



# CASAL2 User Manual

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## 1. Introduction

CASAL2 is a generalised age-structured population dynamics modelling software package that allows flexibility in specifying model structure, population dynamics, parameter estimation, and model outputs. CASAL2 can model population dynamics for an age-structured population using a range of population dynamics observations, including mark-recapture, relative and absolute abundance time series, and age frequency data. CASAL2 does this by implementing an age-structured population dynamics model that can have user defined categories (e.g., immature, mature, male, female, predator, prey, etc.) to specify the population structure, and a user-defined age range.

This manual describes how to use CASAL2, including how to run CASAL2, how to set up an input configuration file. Further, we describe the population dynamics, observations, and estimation methods, and describe how to specify and interpret output.

### 1.1. Version

This document (last modified 2016-06-03) describes CASAL2 v2016-06-03. The CASAL2 version number is suffixed with a date/time (yyyy-mm-dd), giving the revision control system UTC date for the most recent modification of the underlying software source code. User manual updates will usually be issued for each minor version or date release of CASAL2. Any questions of the use of the software can be directed to the authors at [casal@niwa.co.nz](mailto:casal@niwa.co.nz).

### 1.2. Citing CASAL2

A suitable reference for CASAL2 and this document is:

S. Rasmussen, I. Doonan, A. Dunn, C. Marsh, K. Large, S. Mormede (2016). CASAL2 User Manual, v2016-06-03. National Institute of Water & Atmospheric Research Ltd. *NIWA Technical Report 139*. 195 p.

### 1.3. Software license

This program and the accompanying materials are made available under the terms of the licence GNU GPL v2 which accompanies this software (see Section 19).

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### 1.4. System requirements

CASAL2 is available for most IBM compatible machines running 64-bit Linux and Microsoft Windows operating systems.

Several of CASAL2s tasks are highly computer intensive and a fast processor is recommended. Depending on the model implemented, some of CASAL2s tasks can take a considerable amount of time (minutes to hours), and in extreme cases can even take several days to undertake an MCMC estimate.

The program itself requires only a few megabytes of hard-disk space but output files can consume large amounts of disk space. Depending on number and type of user output requests, the output could range from a few hundred kilobytes to several hundred megabytes. When estimating model

fits, several hundred megabytes of RAM may be required, depending on the spatial size of the model, number of categories, and complexity of processes and observations. For extremely large models, several gigabytes of RAM may occasionally be required.

### 1.5. Necessary files

For both 64-bit Linux and Microsoft Windows, only the binary file `casal2` or `casal2.exe` is required to run CASAL2. No other software is required. We do not compile a version for 32-bit operating systems.

CASAL2 offers little in the way of post-processing of model output, and a package available that allows tabulation and graphing of model outputs is recommended. We suggest software such as **R** (R Core Team, 2014) to assist in the post processing of CASAL2 output. We provide the CASAL2 **R** package for importing the CASAL2 output into **R** (see Section 14).

### 1.6. Getting help

CASAL2 is distributed as unsupported software, however we would appreciate being notified of any problems or errors in CASAL2. See Section 15.2 for the recommended template for reporting issues. For further information on CASAL2 please contact the development team at [casal@niwa.co.nz](mailto:casal@niwa.co.nz).

### 1.7. Technical details

CASAL2 was compiled on Linux using `gcc`, the C/C++ compiler developed by the GNU Project. The 64-bit Linux version was compiled using `gcc` version 5.2.1 20151010 (Ubuntu Linux). The Microsoft Windows version was compiled using Mingw32 `gcc` (tdm64-1) 5.1.0. The Microsoft Windows installer was built using the Inno Setup 5 application.

CASAL2 includes six different minimisers — Different minimisers may be better at some models than others. The first three are non-differentiation based minimisers: the first is closely based on the main algorithm of Dennis Jr and Schnabel (1996), and which uses finite difference gradients; the second is an implementation of the differential evolution solver (Storn and Price, 1995), and based on code by Lester E. Godwin of PushCorp, Inc.; and the third is Dlib (King, 2009). The three differentiation based minimisers are: ADOLC, an auto differentiation minimiser (Walther et al., 1996); CPPAD is an auto differentiation minimiser similar to ADOLC (Wächter and Biegler, 2006); and the third is a modified version of an older version of ADOL-C (v1.8.4) that was used in the original version of CASAL (Bull et al., 2012).

The random number generator used by CASAL2 uses an implementation of the Mersenne twister random number generator (Matsumoto and Nishimura, 1998). This, the command line functionality, matrix operations, and a number of other functions use the BOOST C++ library (Version 1.58.0).

Note that the output from CASAL2 may differ slightly on the different platforms due to different precision arithmetic or other platform dependent implementation issues. The source code for CASAL2 is available in the windows bundle or on the github repository at <https://github.com/NIWAFisheriesModelling/CASAL2>.

Unit tests of the underlying CASAL2 code are carried out at build time, using the GOOGLE mock and unit testing framework. The unit test framework aims to cover a significant proportion of the key functionality within the CASAL2 code base. The unit test code for CASAL2 is available as a part of the underlying source code.

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## 2. Model overview

### 2.1. Introduction

CASAL2 is an age-structured population dynamics model. It implements a statistical catch-at-age population dynamics, using a discrete time-step state-space model that represents a cohort-based population age structure .

CASAL2 is run from the console window on Microsoft Windows or from a terminal window on Linux. CASAL2 gets its information from input data files, the main one of which is the *input configuration file*. Commands and subcommands in the input configuration file are used to define the model structure, provide observations, define parameters, and define the outputs (reports) for CASAL2. Command line switches tell CASAL2 the run mode and where to direct its output. See Section 3 for details.

We define the model in terms of the *state*. The state consists of two parts, the *partition*, and any *derived quantities*. The state will typically change in each *time-step* of every year, depending on the *processes* defined for those time-steps in the model.

The *partition* is a representation of the population at an instance in time, and can be considered a matrix of the numbers of individuals within each category and at each age.

A *derived quantity* is a summary of the abundance or biomass in a selected part of the partition at some instance in time. Unlike the partition (which is updated as each new process is applied), a derived quantity records a single value for each year of the model run. Hence, derived quantities build up a vector of values over the time period represented by the model. For example, the total biomass of individuals in categories labelled, say, ‘mature’ at some instance in the annual cycle may be a derived quantity. The derived quantity is then available to the model to be reported, or to be an input into another process (for example, recruitment) at some instance in the model in a subsequent year.

The state at some instance in time is the term for the combination of the partition and any derived quantities at that instance in time. Throughout the model, changes to the state occur from the application of *processes*. This state then provides the basis for the generation of expected values for *observations*, as well as for reports and other outputs.

Running of the model consists of two steps — first the model state is initialised for a number of iterations (years), then the model runs over a range of predefined years.

Initialisation can be in one or more phases, and for each phase, the processes that occur in each year, and the order in which they are applied, need to be defined. The processes that occur is controlled by the *annual cycle*. This defines what processes happen in each model year and in what sequence. Further, the processes in each year are split up into one or more time-steps (with at least one process occurring in each time-step). You can think of each time-step as representing a particular part of the calendar year, or you can just treat them as an abstract sequence of events.

The division of the year into an arbitrary number of time-steps allows the user to specify the exact order in which processes occur, and how/when observations are evaluated. The user specifies the time-steps, their order, and the processes within each time-step. If more than one process occurs in the same time-step, then they occur in the order that they are specified.

Observations are always linked to a time-step, and are evaluated by the model in time-step in which they occur. Hence, time-steps can be used to break processes into groups, and assist in defining the timing of the observations within the annual cycle. The manner in which observations are evaluated and how the expected values are calculated by the model is described later in Section 6.

The population structure of CASAL2 follows the usual population modelling conventions and is similar to those implemented in, for example, CASAL (Bull et al., 2012). The model records the numbers of individuals by category and age (e.g., numbers of males and females at age). In general, cohorts are added via a recruitment event, are aged annually, and are removed from the population via various forms of mortality. The population is assumed to be closed (i.e., no immigration or emigration from the modelled area)

A model is implemented in CASAL2 using an input configuration file, which provides a complete description of the model structure (i.e., population structure, initialisation, and the subsequent population processes), observations, estimation methods, and reports (outputs) requested. CASAL2 runs from a console window on Microsoft Windows or from a text terminal on Linux. A model can be either *run*, estimable parameters can be *estimated* or *profiled*, *MCMC* distributions calculated, and these estimates can be *projected* into the future or used by CASAL2 as parameters of an operating model to *simulate* observations.

A model in CASAL2 is specified by an input configuration file, and comprises of four main components. These are the population section that defines the model structure, population dynamics, etc.; the estimation section that defines the methods of estimation (minimisation methods or MCMC algorithms) and the model parameters to be estimated; the observation section that defines the observational data and associated likelihoods; and the report section that defines the printouts and reports from the model and where these are saved. The input configuration file completely describes a model implemented in CASAL2. See Sections 8, 9, 10, and 11 for details and specification of CASAL2s command and subcommand syntax within the input configuration file.

### 2.2. The population section

The population section (Section 4) defines the model of the population dynamics. It describes the model structure (i.e. the population structure), initialisation method and phases, run and projection years (model period), population processes (for example, recruitment, migration, and mortality), selectivities, and key population parameters.

### 2.3. The estimation section

The estimation section (Section 5) specifies the parameters to be estimated, estimation methods, penalties and priors. Estimation is based on an objective function (e.g., negative log posterior). Depending on the run mode, the estimation section is used to specify the methods for finding a point estimate (i.e., the set of parameter values that minimizes the objective function), doing profiles, or MCMC methods and options, etc.

Further, the estimation section specifies the parameters to be estimated within each model run and the estimation methods. The estimation section specifies the choice of estimation method, which model parameters are to be estimated, priors, starting values, and minimiser control values.

Penalties and priors act as constraints on the estimation. They can either encourage or discourage (depending on the specific implementation) parameter estimates that are ‘near’ some value, and hence influence the estimation process. For example, a penalty can be included in the objective function to discourage parameter estimates that lead to models where the recorded catch was unable to be fully taken.



## **2.4. The observation section**

Types of observations, their values, and the associated error structures are defined in the observation section (Section 6). Observations are data which allow us to make inferences about unknown parameters. The observation section specifies the observations, their errors, likelihoods, and when the observations occur. Examples include relative or absolute abundance indices, proportions-at-age frequencies, tag recapture observations, etc. Estimation uses the observations to find values for each of the estimated parameters so that each observation is ‘close’ (in some mathematical sense) to a corresponding expected value.

## **2.5. The report section**

The report section (Section 7) specifies the model outputs. It defines the quantities and model summaries to be output to external files or to the standard output. While CASAL2 will provide informational messages to the screen, CASAL2 will only produce model estimates, population states, and other data as requested by the report section. Note that if no reports are specified, then no output will be produced.



---

### 3. Running CASAL2

CASAL2 is run from the console window (i.e., the command line) on Microsoft Windows or from a terminal window on Linux. CASAL2 gets its information from input data files, the key one of which is the input configuration file.

The input configuration file is compulsory and defines the model structure, processes, observations, parameters (both the fixed parameters and the parameters to be estimated), and the reports (outputs) requested. The following sections describe how to construct the CASAL2 configuration file. By convention, the name of the input configuration file ends with the suffix `.cs12`, however, any file name is acceptable. Note that the input configuration file can ‘include’ other files as a part of its syntax. Collectively, these are called the input configuration file.

Other input files can, in some circumstances, be supplied, depending on what is required. For example, a file can be supplied that defines the starting point for estimation, as points from which to simulate observations, or as points from which to run projections.

Simple command line arguments are used to determine the actions or *tasks* of CASAL2, i.e., to run a model with a set of parameter values, estimate parameter values (either point estimates or MCMC), project quantities into the future, simulate observations, etc.,. Hence, the *command line arguments* define the *task*. For example, `-r` is the *run*, `-e` is the *estimation*, and `-m` is the *MCMC* task. The *command line arguments* are described in Section 3.4.

#### 3.1. Using CASAL2

To use CASAL2, open a console (i.e. the command prompt) window (Microsoft Windows) or a terminal window (Linux). Navigate to a directory of your choice, where your input configuration files are located. Then type `casal2` with any arguments (see Section 3.4 for the the list of possible arguments). CASAL2 will print output to the screen and return you to the command prompt when it completes its task. Note that the CASAL2 executable (binary) and shared libraries (extension `.dll`) must be either in the directory where you run it or in your systems `PATH`. The CASAL2 installer should update your path on Windows in any case, but see your operating system documentation for help on identifying or modifying your `PATH`.

#### 3.2. The input configuration file

The input configuration file is made up of four broad sections; the description of the population structure and parameters (the population section), the estimation methods and variables (the estimation section), the observations and their associated likelihoods (the observation section), and the outputs and reports that CASAL2 will return (the report section). The input configuration file is made up of a number of commands (many with subcommands) which specify various options for each of these components.

The command and subcommand definitions in the input configuration file can be extensive (especially when you have a model that has many observations), and can result in a input configuration file that is long and difficult to navigate. To aid readability and flexibility, we can use the input configuration file command `!include file`. The command causes an external file, *file*, to be read and processed, exactly as if its contents had been inserted in the main input configuration file at that point. The file name must be a complete file name with extension, but can use either a relative or absolute path as part of its name. Note that included files can also contain `!include` commands. See Section 12 for more detail.

### 3.3. Redirecting standard output

CASAL2 uses the standard output stream `standard output` to display run-time information. The standard error stream is used by CASAL2 to output the program exit status and run-time errors. We suggest redirecting both the standard output and standard error into files. With the bash shell (on Linux systems), you can do this using the command structure,

```
(casal2 [arguments] > out) >& err &
```

It may be useful to redirect the standard input, especially if you're using CASAL2 inside a batch job software, i.e.

```
(casal2 [arguments] > out < /dev/null) >& err &
```

On Microsoft Windows systems, you can redirect to standard output using,

```
casal2 [arguments] > out
```

And, on some Microsoft Windows systems (e.g., Windows10), you can redirect to both standard output and standard error, using the syntax,

```
casal2 [arguments] > out 2> err
```

Note that CASAL2 outputs a few lines of header information to the output. The header consists of the program name and version, the arguments passed to CASAL2 from the command line, the date and time that the program was called (derived from the system time), the user name, and the machine name (including the operating system and the process identification number). These can be used to track outputs as well as identifying the version of CASAL2 used to run the model.

### 3.4. Command line arguments

The call to CASAL2 is of the following form:

```
casal2[-c config_file] [task] [options]
```

**-c *config\_file*** Define the input configuration file for CASAL2. If omitted, then CASAL2 looks for a file named `config.csl2`.

and where *task* is one of;

**-h** Display help (this page).

**-l** Display the reference for the software license (GPL v2).

**-v** Display the CASAL2 version number.

**-r** Run the model once using the parameter values in the input configuration file, or optionally, with the values from the file denoted with the command line argument `-i file`.

**-e** Do a point *estimate* using the values in the input configuration file as the starting point for the parameters to be estimated, or optionally, with the start values from the file denoted with the command line argument `-i file`.

- p** Do a likelihood *profile* using the parameter values in the input configuration file as the starting point, or optionally, with the start values from the file denoted with the command line argument `-i file`.
- m** Do an *MCMC* estimate using the values in the input configuration file as the starting point for the parameters to be estimated, or optionally, with the start values from the file denoted with the command line argument `-i file`.
- f** Project the model *forward* in time using the parameter values in the input configuration file as the starting point for the estimation, or optionally, with the start values from the file denoted with the command line argument `-i file`.
- s number** Simulate the *number* of observation sets using values in the input configuration file as the parameter values, or optionally, with the values for the parameters denoted as estimated from the file with the command line argument `-i file`.

In addition, the following are optional arguments [*options*],

- i file** Input one or more sets of free (estimated) parameter values from *file*. See Section 11 for details about the format of *file*.
- o file** Output a report of the free (estimated) parameter values in a format suitable for `-i file`. See Section 11 for details about the format of *file*.
- g seed** Seed the random number *generator* with *seed*, a positive (long) integer value. Note, if `-g` is not specified, then CASAL2 will generate a random number seed based on the computer clock time.
- loglevel** arg = {trace, finest, fine, medium} See Section 7.
- tabular** Run with `-r` or `-f` command it will print @report in tabular format. See Section 7.
- single-step** Run with `-r`, this additional option will pause the model and ask the user to specify parameters and their values to use for the next iteration. See Section 4.6.1.

### 3.5. Constructing a CASAL2 input configuration files

The model definition, parameters, observations, and reports are specified in an input configuration files. The population section is described in Section 4 and the population commands in Section 8. Similarly, the estimation section is described in Section 5 and its commands in Section 9, and in Section 7 and Section 11 for the report and report commands.

#### 3.5.1. Commands

CASAL2 has a range of commands that define the model structure, processes, observations, and how tasks are carried out. There are three types of commands,

1. Commands that have an argument and do not have subcommands (for example, `!include file`)
2. Commands that have a label and subcommands (for example @process must have a label, and has subcommands)
3. Commands that do not have either a label or argument, but have subcommands (for example @model)

Commands that have a label must have a unique label, i.e., the label cannot be used on more than one command of that type. The labels can contain alpha numeric characters, period ('.'), underscore ('\_') and dash ('-'). Labels must not contain white-space, or other characters that are not letters, numbers, dash, period or an underscore. For example,

```
@process NaturalMortality
or
!include MyModelSpecification.csl2
```

### 3.5.2. Subcommands

Subcommands in CASAL2 are for defining options and parameter values for commands. They always take an argument which is one of a specific *type*. The types acceptable for each subcommand are defined in Section 12, and are summarised below.

Like commands (@command), subcommands and their arguments are not order specific — except that that all subcommands of a given command must appear before the next @command block. CASAL2 may report an error if they are not supplied in this way, however, in some circumstances a different order may result in a valid, but unintended set of actions, leading to possible errors in your expected results.

The arguments for a subcommand are either:

<b>switch</b>	true/false
<b>integer</b>	an integer number,
<b>integer vector</b>	a vector of integer numbers,
<b>integer range</b>	a range of integer numbers separated by a colon (:), e.g. 1994:1996 is expanded to an integer vector of values 1994 1995 1996),
<b>constant</b>	a real number (i.e. double),
<b>constant vector</b>	a vector of real numbers (i.e. vector of doubles),
<b>estimable</b>	a real number that can be estimated (i.e. estimable double),
<b>estimable vector</b>	a vector of real numbers that can be estimated (i.e. vector of estimable doubles),
<b>string</b>	a categorical (string) value, or
<b>string vector</b>	a vector of categorical values.

Switches are parameters which are either true or false. Enter *true* as true or t, and *false* as false or f.

Integers must be entered as integers (i.e., if year is an integer then use 2008, not 2008.0)

Arguments of type integer vector, integer range, constant vector, estimable vector, or categorical vector contain one or more entries on a row, separated by white space (tabs or spaces).

*Estimable* parameters are those parameters that CASAL2 can estimate, if requested. If a particular parameter is not being estimated in a particular model run, then it acts as a constant. Within CASAL2 only estimable parameters can be estimated. And, you have to tell CASAL2 those that are to be estimated in any particular model. Estimable parameters that are being estimated within a particular model run are called the *estimated parameters*.

### 3.5.3. The command-block format

Each command-block either consists of a single command (starting with the symbol @) and, for most commands, a unique label or an argument. Each command is then followed by its subcommands

and their arguments, e.g.,

```
@command, or
@command argument, or
@command label
```

and then

```
subcommand argument
subcommand argument
etc.,
```

Blank lines are ignored, as is extra white space (i.e., tabs and spaces) between arguments. But don't put extra white space before a @ character (which must also be the first character on the line), and make sure the file ends with a carriage return.

There is no need to mark the end of a command block. This is automatically recognized by either the end of the file, section, or the start of the next command block (which is marked by the @ on the first character of a line). Note, however, that the *!include* is the only exception to this rule. See Section 12) for details of the use of *!include*.

Note that in the input configuration file, commands, sub-commands, and arguments are not case sensitive. However, labels and variable values are case sensitive. Also note that if you are on a Linux system then external calls to files are case sensitive (i.e., when using *!include file*, the argument *file* will be case sensitive).

#### 3.5.4. Commenting out lines

Text that follows a # on a line are considered to be comments and are ignored. If you want to remove a group of commands or subcommands using #, then comment out all lines in the block, not just the first line.

Alternatively, you can comment out an entire block or section by placing curly brackets around the text that you want to comment out. Put in a { as the first character on the line to start the comment block, then end it with }. All lines (including line breaks) between { and } inclusive are ignored.

```
# This is a comment and will be ignored
@process NaturalMortality
m 0.2
{
This block of code
is a comment and
will be ignored
}
```

#### 3.5.5. Determining parameter names

When CASAL2 processes a input configuration file, it translates each command and each subcommand into a parameter with a unique name. For commands, this parameter name is simply the command label. For subcommands, the parameter name format is either

```
command[label].subcommand if the command has a label, or
```

`command.subcommand` if the command has no label, or

`command[label].subcommand(i)` if the command has a label and the subcommand arguments are a vector, and we are accessing the  $i$ th element of that vector.

`command[label].subcommand(i:j)` if the command has a label, and the subcommand arguments are a vector, and we are accessing the elements from  $i$  to  $j$  (inclusive) of that vector.

The unique parameter name is used to reference the parameter when estimating, applying a penalty, projecting, time varying or applying a profile. For example, the parameter name of subcommand `m` of the command `@process` with the label `NaturalMortality` is

```
process[NaturalMortality].m
```

#### 3.6. CASAL2 exit status values

When CASAL2 completes its task successfully or errors out gracefully, it returns a single exit status value 'completed' to the standard output. Error messages will be printed to the console. If configuration errors are found, CASAL2 will print an error messages along with the associated files and line numbers where the errors were identified.



---

## 4. The population section

### 4.1. Introduction

The population section specifies the model structure, population dynamics, and other associated parameters. It describes the model structure (population structure), defines the population processes (e.g., recruitment, migration, and mortality), selectivities, and their parameters.

The population section consists of several components, including;

- The population structure;
- Model initialisation (i.e., the state of the partition at the start of the first year);
- The years over which the model runs (i.e., the start and end years of the model)
- The annual cycle (time-steps and processes that are applied in each time-step);
- The specifications and parameters of the population processes (i.e., processes that add, remove individuals to or from the partition, or shift numbers between ages and categories in the partition);
- Selectivities;
- Parameter values and their definitions;
- Derived quantities, required as parameters for some processes (e.g. Mature biomass to resolve any density dependent processes such as the spawner-recruit relationship, in a recruitment process).

