models without maturing in the partition . . . . .	30
4.12	Selectivities . . . . .	30
4.12.1	Constant . . . . .	31
4.12.2	Knife-edge . . . . .	31
4.12.3	All-values . . . . .	31
4.12.4	All-values-bounded . . . . .	31
4.12.5	Increasing . . . . .	32
4.12.6	Logistic . . . . .	32
4.12.7	Inverse logistic . . . . .	32
4.12.8	Logistic producing . . . . .	32
4.12.9	Double-normal . . . . .	32
4.12.10	Double-exponential . . . . .	33
4.13	Time Varying Parameters . . . . .	33
4.13.1	Constant . . . . .	33
4.13.2	Random Walk . . . . .	33
4.13.3	Annual shift . . . . .	34
4.13.4	Exogenous . . . . .	34
<b>5</b>	<b>The estimation section</b>	<b>35</b>
5.1	Role of the estimation section . . . . .	35
5.2	The objective function . . . . .	35
5.3	Specifying the parameters to be estimated . . . . .	35
5.4	Point estimation . . . . .	36
5.4.1	The numerical differences minimiser . . . . .	36
5.4.2	The differential evolution minimiser . . . . .	37
5.4.3	Betadiff minimiser . . . . .	38
5.4.4	ADOL-C minimiser . . . . .	38
5.4.5	CPPAD minimiser . . . . .	38
5.4.6	Dlib minimiser . . . . .	38
5.4.7	De solver minimiser . . . . .	38
5.5	Posterior profiles . . . . .	39
5.6	Bayesian estimation . . . . .	39

5.7	Priors . . . . .	42
5.8	Penalties . . . . .	43
5.9	Additional Priors . . . . .	44
5.9.1	Estimate Transformations . . . . .	44
<b>6</b>	<b>The observation section</b>	<b>45</b>
6.1	Observations . . . . .	45
6.1.1	Mortality block associated observations . . . . .	45
6.1.2	General process observations . . . . .	52
6.1.3	Specific process observations . . . . .	52
6.2	Likelihoods . . . . .	55
6.2.1	Likelihoods for proportions-at-age observations . . . . .	55
6.2.2	Likelihoods for abundance and biomass observations . . . . .	56
6.2.3	Likelihoods for tag recapture by age and length observations . . . . .	57
6.2.4	Likelihoods for proportions-by-category observations . . . . .	57
6.3	Process error . . . . .	58
6.4	Calculating nuisance q's . . . . .	58
6.5	Ageing error . . . . .	60
6.6	Simulating observations . . . . .	61
6.7	Pseudo-observations . . . . .	61
<b>7</b>	<b>The report section</b>	<b>63</b>
7.1	Print the partition at the end of an initialisation . . . . .	63
7.2	Print the partition . . . . .	63
7.3	Print the age length and length weight values . . . . .	64
7.4	Print a process summary . . . . .	64
7.5	Print derived quantities . . . . .	64
7.6	Print the estimated parameters . . . . .	64
7.7	Print the estimated parameters in a vector format . . . . .	64
7.8	Print the objective function . . . . .	64
7.9	Print the covariance matrix . . . . .	64
7.10	Print observations, fits, and residuals . . . . .	64
7.11	Print simulated observations . . . . .	65
7.12	Print the ageing error misclassification matrix . . . . .	65
7.13	Print selectivities . . . . .	65
7.14	Print the random number seed . . . . .	65
7.15	Print the results of an MCMC . . . . .	65
7.16	Print the MCMC samples as they are calculated . . . . .	65
7.17	Print the MCMC objective function values as they are calculated . . . . .	65
7.18	Print time varying parameters . . . . .	66
7.19	Tabular reporting . . . . .	66
<b>8</b>	<b>Population command and subcommand syntax</b>	<b>67</b>

8.1	Model structure . . . . .	67
8.2	Initialisation . . . . .	68
8.2.1	Cinitial . . . . .	68
8.2.2	Derived . . . . .	68
8.2.3	Iterative . . . . .	69
8.2.4	State Category By Age . . . . .	69
8.3	Categories . . . . .	69
8.4	Time-steps . . . . .	70
8.5	Processes . . . . .	70
8.5.1	Ageing . . . . .	71
8.5.2	Maturation . . . . .	71
8.5.3	Mortality Constant Rate . . . . .	71
8.5.4	Mortality Event . . . . .	72
8.5.5	Mortality Event Biomass . . . . .	72
8.5.6	Mortality Holling Rate . . . . .	73
8.5.7	Mortality Instantaneous . . . . .	74
8.5.8	Mortality Prey Suitability . . . . .	75
8.5.9	Nop . . . . .	76
8.5.10	Recruitment Beverton Holt . . . . .	76
8.5.11	Recruitment Constant . . . . .	77
8.5.12	Survival Constant Rate . . . . .	77
8.5.13	Tag By Age . . . . .	78
8.5.14	Tag By Length . . . . .	79
8.5.15	Tag Loss . . . . .	80
8.5.16	Transition Category . . . . .	80
8.5.17	Transition Category By Age . . . . .	81
8.6	Time varying parameters . . . . .	82
8.6.1	Annual Shift . . . . .	82
8.6.2	Constant . . . . .	83
8.6.3	Exogenous . . . . .	83
8.6.4	Linear . . . . .	83
8.6.5	Random Draw . . . . .	83
8.6.6	Random Walk . . . . .	84
8.7	Derived quantities . . . . .	84
8.7.1	Abundance . . . . .	85
8.7.2	Biomass . . . . .	85
8.8	Age-length relationship . . . . .	85
8.8.1	Data . . . . .	86
8.8.2	None . . . . .	86
8.8.3	Schnute . . . . .	86
8.8.4	Von Bertalanffy . . . . .	87
8.9	Length-weight . . . . .	87



8.9.1	Basic . . . . .	88
8.9.2	None . . . . .	88
8.10	Selectivities . . . . .	88
8.10.1	All Values . . . . .	89
8.10.2	All Values Bounded . . . . .	89
8.10.3	Constant . . . . .	89
8.10.4	Double Exponential . . . . .	89
8.10.5	Double Normal . . . . .	90
8.10.6	Increasing . . . . .	90
8.10.7	Inverse Logistic . . . . .	91
8.10.8	Knife Edge . . . . .	91
8.10.9	Logistic . . . . .	91
8.10.10	Logistic Producing . . . . .	92
<b>9</b>	<b>Estimation command and subcommand syntax</b>	<b>92</b>
9.1	Estimation methods . . . . .	92
9.1.1	Beta . . . . .	93
9.1.2	Lognormal . . . . .	93
9.1.3	Normal . . . . .	94
9.1.4	Normal By Stdev . . . . .	94
9.1.5	Normal Log . . . . .	94
9.1.6	Uniform . . . . .	94
9.1.7	Uniform Log . . . . .	94
9.2	Point estimation . . . . .	94
9.2.1	A D O L C . . . . .	95
9.2.2	Beta Diff . . . . .	95
9.2.3	C P P A D . . . . .	96
9.2.4	D E Solver . . . . .	96
9.2.5	D Lib . . . . .	96
9.2.6	Gamma Diff . . . . .	96
9.3	Monte Carlo Markov Chain (MCMC) . . . . .	97
9.3.1	Independence Metropolis . . . . .	97
9.4	Profiles . . . . .	98
9.5	Defining catchability constants . . . . .	99
9.5.1	Free . . . . .	99
9.5.2	Nuisance . . . . .	99
9.6	Defining penalties . . . . .	99
9.6.1	Process . . . . .	100
9.7	Defining priors on parameter ratios, differences, and means . . . . .	100
9.7.1	Beta . . . . .	100
9.7.2	Vector Average . . . . .	101
9.7.3	Vector Smoothing . . . . .	101

<b>10 Observation command and subcommand syntax</b>	<b>102</b>
10.1 Observation types . . . . .	102
10.1.1 Process Abundance . . . . .	103
10.1.2 Abundance . . . . .	104
10.1.3 Process Biomass . . . . .	104
10.1.4 Biomass . . . . .	105
10.1.5 Process Removals By Age . . . . .	106
10.1.6 Process Removals By Length . . . . .	107
10.1.7 Process Proportions At Age . . . . .	108
10.1.8 Proportions At Age . . . . .	109
10.1.9 Process Proportions At Length . . . . .	110
10.1.10 Proportions At Length . . . . .	111
10.1.11 Process Proportions By Category . . . . .	112
10.1.12 Proportions By Category . . . . .	113
10.1.13 Proportions Migrating . . . . .	114
10.1.14 Tag Recapture By Age . . . . .	115
10.1.15 Tag Recapture By Length . . . . .	117
10.2 Likelihoods . . . . .	118
10.2.1 Binomial . . . . .	118
10.2.2 Binomial Approx . . . . .	118
10.2.3 Dirichlet . . . . .	118
10.2.4 Log Normal . . . . .	118
10.2.5 Log Normal With Q . . . . .	118
10.2.6 Multinomial . . . . .	118
10.2.7 Normal . . . . .	118
10.2.8 Pseudo . . . . .	118
10.3 Defining ageing error . . . . .	118
10.3.1 Data . . . . .	119
10.3.2 None . . . . .	119
10.3.3 Normal . . . . .	119
10.3.4 Off By One . . . . .	119
<b>11 Report command and subcommand syntax</b>	<b>120</b>
11.1 Report commands and subcommands . . . . .	120
11.1.1 Ageing Error Matrix . . . . .	120
11.1.2 Catchabilities . . . . .	121
11.1.3 Category Info . . . . .	121
11.1.4 Category List . . . . .	121
11.1.5 Correlation Matrix . . . . .	121
11.1.6 Covariance Matrix . . . . .	121
11.1.7 Derived Quantity . . . . .	121
11.1.8 Estimable . . . . .	121

11.1.9 Estimate Summary . . . . .	122
11.1.10 Estimate Value . . . . .	122
11.1.11 Hessian Matrix . . . . .	122
11.1.12 Initialisation Partition . . . . .	122
11.1.13 M C M C Covariance . . . . .	122
11.1.14 M C M C Objective . . . . .	122
11.1.15 M C M C Sample . . . . .	122
11.1.16 M P D . . . . .	122
11.1.17 Objective Function . . . . .	122
11.1.18 Observation . . . . .	122
11.1.19 Output Parameters . . . . .	122
11.1.20 Partition . . . . .	122
11.1.21 Partition Biomass . . . . .	122
11.1.22 Partition Mean Weight . . . . .	123
11.1.23 Process . . . . .	123
11.1.24 Random Number Seed . . . . .	123
11.1.25 Selectivity . . . . .	123
11.1.26 Simulated Observation . . . . .	123
11.1.27 Standard Header . . . . .	123
11.1.28 Time Varying . . . . .	123
<b>12 Including commands from other files</b>	<b>123</b>
<b>13 Examples</b>	<b>125</b>
13.1 Input File Specification . . . . .	125
13.1.1 Keywords And Reserved Characters . . . . .	125
13.2 An example of a simple model . . . . .	128
13.3 More examples of shorthand syntax and use of CASAL2's reserved and key characters	130
<b>14 Post processing output using R</b>	<b>135</b>
<b>15 Troubleshooting</b>	<b>137</b>
15.1 Introduction . . . . .	137
15.2 Reporting errors . . . . .	137
15.3 Guidelines for reporting a problem with CASAL2 . . . . .	137
<b>16 CASAL2 software license</b>	<b>139</b>
<b>17 Acknowledgements</b>	<b>143</b>
<b>18 Quick reference</b>	<b>145</b>



---

## 1. Introduction

CASAL2 is a generalised age-structured population dynamics modelling software package that allows flexibility in specifying model structure, population dynamics, parameter estimation, and model outputs. CASAL2 can model population dynamics for an age-structured population using a range of population dynamics observations, including mark-recapture, relative and absolute abundance time series, and age frequency data. CASAL2 does this by implementing an age-structured population dynamics model that can have user defined categories (e.g., immature, mature, male, female, predator, prey, etc.) to specify the population structure, and a user-defined age range.

### 1.1. Where to get CASAL2

In the first instance, see <http://www.niwa.co.nz/> for information about CASAL2. The CASAL2 source code is hosted on github, and can be found at <https://github.com/NIWAFisheriesModelling/CASAL2>.

A Microsoft Windows bundle includes the binary, manual, examples and other help guides. It can be downloaded at <ftp://ftp.niwa.co.nz/Casal2/windows/Casal2.zip> for the Microsoft Windows version. The Linux bundle which includes a binary, manual, examples and other help guides can be downloaded at <ftp://ftp.niwa.co.nz/Casal2/linux/Casal2.tar.gz>.

### 1.2. System requirements

CASAL2 is available for most IBM compatible machines running 64-bit Linux and Microsoft Windows operating systems.

Several of CASAL2s tasks are highly computer intensive and a fast processor is recommended. Depending on the model implemented, some of CASAL2s tasks can take a considerable amount of time (minutes to hours), and in extreme cases can even take several days to undertake an MCMC estimate.

The program itself requires only a few megabytes of hard-disk space but output files can consume large amounts of disk space. Depending on number and type of user output requests, the output could range from a few hundred kilobytes to several hundred megabytes. When estimating model fits, several hundred megabytes of RAM may be required, depending on the spatial size of the model, number of categories, and complexity of processes and observations. For extremely large models, several gigabytes of RAM may occasionally be required.

### 1.3. Necessary files

For both 64-bit Linux and Microsoft Windows, only the binary executable `casal2` or `casal2.exe` is required to run CASAL2. No other software is required. We do not provide a version for 32-bit operating systems.

CASAL2 offers little in the way of post-processing of model output, and a package available that allows tabulation and graphing of model outputs is recommended. We suggest software such as **R** (?) to assist in the post processing of CASAL2 output. We provide the CASAL2 **R** package for importing the CASAL2 output into **R** (see Section 14).

### 1.4. Getting help

CASAL2 is distributed as unsupported software, however the Development Team would appreciate being notified of any problems or errors in CASAL2. See Section 15.2 for the recommended template for reporting issues. For further information on CASAL2 please contact the Development Team at [casal2@niwa.co.nz](mailto:casal2@niwa.co.nz).

### 1.5. Technical details

CASAL2 was compiled on Linux using gcc (<http://gcc.gnu.org>), the C/C++ compiler developed by the GNU Project (<http://gcc.gnu.org>). The 64-bit Linux version was compiled using gcc version 5.2.1 20151010 Ubuntu Linux (<http://www.ubuntu.com/>). The Microsoft Windows (<http://www.microsoft.com>) version was compiled using MingW (<http://www.mingw.org>) gcc (tdm64-1) 5.1.0 (<http://gcc.gnu.org>). The Microsoft Windows(<http://www.microsoft.com>) installer was built using the Inno Setup 5 (<http://www.jrsoftware.org/isdl.php>).

CASAL2 includes number of different minimisers — Different minimisers may be better at some models than others. The first three are non-differentiation based minimisers: the first is closely based on the main algorithm of ?, and which uses finite difference gradients; the second is an implementation of the differential evolution solver (?), and based on code by Lester E. Godwin of PushCorp, Inc.; and the third is Dlib (?). The three differentiation based minimisers are: ADOLC, an auto differentiation minimiser (?); CPPAD an auto differentiation minimiser similar to ADOLC (?); and the third is a modified version of an older version of ADOL-C (v1.8.4) that was used as the auto differentiation minimiser in the first version of CASAL (?).

The random number generator used by CASAL2 uses an implementation of the Mersenne twister random number generator (?). This, the command line functionality, matrix operations, and a number of other functions use the BOOST C++ library (Version 1.58.0).

Note that the output from CASAL2 may differ slightly on the different platforms due to different precision arithmetic or other platform dependent implementation issues. The source code for CASAL2 is available in the windows bundle or on the github repository at <https://github.com/NIWAFisheriesModelling/CASAL2>.

Unit tests of the underlying CASAL2 code are carried out at build time, using the GOOGLE mock and unit testing framework. The unit test framework aims to cover a significant proportion of the key functionality within the CASAL2 code base. The unit test code for CASAL2 is available as a part of the underlying source code.

---

## 2. Model overview

### 2.1. Introduction

CASAL2 is an age-structured population dynamics model. It implements a statistical catch-at-age population dynamics, using a discrete time-step state-space model that represents a cohort-based population age structure .

CASAL2 is run from the console window in Microsoft Windows or from a terminal window in Linux. CASAL2 gets its information from input data files, the main one of which is the *input configuration file*. Commands and subcommands in the input configuration file are used to define the model structure, provide observations, define parameters, and define the outputs (reports) for CASAL2. Command line switches tell CASAL2 the run mode and where to direct its output. See Section 3 for details.

We define the model in terms of the *state*. The state consists of two parts, the *partition*, and any *derived quantities*. The state will typically change in each *time-step* of every year, depending on the *processes* defined for those time-steps in the model.

The *partition* is a representation of the population at an instance in time, and can be considered a matrix of the numbers of individuals within each category and at each age.

A *derived quantity* is a summary of the abundance or biomass in a selected part of the partition at some instance in time. Unlike the partition (which is updated as each new process is applied), a derived quantity records a single value for each year of the model run. Hence, derived quantities build up a vector of values over the time period represented by the model. For example, the total biomass of individuals in categories labelled, say, ‘mature’ at some instance in the annual cycle may be a derived quantity. The derived quantity is then available to the model to be reported, or to be an input into another process (for example, recruitment) at some instance in the model in a subsequent year.

The state at some instance in time is the term for the combination of the partition and any derived quantities at that instance in time. Throughout the model, changes to the state occur from the application of *processes*. This state then provides the basis for the generation of expected values for *observations*, as well as for reports and other outputs.

Running of the model consists of two steps — first the model state is initialised for a number of iterations (years), then the model runs over a range of predefined years.

Initialisation can be in one or more phases, and for each phase, the processes that occur in each year, and the order in which they are applied, need to be defined. The processes that occur is controlled by the *annual cycle*. This defines what processes happen in each model year and in what sequence. Further, the processes in each year are split up into one or more time-steps (with at least one process occurring in each time-step). You can think of each time-step as representing a particular part of the calendar year, or you can just treat them as an abstract sequence of events.

The division of the year into an arbitrary number of time-steps allows the user to specify the exact order in which processes occur, and how/when observations are evaluated. The user specifies the time-steps, their order, and the processes within each time-step. If more than one process occurs in the same time-step, then they occur in the order that they are specified.

Observations are always linked to a time-step, and are evaluated by the model in time-step in which they occur. Hence, time-steps can be used to break processes into groups, and assist in defining the timing of the observations within the annual cycle. The manner in which observations are evaluated and how the expected values are calculated by the model is described later in Section 6.

The population structure of CASAL2 follows the usual population modelling conventions and is similar to those implemented in, for example, CASAL (?). The model records the numbers of individuals by category and age (e.g., numbers of males and females at age). In general, cohorts are added via a recruitment event, are aged annually, and are removed from the population via various forms of mortality. The population is assumed to be closed (i.e., no immigration or emigration from the modelled area)

A model is implemented in CASAL2 using an input configuration file, which provides a complete description of the model structure (i.e., population structure, initialisation, and the subsequent population processes), observations, estimation methods, and reports (outputs) requested. CASAL2 runs from a console window on Microsoft Windows or from a text terminal on Linux. A model can be either *run*, estimable parameters can be *estimated* or *profiled*, *MCMC* distributions calculated, and these estimates can be *projected* into the future or used by CASAL2 as parameters of an operating model to *simulate* observations.

A model in CASAL2 is specified by an input configuration file, and comprises of four main components. These are the population section that defines the model structure, population dynamics, etc.; the estimation section that defines the methods of estimation (minimisation methods or MCMC algorithms) and the model parameters to be estimated; the observation section that defines the observational data and associated likelihoods; and the report section that defines the printouts and reports from the model and where these are saved. The input configuration file completely describes a model implemented in CASAL2. See Sections 8, 9, 10, and 11 for details and specification of CASAL2s command and subcommand syntax within the input configuration file.

### 2.2. The population section

The population section (Section 4) defines the model of the population dynamics. It describes the model structure (i.e. the population structure), initialisation method and phases, run and projection years (model period), population processes (for example, recruitment, migration, and mortality), selectivities, and key population parameters.

### 2.3. The estimation section

The estimation section (Section 5) specifies the parameters to be estimated, estimation methods, penalties and priors. Estimation is based on an objective function (e.g., negative log posterior). Depending on the run mode, the estimation section is used to specify the methods for finding a point estimate (i.e., the set of parameter values that minimizes the objective function), doing profiles, or MCMC methods and options, etc.

Further, the estimation section specifies the parameters to be estimated within each model run and the estimation methods. The estimation section specifies the choice of estimation method, which model parameters are to be estimated, priors, starting values, and minimiser control values.

Penalties and priors act as constraints on the estimation. They can either encourage or discourage (depending on the specific implementation) parameter estimates that are ‘near’ some value, and hence influence the estimation process. For example, a penalty can be included in the objective function to discourage parameter estimates that lead to models where the recorded catch was unable to be fully taken.



## **2.4. The observation section**

Types of observations, their values, and the associated error structures are defined in the observation section (Section 6). Observations are data which allow us to make inferences about unknown parameters. The observation section specifies the observations, their errors, likelihoods, and when the observations occur. Examples include relative or absolute abundance indices, proportions-at-age frequencies, tag recapture observations, etc. Estimation uses the observations to find values for each of the estimated parameters so that each observation is ‘close’ (in some mathematical sense) to a corresponding expected value.

## **2.5. The report section**

The report section (Section 7) specifies the model outputs. It defines the quantities and model summaries to be output to external files or to the standard output. While CASAL2 will provide informational messages to the screen, CASAL2 will only produce model estimates, population states, and other data as requested by the report section. Note that if no reports are specified, then no output will be produced.



---

### 3. Running CASAL2

CASAL2 is run from the console window (i.e., the command line) on Microsoft Windows or from a terminal window on Linux. CASAL2 gets its information from input data files, the key one of which is the input configuration file.

The input configuration file is compulsory and defines the model structure, processes, observations, parameters (both the fixed parameters and the parameters to be estimated), and the reports (outputs) requested. The following sections describe how to construct the CASAL2 configuration file. By convention, the name of the input configuration file ends with the suffix `.cs12`, however, any file name is acceptable. Note that the input configuration file can ‘include’ other files as a part of its syntax. Collectively, these are called the input configuration file.

Other input files can, in some circumstances, be supplied, depending on what is required. For example, a file can be supplied that defines the starting point for estimation, as points from which to simulate observations, or as points from which to run projections.

Simple command line arguments are used to determine the actions or *tasks* of CASAL2, i.e., to run a model with a set of parameter values, estimate parameter values (either point estimates or MCMC), project quantities into the future, simulate observations, etc.,. Hence, the *command line arguments* define the *task*. For example, `-r` is the *run*, `-e` is the *estimation*, and `-m` is the *MCMC* task. The *command line arguments* are described in Section 3.4.

#### 3.1. Using CASAL2

To use CASAL2, open a console (i.e. the command prompt) window (Microsoft Windows) or a terminal window (Linux). Navigate to a directory of your choice, where your input configuration files are located. Then type `casal2` with any arguments (see Section 3.4 for the the list of possible arguments). CASAL2 will print output to the screen and return you to the command prompt when it completes its task. Note that the CASAL2 executable (binary) and shared libraries (extension `.dll`) must be either in the directory where you run it or in your systems `PATH`. The CASAL2 installer should update your path on Windows in any case, but see your operating system documentation for help on identifying or modifying your `PATH`.

#### 3.2. The input configuration file

The input configuration file is made up of four broad sections; the description of the population structure and parameters (the population section), the estimation methods and variables (the estimation section), the observations and their associated likelihoods (the observation section), and the outputs and reports that CASAL2 will return (the report section). The input configuration file is made up of a number of commands (many with subcommands) which specify various options for each of these components.

The command and subcommand definitions in the input configuration file can be extensive (especially when you have a model that has many observations), and can result in a input configuration file that is long and difficult to navigate. To aid readability and flexibility, we can use the input configuration file command `!include file`. The command causes an external file, *file*, to be read and processed, exactly as if its contents had been inserted in the main input configuration file at that point. The file name must be a complete file name with extension, but can use either a relative or absolute path as part of its name. Note that included files can also contain `!include` commands. See Section 12 for more detail.

### 3.3. Redirecting standard output

CASAL2 uses the standard output stream `standard output` to display run-time information. The standard error stream is used by CASAL2 to output the program exit status and run-time errors. We suggest redirecting both the standard output and standard error into files. With the bash shell (on Linux systems), you can do this using the command structure,

```
(casal2 [arguments] > out) >& err &
```

It may be useful to redirect the standard input, especially if you're using CASAL2 inside a batch job software, i.e.

```
(casal2 [arguments] > out < /dev/null) >& err &
```

On Microsoft Windows systems, you can redirect to standard output using,

```
casal2 [arguments] > out
```

And, on some Microsoft Windows systems (e.g., Windows10), you can redirect to both standard output and standard error, using the syntax,

```
casal2 [arguments] > out 2> err
```

Note that CASAL2 outputs a few lines of header information to the output. The header consists of the program name and version, the arguments passed to CASAL2 from the command line, the date and time that the program was called (derived from the system time), the user name, and the machine name (including the operating system and the process identification number). These can be used to track outputs as well as identifying the version of CASAL2 used to run the model.

### 3.4. Command line arguments

The call to CASAL2 is of the following form:

```
casal2[-c config-file] [task] [options]
```

**-c *config-file*** Define the input configuration file for CASAL2. If omitted, then CASAL2 looks for a file named `config.csl2`.

and where *task* is one of, if there are square brackets [] this indicates a secondary label to call the same task for example **-h** will execute the same task as **--help**;

**-h [--help]** Display help (this page).

**-l [--licence]** Display the reference for the software license (GPL v2).

**-v [--version]** Display the CASAL2 version number.

**-r [--run]** Run the model once using the parameter values in the input configuration file, or optionally, with the values from the file denoted with the command line argument **-i *file***.

**-e [--estimate]** Do a point *estimate* using the values in the input configuration file as the starting point for the parameters to be estimated, or optionally, with the start values from the file denoted with the command line argument **-i *file***.

- p** [**--profiling**] Do a likelihood *profile* using the parameter values in the input configuration file as the starting point, or optionally, with the start values from the file denoted with the command line argument **-i file**.
- m** [**--mcmc**] Do an *MCMC* estimate using the values in the input configuration file as the starting point for the parameters to be estimated, or optionally, with the start values from the file denoted with the command line argument **-i file**.
- f** [**--projection**] Project the model *forward* in time using the parameter values in the input configuration file as the starting point for the estimation, or optionally, with the start values from the file denoted with the command line argument **-i file**.
- s** [**--simulation**] *number* Simulate the *number* of observation sets using values in the input configuration file as the parameter values, or optionally, with the values for the parameters denoted as estimated from the file with the command line argument **-i file**.

In addition, the following are optional arguments [*options*],

- i** [**--input**] *file* Input one or more sets of free (estimated) parameter values from *file*. See Section 11 for details about the format of *file*.
- o** [**--output**] *file* Output a report of the free (estimated) parameter values in a format suitable for **-i file**. See Section 11 for details about the format of *file*.
- g** [**--seed**] *seed* Seed the random number *generator* with *seed*, a positive (long) integer value. Note, if **-g** is not specified, then CASAL2 will generate a random number seed based on the computer clock time.
- loglevel** *arg* = {trace, finest, fine, medium} See Section 7.
- tabular** Run with **-r** or **-f** command it will print @report in tabular format. See Section 7.
- single-step** Run with **-r**, this additional option will pause the model and ask the user to specify parameters and their values to use for the next iteration. See Section 3.6.
- q** [**--query**] Query an object type to see it's description and parameter definitions. This will print out an extract of the object. An object can be defined as block.type. For example `casal2 --query process.recruitment_constant`, will query the constant recruitment block.

### 3.5. Constructing a CASAL2 input configuration files

The model definition, parameters, observations, and reports are specified in an input configuration files. The population section is described in Section 4 and the population commands in Section 8. Similarly, the estimation section is described in Section 5 and its commands in Section 9, and in Section 7 and Section 11 for the report and report commands.

#### 3.5.1. Commands

CASAL2 has a range of commands that define the model structure, processes, observations, and how tasks are carried out. There are three types of commands,

1. Commands that have an argument and do not have subcommands (for example, `!include file`)
2. Commands that have a label and subcommands (for example @process must have a label, and has subcommands)

3. Commands that do not have either a label or argument, but have subcommands (for example `@model`)

Commands that have a label must have a unique label, i.e., the label cannot be used on more than one command of that type. The labels can contain alpha numeric characters, period ('.'), underscore ('\_') and dash ('-'). Labels must not contain white-space, or other characters that are not letters, numbers, dash, period or an underscore. For example,

```
@process NaturalMortality
or
!include MyModelSpecification.csl2
```

### 3.5.2. Subcommands

Subcommands in CASAL2 are for defining options and parameter values for commands. They always take an argument which is one of a specific *type*. The types acceptable for each subcommand are defined in Section 12, and are summarised below.

Like commands (`@command`), subcommands and their arguments are not order specific — except that that all subcommands of a given command must appear before the next `@command` block. CASAL2 may report an error if they are not supplied in this way, however, in some circumstances a different order may result in a valid, but unintended set of actions, leading to possible errors in your expected results.

The arguments for a subcommand are either:

<b>switch</b>	true/false
<b>integer</b>	an integer number,
<b>integer vector</b>	a vector of integer numbers,
<b>integer range</b>	a range of integer numbers separated by a colon (:), e.g. 1994:1996 is expanded to an integer vector of values 1994 1995 1996),
<b>constant</b>	a real number (i.e. double),
<b>constant vector</b>	a vector of real numbers (i.e. vector of doubles),
<b>estimable</b>	a real number that can be estimated (i.e. estimable double),
<b>estimable vector</b>	a vector of real numbers that can be estimated (i.e. vector of estimable doubles),
<b>string</b>	a categorical (string) value, or
<b>string vector</b>	a vector of categorical values.

Switches are parameters which are either true or false. Enter *true* as `true` or `t`, and *false* as `false` or `f`.

Integers must be entered as integers (i.e., if `year` is an integer then use 2008, not 2008.0)

Arguments of type integer vector, integer range, constant vector, estimable vector, or categorical vector contain one or more entries on a row, separated by white space (tabs or spaces).

*Estimable* parameters are those parameters that CASAL2 can estimate, if requested. If a particular parameter is not being estimated in a particular model run, then it acts as a constant. Within CASAL2 only estimable parameters can be estimated. And, you have to tell CASAL2 those that are to be estimated in any particular model. Estimable parameters that are being estimated within a particular model run are called the *estimated parameters*.

### 3.5.3. The command-block format

Each command-block either consists of a single command (starting with the symbol @) and, for most commands, a unique label or an argument. Each command is then followed by its subcommands and their arguments, e.g.,

```
@command, or
@command argument, or
@command label
```

and then

```
subcommand argument
subcommand argument
etc.,
```

Blank lines are ignored, as is extra white space (i.e., tabs and spaces) between arguments. But don't put extra white space before a @ character (which must also be the first character on the line), and make sure the file ends with a carriage return.

There is no need to mark the end of a command block. This is automatically recognized by either the end of the file, section, or the start of the next command block (which is marked by the @ on the first character of a line). Note, however, that the *!include* is the only exception to this rule. See Section 12) for details of the use of *!include*.