### 4.2. Population structure

The basic structure of population section of a CASAL2 model is defined in terms of an annual cycle, time steps, states, and transitions.

The annual cycle defines what processes happen in each model year, and in what sequence. CASAL2 runs on an annual cycle rather than, for example, a 6-monthly cycle.)

Each year is split into one or more time steps, with at least one process occurring in each time step. Each time step can be thought of as representing a particular part of the calendar year, or you can just treat them as an abstract sequence of events. In every time step, there exists a mortality block, this is a block (a group of consecutive processes) where individuals are removed from the partition. If there are no mortality processes then the mortality block is empty (nothing happens) and occurs at the end of a time step. CASAL2 will error out if the user defines multiple mortality processes in a single time step, that are not consecutive processes.

The state is the current status of the population, at any given time. The state can change one or more times in every time step of every year. The state object must contain sufficient information to figure out how the underlying population changes over time (given a model and a complete set of parameters).

There are a number of possible changes in the state, which are called transitions. These include processes that include recruitment, natural mortality, anthropogenic mortality, ageing, migration, tagging events, and maturation. Different processes may be useful for different models in different circumstances.

The division of the year into an arbitrary number of time steps allows the user to specify the exact order in which processes and observations occur throughout the year. The user needs to specify the

time step in which each process occurs. If more than one process occurs in the same time step, they will be applied in the order specified in the @time\_step block.

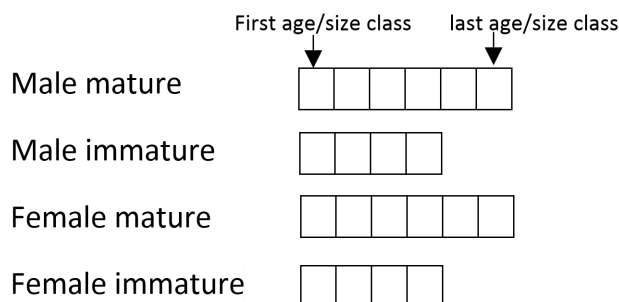
The key element of the state is the partition. This is a broadly applicable concept that can be used to describe many different kinds of population model. The partition is simply a breakdown of the total number of individuals in the current population into different categories. (Note that the partition records numbers of individuals, not biomass). The individuals are grouped into categories, for example, sex, maturity state, area, and species. However CASAL2 has no predefined categories, and these are defined by the user. This differs from CASAL (Bull et al., 2012) that has only pre-defined partition categories.

The resulting partition can be conceptualised as matrix, where each row is represented by a category and the columns are the age classes, shown in Figure 4.1. Each row represents the number of individuals for that category in that age class.

The names of categories are user defined, and there must be at least one category defined for a model. The ages are defined as a sequence from  $age_{min}$  to  $age_{max}$ , with the last age optionally a plus group. In order to calculate biomass, the age-length relationship for each category must also be defined for an age based model (but could be defined as ‘none’). An example of how this is specified for four categories based on sex and area is as follows,

```
@categories
format mature.sex
names  spawn.male  spawn.female  nonspawn.male  nonspawn.female
age_lengths  male_AL  female_AL  male_AL  female_AL
```

For an example of these ideas, consider a model of a fish population with a mature and non-spawning fishery. If we assume that the non-spawning fishery happens over most of the year (say 10 months) in the non-spawning area. The mature fish then migrate to the spawning area, where the spawning fishery operates. At the end of spawning, these fish, along with the recruits from the previous year, migrate back to the non-spawning area. The modeller decides that fish will be divided in the partition by age, sex, maturity, and area (spawning and non-spawning grounds). So the partition has 8 rows (2 sexes (mature or immature) 2 areas) and one column per age class.



**Figure 4.1: A visual representation of a partition**

So they define four time steps, labelled 1 through 4. Step 1 includes the non-spawning fishery. Step 2 includes the migration to the spawning area. Step 3 includes the spawning fishery. Step 4 includes recruitment and the migration back to the non-spawning area. (In fact, they could have used only 3 time steps, by using a single step in place of their steps 2 and 3. Because the default order of processes within a time step places migrations before fisheries, the processes would still have occurred in the right order.) There are other details to be sorted out, such as the proportion of

natural mortality occurring in each time step and where observations occur, but this gives the basic idea.

This structure can be used to implement complex models, with intermingling of separate species and stocks, with complex migration patterns over multiple areas, and multiple sources of anthropogenic impact using different methods and covering different areas and times. However, we note that there is little point in using a complex structure to model a population when there are no observations to support that structure. In other words, use a structure for your model that is compatible with the data available.

The model is run from an initial year up to the final(current) year. It can also be run past the final year to make projections — things that happen in the future — up to the final projection year.

An example, to specify a model with 2 categories (male and female) with ages 1-20 (with the last age a plus group) and an age-length relationship defined with the label `male-growth` and `female-growth`, then the `@model` example from above becomes,

```
@model
start_year
final_year
min_age 1
max_age 20
age_plus_group True
initialisation_phases iphase
time_steps step1 step2
```

### 4.3. The state object and the partition

The key component of the state object is the partition, a matrix that store numbers of individuals at age for each category. A category represents a group of individuals that have the same specific attributes, examples of such attributes include life histories and growth rates, etc. For example, categories may include labels such as:

- Sex (male or female);
- Area (any number of areas, named by the user);
- Maturity (immature or mature);
- Growth-path (any number of growth-paths);
- Tag (any number of tagging events);
- Species

A stock can be thought of as a population of individuals which recruits separately. See Section 4.11 for the treatment of maturity when it is not a category in the partition.

So, you need to tell CASAL2 the following:

- The minimum and maximum age classes in an age-based model.
- Whether there is an age-plus group.
- The names of all categories.

Age classes are always one year wide, except that the maximum age group can optionally be a plus group. Users need to choose the minimum and maximum age classes.

CASAL2 allows categories of the partition to exist for certain years of the model. This is added for computational efficiency, when models contain a large number of categories that do not persist for all model years. Situations where this is beneficial is when a model contains a process that does a one off transition of fish from one category into another category in a subset of the model initialisation phases or years (for example, tagging events). Excluding categories for certain years can save a considerable amount of time as CASAL2 does not need to, for example, initialising empty categories or implement processes in time periods when they have no effect.

Another important component of the state object in CASAL2 are derived quantities. This includes quantities such as a mature biomass (for example, in fisheries models, the mid-spawning season biomasses of spawning fish, SSB) for either one or sum of more than one category. CASAL2 derives through the command `@derived_quantity`, and may be required in the specification of some processes (i.e., in fisheries models, a recruitment process that specifies a stock recruitment relationship requires the definition of a derived quantity that specifies the mid-season spawning stock biomass).

### 4.4. Time sequences

The time sequence of the model is defined in the following parts;

- Annual cycle
- Initialisation
- Model run years
- Projection years

#### Annual cycle

The annual cycle is implemented as a set of processes that occur, in a user-defined order, within each year. Time-steps are used to break the annual cycle into separate components, and allow observations to be associated with different time periods and processes. Any number of processes can occur within each time-step, in any order (although there are some limitations - see later) and can occur multiple times within each time-step. Note that time-steps are not implemented during the initialisation phases (effectively, there is only one time-step), and that the annual cycle in the initialisation phases can, optionally, be different from that which is applied during the model years.

#### 4.4.1. Initialisation

There are multiple methods to initialise a partition in CASAL2. These methods are: iterative, fixed, derived, and Cinitial. Model initialisation can occur in several phases, each of which can be a different method. At the end of the initialisation step, CASAL2 then runs through the model years carrying out processes in the order defined in the annual cycle, and can evaluate expected values of observations in order to calculate likelihoods, project the model forward to determine future states, or simulate observations from the current state.

#### Iterative Initialisation

One of CASAL2 methods for initialising the initial equilibrium state as an iterative process: a general solution that initialises complex structured models that may be difficult or impossible to

implement using analytic approximations. However, initialising via iteration for a long-lived species with complex transitions can take many iterations and may be slow to run. In CASAL2, we allow for user-defined multi-phased initialisation to allow the user to phase the initialisation and assist with optimising the models for speed. Each phase of the initialisation can involve any number of processes. Note that the number of iterations in the initialisation may affect the model outputs, and that a period should be chosen to allow the population state to fully converge. CASAL2 can report convergence statistics to assist the user determine an appropriate method of initialisation.

In addition, each initialisation phase can optionally be stopped early if a user defined convergence criteria is met. For a set of user defined years in the initialisation phase, convergence is defined as met if the proportional absolute summed difference between the the state in year  $t - 1$  and the state in year  $t$  ( $\hat{\lambda}$ ) is less than a user defined  $\lambda$  where,

$$\hat{\lambda} = \frac{\sum_i \sum_j |\text{element}(i, j)_t - \text{element}(i, j)_{t-1}|}{\sum_i \sum_j \text{element}(i, j)_t} \quad (4.1)$$

In each initialisation phase, the processes defined for that phase are carried out and used as the starting point for the following phase or, if it is the last phase, then the years that the model is run over. The *first* phase is always initialised with each element (i.e., each age and category) set at zero. Note that this means that recruitment processes where the numbers of recruits is based on a stock recruitment or density dependant relationship will likely fail if used in the first phase of an initialisation.

The multi-phase iteration allows the user to determine if the initialisation has converged in a particular model run. Here, add an additional initialisation phase for, say, 1 year as the last initialisation phase (with the same processes applied). Then, using the initialisation reports (`@report[label].type=initialisation_partition`), print a copy of the partition just before and just after that phase. If the initialisation has converged to an equilibrium state, then the partition at both these time intervals will be the same.

Hence, for an iterative initialisation you need to define;

- The initialisation phases.
- The number of years in each phase and the processes to apply in each (default is the annual cycle).

### Derived Initialisation

Derived initialisation is an analytical solution to calculate the equilibrium plus group using a geometric series. The benefit of this method is it can be solved in `max_age - min_age + 1` years, so is computationally faster than the iterative initialisation phase. Users should be warned that we have found under some process combinations (for example. one way migrations) that this solution does not reach the exact equilibrium partition. We advise to use this method for the computation benefits, but you should always compare to an iterative initialisation to satisfy the assumption that the partition is at an equilibrium state.

### Cinital Initialisation

This phase can only be applied once a derived or iterative initialisation phases has been implemented. It works off an equilibrium state and uses Cinital factors that can be estimated to shift the initial

population away from an equilibrium state prior to start year. If there is known exploitation before data exists for a population this can be a solution for estimating a non equilibrium population. Note that it may be advisable to include an observation of age composition data for the first year of the model in order to estimate the non equilibrium population state.

### Fixed Initialisation

This is a user defined table that is taken to be the initial partition prior to start year. Users have the ability to initialise models by specify the numbers at age for each category. See initialisation type `state_category_by_age` for how to implement this.

## 4.5. Model run years

Following initialisation, the model then runs over a number of user-defined years from (`initial_year` to `final_year`). For this part of the model, the annual cycle can be broken into separate time-steps, and observations can be associated with the state of the model at the end of any time-step, i.e., likelihoods for particular observations are evaluated, if required, within each time-step.

Processes are carried out in the order specified within each time-step, and can be the same or different to processes in other initialisation phases of the model. The run years define the years over which the model is to run and the annual cycle within each year. The model runs from the start of year `initial` and runs to the end of year `current`. The projection part then extends the run time up to the end of year `final`.

- The time-steps and the processes applied in each
- The initial year (i.e., the model start year)
- The final year (i.e., the model end year)
- The projection final year (i.e., the model projection end year)

## 4.6. Projection years

Projection years follow model run years. Projecting is the process of running the model forwards into the future, using stochastic and or deterministic values for population dynamic parameters, such as recruitments and catches. In a projection run in CASAL2 a model is initialised and run through the model years from `initial` to the `final`. Then, the model is re-run from `initial` to `projection_final_year`, where any parameter can be fixed or drawn from a stochastic process between this time period. CASAL2 does not have default projections. Users must specify them using the `@project` command blocks. This is important for parameters that are year specific such as year class parameters. If there is no `@project` for these parameters, they will not exist after `final_year` processes that call them will cause nonsensical output. Any estimable parameter can be projected forward. The types of processes where parameters are drawn during the projection years are: constant, lognormal, and empirical sampling.

### Constant

A parameter can be fixed during all projection years or can be individually specified for each projection year. This is a deterministic process, where we are assuming the parameter is known without error for future years.

## Empirical Sampling

Parameters that are of type vector or map are re-sampled with replacement between a year range for projected years. This process redraws from the empirical distribution of their values.

## Lognormal

The randomised parameter are lognormally distributed, with mean 1, and specified standard deviation and autocorrelation on the log-scale.  $YCS_i = \exp(X_i)$ , where  $(X_i)$  are generated as a Gaussian process with standard deviation  $\sigma_R$  and mean  $-0.5 \sigma_R$  (so that the mean of the parameter will be 1). If the randomised parameter are modified by an arbitrary multiplier, then the only change is that parameter will have mean  $\mu$ , where  $\mu$  is the multiplier.

### 4.6.1. Single stepping CASAL2

CASAL2 has the ability to pause after calculating the model state and outcome at the end of a year and query the user to input updated estimable parameters for the next year. This is an active area of development for CASAL2. The aim of this is to allow CASAL2 to be used for operational management procedures or other similar studies. For example, CASAL2 could be called and controlled by **R** to update and provide management actions (for examples, catches in a fisheries model) using a harvest control rule to evaluate management strategies.

## 4.7. Population processes

Population processes are those processes that change the model state. Processes produce changes in the model partition, by adding, removing or moving individuals between ages and/or categories. The population processes include recruitment, ageing, mortality events (e.g., natural and anthropogenic) and category transition processes (i.e., processes that move individuals between categories while preserving their age structure). See Section 4 for a complete list of available processes.

There are two types of processes, processes that occur across multiple time steps in the annual cycle e.g Natural Mortality and Instantaneous Mortality. There are also processes that only occur within the time step they are defined. Each of these processes is carried out in the user-defined prescribed order when initialising the model, and then for a user-defined order in each year in the annual cycle.

### 4.7.1. Recruitment

Recruitment processes are defined as a process that introduces new individuals into the model. CASAL2 currently implements two types of recruitment process, constant recruitment and Beverton-Holt recruitment (Beverton and Holt, 1957).

In the recruitment processes, the number of individuals are added to a single age class within the partition, with the amount defined by the type of recruitment process and its function. If more than one category is defined, then the proportion of recruiting individuals to be added to each category is specified by the `proportions` parameter. For example, if recruiting to categories labelled male and female, then you might set the proportions as 0.5 and 0.5 respectively to denote that half of the recruits recruit to the male category and the remaining half to the female category.

For the constant and Beverton-Holt recruitment processes, the number of individuals following

recruitment in year  $y$  is,

$$N_{i,j} \leftarrow N_{i,j} + p_j(R_y) \quad (4.2)$$

where  $N_{i,j}$  is the numbers in category  $j$  at age  $i$ ,  $p_j$  is the proportion to category  $j$ , and  $R_y$  is the number of recruits for year  $y$ . See below for how  $R_y$  is determined in each of these cases.

### Constant Recruitment

In the constant recruitment process the total number of recruits added each year is  $R_y$ , and is simply  $R_0$ , i.e.

$$R_y = R_0 \quad (4.3)$$

Constant recruitment recruits a constant number of individuals each year. It is equivalent to a Beverton-Holt recruitment process with steepness set equal to one ( $h = 1$ ).

For example, to specify a constant recruitment process, where individuals are added to male and female immature categories at  $age = 1$ , and the number to add is  $R_0 = 5 \times 10^5$ , then the syntax is

```
@process Recruitment
type constant_recruitment
categories male.immature female.immature
proportions 0.5 0.5
r0 500000
age 1
```

### Beverton-Holt recruitment

In the Beverton-Holt recruitment process the total number of recruits added each year is  $R_y$ , and is the product of the average recruitment  $R_0$ , the annual year class strength multiplier,  $YCS$ , and the stock-recruit relationship i.e.,

$$R_y = R_0 \times YCS_{y-ssb\_offset} \times SR(SSB_{y-ssb\_offset}) \quad (4.4)$$

where  $ssb\_offset$  is the number of years offset to link the year class with the year of spawning  $y$ , and  $SR$  is the Beverton-Holt stock-recruit relationship parametrised by the steepness  $h$ ,

$$SR(SSB_y) = \frac{SSB_y}{B_0} / \left( 1 - \frac{5h-1}{4h} \left( 1 - \frac{SSB_y}{B_0} \right) \right) \quad (4.5)$$

Note that the Beverton-Holt recruitment process requires a value for  $B_0$  and  $SSB_y$  to resolve the stock-recruitment relationship. Here, a derived quantity (see Section 4.8) must be defined that provides the annual  $SSB_y$  for the recruitment process.  $B_0$  is then defined as the value of the  $SSB$  at the end of one of the initialisation phases. During initialisation the  $YCS$  multipliers are assumed to be equal to one, and recruitment that happens in the initialisation phases that occur before and during the phase when  $B_0$  is determined is assumed to have steepness  $h = 1$  (i.e. in those initialisation phases, recruitment is simply equal to  $R_0$ ). Recruitment in the initialisation phases after the phase where  $B_0$  was determined follow the Beverton-Holt stock-recruit relationship defined above.  $R_0$  and  $B_0$  have a direct relationship when there are no density dependent processes, for this reason users can choose to initialise models using  $B_0$  or  $R_0$ . In New Zealand  $B_0$  is often used, as biological reference points for managing marine populations is based on a percentage of  $B_0$ .



Year classes are standardised to be equal to one over the period  $S$  defined by standardise YCS years, i.e., the year classes (YCS) for each year of the model are calculated as

$$YCS_i = \begin{cases} Y_i / \text{mean}_{y \in S} & : y \in S \\ Y_i & : y \notin S \end{cases}$$

Note that the an effect of this parameterisation is that  $R_0$  is then defined as the mean estimated recruitment over the years  $S$ , because the mean year class multiplier over these years will always be one.

For example, assume a Beverton-Holt recruitment process, where individuals are added to the category ‘immature’ at  $age = 1$ , the number to add is  $R_0 = 5 \times 10^5$ . Then `SSB_derived_quantity` is a derived quantity that specifies the total spawning stock biomass, with  $B_0$  the value of the derived quantity at the end of the initialisation phase labelled `phase1`. The YCS are standardised to have mean one in the period 1994 to 2004, and recruits enter into the model two years following spawning. Then the command specification would be,

```
@process Recruitment
type recruitment_beverton_holt
categories immature
proportions 1.0
r0 500000
b0_initialisation_phase phase1
steepness 0.75
age 1
ssb SSB_derived_quantity
standardise_ycs_years 1994-2004
ycs_years 1994 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006
YCS_values 1 1 1 1 1 1 1 1 1 1 1 1 1
```

Note that the SSB year used in the Beverton-Holt stock recruitment relationship (`ssb_offset`) is determined by the order of ageing, recruitment, and spawning,

- If recruitment then ageing then spawning, then `ssb_offset` should equal `min_age + 1`.
- If spawning then ageing then recruitment, then `ssb_offset` should equal `min_age - 1`.

If any other order is used, then `ssb_offset` should equal `min_age`.

If you have more than one ageing process and a Beverton-Holt recruitment process you will be warned to set your own `ssb_offset` as CASAL2 will, by default, set it based upon the first ageing process in the annual cycle — which may be not be what was desired.

#### 4.7.2. Ageing

The ageing process ‘ages’ individuals — it simply moves all individuals in the named categories  $i$  to the next age class  $j + 1$ , or accumulates them if the last age class is a plus group.

The ageing process is defined as,

$$\text{element}(i, j) \leftarrow \text{element}(i, j - 1) \quad (4.6)$$

except that in the case of the plus group (if defined),

$$\text{element}(i, \text{age}_{\max}) \leftarrow \text{element}(i, \text{age}_{\max}) + \text{element}(i, \text{age}_{\max-1}). \quad (4.7)$$

For example, to apply ageing to the categories `immature` and `mature`, then the syntax is,

```
@process Ageing
type ageing
categories immature mature
```

Note that ageing is *not* applied by CASAL2 by default. As with other processes, CASAL2 will not apply a process unless its defined and specified as a process within the annual cycle. Hence, it is possible to specify a model where a category is not aged. CASAL2 will not check or otherwise warn if there is a category defined where ageing is not applied.

### 4.7.3. Mortality

Four types of mortality processes are permissible in CASAL2, constant rate, event, biomass-event and instantaneous. These processes remove individuals from the partition, either as a rate, as a total number (abundance), as a biomass of individuals or as a mixture of these. Note that CASAL2 does not (yet) implement the Baranov catch equation. To apply both natural and biomass-event mortality, users can use `mortality_instantaneous`.

Note that all mortality processes occur within a ‘mortality block’ of a time step. The mortality block is defined as the part of a time-step where a number of consecutive mortality processes occur sequentially. Each time step can have at most one mortality block, and if no mortality processes occur in a time step then it defaults to the end of the time step. CASAL2 will error out if you attempt to put multiple mortality processes into a single time step in such a way that they are not consecutive. Note that the definition of mortality blocks is an important concept in the model structure, and is used for derived quantities (see Section 4.8) and observations (see Section 6).

#### 4.7.3.1. Constant mortality rate

To specify a constant annual mortality rate ( $M = 0.2$ ) for categories ‘male’ and ‘female’, then,

```
@process NaturalMortality
type mortality_constant_rate
categories male female
selectivities One One
m 0.2 0.2
```

Note that the mortality rate process requires a selectivity. To apply the same mortality rate over all age classes, use a selectivity defined as  $S_j = 1.0$  for all ages  $j$ , e.g.,

```
@selectivity One
type constant
c 1
```

#### 4.7.3.2. Event and biomass-event mortality

The event mortality process and biomass mortality processes act in a similar manner, except that they remove a specified abundance (number of individuals) or biomass respectively. These can be used to include anthropogenic mortality where numbers of removals are known, for example, fishing in a fisheries model, rather than applying mortality as a rate.

In these cases, the abundance or biomass removed is also constrained by a maximum exploitation rate. CASAL2 removes as many individuals or as much biomass as it can while not exceeding the maximum exploitation rate. When minimising, event mortality processes require a penalty to discourage parameter values that do not allow the defined number of individuals to be removed. Here, the model penalises those parameter estimates that result in an too low a number of individuals in the defined categories (after applying selectivities) to allow for removals at the maximum exploitation rate. See Section 5.8 for more information on how to specify penalties.

For example, the event mortality applied to user-defined categories  $i$ , with the numbers removed at age  $j$  determined by a selectivity-at-age  $S_j$  is applied as follows:

First, calculate the vulnerable abundance for each category  $i$  in  $1 \dots I$  for ages  $j = 1 \dots J$  that are subject to event mortality,

$$V(i, j) = S(j)N(i, j) \quad (4.8)$$

And hence define the total vulnerable abundance  $V_{total}$  as,

$$V_{total} = \sum_i \sum_j V(i, j) \quad (4.9)$$

Hence the exploitation rate to apply is

$$U = \begin{cases} C/V_{total}, & \text{if } C/V_{total} \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \quad (4.10)$$

And the number removed  $R$  from each age  $j$  in category  $i$  is,

$$R(i, j) = UV(i, j) \quad (4.11)$$

For example, to specify fishing mortality in a fisheries model, with catches given for a set of specific years, over categories 'immature' and 'mature', with selectivity 'FishingSel' and assuming a maximum possible exploitation rate of 0.7, then the syntax would be,

```
@process Fishing
type event_mortality
categories immature mature
years 2000 2001 2002 2003
U_max 0.70
selectivities FishingSel FishingSel
penalty event_mortality_penalty
```

#### 4.7.3.3. Instantaneous mortality

The instantaneous mortality process is a process that combines both natural mortality and event biomass mortality into a single process. This allows the natural mortality to occur across multiple time steps, and can specify multiple instances of event mortality to account for, say, multiple fisheries operating sequentially or concurrently. This process applies half the natural mortality in each time step, then the mortalities from all the concurrent fisheries instantaneously, then the remaining half of the natural mortality.

When instantaneous mortality is applied the following equations are used.

- An exploitation rate (actually a proportion) is calculated for each fishery, as the catch over the selected-and-retained biomass,

$$U_f = \frac{C_f}{\sum_j \bar{w}_j S_{f,j} n_j e^{-0.5tM_j}}$$

- The fishing pressure associated with fishery  $f$  is defined as the maximum proportion of fish taken from any element of the partition in the area affected by fishery  $f$ ,

$$U_{f,obs} = \max_j (\sum_k S_{k,j} U_k)$$

where the maximum is over all partition elements affected by fishery  $f$ , and the summation is over all fisheries  $k$  which affect the  $j$ th partition element in the same time step as fishery  $f$ .

In most cases the fishing pressure will be equal to the exploitation rate (i.e.,  $U_{f,obs} = U_f$ ), but they can be different if (a) there is another fishery operating in the same time step as fishery  $f$  and affecting some of the same partition elements, and/or (b) the selectivity  $S_{f,j}$  does not have a maximum value of 1.

There is a maximum fishing pressure limit of  $U_{f,max}$  for each fishery  $f$ . So, no more than proportion  $U_{f,max}$  can be taken from any element of the partition affected by fishery  $f$  in that time step. Clearly  $0 \leq U_{max} \leq 1$ . It is an error if two fisheries which affect the same partition elements in the same time step do not have the same  $U_{max}$ .

For each  $f$ , if  $U_{f,obs} > U_{f,max}$ , then  $U_f$  is multiplied by  $U_{f,max}/U_{f,obs}$  and the fishing pressures are recalculated. In this case the catch actually taken from the population in the model will differ from the specified catch,  $C_f$ .

- The partition is updated using

$$n'_j = n_j \exp(-tM_j) [1 - \sum_f S_{f,j} U_f]$$

An example of the syntax is if we want to apply natural mortality of 0.20 across three time steps on both male and female categories. And we have two fisheries FishingWest FishingEast with there respective catches known for years 1975:1977 in kilograms. These are given in the catches table and information on selectivities, penalties and maximum exploitation rates are given in the fisheries table.

```
@process instant_mort
type mortality_instantaneous
m 0.20
time_step_ratio 0.42 0.25 0.33
selectivities One
categories male female
units kgs
```

```
table catches
year FishingWest FishingEast
1975 80000 111000
1976 152000 336000
1977 74000 1214000
end table
```

```
table fisheries
fishery      category  selectivity u_max  time_step penalty
FishingWest  stock     westFSel   0.7   step1    CatchPenalty
FishingEast  stock     eastFSel   0.7   step1    CatchPenalty
end_table
```

#### 4.7.4. Transition By Category

This process covers moves individuals between categories. Because the CASAL2 partition user defined, this type of process is used to move individuals between categorised, and is used to specify processes such as maturation (move individuals from an immature to mature state) or migration (move individuals from one area to another).

##### 4.7.4.1. Annual transition by category

A special case is annual transition by category, which allows a transition to occur in a specific subset of years only, where each year can have a different rate.

In both cases, there has to be a one to one relationship between the ‘from’ category and the ‘to’ category — for every source category there is one target category. If however, you want to merge categories, then just repeat the ‘to’ category multiple times.

$$N_{a,j} = N_{a,i} \times P_i \times S_{a,i} \quad (4.12)$$

where  $N_{a,j}$  is the number of individuals that have moved to category  $j$  from category  $i$  in age  $a$  and  $N_{a,i}$  is the number of individuals in category  $i$ .  $P_i$  is the proportion parameter for category  $i$  and  $S_{a,i}$  is the selectivity at age  $a$  for category  $i$ .

An example, to specify a simple spawning migration of mature males from a western area migrating to an eastern (spawning) area, then the syntax is

```
@process Spawning_migration
type category_transition
from West.males
to East.males
selectivities MatureSel
proportions 1
```

Where `MatureSel` is a selectivity that describes the proportion of age or length classes that are mature and thus move to the eastern area.

#### 4.7.5. Tag Release events

Tagging processes can be age or length based processes, where by numbers of fished are moved from an untagged category to a tagged category that the user has defined in the `@Categories` block. Tag release processes can also account for tag induced mortality on individuals. Age based tag release events take a known number of individuals tagged for each age and do a straightforward category transition along with extra mortality. Length based tag release processes are more complicated, as CASAL2 needs to calculate the age length matrix and exploitation by each length to then move the correct numbers at age based on a length input.

#### 4.7.6. Tag Loss

Tag Loss is the process where tags are lost from tagged categories over time from tag failure or getting knocked off. This process is applied as a instantaneous mortality rate that can happen over multiple time steps in the annual cycle. This method assumes when tags are lost that the

fish is removed from the partition. All though this seems logically incorrect, we are dealing with such a small number of fish that the impact is minimal and computationally simpler. Note that if your tagging events make up a large proportion of the population you may want to adjust this method. There will be two types of tag loss processes that are termed `single` and `double`. Currently only `single` exists in CASAL2. `double` will deal with situations where a tag release process tags individuals with two tags. In which there is another formulae to work out the rate of tag loss.

```
@process Tag_loss
type tag_loss
categories tagged_fish
tag_loss_rate 0.02
time_step_ratio 0.25 0.75
selectivities One
tag_loss_type single
year 1985
```

#### 4.8. Derived quantities

Some processes require, as arguments, a population value derived from the population state. These are termed `derived quantities`. Derived quantities are values, calculated by CASAL2 as the end of a specified time-step in every year, and hence they have a single value for each year of the model. Derived quantities can be calculated as either an abundance or as a biomass. Abundance derived quantities are simply the count or sum of categories (after applying a selectivity). Biomass derived quantities are similar, except they are a measure of biomass. Derived quantities are also calculated during the initialisation phases, and hence the time-step during each phase must also be specified. If the initialisation time-steps are not specified, CASAL2 will calculate the derived quantity during the initialisation phases in every year, at the end of the annual cycle.

Derived quantities are required by some processes, for example the Beverton-Holt recruitment process. The Beverton-Holt recruitment process can require an equilibrium biomass ( $B_0$ ) and annual spawning stock biomass values ( $SSB_y$ ) to resolve the stock-recruit relationship. Here, these would be defined as the abundance or biomass of a part of the population at some point in the annual cycle for selected ages and categories, and would be calculated as a derived quantity.

Derived quantities are associated with a mortality block see section 4.7.3 for more detail on mortality blocks. Users can ask for derived quantities partway through mortality blocks. Currently two methods are implemented in CASAL2 to interpolate derived quantities part-way through a mortality block, these are `weighted_sum` and `weighted_product`, they are defined as,

- `weighted_sum`: after proportion  $p$  of the mortality block, the partition elements are given by  $n_{p,j} = (1 - p)n_j + p'n'_j$
- `weighted_product`: after proportion  $p$  of the mortality block, the partition elements are given by  $n_{p,j} = n_j^{1-p} n_j'^p$

where,  $n_{p,j}$  is the derived quantity at proportion  $p$  of the mortality block for category  $j$ .  $n_j$  is the quantity at the beginning of the mortality block and  $n'_j$  is the quantity at the end of the mortality block.

As an example, to define a biomass derived quantity (say spawning stock biomass,  $SSB$ ) for a model, evaluated at the end of the first time-step (labelled `step_one`), over all 'mature' male and female categories and halfway through the mortality block using the `weighted_sum` method, we would use the syntax,

```
@derived_quantity SSB
type biomass
time_step step_one
categories mature.male mature.female
selectivities One
time_step_proportion 0.5
time_step_proportion_method weighted_sum
```

#### 4.9. Age-length relationship

The age-length relationship defines the length at age (and the weight at length, see Section 4.9) of individuals at age/category within the model. There are three length-age relationships available in CASAL2. The first is the naive no relationship (where each individual has length 1 irrespective of age). The second and third are the von-Bertalanffy and Schnute relationships respectively. The length-at-age relationship is used to determine the length frequency, given age, and then with the length-weight relationship, a weight-at-age of individuals within an age/category.

The three age-length relationships are,

None: where the length of each individual is exactly 1 for all ages, in which case the `none` length-weight relationship must also be used.

von Bertalanffy: where length at age is defined as,

$$\bar{s}(\text{age}) = L_{\infty} (1 - \exp(-k(\text{age} - t_0))) \quad (4.13)$$

Schnute: where length at age is defined as,

$$\bar{s}(\text{age}) = \begin{cases} \left[ y_1^b + (y_2^b - y_1^b) \frac{1 - \exp(-a(\text{age} - \tau_1))}{1 - \exp(-a(\tau_2 - \tau_1))} \right]^{1/b}, & \text{if } a \neq 0 \text{ and } b \neq 0 \\ y_1 \exp \left[ \ln(y_2/y_1) \frac{1 - \exp(-a(\text{age} - \tau_1))}{1 - \exp(-a(\tau_2 - \tau_1))} \right], & \text{if } a \neq 0 \text{ and } b = 0 \\ \left[ y_1^b + (y_2^b - y_1^b) \frac{\text{age} - \tau_1}{\tau_2 - \tau_1} \right]^{1/b}, & \text{if } a = 0 \text{ and } b \neq 0 \\ y_1 \exp \left[ \ln(y_2/y_1) \frac{\text{age} - \tau_1}{\tau_2 - \tau_1} \right], & \text{if } a = 0 \text{ and } b = 0 \end{cases} \quad (4.14)$$

The von Bertalanffy curve is parameterised by  $L_{\infty}$ ,  $k$ , and  $t_0$ ; the Schnute curve (Schnute, 1981) by  $y_1$  and  $y_2$ , which are the mean lengths at reference ages  $\tau_1$  and  $\tau_2$ , and  $a$  and  $b$  (when  $b = 1$ , this reduces to the von Bertalanffy with  $k = a$ ).

When defining length-at-age in CASAL2, you must also define a length-weight relationship (see Section 4.9 below).

**Calculation of length-at-age (in an age-based model)****Interpolation of length-at-age****Size-weight relationship**

There are two length-weight relationships available in CASAL2. The first is the naive no relationship. Here, the weight of an individual, regardless of length, is always 1. The second is the basic relationship.

The two length-weight relationships are,

- None: The length-weight relationship where

$$\text{mean weight} = 1 \quad (4.15)$$

- Basic: The length-weight relationship where the mean weight  $w$  of an individual of length  $l$  is

$$w = al^b \quad (4.16)$$

Note that if a distribution of length-at-age is specified, then the mean weight is calculated over the distribution of lengths, and is

$$w = (al^b) \left(1 + cv^2\right)^{\frac{b(b-1)}{2}} \quad (4.17)$$

where the  $cv$  is the c.v. of lengths-at-age. This adjustment is exact for lognormal distributions, and a close approximation for normal distributions if the c.v. is not large (Bull et al., 2012).

Be careful about the scale of  $a$  — this can easily be specified incorrectly. If the catch is in tonnes and the growth curve in centimetres, then  $a$  should be on the right scale to convert a length in centimetres to a weight in tonnes. Note that there are reports available that can be used to help check that the units specified are plausible (see Section 7).

**Calculation of mean weight****4.10. Weightless model****4.11. Maturity, in models without maturing in the partition**

If maturity is not a character of the partition it can easily be derived at in instance in time using selectivities. Applying a maturity selectivity on to the partition allows CASAL2 to use mature elements in processes, derive mature biomasses estimates (using derived quantities), and report the mature partition as an output.

**4.12. Selectivities**

A selectivity is a function that can have a different value for each age class. Selectivities are used throughout CASAL2 to interpret observations (Section 5) or to modify the effects of processes on each age class (Section 4). CASAL2 implements a number of different parametric forms, including logistic, knife edge, and double normal selectivities. Selectivities are defined in there own command



block (@selectivity), where the unique label is used by observations or processes to identify which selectivity to apply.

Selectivities are indexed by age, with indices from `min_age` to `max_age`. For example, you might have an age-based selectivity that was logistic with 50% selected at age 5 and 95% selected at age 7. This would be defined by the `type=logistic` with parameters  $a_{50} = 5$  and  $a_{0.95} = (7 - 5) = 2$ . Then the value of the selectivity at age  $x = 7$  is 0.95 and the selectivity at  $x = 3$  is 0.05. Note selectivities can be length based, However Caution, more testing is needed for this functionality.

Note that the function values for some choices of parameters for some selectivities can result in a computer numeric overflow error (i.e., the number calculated from parameter values is either too large or too small to be represented in computer memory). CASAL2 implements range checks on some parameters to test for a possible numeric overflow error before attempting to calculate function values. For example, the logistic selectivity is implemented such that if  $(a_{50} - x)/a_{0.95} > 5$  then the value of the selectivity at  $x = 0$ , i.e., for  $a_{50} = 5$ ,  $a_{0.95} = 0.1$ , then the value of the selectivity at  $x = 1$ , without range checking would be  $7.1 \times 10^{-52}$ . With range checking, that value is 0 (as  $(a_{50}x)/a_{0.95} = 40 > 5$ ).

The available selectivities are;

- Constant
- Knife-edge
- All values
- All values bounded
- Increasing
- Logistic
- Inverse logistic
- Logistic producing
- Double normal
- Double exponential
- Cubic spline (Not yet implemented)

The available selectivities are described below.

#### 4.12.1. constant

$$f(x) = C \tag{4.18}$$

The constant selectivity has the estimable parameter  $C$ .

#### 4.12.2. knife\_edge

$$f(x) = \begin{cases} 0, & \text{if } x < E \\ \alpha, & \text{if } x \geq E \end{cases} \tag{4.19}$$

The knife-edge ogive has the estimable parameter  $E$  and a scaling parameter  $\alpha$ , where the default value of  $\alpha = 1$

**4.12.3. all\_values**

$$f(x) = V_x \quad (4.20)$$

The all-values selectivity has estimable parameters  $V_{low}, V_{low+1} \dots V_{high}$ . Here, you need to provide the selectivity value for each age class.

**4.12.4. all\_values\_bounded**

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ V_x, & \text{if } L \leq x \leq H \\ V_H, & \text{if } x > H \end{cases} \quad (4.21)$$

The all-values-bounded selectivity has non-estimable parameters  $L$  and  $H$ . The estimable parameters are  $V_L, V_{L+1} \dots V_H$ . Here, you need to provide an selectivity value for each age class from  $L \dots H$ .

**4.12.5. increasing**

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ f(x-1) + \pi_x(\alpha - f(x-1)), & \text{if } L \leq x \leq H \\ f(\alpha), & \text{if } x \geq H \end{cases} \quad (4.22)$$

The increasing ogive has non-estimable parameters  $L$  and  $H$ . The estimable parameters are  $\pi_L, \pi_{L+1} \dots \pi_H$  (but if these are estimated, they should always be constrained to be between 0 and 1).  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . Note that the increasing ogive is similar to the all-values-bounded ogive, but is constrained to be non-decreasing.

**4.12.6. logistic**

$$f(x) = \alpha / [1 + 19^{(a_{50}-x)/a_{t095}}] \quad (4.23)$$

The logistic selectivity has estimable parameters  $a_{50}$  and  $a_{t095}$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . The logistic selectivity takes values  $0.5\alpha$  at  $x = a_{50}$  and  $0.95\alpha$  at  $x = a_{50} + a_{t095}$ .

**4.12.7. inverse\_logistic**

$$f(x) = \alpha - \alpha / [1 + 19^{(a_{50}-x)/a_{t095}}] \quad (4.24)$$

The inverse logistic selectivity has estimable parameters  $a_{50}$  and  $a_{t095}$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . The logistic selectivity takes values  $0.5\alpha$  at  $x = a_{50}$  and  $0.95\alpha$  at  $x = a_{50} - a_{t095}$ .

**4.12.8. logistic\_producing**

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ \lambda(L), & \text{if } x = L \\ (\lambda(x) - \lambda(x-1)) / (1 - \lambda(x-1)), & \text{if } L < x < H \\ 1, & \text{if } x \geq H \end{cases} \quad (4.25)$$

The logistic-producing selectivity has the non-estimable parameters  $L$  and  $H$ , and has estimable parameters  $a_{50}$  and  $a_{t095}$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . For category transitions,  $f(x)$  represents the proportion moving, not the proportion that have moved. This selectivity was designed for use in an age-based model to model maturity. In such a model, a logistic-producing maturation selectivity will (in the absence of other influences) make the proportions mature follow a logistic curve with parameters  $a_{50}$ ,  $a_{t095}$ .

#### 4.12.9. double\_normal

$$f(x) = \begin{cases} \alpha 2^{-[(x-\mu)/\sigma_L]^2}, & \text{if } x \leq \mu \\ \alpha 2^{-[(x-\mu)/\sigma_R]^2}, & \text{if } x \geq \mu \end{cases} \quad (4.26)$$

The double-normal selectivity has estimable parameters  $a_1$ ,  $s_L$ , and  $s_R$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . It has values  $\alpha$  at  $x = a_1$ , and  $0.5\alpha$  at  $x = a_1 - s_L$  and  $x = a_1 + s_R$ .

#### 4.12.10. double\_exponential

$$f(x) = \begin{cases} \alpha y_0 (y_1/y_0)^{(x-x_0)/(x_1-x_0)}, & \text{if } x \leq x_0 \\ \alpha y_0 (y_2/y_0)^{(x-x_0)/(x_2-x_0)}, & \text{if } x > x_0 \end{cases} \quad (4.27)$$

The double-exponential selectivity has non-estimable parameters  $x_1$  and  $x_2$ , and estimable parameters  $x_0$ ,  $y_0$ ,  $y_1$ , and  $y_2$ .  $\alpha$  is a scaling parameter, with default value of  $\alpha = 1$ . It can be ‘U-shaped’. Bounds for  $x_0$  must be such that  $x_1 < x_0 < x_2$ . With  $\alpha = 1$ , the selectivity passes through the points  $(x_1, y)$ ,  $(x_0, y_0)$ , and  $(x_2, y_2)$ . If both  $y_1$  and  $y_2$  are greater than  $y_0$  the selectivity is ‘U-shaped’ with minimum at  $(x_0, y_0)$ .

#### 4.12.11. spline

The spline selectivity implements a cubic spline that has non-estimable knots, and an estimable value for each knot. The cubic spline is either (i) a natural splines where the second derivatives are set to 0 at the boundaries, i.e., the values at the boundaries are horizontal, (ii) a spline with a fixed first derivative at the boundaries (linear, but not necessarily horizontal) and (iii) spline which turns into a parabola at the boundaries.

### 4.13. Time Varying Parameters

CASAL2 has the functionality to vary a parameter annually between the start and final year of a model run. This can be for blocks of years or specific years if chosen. For years that are not specified the parameter will default to the input or if in a iterative state such as estimation mode, the value being trialled at that iteration. Available methods for time varying a parameter. Where this functionality will become quite useful is in simulating more realistic observations. When you allow fisheries to have annual varying catchabilities and other more realistic model components simulated observations become more real data and thus conclusions based on simulated data are more useful.

**4.13.1. Constant**

Allows a parameter to have an alternative values during certain years, which can be estimated.

**4.13.2. Random Walk**

A random deviate added into the last value drawn from a standard normal distribution. This has an estimable parameter  $\sigma_p$  for each time varying parameter  $p$ . For reproducible modelling, it is highly recommended that users set the seed (see Section 3.4) when using stochastic functionality like this, otherwise reproducing models becomes almost impossible.

**4.13.3. Annual shift**

A parameter generated in year  $y$  ( $\theta'_y$ ) depends on the value specified by the user ( $\theta_y$ ) along with three coefficients  $a, b$  and  $c$  as follows,

$$\bar{\theta}_y = \frac{\sum_y^Y \theta_y}{Y} \quad (4.28)$$

$$\theta'_y = a\bar{\theta}_y + b\bar{\theta}_y^2 + c\bar{\theta}_y^3 \quad (4.29)$$

**4.13.4. Exogenous**

parameters are shifted based on an exogenous variable, an example of this is an exploitation selectivity parameters that may vary between years based on known changes in exploitation behaviour such as season, start time, and average depth of exploitation.

$$\delta_y = a(E_y - \bar{E}) \quad (4.30)$$

$$\theta'_y = \theta_y + \delta_y \quad (4.31)$$

where  $\delta_y$  is the shift or deviation in parameter  $\theta_y$  in year  $y$  to generate the new parameter value in year  $y$  ( $\theta'_y$ ).  $a$  is an estimable shift parameter,  $E$  is the exogenous variable and  $E_y$  is the value of this variable in year  $y$ . For more information readers can see Francis et al. (2003).