Note that in the input configuration file, commands, sub-commands, and arguments are not case sensitive. However, labels and variable values are case sensitive. Also note that if you are on a Linux system then external calls to files are case sensitive (i.e., when using *!include file*, the argument *file* will be case sensitive).

### 3.5.4. Commenting out lines

Text that follows a # on a line are considered to be comments and are ignored. If you want to remove a group of commands or subcommands using #, then comment out all lines in the block, not just the first line.

Alternatively, you can comment out an entire block or section by placing curly brackets around the text that you want to comment out. Put in a { as the first character on the line to start the comment block, then end it with }. All lines (including line breaks) between { and } inclusive are ignored.

```
# This is a comment and will be ignored
@process NaturalMortality
m 0.2
{
This block of code
is a comment and
will be ignored
}
```

### 3.5.5. Determining parameter names

When CASAL2 processes a input configuration file, it translates each command and each subcommand into a parameter with a unique name. For commands, this parameter name is simply

the command label. For subcommands, the parameter name format is either

`command[label].subcommand` if the command has a label, or

`command.subcommand` if the command has no label, or

`command[label].subcommand(i)` if the command has a label and the subcommand arguments are a vector, and we are accessing the  $i$ th element of that vector.

`command[label].subcommand(i:j)` if the command has a label, and the subcommand arguments are a vector, and we are accessing the elements from  $i$  to  $j$  (inclusive) of that vector.

The unique parameter name is used to reference the parameter when estimating, applying a penalty, projecting, time varying or applying a profile. For example, the parameter name of subcommand `m` of the command `@process` with the label `NaturalMortality` is

```
process[NaturalMortality].m
```

#### 3.6. Single stepping CASAL2

Single stepping in CASAL2 gives it the ability to write observations and ‘pause’ after each annual cycle during a run, and then wait and process user input of updated estimable parameters for the next year.

This can allow, for example, CASAL2 to be used for implementing models that require feedback management simulations or scenarios, for example for use in operational management procedures (OMPs). This can be automated using, for example, **R**, where CASAL2 may be controlled by **R** to update input harvest values (for examples, catches in a fisheries model) to evaluate a particular management strategy.

#### 3.7. CASAL2 exit status values

When CASAL2 completes its task successfully or errors out gracefully, it returns a single exit status value ‘completed’ to the standard output. Error messages will be printed to the console. If configuration errors are found, CASAL2 will print an error messages along with the associated files and line numbers where the errors were identified.



---

## 4. The population section

### 4.1. Introduction

The population section specifies the model structure, population dynamics, and other associated parameters. It describes the model structure (population structure), defines the population processes (e.g., recruitment, migration, and mortality), selectivities, and their parameters.

The population section consists of several components, including;

- The population structure;
- Model initialisation (i.e., the state of the partition at the start of the first year);
- The years over which the model runs (i.e., the start and end years of the model)
- The annual cycle (time-steps and processes that are applied in each time-step);
- The specifications and parameters of the population processes (i.e., processes that add, remove individuals to or from the partition, or shift numbers between ages and categories in the partition);
- Selectivities;
- Parameter values and their definitions;
- Derived quantities, required as parameters for some processes (e.g. Mature biomass to resolve any density dependent processes such as the spawner-recruit relationship, in a recruitment process).

### 4.2. Population structure

The basic structure of population section of a CASAL2 model is defined in terms of an annual cycle, time steps, states, and transitions.

The annual cycle defines what processes happen in each model year, and in what sequence. CASAL2 runs on an annual cycle rather than, for example, a 6-monthly cycle.)

Each year is split into one or more time steps, with at least one process occurring in each time step. Each time step can be thought of as representing a particular part of the calendar year, or you can just treat them as an abstract sequence of events. In every time step, there exists a mortality block, this is a group of consecutive mortality based processes, where individuals are removed from the partition. For more information on mortality blocks see Section 4.4 for more detail.

The state is the current status of the population, at any given time. The state can change one or more times in every time step of every year. The state object must contain sufficient information to figure out how the underlying population changes over time (given a model and a complete set of parameters).

There are a number of possible changes in the state, which are called transitions. These include processes that include recruitment, natural mortality, anthropogenic mortality, ageing, migration, tagging events, and maturation. Different processes may be useful for different models in different circumstances.

The division of the year into an arbitrary number of time steps allows the user to specify the exact order in which processes and observations occur throughout the year. The user needs to specify the time step in which each process occurs. If more than one process occurs in the same time step, they will be applied in the order specified in the `@time_step` block.

The key element of the state is the partition. This is a broadly applicable concept that can be used to describe many different kinds of population model. The partition is simply a breakdown of the total number of individuals in the current population into different categories. (Note that the partition records numbers of individuals, not biomass). The individuals are grouped into categories, for example, sex, maturity state, area, and species. However CASAL2 has no predefined categories, and these are defined by the user. This differs from CASAL (?) that has only pre-defined partition categories.

The resulting partition can be conceptualised as a matrix, where each row is represented by a category and the columns are the age classes, shown in Figure 4.1. Each row represents the number of individuals for that category in that age class.

The names of categories are user defined, and there must be at least one category defined for a model. The ages are defined as a sequence from  $age_{min}$  to  $age_{max}$ , with the last age optionally a plus group. In order to calculate biomass, the age-length relationship for each category must also be defined for an age based model (but could be defined as 'none'). An example of how this is specified for four categories based on sex and area is as follows,

```
@categories
format mature.sex
names spawn.male spawn.female nonspawn.male nonspawn.female
age_lengths male_AL female_AL male_AL female_AL
```

For an example of these ideas, consider a model of a fish population with a mature and non-spawning fishery. If we assume that the non-spawning fishery happens over most of the year (say 10 months) in the non-spawning area. The mature fish then migrate to the spawning area, where the spawning fishery operates. At the end of spawning, these fish, along with the recruits from the previous year, migrate back to the non-spawning area. The modeller decides that fish will be divided in the partition by age, sex, maturity, and area (spawning and non-spawning grounds). So the partition has 8 rows (2 sexes (mature or immature) 2 areas) and one column per age class.



**Figure 4.1: A visual representation of a partition**

So they define four time steps, labelled 1 through 4. Step 1 includes the non-spawning fishery. Step 2 includes the migration to the spawning area. Step 3 includes the spawning fishery. Step 4 includes recruitment and the migration back to the non-spawning area. (In fact, they could have used only 3 time steps, by using a single step in place of their steps 2 and 3. Because the default order of processes within a time step places migrations before fisheries, the processes would still have occurred in the right order.) There are other details to be sorted out, such as the proportion of natural mortality occurring in each time step and where observations occur, but this gives the basic idea.

This structure can be used to implement complex models, with intermingling of separate species and stocks, with complex migration patterns over multiple areas, and multiple sources of anthropogenic impact using different methods and covering different areas and times. However, we note that there is little point in using a complex structure to model a population when there are no observations to support that structure. In other words, use a structure for your model that is compatible with the data available. For information on how to define categories and using CASAL2's shorthand syntax see Section 13.3.

The model is run from an initial year up to the final(current) year. It can also be run past the final year to make projections — things that happen in the future — up to the final projection year.

An example, to specify a model with 2 categories (male and female) with ages 1-20 (with the last age a plus group) and an age-length relationship defined with the label `male_growth` and `female_growth`, then the `@model` example from above becomes,

```
@model
start_year
final_year
min_age 1
max_age 20
age_plus_group True
initialisation_phases iphase
time_steps step1 step2
```

### 4.3. The state object and the partition

The key component of the state object is the partition, a matrix that store numbers of individuals at age for each category. A category represents a group of individuals that have the same specific attributes, examples of such attributes include life histories and growth rates, etc. For example, categories may include labels such as:

- Sex (male or female);
- Area (any number of areas, named by the user);
- Maturity (immature or mature);
- Growth-path (any number of growth-paths);
- Tag (any number of tagging events);
- Species

A stock can be thought of as a population of individuals which recruits separately. See Section 4.11 for the treatment of maturity when it is not a category in the partition.

So, you need to tell CASAL2 the following:

- The minimum and maximum age classes in an age-based model.
- Whether there is an age-plus group.
- The names of all categories.

Age classes are always one year wide, except that the maximum age group can optionally be a plus group. Users need to choose the minimum and maximum age classes.

CASAL2 allows categories of the partition to exist for certain years of the model. This is added for computational efficiency, when models contain a large number of categories that do not persist

for all model years. Situations where this is beneficial is when a model contains a process that does a one off transition of fish from one category into another category in a subset of the model initialisation phases or years (for example, tagging events). Excluding categories for certain years can save a considerable amount of time as CASAL2 does not need to, for example, initialising empty categories or implement processes in time periods when they have no effect.

Another important component of the state object in CASAL2 are derived quantities. This includes quantities such as a mature biomass (for example, in fisheries models, the mid-spawning season biomasses of spawning fish, SSB) for either one or sum of more than one category. CASAL2 derives through the command `@derived_quantity`, and may be required in the specification of some processes (i.e., in fisheries models, a recruitment process that specifies a stock recruitment relationship requires the definition of a derived quantity that specifies the mid-season spawning stock biomass).

#### 4.4. Time sequences

The time sequence of the model is defined in the following parts;

- Annual cycle
- Initialisation
- Model run years
- Projection years

##### Annual cycle

The annual cycle is implemented as a set of processes that occur, in a user-defined order, within each year. Time-steps are used to break the annual cycle into separate components, and allow observations to be associated with different time periods and processes. Any number of processes can occur within each time-step, in any order (although there are limitations around mortality based processes - see Section 4.4) and can occur multiple times within each time-step. Note that time-steps are not implemented during the initialisation phases (effectively, there is only one time-step), and that the annual cycle in the initialisation phases can, optionally, be different from that which is applied during the model years.

##### Mortality blocks

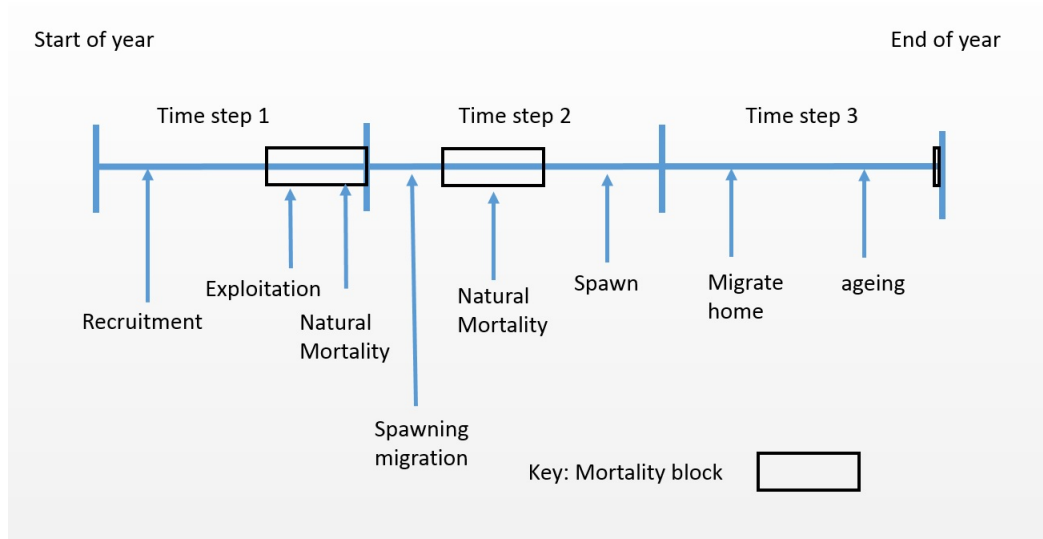
For every time step in an annual cycle there is an associated *mortality block*. Mortality blocks are a key concept in CASAL2.

Mortality blocks are used to define the ‘point’ in the model time sequence when observations (see Section 6) are evaluated, and derived quantities (see Section 4.8) are calculated.

A mortality block is defined as a consecutive sequence of mortality processes within a time step. The processes that are mortality processes are all pre-defined in CASAL2, and cannot be modified. These include all the processes described in subsection 4.7.3.

CASAL2 requires that each time step has exactly one mortality block. To achieve this, either all the mortality processes in a time step must be sequential (i.e., there can not be a non-mortality process between any two mortality processes within any one time step); or if no mortality processes occur in a time step then the mortality block is defined to occur at the end of the time step.

CASAL2 will error out if more than one mortality block occurs in a single time step.



**Figure 4.2: A visual representation of a hypothetical sequence for an annual cycle.**

#### 4.4.1. Initialisation

Initialisation is the process of determining the model equilibrium starting state, or some other initial state for the model, prior to the start year of the model.

There are multiple methods to initialise a partition in CASAL2. These methods are: iterative, fixed, derived, and Cinitial.

Model initialisation can also occur in several phases, each of which can be a different method. These are carried out in sequence. At the end of all of the initialisations, CASAL2 then runs the model years carrying out processes in each time step in the annual cycle.

The multi-phased initialisation allows the user to choose a number of initialisations that may assist with optimising the models for speed, initialise a non-equilibrium starting state, or resolve simple processes before introducing more complex ones.

Each phase of the initialisation can involve any number of processes.

In each initialisation phase, the processes defined for that phase are carried out and used as the starting point for the following phase or, if it is the last phase, then the years that the model is run over.

Note that the *first* initialisation phase is always initialised with each element (i.e., each age and category) set at zero. Note that you may need to be careful when using complex category inter-relationships or density dependent processes that depend on a previously calculated state, as they may fail when used in the first phase of an initialisation.

Multi-phase iterations can also be used to determine if the initialisation has converged. Here, add a second initialisation phase for, say, 1 year (with the same processes applied). Then report the state at the end of the first and second phase. If these states are identical, then its likely that the initialisation has converged to an equilibrium state.

### Iterative Initialisation

The iterative initialisation is a general solution for initialising the model. The iterative method can be slow to converge, depending on the nature of the problem being resolved, but will work on even complex structured models that may be difficult or impossible to implement using analytic approximations.

The number of iterations in the iterative initialisation can effect the model output, and these should be chosen to be large enough to allow the population state to fully converge. We recommend that a period of about two generations to ensure convergence. CASAL2 can be requested to report a number of convergence statistics that can assist the user determine the level of convergence.

In addition, the iterative initialisation phase can optionally be stopped early if some user defined convergence criteria is met. For list of supplied years in the initialisation phase, convergence is defined as met if the proportional absolute summed difference between the state in year  $t - 1$  and the state in year  $t$  ( $\hat{\lambda}$ ) is less than a user defined  $\lambda$  where,

$$\hat{\lambda} = \frac{\sum_i \sum_j |\text{element}(i, j)_t - \text{element}(i, j)_{t-1}|}{\sum_i \sum_j \text{element}(i, j)_t} \quad (4.1)$$

Hence, for an iterative initialisation you need to define;

- The initialisation phases.
- The number of years in each phase and the processes to apply in each (default is the annual cycle).

### Derived Initialisation

Derived initialisation is an analytical solution that calculates the equilibrium age structure and the plus group using a geometric series solution. The benefit of this method is it can be solved in  $\text{max\_age} - \text{min\_age} + 1$  years, so is computationally faster than the iterative initialisation phase. Users should be warned that we have found under some process combinations (for example. one way migrations) that this solution does not reach the exact equilibrium partition. We note that if using this method, that users confirm the partition has reached an equilibrium state by either comparing with and iterative initialisation, or by adding a second iterative initialisation phase of a limited number of iterations to confirm convergence.

### Cinital Initialisation

This initialisation is only available as a second or greater phase initialisation, and can only be applied after derived or iterative initialisation phases. The Cinital factors that can be estimated to shift the initial population away from an equilibrium state prior to start year. If there is known exploitation before data exists for a population this can be a solution for estimating a non equilibrium population. Note that it may be advisable to include an observation of age composition data for the first year of the model in order to estimate the non equilibrium population state.

### Fixed Initialisation

This is a user defined table that is taken to be the initial partition prior to the start year. Users have the ability to initialise models by specify the numbers at age for each category.

## 4.5. Model run years

Following initialisation, the model then runs over a number of user-defined years from (`initial_year` to `final_year`). For this part of the model, the annual cycle can be broken into separate time-steps, and observations can be associated with the state of the model at the end of any time-step, i.e., likelihoods for particular observations are evaluated, if required, within each time-step.

Processes are carried out in the order specified within each time-step. These can be the same or different to the processes in initialisation phases of the model.

The run years define the years over which the model is to run and the annual cycle within each year. The model runs from the start of year `initial` and runs to the end of year `current`. The projection part then extends the run time up to the end of year `final`.

- The time-steps and the processes applied in each
- The initial year (i.e., the model start year)
- The final year (i.e., the model end year)
- The projection final year (i.e., the model projection end year)

## 4.6. Projection years

Projecting is the process of running the model forwards into the future, using stochastic and or deterministic values for population dynamic parameters, such as recruitments and catches.

Projection years occur immediately after the model run years.

In a projection run in CASAL2 a model is initialised and run through the model years from `initial` to the `final`. Then, the model is re-run from `initial` to `projection_final_year`, where any parameter can be either fixed or, if specified, drawn from a stochastic distribution or process during that time period.

CASAL2 does not have any default projections for when parameters are specified by year. These must be specified using the `@project` command blocks. This is important for parameters that may vary from year to year (such as year class strength parameters).

CASAL2 allows any estimable parameter to be specified in a `@project` block and then used in a projection. The available projection types for these parameters include constant, lognormal, empirical-lognormal, or empirical re-sampling.

### Constant

A parameter can either be fixed during all projection years or specified individually for each projection year. This is a deterministic assumption, where the parameter is assumed to be known without error in each future year.

### Empirical resampling

Parameters that are of type vector or map can be re-sampled with replacement over a range of years and used as the projected year values.

**Lognormal**

The randomised parameters are sampled from a lognormal distribution with mean one and the specified standard deviation and autocorrelation on the log-scale. For example, when projecting year class strengths as a lognormal, they are generated as a Gaussian process with standard deviation  $\sigma_R$  and mean  $-0.5 \sigma_R$  (so that the mean of the parameter will be 1). If the randomised parameter is modified by the optional multiplier, then the parameter will have mean  $\mu$ , where  $\mu$  is the multiplier.

**4.7. Population processes**

Population processes are those processes that change the model state. Processes produce changes in the model partition, by adding, removing or moving individuals between ages and/or categories. The population processes include recruitment, ageing, mortality events (e.g., natural and anthropogenic) and category transition processes (i.e., processes that move individuals between categories while preserving their age structure). See Section 4 for a complete list of available processes.

There are two types of processes, processes that occur across multiple time steps in the annual cycle e.g Natural Mortality and Instantaneous Mortality. There are also processes that only occur within the time step they are defined. Each of these processes is carried out in the user-defined prescribed order when initialising the model, and then for a user-defined order in each year in the annual cycle.

**4.7.1. Recruitment**

Recruitment processes are defined as a process that introduces new individuals into the model. CASAL2 currently implements two types of recruitment process, constant recruitment and Beverton-Holt recruitment (?).

In the recruitment processes, the number of individuals are added to a single age class within the partition, with the amount defined by the type of recruitment process and its function. If more than one category is defined, then the proportion of recruiting individuals to be added to each category is specified by the `proportions` parameter. For example, if recruiting to categories labelled male and female, then you might set the proportions as 0.5 and 0.5 respectively to denote that half of the recruits recruit to the male category and the remaining half to the female category.

For the constant and Beverton-Holt recruitment processes, the number of individuals following recruitment in year  $y$  is,

$$N_{i,j} \leftarrow N_{i,j} + p_j(R_y) \quad (4.2)$$

where  $N_{i,j}$  is the numbers in category  $j$  at age  $i$ ,  $p_j$  is the proportion to category  $j$ , and  $R_y$  is the number of recruits for year  $y$ . See below for how  $R_y$  is determined in each of these cases.

**Constant Recruitment**

In the constant recruitment process the total number of recruits added each year is  $R_y$ , and is simply  $R_0$ , i.e.

$$R_y = R_0 \quad (4.3)$$

Constant recruitment recruits a constant number of individuals each year. It is equivalent to a Beverton-Holt recruitment process with steepness set equal to one (i.e.,  $h = 1$ ).



For example, to specify a constant recruitment process, where individuals are added to male and female immature categories at  $age = 1$ , and the number to add is  $R_0 = 5 \times 10^5$ , then the syntax is

```
@process Recruitment
type constant_recruitment
categories male.immature female.immature
proportions 0.5 0.5
r0 500000
age 1
```

### Beverton-Holt recruitment

In the Beverton-Holt recruitment process the total number of recruits added each year is  $R_y$ , and is the product of the average recruitment  $R_0$ , the annual year class strength multiplier,  $YCS$ , and the stock-recruit relationship i.e.,

$$R_y = R_0 \times YCS_{y-ssb\_offset} \times SR(SSB_{y-ssb\_offset}) \quad (4.4)$$

where  $ssb\_offset$  is the number of years offset to link the year class with the year of spawning  $y$ , and  $SR$  is the Beverton-Holt stock-recruit relationship parametrised by the steepness  $h$ ,

$$SR(SSB_y) = \frac{SSB_y}{B_0} / \left( 1 - \frac{5h-1}{4h} \left( 1 - \frac{SSB_y}{B_0} \right) \right) \quad (4.5)$$

Note that the Beverton-Holt recruitment process requires a value for  $B_0$  and  $SSB_y$  to resolve the stock-recruitment relationship. Here, a derived quantity (see Section 4.8) must be defined that provides the annual  $SSB_y$  for the recruitment process.  $B_0$  is then defined as the value of the  $SSB$  at the end of one of the initialisation phases. During initialisation the  $YCS$  multipliers are assumed to be equal to one, and recruitment that happens in the initialisation phases that occur before and during the phase when  $B_0$  is determined is assumed to have steepness  $h = 1$  (i.e. in those initialisation phases, recruitment is simply equal to  $R_0$ ). Recruitment in the initialisation phases after the phase where  $B_0$  was determined follow the Beverton-Holt stock-recruit relationship defined above.  $R_0$  and  $B_0$  have a direct relationship when there are no density dependent processes, for this reason users can choose to initialise models using  $B_0$  or  $R_0$ . In New Zealand  $B_0$  is often used, as biological reference points for managing marine populations is based on a percentage of  $B_0$ .

Year classes are standardised to be equal to one over the period  $S$  defined by standardise  $YCS$  years, i.e., the year classes ( $YCS$ ) for each year of the model are calculated as

$$YCS_i = \begin{cases} Y_i / \text{mean}_{y \in S} & : y \in S \\ Y_i & : y \notin S \end{cases}$$

Note that the an effect of this parameterisation is that  $R_0$  is then defined as the mean estimated recruitment over the years  $S$ , because the mean year class multiplier over these years will always be one.

For example, assume a Beverton-Holt recruitment process, where individuals are added to the category ‘immature’ at  $age = 1$ , the number to add is  $R_0 = 5 \times 10^5$ . Then `SSB_derived_quantity` is a derived quantity that specifies the total spawning stock biomass, with  $B_0$  the value of the derived quantity at the end of the initialisation phase labelled `phase1`. The  $YCS$  are standardised to have mean one in the period 1994 to 2004, and recruits enter into the model two years following spawning. Then the command specification would be,

```
@process Recruitment
type recruitment_beverton_holt
categories immature
proportions 1.0
r0 500000
b0_initialisation_phase phase1
steepness 0.75
age 1
ssb SSB_derived_quantity
standardise_ycs_years 1994-2004
ycs_years 1994 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006
YCS_values 1 1 1 1 1 1 1 1 1 1 1 1 1
```

Note that the SSB year used in the Beverton-Holt stock recruitment relationship (`ssb_offset`) is determined by the order of ageing, recruitment, and spawning,

- If recruitment then ageing then spawning, then `ssb_offset` should equal `min_age + 1`.
- If spawning then ageing then recruitment, then `ssb_offset` should equal `min_age - 1`.

If any other order is used, then `ssb_offset` should equal `min_age`.

If you have more than one ageing process and a Beverton-Holt recruitment process you will be warned to set your own `ssb_offset` as CASAL2 will, by default, set it based upon the first ageing process in the annual cycle — which may be not be what was desired.

#### 4.7.2. Ageing

The ageing process ‘ages’ individuals — it simply moves all individuals in the named categories  $i$  to the next age class  $j + 1$ , or accumulates them if the last age class is a plus group.

The ageing process is defined as,

$$\text{element}(i, j) \leftarrow \text{element}(i, j - 1) \quad (4.6)$$

except that in the case of the plus group (if defined),

$$\text{element}(i, \text{age}_{\max}) \leftarrow \text{element}(i, \text{age}_{\max}) + \text{element}(i, \text{age}_{\max} - 1). \quad (4.7)$$

For example, to apply ageing to the categories `immature` and `mature`, then the syntax is,

```
@process Ageing
type ageing
categories immature mature
```

Note that ageing is *not* applied by CASAL2 by default. As with other processes, CASAL2 will not apply a process unless its defined and specified as a process within the annual cycle. Hence, it is possible to specify a model where a category is not aged. CASAL2 will not check or otherwise warn if there is a category defined where ageing is not applied.

#### 4.7.3. Mortality

Four types of mortality processes are permissible in CASAL2, constant rate, event, biomass-event and instantaneous. These processes remove individuals from the partition, either as a rate, as a

total number (abundance), as a biomass of individuals or as a mixture of these. Note that CASAL2 does not (yet) implement the Baranov catch equation. To apply both natural and biomass-event mortality, users can use `mortality_instantaneous`. Note that all mortality processes occur within a mortality block of a time step

#### 4.7.3.1. Constant mortality rate

To specify a constant annual mortality rate ( $M = 0.2$ ) for categories ‘male’ and ‘female’, then,

```
@process NaturalMortality
type mortality_constant_rate
categories male female
selectivities One One
m 0.2 0.2
```

$$D_{j,t} = \sum_a N_{a,j} (1 - \exp S_{a,j} M_j p_t) \quad (4.8)$$

Where,  $D_{j,t}$  is the number of deaths in category  $j$  in time step  $t$ ,  $N_{a,j}$  is the number of individuals in category  $j$  at age  $a$ .  $S_{a,j}$  is the selectivity value for age  $a$  in category  $j$ ,  $M_j$  is the mortality rate for category  $j$ , and  $p_t$  is the proportion of the mortality rate to apply in time step  $t$ .

Note that the mortality rate process requires a selectivity. To apply the same mortality rate over all age classes, use a selectivity defined as  $S_j = 1.0$  for all ages  $j$ , e.g.,

```
@selectivity One
type constant
c 1
```

#### 4.7.3.2. Event and biomass-event mortality

The event mortality process and biomass mortality processes act in a similar manner, except that they remove a specified abundance (number of individuals) or biomass respectively. These can be used to include anthropogenic mortality where numbers of removals are known, for example, fishing in a fisheries model, rather than applying mortality as a rate.

In these cases, the abundance or biomass removed is also constrained by a maximum exploitation rate. CASAL2 removes as many individuals or as much biomass as it can while not exceeding the maximum exploitation rate. When minimising, event mortality processes require a penalty to discourage parameter values that do not allow the defined number of individuals to be removed. Here, the model penalises those parameter estimates that result in an too low a number of individuals in the defined categories (after applying selectivities) to allow for removals at the maximum exploitation rate. See Section 5.8 for more information on how to specify penalties.

For example, the event mortality applied to user-defined categories  $i$ , with the numbers removed at age  $j$  determined by a selectivity-at-age  $S_j$  is applied as follows:

First, calculate the vulnerable abundance for each category  $i$  in  $1 \dots I$  for ages  $j = 1 \dots J$  that are subject to event mortality,

$$V(i, j) = S(j)N(i, j) \quad (4.9)$$

And hence define the total vulnerable abundance  $V_{total}$  as,

$$V_{total} = \sum_i \sum_j V(i, j) \quad (4.10)$$

Hence the exploitation rate to apply is

$$U = \begin{cases} C/V_{total}, & \text{if } C/V_{total} \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \quad (4.11)$$

And the number removed  $R$  from each age  $j$  in category  $i$  is,

$$R(i, j) = UV(i, j) \quad (4.12)$$

For example, to specify fishing mortality in a fisheries model, with catches given for a set of specific years, over categories ‘immature’ and ‘mature’, with selectivity ‘FishingSel’ and assuming a maximum possible exploitation rate of 0.7, then the syntax would be,

```
@process Fishing
type event_mortality
categories immature mature
years 2000 2001 2002 2003
U_max 0.70
selectivities FishingSel FishingSel
penalty event_mortality_penalty
```

#### 4.7.3.3. Instantaneous mortality

The instantaneous mortality process is a process that combines both natural mortality and event biomass mortality into a single process. This allows the natural mortality to occur across multiple time steps, and can specify multiple instances of event mortality to account for, say, multiple fisheries operating sequentially or concurrently. This process applies half the natural mortality in each time step, then the mortalities from all the concurrent fisheries instantaneously, then the remaining half of the natural mortality.

When instantaneous mortality is applied the following equations are used.

- An exploitation rate (actually a proportion) is calculated for each fishery, as the catch over the selected-and-retained biomass,

$$U_f = \frac{C_f}{\sum_j \bar{w}_j S_{f,j} n_j e^{-0.5tM_j}}$$

- The fishing pressure associated with fishery  $f$  is defined as the maximum proportion of fish taken from any element of the partition in the area affected by fishery  $f$ ,

$$U_{f,obs} = \max_j \left( \sum_k S_{k,j} U_k \right)$$

where the maximum is over all partition elements affected by fishery  $f$ , and the summation is over all fisheries  $k$  which affect the  $j$ th partition element in the same time step as fishery  $f$ .

In most cases the fishing pressure will be equal to the exploitation rate (i.e.,  $U_{f,obs} = U_f$ ), but they can be different if (a) there is another fishery operating in the same time step as fishery

$f$  and affecting some of the same partition elements, and/or (b) the selectivity  $S_{f,j}$  does not have a maximum value of 1.

There is a maximum fishing pressure limit of  $U_{f,max}$  for each fishery  $f$ . So, no more than proportion  $U_{f,max}$  can be taken from any element of the partition affected by fishery  $f$  in that time step. Clearly  $0 \leq U_{max} \leq 1$ . It is an error if two fisheries which affect the same partition elements in the same time step do not have the same  $U_{max}$ .

For each  $f$ , if  $U_{f,obs} > U_{f,max}$ , then  $U_f$  is multiplied by  $U_{f,max}/U_{f,obs}$  and the fishing pressures are recalculated. In this case the catch actually taken from the population in the model will differ from the specified catch,  $C_f$ .

- The partition is updated using

$$n'_j = n_j \exp(-tM_j) \left[ 1 - \sum_f S_{f,j} U_f \right]$$

An example of the syntax is if we want to apply natural mortality of 0.20 across three time steps on both male and female categories. And we have two method of removals (fisheries) `FishingWest` `FishingEast` with there respective catches known for years 1975:1977 in kilograms. These are given in the `catches` table and information on selectivities, penalties and maximum exploitation rates are given in the `fisheries` table.

```
@process instant_mort
type mortality_instantaneous
m 0.20
time_step_ratio 0.42 0.25 0.33
selectivities One
categories male female
units kgs

table catches
year FishingWest FishingEast
1975 80000 111000
1976 152000 336000
1977 74000 1214000
end table

table method
method      category  selectivity u_max  time_step penalty
FishingWest  stock      westFSel   0.7   step1    CatchPenalty
FishingEast  stock      eastFSel   0.7   step1    CatchPenalty
end_table
```

#### 4.7.3.4. Hollings mortality rate

The density-dependent Holling mortality process applies the Holling Type II and Type III functions (?), but is generalised using the Michaelis-Menten equation (?). The function removes a number or biomass from a set of categories according to their total (selected) abundance (or biomass) and some 'predator' abundance (or biomass), but constrained by a maximum exploitation rate.

For example, the mortality applied to user-defined categories  $k$ , with the numbers removed at age  $l$  determined by a selectivity-at-age  $S(l)$  is applied as follows:

First, calculate the total predator abundance (or biomass) over all predator categories  $k$  in  $1 \dots K$  and ages  $l = 1 \dots L$  that are applying the mortality,

$$P(k, l) = S_{predator}(l) N_{predator}(k, l) \quad (4.13)$$

And define the total predator abundance (or biomass)  $P_{total}$  as,

$$P_{total} = \sum_K \sum_L P(k, l) \quad (4.14)$$

Then, calculate the total vulnerable abundance (or biomass) over all prey categories  $k$  in  $1 \dots K$  and ages  $l = 1 \dots L$  that are subject to the mortality,

$$V(k, l) = S_{prey}(l) N_{prey}(k, l) \quad (4.15)$$

And hence define the total vulnerable abundance (or biomass)  $V_{total}$  as,

$$V_{total} = \sum_K \sum_L V(k, l) \quad (4.16)$$

and then, the the number to remove is determined as,

$$R_{total} = P_{total} \frac{a V_{total}^{x-1}}{b + V_{total}^{x-1}} \quad (4.17)$$

where  $x = 2$  for Holling type II function,  $x = 3$  for Holling type III function, or any value of  $x \geq 1$  for the generalised Michaelis-Menten function, and  $a > 0$  and  $b > 0$  are the Holling function parameters.

Hence the exploitation rate to apply is

$$U = \begin{cases} R_{total}/V_{total}, & \text{if } R_{total}/V_{total} \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \quad (4.18)$$

And the number removed  $R$  from each age  $l$  in category  $k$  is,

$$R(k, l) = UV(k, l) \quad (4.19)$$

The density-dependent Holling mortality process is applied either as a biomass or an abundance depending on the value of the `is_abundance` switch.

For example, a biomass Holling type II mortality process on prey by our predator `predator` would have syntax,

```
@process HollingMortality
type Holling_mortality_rate
is_abundance F
a 0.08
b 10000
x 2
categories prey
selectivities One
predator_categories predator
predator_selectivities One
u_max 0.8
```

#### 4.7.4. Transition By Category

This process covers moves individuals between categories. Because the CASAL2 partition user defined, this type of process is used to move individuals between categorised, and is used to specify processes such as maturation (move individuals from an immature to mature state) or migration (move individuals from one area to another).

#### 4.7.4.1. Annual transition by category

A special case is annual transition by category, which allows a transition to occur in a specific subset of years only, where each year can have a different rate.

In both cases, there has to be a one to one relationship between the ‘from’ category and the ‘to’ category — for every source category there is one target category. If however, you want to merge categories, then just repeat the ‘to’ category multiple times.

$$N_{a,j} = N_{a,i} \times P_i \times S_{a,i} \quad (4.20)$$

where  $N_{a,j}$  is the number of individuals that have moved to category  $j$  from category  $i$  in age  $a$  and  $N_{a,i}$  is the number of individuals in category  $i$ .  $P_i$  is the proportion parameter for category  $i$  and  $S_{a,i}$  is the selectivity at age  $a$  for category  $i$ .

An example, to specify a simple spawning migration of mature males from a western area migrating to an eastern (spawning) area, then the syntax is

```
@process Spawning_migration
type category_transition
from West.males
to East.males
selectivities MatureSel
proportions 1
```

Where `MatureSel` is a selectivity that describes the proportion of age or length classes that are mature and thus move to the eastern area.

#### 4.7.5. Tag Release events

Tagging processes can be age or length based processes, where by numbers of fished are moved from an untagged category to a tagged category that the user has defined in the `@Categories` block. Tag release processes can also account for tag induced mortality on individuals. Age based tag release events take a known number of individuals tagged for each age and do a straightforward category transition along with extra mortality. Length based tag release processes are more complicated, as CASAL2 needs to calculate the age length matrix and exploitation by each length to then move the correct numbers at age based on a length input.

#### 4.7.6. Tag Loss

Tag Loss is the process where tags are lost from tagged categories over time from tag failure or getting knocked off. This process is applied as a instantaneous mortality rate that can happen over multiple time steps in the annual cycle. This method assumes when tags are lost that the fish is removed from the partition. All though this seems logically incorrect, we are dealing with such a small number of fish that the impact is minimal and computationally simpler. Note that if your tagging events make up a large proportion of the population you may want to adjust this method. There will be two types of tag loss processes that are termed `single` and `double`. Currently only `single` exists in CASAL2. `double` will deal with situations where a tag release process tags individuals with two tags. In which there is another formulae to work out the rate of tag loss.

```
@process Tag_loss
type tag_loss
categories tagged_fish
tag_loss_rate 0.02
time_step_ratio 0.25 0.75
selectivities One
tag_loss_type single
year 1985
```

#### 4.8. Derived quantities

Some processes require, as arguments, a population value derived from the population state. These are termed derived quantities. Derived quantities are values, calculated by CASAL2 at the end of a specified time-step in every year, and hence they have a single value for each year of the model. Derived quantities can be calculated as either an abundance or as a biomass. Abundance derived quantities are simply the count or sum of categories (after applying a selectivity). Biomass derived quantities are similar, except they are a measure of biomass. Derived quantities are also calculated during the initialisation phases, and hence the time-step during each phase must also be specified. If the initialisation time-steps are not specified, CASAL2 will calculate the derived quantity during the initialisation phases in every year, at the end of the annual cycle.

Derived quantities are required by some processes, for example the Beverton-Holt recruitment process. The Beverton-Holt recruitment process can require an equilibrium biomass ( $B_0$ ) and annual spawning stock biomass values ( $SSB_y$ ) to resolve the stock-recruit relationship. Here, these would be defined as the abundance or biomass of a part of the population at some point in the annual cycle for selected ages and categories, and would be calculated as a derived quantity.

Derived quantities are associated with a mortality block see section 4.4 for more detail on mortality blocks. Users can ask for derived quantities partway through mortality blocks. Currently two methods are implemented in CASAL2 to interpolate derived quantities part-way through a mortality block, these are `weighted_sum` and `weighted_product`, they are defined as,

- `weighted_sum`: after proportion  $p$  of the mortality block, the partition elements are given by  $n_{p,j} = (1 - p)n_j + p'n'_j$
- `weighted_product`: after proportion  $p$  of the mortality block, the partition elements are given by  $n_{p,j} = n_j^{1-p} n_j'^p$

where,  $n_{p,j}$  is the derived quantity at proportion  $p$  of the mortality block for category  $j$ .  $n_j$  is the quantity at the beginning of the mortality block and  $n'_j$  is the quantity at the end of the mortality block.

As an example, to define a biomass derived quantity (say spawning stock biomass, SSB) for a model, evaluated at the end of the first time-step (labelled `step_one`), over all 'mature' male and female categories and halfway through the mortality block using the `weighted_sum` method, we would use the syntax,

```
@derived_quantity SSB
type biomass
time_step step_one
categories mature.male mature.female
selectivities One
time_step_proportion 0.5
time_step_proportion_method weighted_sum
```



#### 4.9. Age-length relationship

The age-length relationship defines the length at age (and the weight at length, see Section 4.9) of individuals at age/category within the model. There are three length-age relationships available in CASAL2. The first is the naive no relationship (where each individual has length 1 irrespective of age). The second and third are the von-Bertalanffy and Schnute relationships respectively. The length-at-age relationship is used to determine the length frequency, given age, and then with the length-weight relationship, a weight-at-age of individuals within an age/category.

The three age-length relationships are,

None: where the length of each individual is exactly 1 for all ages, in which case the none length-weight relationship must also be used.

von Bertalanffy: where length at age is defined as,

$$\bar{s}(age) = L_{\infty} (1 - \exp(-k(age - t_0))) \quad (4.21)$$

Schnute: where length at age is defined as,

$$\bar{s}(age) = \begin{cases} \left[ y_1^b + (y_2^b - y_1^b) \frac{1 - \exp(-a(age - \tau_1))}{1 - \exp(-a(\tau_2 - \tau_1))} \right]^{1/b}, & \text{if } a \neq 0 \text{ and } b \neq 0 \\ y_1 \exp \left[ \ln(y_2/y_1) \frac{1 - \exp(-a(age - \tau_1))}{1 - \exp(-a(\tau_2 - \tau_1))} \right], & \text{if } a \neq 0 \text{ and } b = 0 \\ \left[ y_1^b + (y_2^b - y_1^b) \frac{age - \tau_1}{\tau_2 - \tau_1} \right]^{1/b}, & \text{if } a = 0 \text{ and } b \neq 0 \\ y_1 \exp \left[ \ln(y_2/y_1) \frac{age - \tau_1}{\tau_2 - \tau_1} \right], & \text{if } a = 0 \text{ and } b = 0 \end{cases} \quad (4.22)$$

The von Bertalanffy curve is parameterised by  $L_{\infty}$ ,  $k$ , and  $t_0$ ; the Schnute curve (?) by  $y_1$  and  $y_2$ , which are the mean lengths at reference ages  $\tau_1$  and  $\tau_2$ , and  $a$  and  $b$  (when  $b = 1$ , this reduces to the von Bertalanffy with  $k = a$ ).

When defining length-at-age in CASAL2, you must also define a length-weight relationship (see Section 4.9 below).

#### Calculation of length-at-age (in an age-based model)

##### Interpolation of length-at-age

##### Size-weight relationship

There are two length-weight relationships available in CASAL2. The first is the naive no relationship. Here, the weight of an individual, regardless of length, is always 1. The second is the basic relationship.

The two length-weight relationships are,

- None: The length-weight relationship where

$$\text{mean weight} = 1 \quad (4.23)$$

- Basic: The length-weight relationship where the mean weight  $w$  of an individual of length  $l$  is

$$w = al^b \quad (4.24)$$

Note that if a distribution of length-at-age is specified, then the mean weight is calculated over the distribution of lengths, and is

$$w = (al^b)(1 + cv^2)^{\frac{b(b-1)}{2}} \quad (4.25)$$

where the  $cv$  is the c.v. of lengths-at-age. This adjustment is exact for lognormal distributions, and a close approximation for normal distributions if the c.v. is not large (?).

Be careful about the scale of  $a$  — this can easily be specified incorrectly. If the catch is in tonnes and the growth curve in centimetres, then  $a$  should be on the right scale to convert a length in centimetres to a weight in tonnes. Note that there are reports available that can be used to help check that the units specified are plausible (see Section 7).

## Calculation of mean weight

### 4.10. Weightless model

### 4.11. Maturity, in models without maturing in the partition

If maturity is not a character of the partition it can easily be derived at an instance in time using selectivities. Applying a maturity selectivity on to the partition allows CASAL2 to use mature elements in processes, derive mature biomasses estimates (using derived quantities), and report the mature partition as an output.

### 4.12. Selectivities

A selectivity is a function that can have a different value for each age class. Selectivities are used throughout CASAL2 to interpret observations (Section 5) or to modify the effects of processes on each age class (Section 4). CASAL2 implements a number of different parametric forms, including logistic, knife edge, and double normal selectivities. Selectivities are defined in there own command block (@selectivity), where the unique label is used by observations or processes to identify which selectivity to apply.

Selectivities are indexed by age, with indices from `min_age` to `max_age`. For example, you might have an age-based selectivity that was logistic with 50% selected at age 5 and 95% selected at age 7. This would be defined by the `type=logistic` with parameters  $a_{50} = 5$  and  $a_{0.95} = (7 - 5) = 2$ . Then the value of the selectivity at age  $x = 7$  is 0.95 and the selectivity at  $x = 3$  is 0.05. Note selectivities can be length based, However Caution, more testing is needed for this functionality.

Note that the function values for some choices of parameters for some selectivities can result in a computer numeric overflow error (i.e., the number calculated from parameter values is either too large or too small to be represented in computer memory). CASAL2 implements range checks on some parameters to test for a possible numeric overflow error before attempting to calculate function values. For example, the logistic selectivity is implemented such that if  $(a_{50} - x)/a_{0.95} > 5$  then the value of the selectivity at  $x = 0$ , i.e., for  $a_{50} = 5$ ,  $a_{0.95} = 0.1$ , then the value of the selectivity at  $x = 1$ , without range checking would be  $7.1 \times 10^{-52}$ . With range checking, that value is 0 (as  $(a_{50}x)/a_{0.95} = 40 > 5$ ).

The available selectivities are;

- Constant
- Knife-edge
- All values
- All values bounded
- Increasing
- Logistic
- Inverse logistic
- Logistic producing
- Double normal
- Double exponential
- Cubic spline (Not yet implemented)

The available selectivities are described below.

#### 4.12.1. **constant**

$$f(x) = C \tag{4.26}$$

The constant selectivity has the estimable parameter C.

#### 4.12.2. **knife\_edge**

$$f(x) = \begin{cases} 0, & \text{if } x < E \\ \alpha, & \text{if } x \geq E \end{cases} \tag{4.27}$$

The knife-edge ogive has the estimable parameter E and a scaling parameter  $\alpha$ , where the default value of  $\alpha = 1$

#### 4.12.3. **all\_values**

$$f(x) = V_x \tag{4.28}$$

The all-values selectivity has estimable parameters  $V_{low}, V_{low+1} \dots V_{high}$ . Here, you need to provide the selectivity value for each age class.

#### 4.12.4. **all\_values\_bounded**

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ V_x, & \text{if } L \leq x \leq H \\ V_H, & \text{if } x > H \end{cases} \tag{4.29}$$

The all-values-bounded selectivity has non-estimable parameters L and H. The estimable parameters are  $V_L, V_{L+1} \dots V_H$ . Here, you need to provide an selectivity value for each age class from  $L \dots H$ .

**4.12.5. increasing**

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ f(x-1) + \pi_x(\alpha - f(x-1)), & \text{if } L \leq x \leq H \\ f(\alpha), & \text{if } x \geq H \end{cases} \quad (4.30)$$

The increasing ogive has non-estimable parameters  $L$  and  $H$ . The estimable parameters are  $\pi_L, \pi_{L+1} \dots \pi_H$  (but if these are estimated, they should always be constrained to be between 0 and 1).  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . Note that the increasing ogive is similar to the all-values-bounded ogive, but is constrained to be non-decreasing.

**4.12.6. logistic**

$$f(x) = \alpha / [1 + 19^{(a_{50}-x)/a_{t095}}] \quad (4.31)$$

The logistic selectivity has estimable parameters  $a_{50}$  and  $a_{t095}$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . The logistic selectivity takes values  $0.5\alpha$  at  $x = a_{50}$  and  $0.95\alpha$  at  $x = a_{50} + a_{t095}$ .

**4.12.7. inverse\_logistic**

$$f(x) = \alpha - \alpha / [1 + 19^{(a_{50}-x)/a_{t095}}] \quad (4.32)$$

The inverse logistic selectivity has estimable parameters  $a_{50}$  and  $a_{t095}$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . The logistic selectivity takes values  $0.5\alpha$  at  $x = a_{50}$  and  $0.95\alpha$  at  $x = a_{50} - a_{t095}$ .

**4.12.8. logistic\_producing**

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ \lambda(L), & \text{if } x = L \\ (\lambda(x) - \lambda(x-1)) / (1 - \lambda(x-1)), & \text{if } L < x < H \\ 1, & \text{if } x \geq H \end{cases} \quad (4.33)$$

The logistic-producing selectivity has the non-estimable parameters  $L$  and  $H$ , and has estimable parameters  $a_{50}$  and  $a_{t095}$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . For category transitions,  $f(x)$  represents the proportion moving, not the proportion that have moved. This selectivity was designed for use in an age-based model to model maturity. In such a model, a logistic-producing maturation selectivity will (in the absence of other influences) make the proportions mature follow a logistic curve with parameters  $a_{50}, a_{t095}$ .

**4.12.9. double\_normal**

$$f(x) = \begin{cases} \alpha 2^{-[(x-\mu)/\sigma_L]^2}, & \text{if } x \leq \mu \\ \alpha 2^{-[(x-\mu)/\sigma_R]^2}, & \text{if } x \geq \mu \end{cases} \quad (4.34)$$

The double-normal selectivity has estimable parameters  $a_1, s_L$ , and  $s_R$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . It has values  $\alpha$  at  $x = a_1$ , and  $0.5\alpha$  at  $x = a_1 - s_L$  and  $x = a_1 + s_R$ .

**4.12.10. double\_exponential**

$$f(x) = \begin{cases} \alpha y_0 (y_1/y_0)^{(x-x_0)/(x_1-x_0)}, & \text{if } x \leq x_0 \\ \alpha y_0 (y_2/y_0)^{(x-x_0)/(x_2-x_0)}, & \text{if } x > x_0 \end{cases} \quad (4.35)$$

The double-exponential selectivity has non-estimable parameters  $x_1$  and  $x_2$ , and estimable parameters  $x_0$ ,  $y_0$ ,  $y_1$ , and  $y_2$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . It can be ‘U-shaped’. Bounds for  $x_0$  must be such that  $x_1 < x_0 < x_2$ . With  $\alpha = 1$ , the selectivity passes through the points  $(x_1, y)$ ,  $(x_0, y_0)$ , and  $(x_2, y_2)$ . If both  $y_1$  and  $y_2$  are greater than  $y_0$  the selectivity is ‘U-shaped’ with minimum at  $(x_0, y_0)$ .

**4.13. Time Varying Parameters**

CASAL2 has the functionality to vary a parameter annually between the start and final year of a model run. This can be for blocks of years or specific years if chosen. For years that are not specified the parameter will default to the input or if in a iterative state such as estimation mode, the value being trialled at that iteration. Available methods for time varying a parameter. Where this functionality will become quite useful is in simulating more realistic observations. When you allow fisheries to have annual varying catchabilities and other more realistic model components simulated observations become more real data and thus conclusions based on simulated data are more useful.

**4.13.1. Constant**

Allows a parameter to have an alternative values during certain years, which can be estimated.

```
@time_varying q_time_var
type constant
parameter catchability[survey_q].q
years 1975:1988
value 0.001
```

**4.13.2. Random Walk**

A random deviate added into the last value drawn from a standard normal distribution. This has an estimable parameter  $\sigma_p$  for each time varying parameter  $p$ . For reproducible modelling, it is highly recommended that users set the seed (see Section 3.4) when using stochastic functionality like this, otherwise reproducing models becomes almost impossible.

```
@time_varying q_time_var
type random_walk
parameter catchability[survey_q].q
distribution normal
mean 0
sigma 3
```

If the parameter specified in the `@time_varying` is associated with an `@estimate` block then the parameter is constrained to stay within the lower and upper bounds of the `@estimate` block. Warning, if the parameter does not have an associated `@estimate` block then there is no safe guard for a random deviate to put the parameter in a space where the model fails, i.e generates NA or INF values. to avoid this from happening it is recommended you specify an `@estimate` block even though you are not estimating the parameter like below.

```
@estimate survey_q_est
type uniform
parameter catchability[survey_q].q
lower_bound 1e-6
upper_bound 10
```

This will insure the random walk time varying process will set the any new candidate within the lower and upper bound of the @estimate block.

#### 4.13.3. Annual shift

A parameter generated in year  $y$  ( $\theta'_y$ ) depends on the value specified by the user ( $\theta_y$ ) along with three coefficients  $a, b$  and  $c$  as follows,

$$\bar{\theta}_y = \frac{\sum_y^Y \theta_y}{Y} \quad (4.36)$$

$$\theta'_y = a\bar{\theta}_y + b\bar{\theta}_y^2 + c\bar{\theta}_y^3 \quad (4.37)$$

#### 4.13.4. Exogenous

Parameters are shifted based on an exogenous variable, an example of this is an exploitation selectivity parameters that may vary between years based on known changes in exploitation behaviour such as season, start time, and average depth of exploitation.

$$\delta_y = a(E_y - \bar{E}) \quad (4.38)$$

$$\theta'_y = \theta_y + \delta_y \quad (4.39)$$

where  $\delta_y$  is the shift or deviation in parameter  $\theta_y$  in year  $y$  to generate the new parameter value in year  $y$  ( $\theta'_y$ ).  $a$  is an estimable shift parameter,  $E$  is the exogenous variable and  $E_y$  is the value of this variable in year  $y$ . For more information readers can see ?.

---

## 5. The estimation section

### 5.1. Role of the estimation section

The role of the estimation section is to define the tasks carried out by CASAL2:

1. Define the objective function (see Section 5.2)
2. Define the parameters to be estimated (see Section 5.3)
3. Calculate a point estimate, i.e., the maximum posterior density estimate (MPD) (see Section 5.4).
4. Calculate a posterior profile selected parameters, i.e., find, for each of a series of values of a parameter, allowing the other estimated parameters to vary, the minimum value of the objective function (see Section 5.5).
5. Generate an MCMC sample from the posterior distribution (see Section 5.6).
6. Calculate the approximate covariance matrix of the parameters as the inverse of the minimizer's approximation to the Hessian, and the corresponding correlation matrix (see Section 5.4).

The estimation section defines the objective function, parameters of the model, and the method of estimation (point estimates, Bayesian posteriors, profiles, etc.). The objective function is based on a goodness-of-fit measure of the model to observations, priors and penalties. See the observation section for a description of the observations, likelihoods, priors and penalties.

### 5.2. The objective function

In Bayesian estimation, the objective function is a negative log-posterior,

$$Objective(p) = -\sum_i \log [L(\mathbf{p}|O_i)] - \log [\pi(\mathbf{p})] \quad (5.1)$$

where  $\pi$  is the joint prior density of the parameters  $p$ .

The contribution to the objective function from the likelihoods are defined in Section ???. In addition to likelihoods, priors (see Section 5.7) and penalties (see Section 5.8) are components of the objective function. Note that if the priors are specified as uniform, then the prior contribution is zero and the estimation problem turns into penalised-likelihood and not Bayesian.

Penalties can be used to ensure that the exploitation rate constraints on mortality events (i.e., fisheries) are not breached (otherwise there is nothing to prevent the model from having abundances so low that the recorded mortalities could not have been taken), penalties on category transitions (to ensure there are enough individuals to move), and possibly penalties to encourage estimated values to be similar or smooth, etc. Equation 5.1 can mathematically reduce to a penalised likelihood equation if all priors are assumed to be uniform. This is because uniform priors have a zero contribution to the objective function so Equation 5.1 reduces to likelihoods plus penalties.

### 5.3. Specifying the parameters to be estimated

The estimable parameters that will be estimated are defined using `@estimate` commands (see Section 9). An `@estimate` command-block looks like,

```
@estimate process[NaturalMortality].m
lower_bound 0.1
upper_bound 0.4
type uniform
```

See Section 3.5.5 for instructions on how to generate the parameter name. At least one parameter is to be estimated if doing an estimation `-e`, profile `-p`, or MCMC `-m` run. Initial values for the parameters to be estimated will still need to be provided, and these are used as the starting values for the minimiser. However, these may be overwritten if you provide a set of alternative starting values (i.e., using `casal2 -i`, see Section 3.4).

All parameters are estimated within bounds. For each parameter to be estimated, you need to specify the bounds and the prior (`type`) (Section 5.7). Note that the bounds and prior for each parameter refer to the values of the parameters, not the actual values resulting from the application of the parameter to an equation. Bounds should be carefully chosen as they effect the space in which the minimisers search over. Some minimisers convert lower and upper bound into a minimisation space (for example `-1,1` space for the numerical differences algorithm). If estimating only some elements of a vector, either define each element of the vector to be estimated (see 3.5.5) or fix the others by setting the bounds equal.

## 5.4. Point estimation

Point estimation is invoked with `casal2 -e`. Mathematically, it is an attempt to find a minimum of the objective function. CASAL2 has multiple algorithms for solving (minimising) the optimisation problem. There are three non auto differential minimisers: numerical differences (GAMMA DIFF), differential evolution minimiser, and the `dlib` minimiser. There are also three auto differential minimisers being: ADOL-C, CPPAD, and BETADIFF. For references see section 1.5

### 5.4.1. The numerical differences minimiser

The minimiser has three kinds of (non-error) exit status, depending on the minimiser:

1. Successful convergence (suggests you have found a local minimum, at least).
2. Convergence failure (you have not reached a local minimum, though you may deem yourself to be ‘close enough’ at your own risk).
3. Convergence unclear (the minimiser halted but was unable to determine if convergence occurred. You may be at a local minimum, although you should check by restarting the minimiser at the final values of the estimated parameters).

You can choose the maximum number of quasi-Newton iterations and objective function evaluations allotted to the minimiser. If it exceeds either limit, it exits with a convergence failure. We recommend large numbers of evaluations and iterations (at least the defaults of 300 and 1000) unless you successfully reach convergence with less. You can also specify an alternative starting point of the minimiser using `casal2 -i`.

We want to stress that the minimisers are local optimisation algorithms trying to solve a global optimisation problem. What this means is that, even if you get a ‘successful convergence’ message, your solution may be only a local minimum, not a global one. To diagnose this problem, try doing multiple runs from different starting points and comparing the results, or doing profiles of one or



more key parameters and seeing if any of the profiled estimates finds a better optimum than the original point estimate.

The approximate covariance matrix of the estimated parameters can be calculated as the inverse of the minimiser's approximation to the Hessian, and the corresponding correlation matrix is also calculated. Be aware that

- the Hessian approximation develops over many minimiser steps, so if the minimiser has only run for a small number of iterations the covariance matrix can be a very poor approximation
- the inverse Hessian is not a good approximation to the covariance matrix of the estimated parameters, and may not be useful to construct, for example, confidence intervals.

Also note that if an estimated parameter has equal lower and upper bounds, it will have entries of '0' in the covariance matrix and NaN or -1.#IND (depending on the operating system) in the correlation matrix.

```
@minimiser numerical_diff
type numerical_differences
tolerance 1e-6
iterations 2500
evaluations 4000
```

#### 5.4.2. The differential evolution minimiser

The differential evolution minimiser is a simple population based, stochastic function minimizer, but is claimed to be quite powerful in solving minimisation problems. It is a method of mathematical optimization of multidimensional functions and belongs to the class of evolution strategy optimizers. Initially, the procedure randomly generates and evaluates a number of solution vectors (the population size), each with  $p$  parameters. Then, for each generation (iteration), the algorithm creates a candidate solution for each existing solution by random mutation and uniform crossover. The random mutation generates a new solution by multiplying the difference between two randomly selected solution vectors by some scale factor, then adding the result to a third vector. Then an element-wise crossover takes place with probability  $P_{cr}$ , to generate a potential candidate solution. If this is better than the initial solution vector, it replaces it, otherwise the original solution is retained. The algorithm is terminated after either a predefined number of generations (`max_generations`) or when the maximum difference between the scaled individual parameters from the candidate solutions from all populations is less than some predefined amount `tolerance`.

The differential evolution minimiser can be good at finding global minimums in surfaces that may have local minima. However, the speed of the minimiser, and the ability to find a good minima depend on the number of initial 'populations'. Some authors recommend that the number of populations be set at about  $10 * p$ , where  $p$  is the number of free parameters. However, depending on your problem, you may find that you may need more, or that less will suffice.

We note that there is no proof of convergence for the differential evolution solver, but several papers have found it to be an efficient method of solving multidimensional problems. Our (limited) experience suggests that it can often find a better minima and may be faster or longer (depending on the actual model specification) at finding a solution when compared with the numerical differences minimiser. Comparisons with auto-differentiation minimisers or other more sophisticated algorithms have not been made.

```
@minimiser DE_solver
```

```
type de_solver
tolerance 1e-6
iterations 2500
evaluations 4000
```

### 5.4.3. Betadiff minimiser

An auto-differentiable minimiser for non-linear models, This is the minimiser from the original CASAL package.

```
@minimiser beta_diff
type beta_diff
tolerance 1e-6
iterations 2500
evaluations 4000
```

### 5.4.4. ADOL-C minimiser

An auto-differentiable minimiser for non-linear models.

```
@minimiser ADOLC
type adolc
step_size 1e-6
iterations 2500
evaluations 4000
tolerance 1e-6
```

### 5.4.5. CPPAD minimiser

An auto-differentiable minimiser for non-linear models.

```
@minimiser CPPAD
type cppad
```

### 5.4.6. Dlib minimiser

Non auto-diff minimiser

```
@minimiser Dlib
type dlib
tolerance 1e-6
iterations 2500
evaluations 4000
```

### 5.4.7. De solver minimiser

Non auto-diff minimiser

```
@minimiser de_soler
type de_solver
covariance false
population_size 100
max_generations 1000
```

## 5.5. Posterior profiles

If profiles are requested `casal2 -p`, CASAL2 will first calculate a point estimate. For each scalar parameter or, in the case of vectors or selectivities, the element of the parameter to be profiled, CASAL2 will fix its value at a sequence of  $n$  evenly spaced numbers (*step*) between a specified lower and upper bounds  $l$  and  $u$ , and calculate a point estimate at each value.

By default  $step = 10$ , and  $(l, u) = (\text{lower bound on parameter plus } (range/(2n)), \text{upper bound on parameter less } (range/(2n)))$ . Each minimisation starts at the final parameter values from the previous resulting value of the parameter being profiled. CASAL2 will report the objective function for each parameter value. Note that an initial point estimate should be compared with the profile, not least to check that none of the other points along the profile have a better objective function value than the initial ‘minimum’.

You specify which parameters are to be profiled, and optionally the number of steps, lower bound, and upper bound for each. In the case of vector parameters, you will also need to specify the element of the vector being profiled.

You can also supply the initial starting point for the estimation using `casal2 -i file` — this may improve the minimiser performance for the profiles.

If you get an implausible profile, it may be a result of not using enough iterations in the minimiser or a poor choice of minimiser control variables (e.g., the minimiser tolerance). It also may be useful to try both if the minimisers in CASAL2 and compare the results.

## 5.6. Bayesian estimation

CASAL2 can use a Monte Carlo Markov Chain (MCMC) to generate a sample from the posterior distribution of the estimated parameters `casal2 -m` and output the sampled values to a file (optionally keeping only every  $n$ th set of values).

As CASAL2 has no post-processing capabilities. CASAL2 cannot produce MCMC convergence diagnostics (use a package such as BOA) or plot/summarize the posterior distributions of the output quantities (for example, using a general-purpose statistical or spreadsheet package such as S-Plus, R, or Microsoft Excel).

Bayesian methodology and MCMC are both large and complex topics, and we do not describe either properly here. See Gelman et al. (?) and Gilks et al. (?) for details of both Bayesian analysis and MCMC methods. In addition, see Punt & Hilborn (?) for an introduction to quantitative fish stock assessment using Bayesian methods.

This section only briefly describes the MCMC algorithms used in CASAL2. See Section 9.3 for a better description of the sequence of CASAL2 commands used in a full Bayesian analysis.

CASAL2 uses a straightforward implementation of the Metropolis-Hastings algorithm (??). The Metropolis-Hastings algorithm attempts to draw a sample from a Bayesian posterior distribution, and calculates the posterior density  $\pi$ , scaled by an unknown constant. The algorithm generates a ‘chain’ or sequence of values. Typically the beginning of the chain is discarded and every  $N$ th element of the remainder is taken as the posterior sample. The chain is produced by taking an initial point  $x_0$  and repeatedly applying the following rule, where  $x_i$  is the current point:

- Draw a candidate step  $s$  from a proposal distribution  $J$ , which should be symmetric i.e.,  $J(-s) = J(s)$ .
- Calculate  $r = \min(\pi(x_i + s)/\pi(x_i), 1)$ .