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## 5. The estimation section

### 5.1. Role of the estimation section

The role of the estimation section is to define the tasks carried out by CASAL2:

1. Define the objective function (see Section 5.2)
2. Define the parameters to be estimated (see Section 5.3)
3. Calculate a point estimate, i.e., the maximum posterior density estimate (MPD) (see Section 5.4).
4. Calculate a posterior profile selected parameters, i.e., find, for each of a series of values of a parameter, allowing the other estimated parameters to vary, the minimum value of the objective function (see Section 5.5).
5. Generate an MCMC sample from the posterior distribution (see Section 5.6).
6. Calculate the approximate covariance matrix of the parameters as the inverse of the minimizer's approximation to the Hessian, and the corresponding correlation matrix (see Section 5.4).

The estimation section defines the objective function, parameters of the model, and the method of estimation (point estimates, Bayesian posteriors, profiles, etc.). The objective function is based on a goodness-of-fit measure of the model to observations, priors and penalties. See the observation section for a description of the observations, likelihoods, priors and penalties.

### 5.2. The objective function

In Bayesian estimation, the objective function is a negative log-posterior,

$$Objective(p) = -\sum_i \log [L(\mathbf{p}|O_i)] - \log [\pi(\mathbf{p})] \quad (5.1)$$

where  $\pi$  is the joint prior density of the parameters  $p$ .

The contribution to the objective function from the likelihoods are defined in Section 6.1. In addition to likelihoods, priors (see Section 5.7) and penalties (see Section 5.8) are components of the objective function.

Penalties can be used to ensure that the exploitation rate constraints on mortality events (i.e., fisheries) are not breached (otherwise there is nothing to prevent the model from having abundances so low that the recorded mortalities could not have been taken), penalties on category transitions (to ensure there are enough individuals to move), and possibly penalties to encourage estimated values to be similar or smooth, etc.

### 5.3. Specifying the parameters to be estimated

The estimable parameters that will be estimated are defined using `@estimate` commands (see Section 9). An `@estimate` command-block looks like,

```
@estimate process[NaturalMortality].m
```

```
lower_bound 0.1  
upper_bound 0.4  
type uniform
```

See Section 3.5.5 for instructions on how to generate the parameter name. At least one parameter is to be estimated if doing an estimation, profile, or MCMC run. Initial values for the parameters to be estimated will still need to be provided, and these are used as the starting values for the minimiser. However, these may be overwritten if you provide a set of alternative starting values (i.e., using `casal2 -i`, see Section 3.4).

All parameters are estimated within bounds. For each parameter to be estimated, you need to specify the bounds and the prior (type) (Section 5.7). Note that the bounds and prior for each parameter refer to the values of the parameters, not the actual values resulting from the application of the parameter to an equation. Bounds should be carefully chosen as they effect the space in which the minimisers search over. Minimisers convert lower and upper bound into a minimisation space (for example  $-1,1$  space). If estimating only some elements of a vector, either define each element of the vector to be estimated (see 3.5.5) or fix the others by setting the bounds equal.

#### 5.4. Point estimation

Point estimation is invoked with `casal2 -e`. Mathematically, it is an attempt to find a minimum of the objective function. CASAL2 has multiple algorithms for solving (minimising) the optimisation problem. There are three non auto differential minimisers: numerical differences, differential evolution minimiser, and the dlib minimiser. There are also three auto differential minimisers being: ADOL-C, CPPAD, and BETADIFF. For references see section 1.7

##### 5.4.1. The numerical differences minimiser

The minimiser has three kinds of (non-error) exit status, depending on the minimiser:

1. Successful convergence (suggests you have found a local minimum, at least).
2. Convergence failure (you have not reached a local minimum, though you may deem yourself to be ‘close enough’ at your own risk).
3. Convergence unclear (the minimiser halted but was unable to determine if convergence occurred. You may be at a local minimum, although you should check by restarting the minimiser at the final values of the estimated parameters).

You can choose the maximum number of quasi-Newton iterations and objective function evaluations allotted to the minimiser. If it exceeds either limit, it exits with a convergence failure. We recommend large numbers of evaluations and iterations (at least the defaults of 300 and 1000) unless you successfully reach convergence with less. You can also specify an alternative starting point of the minimiser using `casal2 -i`.

We want to stress that the minimisers are local optimisation algorithms trying to solve a global optimisation problem. What this means is that, even if you get a ‘successful convergence’ message, your solution may be only a local minimum, not a global one. To diagnose this problem, try doing multiple runs from different starting points and comparing the results, or doing profiles of one or more key parameters and seeing if any of the profiled estimates finds a better optimum than the original point estimate.

The approximate covariance matrix of the estimated parameters can be calculated as the inverse of the minimiser's approximation to the Hessian, and the corresponding correlation matrix is also calculated. Be aware that

- the Hessian approximation develops over many minimiser steps, so if the minimiser has only run for a small number of iterations the covariance matrix can be a very poor approximation
- the inverse Hessian is not a good approximation to the covariance matrix of the estimated parameters, and may not be useful to construct, for example, confidence intervals.

Also note that if an estimated parameter has equal lower and upper bounds, it will have entries of '0' in the covariance matrix and NaN or -1.#IND (depending on the operating system) in the correlation matrix.

#### 5.4.2. The differential evolution minimiser

The differential evolution minimiser is a simple population based, stochastic function minimizer, but is claimed to be quite powerful in solving minimisation problems. It is a method of mathematical optimization of multidimensional functions and belongs to the class of evolution strategy optimizers. Initially, the procedure randomly generates and evaluates a number of solution vectors (the population size), each with  $p$  parameters. Then, for each generation (iteration), the algorithm creates a candidate solution for each existing solution by random mutation and uniform crossover. The random mutation generates a new solution by multiplying the difference between two randomly selected solution vectors by some scale factor, then adding the result to a third vector. Then an element-wise crossover takes place with probability  $P_{cr}$ , to generate a potential candidate solution. If this is better than the initial solution vector, it replaces it, otherwise the original solution is retained. The algorithm is terminated after either a predefined number of generations (`max_generations`) or when the maximum difference between the scaled individual parameters from the candidate solutions from all populations is less than some predefined amount `tolerance`.

The differential evolution minimiser can be good at finding global minimums in surfaces that may have local minima. However, the speed of the minimiser, and the ability to find a good minima depend on the number of initial 'populations'. Some authors recommend that the number of populations be set at about  $10 * p$ , where  $p$  is the number of free parameters. However, depending on your problem, you may find that you may need more, or that less will suffice.

We note that there is no proof of convergence for the differential evolution solver, but several papers have found it to be an efficient method of solving multidimensional problems. Our (limited) experience suggests that it can often find a better minima and may be faster or longer (depending on the actual model specification) at finding a solution when compared with the numerical differences minimiser. Comparisons with auto-differentiation minimisers or other more sophisticated algorithms have not been made.

#### 5.4.3. Betadiff minimiser

An auto-differentiable minimiser for non-linear models, This is the minimiser from the original CASAL package.

#### 5.4.4. ADOL-C minimiser

An auto-differentiable minimiser for non-linear models.

#### 5.4.5. CPPAD minimiser

An auto-differentiable minimiser for non-linear models.

#### 5.4.6. Dlib minimiser

Non auto-diff minimiser

### 5.5. Posterior profiles

If profiles are requested `casal2 -p`, CASAL2 will first calculate a point estimate. For each scalar parameter or, in the case of vectors or selectivities, the element of the parameter to be profiled, CASAL2 will fix its value at a sequence of  $n$  evenly spaced numbers (*step*) between a specified lower and upper bounds  $l$  and  $u$ , and calculate a point estimate at each value.

By default  $step = 10$ , and  $(l, u) = (\text{lower bound on parameter plus } (range/(2n)), \text{upper bound on parameter less } (range/(2n)))$ . Each minimisation starts at the final parameter values from the previous resulting value of the parameter being profiled. CASAL2 will report the objective function for each parameter value. Note that an initial point estimate should be compared with the profile, not least to check that none of the other points along the profile have a better objective function value than the initial ‘minimum’.

You specify which parameters are to be profiled, and optionally the number of steps, lower bound, and upper bound for each. In the case of vector parameters, you will also need to specify the element of the vector being profiled.

You can also supply the initial starting point for the estimation using `casal2 -i file` — this may improve the minimiser performance for the profiles.

If you get an implausible profile, it may be a result of not using enough iterations in the minimiser or a poor choice of minimiser control variables (e.g., the minimiser tolerance). It also may be useful to try both if the minimisers in CASAL2 and compare the results.

### 5.6. Bayesian estimation

CASAL2 can use a Monte Carlo Markov Chain (MCMC) to generate a sample from the posterior distribution of the estimated parameters `casal2 -m` and output the sampled values to a file (optionally keeping only every  $n$ th set of values).

As CASAL2 has no post-processing capabilities. CASAL2 cannot produce MCMC convergence diagnostics (use a package such as BOA) or plot/summarize the posterior distributions of the output quantities (for example, using a general-purpose statistical or spreadsheet package such as S-Plus, R, or Microsoft Excel).

Bayesian methodology and MCMC are both large and complex topics, and we do not describe either properly here. See Gelman et al. (1995) and Gilks et al. (1994) for details of both Bayesian analysis and MCMC methods. In addition, see Punt & Hilborn (2001) for an introduction to quantitative fish stock assessment using Bayesian methods.

This section only briefly describes the MCMC algorithms used in CASAL2. See Section 9.3 for a better description of the sequence of CASAL2 commands used in a full Bayesian analysis.

CASAL2 uses a straightforward implementation of the Metropolis-Hastings algorithm (Gelman



et al., 1995, Gilks et al., 1994). The Metropolis-Hastings algorithm attempts to draw a sample from a Bayesian posterior distribution, and calculates the posterior density  $\pi$ , scaled by an unknown constant. The algorithm generates a ‘chain’ or sequence of values. Typically the beginning of the chain is discarded and every  $N$ th element of the remainder is taken as the posterior sample. The chain is produced by taking an initial point  $x_0$  and repeatedly applying the following rule, where  $x_i$  is the current point:

- Draw a candidate step  $s$  from a proposal distribution  $J$ , which should be symmetric i.e.,  $J(-s) = J(s)$ .
- Calculate  $r = \min(\pi(x_i + s)/\pi(x_i), 1)$ .
- Let  $x_{i+1} = x_i + s$  with probability  $r$ , or  $x_i$  with probability  $1 - r$ .

An initial point estimate is produced before the chain starts, which is done so as to calculate the approximate covariance matrix of the estimated parameters (as the inverse Hessian), and may also be used as the starting point of the chain.

The user can specify the starting point of the point estimate minimiser using `casal2 -i`. Don’t start it too close to the actual estimate (either by using `casal2 -i`, or by changing the initial parameter values in input configuration file) as it takes a few iterations to form a reasonable approximation to the Hessian.

There are two options for the starting point of the Markov Chain:

- Start from the point estimate.
- Start from a random point near the point estimate (the point is generated from a multivariate normal distribution, centred on the point estimate, with covariance equal to the inverse Hessian times a user-specified constant). This may be useful if the chain gets ‘stuck’ at the point estimate, or if you wish to generate multiple chains from for later MCMC diagnostic tests.
- Start from a point specified by the user with `casal2 -i`

The chain moves in natural space, i.e., no transformations are applied to the estimated parameters. The default proposal distribution is a multivariate  $t$  centred on the current point, with covariance matrix equal to a matrix based on the approximate covariance produced by the minimiser, times some stepsize factor. The following steps define the initial covariance matrix of the proposal distribution:

- The covariance matrix is taken as the inverse of the approximate Hessian from the quasi-Newton minimiser.
- The covariance matrix is modified so as to decrease all correlations greater than `@mcmc.max_correlation` down to `@mcmc.max_correlation`, and similarly to increase all correlations less than `-@mcmc.max_correlation` up to `-@mcmc.max_correlation` (the `@mcmc.max_correlation` parameter defaults to 0.8). This should help to avoid getting ‘stuck’ in a lower-dimensional subspace.
- The covariance matrix is then modified either by,
  - if `@mcmc.adjustment_method=covariance`: that if the variance of the  $i$ th parameter is non-zero and less than `@mcmc.min_difference` times the difference between the parameters’ lower and upper bound, then the variance is changed, without changing the associated correlations, to  $k = \min\_diff(upper\_bound_i - lower\_bound_i)$ . This is done by setting

$$Cov(i, j)' = \sqrt{k} Cov(i, j) / sd(i)$$

for  $i \neq j$ , and  $\text{var}(i)' = k$

- if `@mcmc.adjustment_method=correlation`: that if the variance of the  $i$ th parameter is non-zero and less than `@mcmc.min_difference` times the difference between the parameters' lower and upper bound, then its variance is changed to  $k = \text{min\_diff}(\text{upper\_bound}_i - \text{lower\_bound}_i)$ . This differs from (i) above in that the effect of this option is that it also modifies the resulting correlations between the  $i$ th parameter and all other parameters.

This allows each estimated parameter to move in the MCMC even if its variance is very small according to the inverse Hessian. In both cases, the `@mcmc.min_difference` parameter defaults to 0.0001.

- The `@mcmc.stepsize` (a scalar factor applied to the covariance matrix to improve the acceptance probability) is chosen by the user. The default is  $2.4d^{-0.5}$  where  $d$  is the number of estimated parameters, as recommended by Gelman et al. (Gelman et al., 1995). However, you may find that a smaller value may often be better.

The proposal distribution can also change adaptively during the chain, using two different mechanisms. Both are offered as means of improving the convergence properties of the chain. It is important to note that any adaptive behaviour must finish before the end of the burn-in period, i.e., the proposal distribution must be finalised before the kept portion of the chain starts. The adaptive mechanisms are as follows:

1. You can request that the stepsize change adaptively at one or more sample numbers. At each adaptation, the stepsize is doubled if the acceptance rate since the last adaptation is more than 0.5, or halved if the acceptance rate is less than 0.2. (See Gelman et al. (Gelman et al., 1995) for justification.)
2. You can request that the entire covariance matrix change adaptively at one or more sample numbers. At each adaptation, it is replaced with a matrix based on the sample covariance of an earlier section of the chain. The theory here is that the covariance of a portion of chain could potentially be a better estimate of the covariance of the posterior distribution than the inverse Hessian.

The procedure used to choose the sample of points is as follows. First, all points on the chain so far are taken. All points in an initial user-specified period are discarded. The assumption is that the chain will have started moving during this period - if this is incorrect and the chain has still not moved by the end of this period, it is a fatal error and CASAL2 stops. The remaining set of points must contain at least some user-specified number of transitions - if this is incorrect and the chain has not moved this often, it is again a fatal error. If this test is passed, the set of points is systematically sub-sampled down to 1000 points (it must be at least this long to start with).

The variance-covariance matrix of this sub-sample of chain is calculated. As above, correlations greater than `@mcmc.max_correlation` are reduced to `@mcmc.max_correlation`, correlations less than `@mcmc.max_correlation` are increased to `@mcmc.max_correlation`, and very small non-zero variances are increased (`@mcmc.covariance_adjustment` and `@mcmc.min_difference`). The result is the new variance-covariance matrix of the proposal distribution.

The stepsize parameter is now on a completely different scale, and must be reset. It is set to a user-specified value (which may or may not be the same as the initial stepsize). We recommend that some of the stepsize adaptations are set to occur after this, so that the stepsize can be readjusted to an appropriate value which gives good acceptance probabilities with the new matrix.

All modified versions of the covariance matrix are printed to the standard output, but only the

initial covariance matrix (inverse Hessian) is saved to the objectives file. The number of covariance modifications by each iteration is recorded as a column on the objectives file.

The probability of acceptance for each jump is 0 if it would move out of the bounds, or 1 if it improves the posterior, or (new posterior/old posterior) otherwise. You can specify how often the position of the chain is recorded using the keep parameter. For example, with keep 10, only every 10th sample is recorded.

You have the option to specify that some of the estimated parameters are fixed during the MCMC. If the chain starts at the point estimate or at a random location, these fixed parameters are set to their values at the point estimate.

If you specify the start of the chain using `casal2 -i`, these fixed parameters are set to the values in the file.

The posterior sample can be used for (projections (Section 4.6)) or simulations (Section 6.7) with the values supplied using `casal2 -i file`.

A multivariate t distribution is available as an alternative to the multivariate normal proposal distribution. If you request multivariate t proposals, you may want to change the degrees of freedom from the default of 4. As the degrees of freedom decrease, the t distribution becomes more heavy tailed. This may lead to better convergence properties.

Having produced one or more Markov chains and looked at the diagnostics, reload all the chain output files into CASAL and use them to generate a single posterior sample (using `-C`). At this stage, the first `burn_in` iterations for each chain are discarded (so, with keep 10, `burn_in` 1000, the first 1000 recorded samples are discarded for each chain). Unless a very large value of keep was originally chosen, it will be necessary to further reduce the size of the posterior sample (possibly down to several hundred) such that it can be analysed in a reasonable amount of time. This is done by sub-sampling. You specify the size of the sub-sample to be produced (or else no sub-sampling is done). You have the option to generate a systematic sub-sample (i.e., every `nth` point is kept) or a random sub-sample (the former is recommended except with prior re-weighting, when the latter must be used).

Given a posterior (sub)sample, CASAL can calculate a list of output quantities for each sample point (see Section 7.2). These quantities can be dumped into a file (using `casal -v`) and read into an external software package where the posterior distributions can be plotted and/or summarised.

The posterior sample can also be used for projections (Section 7.3) and stochastic yield calculations (Section 7.5). The advantage of this is that the parameter uncertainty, as expressed in your posterior distribution, can be included into the risk and yield estimates.

It is possible to investigate the results that would have been obtained if a different prior had been specified. This is called prior re-weighting and is done by calculating the ratio of the new prior to the original prior for each point in the posterior sample, then using these ratios as probability weights when generating a random (not systematic) sub-sample with `casal -C`. Prior re-weighting is applicable only if the new prior is zero in every part of the parameter space for which the original prior was zero. Also, it is likely to be numerically unstable unless the new prior is very small in every part of the parameter space for which the original prior was very small.

## 5.7. Priors

In a Bayesian analysis, you need to give a prior for every parameter that is being estimated. There are no default priors.

Note that when some of these priors are parameterised in terms of mean, c.v., and standard deviation,

these refer to the parameters of the distribution before bounds are applied. The moments of the prior after the bounds are applied may differ.

CASAL2 has the following priors (expressed in terms of their contribution to the objective function):

1. Uniform

$$-\log(\pi(p)) = 0 \quad (5.2)$$

2. Uniform-log (i.e.,  $\log(p) \sim \text{uniform}$ )

$$-\log(\pi(p)) = \log(p) \quad (5.3)$$

3. Normal with mean  $\mu$  and c.v.  $c$

$$-\log(\pi(p)) = 0.5 \left( \frac{p - \mu}{c\mu} \right)^2 \quad (5.4)$$

4. Normal with mean  $\mu$  and standard deviation  $\sigma$

$$-\log(\pi(p)) = 0.5 \left( \frac{p - \mu}{\sigma} \right)^2 \quad (5.5)$$

5. Lognormal with mean  $\mu$  and c.v.  $c$

$$-\log(\pi(p)) = \log(p) + 0.5 \left( \frac{\log(p/\mu)}{s} + \frac{s}{2} \right)^2 \quad (5.6)$$

where  $s$  is the standard deviation of  $\log(p)$  and  $s = \sqrt{\log(1 + c^2)}$ .

6. Normal-log with  $\log(p)$  having mean  $m$  and standard deviation  $s$ ,

6. Beta with mean  $\mu$  and standard deviation  $\sigma$ , and range parameters  $A$  and  $B$

$$-\log(\pi(p)) = (1 - m) \log(p - A) + (1 - n) \log(B - p) \quad (5.7)$$

where  $v = \frac{\mu - A}{B - A}$ , and  $\tau = \frac{(\mu - A)(B - \mu)}{\sigma^2} - 1$  and then  $\mu = \tau v$  and  $n = \tau(1 - v)$ . Note that the beta prior is undefined when  $\tau \leq 0$ .

Vectors of parameters can be independently (but not necessarily identically) distributed according to any of the above forms, in which case the joint negative-log-prior for the vector is the sum of the negative-log-priors of the components. Values of each parameter need to be specified for each element of the vector.

In addition, for a vector  $p$  of  $n$  identically distributed parameters (for example, YCS) the following priors are allowed:

1. Multivariate normal from a stationary AR(1) process with parameters
  - .
  - .
  - .
2. Multivariate normal-log, where  $\log(p)$  forms a stationary AR(1) process as per 1. above, with parameters
  - .
  - .
  - .
3. Multivariate normal-log with mean 1, where  $E(\pi)=1$  and  $\log(p)$  forms a stationary AR(1) process as for the multivariate normal above, with parameters
  - .
  - .
  - .

## 5.8. Penalties

Penalties are associated with processes and can be used to encourage or discourage parameter values or model outputs that are unlikely to be sensible, by adding a penalty to the objective function. For example, parameter estimates that do not allow a known mortality event to remove enough individuals from the population can be discouraged with an event mortality penalty. CASAL2 requires penalty functions for processes that move or shift a *number* of individuals between categories or from the partition.

For most penalties, you need to specify a multiplier, and the objective function is increased by this multiplier times the penalty value as described below. In some cases you will need to make the multiplier quite large to prohibit some model behaviour.

Currently, the penalties for the processes `@process[label].type=event_mortality`, `@process[label].type=tag_by_length` and `@process[label].type=category_transition` are the only penalties implemented.

For these processes, two types of penalty can be defined, natural scale (the default) and log scale. Both of these types add a penalty value of the squared difference between the observed value (i.e., the actual number of individuals to be removed in an event mortality process or the actual number of individuals to shift in a category transition process), and the number that were moved (if less than or equal), times the penalty multiplier.

The natural scale penalty just uses the squared difference on a natural scale, while the log scale penalty uses the squared difference of the logged values.

## 5.9. Additional Priors

Additional priors are the inverse

## 5.10. Estimate Transformations

CASAL2 has the untested functionality of transforming an estimated parameter in a new space. This may be done to remove correlation for other convergence or optimisation purposes. This functionality transforms the estimate and the bounds to the transformed space along with the prior. To account for the change variable a Jacobian is added to the objective function. For more information users are asked to read the STAN manual **REFERENCE**. The user must supply the type,

bounds for the transformed variable can be supplied by the user, but if not CASAL2 will work them out. NOTE must be used with caution. May be buggy!!!

**5.10.1. log**

**5.10.2. Inverse**

**5.10.3. Log odds**

**5.10.4. Simplex**

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## 6. The observation section

### 6.1. Observations and likelihoods

Observations are typically supplied as observations at an instance in time, over some spatially aggregated area. Time series of observations can be supplied as separate observations for each year or point in time.