- Let  $x_{i+1} = x_i + s$  with probability  $r$ , or  $x_i$  with probability  $1 - r$ .

An initial point estimate is produced before the chain starts, which is done so as to calculate the approximate covariance matrix of the estimated parameters (as the inverse Hessian), and may also be used as the starting point of the chain.

The user can specify the starting point of the point estimate minimiser using `casal2 -i`. Don't start it too close to the actual estimate (either by using `casal2 -i`, or by changing the initial parameter values in input configuration file) as it takes a few iterations to form a reasonable approximation to the Hessian.

There is currently two options for the starting point of the Markov Chain:

- Start from the point estimate.
- Restart a chain given a covariance matrix and starting points (see section `arg1`)

The chain moves in natural space, i.e., no transformations are applied to the estimated parameters. The default proposal distribution is a multivariate t centred on the current point, with covariance matrix equal to a matrix based on the approximate covariance produced by the minimiser, times some stepsize factor. The following steps define the initial covariance matrix of the proposal distribution:

- The covariance matrix is taken as the inverse of the approximate Hessian from the quasi-Newton minimiser.
- The covariance matrix is modified so as to decrease all correlations greater than `@mcmc.max_correlation` down to `@mcmc.max_correlation`, and similarly to increase all correlations less than `-@mcmc.max_correlation` up to `-@mcmc.max_correlation` (the `@mcmc.max_correlation` parameter defaults to 0.8). This should help to avoid getting 'stuck' in a lower-dimensional subspace.
- The covariance matrix is then modified either by,
  - if `@mcmc.adjustment_method=covariance`: that if the variance of the  $i$ th parameter is non-zero and less than `@mcmc.min_difference` times the difference between the parameters' lower and upper bound, then the variance is changed, without changing the associated correlations, to  $k = \min\_diff(upper\_bound_i - lower\_bound_i)$ . This is done by setting

$$\text{Cov}(i, j)' = \sqrt{k} \text{Cov}(i, j) / \text{sd}(i)$$

for  $i \neq j$ , and  $\text{var}(i)' = k$

- if `@mcmc.adjustment_method=correlation`: that if the variance of the  $i$ th parameter is non-zero and less than `@mcmc.min_difference` times the difference between the parameters' lower and upper bound, then its variance is changed to  $k = \min\_diff(upper\_bound_i - lower\_bound_i)$ . This differs from (i) above in that the effect of this option is that it also modifies the resulting correlations between the  $i$ th parameter and all other parameters.

This allows each estimated parameter to move in the MCMC even if its variance is very small according to the inverse Hessian. In both cases, the `@mcmc.min_difference` parameter defaults to 0.0001.

- The `@mcmc.stepsize` (a scalar factor applied to the covariance matrix to improve the acceptance probability) is chosen by the user. The default is  $2.4d^{-0.5}$  where  $d$  is the number

of estimated parameters, as recommended by Gelman et al. (?). However, you may find that a smaller value may often be better.

The proposal distribution can also change adaptively during the chain, using two different mechanisms. Both are offered as means of improving the convergence properties of the chain. It is important to note that any adaptive behaviour must finish before the end of the burn-in period, i.e., the proposal distribution must be finalised before the kept portion of the chain starts. The adaptive mechanisms are as follows:

1. You can request that the stepsize change adaptively at one or more sample numbers (See next paragraph for details on the stepsize adaptation methods)
2. You can request that the entire covariance matrix change adaptively at one or more sample numbers. At each adaptation, the covariance matrix is replaced with an empirical covariance, derived from the MCMC chain. The idea here is that an empirical covariance is a better approximation to the proposal distribution than the inverse of the hessian matrix, and can improve convergence and mixing of your chain.

The two methods that you can choose to adapt the step size are `double_half` or `ratio`, this is done through the input parameter `adapt_stepsize_method`. The `double_half` method is used in CASAL and (See Gelman et al. (?) for justification). The algorithm for `double_half` is, at each adaptation, the stepsize is doubled if the acceptance rate since the last adaptation is more than 0.5, or halved if the acceptance rate is less than 0.2. The `ratio` is taken from SPM. It adapts the current step size by, the acceptance rate since the last adaptation multiplied by 4.1667 to reach an acceptance rate of  $\approx 0.24$  see ? for justification on that acceptance rate.

The stepsize parameter is now on a completely different scale, and must be reset. It is set to a user-specified value (which may or may not be the same as the initial stepsize). We recommend that some of the stepsize adaptations are set to occur after this, so that the stepsize can be readjusted to an appropriate value which gives good acceptance probabilities with the new matrix.

All modified versions of the covariance matrix are printed to the standard output, but only the initial covariance matrix (inverse Hessian) is saved to the objectives file. The number of covariance modifications by each iteration is recorded as a column on the objectives file.

The variance-covariance matrix of this sub-sample of chain is calculated. As above, correlations greater than `@mcmc.max_correlation` are reduced to `@mcmc.max_correlation`, correlations less than `@mcmc.max_correlation` are increased to `@mcmc.max_correlation`, and very small non-zero variances are increased (`@mcmc.covariance_adjustment` and `@mcmc.min_difference`). The result is the new variance-covariance matrix of the proposal distribution.

The procedure used to choose the sample of points is as follows. First, all points on the chain so far are taken. All points in an initial user-specified period are discarded. The assumption is that the chain will have started moving during this period - if this is incorrect and the chain has still not moved by the end of this period, it is a fatal error and CASAL2 stops. The remaining set of points must contain at least some user-specified number of transitions - if this is incorrect and the chain has not moved this often, it is again a fatal error. If this test is passed, the set of points is systematically sub-sampled down to 1000 points (it must be at least this long to start with).

The probability of acceptance for each jump is 0 if it would move out of the bounds, or 1 if it improves the posterior, or (new posterior/old posterior) otherwise. You can specify how often the position of the chain is recorded using the `keep` parameter. For example, with `keep 10`, only every 10th sample is recorded.

You have the option to specify that some of the estimated parameters are fixed during the MCMC. If

the chain starts at the point estimate or at a random location, these fixed parameters are set to their values at the point estimate.

If you specify the start of the chain using `casal2 -i`, these fixed parameters are set to the values in the file.

Restarting a mcmc chain, in the case where computers get turned off and an mcmc execution is halted. There is the ability to restart it from where it finishes.

```
casal2 -m --resume --objective-file Objective_file_name --sample-file Sample_file_name
```

where `Objective_file_name` is the file name containing the objective report and `Sample_file_name` is the file name containing the sample report from a mcmc chain.

The posterior sample can be used for (projections (Section 4.6)) or simulations (Section 6.6) with the values supplied using `casal2 -i file`.

A multivariate t distribution is available as an alternative to the multivariate normal proposal distribution. If you request multivariate t proposals, you may want to change the degrees of freedom from the default of 4. As the degrees of freedom decrease, the t distribution becomes more heavy tailed. This may lead to better convergence properties.

Given a posterior (sub)sample, CASAL2 can calculate a list of output quantities for each sample point (see Section 7 specifically tabular report). These quantities can be dumped into a file (using `casal2 -r --tabular`) and read into an external software package where the posterior distributions can be plotted and/or summarised.

The posterior sample can also be used for projections (Section 4.6). The advantage of this is that the parameter uncertainty, as expressed in your posterior distribution, can be included into the risk estimates.

## 5.7. Priors

In a Bayesian analysis, you need to give a prior for every parameter that is being estimated. There are no default priors.

Note that when some of these priors are parameterised in terms of mean, c.v., and standard deviation, these refer to the parameters of the distribution before bounds are applied. The moments of the prior after the bounds are applied may differ.

CASAL2 has the following priors (expressed in terms of their contribution to the objective function):

1. Uniform

$$-\log(\pi(p)) = 0 \tag{5.2}$$

2. Uniform-log (i.e.,  $\log(p) \sim \text{uniform}$ )

$$-\log(\pi(p)) = \log(p) \tag{5.3}$$

3. Normal with mean  $\mu$  and c.v.  $c$

$$-\log(\pi(p)) = 0.5 \left( \frac{p - \mu}{c\mu} \right)^2 \tag{5.4}$$

4. Normal with mean  $\mu$  and standard deviation  $\sigma$

$$-\log(\pi(p)) = 0.5 \left( \frac{p - \mu}{\sigma} \right)^2 \quad (5.5)$$

5. Lognormal with mean  $\mu$  and c.v.  $c$

$$-\log(\pi(p)) = \log(p) + 0.5 \left( \frac{\log(p/\mu)}{s} + \frac{s}{2} \right)^2 \quad (5.6)$$

where  $s$  is the standard deviation of  $\log(p)$  and  $s = \sqrt{\log(1 + c^2)}$ .

6. Normal-log with  $\log(p)$  having mean  $m$  and standard deviation  $s$ ,

6. Beta with mean  $\mu$  and standard deviation  $\sigma$ , and range parameters  $A$  and  $B$

$$-\log(\pi(p)) = (1 - m) \log(p - A) + (1 - n) \log(B - p) \quad (5.7)$$

where  $v = \frac{\mu - A}{B - A}$ , and  $\tau = \frac{(\mu - A)(B - \mu)}{\sigma^2} - 1$  and then  $\mu = \tau v$  and  $n = \tau(1 - v)$ . Note that the beta prior is undefined when  $\tau \leq 0$ .

Vectors of parameters can be independently (but not necessarily identically) distributed according to any of the above forms, in which case the joint negative-log-prior for the vector is the sum of the negative-log-priors of the components. Values of each parameter need to be specified for each element of the vector.

In addition, for a vector  $p$  of  $n$  identically distributed parameters (for example, YCS) the following priors are allowed:

## 5.8. Penalties

Penalties are associated with processes and can be used to encourage or discourage parameter values or model outputs that are unlikely to be sensible, by adding a penalty to the objective function. For example, parameter estimates that do not allow a known mortality event to remove enough individuals from the population can be discouraged with an event mortality penalty. CASAL2 requires penalty functions for processes that move or shift a *number* of individuals between categories or from the partition.

For most penalties, you need to specify a multiplier, and the objective function is increased by this multiplier times the penalty value as described below. In some cases you will need to make the multiplier quite large to prohibit some model behaviour.

Currently, the penalties for the processes `@process[label].type=event_mortality`, `@process[label].type=tag_by_length` and `@process[label].type=category_transition` are the only penalties implemented.

For these processes, two types of penalty can be defined, natural scale (the default) and log scale. Both of these types add a penalty value of the squared difference between the observed value (i.e., the actual number of individuals to be removed in an event mortality process or the actual number

of individuals to shift in a category transition process), and the number that were moved (if less than or equal), times the penalty multiplier.

The natural scale penalty just uses at the squared difference on a natural scale, while the log scale penalty uses the squared difference of the logged values.

### 5.9. Additional Priors

Additional priors can be thought of as the inverse of penalties. They constrain parameters in certain spaces. The types of additional priors available in CASAL2 are `vector_smoothing` and `vector_averaging`, defined as,

#### 1. `vector_averaging`

Applied to a vector parameter. Sum of squares of  $r$ th differences, optionally on a log scale. This encourages the vector to be like a polynomial of degree  $(r-1)$ . Note a range of the vector to be smoothed can be specified (and if not, the smoother is applied to the entire vector), but this must be specified by an index of the vector and must be between 1 and the length of the vector, inclusive.

#### 2. `vector_smoothing`

Applied to a vector parameter. Square of  $(\text{mean}(\text{vector})-k)$ , or of  $(\text{mean}(\log(\text{vector}))-l)$ , or of  $(\log(\text{mean}(\text{vector})/m))$ . Encourages the vector to average arithmetically to  $k$  or  $m$ , or geometrically to  $\exp(l)$ . Typically used for YCS with  $k=1$  or  $m=1$  or  $l=0$ , to encourage the YCS to centre on 1. Optionally, you can choose to exclude indices outside a given set of bounds.

#### 5.9.1. Estimate Transformations

The support of a random variable  $X$  with density  $p_X(x)$  is that subset of values for which it has non-zero density,

$$\text{supp}(X) = \{x | p_X(x) > 0\}$$

If  $f$  is a transformation function defined on the support of  $X$ , then  $Y = f(X)$  is a new random variable. This section shows the available transformations in CASAL2 and the probability density function of  $Y$ . This theory follows the STAN manual ?.

Suppose  $X$  is one dimensional and  $f: \text{supp}(X) \rightarrow \mathbf{R}$  is a one-to-one, monotonic function with a differentiable inverse  $f^{-1}$ . Then the density of  $Y$  is given by

$$p_Y(y) = p_X(f^{-1}(y)) \left| \frac{\partial}{\partial y} f^{-1}(y) \right|$$

The absolute derivative of the inverse transform measures how the scale of the transformed variable changes with respect to the underlying variable.



---

## 6. The observation section

### 6.1. Observations

Observations are typically supplied at an instance in time, over a group of aggregated categories. Time series of observations can be supplied as separate observations for each year or point in time.

The definitions for each type of observation are described below, including how the observed values should be supplied, how CASAL2 calculates the expected values, and the likelihoods that are available for each type of observation.

There are two types of observations available in CASAL2. The first are observations that are associated with a **mortality block** and secondly observations that are associated with a specific process. These can be distinguished by the type definition. If an observation type begins with `process` it is an observation that is associated with a process. If a type does **not** begin with `process` it is associated with the mortality block of the time step that you define. For example the observation type `process_abundance` is a process based observation vs `process_abundance_abundance`, which is an observation that is associated with a mortality block.

Process specific observations can also be broken into two types. **Specific process observations** are observations that are associated to a specific process (e.g. `process_proportions_migrating`), and **general process observations** are observations that can be associated with any process (e.g. `process_proportions_at_age`). These tiers of observations have been separated in different sections as to reduce the confusion.

#### 6.1.1. Mortality block associated observations

All observations within this class are calculated in a similar fashion. That is an expectation is calculated at the beginning of the mortality block and at the end of the mortality block. CASAL2 then uses a linear interpolation to approximate an expectation part way through a mortality block using the subcommand `time_step_proportion`. This could be useful if a survey occurs part-way through an exploitation phase. For example for if modelling a fish population this may be part-way through a fishing season. Each observation in this class will evaluate different expectations of the partition which will be explained in the following descriptions. A list of observation types that are available with this class of observations are as follows,

- `abundance`
- `biomass`
- `proportions_at_age`
- `proportions_at_length`
- `proportions_by_category`
- `tag_recapture_by_length`
- `tag_recapture_by_age`

#### Abundance or biomass observations

Abundance (or biomass) observations are observations of either a relative or absolute number (or biomass) of individuals from a set of categories after applying a selectivity. The observations classes are the same, except that a biomass observation will use the biomass as the observed (and expected)

value (calculated from mean weight of individuals within each age and category) while an abundance observation is just the number of individuals.

Each observation is for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity), for aggregated categories. Further, you need to provide the label of the catchability coefficient  $q$ , which can either be estimated or fixed. For absolute abundance or absolute biomass observations, define a catchability where  $q = 1$ .

The observations can be supplied for any set of categories. For example, for a model with the two categories *male* and *female*, we might supply an observation of the total abundance/biomass (male + female) or just male abundance/biomass. The subcommand `categories` defines the categories used to aggregate the abundance/biomass. In addition, each category must have an associated selectivity, defined by `selectivities`. For example,

```
categories male
selectivities male-selectivity
```

defines an observation for males after applying the selectivity `male-selectivity`. CASAL2 then expects that there will be a single observation supplied. The expected values for the observations will be the expected abundance (or biomass) of males, after applying the selectivities, at the year and time-step specified.

CASAL2 calculates the expected values by summing over the defined ages (via the age range and selectivity) and categories at both the beginning and end of a mortality block. You can prompt CASAL2 to approximate the expectation part way through the mortality block using the `time_step_proportion`. The default value CASAL2 uses is 0.5, which does linear interpolation between the start and end abundance (or biomass) from the mortality block.

```
@observation MyAbundance
type abundance
years 1999
...
categories male
obs 1000
...
```

Or, for an observation aggregated over multiple categories,

```
@observation MyAbundance
type abundance
years 1990 1991
...
categories male+female
table obs
1990 1000
1991 1200
end_table
...
```

Note that, to define a biomass observation instead of an abundance observation, use

```
@observation MyBiomass
type biomass
...
```

## Proportions-at-age

Proportions-at-age observations are observations of the relative number of individuals at age, via some selectivity.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity), for categories aggregated over a set of spatial cells. Note that the categories defined in the observations must have an associated selectivity, defined by `selectivities`.

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive), but the upper end of the age range can optionally be a plus group — which must be either the same or less than the plus group defined for the partition.

Proportions-at-age observations can be supplied as;

1. a set of proportions for a single category,
2. a set of proportions for multiple categories, or
3. a set of proportions across aggregated categories.

The method of evaluating expectation are the same for all three of these sceneries. We will describe how you define these different scenarios and the expected dimensions of observation and error inputs that CASAL2 expects for each respective scenario with examples.

Like all types of observations that are associated with the mortality block, CASAL2 will evaluate the numbers at age before the mortality block (after taking into account a selectivity that the user defines) and after for the specified time step of the observation. CASAL2 will generate expectations from the partition part way through the mortality block using the subcommand `time_step_proportion`. This approximation is an linear interpolation of the numbers at age over the mortality block.

Once the interpolation is evaluated CASAL2 will apply ageing error if the user has specified it. CASAL2 finally converts numbers at age to proportions at age by dividing all numbers at age bin by the total and sending that to the likelihood to be evaluated.

Defining an observation for a single category is the simplest, and is used to model a set of proportions of a single category by age class. For example, to specify that the observations are of the proportions of male within each age class, then the subcommand `categories` for the `@observation[label].type=proportion.by_age` command is,

```
categories male
```

CASAL2 then expects that there will be a single vector of proportions supplied, with one proportion for each age class within the defined age range, and that these proportions sum to one.

For example, if the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10). The expected values will be the expected proportions of males within each of these age classes (after ignoring any males aged less than 3 or older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 8 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

```
@observation MyProportions
type proportions_at_age
...
categories male
```

```
min_age 3
max_age 9
years 1990
table obs
1990 0.01 0.09 0.20 0.20 0.35 0.10 0.05
end_table
...
```

Defining an observation for multiple categories extends on the single category implementation. It is used to model a set of proportions over several categories by age class. For example, to specify that the observations are of the proportions of male or females within each age class, then the subcommand `categories` for the `@observation[label].type=proportion.by_age` command is,

```
categories male female
```

CASAL2 then expects that there will be a single vector of proportions supplied, with one proportion for each category and age class combination, and that these proportions sum to one across all ages and categories.

For example, if there were two categories and the age range was 3 to 10, then 16 proportions should be supplied (one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10, for each category male and female). The expected values will be the expected proportions of males and within each of these age classes (after ignoring those aged less than 3 or older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 16 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example,

```
@observation MyProportions
type proportions_at_age
...
categories male female
min_age 1
max_age 5
years 1990 1991
table obs
1990 0.01 0.05 0.10 0.20 0.20 0.01 0.05 0.15 0.20 0.03
1991 0.02 0.06 0.10 0.21 0.18 0.02 0.03 0.17 0.20 0.01
end_table
...
```

Defining an observation across aggregated categories allows categories to be aggregated before the proportions are calculated. It is used to model a set of proportions from several categories that have been combined by age class. To indicate that two (or more) categories are to be aggregated, separate them with a '+' symbol. For example, to specify that the observations are of the proportions of male and females combined within each age class, then the subcommand `categories` for the `@observation[label].type=proportion.by_age` command is,

```
categories male + female
```

CASAL2 then expects that there will be a single vector of proportions supplied, with one proportion for each age class, and that these proportions sum to one.

For example, if there were two categories and the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the ages 3, 4, 5, 6, 7, 8, 9, and 10, for the sum of males and females within each age class). The expected values will be the expected proportions of males + females within each of these age classes (after ignoring those aged less than 3 or older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 16 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example,

```
@observation MyProportions
type proportions_at_age
...
years 1990 1991
categories male+female
min_age 1
max_age 5
table obs
1990 0.02 0.13 0.25 0.30 0.30
1991 0.02 0.06 0.18 0.35 0.39
end_table
...
```

The later form can then be extended to include multiple categories, or multiple aggregated categories. For example, to describe proportions for the three groups: immature males, mature males, and all females (immature and mature females added together) for ages 1–4, a total of 12 proportions are required

```
@observation MyProportions
type proportions_at_age
...
categories male_immature male_mature female_immature+female_mature
min_age 1
max_age 4
years 1990
table obs
year 1990 0.05 0.15 0.15 0.05 0.02 0.03 0.08 0.04 0.05 0.15 0.15 0.08
end_table
...
```

## Proportions-at-length

Functionality regarding defining combinations of categories and aggregated categories directly translates over from proportions at age to proportions at length. The difference is the observation is over length bins instead of age-classes. CASAL2 calculates expectations of numbers at length by converting numbers at age to numbers by length by using the age-length relationship and distribution specified for the category specified in the @age\_length block. Commands that are different are instead of supplying a minimum and maximum age users must supply a vector of length bins. If there is no plus group i.e. length\_plus\_group=false CASAL2 expects a vector of proportions for each year that is  $n - 1$ , where  $n$  is the number of lengths supplied. If length\_plus\_group=true CASAL2 expects a vector of proportions for each year that is  $n$ . The last proportion represents the numbers from the last length bin to the maximum length the age-length relationship allows.

```
@observation Observed_Length_frequency_Chat_east
type process_removals_by_length
years 1991 1992
likelihood multinomial
```

```
time_step Summer
fishery EastChathamRise
process instant_mort
categories male
length_plus_group false
length_bins 0 20 40 60 80 110
table obs
1991 0.2 0.25 0.15 0.2 0.2
1992 0.12 0.25 0.28 0.25 0.1
end_table
table error_values
1991 25
1992 37
end_table
```

### Proportions-by-category observations

Proportions-by-category observations are observations of either the relative number of individuals between categories within age classes, or relative biomass between categories within age classes.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity).

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive), but the upper end of the age range can optionally be a plus group — which may or may not be the same as the plus group defined for the partition.

Proportions-by-category observations can be supplied for any set of categories as a proportion of themselves and any set of additional categories. For example, for a model with the two categories *male* and *female*, we might supply observations of the proportions of males in the population at each age class. The subcommand `categories` defines the categories for the numerator in the calculation of the proportion, and the subcommand `categories2` supplies the additional categories to be used in the denominator of the calculation. In addition, each category must have an associated selectivity, defined by `selectivities` for the numerator categories and `selectivities2` for the additional categories used in the denominator, e.g.,

```
categories male
categories2 female
selectivities male-selectivity
selectivities2 female-selectivity
```

defines that the proportion of males in each age class as a proportion of males + females. CASAL2 then expects that there will be a vector of proportions supplied, with one proportion for each age class within the defined age range, i.e., if the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the ages 3, 4, 5, 6, 7, 8, 9, and 10). The expected values will be the expected proportions of male to male + female within each of these age classes, after applying the selectivities at the year and time-step specified.

The observations must be supplied using all or some of the values defined by a categorical layer. CASAL2 calculates the expected values by summing over the ages (via the age range and selectivity) and categories for those spatial cells where the categorical layer has the same value as defined for each vector of observations i.e.,

```
@observation MyProportions
type proportions_by_category
years 1990 1991
...
categories male
```

```

categories2 female
min_age 1
max_age 5
table obs
1990 0.01 0.05 0.10 0.20 0.20
1991 0.02 0.06 0.10 0.21 0.18
end_table
...

```

### Tag Recapture by length

Tag data is primarily used to estimate the population abundance of fish. In some models, this estimation can only be made outside the model and the result is used as an estimate of abundance in the model. But in CASAL the tagging data can, alternatively, be fitted within the model.

Before adding a tag-recapture time series, you will need to define a tag-release process (Section 4.7.5). Tagging events list the labels of the tags which are modelled, and define the events where fish are tagged (i.e., CASAL2 moves fish into the section of the partition corresponding to a specific tag).

The observations are divided into two parts: (i) the number of fish that were scanned, and (ii) the number of tags that were recaptured. Each can be specified by categories, or for combinations of categories. The precise content of the scanned and recaptured observations depends on the sampling method, and the available options are:

1. age: both scanned and recaptured are vectors containing numbers-at-age. Only available in an age-based model. The selectivity ogive is redundant and cannot be supplied.
2. size: both scanned and recaptured are vectors containing numbers-at-size. Can be used in either an age- or size-based model. The selectivity ogive is redundant and cannot be supplied.

When defining the tag-recapture time series, you also need to specify:

- the time step,
- the years (unlike a tag-release process, the tag-recapture observations can occur over several years),
- the probability that each scanned tagged fish is detected as tagged (may be less than 1 if the observers are not infallible). The expected number of tags detected is calculated by multiplying this number by the number of tagged fish in the sample,
- the tagged category or categories (Make up the recaptures),
- the categories scanned (All the fish sampled for tags),
- A selectivity used in the recapture process,
- the size classes if the observations are size-based in an age-based model.

An example of a tag recapture observation applied in CASAL2 is shown, below

```

## For the following partition
@categories
format sex.area.tag
names male.Areal.2011,notag female.Areal.2011,notag

@observation Tag_2011_Areal_recap_2012 ## individuals tagged in 2011 and recaptured in 2012
## in Areal
type tag_recapture_by_length
categories *.Areal.2011+ ## male and female tagged categories
categories2 format=*.Areal.*+ ## scanned categories in Areal
detection 0.85 ## detection probability
likelihood binomial ## likelihood choice

```

```

selectivities One ## label of selectivity for tagged
selectivities2 One ## label of selectivity for scanned
years 2012 ## years to apply observation
time_step step2 ## time_step to apply observation
time_step_proportion 0.5 ## proportion of mortality applied before observation is calculated
length_bins 21 30 40 50 ## size bins
plus_group true ## is the last bin a plus group i.e. 50cm +

table scanned
2012 281271 41360 30239 12234
end_table

table recaptured
2012 15 20 12 2
end_table

delta 1e-11 ## robustification value
dispersion 6.3 ## dispersion factor

```

The tag-recapture likelihood (binomial) is specified below as it is a modified version of the more general binomial. Note that this likelihood does not have any user-set precision parameters such as  $N$  or  $c.v.$  (though there are user-specified robustification and dispersion parameters available). Note that factorials are calculated using the log-gamma function, to allow for non-integer arguments where necessary (and avoid overflow errors).

### 6.1.2. General process observations

A list of types that are associated with this set of observations.

- process\_abundance
- process\_biomass
- process\_proportions\_at\_age
- process\_proportions\_at\_length
- process\_proportions\_by\_category

These observations have the same expectations as the mortality block versions described in Section 4.4. With the exception that instead of wrapping a mortality block they can wrap any process type available in CASAL2.

### 6.1.3. Specific process observations

A list of types that are associated with this set of observations are;

- process\_removals\_by\_age,
- process\_removals\_by\_length,
- process\_proportions\_migrating.

#### Process removals by age

Removals at age observations are observations of the relative number of individuals at age, partway through a process of type `mortality_instantaneous`. This observation is exclusively associated with the process of type `mortality_instantaneous`, and will error out if associated with any other process type.



The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity that is associated with the process).

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive), but the upper end of the age range can optionally be a plus group — which must be either the same or less than the plus group defined for the partition.

The expectations from this observation are generated whilst the process is being executed. The expectation of numbers at age  $a$  for category  $c$  from exploitation method  $m$  ( $E[N_{a,c,m}]$ ) are defined as,

$$E[N_{a,c,m}] = N_{a,c} U_{a,m} S_{a,c,m} 0.5 M_{a,c} \quad (6.1)$$

where,  $N_{a,c}$  are the numbers at age in category  $c$  before the process is executed,  $U_{a,m}$  is the exploitation rate for age  $a$  from method  $m$ .  $S_{a,c,m}$  is the selectivity and  $M$  is the natural mortality. These are all relevant to the time step which the user defines.

The observation class then acquires the variable  $E[N_{a,c,m}]$  and applies ageing error if the user has specified it. Then it amalgamates the observations by method and category depending on how the user specifies the observation, before converting numbers at age to proportions and sending them to the likelihood to be evaluated.

Likelihoods that are available for this observation class are the multinomial, dirichlet and the lognormal. See Section 6.2 for information on the respected likelihood.

### Process removals by length

Removals by length observations are observations of the relative number of individuals at length, partway through a process of type `mortality_instantaneous`. This observation is exclusively associated with the process of type `mortality_instantaneous`, and will error out if associated with any other process type.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity that is associated with the process).

The expectations from this observation are generated whilst the process is being executed. The expectation of numbers at age  $a$  for category  $c$  from exploitation method  $m$  ( $E[N_{a,c,m}]$ ) are defined as,

$$E[N_{a,c,m}] = N_{a,c} U_{a,m} S_{a,c,m} 0.5 M_{a,c} \quad (6.2)$$

where,  $N_{a,c}$  are the numbers at age in category  $c$  before the process is executed,  $U_{a,m}$  is the exploitation rate for age  $a$  from method  $m$ .  $S_{a,c,m}$  is the selectivity and  $M$  is the natural mortality. These are all relevant to the time step which the user defines.

The observation class acquires the variable  $E[N_{a,c,m}]$  from the process and applies the age-length relationship specified in the model. This converts numbers at age to numbers at age and length, where CASAL2 then converts to numbers at length. Then it amalgamates the observations by method and category depending on how the user specifies the observation, before converting numbers at age to proportions and sending them to the likelihood to be evaluated.

```
@observation observation_fishery_LF
type process_removals_by_length
...
years 1993 1994 1995
method_of_removal FishingEast
```

```
mortality_instantaneous_process instant_mort
length_plus_group false
length_bins 0 20 40 60 80 110
delta 1e-5
table obs
1993 0.0 0.05 0.05 0.10 0.80
1994 0.05 0.1 0.05 0.05 0.75
1995 0.3 0.4 0.2 0.05 0.05
end_table
```

```
table error_values
1993 31
1994 34
1995 22
end_table
```

Likelihoods that are available for this observation are the multinomial, dirichlet and the lognormal. See Section 6.2 for information on the respected likelihood.

### Proportions migrating

This observation is of the proportion migrating from one area to another. This observation is exclusively associated with the process type `transition_category`, and will error out when trying to associate with any other process type. This observation is used to inform migration rates in migration processes. This observation class is used in the Hoki stock assessment see ? for more information on how these observations are collected and the situation you would use it. This observation calculates an expectation  $E_a$  of proportions for each age class  $a$  that have migrated, by evaluating the following,

$$E_a = \frac{N_a - N'_a}{N_a} \quad (6.3)$$

where,  $N_a$  are the numbers of individuals in age  $a$  before the migration process occurs and  $N'_a$  is the number of individuals after the migration process occurs.

The likelihoods that are allowed for this observation are the lognormal, multinomial and dirichlet.

An extract of the Hoki stock assessment is as follows,

```
@observation pspawn_1993
type process_proportions_migrating
years 1993
time_step step4
process Wspmg ## migration process that the observation is associated with
age_plus true
min_age 4
max_age 9
likelihood lognormal
categories male.west+female.west ## Categories to evaluate the prportion for
ageing_error Normal_offset ## label for an @ageing_error block
table obs
#age 4 5 6 7 8 9
1993 0.64 0.58 0.65 0.66 0.71 0.60
end_table

table error_values
## if lognormal these are c.v.'s
1993 0.25
end_table
```

## 6.2. Likelihoods

### 6.2.1. Likelihoods for proportions-at-age observations

CASAL2 implements three likelihoods for proportions-at-age observations, the multinomial likelihood, dirichlet, and the lognormal likelihood.

#### The multinomial likelihood

For the observed proportions at age  $O_i$  for age classes  $i$ , with sample size  $N$ , and the expected proportions at the same age classes  $E_i$ , the negative log-likelihood is defined as;

$$-\log(L) = -\log(N!) + \sum_i \log((NO_i)!) - NO_i \log(Z(E_i, \delta)) \quad (6.4)$$

where  $\sum_i O_i = 1$  and  $\sum_i E_i = 1$ .  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta/\delta), & \text{otherwise} \end{cases} \quad (6.5)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

#### The dirichlet likelihood

For the observed proportions at age  $O_i$  for age classes  $i$ , with sample size  $N$ , and the expected proportions at the same age classes  $E_i$ , the negative log-likelihood is defined as;

$$-\log(L) = -\log(\Gamma(\sum_i \alpha_i)) + \sum_i \log(\Gamma(\alpha_i)) - \sum_i (\alpha_i - 1) \log(Z(O_i, \delta)) \quad (6.6)$$

where  $\alpha_i = Z(NE_i, \delta)$ ,  $\sum_i O_i = 1$ , and  $\sum_i E_i = 1$ .  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta/\delta), & \text{otherwise} \end{cases} \quad (6.7)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

#### The lognormal likelihood

For the observed proportions at age  $O_i$  for age classes  $i$ , with c.v.  $c_i$ , and the expected proportions at the same age classes  $E_i$ , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left( \log(\sigma_i) + 0.5 \left( \frac{\log(O_i/Z(E_i, \delta))}{\sigma_i} + 0.5\sigma_i \right)^2 \right) \quad (6.8)$$

where

$$\sigma_i = \sqrt{\log(1 + c_i^2)} \quad (6.9)$$

and the  $c_i$ 's are the c.v.s for each age class  $i$ , and  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.10)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

### 6.2.2. Likelihoods for abundance and biomass observations

#### The lognormal likelihood

For observations  $O_i$ , c.v.  $c_i$ , and expected values  $qE_i$ , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left( \log(\sigma_i) + 0.5 \left( \frac{\log(O_i / qZ(E_i, \delta))}{\sigma_i} + 0.5 \sigma_i \right)^2 \right) \quad (6.11)$$

where

$$\sigma_i = \sqrt{\log(1 + c_i^2)} \quad (6.12)$$

and  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.13)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

#### The normal likelihood

For observations  $O_i$ , c.v.  $c_i$ , and expected values  $qE_i$ , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left( \log(c_i E_i) + 0.5 \left( \frac{O_i - E_i}{Z(c_i E_i, \delta)} \right)^2 \right) \quad (6.14)$$

and  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.15)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

### 6.2.3. Likelihoods for tag recapture by age and length observations

#### The binomial likelihood

Designed for situations where the size frequencies or age frequencies of the recaptured tagged fish and of the scanned fish are known. Available in both age or size based models.

Here we define the likelihood as a binomial, but based on sizes, rather than ages,

$$-\log(L)' = -\sum_i \left[ \log(n_i!) - \log((n_i - m_i)!) - \log((m_i)!) + m_i \log \left( Z \left( \frac{M_i}{N_i}, \delta \right) \right) + (n_i - m_i) \log \left( Z \left( 1 - \frac{M_i}{N_i}, \delta \right) \right) \right] \quad (6.16)$$

where

$n_i$  = number of fish at size or age  $i$  that were scanned

$m_i$  = number of fish at size or age  $i$  that were recaptured

$N_i$  = number of fish at size or age  $i$  in the available population (tagged and untagged)

$M_i$  = number of fish at size or age  $i$  in the available population that have the tag after a detection probability  $p_d$  has been applied,  $M_i = M'_i p_d$ , where  $M'_i$  is the expected available population that have the tag.

where  $Z(x, \delta)$  is a robustifying function with parameter  $r > 0$  (to prevent division by zero errors), defined as

$$Z(x, \delta) = \begin{cases} x & \text{where } x \geq \delta \\ \frac{\delta}{(2-x/\delta)} & \text{otherwise} \end{cases}$$

Finally if a dispersion parameter ( $\tau$ ) is described in the observation then the final negative log likelihood  $-\log(L)$  contribution is,

$$-\log(L) = -\log(L)' / \tau$$

### 6.2.4. Likelihoods for proportions-by-category observations

CASAL2 implements two likelihoods for proportions-by-category observations, the binomial likelihood, and the normal approximation to the binomial (binomial-approx).

#### The binomial likelihood

For observed proportions  $O_i$  for age class  $i$ , where  $E_i$  are the expected proportions for age class  $i$ , and  $N_i$  is the effective sample size for age class  $i$ , then the negative log-likelihood is defined as;

$$-\log(L) = -\sum_i \left[ \log(N_i!) - \log((N_i(1 - O_i))!) - \log((N_i O_i)!) + N_i O_i \log(Z(E_i, \delta)) + N_i(1 - O_i) \log(Z(1 - E_i, \delta)) \right] \quad (6.17)$$

where  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.18)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

### The normal approximation to the binomial likelihood

For observed proportions  $O_i$  for age class  $i$ , where  $E_i$  are the expected proportions for age class  $i$ , and  $N_i$  is the effective sample size for age class  $i$ , then the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \log \left( \sqrt{Z(E_i, \delta) Z(1 - E_i, \delta) / N_i} \right) + \frac{1}{2} \left( \frac{O_i - E_i}{\sqrt{Z(E_i, \delta) Z(1 - E_i, \delta) / N_i}} \right)^2 \quad (6.19)$$

where  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.20)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

### 6.3. Process error

Additional ‘process error’ can be defined for each set of observations. Additional process error has the effect of increasing the observation error in the data, and hence of decreasing the relative weight given to the data in the fitting process.

For observations where the likelihood is parameterised by the c.v., you can specify the process error for a given set of observations as a c.v., in which case all the c.v.s  $c_i$  are changed to

$$c'_i = \sqrt{c_i^2 + c_{process\_error}^2} \quad (6.21)$$

Note that  $c_{process\_error} \geq 0$ , and that  $c_{process\_error} = 0$  is equivalent to no process error.

Similarly, if the likelihood is parameterised by the effective sample size  $N$ ,

$$N'_i = \frac{1}{1/N_i + 1/N_{process\_error}} \quad (6.22)$$

Note that this requires that  $N_{process\_error} > 0$ , but we allow the special case of  $N_{process\_error} = 0$ , and define  $N_{process\_error} = 0$  as no process error (i.e., defined to be equivalent to  $N_{process\_error} = \infty$ ).

For both the c.v. and  $N$  process errors, the process error has more effect on small errors than on large ones. Be clear that a large value for the  $N$  process error means a small process error.

### 6.4. Calculating nuisance q's

This section describes the equations used to calculate nuisance catchability coefficients  $q_s$  (see Section 6.7.1). From the users point of view, the essence is that you can use nuisance  $q_s$  in the following situations:

1. With maximum likelihood.
2. With Bayesian estimation, providing that your prior on the  $q$  is one of the following:
  - Uniform
  - Uniform-log

**Table 6.1: Equations used to calculate nuisance  $q$ 's. (\*=no analytic solution found.)**

Distribution of observations	Maximum Likelihood	Uniform	Uniform-log	Normal	lognormal
Normal	(6.23)	(6.23)	(6.25)	*	*
Lognormal	(6.26)	(6.26)	(6.30)	*	(6.31)

- Lognormal with observations distributed lognormal, robustified lognormal

The equations used for calculating nuisance  $q$ s in maximum likelihood or Bayesian analysis are indexed in Table ?.

Note that  $q$ s are calculated for robustified lognormal likelihoods as if they were ordinary lognormal likelihoods.

The equations and their derivations follow. Let  $\sigma_i = \sqrt{\log(1 + c_i^2)}$  throughout, and let  $n$  be the number of observations in the time series. The case of multiple time series sharing the same  $q$ , and the modifications required for the assumption of curvature, are addressed at the end of this subsection.

First, consider maximum likelihood estimation. When the  $(O_i)$  are assumed to be normally distributed,

$$-\log(L) = \sum_i \log(c_i q E_i) + 0.5 \sum_i \left( \frac{O_i - q E_i}{c_i q E_i} \right)^2 \quad (6.23)$$

The value of  $q$  which minimises the objective function is found by solving  $\partial/\partial q(-\log(L))$

$$\frac{\partial}{\partial q}(-\log(L)) = \frac{n}{q} + \frac{1}{q^2} \sum_i \frac{O_i}{c_i^2 E_i} - \frac{1}{q^3} \sum_i \left( \frac{O_i}{c_i E_i} \right)^2 \quad (6.24)$$

hence

$$\hat{q} = \frac{-S_1 + \sqrt{S_1^2 + 4nS_2}}{2n} \quad (6.25)$$

where  $S_1 = \sum_i (O_i/c_i^2 E_i)$  and  $S_2 = \sum_i (O_i/c_i E_i)^2$

When the  $(O_i)$  are assumed to be lognormally distributed,

$$-\log(L) = \sum_i \log(\sigma_i) + 0.5 \sum_i \left( \frac{\log(O_i) - \log(q E_i) + 0.5 \sigma_i^2}{\sigma_i} \right)^2 \quad (6.26)$$

$$\frac{\partial}{\partial q}(-\log(L)) = \frac{-1}{q} \sum_i \left( \frac{\log(O_i/E_i) - \log(q) + 0.5 \sigma_i^2}{\sigma_i^2} \right) \quad (6.27)$$

$$\hat{q} = \exp \frac{0.5n + S_3}{S_4} \quad (6.28)$$

where  $S_3 = \sum_i (\log(O_i/E_i)/\sigma_i^2)$  and  $S_4 = \sum_i (1/\sigma_i^2)$

Next consider Bayesian estimation, where we must also specify a prior for  $q$ .

The effects of the prior on the equations are to replace likelihood  $L$  by posterior  $P$  throughout, to add  $-\log(\pi(q))$  to the equation for  $-\log(P)$  and  $\partial/\partial q(-\log(-\pi(q)))$  to the equation for  $\partial/\partial q(-\log(P))$

This last term is 0 for a uniform prior on  $q$ ,  $1/q$  for a log-uniform prior, and  $\frac{1}{q} \left( 1.5 + \frac{\log(q) - \log(\mu_q)}{\sigma_q^2} \right)$  for a lognormal prior,

where  $\mu_q$  and  $c_q$  are the mean and c.v of the prior on  $q$  and  $\sigma_q = \sqrt{\log(1 + c_q^2)}$ . Clearly, if the prior is uniform, the equation for  $\hat{q}$  is the same as the maximum likelihood estimation.

When the  $(O_i)$  are assumed to be normally distributed and the prior is log-uniform equation (6.25) becomes,

$$\hat{q} = \frac{-S_1 + \sqrt{S_1^2 + 4(n+1)S_2}}{2(n+1)} \quad (6.29)$$

but we cannot solve for  $\hat{q}$  with either a normal or lognormal prior.

When the  $O_i$  are assumed to be lognormally distributed and the prior is log-uniform, equation (6.28) becomes

$$\hat{q} = \exp \frac{0.5n - 1 + S_3}{S_4} \quad (6.30)$$

and if the prior is lognormal,

$$\hat{q} = \exp \frac{0.5n - 1.5 + \log(\mu_q)/\sigma_q^2 + S_3}{S_4 + 1/\sigma_q^2} \quad (6.31)$$

but it is not possible to solve for  $\hat{q}$  with a normal prior.

## 6.5. Ageing error

CASAL2 can apply ageing error age frequency observations. Ageing error is applied to the expected values for proportions-at-age observations. The ageing error is applied as a misclassification matrix, which has the effect of 'smearing' the age frequencies. These are used in calculating the fits to the observed values, and hence the contribution to the total objective function.

Ageing error is optional, and if it is used, it may be omitted for any individual time series. Different ageing error models may be applied for different observation commands. See Section 7.12 for reporting the misclassification matrix.

The ageing error models implemented are,

1. None: The default model is to apply no ageing error.
2. Off by one: Proportion  $p_1$  of individuals of each age  $a$  are misclassified as age  $a - 1$  and proportion  $p_2$  are misclassified as age  $a + 1$ . Individuals of age  $a < k$  are not misclassified. If there is no plus group in the population model, then proportion  $p_2$  of the oldest age class will 'fall off the edge' and disappear.
3. Normal: Individuals of age  $a$  are classified as ages which are normally distributed with mean  $a$  and constant c.v.  $c$ . As above, if there is no plus group in the population model, some individuals of the older age classes may disappear. If  $c$  is high enough, some of the younger age classes may 'fall off the other edge'. Individuals of age  $a < k$  are not misclassified.

Note that the expected values (fits) reported by CASAL2 for observations with ageing error will have had the ageing error applied.



## 6.6. Simulating observations

CASAL2 can generate simulated observations for a given model with given parameter values using `casal2 -s 1` (To simulate one set of simulated observations). Simulated observations are randomly distributed values, generated according to the error assumptions defined for each observation, around fits calculated from one or more sets of the 'true' parameter values. Simulating from a set of parameters can be used to generate observations from an operating model or as a form of parametric bootstrap.

The procedure CASAL2 uses for simulating observations is to first run using the 'true' parameter values and generate the expected values. Then, if a set of observations uses ageing error, ageing error is applied. Finally a random value for each observed value is generated based on (i) the expected values, (ii) the type of likelihood specified, and (iii) the variability parameters (e.g., `error_value` and `process_error`).

Methods for generating the random error, and hence simulated values, depend on the specific likelihood type of each observation.

1. Normal likelihood parameterised by c.v.: Let  $E_i$  be the fitted value for observation  $i$ , and  $c_i$  be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value  $S_i$  is generated as an independent normal deviate with mean  $E_i$  and standard deviation  $E_i c_i$ .
2. Log-normal likelihood: Let  $E_i$  be the fitted value for observation  $i$  and  $c_i$  be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value  $S_i$  is generated as an independent lognormal deviate with mean and standard deviation (on the natural scale, not the log-scale) of  $E_i$  and  $E_i c_i$  respectively. The robustification parameter  $\delta$  is ignored.
3. Multinomial likelihood: Let  $E_i$  be the fitted value for observation  $i$ , for  $i$  between 1 and  $n$ , and let  $N$  be the sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter  $\delta$  is ignored. Then,
  - a) A sample of  $N$  values from 1 to  $n$  is generated using the multinomial distribution, using sample probabilities proportional to the values of  $E_i$ .
  - b) Each simulated observation value  $S_i$  is calculated as the proportion of the  $N$  sampled values equalling  $i$
  - c) The simulated observation values  $S_i$  are then rescaled so that their sum is equal to 1
4. Binomial and the normal approximation to the binomial likelihoods: Let  $E_i$  be the fitted value for observation  $i$ , for  $i$  between 1 and  $n$ , and  $N_i$  the corresponding equivalent sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter  $\delta$  is ignored. Then,
  - a) A sample of  $N_i$  independent binary variates is generated, equalling 1 with probability  $E_i$
  - b) The simulated observation value  $S_i$  is calculated as the sum of these binary variates divided by  $N_i$

Note that CASAL2 will report simulated observations using the usual observation report (`@report[label].type=observation`). The report `@report[label].type=simulated.observation` will generate simulated observations in a form suitable for use as input within a CASAL2 input configuration file. See Section 7 for more detail.

## 6.7. Pseudo-observations

CASAL2 can generate expected values for observations without them contributing to the total objective function. These are called pseudo-observations, and can be used to either generate the expected values from CASAL2 for reporting or diagnostic purposes. To define an observation as a pseudo-observation, use the command `@observation[label].likelihood=none`. Any observation type can be used as a pseudo-observation. CASAL2 can also generate simulated observations from pseudo-observations. Note that;

- Output will only be generated if a report command `@report[label].type=observation` is specified.

- The observed values should be supplied (even if they are ‘dummy’ observation). These will be processed by CASAL2 as if they were actual observation values, and must conform to the validations carried out for the other types of likelihood.
- The subcommands `likelihood`, `obs`, `error_value` and `process_error` have no effect when generating the expected values for the pseudo-observation.
- When simulating observations, CASAL2 needs the subcommand `simulation_likelihood` to tell it what sort of likelihood to use. In this case, the `obs`, `error_value` and `process_error` are used to determine the appropriate terms to use for the likelihood when simulating.

---

## 7. The report section

The report section specifies the printouts and other outputs from the model. CASAL2 does not, in general, produce any output unless requested by a valid `@report` block.

Reports from CASAL2 can be defined to print partition and states objects at a particular point in time, observation summaries, estimated parameters and objective function values. See below for a more extensive list, and an example of an observation report.

```
@report observation_age ## label of report
type observation ## Type of report
observation age_1990 ## label corresponding to an @observation report, shown below

@observation age_1990
type proportion_at_age
year 1990
plus_group
etc ...
```

Reports from CASAL2 all conform to a standard style (with one exception — the `output_parameters` report, see below). The standard style is that reports are prefixed with an aster-ix followed by a user-defined label and type of report in brackets (e.g., `*label (type)`), with the report ending with the line `*end`. For example,

```
*My_report (type)
...
*end
```

This syntax should make it easier for external packages to be configured to read CASAL2 output. The `extract` functions in the **R** CASAL2 package uses this information to identify and read CASAL2 output within an **R** environment.

Note that the `output_parameters` report does not print either a header or `*end` at the end of the report. This is as the `output_parameters` report is designed to provide a single line (or multi-line for more than one set) vector of the estimated parameter values, suitable for reading by CASAL2 (with the command `casal2 -i`). This is a specialised report for `casal2 -o filename` command. For estimate values in standard output users are recommended to use `type=estimate_value`.

Reports can be defined in an `@report` but may not be generated. For example printing the partition for a year and/or time-step that does not exist or reporting the covariance matrix when not estimating. Certain reports are associated with certain CASAL2 run modes. Such reports are ignored by CASAL2 and the program will not generate any output for these reports — although they must still conform to CASAL2s syntax requirements.

Not all reports will be generated in all run modes. Some reports are only available in some run modes. For example, when simulating, only simulation reports will be output.

### 7.1. Print the partition at the end of an initialisation

Print the partition following an initialisation phase. This prints out, the numbers of individuals in each age class and category in the partition following an initialisation phase. This report will print out in the following runmodes `-r`, `-e`, `-f`.

### 7.2. Print the partition

Print the partition for a given year or given years and time-step. This prints out, the numbers of individuals in each age class and category in the partition for each year. Note that this report is evaluated at the end of the time-step in the given year(s). This report will print out in the following runmodes `-r`, `-e`, `-f`.

### 7.3. Print the age length and length weight values

Print the length and weight for an age of the partition for a given year or given years and time-step. This prints out, the length and weight value for each age class and category in the partition for each year and time step. Note that this report is evaluated at the end of the time-step in the given year(s). This report will print out in the following runmodes `-r`, `-e`, `-f`.

```
@report length_weight_at_age
type partition_mean_weight
time_step step2
years 1900:2013
```

### 7.4. Print a process summary

Print a summary of a process. Depending on the process, different summaries are produced. These typically detail the type of process, its parameters and other options, and any associated details. This report will print out in the following runmodes `-r`, `-e`, `-f`.

### 7.5. Print derived quantities

Print out the description of the derived quantity, and the values of the derived quantity as recorded in the model state, for each year of the model. and for all years in the initialisation phases. This report will print out in the following runmodes `-r`, `-e`, `-f`.

### 7.6. Print the estimated parameters

Print a summary of the estimated parameters using the following type `estimate_summary`, including the parameter name, lower and upper bounds, the label of the prior, and its value. This report will print out in the following runmodes `-r`, `-e`.

### 7.7. Print the estimated parameters in a vector format

Print the estimated parameter values out as a vector. The `estimate_values` report prints the name of the parameter, followed by the value of that run. This report will print out in the following runmodes `-r`, `-e`.

### 7.8. Print the objective function

Print the total objective function value, and the value of all observations, the values of all priors, and the value of any penalties that have been incurred in the model. Note that if an individual model run does not incur a penalty, then the penalty will not be reported. This report will print out in the following runmodes `-r`, `-e`, `-f`.

### 7.9. Print the covariance matrix

Print the Hessian and covariance matrices if estimating and if the covariance has been requested by `@minimiser[label].covariance=true`.

### 7.10. Print observations, fits, and residuals

Prints out for each category or combination of categories, expected values as calculated by the model, residuals (observed – expected), the error value, process error, and the total error (i.e., the error value as

modified by any additional process error), and the contribution to the total objective function of that individual point in the observation.

Note that constants in likelihoods are often ignored in the objective function score of individual points. Hence, the total score from an observation equals the contribution of the objective function scores from each individual point plus a constant term (if applicable). In likelihoods without a constant term, then the total score from an observation will equal the contribution of the objective function scores from each individual point.

If simulating, then the contribution to the objective function of each observation is reported as zero.

### **7.11. Print simulated observations**

Prints out a complete observation definition (i.e., in the form defined by `@report[label].type=observation`), but with observed values replaced by randomly generated simulated values. The output is in a form suitable for use within a CASAL2 input configuration file, reproducing the command and subcommands from the input configuration file. This report will print out in the following runmodes `-s`.

### **7.12. Print the ageing error misclassification matrix**

Prints out the ageing error misclassification matrix used to offset observations within during model the model fitting procedure.

### **7.13. Print selectivities**

Prints the values of a selectivity for each age in the partition, for a given year and at then end of a given time-step.

### **7.14. Print the random number seed**

Prints the random number seed used by CASAL2 to generate the random number sequence. Future runs made with the same random number seed and the same model will produce identical outputs.

### **7.15. Print the results of an MCMC**

Print the MCMC samples, objective function values, and proposal covariance matrix following an MCMC. This report will print out in the following runmode `-m`.

### **7.16. Print the MCMC samples as they are calculated**

Print the MCMC samples for each new *i*th sample as they are calculated while doing an MCMC. The output file will be updated with each new sample as it is calculated by CASAL2. This report will print out in the following runmodes `-m`.

### **7.17. Print the MCMC objective function values as they are calculated**

Print the MCMC objective function values (along with the proposal covariance matrix) for each new *i*th sample as they are calculated while doing an MCMC. The output file will be updated with each new set of objective function values as it is calculated by CASAL2. This report will print out in the following runmodes `-m`.

### 7.18. Print time varying parameters

Print all `@time_varying` blocks with the values and years that they were implemented in. This report will print out in the following runmodes `-r`, `-e`, `-m`.

```
@report time_varying_parameters
type time_varying
```

### 7.19. Tabular reporting

An alternative reporting framework to the standard output is the tabular reporting. Tabular reporting is used with multiline `-i` input files (like the MCMC sample or `-o` outputs). Tabular reports will print out a row that will correspond with each row of the `-i` input files. Tabular reporting is invoked at the command line using the following command `casal2 -r --tabular -i file_name`. Currently derived quantities and `estimate_values` are the only report types that are within this framework. For each input file the output will begin with the names of each column followed by a multiline report ending with the `*end` syntax. These tables can be easily read into **R** using the `CASAL2` package and for the example of MCMC multi-line files posteriors of derived quantities can be plotted.

---

## 8. Population command and subcommand syntax

### 8.1. Model structure

**@model1** *label*     Define an object of type *model*

**start\_year**     Define the first year of the model, immediately following initialisation

Type: non-negative integer

Default: No Default

Value: Defines the first year of the model,  $\geq 1$ , e.g. 1990

**final\_year**     Define the final year of the model, excluding years in the projection period

Type: non-negative integer

Default: No Default

Value: Defines the last year of the model, i.e., the model is run from *start\_year* to *final\_year*

**min\_age**     Minimum age of individuals in the population

Type: non-negative integer

Default: 0

Value:  $0 \leq \text{age}_{\min} \leq \text{age}_{\max}$

**max\_age**     Maximum age of individuals in the population

Type: non-negative integer

Default: 0

Value:  $0 \leq \text{age}_{\min} \leq \text{age}_{\max}$

**age\_plus**     Define the oldest age as a plus group

Type: boolean

Default: false

Value: true, false

**initialisation\_phases**     Define the labels of the phases of the initialisation

Type: string vector

Default: true

Value: A list of valid labels defined by @initialisation\_phase

**time\_steps**     Define the labels of the time steps, in the order that they are applied, to form the annual cycle

Type: string vector

Default: No Default

Value: A list of valid labels defined by @time\_step

**projection\_final\_year**     Define the final year of the model in projection mode

Type: non-negative integer

Default: 0

Value: Defines the last year of the projection period, i.e., the projection period runs from *final\_year*+1 to *projection\_final\_year*. For the default, 0, no projections are run.

length\_bins

Type: constant vector

Default: true

base\_weight\_units      Define the units for the base weight. This will be the default unit of any weight input parameters

Type: string

Default: tonnes

Allowed Values: grams, tonnes, kgs

## 8.2. Initialisation

**@initialisation\_phase** *label*      Define an object of type *initialisation\_phase*

*label*      The label of the initialisation phase

Type: string

Default: No Default

*type*      The type of initialisation

Type: string

Default: iterative

### 8.2.1. @initialisation\_phase[label].type=cinitial

*categories*      The list of categories for the Cinitial initialisation

Type: string vector

Default: No Default

### 8.2.2. @initialisation\_phase[label].type=derived

*insert\_processes*      Additional processes not defined in the annual cycle, that are to be inserted into this initialisation phase

Type: string vector

Default: true

*exclude\_processes*      Processes in the annual cycle to be excluded from this initialisation phase

Type: string vector

Default: true

*casal\_intialisation\_switch*      Run an extra annual cycle to evaluate equilibrium SSB's. Warning - if true, this may not correctly evaluate the equilibrium state. Use true if attempting to replicate a legacy CASAL model

Type: boolean

Default: false



**8.2.3. @initialisation\_phase[label].type=iterative**

years      The number of iterations (years) over which to execute this initialisation phase

Type: non-negative integer

Default: No Default

insert\_processes      (years) over which to execute this initialisation phase

Type: string vector

Default: true

exclude\_processes      Processes in the annual cycle to be excluded from this initialisation phase

Type: string vector

Default: true

convergence\_years      The iteration (year) when the test for convergence (lambda) is evaluated

Type: non-negative integer vector

Default: true

lambda      The maximum value of the absolute sum of differences (lambda) between the partition at year-1 and year that indicates successful convergence

Type: constant

Default: 0.0

**8.2.4. @initialisation\_phase[label].type=state\_category\_by\_age**

categories      The list of categories for the category state initialisation

Type: string vector

Default: No Default

min\_age      The minimum age of values supplied in the definition of the category state

Type: non-negative integer

Default: No Default

max\_age      The minimum age of values supplied in the definition of the category state

Type: non-negative integer

Default: No Default

**8.3. Categories**

**@categories** *label*      Define an object of type *categories*

format      The format that the category names adhere too

Type: string  
Default: No Default

**names**      The names of the categories to be used in the model  
Type: string vector  
Default: No Default

**years**      The years that individual categories will be active for. This overrides the model values  
Type: string vector  
Default: true

**age\_lengths**      The labels of age\_length objects that are assigned to categories  
Type: string vector  
Default: true

### 8.4. Time-steps

**@time\_step** *label*      Define an object of type *time\_step*

**label**      The label of the timestep  
Type: string  
Default: No Default

**processes**      The labels of the processes for this time step in the order that they occur  
Type: string vector  
Default: No Default

### 8.5. Processes

**@process** *label*      Define an object of type *process*

**label**      The label of the process  
Type: string  
Default: No Default

**type**      The type of process  
Type: string  
Default: ""

**print\_report**      Indicates if a process report should be generated for this process  
Type: boolean  
Default: false

**8.5.1. @process[label].type=ageing**

categories      The labels of the categories  
Type: string vector  
Default: No Default

**8.5.2. @process[label].type=maturation**

from      List of categories to mature from  
Type: string vector  
Default: No Default

to      List of categories to mature too  
Type: string vector  
Default: No Default

selectivities      List of selectivities to use for maturation  
Type: string vector  
Default: No Default

years      The years to be associated with rates  
Type: non-negative integer vector  
Default: No Default

rates      The rates to mature for each year  
Type: estimable vector  
Default: No Default

**8.5.3. @process[label].type=mortality\_constant\_rate**

categories      List of categories labels  
Type: string vector  
Default: No Default

m      Mortality rates  
Type: estimable  
Default: No Default

time\_step\_ratio      Time step ratios for the mortality rates  
Type: constant vector  
Default: true

selectivities      List of selectivities for the categories

Type: string vector  
Default: No Default

#### **8.5.4. @process[label].type=mortality\_event**

categories      Categories  
Type: string vector  
Default: No Default

years      Years in which to apply the mortality process  
Type: non-negative integer vector  
Default: No Default

catches      The number of removals (catches) to apply for each year  
Type: estimable vector  
Default: No Default

u\_max      Maximum exploitation rate ( $U_{max}$ )  
Type: estimable  
Default: 0.99

selectivities      List of selectivities  
Type: string vector  
Default: No Default

penalty      The label of the penalty to apply if the total number of removals cannot be taken  
Type: string  
Default: ""

#### **8.5.5. @process[label].type=mortality\_event\_biomass**

categories      Category labels  
Type: string vector  
Default: No Default

selectivities      The labels of the selectivities for each of the categories  
Type: string vector  
Default: No Default

years      Years in which to apply the mortality process  
Type: non-negative integer vector  
Default: No Default

catches      The biomass of removals (catches) to apply for each year

Type: estimable vector

Default: No Default

`u_max` Maximum exploitation rate ( $U_{max}$ )

Type: estimable

Default: 0.99

`penalty` The label of the penalty to apply if the total biomass of removals cannot be taken

Type: string

Default: ""

### 8.5.6. `@process[label].type=mortality_holling_rate`

`prey_categories` Prey Categories labels

Type: string vector

Default: No Default

`predator_categories` Predator Categories labels

Type: string vector

Default: No Default

`is_abundance` Is vulnerable amount of prey and predator an abundance [true] or biomass [false]

Type: boolean

Default: true

`a` parameter a

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

`b` parameter b

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

`x` This parameter controls the type of functional form, Holling function type 2 ( $x=2$ ) or 3 ( $x=3$ ), or generalised (Michaelis Menten,  $x=1$ )

Type: estimable

Default: No Default

Lower Bound: 1.0 (inclusive)

`u_max` Maximum exploitation rate ( $U_{max}$ )

Type: constant  
Default: No Default  
Lower Bound: 0.0 (inclusive)  
Upper Bound: 1.0 (inclusive)

`prey_selectivities`      Selectivities for prey categories  
Type: string vector  
Default: No Default

`predator_selectivities`      Selectivities for predator categories  
Type: string vector  
Default: No Default

`penalty`      Label of penalty to be applied  
Type: string  
Default: ""

`years`      Years in which to apply the mortality process  
Type: non-negative integer vector  
Default: No Default

### **8.5.7. `@process[label].type=mortality_instantaneous`**

`categories`      Categories for instantaneous mortality  
Type: string vector  
Default: No Default

`m`      Natural mortality rates for each category  
Type: estimable  
Default: No Default  
Lower Bound: 0.0 (inclusive)  
Upper Bound: 1.0 (inclusive)

`time_step_ratio`      Time step ratios for natural mortality  
Type: constant vector  
Default: true

`selectivities`      The selectivities to apply on the categories for natural mortality  
Type: string vector  
Default: No Default