CASAL2 allows the following types of observations;

- Observations of proportions by age class within categories
- Observations of proportions between categories within age classes
- Relative and absolute abundance/biomass observations

The definitions for each type of observation are described below, including how the observed values should be supplied, how CASAL2 calculates the expected values, and the likelihoods that are available for each type of observation.

CASAL2 evaluates the observations at the end of a time-step (i.e., after all of the processes for that time-step have been applied). However, the observation can be applied to the abundance at the start of a time-step or part-way through a time-step by the use of the `proportion_time_step` subcommand.

By default (i.e., if `proportion_method = mean`), the partition at some point  $p$  during the time-step is then evaluated as the weighted sum between the start and end of the time-step, i.e, for any element  $i$  in the partition,  $n_i = (1 - p)n_i^{start} + pn_i^{end}$ . Note that it may not be sensible to use a value other than one, depending on the processes that happen during the time-step (for example, if the time-step contains an ageing process).

If the `proportion_method = difference`, then the observation is of the *difference* between the population state at the start of the time-step and the end. This can be used to generate expected values for observations of, for example removals due to a mortality event, by only having a single process in the time-step. In this case, the `proportion_time_step` is simply a multiplier of the population state.

### 6.2. Proportions-at-age observations

Proportions-at-age observations are observations of either the relative number of individuals at age or relative biomass at age, via some selectivity.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity), for categories aggregated over a set of spatial cells. Note that the categories defined in the observations must have an associated selectivity, defined by `selectivities`.

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive), but the upper end of the age range can optionally be a plus group — which must be either the same or less than the plus group defined for the partition.

Proportions-at-age observations can be supplied as;

1. a set of proportions for a single category,
2. a set of proportions for multiple categories, or
3. a set of proportions across aggregated categories.

For example, for a model with the two categories *male* and *female*, we might supply either (i) a set of proportions for a single category (i.e., males) within each age class; (ii) a set of proportions describing the proportions of individuals within each age class across multiple categories (i.e., males and females) simultaneously, or (iii) a set of proportions for the total number of individuals over the aggregated categories (i.e., males + females) combined, within each age class.

The way the categories of the observation are defined specifies which of these alternatives are used. It is also possible to have an observation with multiple and aggregated categories simultaneously.

### Proportions-at-age for a single category

This form of defining the observation is the simplest, and is used to model a set of proportions of a single category by age class. For example, to specify that the observations are of the proportions of male within each age class, then the subcommand `categories` for the `@observation[label].type=proportion.by_age` command is,

```
categories male
```

CASAL2 then expects that there will be a single vector of proportions supplied, with one proportion for each age class within the defined age range, and that these proportions sum to one.

For example, if the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the ages 3, 4, 5, 6, 7, 8, 9, and 10). The expected values will be the expected proportions of males within each of these age classes (after ignoring any males aged less than 3 or older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 8 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

The observations must be also supplied using all or some of the values of defined by some *categorical* layer. CASAL2 calculates the expected values by summing over the defined ages (via the age range and selectivity) and categories for those spatial cells where the categorical layer has the same value as defined for each vector of observations.

For example, in a  $2 \times 2$  spatial model a categorical layer (e.g., with label *Area*) may define that cells (1, 1) and (1, 2) have value *A* and cells (2, 1) and (2, 2) have value *B*, i.e.,

```
@layer Area
type categorical
data A A
data B B
```

The observations for those spatial cells where the categorical layer has value *A* would be,

```
@observation MyProportions
type proportions_at_age
layer Area
...
categories male
min_age 1
max_age 5
obs A 0.01 0.09 0.20 0.30 0.40
...
```



Or, for both *A* and *B* as,

```
@observation MyProportions
type proportions_at_age
layer Area
...
categories male
min_age 1
max_age 5
obs A 0.01 0.09 0.20 0.30 0.40
obs B 0.02 0.06 0.12 0.25 0.55
...
```

Note that to have an observation for each individual spatial cell in a model, then define a categorical layer that has a single, unique value for each spatial cell for use in the observation.

### Proportions-at-age for multiple categories

This form of the observation extends the idea above for multiple categories. It is used to model a set of proportions over several categories by age class. For example, to specify that the observations are of the proportions of male or females within each age class, then the subcommand `categories` for the `@observation[label].type=proportion_by_age` command is,

```
categories male female
```

CASAL2 then expects that there will be a single vector of proportions supplied, with one proportion for each category and age class combination, and that these proportions sum to one.

For example, if there were two categories and the age range was 3 to 10, then 16 proportions should be supplied (one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10, for each category male and female). The expected values will be the expected proportions of males and within each of these age classes (after ignoring those aged less than 3 or older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 16 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example, using the earlier spatial model with a categorical layer that has label *Area*, the observations for those spatial cells where the categorical layer has value *A* would be,

```
@observation MyProportions
type proportions_at_age
layer Area
...
categories male female
min_age 1
max_age 5
obs A 0.01 0.05 0.10 0.20 0.20 0.01 0.05 0.15 0.20 0.03
obs B 0.02 0.06 0.10 0.21 0.18 0.02 0.05 0.15 0.20 0.01
...
```

### Proportions-at-age across aggregated categories

This form of the observation extends the idea above, but allows categories to be aggregated before the proportions are calculated. It is used to model a set of proportions from several categories that have been combined by age class. To indicate that two (or more) categories are to be aggregated,

separate them with a '+' symbol. For example, to specify that the observations are of the proportions of male and females combined within each age class, then the subcommand `categories` for the `@observation[label].type=proportion.by_age` command is,

```
categories male + female
```

CASAL2 then expects that there will be a single vector of proportions supplied, with one proportion for each age class, and that these proportions sum to one.

For example, if there were two categories and the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the ages 3, 4, 5, 6, 7, 8, 9, and 10, for the sum of males and females within each age class). The expected values will be the expected proportions of males + females within each of these age classes (after ignoring those aged less than 3 or older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 16 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example, using the earlier spatial model with a categorical layer that has label `Area`, the observations for those spatial cells where the categorical layer has value `A` would be,

```
@observation MyProportions
type proportions_at_age
layer Area
...
categories male + female
min_age 1
max_age 5
obs A 0.02 0.13 0.25 0.30 0.30
obs B 0.02 0.06 0.18 0.35 0.39
...
```

The later form can then be extended to include multiple categories, or multiple aggregated categories. For example, to describe proportions for the three groups: immature males, mature males, and all females (immature and mature females added together) for ages 1–4, a total of 12 proportions are required

```
@observation MyProportions
type proportions_at_age
layer Area
...
categories male_immature male_mature female_immature + female_mature
min_age 1
max_age 4
obs A 0.05 0.15 0.15 0.05 0.02 0.03 0.08 0.04 0.05 0.15 0.15 0.08
...
```

### 6.2.1. Likelihoods for proportions-at-age observations

CASAL2 implements two likelihoods for proportions-at-age observations, the multinomial likelihood and the lognormal likelihood.

#### The multinomial likelihood

For the observed proportions at age  $O_i$  for age classes  $i$ , with sample size  $N$ , and the expected proportions at the same age classes  $E_i$ , the negative log-likelihood is defined as;

$$-\log(L) = -\log(N!) + \sum_i \log((NO_i)!) - NO_i \log(Z(E_i, \delta)) \quad (6.1)$$

where  $\sum_i O_i = 1$  and  $\sum_i E_i = 1$ .  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.2)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

### The lognormal likelihood

For the observed proportions at age  $O_i$  for age classes  $i$ , with c.v.  $c_i$ , and the expected proportions at the same age classes  $E_i$ , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left( \log(\sigma_i) + 0.5 \left( \frac{\log(O_i / Z(E_i, \delta))}{\sigma_i} + 0.5 \sigma_i \right)^2 \right) \quad (6.3)$$

where

$$\sigma_i = \sqrt{\log(1 + c_i^2)} \quad (6.4)$$

and the  $c_i$ 's are the c.v.s for each age class  $i$ , and  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.5)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

## 6.3. Proportions-by-category observations

Proportions-by-category observations are observations of either the relative number of individuals between categories within age classes, or relative biomass between categories within age classes.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity), for categories aggregated over a set of spatial cells.

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive), but the upper end of the age range can optionally be a plus group — which may or may not be the same as the plus group defined for the partition.

Proportions-by-category observations can be supplied for any set of categories as a proportion of themselves and any set of additional categories. For example, for a model with the two categories *male* and *female*, we might supply observations of the proportions of males in the population at each age class. The subcommand `categories` defines the categories for the numerator in the calculation of the proportion, and the subcommand `categories2` supplies the additional categories to be used in the denominator of the calculation. In addition, each category must have an associated selectivity, defined by `selectivities` for the numerator categories and `selectivities2` for the additional categories used in the denominator, e.g.,

```
categories male
```

```
categories2 female
selectivities male-selectivity
selectivities2 female-selectivity
```

defines that the proportion of males in each age class as a proportion of males + females. CASAL2 then expects that there will be a vector of proportions supplied, with one proportion for each age class within the defined age range, i.e., if the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the ages 3, 4, 5, 6, 7, 8, 9, and 10). The expected values will be the expected proportions of male to male + female within each of these age classes, after applying the selectivities at the year and time-step specified.

The observations must be supplied using all or some of the values defined by a categorical layer. CASAL2 calculates the expected values by summing over the ages (via the age range and selectivity) and categories for those spatial cells where the categorical layer has the same value as defined for each vector of observations.

For example, in a  $2 \times 2$  spatial model a categorical layer (e.g., with label Area) may define that cells (1,1) and (1,2) have value A and cells (2,1) and (2,2) have value B, i.e.,

```
@layer Area
type categorical
data A A
data B B
```

Here we supply observations for those spatial cells where the categorical layer has value A as,

```
@observation MyProportions
type proportions_by_category
layer Area
...
categories male
categories2 female
min_age 1
max_age 5
obs A 0.01 0.05 0.10 0.20 0.20
...
```

Or, for both A and B as,

```
@observation MyProportions
type proportions_by_category
layer Area
...
categories male
categories2 female
min_age 1
max_age 5
obs A 0.01 0.05 0.10 0.20 0.20
obs B 0.02 0.06 0.10 0.21 0.18
...
```

To supply an observation for individual spatial cells, then you will need to define a categorical layer with a single, unique value for each spatial cell.

### 6.3.1. Likelihoods for proportions-by-category observations

CASAL2 implements two likelihoods for proportions-by-category observations, the binomial likelihood, and the normal approximation to the binomial (binomial-approx).

### The binomial likelihood

For observed proportions  $O_i$  for age class  $i$ , where  $E_i$  are the expected proportions for age class  $i$ , and  $N_i$  is the effective sample size for age class  $i$ , then the negative log-likelihood is defined as;

$$-\log(L) = -\sum_i [\log(N_i!) - \log((N_i(1 - O_i))!) - \log((N_i O_i)!) + N_i O_i \log(Z(E_i, \delta)) + N_i(1 - O_i) \log(Z(1 - E_i, \delta))] \quad (6.6)$$

where  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.7)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

### The normal approximation to the binomial likelihood

For observed proportions  $O_i$  for age class  $i$ , where  $E_i$  are the expected proportions for age class  $i$ , and  $N_i$  is the effective sample size for age class  $i$ , then the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \log \left( \sqrt{Z(E_i, \delta) Z(1 - E_i, \delta) / N_i} \right) + \frac{1}{2} \left( \frac{O_i - E_i}{\sqrt{Z(E_i, \delta) Z(1 - E_i, \delta) / N_i}} \right)^2 \quad (6.8)$$

where  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.9)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

## 6.4. Abundance or biomass observations

Abundance (or biomass) observations are observations of either a relative or absolute number (or biomass) of individuals from a set of categories after applying a selectivity. The observations classes are the same, except that a biomass observation will use the biomass as the observed (and expected) value (calculated from mean weight of individuals within each age and category) while an abundance observation is just the number of individuals.

Each observation is for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity), for categories aggregated over a set of spatial cells. Further, you need to provide the label of the catchability coefficient  $q$ , which can either be estimated or fixed. For absolute abundance or absolute biomass observations, define a catchability where  $q = 1$ .

The observations can be supplied for any set of categories. For example, for a model with the two categories *male* and *female*, we might supply an observation of the total abundance/biomass (male + female) or just male abundance/biomass. The subcommand `categories` defines the categories used to aggregate the abundance/biomass. In addition, each category must have an associated selectivity, defined by `selectivities`. For example,

```
categories male
selectivities male-selectivity
```

defines an observation for males after applying the selectivity male-selectivity. CASAL2 then expects that there will be a single observation supplied. The expected values for the observations will be the expected abundance (or biomass) of males, after applying the selectivities, at the year and time-step specified.

The observations must be supplied using all or some of the values of defined by a categorical layer. CASAL2 calculates the expected values by summing over the defined ages (via the age range and selectivity) and categories for those spatial cells where the categorical layer has the same value as defined for each vector of observations.

For example, in a  $2 \times 2$  spatial model a categorical layer (e.g., with label Area) may define that cells (1,1) and (1,2) have value *A* and cells (2,1) and (2,2) have value *B*, i.e.,

```
@layer Area
type categorical
data A A
data B B
```

Here we supply abundance observations for those spatial cells where the categorical layer has value *A* as,

```
@observation MyAbundance
type abundance
layer Area
...
categories male
obs A 1000
...
```

Or, for both *A* and *B* as,

```
@observation MyAbundance
type abundance
layer Area
...
categories male
obs A 1000
obs B 1200
...
```

To supply an observation for individual spatial cells, then you will need to define a categorical layer with a single, unique value for each spatial cell.

Note that, to define a biomass observation instead of an abundance observation, use

```
@observation MyBiomass
type biomass
...
```

### 6.4.1. Likelihoods for abundance observations

#### The lognormal likelihood

For observations  $O_i$ , c.v.  $c_i$ , and expected values  $qE_i$ , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left( \log(\sigma_i) + 0.5 \left( \frac{\log(O_i/qZ(E_i, \delta))}{\sigma_i} + 0.5\sigma_i \right)^2 \right) \quad (6.10)$$

where

$$\sigma_i = \sqrt{\log(1 + c_i^2)} \quad (6.11)$$

and  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta/\delta), & \text{otherwise} \end{cases} \quad (6.12)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

#### The normal likelihood

For observations  $O_i$ , c.v.  $c_i$ , and expected values  $qE_i$ , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left( \log(c_i E_i) + 0.5 \left( \frac{O_i - E_i}{Z(c_i E_i, \delta)} \right)^2 \right) \quad (6.13)$$

and  $Z(\theta, \delta)$  is a robustifying function to prevent division by zero errors, with parameter  $\delta > 0$ .  $Z(\theta, \delta)$  is defined as,

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta/\delta), & \text{otherwise} \end{cases} \quad (6.14)$$

The default value of  $\delta$  is  $1 \times 10^{-11}$ .

### 6.5. Process error

Additional ‘process error’ can be defined for each set of observations. Additional process error has the effect of increasing the observation error in the data, and hence of decreasing the relative weight given to the data in the fitting process.

For observations where the likelihood is parameterised by the c.v., you can specify the process error for a given set of observations as a c.v., in which case all the c.v.s  $c_i$  are changed to

$$c'_i = \sqrt{c_i^2 + c_{process\_error}^2} \quad (6.15)$$

Note that  $c_{process\_error} \geq 0$ , and that  $c_{process\_error} = 0$  is equivalent to no process error.

Similarly, if the likelihood is parameterised by the effective sample size  $N$ ,

$$N'_i = \frac{1}{1/N_i + 1/N_{process\_error}} \quad (6.16)$$

Note that this requires that  $N_{process\_error} > 0$ , but we allow the special case of  $N_{process\_error} = 0$ , and define  $N_{process\_error} = 0$  as no process error (i.e., defined to be equivalent to  $N_{process\_error} = \infty$ ).

For both the c.v. and  $N$  process errors, the process error has more effect on small errors than on large ones. Be clear that a large value for the  $N$  process error means a small process error.

## 6.6. Ageing error

CASAL2 can apply ageing error age frequency observations. Ageing error is applied to the expected values for proportions-at-age observations. The ageing error is applied as a misclassification matrix, which has the effect of 'smearing' the age frequencies. These are used in calculating the fits to the observed values, and hence the contribution to the total objective function.

Ageing error is optional, and if it is used, it may be omitted for any individual time series. Different ageing error models may be applied for different observation commands. See Section 7.11 for reporting the misclassification matrix.

The ageing error models implemented are,

1. None: The default model is to apply no ageing error.
2. Off by one: Proportion  $p_1$  of individuals of each age  $a$  are misclassified as age  $a - 1$  and proportion  $p_2$  are misclassified as age  $a + 1$ . Individuals of age  $a < k$  are not misclassified. If there is no plus group in the population model, then proportion  $p_2$  of the oldest age class will 'fall off the edge' and disappear.
3. Normal: Individuals of age  $a$  are classified as ages which are normally distributed with mean  $a$  and constant c.v.  $c$ . As above, if there is no plus group in the population model, some individuals of the older age classes may disappear. If  $c$  is high enough, some of the younger age classes may 'fall off the other edge'. Individuals of age  $a < k$  are not misclassified.

Note that the expected values (fits) reported by CASAL2 for observations with ageing error will have had the ageing error applied.

## 6.7. Simulating observations

CASAL2 can generate simulated observations for a given model with given parameter values (using `spm -s`). Simulated observations are randomly distributed values, generated according to the error assumptions defined for each observation, around fits calculated from one or more sets of the 'true' parameter values. Simulating from a set of parameters can be used to generate observations from an operating model or as a form of parametric bootstrap.

The procedure CASAL2 uses for simulating observations is to first run using the 'true' parameter values and generate the expected values. Then, if a set of observations uses ageing error, ageing error is applied. Finally a random value for each observed value is generated based on (i) the expected values, (ii) the type of likelihood specified, and (iii) the variability parameters (e.g., `error_value` and `process_error`).

Methods for generating the random error, and hence simulated values, depend on the specific likelihood type of each observation.

1. Normal likelihood parameterised by c.v.: Let  $E_i$  be the fitted value for observation  $i$ , and  $c_i$  be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value  $S_i$  is generated as an independent normal deviate with mean  $E_i$  and standard deviation  $E_i c_i$ .



2. Log-normal likelihood: Let  $E_i$  be the fitted value for observation  $i$  and  $c_i$  be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value  $S_i$  is generated as an independent lognormal deviate with mean and standard deviation (on the natural scale, not the log-scale) of  $E_i$  and  $E_i c_i$  respectively. The robustification parameter  $\delta$  is ignored.
3. Multinomial likelihood: Let  $E_i$  be the fitted value for observation  $i$ , for  $i$  between 1 and  $n$ , and let  $N$  be the sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter  $\delta$  is ignored. Then,
  - a) A sample of  $N$  values from 1 to  $n$  is generated using the multinomial distribution, using sample probabilities proportional to the values of  $E_i$ .
  - b) Each simulated observation value  $S_i$  is calculated as the proportion of the  $N$  sampled values equalling  $i$
  - c) The simulated observation values  $S_i$  are then rescaled so that their sum is equal to 1
4. Binomial and the normal approximation to the binomial likelihoods: Let  $E_i$  be the fitted value for observation  $i$ , for  $i$  between 1 and  $n$ , and  $N_i$  the corresponding equivalent sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter  $\delta$  is ignored. Then,
  - a) A sample of  $N_i$  independent binary variates is generated, equalling 1 with probability  $E_i$
  - b) The simulated observation value  $S_i$  is calculated as the sum of these binary variates divided by  $N_i$

Note that CASAL2 will report simulated observations using the usual observation report (`@report[label].type=observation`). The report `@report[label].type=simulated_observation` will generate simulated observations in a form suitable for use as input within a CASAL2 input configuration file. See Section 7 for more detail.

## 6.8. Pseudo-observations

CASAL2 can generate expected values for observations without them contributing to the total objective function. These are called pseudo-observations, and can be used to either generate the expected values from CASAL2 for reporting or diagnostic purposes. To define an observation as a pseudo-observation, use the command `@observation[label].likelihood=none`. Any observation type can be used as a pseudo-observation. CASAL2 can also generate simulated observations from pseudo-observations. Note that;

- Output will only be generated if a report command `@report[label].type=observation` is specified.
- The observed values should be supplied (even if they are ‘dummy’ observation). These will be processed by CASAL2 as if they were actual observation values, and must conform to the validations carried out for the other types of likelihood.
- The subcommands `likelihood`, `obs`, `error_value` and `process_error` have no effect when generating the expected values for the pseudo-observation.
- When simulating observations, CASAL2 needs the subcommand `simulation_likelihood` to tell it what sort of likelihood to use. In this case, the `obs`, `error_value` and `process_error` are used to determine the appropriate terms to use for the likelihood when simulating.



---

## 7. The report section

The report section specifies the printouts and other outputs from the model. CASAL2 does not, in general, produce any output unless requested by a valid `@report` block.

Reports from CASAL2 can be defined to print partition and states objects at a particular point in time, observation summaries, estimated parameters and objective function values. See below for a more extensive list, and an example of an observation report.

```
@report observation_age ## label of report
type observation ## Type of report
observation age_1990 ## label corresponding to an @observation report, shown below

@observation age_1990
type proportion_at_age
year 1990
plus_group
etc ...
```

Reports from CASAL2 all conform to a standard style (with one exception — the `output_parameters` report, see below). The standard style is that reports are prefixed with an asterisk followed by a user-defined label and type of report in brackets (e.g., `*label (type)`), with the report ending with the line `*end`. For example,

```
*My_report (type)
...
*end
```

This syntax should make it easier for external packages to be configured to read CASAL2 output. The `extract` functions in the **R** CASAL2 package uses this information to identify and read CASAL2 output.

Note that the `output_parameters` report does not print either a header or `*end` at the end of the report. This is as the `output_parameters` report is designed to provide a single line (or multi-line for more than one set) vector of the estimated parameter values, suitable for reading by CASAL2 (with the command `casal2 -i`). This is a specialised report for `casal2 -o` command. For estimate values in standard output users are recommended to use `type=estimate_value`.

Note that reports can be defined that may not be generated. For example printing the partition for a year and/or time-step that does not exist or reporting the covariance matrix when not estimating. Such reports are ignored by CASAL2 and the program will not generate any output for these reports — although they must still conform to CASAL2s syntax requirements.

Not all reports will be generated in all run modes. Some reports are only available in some run modes. For example, when simulating, only simulation reports will be output.

### 7.1. Print the partition

Print the partition for a given year or given years and time-step. This prints out, the numbers of individuals in each age class and category in the partition for each year. Note that this report is evaluated at the end of the time-step in the given year(s).