**8.5.8. @process[label].type=mortality\_prey\_suitability**

prey\_categories      Prey Categories labels

Type: string vector

Default: No Default

predator\_categories      Predator Categories labels

Type: string vector

Default: No Default

consumption\_rate      Predator consumption rate

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

electivities      Prey Electivities

Type: estimable vector

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

u\_max      Umax

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

prey\_selectivities      Selectivities for prey categories

Type: string vector

Default: No Default

predator\_selectivities      Selectivities for predator categories

Type: string vector

Default: No Default

penalty      Label of penalty to be applied

Type: string

Default: ""

years      Year that process occurs

Type: non-negative integer vector

Default: No Default

**8.5.9. @process[label].type=nop**

**8.5.10. @process[label].type=recruitment\_beverton\_holt**

categories      Category labels

Type: string vector

Default: No Default

r0      R0

Type: estimable

Default: false

b0      B0

Type: estimable

Default: false

proportions      Proportions

Type: estimable vector

Default: No Default

age      Age to recruit at

Type: non-negative integer

Default: true

ssb\_offset      Spawning biomass year offset

Type: integer

Default: false

steepness      Steepness

Type: estimable

Default: 1.0

ssb      SSB Label (derived quantity)

Type: string

Default: No Default

b0\_initialisation\_phase      Initialisation phase Label that b0 is from

Type: string

Default: ""

ycs\_values      YCS Values

Type: estimable vector

Default: No Default

prior\_standardised\_ycs      Priors for year class strength on ycs values (not standardised ycs)



values

Type: boolean

Default: true

standardise\_ycs\_years      Years that are included for year class standardisation

Type: non-negative integer vector

Default: true

#### **8.5.11. @process[label].type=recruitment\_constant**

categories      Categories

Type: string vector

Default: No Default

proportions      Proportions

Type: estimable

Default: true

age      Age

Type: non-negative integer

Default: No Default

r0      R0

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

#### **8.5.12. @process[label].type=survival\_constant\_rate**

categories      List of categories

Type: string vector

Default: No Default

s      Survival rates

Type: estimable

Default: No Default

time\_step\_ratio      Time step ratios for S

Type: constant vector

Default: true

selectivities      Selectivity label

Type: string vector

Default: No Default

### 8.5.13. @process[label].type=tag\_by\_age

from      Categories to transition from

Type: string vector

Default: No Default

to      Categories to transition to

Type: string vector

Default: No Default

min\_age      Minimum age to transition

Type: non-negative integer

Default: No Default

max\_age      Maximum age to transition

Type: non-negative integer

Default: No Default

penalty      Penalty label

Type: string

Default: ""

u\_max      U Max

Type: constant

Default: 0.99

years      Years to execute the transition in

Type: non-negative integer vector

Default: No Default

initial\_mortality

Type: constant

Default: 0

initial\_mortality\_selectivity

Type: string

Default: ""

loss\_rate

Type: constant vector

Default: No Default

loss\_rate\_selectivities

Type: string vector  
Default: true

selectivities  
Type: string vector  
Default: No Default

n  
Type: constant vector  
Default: true

#### 8.5.14. @process[label].type=tag\_by\_length

from      Categories to transition from  
Type: string vector  
Default: No Default

to      Categories to transition to  
Type: string vector  
Default: No Default

plus\_group      Use plus group for last length bin  
Type: boolean  
Default: false

maximum\_length      The upper length when there is no plus group  
Type: constant  
Default: 0

penalty      Penalty label  
Type: string  
Default: ""

u\_max      U Max  
Type: constant  
Default: 0.99

years      Years to execute the transition in  
Type: non-negative integer vector  
Default: No Default

initial\_mortality  
Type: constant  
Default: 0

`initial_mortality_selectivity`

Type: string

Default: ""

`selectivities`

Type: string vector

Default: No Default

`n`

Type: constant vector

Default: true

### **8.5.15. @process[label].type=tag\_loss**

`categories`      List of categories

Type: string vector

Default: No Default

`tag_loss_rate`      Tag Loss rates

Type: constant vector

Default: No Default

`time_step_ratio`      Time step ratios for Tag Loss

Type: constant vector

Default: true

`tag_loss_type`      Type of tag loss

Type: string

Default: No Default

`selectivities`      Selectivities

Type: string vector

Default: No Default

`year`      The year the first tagging release process was executed

Type: non-negative integer

Default: No Default

### **8.5.16. @process[label].type=transition\_category**

`from`      From

Type: string vector

Default: No Default

to      To  
Type: string vector  
Default: No Default

proportions      Proportions  
Type: estimable  
Default: No Default

selectivities      Selectivity names  
Type: string vector  
Default: No Default

### **8.5.17. @process[label].type=transition\_category\_by\_age**

from      Categories to transition from  
Type: string vector  
Default: No Default

to      Categories to transition to  
Type: string vector  
Default: No Default

min\_age      Minimum age to transition  
Type: non-negative integer  
Default: No Default

max\_age      Maximum age to transition  
Type: non-negative integer  
Default: No Default

penalty      Penalty label  
Type: string  
Default: ""

u\_max      U Max  
Type: constant  
Default: 0.99

years      Years to execute the transition in  
Type: non-negative integer vector  
Default: No Default

## 8.6. Time varying parameters

**@time\_varying** *label* Define an object of type *time\_varying*

*label* The time-varying label

Type: string

Default: No Default

*type* The time-varying type

Type: string

Default: ""

*years* Years in which to vary the values

Type: non-negative integer vector

Default: No Default

*parameter* The name of the parameter to time vary

Type: string

Default: No Default

### 8.6.1. @time\_varying[label].type=annual\_shift

*values*

Type: constant vector

Default: No Default

*a*

Type: constant

Default: No Default

*b*

Type: constant

Default: No Default

*c*

Type: constant

Default: No Default

*scaling\_years*

Type: non-negative integer vector

Default: true

**8.6.2. @time\_varying[label].type=constant**

value      Value to assign to estimable  
Type: estimable vector  
Default: No Default

**8.6.3. @time\_varying[label].type=exogenous**

a      Shift parameter  
Type: estimable  
Default: No Default

exogeneous\_variable      Values of exogeneous variable for each year  
Type: constant vector  
Default: No Default

**8.6.4. @time\_varying[label].type=linear**

slope      The slope of the linear trend (additive unit per year  
Type: estimable  
Default: No Default

intercept      The intercept of the linear trend value for the first year  
Type: estimable  
Default: No Default

**8.6.5. @time\_varying[label].type=random\_draw**

mean      Mean  
Type: estimable  
Default: 0

sigma      Standard deviation  
Type: estimable  
Default: 1

distribution      distribution  
Type: string  
Default: normal

### 8.6.6. @time\_varying[label].type=random\_walk

mean      Mean  
Type: estimable  
Default: 0

sigma      Standard deviation  
Type: estimable  
Default: 1

distribution      distribution  
Type: string  
Default: normal

## 8.7. Derived quantities

**@derived\_quantity** *label*      Define an object of type *derived\_quantity*

label      Label of the derived quantity  
Type: string  
Default: No Default

type      Type of derived quantity  
Type: string  
Default: No Default

time\_step      The time step in which to calculate the derived quantity after  
Type: string  
Default: No Default

categories      The list of categories to use when calculating the derived quantity  
Type: string vector  
Default: No Default

selectivities      A list of one selectivity  
Type: string vector  
Default: No Default

time\_step\_proportion      Proportion through the mortality block of the time step when  
calculated  
Type: constant  
Default: 0.5  
Lower Bound: 0.0 (inclusive)  
Upper Bound: 1.0 (inclusive)

time\_step\_proportion\_method      Method for interpolating for the proportion through the



mortality block

Type: string

Default: weighted\_sum

Allowed Values: weighted\_sum, weighted\_product

### 8.7.1. @derived\_quantity[label].type=abundance

### 8.7.2. @derived\_quantity[label].type=biomass

## 8.8. Age-length relationship

**@age\_length** *label* Define an object of type *age\_length*

**label** Label of the age length relationship

Type: string

Default: No Default

**type** Type of age length relationship

Type: string

Default: No Default

**time\_step\_proportions** the fraction of the year applied in each time step that is added to the age for the purposes of evaluating the length, i.e., a value of 0.5 for a time step will evaluate the length of individuals at age+0.5 in that time step

Type: constant vector

Default: true

**distribution** The assumed distribution for the growth curve

Type: string

Default: normal

**cv\_first** CV for the first age class

Type: estimable

Default: 0.0

Lower Bound: 0.0 (inclusive)

**cv\_last** CV for last age class

Type: estimable

Default: 0.0

Lower Bound: 0.0 (inclusive)

**casal\_switch** If true, use the (less accurate) equation for the cumulative normal function as was used in the legacy version of CASAL.

Type: boolean

Default: false

### 8.8.1. @age\_\_length[label].type=data

external\_gaps

Type: string

Default: mean

Allowed Values: mean, nearest\_neighbour

internal\_gaps

Type: string

Default: mean

Allowed Values: mean, nearest\_neighbour, interpolate

length\_weight      The label from an associated length-weight block

Type: string

Default: No Default

by\_length      Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age

Type: boolean

Default: true

### 8.8.2. @age\_\_length[label].type=none

### 8.8.3. @age\_\_length[label].type=schnute

y1      Define the y1 parameter of the Schnute relationship

Type: estimable

Default: No Default

y2      Define the y2 parameter of the Schnute relationship

Type: estimable

Default: No Default

tau1      Define the  $\tau_1$  parameter of the Schnute relationship

Type: estimable

Default: No Default

tau2      Define the  $\tau_2$  parameter of the Schnute relationship

Type: estimable

Default: No Default

a      Define the  $a$  parameter of the Schnute relationship

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

**b** Define the  $b$  parameter of the Schnute relationship

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

**length\_weight** Define the label of the associated length-weight relationship

Type: string

Default: No Default

**by\_length** Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age

Type: boolean

Default: true

#### 8.8.4. @age\_\_length[label].type=von\_bertalanffy

**linf** Define the  $L_{infinity}$  parameter of the von Bertalanffy relationship

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

**k** Define the  $k$  parameter of the von Bertalanffy relationship

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

**t0** Define the  $t_0$  parameter of the von Bertalanffy relationship

Type: estimable

Default: No Default

**length\_weight** Define the label of the associated length-weight relationship

Type: string

Default: No Default

**by\_length** Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age

Type: boolean

Default: true

### 8.9. Length-weight

**@length.weight label** Define an object of type *length\_weight*

**label** The label of the length-weight relationship

Type: string  
Default: No Default

`type`     The type of the length-weight relationship  
Type: string  
Default: No Default

### 8.9.1. `@length_weight[label].type=basic`

- a     The *a* parameter in the basic length-weight relationship  
Type: constant  
Default: No Default
- b     The *b* parameter in the basic length-weight relationship  
Type: constant  
Default: No Default

`units`     Units of measure (tonnes, kgs, grams)  
Type: string  
Default: No Default  
Allowed Values: tonnes, kgs, grams

### 8.9.2. `@length_weight[label].type=none`

## 8.10. Selectivities

**`@selectivity label`**     Define an object of type *selectivity*

`label`     The label for this selectivity  
Type: string  
Default: No Default

`type`     The type of selectivity  
Type: string  
Default: No Default

`length_based`     Is the selectivity length based  
Type: boolean  
Default: false

`intervals`     Number of quantiles to evaluate a length based selectivity over the age length distribution  
Type: non-negative integer  
Default: 5

**8.10.1. @selectivity[label].type=all\_values**

v     V  
Type: estimable vector  
Default: No Default

**8.10.2. @selectivity[label].type=all\_values\_bounded**

l     L  
Type: non-negative integer  
Default: No Default

h     H  
Type: non-negative integer  
Default: No Default

v     V  
Type: estimable vector  
Default: No Default

**8.10.3. @selectivity[label].type=constant**

c     C  
Type: estimable  
Default: No Default

**8.10.4. @selectivity[label].type=double\_exponential**

x0    X0  
Type: estimable  
Default: No Default

x1    X1  
Type: constant  
Default: No Default

x2    X2  
Type: constant  
Default: No Default

y0    Y0  
Type: estimable  
Default: No Default

y1     Y1  
Type: estimable  
Default: No Default

y2     Y2  
Type: estimable  
Default: No Default

alpha    Alpha  
Type: estimable  
Default: 1.0

#### **8.10.5. @selectivity[label].type=double normal**

mu     Mu  
Type: estimable  
Default: No Default

sigma\_l    Sigma L  
Type: estimable  
Default: No Default

sigma\_r    Sigma R  
Type: estimable  
Default: No Default

alpha    Alpha  
Type: estimable  
Default: 1.0

#### **8.10.6. @selectivity[label].type=increasing**

l     Low  
Type: non-negative integer  
Default: No Default

h     High  
Type: non-negative integer  
Default: No Default

v     V  
Type: estimable vector  
Default: No Default

alpha     Alpha  
Type: constant  
Default: 1.0

#### **8.10.7. @selectivity[label].type=inverse\_logistic**

a50     A50  
Type: estimable  
Default: No Default

ato95     aTo95  
Type: estimable  
Default: No Default

alpha     Alpha  
Type: estimable  
Default: 1.0

#### **8.10.8. @selectivity[label].type=knife\_edge**

e     Edge  
Type: estimable  
Default: No Default

alpha     Alpha  
Type: estimable  
Default: 1.0

#### **8.10.9. @selectivity[label].type=logistic**

a50     A50  
Type: estimable  
Default: No Default

ato95     Ato95  
Type: estimable  
Default: No Default

alpha     Alpha  
Type: estimable  
Default: 1.0

#### 8.10.10. @selectivity[label].type=logistic\_producing

l Low  
 Type: non-negative integer  
 Default: No Default

h High  
 Type: non-negative integer  
 Default: No Default

a50 A50  
 Type: estimable  
 Default: No Default

ato95 Ato95  
 Type: estimable  
 Default: No Default

alpha Alpha  
 Type: estimable  
 Default: 1.0

### 9. Estimation command and subcommand syntax

#### 9.1. Estimation methods

**@estimate** *label* Define an object of type *estimate*

*label* The label of the estimate  
 Type: string  
 Default: ""

*type* The prior type for the estimate  
 Type: string  
 Default: No Default

*parameter* The name of the parameter to estimate in the model  
 Type: string  
 Default: No Default

*lower\_bound* The lower bound for the parameter  
 Type: constant  
 Default: No Default

*upper\_bound* The upper bound for the parameter



Type: constant  
Default: No Default

same      List of parameters that are constrained to have the same value as this parameter  
Type: string vector  
Default: ""

mcmc      Indicates if this parameter is fixed at the point estimate during an MCMC run  
Type: boolean  
Default: false

### 9.1.1. `@estimate[label].type=beta`

mu      Beta prior mean ( $\mu$ ) parameter  
Type: estimable  
Default: No Default

sigma      Beta prior variance ( $\sigma$ ) parameter  
Type: estimable  
Default: No Default  
Lower Bound: 0.0 (exclusive)

a      Beta prior lower bound of the range (A) parameter  
Type: constant  
Default: No Default

b      Beta prior upper bound of the range (B) parameter  
Type: constant  
Default: No Default

### 9.1.2. `@estimate[label].type=lognormal`

mu      The lognormal prior mean ( $\mu$ ) parameter  
Type: estimable  
Default: No Default  
Lower Bound: 0.0 (exclusive)

cv      The Lognormal variance (CV) parameter  
Type: estimable  
Default: No Default  
Lower Bound: 0.0 (exclusive)

### 9.1.3. `@estimate[label].type=normal`

`mu` The normal prior mean ( $\mu$ ) parameter

Type: estimable

Default: No Default

`cv` The normal variance (standard deviation) parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

### 9.1.4. `@estimate[label].type=normal_by_stdev`

`mu` The normal prior mean ( $\mu$ ) parameter

Type: estimable

Default: No Default

`sigma` The normal variance (standard deviation) parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

### 9.1.5. `@estimate[label].type=normal_log`

`mu` The normal-log prior mean ( $\mu$ ) parameter

Type: estimable

Default: No Default

`sigma` The normal-log prior variance (standard deviation) parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

### 9.1.6. `@estimate[label].type=uniform`

### 9.1.7. `@estimate[label].type=uniform_log`

## 9.2. Point estimation

`@minimiser label` Define an object of type *minimiser*

`label` The minimiser label

Type: string

Default: No Default

`type`      The type of minimiser to use  
Type: string  
Default: No Default

`active`     Indicates if this minimiser is active  
Type: boolean  
Default: false

`covariance`   Indicates if a covariance matrix should be generated  
Type: boolean  
Default: true

### 9.2.1. `@minimiser[label].type=adolc`

`iterations`    Maximum number of iterations  
Type: integer  
Default: 1000

`evaluations`   Maximum number of evaluations  
Type: integer  
Default: 4000

`tolerance`     Tolerance of the gradient for convergence  
Type: constant  
Default: 0.02

`step_size`     Minimum Step-size before minimisation fails  
Type: constant  
Default: 1e-7

### 9.2.2. `@minimiser[label].type=betadiff`

`iterations`    Maximum number of iterations  
Type: integer  
Default: 1000

`evaluations`   Maximum number of evaluations  
Type: integer  
Default: 4000

`tolerance`     Tolerance of the gradient for convergence  
Type: constant  
Default: 2e-3

### 9.2.3. @minimiser[label].type=cppad

### 9.2.4. @minimiser[label].type=de\_solver

population\_size      The number of candidate solutions to have in the population  
Type: non-negative integer  
Default: No Default

crossover\_probability      Define the minimisers crossover probability  
Type: constant  
Default: 0.9

difference\_scale      The scale to apply to new solutions when comparing candidates  
Type: constant  
Default: 0.02

max\_generations      The maximum number of iterations to run  
Type: non-negative integer  
Default: No Default

tolerance      The total variance between the population and best candidate before acceptance  
Type: constant  
Default: 0.01

method      The type of candidate generation method to use  
Type: string  
Default: ""  
Value: not\_yet\_implemented

### 9.2.5. @minimiser[label].type=dlib

### 9.2.6. @minimiser[label].type=numerical\_differences

iterations      Maximum number of iterations  
Type: integer  
Default: 1000

evaluations      Maximum number of evaluations  
Type: integer  
Default: 4000

tolerance      Tolerance of the gradient for convergence  
Type: constant  
Default: 0.02

`step_size` Minimum Step-size before minimisation fails  
Type: constant  
Default: 1e-7

### 9.3. Monte Carlo Markov Chain (MCMC)

**@mcmc** *label* Define an object of type *mcmc*

`label` The label of the MCMC  
Type: string  
Default: No Default

`type` The type of MCMC  
Type: string  
Default: ""

`length` The number of iterations in for the MCMC chain  
Type: non-negative integer  
Default: No Default

`active` Indicates if this is the active MCMC algorithm  
Type: boolean  
Default: true

`print_default_reports` Indicates if the output prints the default reports  
Type: boolean  
Default: true

`step_size` Initial stepsize (as a multiplier of the approximate covariance matrix)  
Type: constant  
Default: 0.02

#### 9.3.1. @mcmc[label].type=independence.metropolis

`start` Covariance multiplier for the starting point of the MCMC  
Type: constant  
Default: 0.0

`keep` Spacing between recorded values in the MCMC  
Type: non-negative integer  
Default: 1u

`max_correlation` Maximum absolute correlation in the covariance matrix of the proposal

distribution	
Type: constant	
Default: 0.8	
covariance_adjustment_method	Method for adjusting small variances in the covariance proposal matrix
Type: string	
Default: covariance	
correlation_adjustment_diff	Minimum non-zero variance times the range of the bounds in the covariance matrix of the proposal distribution
Type: constant	
Default: 0.0001	
proposal_distribution	The shape of the proposal distribution (either the t or the normal distribution)
Type: string	
Default: t	
df	Degrees of freedom of the multivariate t proposal distribution
Type: non-negative integer	
Default: 4	
adapt_stepsize_at	Iterations in the chain to check and resize the MCMC stepsize
Type: non-negative integer vector	
Default: true	
adapt_covariance_matrix_at	Iterations in the chain to check and resize the MCMC stepsize
Type: non-negative integer vector	
Default: true	
adapt_stepsize_method	Method to adapt step size.
Type: string	
Default: ratio	
Allowed Values: ratio, double_half	

## 9.4. Profiles

<b>@profile</b> <i>label</i>	Define an object of type <i>profile</i>
<i>label</i>	Label
Type: string	
Default: ""	
steps	The number of steps to take between the lower and upper bound

Type: non-negative integer  
Default: No Default

`lower_bound`      The lower bounds  
Type: constant  
Default: No Default

`upper_bound`      The upper bounds  
Type: constant  
Default: No Default

`parameter`      The system parameter to profile  
Type: string  
Default: No Default

## 9.5. Defining catchability constants

**@catchability** *label*      Define an object of type *catchability*

`label`      Label of the catchability  
Type: string  
Default: No Default

`type`      Type of catchability  
Type: string  
Default: No Default

### 9.5.1. @catchability[label].type=free

`q`      value of the catchability  
Type: estimable  
Default: No Default

### 9.5.2. @catchability[label].type=nuisance

## 9.6. Defining penalties

**@penalty** *label*      Define an object of type *penalty*

`label`      The label of the penalty  
Type: string  
Default: No Default

`type`      The type of penalty

Type: string  
 Default: No Default

### 9.6.1. @penalty[label].type=process

`multiplier`     The penalty multiplier  
 Type: constant  
 Default: 1.0

`log_scale`     Indicates if the sums of squares is calculated on the log scale  
 Type: boolean  
 Default: false

## 9.7. Defining priors on parameter ratios, differences, and means

**@additional\_prior** *label*     Define an object of type *additional\_prior*

`label`     Label for the additional prior  
 Type: string  
 Default: No Default

`type`     Type of additional prior  
 Type: string  
 Default: No Default

### 9.7.1. @additional\_\_prior[label].type=beta

`mu`     Beta distribution mean ( $\mu$ ) parameter  
 Type: constant  
 Default: No Default

`sigma`     Beta distribution variance ( $\sigma$ ) parameter  
 Type: constant  
 Default: No Default  
 Lower Bound: 0.0 (inclusive)

`a`     Beta distribution lower bound of the range (A) parameter  
 Type: constant  
 Default: No Default

`b`     Beta distribution upper bound of the range (B) parameter  
 Type: constant  
 Default: No Default



**9.7.2. @additional\_prior[label].type=vector\_average**

parameter      Name of the parameter to generate additional prior on

Type: string

Default: No Default

method      What calculation method to use, either k, l, or m

Type: string

Default: k

k      K Value to use in the calculation

Type: constant

Default: No Default

multiplier      Multiplier for the penalty amount

Type: constant

Default: 1

**9.7.3. @additional\_prior[label].type=vector\_smoothing**

parameter      Name of the parameter to generate additional prior on

Type: string

Default: No Default

log\_scale      Should sums of squares be calculated on the log scale?

Type: boolean

Default: false

multiplier      Multiply the penalty by this factor

Type: constant

Default: 1

lower\_bound      First element to apply the penalty to in the vector

Type: non-negative integer

Default: 0u

upper\_bound      Last element to apply the penalty to in the vector

Type: non-negative integer

Default: 0u

r      Penalty applied to rth differences

Type: non-negative integer

Default: 2u

## 10. Observation command and subcommand syntax

### 10.1. Observation types

The observation types available are,

Observations of proportions of individuals by age class

Observations of proportions of individuals between categories within each age class

Relative and absolute abundance observations

Relative and absolute biomass observations

Each type of observation requires a set of subcommands and arguments specific to that process.

**@observation** *label*     Define an object of type *observation*

*label*     Label

Type: string

Default: No Default

*type*     Type of observation

Type: string

Default: No Default

*likelihood*     Type of likelihood to use

Type: string

Default: No Default

*categories*     Category labels to use

Type: string vector

Default: true

*simulation\_likelihood*     Simulation likelihood to use

Type: string

Default: ""

*likelihood\_multiplier*     Likelihood score multiplier

Type: constant

Default: 1.0

*error\_value\_multiplier*     Error value multiplier for likelihood

Type: constant

Default: 1.0

**10.1.1. @observation[label].type=process\_abundance**

selectivities      Labels of the selectivities

Type: string vector

Default: true

time\_step      The label of time-step that the observation occurs in

Type: string

Default: No Default

catchability      The label of the catchability (q) block assumed for this observation

Type: string

Default: No Default

obs      The observed values

Type: string vector

Default: No Default

years      The years of the observed values

Type: non-negative integer vector

Default: No Default

error\_value      The error values of the observed values (note the units depend on the likelihood)

Type: constant vector

Default: No Default

delta      Robustification value (delta) for the likelihood

Type: constant

Default: DELTA

process\_error      The label of the process error

Type: constant

Default: 0.0

process      The label of the process for the observation

Type: string

Default: No Default

process\_proportion      Proportion through the process when the observation is evaluated

Type: constant

Default: 0.5

### 10.1.2. @observation[label].type=abundance

selectivities      Labels of the selectivities

Type: string vector

Default: true

time\_step      The label of time-step that the observation occurs in

Type: string

Default: No Default

catchability      The label of the catchability coefficient (q) assumed

Type: string

Default: No Default

obs      The observed values

Type: string vector

Default: No Default

years      Years for which there are observations

Type: non-negative integer vector

Default: No Default

error\_value      The error values of the observed values (note the units depend on the likelihood)

Type: constant vector

Default: No Default

delta      The value of the delta robustification parameter

Type: constant

Default: DELTA

process\_error      The label of the process error block

Type: constant

Default: 0.0

time\_step\_proportion      Proportion through the mortality block of the time step when the observation is evaluated

Type: constant

Default: 0.5

### 10.1.3. @observation[label].type=process\_biomass

catchability      The time-step of the observation

Type: string

Default: No Default

`time_step`     The label of time-step that the observation occurs in

Type: string

Default: No Default

`obs`     The observed values

Type: string vector

Default: No Default

`years`     The years of the observed values

Type: non-negative integer vector

Default: No Default

`error_value`     The error values of the observed values (note the units depend on the likelihood)

Type: constant vector

Default: No Default

`delta`     Robustification value (delta) for the likelihood

Type: constant

Default: 1e-10

`selectivities`     Labels of the selectivities

Type: string vector

Default: true

`process_error`     Value for process error

Type: constant

Default: 0.0

`process`     The label of the process for the observation

Type: string

Default: No Default

`process_proportion`     Proportion through the process when the observation is evaluated

Type: constant

Default: 0.5

#### **10.1.4. @observation[label].type=biomass**

`catchability`     The time-step of the observation

Type: string

Default: No Default

`time_step`     The label of time-step that the observation occurs in

Type: string

Default: No Default

obs      The observed values

Type: string vector

Default: No Default

years    The years of the observed values

Type: non-negative integer vector

Default: No Default

error\_value    The error values of the observed values (note the units depend on the likelihood)

Type: constant vector

Default: No Default

delta      Robustification value (delta) for the likelihood

Type: constant

Default: 1e-10

selectivities    Labels of the selectivities

Type: string vector

Default: true

process\_error    Value for process error

Type: constant

Default: 0.0

time\_step\_proportion    Proportion through the mortality block of the time step when the observation is evaluated

Type: constant

Default: 0.5

#### **10.1.5. @observation[label].type=process\_removals\_by\_age**

min\_age    Minimum age

Type: non-negative integer

Default: No Default

max\_age    Maximum age

Type: non-negative integer

Default: No Default

age\_plus    Use age plus group

Type: boolean

Default: true

`time_step`      The label of time-step that the observation occurs in  
Type: string vector  
Default: No Default

`tolerance`      Tolerance  
Type: constant  
Default: 0.001

`years`      Years for which there are observations  
Type: non-negative integer vector  
Default: No Default

`delta`      Robustification value (delta) for the likelihood  
Type: constant  
Default: DELTA

`process_errors`      Label of process error to use  
Type: constant vector  
Default: true

`ageing_error`      Label of ageing error to use  
Type: string  
Default: ""

`method_of_removal`      Label of observed method of removals  
Type: string vector  
Default: ""

`mortality_instantaneous_process`      The label of the mortality instantaneous process for the observation  
Type: string  
Default: No Default

#### **10.1.6. @observation[label].type=process\_removals\_by\_length**

`length_bins`      Length bins  
Type: constant vector  
Default: No Default

`time_step`      Time step to execute in  
Type: string  
Default: No Default

`length_plus_group`      Is the last bin a plus group

Type: boolean

Default: true

tolerance      Tolerance for rescaling proportions

Type: constant

Default: 0.001

years      Years for which there are observations

Type: non-negative integer vector

Default: No Default

delta      The value of the delta robustification parameter

Type: constant

Default: DELTA

process\_errors      the value of process error

Type: constant vector

Default: true

method\_of\_removal      Label of observed method of removals

Type: string

Default: ""

mortality\_instantaneous\_process      The label of the mortality instantaneous process for the observation

Type: string

Default: No Default

### 10.1.7. `@observation[label].type=process_proportions_at_age`

min\_age      Minimum age

Type: non-negative integer

Default: No Default

max\_age      Maximum age

Type: non-negative integer

Default: No Default

age\_plus      Use age plus group

Type: boolean

Default: true

time\_step      The label of time-step that the observation occurs in

Type: string

Default: No Default



`tolerance`      Tolerance on the constraint, that for each year the sum of proportions in each age must equal one e.g. `tolerance = 0.1` then `1 - Sum(Proportions)` can be as great as 0.1

Type: constant

Default: 0.001

`years`      The years of the observed values

Type: non-negative integer vector

Default: No Default

`delta`      Robustification value (delta) for the likelihood

Type: constant

Default: DELTA

`selectivities`      Labels of the selectivities

Type: string vector

Default: true

`process_errors`      Process error

Type: constant vector

Default: true

`ageing_error`      Label of ageing error to use

Type: string

Default: ""

`process`      The label of the process for the observation

Type: string

Default: No Default

`process_proportion`      Proportion through the process when the observation is evaluated

Type: constant

Default: 0.5

### 10.1.8. `@observation[label].type=proportions_at_age`

`min_age`      Minimum age

Type: non-negative integer

Default: No Default

`max_age`      Maximum age

Type: non-negative integer

Default: No Default

`age_plus`      Use age plus group

Type: boolean

Default: true

`time_step`      The label of time-step that the observation occurs in

Type: string

Default: No Default

`tolerance`      Tolerance on the constraint, that for each year the sum of proportions in each age must equal one e.g. `tolerance = 0.1` then  $1 - \text{Sum}(\text{Proportions})$  can be as great as 0.1

Type: constant

Default: 0.001

`years`      The years of the observed values

Type: non-negative integer vector

Default: No Default

`delta`      Robustification value (delta) for the likelihood

Type: constant

Default: DELTA

`selectivities`      Labels of the selectivities

Type: string vector

Default: true

`process_errors`      Process error

Type: constant vector

Default: true

`ageing_error`      Label of ageing error to use

Type: string

Default: ""

`time_step_proportion`      Proportion through the mortality block of the time step when the observation is evaluated

Type: constant

Default: 0.5

### **10.1.9. `@observation[label].type=process_proportions_at_length`**

`length_bins`      Length bins

Type: constant vector

Default: No Default

`time_step`      The label of time-step that the observation occurs in

Type: string  
Default: No Default

length\_plus\_group      Is the last bin a plus group  
Type: boolean  
Default: true

tolerance      Tolerance for rescaling proportions  
Type: constant  
Default: 0.001

years      Years for which there are observations  
Type: non-negative integer vector  
Default: No Default

selectivities      The labels of the selectivities  
Type: string vector  
Default: true

delta      The value of the delta robustification parameter  
Type: constant  
Default: DELTA

process\_errors      Process error  
Type: constant vector  
Default: true

process      The label of the process for the observation  
Type: string  
Default: No Default

process\_proportion      Proportion through the process when the observation is evaluated  
Type: constant  
Default: 0.5

#### **10.1.10. @observation[label].type=proportions at length**

length\_bins      Length bins  
Type: constant vector  
Default: No Default

time\_step      The label of time-step that the observation occurs in  
Type: string  
Default: No Default

`length_plus_group`      Is the last bin a plus group  
Type: boolean  
Default: true

`tolerance`      Tolerance for rescaling proportions  
Type: constant  
Default: 0.001

`years`      Years for which there are observations  
Type: non-negative integer vector  
Default: No Default

`selectivities`      The labels of the selectivities  
Type: string vector  
Default: true

`delta`      The value of the delta robustification parameter  
Type: constant  
Default: DELTA

`process_errors`      Process error  
Type: constant vector  
Default: true

`time_step_proportion`      Proportion through the mortality block of the time step when the observation is evaluated  
Type: constant  
Default: 0.5

#### **10.1.11. `@observation[label].type=process_proportions_by_category`**

`min_age`      Minimum age  
Type: non-negative integer  
Default: No Default

`max_age`      Maximum age  
Type: non-negative integer  
Default: No Default

`time_step`      The label of time-step that the observation occurs in  
Type: string  
Default: No Default

`age_plus`      Use age plus group

Type: boolean

Default: true

years      Years for which there are observations

Type: non-negative integer vector

Default: No Default

selectivities      The labels of the selectivities

Type: string vector

Default: true

categories2      Target Categories

Type: string vector

Default: No Default

selectivities2      Target Selectivities

Type: string vector

Default: No Default

delta      The value of the delta robustification parameter

Type: constant

Default: DELTA

Lower Bound: 0.0 (exclusive)

process\_errors      Process error

Type: constant vector

Default: true

process      The label of the process for the observation

Type: string

Default: No Default

process\_proportion      Proportion through the mortality block of the time step when the observation is evaluated

Type: constant

Default: 0.5

#### **10.1.12. @observation[label].type=proportions\_by\_category**

min\_age      Minimum age

Type: non-negative integer

Default: No Default

max\_age      Maximum age

Type: non-negative integer  
Default: No Default

`time_step`      The label of time-step that the observation occurs in  
Type: string  
Default: No Default

`age_plus`      Use age plus group  
Type: boolean  
Default: true

`years`      Years for which there are observations  
Type: non-negative integer vector  
Default: No Default

`selectivities`      The labels of the selectivities  
Type: string vector  
Default: true

`categories2`      Target Categories  
Type: string vector  
Default: No Default

`selectivities2`      Target Selectivities  
Type: string vector  
Default: No Default

`delta`      The value of the delta robustification parameter  
Type: constant  
Default: DELTA  
Lower Bound: 0.0 (exclusive)

`process_errors`      Process error  
Type: constant vector  
Default: true

`time_step_proportion`      Proportion through the time step to analyse the partition from  
Type: constant  
Default: 0.5

### **10.1.13. `@observation[label].type=proportions_migrating`**

`min_age`      Minimum age  
Type: non-negative integer  
Default: No Default

`max_age`      Maximum age

Type: non-negative integer

Default: No Default

`time_step`      The label of time-step that the observation occurs in

Type: string

Default: No Default

`age_plus`      Use age plus group

Type: boolean

Default: true

`years`      Years for which there are observations

Type: non-negative integer vector

Default: No Default

`delta`      The value of the delta robustification parameter

Type: constant

Default: DELTA

`process_errors`      Process error

Type: constant vector

Default: true

`ageing_error`      Label of ageing error to use

Type: string

Default: ""

`process`      Process label

Type: string

Default: No Default

#### **10.1.14. `@observation[label].type=tag_recapture_by_age`**

`min_age`      Minimum age

Type: non-negative integer

Default: No Default

`max_age`      Maximum age

Type: non-negative integer

Default: No Default

`age_plus`      Use age plus group

Type: boolean

Default: true

years      Years for which there are observations

Type: non-negative integer vector

Default: No Default

categories2      The available categories in the partition

Type: string vector

Default: No Default

selectivities      The labels of the selectivities

Type: string vector

Default: true

time\_step      The label of time-step that the observation occurs in

Type: string

Default: No Default

selectivities2      The categories of tagged individuals for the observation

Type: string vector

Default: No Default

delta      The value of the delta robustification parameter

Type: constant

Default: DELTA

Lower Bound: 0.0 (exclusive)

process\_errors      Process error

Type: constant vector

Default: true

detection      Probability of detecting a recaptured individual

Type: constant

Default: No Default

time\_step\_proportion      Proportion through the mortality block of the time step when the observation is evaluated

Type: constant

Default: 0.5



**10.1.15. @observation[label].type=tag\_recapture\_by\_length**

length\_bins      Length Bins

Type: constant vector

Default: No Default

plus\_group      Indicates if the last length bin is a plus group

Type: boolean

Default: true

years      Years for which there are observations

Type: non-negative integer vector

Default: No Default

time\_step      The label of time-step that the observation occurs in

Type: string

Default: No Default

categories2      The categories of tagged individuals for the observation

Type: string vector

Default: No Default

selectivities      The labels of the selectivities

Type: string vector

Default: true

selectivities2      The labels of the tag category selectivities

Type: string vector

Default: No Default

delta      The value of the delta robustification parameter

Type: constant

Default: DELTA

Lower Bound: 0.0 (exclusive)

process\_errors      Process error

Type: constant vector

Default: true

detection      Probability of detecting a recaptured individual

Type: constant

Default: No Default

dispersion      Over-dispersion parameter ( $\phi$ )

Type: constant

Default: 1.0

`time_step_proportion`      Proportion through the mortality block of the time step when the observation is evaluated  
Type: constant  
Default: 0.5

## 10.2. Likelihoods

**@likelihood** *label*      Define an object of type *likelihood*

**10.2.1. @likelihood[label].type=binomial**

**10.2.2. @likelihood[label].type=binomial\_approx**

**10.2.3. @likelihood[label].type=dirichlet**

**10.2.4. @likelihood[label].type=log\_normal**

**10.2.5. @likelihood[label].type=log\_normal\_with\_q**

**10.2.6. @likelihood[label].type=multinomial**

**10.2.7. @likelihood[label].type=normal**

**10.2.8. @likelihood[label].type=pseudo**

## 10.3. Defining ageing error

The methods for including ageing error into estimation with observations are,

- None
- Data
- Normal
- Off-by-one

Each type of ageing error requires a set of subcommands and arguments specific to its type.

**@ageing\_error** *label*      Define an object of type *ageing\_error*

*label*      Label of the ageing error  
Type: string  
Default: No Default

*type*      Type of ageing error  
Type: string  
Default: No Default

**10.3.1. @ageing\_error[label].type=data****10.3.2. @ageing\_error[label].type=none****10.3.3. @ageing\_error[label].type=normal**

cv CV of the misclassification matrix

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

k k defines the minimum age of individuals which can be misclassified, e.g., individuals of age less than k have no ageing error

Type: non-negative integer

Default: 0u

**10.3.4. @ageing\_error[label].type=off\_by\_one**

p1 proportion misclassified as one year younger, e.g., the proportion of age 3 individuals that were misclassified as age 2

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

p2 proportion misclassified as one year older, e.g., the proportion of age 3 individuals that were misclassified as age 4

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

p2 proportion misclassified as one year older, e.g., the proportion of age 3 individuals that were misclassified as age 4

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

k The minimum age of fish which can be misclassified, i.e., fish of age less than k are assumed to be correctly classified

Type: non-negative integer

Default: 0u

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

k The minimum age of fish which can be misclassified, i.e., fish of age less than k are assumed

to be correctly classified  
Type: non-negative integer  
Default: 0u  
Lower Bound: 0.0 (inclusive)  
Upper Bound: 1.0 (inclusive)

## 11. Report command and subcommand syntax

### 11.1. Report commands and subcommands

**@report** *label* Define an object of type *report*

*label* The label for the report  
Type: string  
Default: No Default

*type* The type of report  
Type: string  
Default: No Default

*file.name* The File Name if you want this report to be in a seperate file  
Type: string  
Default: ""

*write.mode* The write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental.suffix

#### 11.1.1. @report [*label*].type=ageing\_error\_matrix

*ageing\_error* Ageing Error label  
Type: string  
Default: No Default

**11.1.2. @report[label].type=catchabilities**

**11.1.3. @report[label].type=category\_info**

**11.1.4. @report[label].type=category\_list**

**11.1.5. @report[label].type=correlation\_matrix**

**11.1.6. @report[label].type=covariance\_matrix**

**11.1.7. @report[label].type=derived\_quantity**

**11.1.8. @report[label].type=estimable**

parameter      Parameter to print

Type: string

Default: No Default

years      Years to print the estimable for

Type: non-negative integer vector

Default: No Default

time\_step      Time Step label

Type: string

Default: ""

**11.1.9. @report[label].type=estimate\_summary**

**11.1.10. @report[label].type=estimate\_value**

**11.1.11. @report[label].type=hessian\_matrix**

**11.1.12. @report[label].type=initialisation\_partition**

**11.1.13. @report[label].type=mcmc\_covariance**

**11.1.14. @report[label].type=mcmc\_objective**

**11.1.15. @report[label].type=mcmc\_sample**

**11.1.16. @report[label].type=m.p.d**

**11.1.17. @report[label].type=objective\_function**

**11.1.18. @report[label].type=observation**

observation      Observation label

Type: string

Default: No Default

**11.1.19. @report[label].type=output\_parameters**

**11.1.20. @report[label].type=partition**

time\_step      Time Step label

Type: string

Default: ""

years      Years

Type: non-negative integer vector

Default: true

**11.1.21. @report[label].type=partition\_biomass**

time\_step      Time Step label

Type: string

Default: ""

years      Years

Type: non-negative integer vector

Default: true

---

units      Units (Default Kgs)  
Type: string  
Default: kgs

#### **11.1.22. @report [label] .type=partition\_mean\_weight**

time\_step      Time Step label  
Type: string  
Default: ""

years      Years  
Type: non-negative integer vector  
Default: true

#### **11.1.23. @report [label] .type=process**

process      Process label that is reported  
Type: string  
Default: ""

#### **11.1.24. @report [label] .type=random\_number\_seed**

#### **11.1.25. @report [label] .type=selectivity**

selectivity      Selectivity name  
Type: string  
Default: No Default

#### **11.1.26. @report [label] .type=simulated\_observation**

observation      Observation label  
Type: string  
Default: No Default

#### **11.1.27. @report [label] .type=standard\_header**

#### **11.1.28. @report [label] .type=time\_varying**

### **12. Including commands from other files**

**@include** *file*      Include an external file

*file*     The name of the external file to include

Type: string

Default: No default

Value: A valid external file

Condition: The file name must be enclosed in double quotes

Example: `@include "my_file.csl2"`

Note: `@include` does not denote the end of the previous command block as is the case for all other commands



---

## 13. Examples

### 13.1. Input File Specification

The file format used for CASAL2 is based on the formats used for CASAL and SPM. It's a standard text file that contains definitions organised into blocks.

Without exception, every object specified in a configuration file is part of a block. At the top level blocks have a one-to-one relationships with components in the system.

Example:

```
@block1 label
parameter value
parameter value_1 value 2
```

```
@block2 label
parameter value
table table_name
column_1 column_2
data_1 data_2
data_3 data_4
end_table
```

Some general notes about writing configuration files:

1. Whitespace can be used freely. Tabs and spaces are both accepted
2. A block ends only at the beginning of a new block or end of final configuration file
3. You can include another configuration file from anywhere
4. Included files are placed inline, so you can continue a block in a new file
5. The configuration files support inline declarations of objects

#### 13.1.1. Keywords And Reserved Characters

In order to allow efficient creation of input files CASAL2's file format contains special keywords and characters that cannot be used for labels etc.

##### @Block Definitions

Every new block in the configuration file must start with a block definition character. The reserved character for this is the @character

Example:

```
@block1 <label>
type <type>
```

```
@block2 <label>
type <type>
```

##### 'type' Keyword

The 'type' keyword is used for declaring the sub-type of a defined block. Any block object that has multiple sub-types will use the type keyword.

Example:

```
@block1 <label>
type <sub_type>
```

```
@block2 <label>
type <sub_type>
```

### # (Single-Line Comment)

Comments are supported in the configuration file in either single-line (to end-of-line) or multi-line Example:

```
@block <label>
type <sub_type> #Descriptive comment
#parameter <value_1> This whole line is commented out
parameter <value_1> #<value_2>(value_2 is commented out)
```

### { } (Multi-Line Comment)

Multiple line comments are supported by surrounding the comments in { and } Example:

```
@block <label>
type <sub_type>
parameter <value_1>
parameter <value_1> <value_2>

{ Do not load this process
@block <label>
type <sub_type>
parameter <value_1>
parameter <value_1> <value_2>
}
```

### ':' (Range Specifier)

The range specifier allows you to specify a range of values at once instead of having to input them manually. Ranges can be either incremental or decremental.

Example:

```
@process my_recruitment_process
type constant_recruitment
years_to_run 1999:2009 #With range specifier

@process my_mortality_process
type natural_mortality
years_to_run 2000 2001 2002 2003 2004 2005 2006 2007 #Without range specifier
```

### ',' (List Specifier)

When a parameter supports multiple values in a single entry you can use the list specifier to supply multiple values as a single parameter.

Example:

```
@categories
format sex.stage
names male,female.immature,mature #With list specifier

@categories
format sex.stage
names male,immature male,mature female.immature female,mature #Without list specifier
```

### 'table' and 'end\_table' Keyword

The table keyword is used to define a table of information used as a parameter. The line following the table declaration must contain a list of columns to be used. Following lines are rows of the table. Each row must have the same number of values as the number of columns specified. The table definition must end with the 'end\_table' keyword on it's own line. The first row of a table will be the name of the columns if required.

Example:

```
@block <label>
type <sub_type>
parameter <value_1>
table <table_label>
<column_1> <column_2> <column_n>
<row1_value1> <row1_value2> <row1_valueN>
<row2_value1> <row2_value2> <row2_valueN>
end_table
```

### [ ] (Inline Declarations)

When an object takes the label of a target object as a parameter this can be replaced with an inline declaration. An inline declaration is a complete declaration of an object one 1 line. This is designed to allow the configuration writer to simplify the configuration writing process.

Example:

```
#With inline declaration with label specified for time step
@model
time_steps step_one=[type=iterative; processes=recruitment ageing]

#With inline declaration with default label (model.1)
@model
time_steps [type=iterative; processes=recruitment ageing]

#Without inline declaration
@model
time_steps step_one

@time_step step_one
processes recruitment ageing
```

### Categories

The CASAL2 model is essentially a 2-dimensional model. The model partition is: Categories x Ages/Lengths.

Each category supports the ability to have a different range of ages/lengths and accessibility



```
!include "Observation.csl2"  
!include "estimation.csl2"
```

Breaking up a CASAL2 model into sections is recommended, as it aids in readability and error checking. `population.csl2` contains the population information. The model runs from 1975-2012 and is initialised over a 120 year period prior to 1975, which applies the following processes,

1. A Beverton-Holt recruitment process, recruiting a constant number of individuals to the first age class (i.e.,  $age = 1$ ).
2. A constant mortality process representing natural mortality( $M$ ). This process is repeated in all three time steps, so that each with its own time step proportion of  $M$  applied.
3. An ageing process, where all individuals are aged by one year, and with a plus group accumulator age class at  $age = 30$ .

Following initialisation, the model runs from the years 1975 to 2012 iterating through two time-steps. The first time-step applies processes of recruitment, and  $\frac{1}{2}M_1 + F + \frac{1}{2}M_1$  processes, where  $M_1$  is the proportion of  $M$  applied in the first time step. The exploitation process (fishing) is applied in the years 1975–2012. Catches are defined in the catches table and attribute information on each fishery such as selectivity and time-step they are implemented are in the fisheries table in the `@process` block.

The second time-step applies an age increment and the remaining natural mortality.

The first 28 lines of the main section of the `population.csl2` are,

```
## Model Block
@model
start_year 1975
final_year 2012
min_age 1
max_age 30
age_plus true
base_weight_units kgs
initialisation_phases iphasel
time_steps step1 step2

## Category Block
@categories
format
names stock
age_lengths age_size

## Initialisation block
@initialisation_phase iphasel
type iterative
years 120

## Annual Cycle definition
@time_step step1
processes Recruitment instant_mort

@time_step step2
processes Ageing instant_mort
```

To carry out a run of the model (to verify that the model runs without any syntax errors), use the command `casal2 -r`. Note that as CASAL2 looks for a file named `casal2.txt` by default, we can override this. Hypothetically speaking if our model was all written in `Mymodel.txt` we could call it using the `-c` command like `casal2 -r -c Mymodel.txt`.

To run an estimation, and hence estimate the parameters defined in the file `estimation.cs12` (the catchability constant  $q$ , recruitment  $R_0$ , and the selectivity parameters  $a_{50}$  and  $a_{t095}$ ), use `casal2 -e`. Here, we have piped the output to `estimate.log` using the command `casal2 -e > estimate.log`, reports the user defined reports `reports.cs12` from the final iteration of the estimation, and successful convergence printed to screen,

```
Total elapsed time: 1 second
Completed
```

The main part of the output from the estimation run is summarised in the file `estimate.log`, and the final MPD parameter values can be piped out as a separate report, in this case named `paramaters.out`, using the command `casal2 -e -o paramaters.out > estimate.log`.

A profile on the  $R_0$  parameter can also be run, using `casal2 -p > profile.log`. See the examples folder for an example of the output.

### 13.3. More examples of shorthand syntax and use of CASAL2's reserved and key characters

#### Categories

CASAL2 allows many user defined categories so shorthand syntax has been added to aid in the readability of complex configuration scripts and partition structures. For example when defining

categories you can use a comma for shortening lists of categories. The following syntax is how we would specify the categories the long way.

```
@categories
format sex.stage
names male,immature male,mature female,immature female,mature
```

for the exact same partition structure but specified in a shorter way users could define the categories as, (note the use of the list character ','),

```
@categories
format sex.stage
names male,female,immature,mature
```

CASAL2 asks for categories in processes and observations so that it can apply the right model dynamics to the right elements of the partition. For the same reason as defining categories shorthand syntax aids in readability and input management. An example of a process where categories need to be supplied as an input command is in ageing,

```
# 1. The standard way
@ageing my_ageing
categories male,immature male,mature female,immature female,mature

# 2. The 1st short-hand way
@ageing my_ageing
categories male,female,immature,mature

# 3. Wild Card (all categories)
@ageing my_ageing
categories *

# 4. The 2nd short-hand way
@ageing my_ageing
categories sex=male sex=female
```

Sometimes in observations we want to amalgamate categories together for example if we had a biomass estimate of the population that was made up of both males and females in the population you can specify this using the + special character, for example

```
@observation CPUE
type biomass
catchability Fishq
time_step one
categories male+female
selectivities FishSel
likelihood lognormal
years 1992:2001
time_step_proportion 1.0
obs 1.50 1.10 0.93 1.33 1.53 0.90 0.68 0.75 0.57 1.23
error_value 0.35
```

Shorthand syntax can be useful when applying processes to a select group of categories from the partition, for example. If we wanted to apply a spawning migration to the mature categories in the partition and the partition was defined by the categories below,

```
@categories
format area.maturity.tag
names north.immature.notag,2011 north.mature.notag,2011 south.immature.notag,2011
south.mature.notag,2011
```

If we wanted to migrate a portion of the mature population from the southern area to the northern area you could use the following syntax,

```
@process spawn_migration
type transition_category
from format=south.mature.*
to format=north.mature.*
proportions 1.0
selectivities One
```

### Parameters

CASAL2 also allows parameters that are of type vector or map to be referenced and estimated partially. An example of a parameter that is type vector is `ycs_values` in a recruitment process. Let say a recruitment block was specified as follows,

```
@process WestRecruitment
type recruitment_beverton_holt
r0 400000
years
ycs_values 1 1 1 1 1 1 1 1
```

An alternative specification to the sequence of values you can use an astrix to shorthand repeating integers e.g.

```
ycs_values 1*8
```

```
steepness 0.9
age 1
```

Lets say we wanted to only estimate the last four values of the parameter `process[WestRecruitment].ycs_values` vector. This can be done as specified in the following **@estimate block**,

```
@estimate
parameter process[WestRecruitment].ycs_values(5:8)
type uniform
lower_bound 0.1 0.1 0.1 0.1
upper_bound 10 10 10 10
```

Note the first element of a vector is indexed by 1. This syntax can be applied to parameters that are of type map as well, for information on what type a parameter is see the syntax section. An example of a parameter that is of type map is `@time_varying[label].type=constant`. For the following **@time\_varying block**,

```
@time_varying q_step1
type constant
parameter catchability[Fishq].q
years 1992 1993 1994 1995
value 0.2 0.2 0.2 0.2
```



In this example a user may want to estimate only one element of the map (say 1992), but force all other years to be the same as the one estimate. This can be done in an estimate block as follows,

```
@estimate
parameter time_varying[q_step1].value(1992)
same time_varying[q_step1].value(1993:1995)
type uniform
lower_bound 0.1 0.1 0.1 0.1
upper_bound 10 10 10 10
```

### **In line declaration**

In line declarations can help shorten models by passing @ blocks, for example

```
@observation chatCPUE
type biomass
catchability [q=6.52606e-005]
time_step one
categories male+female
selectivities chatFselMale chatFselFemale
likelihood lognormal
years 1992:2001
time_step_proportion 1.0
obs 1.50 1.10 0.93 1.33 1.53 0.90 0.68 0.75 0.57 1.23
error_value 0.35
```

```
@estimate
parameter catchability[chatTANbiomass.one].q
type uniform_log
lower_bound 1e-2
upper_bound 1
In line declaration tips
```

In the above code we are defining and estimating catchability without explicitly creating an @catchability block

When you do an inline declaration the new object will be created with the name of the creator's label.index where index will be the word if it's one-nine and the number if it's 10+, for example

```
@mortality halfm
selectivities [type=constant; c=1]

would create
@selectivity halfm.one
```

if there were 10 categories all with there own selectivity the 10<sup>th</sup> selectivity would be labelled;

```
@selectivity halfm.10
```



---

## 14. Post processing output using R

In the downloaded bundle is a R-package that reads CASAL2 output into R. The CASAL2 package has one key function `extract()`.

This function will read and process CASAL2 output files into R.

CASAL2 output is written so that each `@report` will start with a `*` and end with `*end`. Users can use this format as the basis to construct R or other functions that read CASAL2 output to identify and read individual reports for post-processing.



---

## 15. Troubleshooting

### 15.1. Introduction

### 15.2. Reporting errors

If you find a bug or problem in CASAL2, please let the Development Team know by contacting them at [casal2@niwa.co.nz](mailto:casal2@niwa.co.nz) or by submitting an issue on the github repository found at <https://github.com/NIWAFisheriesModelling/CASAL2/issues>. The latter is preferred as it will document the issue better than the development team does. Please follow the guidelines below will assist the Development Team identify and resolve any issues.

### 15.3. Guidelines for reporting a problem with CASAL2

1. Check to ensure you are using the most recent version of CASAL2. Its possible that the error or problem you are having may have ready been resolved.
2. Describe the version of CASAL2 are you using? e.g., CASAL2 v2016-09-03Microsoft Windows executable”
3. What operating system or environment are you using? e.g., “IBM-PC Intel CPU running Microsoft Windows 10 Enterprise”.
4. Give a brief one-line description of the problem, e.g., “a segmentation fault was reported”.
5. If the problem is reproducible, please list the exact steps required to cause it, remembering to include the relevant CASAL2 configuration file, other input files, and any out generated. Specify the *exact* command line arguments that were used, e.g., “Using the command `***. -*` reports a segmentation fault. The input configuration files are attached.”
6. If the problem is not reproducible (only happened once, or occasionally for no apparent reason), please describe the circumstances in which it occurred and the symptoms observed (but note it is much harder to reproduce and hence fix non-reproducible bugs, but if several reports are made over time that relate to the same thing, then this may help to track down the problem), e.g., “CASAL2 crashed, but I cannot reproduce how I did it. It seemed to be related to a local network crash but I cannot be sure.”
7. If the problem causes any error messages to appear, please give the *exact* text displayed, e.g., segmentation fault (core dumped).
8. Remember to attach all relevant input and output files so that the problem can be reproduced (it can helpful to compress these into a single file). Without these, it is usually not possible to determine the cause of the problem, and we are unlikely to provide any assistance. Note that it is helpful to be as specific as possible when describing the problem.



---

## 16. CASAL2 software license

### GNU GENERAL PUBLIC LICENSE

Copyright © 1989, 1991 Free Software Foundation, Inc.

51 Franklin Street, Fifth Floor, Boston, MA 02110-1301, USA

Everyone is permitted to copy and distribute verbatim copies of this license document, but changing it is not allowed.

#### Preamble

The licenses for most software are designed to take away your freedom to share and change it. By contrast, the GNU General Public License is intended to guarantee your freedom to share and change free software—to make sure the software is free for all its users. This General Public License applies to most of the Free Software Foundation’s software and to any other program whose authors commit to using it. (Some other Free Software Foundation software is covered by the GNU Library General Public License instead.) You can apply it to your programs, too.

When we speak of free software, we are referring to freedom, not price. Our General Public Licenses are designed to make sure that you have the freedom to distribute copies of free software (and charge for this service if you wish), that you receive source code or can get it if you want it, that you can change the software or use pieces of it in new free programs; and that you know you can do these things.

To protect your rights, we need to make restrictions that forbid anyone to deny you these rights or to ask you to surrender the rights. These restrictions translate to certain responsibilities for you if you distribute copies of the software, or if you modify it.

For example, if you distribute copies of such a program, whether gratis or for a fee, you must give the recipients all the rights that you have. You must make sure that they, too, receive or can get the source code. And you must show them these terms so they know their rights.

We protect your rights with two steps: (1) copyright the software, and (2) offer you this license which gives you legal permission to copy, distribute and/or modify the software.

Also, for each author’s protection and ours, we want to make certain that everyone understands that there is no warranty for this free software. If the software is modified by someone else and passed on, we want its recipients to know that what they have is not the original, so that any problems introduced by others will not reflect on the original authors’ reputations.

Finally, any free program is threatened constantly by software patents. We wish to avoid the danger that redistributors of a free program will individually obtain patent licenses, in effect making the program proprietary. To prevent this, we have made it clear that any patent must be licensed for everyone’s free use or not licensed at all.

The precise terms and conditions for copying, distribution and modification follow.

#### TERMS AND CONDITIONS FOR COPYING, DISTRIBUTION AND MODIFICATION

0. This License applies to any program or other work which contains a notice placed by the copyright holder saying it may be distributed under the terms of this General Public License. The “Program”, below, refers to any such program or work, and a “work based on the Program” means either the Program or any derivative work under copyright law: that is to say, a work containing the Program or a portion of it, either verbatim or with modifications and/or translated into another language. (Hereinafter, translation is included without limitation in the term “modification”.) Each licensee is addressed as “you”.

Activities other than copying, distribution and modification are not covered by this License; they are outside its scope. The act of running the Program is not restricted, and the output from the Program is covered only if its contents constitute a work based on the Program (independent of having been made by running the Program). Whether that is true depends on what the Program does.

1. You may copy and distribute verbatim copies of the Program's source code as you receive it, in any medium, provided that you conspicuously and appropriately publish on each copy an appropriate copyright notice and disclaimer of warranty; keep intact all the notices that refer to this License and to the absence of any warranty; and give any other recipients of the Program a copy of this License along with the Program.

You may charge a fee for the physical act of transferring a copy, and you may at your option offer warranty protection in exchange for a fee.

2. You may modify your copy or copies of the Program or any portion of it, thus forming a work based on the Program, and copy and distribute such modifications or work under the terms of Section 1 above, provided that you also meet all of these conditions:
  - a) You must cause the modified files to carry prominent notices stating that you changed the files and the date of any change.
  - b) You must cause any work that you distribute or publish, that in whole or in part contains or is derived from the Program or any part thereof, to be licensed as a whole at no charge to all third parties under the terms of this License.
  - c) If the modified program normally reads commands interactively when run, you must cause it, when started running for such interactive use in the most ordinary way, to print or display an announcement including an appropriate copyright notice and a notice that there is no warranty (or else, saying that you provide a warranty) and that users may redistribute the program under these conditions, and telling the user how to view a copy of this License. (Exception: if the Program itself is interactive but does not normally print such an announcement, your work based on the Program is not required to print an announcement.)

These requirements apply to the modified work as a whole. If identifiable sections of that work are not derived from the Program, and can be reasonably considered independent and separate works in themselves, then this License, and its terms, do not apply to those sections when you distribute them as separate works. But when you distribute the same sections as part of a whole which is a work based on the Program, the distribution of the whole must be on the terms of this License, whose permissions for other licensees extend to the entire whole, and thus to each and every part regardless of who wrote it.

Thus, it is not the intent of this section to claim rights or contest your rights to work written entirely by you; rather, the intent is to exercise the right to control the distribution of derivative or collective works based on the Program.

In addition, mere aggregation of another work not based on the Program with the Program (or with a work based on the Program) on a volume of a storage or distribution medium does not bring the other work under the scope of this License.

3. You may copy and distribute the Program (or a work based on it, under Section 2) in object code or executable form under the terms of Sections 1 and 2 above provided that you also do one of the following:
  - a) Accompany it with the complete corresponding machine-readable source code, which must be distributed under the terms of Sections 1 and 2 above on a medium customarily used for software interchange; or,
  - b) Accompany it with a written offer, valid for at least three years, to give any third party, for a charge no more than your cost of physically performing source distribution, a complete machine-readable copy of the corresponding source code, to be distributed under the terms of Sections 1 and 2 above on a medium customarily used for software interchange; or,
  - c) Accompany it with the information you received as to the offer to distribute corresponding source code. (This alternative is allowed only for noncommercial distribution and only if you received the program in object code or executable form with such an offer, in accord with Subsection b above.)



---

The source code for a work means the preferred form of the work for making modifications to it. For an executable work, complete source code means all the source code for all modules it contains, plus any associated interface definition files, plus the scripts used to control compilation and installation of the executable. However, as a special exception, the source code distributed need not include anything that is normally distributed (in either source or binary form) with the major components (compiler, kernel, and so on) of the operating system on which the executable runs, unless that component itself accompanies the executable.

If distribution of executable or object code is made by offering access to copy from a designated place, then offering equivalent access to copy the source code from the same place counts as distribution of the source code, even though third parties are not compelled to copy the source along with the object code.