### 7.2. Print the partition at the end of an initialisation

Print the partition following an initialisation phase. This prints out, the numbers of individuals in each age class and category in the partition following an initialisation phase.

### 7.3. Print a process summary

Print a summary of a process. Depending on the process, different summaries are produced. These typically detail the type of process, its parameters and other options, and any associated details.

### 7.4. Print derived quantities

Print out the description of the derived quantity, and the values of the derived quantity as recorded in the model state, for each year of the model. and for all years in the initialisation phases.

### 7.5. Print the estimated parameters

Print a summary of the estimated parameters, including the parameter name, lower and upper bounds, the label of the prior, and its value.

### 7.6. Print the estimated parameters in a vector format

Print the estimated parameter values out as a vector. The `estimate_values` report prints the name of the parameter, followed by the value of that run.

### 7.7. Print the objective function

Print the total objective function value, and the value of all observations, the values of all priors, and the value of any penalties that have been incurred in the model. Note that if an individual model run does not incur a penalty, then the penalty will not be reported.

### 7.8. Print the covariance matrix

Print the Hessian and covariance matrices if estimating and if the covariance has been requested by `@minimiser[label].covariance=true`.

### 7.9. Print observations, fits, and residuals

Prints out for each category or combination of categories, expected values as calculated by the model, residuals (observed — expected), the error value, process error, and the total error (i.e., the error value as modified by any additional process error), and the contribution to the total objective function of that individual point in the observation.

Note that constants in likelihoods are often ignored in the objective function score of individual points. Hence, the total score from an observation equals the contribution of the objective function scores from each individual point plus a constant term (if applicable). In likelihoods without a constant term, then the total score from an observation will equal the contribution of the objective function scores from each individual point.

If simulating, then the contribution to the objective function of each observation is reported as zero.

### 7.10. Print simulated observations

Prints out a complete observation definition (i.e., in the form defined by `@report[label].type=observation`), but with observed values replaced by randomly generated simulated values. The output is in a form suitable for use within a CASAL2 input configuration file, reproducing the command and subcommands from the input configuration file.

**7.11. Print the ageing error misclassification matrix**

Prints out the ageing error misclassification matrix.

**7.12. Print selectivities**

Prints the values of a selectivity for each age in the partition, for a given year and at then end of a given time-step.

**7.13. Print the random number seed**

Prints the random number seed used by CASAL2 to generate the random number sequence. Future runs made with the same random number seed and the same model will produce identical outputs.

**7.14. Print the results of an MCMC**

Print the MCMC samples, objective function values, and proposal covariance matrix following an MCMC.

**7.15. Print the MCMC samples as they are calculated**

Print the MCMC samples for each new *i*th sample as they are calculated while doing an MCMC. The output file will be updated with each new sample as it is calculated by CASAL2.

**7.16. Print the MCMC objective function values as they are calculated**

Print the MCMC objective function values (along with the proposal covariance matrix) for each new *i*th sample as they are calculated while doing an MCMC. The output file will be updated with each new set of objective function values as it is calculated by CASAL2.

**7.17. Tabular reporting**

An alternative reporting framework to the standard output is the tabular reporting. Tabular reporting is used with multiline *-i* input files (like the MCMC reports). Tabular reports will print out a row that will correspond with each row of the *-i* input files. Tabular reporting is invoked at the command line using the following command `casal2 -r --tabular -i file_name`. Currently derived quantities and estimate values are the only report types that are within this framework. For each input file the output will begin with the names of each column followed by a multiline report ending with the `*end` syntax. These tables can be easily read into **R** using the `CASAL2` package and for the example of MCMC multi-line files posteriors of derived quantities can be plotted.



---

## 8. Population command and subcommand syntax

For ease of reading CASAL2 files in text editors, there exists a syntax highlighter `CASAL2.syn`

### 8.1. Model structure

`@model label` Define an object type Model

`age_plus` Define the oldest age as a plus group

Type: boolean

Default: false

Value: true, false

`final_year` Define the final year of the model, excluding years in the projection period

Type: non-negative integer

Default: No Default

Value: Defines the last year of the model, i.e., the model is run from `start_year` to `final_year`

`initialisation_phases` Define the labels of the phases of the initialisation

Type: string vector

Default: true

Value: A list of valid labels defined by `@initialisation_phase`

`label`

Type: string

Default: No Default

`length_bins`

Type: constant vector

Default: true

`max_age` Maximum age of individuals in the population

Type: non-negative integer

Default: 0

Value:  $0 \leq \text{age}_{\min} \leq \text{age}_{\max}$

`min_age` Minimum age of individuals in the population

Type: non-negative integer

Default: 0

Value:  $0 \leq \text{age}_{\min} \leq \text{age}_{\max}$

`projection_final_year` Define the final year of the model in projection mode

Type: non-negative integer

Default: 0

Value: Defines the last year of the projection period, i.e., the projection period runs from `final_year+1` to `projection_final_year`. For the default, 0, no projections are run.

`start_year`      Define the first year of the model, immediately following initialisation

Type: non-negative integer

Default: No Default

Value: Defines the first year of the model,  $\geq 1$ , e.g. 1990

`time_steps`      Define the labels of the time steps, in the order that they are applied, to form the annual cycle

Type: string vector

Default: No Default

Value: A list of valid labels defined by `@time_step`

`type`      Type of model (the partition structure). Either age, length or hybrid

Type: string

Default: age

## 8.2. Initialisation

**`@initialisation_phase label`**      Define an object type Initialisation.Phase

`label`      Label

Type: string

Default: No Default

`type`      Type

Type: string

Default: iterative

### 8.2.1. `@initialisation_phase[label].type=cinitial`

`categories`      List of categories to use

Type: string vector

Default: No Default

### 8.2.2. `@initialisation_phase[label].type=derived`

`casal.initialisation.switch`      Reset the partition after running an extra annual cycle to take on equilibrium SSB's. Warning should only be set to true if comparing with previous CASAL models

Type: boolean

Default: false

`exclude_processes`      The processes to exclude from all time steps

Type: string vector

Default: true



`insert_processes`      The processes to insert in to target time steps  
Type: string vector  
Default: true

### 8.2.3. `@initialisation_phase[label].type=iterative`

`convergence_years`      The years to test for convergence  
Type: non-negative integer vector  
Default: true

`exclude_processes`      The processes to exclude from all time steps  
Type: string vector  
Default: true

`insert_processes`      The processes to insert in to target time steps  
Type: string vector  
Default: true

`lambda`      Lambda  
Type: constant  
Default: Double(0.0)

`years`      The number of iterations to execute this phase for  
Type: non-negative integer  
Default: No Default

### 8.2.4. `@initialisation_phase[label].type=state_category_by_age`

`categories`      List of categories to use  
Type: string vector  
Default: No Default

`max_age`      Maximum age to use for this process  
Type: non-negative integer  
Default: No Default

`min_age`      Minimum age to use for this process  
Type: non-negative integer  
Default: No Default

### 8.3. Categories

**@categories** *label* Define an object type Categories

*age\_lengths* The labels of *age\_length* objects that are assigned to categories

Type: string vector

Default: true

*format* The format that the category names should adhere too

Type: string

Default: No Default

*names* The names of the categories to be used in the model

Type: string vector

Default: No Default

*years* The years that individual categories will be active for. This overrides the model values

Type: string vector

Default: true

### 8.4. Time-steps

**@time\_step** *label* Define an object type Time\_Step

*label* Label

Type: string

Default: No Default

*processes* Processes

Type: string vector

Default: No Default

*type*

Type: string

Default: No Default

### 8.5. Processes

**@process** *label* Define an object type Process

*print\_report* Generate parameter report

Type: boolean

Default: false

*label* Label

Type: string  
Default: No Default

type      Type  
Type: string  
Default: ""

### 8.5.1. @process[label].type=ageing

categories      Categories  
Type: string vector  
Default: No Default

print\_report      Generate parameter report  
Type: boolean  
Default: false

### 8.5.2. @process[label].type=growth

print\_report      Generate parameter report  
Type: boolean  
Default: false

### 8.5.3. @process[label].type=maturation

print\_report      Generate parameter report  
Type: boolean  
Default: false

from      List of categories to mature from  
Type: string vector  
Default: No Default

rates      The rates to mature for each year  
Type: constant vector  
Default: No Default

selectivities      List of selectivities to use for maturation  
Type: string vector  
Default: No Default

to      List of categories to mature too

Type: string vector  
Default: No Default

years      The years to be associated with rates  
Type: non-negative integer vector  
Default: No Default

#### **8.5.4. @process[label].type=mortality\_constant\_rate**

categories      List of categories  
Type: string vector  
Default: No Default

print\_report      Generate parameter report  
Type: boolean  
Default: false

m      Mortality rates  
Type: constant vector  
Default: No Default

time\_step\_ratio      Time step ratios for M  
Type: constant vector  
Default: true

selectivities      Selectivities  
Type: string vector  
Default: No Default

#### **8.5.5. @process[label].type=mortality\_event**

catches      Catches  
Type: constant vector  
Default: No Default

categories      Categories  
Type: string vector  
Default: No Default

print\_report      Generate parameter report  
Type: boolean  
Default: false

penalty      Penalty label

Type: string  
Default: ""

selectivities      List of selectivities  
Type: string vector  
Default: No Default

u\_max      U Max  
Type: constant  
Default: 0.99

years      Years  
Type: non-negative integer vector  
Default: No Default

### 8.5.6. @process[label].type=mortality\_event\_biomass

catches      Catches for each year  
Type: constant vector  
Default: No Default

categories      Category labels  
Type: string vector  
Default: No Default

print\_report      Generate parameter report  
Type: boolean  
Default: false

penalty      Penalty label  
Type: string  
Default: ""

selectivities      Selectivity labels  
Type: string vector  
Default: No Default

u\_max      U Max  
Type: constant  
Default: 0.99

units      Unit of weight that the Catches table are expressed in  
Type: string  
Default: No Default

years      Years to apply mortality  
Type: non-negative integer vector  
Default: No Default

### 8.5.7. `@process[label].type=mortality holling rate`

a      parameter a  
Type: constant  
Default: No Default  
Lower Bound: 0.0 (inclusive)

b      parameter b  
Type: constant  
Default: No Default  
Lower Bound: 0.0 (inclusive)

print\_report      Generate parameter report  
Type: boolean  
Default: false

penalty      Label of penalty to be applied  
Type: string  
Default: ""

predator\_categories      Predator Categories labels  
Type: string vector  
Default: No Default

predator\_selectivities      Selectivities for predator categories  
Type: string vector  
Default: No Default

prey\_categories      Prey Categories labels  
Type: string vector  
Default: No Default

prey\_selectivities      Selectivities for prey categories  
Type: string vector  
Default: No Default

u\_max      Umax  
Type: constant  
Default: No Default  
Lower Bound: 0.0 (inclusive)  
Upper Bound: 1.0 (inclusive)

x      parameter x  
Type: constant  
Default: No Default  
Lower Bound: 0.0 (inclusive)

years      Year to execute in  
Type: non-negative integer vector  
Default: No Default

### 8.5.8. `@process[label].type=mortality_instantaneous`

categories      Categories for natural mortality  
Type: string vector  
Default: No Default

print\_report      Generate parameter report  
Type: boolean  
Default: false

m      Mortality rates  
Type: constant vector  
Default: No Default  
Lower Bound: 0.0 (inclusive)  
Upper Bound: 1.0 (inclusive)

selectivities      Selectivities for Natural Mortality  
Type: string vector  
Default: No Default

time\_step\_ratio      Time step ratios for M  
Type: constant vector  
Default: true

units      Unit of weight that the Catches table are expressed in  
Type: string  
Default: No Default

### 8.5.9. @process[label].type=mortality\_prey\_suitability

consumption\_rate      Predator consumption rate

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

print\_report      Generate parameter report

Type: boolean

Default: false

electivities      Prey Electivities

Type: constant vector

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

penalty      Label of penalty to be applied

Type: string

Default: ""

predator\_categories      Predator Categories labels

Type: string vector

Default: No Default

predator\_selectivities      Selectivities for predator categories

Type: string vector

Default: No Default

prey\_categories      Prey Categories labels

Type: string vector

Default: No Default

prey\_selectivities      Selectivities for prey categories

Type: string vector

Default: No Default

u\_max      Umax

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

years      Year that process occurs



Type: non-negative integer vector

Default: No Default

#### 8.5.10. `@process[label].type=nop`

`print_report`      Generate parameter report

Type: boolean

Default: false

#### 8.5.11. `@process[label].type=recruitment_beverton_holt`

`age`      Age to recruit at

Type: non-negative integer

Default: true

`b0`      B0

Type: constant

Default: false

`units`      Units of B0, if initialising model using B0

Type: string

Default: ""

`categories`      Category labels

Type: string vector

Default: No Default

`print_report`      Generate parameter report

Type: boolean

Default: false

`b0_initialisation_phase`      Initialisation phase Label that b0 is from

Type: string

Default: ""

`prior_standardised_ycs`      Priors for year class strength on ycs values (not standardised ycs values)

Type: boolean

Default: true

`proportions`      Proportions

Type: constant vector

Default: No Default

r0      R0

Type: constant

Default: false

ssb      SSB Label (derived quantity)

Type: string

Default: No Default

ssb\_offset      Spawning biomass year offset

Type: integer

Default: false

standardise\_ycs\_years      Years that are included for year class standardisation

Type: non-negative integer vector

Default: true

steepness      Steepness

Type: constant

Default: 1.0

ycs\_values      YCS Values

Type: constant vector

Default: No Default

### **8.5.12. @process[label].type=recruitment\_constant**

age      Age

Type: non-negative integer

Default: No Default

categories      Categories

Type: string vector

Default: No Default

print\_report      Generate parameter report

Type: boolean

Default: false

proportions      Proportions

Type: constant vector

Default: true

r0      R0

Type: constant  
Default: No Default  
Lower Bound: 0.0 (exclusive)

### 8.5.13. `@process[label].type=tag_by_age`

`print_report`      Generate parameter report  
Type: boolean  
Default: false

`from`      Categories to transition from  
Type: string vector  
Default: No Default

`initial_mortality`  
Type: constant  
Default: Double(0)

`initial_mortality_selectivity`  
Type: string  
Default: ""

`loss_rate`  
Type: constant vector  
Default: No Default

`loss_rate_selectivities`  
Type: string vector  
Default: true

`max_age`      Maximum age to transition  
Type: non-negative integer  
Default: No Default

`min_age`      Minimum age to transition  
Type: non-negative integer  
Default: No Default

`n`  
Type: constant vector  
Default: true

`penalty`      Penalty label  
Type: string  
Default: ""

selectivities

Type: string vector

Default: No Default

to Categories to transition to

Type: string vector

Default: No Default

u\_max U Max

Type: constant

Default: 0.99

years Years to execute the transition in

Type: non-negative integer vector

Default: No Default

#### **8.5.14. @process[label].type=tag\_by\_length**

print\_report Generate parameter report

Type: boolean

Default: false

from Categories to transition from

Type: string vector

Default: No Default

initial\_mortality

Type: constant

Default: Double(0)

initial\_mortality\_selectivity

Type: string

Default: ""

maximum\_length The upper length when there is no plus group

Type: constant

Default: Double(0)

n

Type: constant vector

Default: true

penalty Penalty label

Type: string  
Default: ""

`plus_group`      Use plus group for last length bin  
Type: boolean  
Default: false

`selectivities`  
Type: string vector  
Default: No Default

`to`      Categories to transition to  
Type: string vector  
Default: No Default

`u_max`      U Max  
Type: constant  
Default: 0.99

`years`      Years to execute the transition in  
Type: non-negative integer vector  
Default: No Default

### 8.5.15. `@process[label].type=tag_loss`

`categories`      List of categories  
Type: string vector  
Default: No Default

`print_report`      Generate parameter report  
Type: boolean  
Default: false

`time_step_ratio`      Time step ratios for Tag Loss  
Type: constant vector  
Default: true

`selectivities`      Selectivities  
Type: string vector  
Default: No Default

`tag_loss_rate`      Tag Loss rates  
Type: constant vector  
Default: No Default

tag\_loss\_type    Type of tag loss  
  Type: string  
  Default: No Default

year    The year the first tagging release process was executed  
  Type: non-negative integer  
  Default: No Default

#### **8.5.16. @process[label].type=transition\_category**

print\_report    Generate parameter report  
  Type: boolean  
  Default: false

from    From  
  Type: string vector  
  Default: No Default

proportions    Proportions  
  Type: constant vector  
  Default: No Default

selectivities    Selectivity names  
  Type: string vector  
  Default: No Default

to    To  
  Type: string vector  
  Default: No Default

#### **8.5.17. @process[label].type=transition\_category\_by\_age**

print\_report    Generate parameter report  
  Type: boolean  
  Default: false

from    Categories to transition from  
  Type: string vector  
  Default: No Default

max\_age    Maximum age to transition  
  Type: non-negative integer  
  Default: No Default

`min_age` Minimum age to transition  
Type: non-negative integer  
Default: No Default

`penalty` Penalty label  
Type: string  
Default: ""

`to` Categories to transition to  
Type: string vector  
Default: No Default

`u_max` U Max  
Type: constant  
Default: 0.99

`years` Years to execute the transition in  
Type: non-negative integer vector  
Default: No Default

## 8.6. Time varying parameters

**@time\_varying** *label* Define an object type Time\_Varying

`label` Label  
Type: string  
Default: No Default

`parameter` Parameter to vary  
Type: string  
Default: No Default

`type` Type  
Type: string  
Default: ""

`years` Years to recalculate the values  
Type: non-negative integer vector  
Default: No Default

### 8.6.1. @time\_varying[label].type=annual\_shift

`a`  
Type: constant  
Default: No Default

b

Type: constant

Default: No Default

c

Type: constant

Default: No Default

parameter      Parameter to vary

Type: string

Default: No Default

scaling\_years

Type: non-negative integer vector

Default: true

values

Type: constant vector

Default: No Default

years      Years to recalculate the values

Type: non-negative integer vector

Default: No Default

### **8.6.2. @time\_varying[label].type=constant**

parameter      Parameter to vary

Type: string

Default: No Default

value      Value to assign to estimable

Type: constant vector

Default: No Default

years      Years to recalculate the values

Type: non-negative integer vector

Default: No Default

### **8.6.3. @time\_varying[label].type=exogenous**

a      Shift parameter

Type: constant

Default: No Default



`exogeneous_variable`      Values of exogeneous variable for each year  
Type: constant vector  
Default: No Default

`parameter`      Parameter to vary  
Type: string  
Default: No Default

`years`      Years to recalculate the values  
Type: non-negative integer vector  
Default: No Default

#### 8.6.4. `@time_varying[label].type=random_walk`

`distribution`      distribution  
Type: string  
Default: normal

`mean`      Mean  
Type: constant  
Default: 0

`parameter`      Parameter to vary  
Type: string  
Default: No Default

`sigma`      Standard deviation  
Type: constant  
Default: 1

`years`      Years to recalculate the values  
Type: non-negative integer vector  
Default: No Default

### 8.7. Derived quantities

`@derived_quantity label`      Define an object type `Derived.Quantity`

`categories`      The list of categories to use when calculating the derived quantity  
Type: string vector  
Default: No Default

`label`      Label

Type: string  
Default: No Default

time\_step\_proportion\_method  
Type: string  
Default: weighted\_sum  
Allowed Values: weighted\_sum, weighted\_product

selectivities      The list of selectivities to use when calculating the derived quantity. 1 per category  
Type: string vector  
Default: No Default

time\_step      The time step to calculate the derived quantity after  
Type: string  
Default: No Default

time\_step\_proportion  
Type: constant  
Default: Double(1.0)

type      Type  
Type: string  
Default: No Default

### 8.7.1. @derived\_quantity[label].type=abundance

categories      The list of categories to use when calculating the derived quantity  
Type: string vector  
Default: No Default

time\_step\_proportion\_method  
Type: string  
Default: weighted\_sum  
Allowed Values: weighted\_sum, weighted\_product

selectivities      The list of selectivities to use when calculating the derived quantity. 1 per category  
Type: string vector  
Default: No Default

time\_step      The time step to calculate the derived quantity after  
Type: string  
Default: No Default

time\_step\_proportion

Type: constant

Default: Double(1.0)

### 8.7.2. @derived\_quantity[label].type=biomass

categories      The list of categories to use when calculating the derived quantity

Type: string vector

Default: No Default

time\_step\_proportion\_method

Type: string

Default: weighted\_sum

Allowed Values: weighted\_sum, weighted\_product

selectivities      The list of selectivities to use when calculating the derived quantity. 1 per category

Type: string vector

Default: No Default

time\_step      The time step to calculate the derived quantity after

Type: string

Default: No Default

time\_step\_proportion

Type: constant

Default: Double(1.0)

## 8.8. Age-length relationship

@age\_length label      Define an object type Age\_Length

casal\_switch      A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm

Type: boolean

Default: false

cv\_first      CV for the first age class

Type: constant

Default: Double(0.0

Lower Bound: 0.0 (inclusive)

cv\_last      CV for last age class

Type: constant  
Default: Double(0.0  
Lower Bound: 0.0 (inclusive)

distribution      TBA  
Type: string  
Default: normal

label      Label  
Type: string  
Default: No Default

time\_step\_proportions      the proportion increase of age through the in each time step that corresponds to a length and thus weight increase  
Type: constant vector  
Default: true

type      Type  
Type: string  
Default: No Default

### 8.8.1. @age\_\_length[label].type=data

by\_length      Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age  
Type: boolean  
Default: true

casal\_switch      A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm  
Type: boolean  
Default: false

cv\_first      CV for the first age class  
Type: constant  
Default: Double(0.0  
Lower Bound: 0.0 (inclusive)

cv\_last      CV for last age class  
Type: constant  
Default: Double(0.0  
Lower Bound: 0.0 (inclusive)

distribution      TBA

Type: string  
Default: normal

external\_gaps  
Type: string  
Default: mean  
Allowed Values: mean, nearest\_neighbour

internal\_gaps  
Type: string  
Default: mean  
Allowed Values: mean, nearest\_neighbour, interpolate

length\_weight      TBA  
Type: string  
Default: No Default

time\_step\_proportions      the proportion increase of age through the in each time step that corresponds to a length and thus weight increase  
Type: constant vector  
Default: true

### 8.8.2. @age\_length[label].type=none

casal\_switch      A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm  
Type: boolean  
Default: false

cv\_first      CV for the first age class  
Type: constant  
Default: Double(0.0  
Lower Bound: 0.0 (inclusive)

cv\_last      CV for last age class  
Type: constant  
Default: Double(0.0  
Lower Bound: 0.0 (inclusive)

distribution      TBA  
Type: string  
Default: normal

time\_step\_proportions      the proportion increase of age through the in each time step that

corresponds to a length and thus weight increase

Type: constant vector

Default: true

### 8.8.3. @age\_\_length[label].type=schnute

a TBA

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

b TBA

Type: constant

Default: No Default

Lower Bound: 0.0 (exclusive)

by\_length TBA

Type: boolean

Default: true

casal\_switch A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm

Type: boolean

Default: false

cv\_first CV for the first age class

Type: constant

Default: Double(0.0

Lower Bound: 0.0 (inclusive)

cv\_last CV for last age class

Type: constant

Default: Double(0.0

Lower Bound: 0.0 (inclusive)

distribution TBA

Type: string

Default: normal

length\_weight TBA

Type: string

Default: No Default

taul TBA

Type: constant  
Default: No Default

tau2      TBA  
Type: constant  
Default: No Default

time\_step\_proportions      the proportion increase of age through the in each time step that corresponds to a length and thus weight increase  
Type: constant vector  
Default: true

y1      TBA  
Type: constant  
Default: No Default

y2      TBA  
Type: constant  
Default: No Default

#### **8.8.4. @age\_length[label].type=von bertalanffy**

by\_length      Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age  
Type: boolean  
Default: true

casal\_switch      A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm  
Type: boolean  
Default: false

cv\_first      CV for the first age class  
Type: constant  
Default: Double(0.0  
Lower Bound: 0.0 (inclusive)

cv\_last      CV for last age class  
Type: constant  
Default: Double(0.0  
Lower Bound: 0.0 (inclusive)

distribution      TBA  
Type: string  
Default: normal

k      TBA

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

length\_weight      TBA

Type: string

Default: No Default

linf      TBA

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

t0      TBA

Type: constant

Default: No Default

time\_step\_proportions      the proportion increase of age through the in each time step that corresponds to a length and thus weight increase

Type: constant vector

Default: true

## 8.9. Length-weight

**@length\_weight** *label*      Define an object type Length\_Weight

label      Label

Type: string

Default: No Default

type      Type

Type: string

Default: No Default

### 8.9.1. @length\_weight[label].type=basic

a      A

Type: constant

Default: No Default

b      B

Type: constant

Default: No Default



`units`      Units of measure (tonnes, kgs, grams)  
Type: string  
Default: No Default

### 8.9.2. `@length_weight[label].type=none`

## 8.10. Selectivities

**`@selectivity label`**      Define an object type Selectivity

`label`      Label  
Type: string  
Default: No Default

`length_based`      Is the selectivity length based  
Type: boolean  
Default: false

`intervals`      Number of quantiles to evaluate a length based selectivity over the age length distribution  
Type: non-negative integer  
Default: 5

`type`      Type  
Type: string  
Default: No Default

### 8.10.1. `@selectivity[label].type=all_values`

`length_based`      Is the selectivity length based  
Type: boolean  
Default: false

`intervals`      Number of quantiles to evaluate a length based selectivity over the age length distribution  
Type: non-negative integer  
Default: 5

`v`      V  
Type: constant vector  
Default: No Default

### 8.10.2. @selectivity[label].type=all\_values\_bounded

h H

Type: non-negative integer

Default: No Default

length\_based Is the selectivity length based

Type: boolean

Default: false

l L

Type: non-negative integer

Default: No Default

intervals Number of quantiles to evaluate a length based selectivity over the age length distribution

Type: non-negative integer

Default: 5

v V

Type: constant vector

Default: No Default

### 8.10.3. @selectivity[label].type=constant

c C

Type: constant

Default: No Default

length\_based Is the selectivity length based

Type: boolean

Default: false

intervals Number of quantiles to evaluate a length based selectivity over the age length distribution

Type: non-negative integer

Default: 5

### 8.10.4. @selectivity[label].type=double\_exponential

alpha Alpha

Type: constant

Default: 1.0

length\_based      Is the selectivity length based  
Type: boolean  
Default: false

intervals      Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
Type: non-negative integer  
Default: 5

x0      X0  
Type: constant  
Default: No Default

x1      X1  
Type: constant  
Default: No Default

x2      X2  
Type: constant  
Default: No Default

y0      Y0  
Type: constant  
Default: No Default

y1      Y1  
Type: constant  
Default: No Default

y2      Y2  
Type: constant  
Default: No Default

#### **8.10.5. @selectivity[label].type=double normal**

alpha      Alpha  
Type: constant  
Default: 1.0

length\_based      Is the selectivity length based  
Type: boolean  
Default: false

mu      Mu

Type: constant  
Default: No Default

`intervals`      Number of quantiles to evaluate a length based selectivity over the age length distribution  
Type: non-negative integer  
Default: 5

`sigma_l`      Sigma L  
Type: constant  
Default: No Default

`sigma_r`      Sigma R  
Type: constant  
Default: No Default

#### **8.10.6. @selectivity[label].type=increasing**

`alpha`      Alpha  
Type: constant  
Default: 1.0

`h`      High  
Type: non-negative integer  
Default: No Default

`length_based`      Is the selectivity length based  
Type: boolean  
Default: false

`l`      Low  
Type: non-negative integer  
Default: No Default

`intervals`      Number of quantiles to evaluate a length based selectivity over the age length distribution  
Type: non-negative integer  
Default: 5

`v`      V  
Type: constant vector  
Default: No Default

**8.10.7. @selectivity[label].type=inverse\_logistic**

a50      A50  
Type: constant  
Default: No Default

alpha     Alpha  
Type: constant  
Default: 1.0

ato95     aTo95  
Type: constant  
Default: No Default

length\_based    Is the selectivity length based  
Type: boolean  
Default: false

intervals      Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
Type: non-negative integer  
Default: 5

**8.10.8. @selectivity[label].type=knife\_edge**

alpha     Alpha  
Type: constant  
Default: 1.0

e      Edge  
Type: constant  
Default: No Default

length\_based    Is the selectivity length based  
Type: boolean  
Default: false

intervals      Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
Type: non-negative integer  
Default: 5

### 8.10.9. `@selectivity[label].type=logistic`

a50      A50

Type: constant

Default: No Default

alpha     Alpha

Type: constant

Default: 1.0

ato95     Ato95

Type: constant

Default: No Default

length\_based    Is the selectivity length based

Type: boolean

Default: false

intervals       Number of quantiles to evaluate a length based selectivity over the age length  
distribution

Type: non-negative integer

Default: 5

### 8.10.10. `@selectivity[label].type=logistic_producing`

a50      A50

Type: constant

Default: No Default

alpha     Alpha

Type: constant

Default: 1.0

ato95     Ato95

Type: constant

Default: No Default

h          High

Type: non-negative integer

Default: No Default

length\_based    Is the selectivity length based

Type: boolean

Default: false

---

`l`      **Low**  
Type: non-negative integer  
Default: No Default

`intervals`      Number of quantiles to evaluate a length based selectivity over the age length distribution  
Type: non-negative integer  
Default: 5

## 9. Estimation command and subcommand syntax

### 9.1. Estimation methods

**@estimate** *label*      Define an object type Estimate

`estimation_phase`      TBA  
Type: non-negative integer  
Default: 1u

`label`      **Label**  
Type: string  
Default: ""

`lower_bound`      The lowest value the parameter is allowed to have  
Type: constant  
Default: No Default

`mcmc`      TBA  
Type: boolean  
Default: false

`parameter`      The name of the variable to estimate in the model  
Type: string  
Default: No Default

`prior`      The name of the prior to use for the parameter  
Type: string  
Default: ""

`same`      A list of parameters that are bound to the value of this estimate  
Type: string vector  
Default: ""

`type`      **Type**

Type: string  
Default: No Default

`upper_bound`      The highest value the parameter is allowed to have  
Type: constant  
Default: No Default

### 9.1.1. `@estimate[label].type=beta`

a      A  
Type: constant  
Default: No Default

b      B  
Type: constant  
Default: No Default

`estimation_phase`      TBA  
Type: non-negative integer  
Default: 1u

`lower_bound`      The lowest value the parameter is allowed to have  
Type: constant  
Default: No Default

`mcmc`      TBA  
Type: boolean  
Default: false

`mu`      Mu  
Type: constant  
Default: No Default

`parameter`      The name of the variable to estimate in the model  
Type: string  
Default: No Default

`prior`      The name of the prior to use for the parameter  
Type: string  
Default: ""

`same`      A list of parameters that are bound to the value of this estimate  
Type: string vector  
Default: ""



`sigma`      **Sigma**

Type: constant

Default: No Default

Lower Bound: 0.0 (exclusive)

`upper_bound`      The highest value the parameter is allowed to have

Type: constant

Default: No Default

### 9.1.2. `@estimate[label].type=lognormal`

`cv`      **Cv**

Type: constant

Default: No Default

Lower Bound: 0.0 (exclusive)

`estimation_phase`      **TBA**

Type: non-negative integer

Default: 1u

`lower_bound`      The lowest value the parameter is allowed to have

Type: constant

Default: No Default

`mcmc`      **TBA**

Type: boolean

Default: false

`mu`      **Mu**

Type: constant

Default: No Default

Lower Bound: 0.0 (exclusive)

`parameter`      The name of the variable to estimate in the model

Type: string

Default: No Default

`prior`      The name of the prior to use for the parameter

Type: string

Default: ""

`same`      A list of parameters that are bound to the value of this estimate

Type: string vector

Default: ""

`upper_bound`     The highest value the parameter is allowed to have  
Type: constant  
Default: No Default

### 9.1.3. `@estimate[label].type=normal`

`cv`     `Cv`  
Type: constant  
Default: No Default  
Lower Bound: 0.0 (exclusive)

`estimation_phase`     TBA  
Type: non-negative integer  
Default: 1u

`lower_bound`     The lowest value the parameter is allowed to have  
Type: constant  
Default: No Default

`mcmc`     TBA  
Type: boolean  
Default: false

`mu`     `Mu`  
Type: constant  
Default: No Default

`parameter`     The name of the variable to estimate in the model  
Type: string  
Default: No Default

`prior`     The name of the prior to use for the parameter  
Type: string  
Default: ""

`same`     A list of parameters that are bound to the value of this estimate  
Type: string vector  
Default: ""

`upper_bound`     The highest value the parameter is allowed to have  
Type: constant  
Default: No Default

**9.1.4. @estimate[label].type=normal\_by\_stdev**

estimation\_phase    TBA

Type: non-negative integer

Default: 1u

lower\_bound    The lowest value the parameter is allowed to have

Type: constant

Default: No Default

mcmc    TBA

Type: boolean

Default: false

mu    Mu

Type: constant

Default: No Default

parameter    The name of the variable to estimate in the model

Type: string

Default: No Default

prior    The name of the prior to use for the parameter

Type: string

Default: ""

same    A list of parameters that are bound to the value of this estimate

Type: string vector

Default: ""

sigma    Sigma

Type: constant

Default: No Default

Lower Bound: 0.0 (exclusive)

upper\_bound    The highest value the parameter is allowed to have

Type: constant

Default: No Default

**9.1.5. @estimate[label].type=normal\_log**

estimation\_phase    TBA

Type: non-negative integer

Default: 1u

`lower_bound`     The lowest value the parameter is allowed to have  
Type: constant  
Default: No Default

`mcmc`     TBA  
Type: boolean  
Default: false

`mu`     Mu  
Type: constant  
Default: No Default

`parameter`     The name of the variable to estimate in the model  
Type: string  
Default: No Default

`prior`     The name of the prior to use for the parameter  
Type: string  
Default: ""

`same`     A list of parameters that are bound to the value of this estimate  
Type: string vector  
Default: ""

`sigma`     Sigma  
Type: constant  
Default: No Default  
Lower Bound: 0.0 (exclusive)

`upper_bound`     The highest value the parameter is allowed to have  
Type: constant  
Default: No Default

#### 9.1.6. **@estimate[label].type=uniform**

`estimation_phase`     TBA  
Type: non-negative integer  
Default: 1u

`lower_bound`     The lowest value the parameter is allowed to have  
Type: constant  
Default: No Default

`mcmc`     TBA

Type: boolean

Default: false

`parameter`     The name of the variable to estimate in the model

Type: string

Default: No Default

`prior`     The name of the prior to use for the parameter

Type: string

Default: ""

`same`     A list of parameters that are bound to the value of this estimate

Type: string vector

Default: ""

`upper_bound`     The highest value the parameter is allowed to have

Type: constant

Default: No Default

### 9.1.7. `@estimate[label].type=uniform_log`

`estimation_phase`     TBA

Type: non-negative integer

Default: 1u

`lower_bound`     The lowest value the parameter is allowed to have

Type: constant

Default: No Default

`mcmc`     TBA

Type: boolean

Default: false

`parameter`     The name of the variable to estimate in the model

Type: string

Default: No Default

`prior`     The name of the prior to use for the parameter

Type: string

Default: ""

`same`     A list of parameters that are bound to the value of this estimate

Type: string vector

Default: ""

`upper_bound`      The highest value the parameter is allowed to have  
     Type: constant  
     Default: No Default

## 9.2. Point estimation

**@minimiser** *label*      Define an object type Minimiser

`active`      True if this minimiser is active  
     Type: boolean  
     Default: false

`covariance`      True if a covariance matrix should be created  
     Type: boolean  
     Default: true

`label`      Label  
     Type: string  
     Default: No Default

`type`      Type of minimiser to use  
     Type: string  
     Default: No Default

### 9.2.1. @minimiser[label].type=adolc

`active`      True if this minimiser is active  
     Type: boolean  
     Default: false

`covariance`      True if a covariance matrix should be created  
     Type: boolean  
     Default: true

`tolerance`      Tolerance of the gradient for convergence  
     Type: constant  
     Default: 0.02

`evaluations`      Maximum number of evaluations  
     Type: integer  
     Default: 4000

`iterations`      Maximum number of iterations  
     Type: integer  
     Default: 1000

`step_size` Minimum Step-size before minimisation fails  
Type: constant  
Default: 1e-7

### 9.2.2. `@minimiser[label].type=beta_diff`

`active` True if this minimiser is active  
Type: boolean  
Default: false

`covariance` True if a covariance matrix should be created  
Type: boolean  
Default: true

`tolerance` Tolerance of the gradient for convergence  
Type: constant  
Default: 2e-3

`evaluations` Maximum number of evaluations  
Type: integer  
Default: 4000

`iterations` Maximum number of iterations  
Type: integer  
Default: 1000

### 9.2.3. `@minimiser[label].type=cppad`

`active` True if this minimiser is active  
Type: boolean  
Default: false

`covariance` True if a covariance matrix should be created  
Type: boolean  
Default: true

### 9.2.4. `@minimiser[label].type=de_solver`

`active` True if this minimiser is active  
Type: boolean  
Default: false

`covariance`      True if a covariance matrix should be created  
Type: boolean  
Default: true

`crossover_probability`      TBA  
Type: constant  
Default: 0.9

`difference_scale`      The scale to apply to new solutions when comparing candidates  
Type: constant  
Default: 0.02

`max_generations`      The maximum number of iterations to run  
Type: non-negative integer  
Default: No Default

`method`      The type of candidate generation method to use  
Type: string  
Default: ""  
Value: not\_yet\_implemented

`population_size`      The number of candidate solutions to have in the population  
Type: non-negative integer  
Default: No Default

`tolerance`      The total variance between the population and best candidate before acceptance  
Type: constant  
Default: 0.01

### **9.2.5. @minimiser[label].type=d\_lib**

`active`      True if this minimiser is active  
Type: boolean  
Default: false

`covariance`      True if a covariance matrix should be created  
Type: boolean  
Default: true

### **9.2.6. @minimiser[label].type=gamma\_diff**

`active`      True if this minimiser is active  
Type: boolean  
Default: false



`covariance`      True if a covariance matrix should be created  
Type: boolean  
Default: true

`tolerance`      Tolerance of the gradient for convergence  
Type: constant  
Default: 0.02

`evaluations`      Maximum number of evaluations  
Type: integer  
Default: 4000

`iterations`      Maximum number of iterations  
Type: integer  
Default: 1000

`step_size`      Minimum Step-size before minimisation fails  
Type: constant  
Default: 1e-7

### 9.3. Monte Carlo Markov Chain (MCMC)

**@mcmc** *label*      Define an object type MCMC

`active`      Is this the active MCMC algorithm  
Type: boolean  
Default: true

`label`      Label  
Type: string  
Default: No Default

`length`      The number of chain links to create  
Type: non-negative integer  
Default: No Default

`print_default_reports`  
Type: boolean  
Default: true

`type`      Type  
Type: string  
Default: ""

### 9.3.1. @m\_c\_m\_c[label].type=independence\_metropolis

`active` Is this the active MCMC algorithm

Type: boolean

Default: true

`adapt_stepsize_at` Iterations in the chain to check and resize the MCMC stepsize

Type: non-negative integer vector

Default: true

`correlation_adjustment_diff` TBA

Type: constant

Default: 0.0001

`covariance_adjustment_method` Method for adjusting small variances in the covariance proposal matrix

Type: string

Default: covariance

`df` Degrees of freedom of the multivariate t proposal distribution

Type: non-negative integer

Default: 4

`keep` Spacing between recorded values in the chain

Type: non-negative integer

Default: 1u

`length` The number of chain links to create

Type: non-negative integer

Default: No Default

`max_correlation` Maximum absolute correlation in the covariance matrix of the proposal distribution

Type: constant

Default: 0.8

`print_default_reports`

Type: boolean

Default: true

`proposal_distribution` The shape of the proposal distribution (either t or normal)

Type: string

Default: t

`start` Covariance multiplier for the starting point of the Markov chain

Type: constant  
Default: 0.0

`step_size`      Initial stepsize (as a multiplier of the approximate covariance matrix)  
Type: constant  
Default: 0.02

## 9.4. Profiles

**@profile** *label*      Define an object type Profile

`label`      Label  
Type: string  
Default: ""

`lower_bound`      The lower bounds  
Type: constant  
Default: No Default

`parameter`      The system parameter to profile  
Type: string  
Default: No Default

`steps`      The number of steps to take between the lower and upper bound  
Type: non-negative integer  
Default: No Default

`type`  
Type: string  
Default: No Default

`upper_bound`      The upper bounds  
Type: constant  
Default: No Default

## 9.5. Defining catchability constants

**@catchability** *label*      Define an object type Catchability

`label`      Label  
Type: string  
Default: No Default

`type`

Type: string  
Default: No Default

### 9.5.1. `@catchability[label].type=free`

`q`      The catchability amount  
Type: constant  
Default: No Default

## 9.6. Defining penalties

**@penalty** *label*      Define an object type Penalty

`label`      Label  
Type: string  
Default: No Default

`type`      Type  
Type: string  
Default: No Default

### 9.6.1. `@penalty[label].type=process`

`log_scale`      Log scale  
Type: boolean  
Default: false

`multiplier`      Multiplier  
Type: constant  
Default: 1.0

## 9.7. Defining priors on parameter ratios, differences and means

**@additional\_prior** *label*      Define an object type Additional\_Prior

`label`      Label  
Type: string  
Default: No Default

`type`      Type  
Type: string  
Default: No Default

**9.7.1. @additional\_prior[label].type=beta**

a     A

Type: constant

Default: No Default

b     B

Type: constant

Default: No Default

mu    Mu

Type: constant

Default: No Default

sigma   Sigma

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

**9.7.2. @additional\_prior[label].type=vector\_average**

k     K Value to use in the calculation

Type: constant

Default: No Default

method   What calculation method to use (k, l, m)

Type: string

Default: k

multiplier   Multiplier for the penalty amount

Type: constant

Default: 1

parameter   Label of the estimate to generate penalty on

Type: string

Default: No Default

**9.7.3. @additional\_prior[label].type=vector\_smoothing**

log\_scale   Log scale

Type: boolean

Default: false

lower\_bound   First element to apply the penalty to in the vector

Type: non-negative integer  
 Default: 0u

`multiplier`      Multiplier for the penalty amount  
 Type: constant  
 Default: 1

`parameter`      Label of the estimate to generate penalty on  
 Type: string  
 Default: No Default

`r`      Penalty applied to  $r$ th differences  
 Type: non-negative integer  
 Default: 2u

`upper_bound`      Last element to apply the penalty to in the vector  
 Type: non-negative integer  
 Default: 0u

## 10. Observation command and subcommand syntax

### 10.1. Observation types

The observation types available are,

Observations of proportions of individuals by age class

Observations of proportions of individuals between categories within each age class

Relative and absolute abundance observations

Relative and absolute biomass observations

Each type of observation requires a set of subcommands and arguments specific to that process.