4. You may not copy, modify, sublicense, or distribute the Program except as expressly provided under this License. Any attempt otherwise to copy, modify, sublicense or distribute the Program is void, and will automatically terminate your rights under this License. However, parties who have received copies, or rights, from you under this License will not have their licenses terminated so long as such parties remain in full compliance.
5. You are not required to accept this License, since you have not signed it. However, nothing else grants you permission to modify or distribute the Program or its derivative works. These actions are prohibited by law if you do not accept this License. Therefore, by modifying or distributing the Program (or any work based on the Program), you indicate your acceptance of this License to do so, and all its terms and conditions for copying, distributing or modifying the Program or works based on it.
6. Each time you redistribute the Program (or any work based on the Program), the recipient automatically receives a license from the original licensor to copy, distribute or modify the Program subject to these terms and conditions. You may not impose any further restrictions on the recipients' exercise of the rights granted herein. You are not responsible for enforcing compliance by third parties to this License.
7. If, as a consequence of a court judgment or allegation of patent infringement or for any other reason (not limited to patent issues), conditions are imposed on you (whether by court order, agreement or otherwise) that contradict the conditions of this License, they do not excuse you from the conditions of this License. If you cannot distribute so as to satisfy simultaneously your obligations under this License and any other pertinent obligations, then as a consequence you may not distribute the Program at all. For example, if a patent license would not permit royalty-free redistribution of the Program by all those who receive copies directly or indirectly through you, then the only way you could satisfy both it and this License would be to refrain entirely from distribution of the Program.

If any portion of this section is held invalid or unenforceable under any particular circumstance, the balance of the section is intended to apply and the section as a whole is intended to apply in other circumstances.

It is not the purpose of this section to induce you to infringe any patents or other property right claims or to contest validity of any such claims; this section has the sole purpose of protecting the integrity of the free software distribution system, which is implemented by public license practices. Many people have made generous contributions to the wide range of software distributed through that system in reliance on consistent application of that system; it is up to the author/donor to decide if he or she is willing to distribute software through any other system and a licensee cannot impose that choice.

This section is intended to make thoroughly clear what is believed to be a consequence of the rest of this License.

8. If the distribution and/or use of the Program is restricted in certain countries either by patents or by copyrighted interfaces, the original copyright holder who places the Program under this License may add an explicit geographical distribution limitation excluding those countries, so that distribution is permitted only in or among countries not thus excluded. In such case, this License incorporates the limitation as if written in the body of this License.
9. The Free Software Foundation may publish revised and/or new versions of the General Public License from time to time. Such new versions will be similar in spirit to the present version, but may differ in detail to address new problems or concerns.

Each version is given a distinguishing version number. If the Program specifies a version number of this License which applies to it and "any later version", you have the option of following the terms and

conditions either of that version or of any later version published by the Free Software Foundation. If the Program does not specify a version number of this License, you may choose any version ever published by the Free Software Foundation.

10. If you wish to incorporate parts of the Program into other free programs whose distribution conditions are different, write to the author to ask for permission. For software which is copyrighted by the Free Software Foundation, write to the Free Software Foundation; we sometimes make exceptions for this. Our decision will be guided by the two goals of preserving the free status of all derivatives of our free software and of promoting the sharing and reuse of software generally.

## NO WARRANTY

11. BECAUSE THE PROGRAM IS LICENSED FREE OF CHARGE, THERE IS NO WARRANTY FOR THE PROGRAM, TO THE EXTENT PERMITTED BY APPLICABLE LAW. EXCEPT WHEN OTHERWISE STATED IN WRITING THE COPYRIGHT HOLDERS AND/OR OTHER PARTIES PROVIDE THE PROGRAM "AS IS" WITHOUT WARRANTY OF ANY KIND, EITHER EXPRESSED OR IMPLIED, INCLUDING, BUT NOT LIMITED TO, THE IMPLIED WARRANTIES OF MERCHANTABILITY AND FITNESS FOR A PARTICULAR PURPOSE. THE ENTIRE RISK AS TO THE QUALITY AND PERFORMANCE OF THE PROGRAM IS WITH YOU. SHOULD THE PROGRAM PROVE DEFECTIVE, YOU ASSUME THE COST OF ALL NECESSARY SERVICING, REPAIR OR CORRECTION.
12. IN NO EVENT UNLESS REQUIRED BY APPLICABLE LAW OR AGREED TO IN WRITING WILL ANY COPYRIGHT HOLDER, OR ANY OTHER PARTY WHO MAY MODIFY AND/OR REDISTRIBUTE THE PROGRAM AS PERMITTED ABOVE, BE LIABLE TO YOU FOR DAMAGES, INCLUDING ANY GENERAL, SPECIAL, INCIDENTAL OR CONSEQUENTIAL DAMAGES ARISING OUT OF THE USE OR INABILITY TO USE THE PROGRAM (INCLUDING BUT NOT LIMITED TO LOSS OF DATA OR DATA BEING RENDERED INACCURATE OR LOSSES SUSTAINED BY YOU OR THIRD PARTIES OR A FAILURE OF THE PROGRAM TO OPERATE WITH ANY OTHER PROGRAMS), EVEN IF SUCH HOLDER OR OTHER PARTY HAS BEEN ADVISED OF THE POSSIBILITY OF SUCH DAMAGES.

---

## 17. Acknowledgements

We thank the developers of CASAL (?) for their ideas that led to the development of the CASAL2. The CASAL2 logo was designed by Ian Doonan and Erika Mackay (NIWA).

Much of the structure of CASAL2, equations, and documentation in this manual draw heavily on similar components of the fisheries population model CASAL (?) and the spatial model SPM (?). We thank the authors of CASAL and SPM for their permission to use their work as the basis for parts of CASAL2 and allow the use of the definitions, concepts, and documentation.

The development of CASAL2 was funded by the New Zealand Ministry for Primary Industries and the National Institute of Water & Atmospheric Research Ltd. (NIWA) under NIWAs Fisheries Centre Research Programme 1.



---

## 18. Quick reference

**@ageing\_error** *label* Define an object of type *ageing\_error*

*label* Label of the ageing error

*type* Type of ageing error

**@ageing\_\_error[*label*].type=data**

**@ageing\_\_error[*label*].type=None**

**@ageing\_\_error[*label*].type=normal**

*cv* CV of the misclassification matrix

*k* *k* defines the minimum age of individuals which can be misclassified, e.g., individuals of age less than *k* have no ageing error

**@ageing\_\_error[*label*].type=off\_by\_one**

*p1* proportion misclassified as one year younger, e.g., the proportion of age 3 individuals that were misclassified as age 2

*p2* proportion misclassified as one year older, e.g., the proportion of age 3 individuals that were misclassified as age 4

*p2* proportion misclassified as one year older, e.g., the proportion of age 3 individuals that were misclassified as age 4

*k* The minimum age of fish which can be misclassified, i.e., fish of age less than *k* are assumed to be correctly classified

*k* The minimum age of fish which can be misclassified, i.e., fish of age less than *k* are assumed to be correctly classified

**@age\_length** *label* Define an object of type *age\_length*

*label* Label of the age length relationship

*type* Type of age length relationship

*time\_step\_proportions* the fraction of the year applied in each time step that is added to the age for the purposes of evaluating the length, i.e., a value of 0.5 for a time step will evaluate the length of individuals at age+0.5 in that time step

*distribution* The assumed distribution for the growth curve

*cv\_first* CV for the first age class

*cv\_last* CV for last age class

*casal\_switch* If true, use the (less accurate) equation for the cumulative normal function as was used in the legacy version of CASAL.

**@age\_\_length[*label*].type=data**

*external\_gaps*

*internal\_gaps*

*length\_weight* The label from an associated length-weight block

*by\_length* Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age

**@age\_\_length[*label*].type=None**

**@age\_\_length[*label*].type=schnute**

*y1* Define the *y1* parameter of the Schnute relationship

`y2` Define the  $y_2$  parameter of the Schnute relationship  
`tau1` Define the  $\tau_1$  parameter of the Schnute relationship  
`tau2` Define the  $\tau_2$  parameter of the Schnute relationship  
`a` Define the  $a$  parameter of the Schnute relationship  
`b` Define the  $b$  parameter of the Schnute relationship  
`length_weight` Define the label of the associated length-weight relationship  
`by_length` Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age

#### **@age\_\_length[label].type=von\_bertalanffy**

`linf` Define the  $L_{infinity}$  parameter of the von Bertalanffy relationship  
`k` Define the  $k$  parameter of the von Bertalanffy relationship  
`t0` Define the  $t_0$  parameter of the von Bertalanffy relationship  
`length_weight` Define the label of the associated length-weight relationship  
`by_length` Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age  
**@catchability** *label* Define an object of type *catchability*  
`label` Label of the catchability  
`type` Type of catchability

#### **@catchability[label].type=free**

`q` value of the catchability

#### **@catchability[label].type=nuisance**

#### **@derived\_quantity label** Define an object of type *derived\_quantity*

`label` Label of the derived quantity  
`type` Type of derived quantity  
`time_step` The time step in which to calculate the derived quantity after  
`categories` The list of categories to use when calculating the derived quantity  
`selectivities` A list of one selectivity  
`time_step_proportion` Proportion through the mortality block of the time step when calculated  
`time_step_proportion_method` Method for interpolating for the proportion through the mortality block

#### **@derived\_quantity[label].type=abundance**

#### **@derived\_quantity[label].type=biomass**

#### **@estimate label** Define an object of type *estimate*

`label` The label of the estimate  
`type` The prior type for the estimate  
`parameter` The name of the parameter to estimate in the model  
`lower_bound` The lower bound for the parameter  
`upper_bound` The upper bound for the parameter  
`same` List of parameters that are constrained to have the same value as this parameter  
`mcmc` Indicates if this parameter is fixed at the point estimate during an MCMC run

#### **@estimate[label].type=beta**

`mu` Beta prior mean ( $\mu$ ) parameter  
`sigma` Beta prior variance ( $\sigma$ ) parameter  
`a` Beta prior lower bound of the range (A) parameter  
`b` Beta prior upper bound of the range (B) parameter

---

**@estimate[label].type=lognormal**

mu      The lognormal prior mean (mu) parameter

cv      The Lognormal variance (CV) parameter

**@estimate[label].type=normal**

mu      The normal prior mean (mu) parameter

cv      The normal variance (standard deviation) parameter

**@estimate[label].type=normal\_by\_stdev**

mu      The normal prior mean (mu) parameter

sigma    The normal variance (standard deviation) parameter

**@estimate[label].type=normal\_log**

mu      The normal-log prior mean (mu) parameter

sigma    The normal-log prior variance (standard deviation) parameter

**@estimate[label].type=uniform**

**@estimate[label].type=uniform\_log**

**@initialisation\_phase label**      Define an object of type *initialisation\_phase*

label    The label of the initialisation phase

type    The type of initialisation

**@initialisation\_phase[label].type=cinitial**

categories    The list of categories for the Cinitial initialisation

**@initialisation\_phase[label].type=derived**

insert\_processes      Additional processes not defined in the annual cycle, that are to be inserted into this initialisation phase

exclude\_processes      Processes in the annual cycle to be excluded from this initialisation phase

casal\_initialisation\_switch      Run an extra annual cycle to evaluate equilibrium SSB's. Warning - if true, this may not correctly evaluate the equilibrium state. Use true if attempting to replicate a legacy CASAL model

**@initialisation\_phase[label].type=iterative**

years      The number of iterations (years) over which to execute this initialisation phase

insert\_processes      (years) over which to execute this initialisation phase

exclude\_processes      Processes in the annual cycle to be excluded from this initialisation phase

convergence\_years      The iteration (year) when the test for convergence (lambda) is evaluated

lambda      The maximum value of the absolute sum of differences (lambda) between the partition at year-1 and year that indicates successful convergence

**@initialisation\_phase[label].type=state\_category\_by\_age**

categories    The list of categories for the category state initialisation

min\_age      The minimum age of values supplied in the definition of the category state

max\_age      The maximum age of values supplied in the definition of the category state

**@likelihood label**      Define an object of type *likelihood*

**@likelihood[label].type=binomial**

```
@likelihood[label].type=binomial_approx
@likelihood[label].type=dirichlet
@likelihood[label].type=log_normal
@likelihood[label].type=log_normal_with_q
@likelihood[label].type=multinomial
@likelihood[label].type=normal
@likelihood[label].type=pseudo

@derived_quantity label    Define an object of type derived_quantity
label    Label of the derived quantity
type     Type of derived quantity
time_step    The time step in which to calculate the derived quantity after
categories   The list of categories to use when calculating the derived quantity
selectivities    A list of one selectivity
time_step_proportion    Proportion through the mortality block of the time step when calculated
time_step_proportion_method    Method for interpolating for the proportion through the mortality block

@derived_quantity[label].type=abundance
@derived_quantity[label].type=biomass

@mcmc label    Define an object of type mcmc
label    The label of the MCMC
type     The type of MCMC
length   The number of iterations in for the MCMC chain
active   Indicates if this is the active MCMC algorithm
print_default_reports    Indicates if the output prints the default reports
step_size    Initial stepsize (as a multiplier of the approximate covariance matrix

@mcmc[label].type=independence_metropolis

start    Covariance multiplier for the starting point of the MCMC
keep     Spacing between recorded values in the MCMC
max_correlation    Maximum absolute correlation in the covariance matrix of the proposal distribution
covariance_adjustment_method    Method for adjusting small variances in the covariance proposal
matrix
correlation_adjustment_diff    Minimum non-zero variance times the range of the bounds in the
covariance matrix of the proposal distribution
proposal_distribution    The shape of the proposal distribution (either the t or the normal distribution
df    Degrees of freedom of the multivariate t proposal distribution
adapt_stepsize_at    Iterations in the chain to check and resize the MCMC stepsize
adapt_covariance_matrix_at    Iterations in the chain to check and resize the MCMC stepsize
adapt_stepsize_method    Method to adapt step size.
@minimiser label    Define an object of type minimiser
label    The minimiser label
type     The type of minimiser to use
active   Indicates if this minimiser is active
covariance    Indicates if a covariance matrix should be generated

@minimiser[label].type=adolc

iterations    Maximum number of iterations
```



---

evaluations      Maximum number of evaluations  
tolerance        Tolerance of the gradient for convergence  
step\_size        Minimum Step-size before minimisation fails

**@minimiser[label].type=betadiff**

iterations        Maximum number of iterations  
evaluations       Maximum number of evaluations  
tolerance        Tolerance of the gradient for convergence

**@minimiser[label].type=cppad**

**@minimiser[label].type=de\_solver**

population\_size    The number of candidate solutions to have in the population  
crossover\_probability    Define the minimisers crossover probability  
difference\_scale    The scale to apply to new solutions when comparing candidates  
max\_generations    The maximum number of iterations to run  
tolerance        The total variance between the population and best candidate before acceptance  
method            The type of candidate generation method to use

**@minimiser[label].type=dlib**

**@minimiser[label].type=numerical\_differences**

iterations        Maximum number of iterations  
evaluations       Maximum number of evaluations  
tolerance        Tolerance of the gradient for convergence  
step\_size        Minimum Step-size before minimisation fails  
**@model label**    Define an object of type *model*

start\_year        Define the first year of the model, immediately following initialisation  
final\_year        Define the final year of the model, excluding years in the projection period  
min\_age           Minimum age of individuals in the population  
max\_age           Maximum age of individuals in the population  
age\_plus          Define the oldest age as a plus group  
initialisation\_phases    Define the labels of the phases of the initialisation  
time\_steps        Define the labels of the time steps, in the order that they are applied, to form the annual cycle  
projection\_final\_year    Define the final year of the model in projection mode  
length\_bins  
base\_weight\_units    Define the units for the base weight. This will be the default unit of any weight  
input parameters

**@observation label**    Define an object of type *observation*

label            Label  
type            Type of observation  
likelihood        Type of likelihood to use  
categories        Category labels to use  
simulation\_likelihood    Simulation likelihood to use  
likelihood\_multiplier    Likelihood score multiplier  
error\_value\_multiplier    Error value multiplier for likelihood

**@observation[label].type=process\_abundance**

selectivities      Labels of the selectivities

time\_step     The label of time-step that the observation occurs in  
 catchability     The label of the catchability (q) block assumed for this observation  
 obs     The observed values  
 years     The years of the observed values  
 error\_value     The error values of the observed values (note the units depend on the likelihood)  
 delta     Robustification value (delta) for the likelihood  
 process\_error     The label of the process error  
 process     The label of the process for the observation  
 process\_proportion     Proportion through the process when the observation is evaluated

**@observation[label].type=abundance**

selectivities     Labels of the selectivities  
 time\_step     The label of time-step that the observation occurs in  
 catchability     The label of the catchability coefficient (q) assumed  
 obs     The observed values  
 years     Years for which there are observations  
 error\_value     The error values of the observed values (note the units depend on the likelihood)  
 delta     The value of the delta robustification parameter  
 process\_error     The label of the process error block  
 time\_step\_proportion     Proportion through the mortality block of the time step when the observation is evaluated

**@observation[label].type=process\_biomass**

catchability     The time-step of the observation  
 time\_step     The label of time-step that the observation occurs in  
 obs     The observed values  
 years     The years of the observed values  
 error\_value     The error values of the observed values (note the units depend on the likelihood)  
 delta     Robustification value (delta) for the likelihood  
 selectivities     Labels of the selectivities  
 process\_error     Value for process error  
 process     The label of the process for the observation  
 process\_proportion     Proportion through the process when the observation is evaluated

**@observation[label].type=biomass**

catchability     The time-step of the observation  
 time\_step     The label of time-step that the observation occurs in  
 obs     The observed values  
 years     The years of the observed values  
 error\_value     The error values of the observed values (note the units depend on the likelihood)  
 delta     Robustification value (delta) for the likelihood  
 selectivities     Labels of the selectivities  
 process\_error     Value for process error  
 time\_step\_proportion     Proportion through the mortality block of the time step when the observation is evaluated

**@observation[label].type=process\_removals\_by\_age**

min\_age     Minimum age

---

max\_age      Maximum age  
age\_plus     Use age plus group  
time\_step    The label of time-step that the observation occurs in  
tolerance    Tolerance  
years        Years for which there are observations  
delta        Robustification value (delta) for the likelihood  
process\_errors      Label of process error to use  
ageing\_error      Label of ageing error to use  
method\_of\_removal      Label of observed method of removals  
mortality\_instantaneous\_process      The label of the mortality instantaneous process for the observation

**@observation[label].type=process\_removals\_by\_length**

length\_bins      Length bins  
time\_step        Time step to execute in  
length\_plus\_group      Is the last bin a plus group  
tolerance        Tolerance for rescaling proportions  
years            Years for which there are observations  
delta            The value of the delta robustification parameter  
process\_errors      the value of process error  
method\_of\_removal      Label of observed method of removals  
mortality\_instantaneous\_process      The label of the mortality instantaneous process for the observation

**@observation[label].type=process\_proportions\_at\_age**

min\_age        Minimum age  
max\_age        Maximum age  
age\_plus        Use age plus group  
time\_step        The label of time-step that the observation occurs in  
tolerance        Tolerance on the constraint, that for each year the sum of proportions in each age must equal one e.g. tolerance = 0.1 then  $1 - \text{Sum}(\text{Proportions})$  can be as great as 0.1  
years            The years of the observed values  
delta            Robustification value (delta) for the likelihood  
selectivities      Labels of the selectivities  
process\_errors      Process error  
ageing\_error      Label of ageing error to use  
process          The label of the process for the observation  
process\_proportion      Proportion through the process when the observation is evaluated

**@observation[label].type=proportions\_at\_age**

min\_age        Minimum age  
max\_age        Maximum age  
age\_plus        Use age plus group  
time\_step        The label of time-step that the observation occurs in  
tolerance        Tolerance on the constraint, that for each year the sum of proportions in each age must equal one e.g. tolerance = 0.1 then  $1 - \text{Sum}(\text{Proportions})$  can be as great as 0.1  
years            The years of the observed values  
delta            Robustification value (delta) for the likelihood  
selectivities      Labels of the selectivities  
process\_errors      Process error  
ageing\_error      Label of ageing error to use  
time\_step\_proportion      Proportion through the mortality block of the time step when the observation is evaluated

**@observation[label].type=process\_proportions\_at\_length**

length\_bins      Length bins  
time\_step      The label of time-step that the observation occurs in  
length\_plus\_group      Is the last bin a plus group  
tolerance      Tolerance for rescaling proportions  
years      Years for which there are observations  
selectivities      The labels of the selectivities  
delta      The value of the delta robustification parameter  
process\_errors      Process error  
process      The label of the process for the observation  
process\_proportion      Proportion through the process when the observation is evaluated

**@observation[label].type=proportions\_at\_length**

length\_bins      Length bins  
time\_step      The label of time-step that the observation occurs in  
length\_plus\_group      Is the last bin a plus group  
tolerance      Tolerance for rescaling proportions  
years      Years for which there are observations  
selectivities      The labels of the selectivities  
delta      The value of the delta robustification parameter  
process\_errors      Process error  
time\_step\_proportion      Proportion through the mortality block of the time step when the observation is evaluated

**@observation[label].type=process\_proportions\_by\_category**

min\_age      Minimum age  
max\_age      Maximum age  
time\_step      The label of time-step that the observation occurs in  
age\_plus      Use age plus group  
years      Years for which there are observations  
selectivities      The labels of the selectivities  
categories2      Target Categories  
selectivities2      Target Selectivities  
delta      The value of the delta robustification parameter  
process\_errors      Process error  
process      The label of the process for the observation  
process\_proportion      Proportion through the mortality block of the time step when the observation is evaluated

**@observation[label].type=proportions\_by\_category**

min\_age      Minimum age  
max\_age      Maximum age  
time\_step      The label of time-step that the observation occurs in  
age\_plus      Use age plus group  
years      Years for which there are observations  
selectivities      The labels of the selectivities  
categories2      Target Categories  
selectivities2      Target Selectivities  
delta      The value of the delta robustification parameter  
process\_errors      Process error  
time\_step\_proportion      Proportion through the time step to analyse the partition from

**@observation[label].type=proportions\_migrating**

---

min\_age      Minimum age  
 max\_age      Maximum age  
 time\_step    The label of time-step that the observation occurs in  
 age\_plus     Use age plus group  
 years        Years for which there are observations  
 delta        The value of the delta robustification parameter  
 process\_errors    Process error  
 ageing\_error    Label of ageing error to use  
 process      Process label

**@observation[label].type=tag\_recapture\_by\_age**

min\_age      Minimum age  
 max\_age      Maximum age  
 age\_plus     Use age plus group  
 years        Years for which there are observations  
 categories2    The available categories in the partition  
 selectivities    The labels of the selectivities  
 time\_step    The label of time-step that the observation occurs in  
 selectivities2    The categories of tagged individuals for the observation  
 delta        The value of the delta robustification parameter  
 process\_errors    Process error  
 detection     Probability of detecting a recaptured individual  
 time\_step\_proportion    Proportion through the mortality block of the time step when the observation is evaluated

**@observation[label].type=tag\_recapture\_by\_length**

length\_bins    Length Bins  
 plus\_group    Indicates if the last length bin is a plus group  
 years        Years for which there are observations  
 time\_step    The label of time-step that the observation occurs in  
 categories2    The categories of tagged individuals for the observation  
 selectivities    The labels of the selectivities  
 selectivities2    The labels of the tag category selectivities  
 delta        The value of the delta robustification parameter  
 process\_errors    Process error  
 detection     Probability of detecting a recaptured individual  
 dispersion    Over-dispersion parameter ( $\phi$ )  
 time\_step\_proportion    Proportion through the mortality block of the time step when the observation is evaluated

**@penalty label**      Define an object of type *penalty*

label      The label of the penalty  
 type      The type of penalty

**@penalty[label].type=process**

multiplier    The penalty multiplier  
 log.scale    Indicates if the sums of squares is calculated on the log scale

**@process label**      Define an object of type *process*

label      The label of the process  
 type      The type of process  
 print\_report    Indicates if a process report should be generated for this process

**@process[label].type=ageing**

categories      The labels of the categories

**@process[label].type=maturation**

from      List of categories to mature from  
to      List of categories to mature too  
selectivities      List of selectivities to use for maturation  
years      The years to be associated with rates  
rates      The rates to mature for each year

**@process[label].type=mortality\_constant\_rate**

categories      List of categories labels  
m      Mortality rates  
time\_step\_ratio      Time step ratios for the mortality rates  
selectivities      List of selectivities for the categories

**@process[label].type=mortality\_event**

categories      Categories  
years      Years in which to apply the mortality process  
catches      The number of removals (catches) to apply for each year  
u\_max      Maximum exploitation rate ( $U_{max}$ )  
selectivities      List of selectivities  
penalty      The label of the penalty to apply if the total number of removals cannot be taken

**@process[label].type=mortality\_event\_biomass**

categories      Category labels  
selectivities      The labels of the selectivities for each of the categories  
years      Years in which to apply the mortality process  
catches      The biomass of removals (catches) to apply for each year  
u\_max      Maximum exploitation rate ( $U_{max}$ )  
penalty      The label of the penalty to apply if the total biomass of removals cannot be taken

**@process[label].type=mortality\_holling\_rate**

prey\_categories      Prey Categories labels  
predator\_categories      Predator Categories labels  
is\_abundance      Is vulnerable amount of prey and predator an abundance [true] or biomass [false]  
a      parameter a  
b      parameter b  
x      This parameter controls the type of functional form, Holling function type 2 ( $x=2$ ) or 3 ( $x=3$ ), or generalised (Michaelis Menten,  $x=1$ )  
u\_max      Maximum exploitation rate ( $U_{max}$ )  
prey\_selectivities      Selectivities for prey categories  
predator\_selectivities      Selectivities for predator categories  
penalty      Label of penalty to be applied  
years      Years in which to apply the mortality process

**@process[label].type=mortality\_instantaneous**

categories      Categories for instantaneous mortality  
m      Natural mortality rates for each category  
time\_step\_ratio      Time step ratios for natural mortality  
selectivities      The selectivities to apply on the categories for natural mortality

---

**@process[label].type=mortality\_prey\_suitability**

prey\_categories      Prey Categories labels  
predator\_categories      Predator Categories labels  
consumption\_rate      Predator consumption rate  
electivities      Prey Electivities  
u\_max      Umax  
prey\_selectivities      Selectivities for prey categories  
predator\_selectivities      Selectivities for predator categories  
penalty      Label of penalty to be applied  
years      Year that process occurs

**@process[label].type=nop****@process[label].type=recruitment\_beverton\_holt**

categories      Category labels  
r0      R0  
b0      B0  
proportions      Proportions  
age      Age to recruit at  
ssb\_offset      Spawning biomass year offset  
steepness      Steepness  
ssb      SSB Label (derived quantity)  
b0.initialisation\_phase      Initialisation phase Label that b0 is from  
ycs\_values      YCS Values  
prior\_standardised\_ycs      Priors for year class strength on ycs values (not standardised ycs values)  
standardise\_ycs\_years      Years that are included for year class standardisation

**@process[label].type=recruitment\_constant**

categories      Categories  
proportions      Proportions  
age      Age  
r0      R0

**@process[label].type=survival\_constant\_rate**

categories      List of categories  
s      Survival rates  
time\_step\_ratio      Time step ratios for S  
selectivities      Selectivity label

**@process[label].type=tag\_by\_age**

from      Categories to transition from  
to      Categories to transition to  
min\_age      Minimum age to transition  
max\_age      Maximum age to transition  
penalty      Penalty label  
u\_max      U Max  
years      Years to execute the transition in  
initial\_mortality  
initial\_mortality\_selectivity  
loss\_rate  
loss\_rate\_selectivities  
selectivities  
n

**@process[label].type=tag\_by\_length**

from      Categories to transition from  
to      Categories to transition to  
plus\_group      Use plus group for last length bin  
maximum\_length      The upper length when there is no plus group  
penalty      Penalty label  
u\_max      U Max  
years      Years to execute the transition in  
initial\_mortality  
initial\_mortality\_selectivity  
selectivities  
n

**@process[label].type=tag\_loss**

categories      List of categories  
tag\_loss\_rate      Tag Loss rates  
time\_step\_ratio      Time step ratios for Tag Loss  
tag\_loss\_type      Type of tag loss  
selectivities      Selectivities  
year      The year the first tagging release process was executed

**@process[label].type=transition\_category**

from      From  
to      To  
proportions      Proportions  
selectivities      Selectivity names

**@process[label].type=transition\_category\_by\_age**

from      Categories to transition from  
to      Categories to transition to  
min\_age      Minimum age to transition  
max\_age      Maximum age to transition  
penalty      Penalty label  
u\_max      U Max  
years      Years to execute the transition in  
**@profile** *label*      Define an object of type *profile*

label      Label  
steps      The number of steps to take between the lower and upper bound  
lower\_bound      The lower bounds  
upper\_bound      The upper bounds  
parameter      The system parameter to profile

**@report label**      Define an object of type *report*

label      The label for the report  
type      The type of report  
file\_name      The File Name if you want this report to be in a separate file  
write\_mode      The write mode

**@report[label].type=ageing\_error\_matrix**

ageing\_error      Ageing Error label



---

```

@report[label].type=catchabilities
@report[label].type=category_info
@report[label].type=category_list
@report[label].type=correlation_matrix
@report[label].type=covariance_matrix
@report[label].type=derived_quantity
@report[label].type=estimable
parameter      Parameter to print
years          Years to print the estimable for
time_step      Time Step label

@report[label].type=estimate_summary
@report[label].type=estimate_value
@report[label].type=hessian_matrix
@report[label].type=initialisation_partition
@report[label].type=mcmc_covariance
@report[label].type=mcmc_objective
@report[label].type=mcmc_sample
@report[label].type=m_p_d
@report[label].type=objective_function
@report[label].type=observation
observation     Observation label

@report[label].type=output_parameters
@report[label].type=partition
time_step      Time Step label
years          Years

@report[label].type=partition_biomass
time_step      Time Step label
years          Years
units          Units (Default Kgs)

@report[label].type=partition_mean_weight
time_step      Time Step label
years          Years

@report[label].type=process
process        Process label that is reported

@report[label].type=random_number_seed
@report[label].type=selectivity
selectivity     Selectivity name

```

**@report[label].type=simulated\_observation**

observation      Observation label

**@report[label].type=standard\_header**

**@report[label].type=time\_varying**

**@selectivity label**      Define an object of type *selectivity*

label      The label for this selectivity

type      The type of selectivity

length\_based      Is the selectivity length based

intervals      Number of quantiles to evaluate a length based selectivity over the age length distribution

**@selectivity[label].type=all\_values**

v      V

**@selectivity[label].type=all\_values\_bounded**

l      L

h      H

v      V

**@selectivity[label].type=constant**

c      C

**@selectivity[label].type=double\_exponential**

x0      X0

x1      X1

x2      X2

y0      Y0

y1      Y1

y2      Y2

alpha      Alpha

**@selectivity[label].type=double\_normal**

mu      Mu

sigma\_l      Sigma L

sigma\_r      Sigma R

alpha      Alpha

**@selectivity[label].type=increasing**

l      Low

h      High

v      V

alpha      Alpha

**@selectivity[label].type=inverse\_logistic**

a50      A50

---

ato95     aTo95  
alpha     Alpha

**@selectivity[label].type=knife\_edge**

e     Edge  
alpha     Alpha

**@selectivity[label].type=logistic**

a50     A50  
ato95     Ato95  
alpha     Alpha

**@selectivity[label].type=logistic\_producing**

l     Low  
h     High  
a50     A50  
ato95     Ato95  
alpha     Alpha

**@length\_weight label**     Define an object of type *length\_weight*

label     The label of the length-weight relationship  
type     The type of the length-weight relationship

**@length\_weight[label].type=basic**

a     The *a* parameter in the basic length-weight relationship  
b     The *b* parameter in the basic length-weight relationship  
units     Units of measure (tonnes, kgs, grams)

**@length\_weight[label].type=none**

**@time\_step label**     Define an object of type *time\_step*

label     The label of the timestep  
processes     The labels of the processes for this time step in the order that they occur