**@observation** *label*      Define an object type Observation

`categories`      Category labels to use  
 Type: string vector  
 Default: true

`error_value_multiplier`      Error value multiplier for likelihood  
 Type: constant  
 Default: Double(1.0)

`label`      Label  
 Type: string  
 Default: No Default

likelihood\_multiplier    Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

likelihood    Type of likelihood to use  
Type: string  
Default: No Default

simulation\_likelihood    Simulation likelihood to use  
Type: string  
Default: ""

type    Type of observation  
Type: string  
Default: No Default

#### **10.1.1. @observation[label].type=process\_abundance**

catchability    Abundance catchability  
Type: string  
Default: No Default

categories    Category labels to use  
Type: string vector  
Default: true

delta    Delta value for error values  
Type: constant  
Default: Double(1e-10)

error\_value\_multiplier    Error value multiplier for likelihood  
Type: constant  
Default: Double(1.0)

error\_value    The error values to use against the observation values  
Type: constant vector  
Default: No Default

likelihood\_multiplier    Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

likelihood    Type of likelihood to use  
Type: string  
Default: No Default

obs      Observation values

Type: string vector

Default: No Default

process\_error      Process error

Type: constant

Default: Double(0.0)

process      Process label

Type: string

Default: No Default

process\_proportion      Process proportion

Type: constant

Default: Double(0.5)

selectivities      Selectivity labels to use

Type: string vector

Default: true

simulation\_likelihood      Simulation likelihood to use

Type: string

Default: ""

time\_step      Time step to execute in

Type: string

Default: No Default

years      Years to execute in

Type: non-negative integer vector

Default: No Default

### **10.1.2. @observation[label].type=time\_step\_abundance**

catchability      TBA

Type: string

Default: No Default

categories      Category labels to use

Type: string vector

Default: true

delta      Delta value for error values



	Type: constant Default: Double(1e-10)
error_value_multiplier	Error value multiplier for likelihood Type: constant Default: Double(1.0)
error_value	The error values to use against the observation values Type: constant vector Default: No Default
likelihood_multiplier	Likelihood score multiplier Type: constant Default: Double(1.0)
likelihood	Type of likelihood to use Type: string Default: No Default
obs	Observation values Type: string vector Default: No Default
process_error	Process error Type: constant Default: Double(0.0)
selectivities	Selectivity labels to use Type: string vector Default: true
simulation_likelihood	Simulation likelihood to use Type: string Default: ""
time_step	Time step to execute in Type: string Default: No Default
time_step_proportion	Proportion through the time step to analyse the partition from Type: constant Default: Double(0.5)
years	Years to execute in

Type: non-negative integer vector

Default: No Default

### 10.1.3. @observation[label].type=process\_biomass

catchability      Catchability of Biomass

Type: string

Default: No Default

categories      Category labels to use

Type: string vector

Default: true

delta      Delta value for error values

Type: constant

Default: Double(1e-10)

error\_value\_multiplier      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

error\_value      The error values to use against the observation values

Type: constant vector

Default: No Default

likelihood\_multiplier      Likelihood score multiplier

Type: constant

Default: Double(1.0)

likelihood      Type of likelihood to use

Type: string

Default: No Default

obs      Observation values

Type: string vector

Default: No Default

process\_error      Process error

Type: constant

Default: Double(0.0)

process      Process label

Type: string

Default: No Default

`process_proportion`      Process proportion  
Type: constant  
Default: Double(0.5)

`selectivities`      Selectivity labels to use  
Type: string vector  
Default: true

`simulation_likelihood`      Simulation likelihood to use  
Type: string  
Default: ""

`time_step`      Time step to execute in  
Type: string  
Default: No Default

`years`      Years to execute in  
Type: non-negative integer vector  
Default: No Default

#### **10.1.4. @observation[label].type=time\_step\_biomass**

`catchability`      Catchability of Biomass  
Type: string  
Default: No Default

`categories`      Category labels to use  
Type: string vector  
Default: true

`delta`      Delta value for error values  
Type: constant  
Default: Double(1e-10)

`error_value_multiplier`      Error value multiplier for likelihood  
Type: constant  
Default: Double(1.0)

`error_value`      The error values to use against the observation values  
Type: constant vector  
Default: No Default

`likelihood_multiplier`      Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

likelihood      Type of likelihood to use

Type: string

Default: No Default

obs      Observation values

Type: string vector

Default: No Default

process\_error      Process error

Type: constant

Default: Double(0.0)

selectivities      Selectivity labels to use

Type: string vector

Default: true

simulation\_likelihood      Simulation likelihood to use

Type: string

Default: ""

time\_step      Time step to execute in

Type: string

Default: No Default

time\_step\_proportion      Proportion through the time step to analyse the partition from

Type: constant

Default: Double(0.5)

years      Years to execute in

Type: non-negative integer vector

Default: No Default

#### 10.1.5. @observation[label].type=process\_proportions\_at\_age

age\_plus      Use age plus group

Type: boolean

Default: true

ageing\_error      Label of ageing error to use

Type: string

Default: ""

categories      Category labels to use

Type: string vector  
Default: true

delta      **Delta**  
Type: constant  
Default: DELTA

error\_value\_multiplier      Error value multiplier for likelihood  
Type: constant  
Default: Double(1.0)

likelihood\_multiplier      Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

likelihood      Type of likelihood to use  
Type: string  
Default: No Default

max\_age      **Maximum age**  
Type: non-negative integer  
Default: No Default

min\_age      **Minimum age**  
Type: non-negative integer  
Default: No Default

process\_errors      Process error  
Type: constant vector  
Default: true

process      Process label  
Type: string  
Default: No Default

process\_proportion      Process proportion  
Type: constant  
Default: Double(0.5)

selectivities      Selectivity labels to use  
Type: string vector  
Default: true

simulation\_likelihood      Simulation likelihood to use

Type: string  
Default: ""

time\_step      Time step to execute in  
Type: string  
Default: No Default

tolerance      Tolerance  
Type: constant  
Default: Double(0.001)

years      Year to execute in  
Type: non-negative integer vector  
Default: No Default

#### **10.1.6. @observation[label].type=time\_step\_proportions\_at\_age**

age\_plus      Use age plus group  
Type: boolean  
Default: true

ageing\_error      Label of ageing error to use  
Type: string  
Default: ""

categories      Category labels to use  
Type: string vector  
Default: true

delta      Delta  
Type: constant  
Default: DELTA

error\_value\_multiplier      Error value multiplier for likelihood  
Type: constant  
Default: Double(1.0)

likelihood\_multiplier      Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

likelihood      Type of likelihood to use  
Type: string  
Default: No Default

`max_age`      Maximum age  
Type: non-negative integer  
Default: No Default

`min_age`      Minimum age  
Type: non-negative integer  
Default: No Default

`process_errors`      Process error  
Type: constant vector  
Default: true

`selectivities`      Selectivity labels to use  
Type: string vector  
Default: true

`simulation_likelihood`      Simulation likelihood to use  
Type: string  
Default: ""

`time_step`      Time step to execute in  
Type: string  
Default: No Default

`time_step_proportion`      Proportion through the time step to analyse the partition from  
Type: constant  
Default: Double(0.5)

`tolerance`      Tolerance  
Type: constant  
Default: Double(0.001)

`years`      Year to execute in  
Type: non-negative integer vector  
Default: No Default

#### **10.1.7. @observation[label].type=proportions.at.age.for.fishery**

`age_plus`      Use age plus group  
Type: boolean  
Default: true

`ageing_error`      Label of ageing error to use  
Type: string  
Default: ""

`categories`      Category labels to use

Type: string vector

Default: true

`delta`      Delta

Type: constant

Default: DELTA

`error_value_multiplier`      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

`fishery`      Label of fishery the observation is from

Type: string vector

Default: ""

`likelihood_multiplier`      Likelihood score multiplier

Type: constant

Default: Double(1.0)

`likelihood`      Type of likelihood to use

Type: string

Default: No Default

`max_age`      Maximum age

Type: non-negative integer

Default: No Default

`min_age`      Minimum age

Type: non-negative integer

Default: No Default

`process_errors`      Process error

Type: constant vector

Default: true

`process`      Process label

Type: string

Default: No Default

`simulation_likelihood`      Simulation likelihood to use

Type: string

Default: ""



`time_step`      Time steps that the fisheries are in  
Type: string vector  
Default: No Default

`tolerance`      Tolerance  
Type: constant  
Default: Double(0.001)

`years`      Year to execute in  
Type: non-negative integer vector  
Default: No Default

#### **10.1.8. `@observation[label].type=process_proportions_at_length`**

`categories`      Category labels to use  
Type: string vector  
Default: true

`delta`      Delta  
Type: constant  
Default: DELTA

`error_value_multiplier`      Error value multiplier for likelihood  
Type: constant  
Default: Double(1.0)

`length_bins`      Length bins  
Type: constant vector  
Default: No Default

`length_plus_group`      Is the last bin a plus group  
Type: boolean  
Default: true

`likelihood_multiplier`      Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

`likelihood`      Type of likelihood to use  
Type: string  
Default: No Default

`process_errors`      Process error  
Type: constant vector  
Default: true

process      Process label

Type: string

Default: No Default

process\_proportion      Process proportion

Type: constant

Default: Double(0.5)

selectivities      Selectivity labels to use

Type: string vector

Default: true

simulation\_likelihood      Simulation likelihood to use

Type: string

Default: ""

time\_step      Time step to execute in

Type: string

Default: No Default

tolerance      Tolerance for rescaling proportions

Type: constant

Default: Double(0.001)

years      Year to execute in

Type: non-negative integer vector

Default: No Default

#### **10.1.9. @observation[label].type=time\_step\_proportions\_at\_length**

categories      Category labels to use

Type: string vector

Default: true

delta      Delta

Type: constant

Default: DELTA

error\_value\_multiplier      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

length\_bins      Length bins

Type: constant vector  
Default: No Default

length\_plus\_group      Is the last bin a plus group  
Type: boolean  
Default: true

likelihood\_multiplier      Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

likelihood      Type of likelihood to use  
Type: string  
Default: No Default

process\_errors      Process error  
Type: constant vector  
Default: true

selectivities      Selectivity labels to use  
Type: string vector  
Default: true

simulation\_likelihood      Simulation likelihood to use  
Type: string  
Default: ""

time\_step      Time step to execute in  
Type: string  
Default: No Default

time\_step\_proportion      Proportion through the time step to analyse the partition from  
Type: constant  
Default: Double(0.5)

tolerance      Tolerance for rescaling proportions  
Type: constant  
Default: Double(0.001)

years      Year to execute in  
Type: non-negative integer vector  
Default: No Default

### 10.1.10. @observation[label].type=proportions\_at\_length\_for\_fishery

categories      Category labels to use

Type: string vector

Default: true

delta      Delta

Type: constant

Default: DELTA

error\_value\_multiplier      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

fishery      Label of fishery the observation is from

Type: string

Default: ""

length\_bins      Length bins

Type: constant vector

Default: No Default

length\_plus\_group      Is the last bin a plus group

Type: boolean

Default: true

likelihood\_multiplier      Likelihood score multiplier

Type: constant

Default: Double(1.0)

likelihood      Type of likelihood to use

Type: string

Default: No Default

process\_errors      Process error

Type: constant vector

Default: true

process      Process label

Type: string

Default: No Default

process\_proportion      Process proportion

Type: constant

Default: Double(0.5)

`simulation_likelihood`      Simulation likelihood to use  
Type: string  
Default: ""

`time_step`      Time step to execute in  
Type: string  
Default: No Default

`tolerance`      Tolerance for rescaling proportions  
Type: constant  
Default: Double(0.001)

`years`      Year to execute in  
Type: non-negative integer vector  
Default: No Default

#### **10.1.11. @observation[label].type=process\_proportions\_by\_category**

`age_plus`      Use age plus group  
Type: boolean  
Default: true

`categories`      Category labels to use  
Type: string vector  
Default: true

`delta`      Delta  
Type: constant  
Default: DELTA  
Lower Bound: 0.0 (exclusive)

`error_value_multiplier`      Error value multiplier for likelihood  
Type: constant  
Default: Double(1.0)

`likelihood_multiplier`      Likelihood score multiplier  
Type: constant  
Default: Double(1.0)

`likelihood`      Type of likelihood to use  
Type: string  
Default: No Default

`max_age`      Maximum age

Type: non-negative integer  
Default: No Default

`min_age`      Minimum age  
Type: non-negative integer  
Default: No Default

`process_errors`      Process error  
Type: constant vector  
Default: true

`process`      Process label  
Type: string  
Default: No Default

`process_proportion`      Process proportion  
Type: constant  
Default: Double(0.5)

`selectivities`      Selectivity labels to use  
Type: string vector  
Default: true

`simulation_likelihood`      Simulation likelihood to use  
Type: string  
Default: ""

`categories2`      Target Categories  
Type: string vector  
Default: No Default

`selectivities2`      Target Selectivities  
Type: string vector  
Default: No Default

`time_step`      Time step to execute in  
Type: string  
Default: No Default

`years`      Year to execute in  
Type: non-negative integer vector  
Default: No Default

**10.1.12. @observation[label].type=time\_step\_proportions\_by\_category**

age\_plus      Use age plus group

Type: boolean

Default: true

categories      Category labels to use

Type: string vector

Default: true

delta      Delta

Type: constant

Default: DELTA

Lower Bound: 0.0 (exclusive)

error\_value\_multiplier      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

likelihood\_multiplier      Likelihood score multiplier

Type: constant

Default: Double(1.0)

likelihood      Type of likelihood to use

Type: string

Default: No Default

max\_age      Maximum age

Type: non-negative integer

Default: No Default

min\_age      Minimum age

Type: non-negative integer

Default: No Default

process\_errors      Process error

Type: constant vector

Default: true

selectivities      Selectivity labels to use

Type: string vector

Default: true

simulation\_likelihood      Simulation likelihood to use

Type: string

Default: ""

categories2      Target Categories

Type: string vector

Default: No Default

selectivities2      Target Selectivities

Type: string vector

Default: No Default

time\_step      Time step to execute in

Type: string

Default: No Default

time\_step\_proportion      Proportion through the time step to analyse the partition from

Type: constant

Default: Double(0.5)

years      Year to execute in

Type: non-negative integer vector

Default: No Default

### **10.1.13. @observation[label].type=proportions migrating**

age\_plus      Use age plus group

Type: boolean

Default: true

ageing\_error      Label of ageing error to use

Type: string

Default: ""

categories      Category labels to use

Type: string vector

Default: true

delta      Delta

Type: constant

Default: DELTA

error\_value\_multiplier      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

likelihood\_multiplier      Likelihood score multiplier



Type: constant  
Default: Double(1.0)

likelihood      Type of likelihood to use  
Type: string  
Default: No Default

max\_age      Maximum age  
Type: non-negative integer  
Default: No Default

min\_age      Minimum age  
Type: non-negative integer  
Default: No Default

process\_errors      Process error  
Type: constant vector  
Default: true

process      Process label  
Type: string  
Default: No Default

process\_proportion      Process proportion  
Type: constant  
Default: Double(0.5)

simulation\_likelihood      Simulation likelihood to use  
Type: string  
Default: ""

time\_step      Time step to execute in  
Type: string  
Default: No Default

years      Year to execute in  
Type: non-negative integer vector  
Default: No Default

#### **10.1.14. @observation[label].type=tag-recapture by age**

age\_plus      Use age plus group  
Type: boolean  
Default: true

categories      Category labels to use

Type: string vector

Default: true

delta      Delta

Type: constant

Default: DELTA

Lower Bound: 0.0 (exclusive)

detection      Detection probability

Type: constant

Default: No Default

error\_value\_multiplier      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

likelihood\_multiplier      Likelihood score multiplier

Type: constant

Default: Double(1.0)

likelihood      Type of likelihood to use

Type: string

Default: No Default

max\_age      Maximum age

Type: non-negative integer

Default: No Default

min\_age      Minimum age

Type: non-negative integer

Default: No Default

process\_errors      Process error

Type: constant vector

Default: true

selectivities      Selectivity labels to use

Type: string vector

Default: true

simulation\_likelihood      Simulation likelihood to use

Type: string

Default: ""

categories2      Target Categories

Type: string vector

Default: No Default

selectivities2      Target Selectivities

Type: string vector

Default: No Default

time\_step      Time step to execute in

Type: string

Default: No Default

time\_step\_proportion      Proportion through the time step to analyse the partition from

Type: constant

Default: Double(0.5)

years      Year to execute in

Type: non-negative integer vector

Default: No Default

#### **10.1.15. @observation[label].type=tag-recapture-by-length**

categories      Category labels to use

Type: string vector

Default: true

delta      Delta

Type: constant

Default: DELTA

Lower Bound: 0.0 (exclusive)

detection      Detection probability

Type: constant

Default: No Default

error\_value\_multiplier      Error value multiplier for likelihood

Type: constant

Default: Double(1.0)

length\_bins      Length Bins

Type: constant vector

Default: No Default

likelihood\_multiplier      Likelihood score multiplier

Type: constant  
Default: Double(1.0)

likelihood      Type of likelihood to use  
Type: string  
Default: No Default

plus\_group      Last length bin a plus group  
Type: boolean  
Default: true

process\_errors      Process error  
Type: constant vector  
Default: true

selectivities      Selectivity labels to use  
Type: string vector  
Default: true

simulation\_likelihood      Simulation likelihood to use  
Type: string  
Default: ""

categories2      Target Categories  
Type: string vector  
Default: No Default

selectivities2      Target Selectivities  
Type: string vector  
Default: No Default

time\_step      Time step to execute in  
Type: string  
Default: No Default

time\_step\_proportion      Proportion through the time step to analyse the partition from  
Type: constant  
Default: Double(0.5)

years      Year to execute in  
Type: non-negative integer vector  
Default: No Default

## 10.2. Likelihoods

**@likelihood** *label*     Define an object type Likelihood

*label*

Type: string

Default: No Default

*type*

Type: string

Default: No Default

**10.2.1. @likelihood[label].type=binomial**

**10.2.2. @likelihood[label].type=binomial\_approx**

**10.2.3. @likelihood[label].type=dirichlet**

**10.2.4. @likelihood[label].type=log\_normal**

**10.2.5. @likelihood[label].type=log\_normal\_with\_q**

**10.2.6. @likelihood[label].type=multinomial**

**10.2.7. @likelihood[label].type=normal**

**10.2.8. @likelihood[label].type=pseudo**

## 10.3. Defining ageing error

Three methods for including ageing error into estimation with observations are,

- None
- Normal
- Off-by-one

Each type of ageing error requires a set of subcommands and arguments specific to its type.

**@ageing\_error** *label*     Define an object type Ageing\_Error

*label*     Label

Type: string

Default: No Default

*type*     Type

Type: string

Default: No Default

### 10.3.1. @ageing\_error[label].type=data

### 10.3.2. @ageing\_error[label].type=normal

cv CV for Misclassification matrix

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

k TBA

Type: non-negative integer

Default: 0u

### 10.3.3. @ageing\_error[label].type=off by one

k The minimum age of fish which can be missclassified

Type: non-negative integer

Default: 0u

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

p1 proprtion of misclassification up by a single age, i.e. Proportion of individuals at age 3 that are actually age 4

Type: constant

Default: No Default

p2 proprtion of misclassification down by a single age

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

## 11. Report command and subcommand syntax

### 11.1. Report commands and subcommands

**@report** *label* Define an object type Report

*file\_name* File Name

Type: string

Default: ""

*label* Label

Type: string

Default: No Default

type      Type  
Type: string  
Default: No Default

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### **11.1.1. @report [label] .type=ageing\_error\_matrix**

ageing\_error      Ageing Error label  
Type: string  
Default: No Default

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### **11.1.2. @report [label] .type=category\_info**

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### **11.1.3. @report [label] .type=category\_list**

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode

Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.4. @report[label].type=covariance.matrix

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.5. @report[label].type=derived.quantity

file\_name      File Name  
Type: string  
Default: ""

units      Unit of weight output expressed in  
Type: string  
Default: No Default

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.6. @report[label].type=estimable

file\_name      File Name  
Type: string  
Default: ""

parameter      Parameter to print  
Type: string  
Default: No Default

time\_step      Time Step label  
Type: string  
Default: ""



write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

years      Years to print the estimable for  
Type: non-negative integer vector  
Default: No Default

#### **11.1.7. @report[label].type=estimate\_summary**

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### **11.1.8. @report[label].type=estimate\_value**

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### **11.1.9. @report[label].type=initialisation\_partition**

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.10. @report[label].type=mcmc\_covariance

file\_name      File Name

Type: string

Default: ""

write\_mode      Write mode

Type: string

Default: overwrite

Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.11. @report[label].type=mcmc\_objective

file\_name      File Name

Type: string

Default: ""

write\_mode      Write mode

Type: string

Default: overwrite

Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.12. @report[label].type=mcmc\_sample

file\_name      File Name

Type: string

Default: ""

write\_mode      Write mode

Type: string

Default: overwrite

Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.13. @report[label].type=m.p.d

file\_name      File Name

Type: string

Default: ""

write\_mode      Write mode

Type: string

Default: overwrite

Allowed Values: overwrite, append, incremental\_suffix

**11.1.14. @report [label] .type=objective\_function**

file\_name      File Name

Type: string

Default: ""

write\_mode      Write mode

Type: string

Default: overwrite

Allowed Values: overwrite, append, incremental\_suffix

**11.1.15. @report [label] .type=observation**

file\_name      File Name

Type: string

Default: ""

observation      Observation label

Type: string

Default: No Default

write\_mode      Write mode

Type: string

Default: overwrite

Allowed Values: overwrite, append, incremental\_suffix

**11.1.16. @report [label] .type=output\_parameters**

file\_name      File Name

Type: string

Default: ""

write\_mode      Write mode

Type: string

Default: overwrite

Allowed Values: overwrite, append, incremental\_suffix

**11.1.17. @report [label] .type=partition**

file\_name      File Name

Type: string

Default: ""

time\_step      Time Step label

    Type: string

    Default: ""

write\_mode      Write mode

    Type: string

    Default: overwrite

    Allowed Values: overwrite, append, incremental\_suffix

years          Years

    Type: non-negative integer vector

    Default: true

#### 11.1.18. @report[label].type=partition\_biomass

file\_name      File Name

    Type: string

    Default: ""

time\_step      Time Step label

    Type: string

    Default: ""

units          Units (Default Kgs

    Type: string

    Default: kgs

write\_mode      Write mode

    Type: string

    Default: overwrite

    Allowed Values: overwrite, append, incremental\_suffix

years          Years

    Type: non-negative integer vector

    Default: true

#### 11.1.19. @report[label].type=partition\_mean\_weight

file\_name      File Name

    Type: string

    Default: ""

time\_step      Time Step label

Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

years      Years  
Type: non-negative integer vector  
Default: true

#### **11.1.20. @report [label] .type=process**

file\_name      File Name  
Type: string  
Default: ""

process      Process label that is reported  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### **11.1.21. @report [label] .type=random\_number\_seed**

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### **11.1.22. @report [label] .type=selectivity**

file\_name      File Name  
Type: string  
Default: ""

selectivity      Selectivity name  
Type: string  
Default: No Default

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.23. @report [label] .type=simulated\_observation

file\_name      File Name  
Type: string  
Default: ""

observation      Observation label  
Type: string  
Default: No Default

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.24. @report [label] .type=standard\_header

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode  
Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

#### 11.1.25. @report [label] .type=time\_varying

file\_name      File Name  
Type: string  
Default: ""

write\_mode      Write mode

---

Type: string  
Default: overwrite  
Allowed Values: overwrite, append, incremental\_suffix

## 12. Other commands and subcommands

**@include** *file*    Include an external file

*file*    The name of the external file to include

Type: string

Default: No default

Value: A valid external file

Condition: The file name must be enclosed in double quotes

Example: @include "my\_file.txt"

Note: @include does not denote the end of the previous command block as is the case for all other commands





---

## 13. Examples

### 13.1. An example of a simple model

This example implements a very simple single species and area model, with recruitment, maturation, natural and fishing mortality, and an annual age increment. The population structure has ages 1 – 30<sup>+</sup> with a single category.

CASAL2 default file to search for in your current working directory is `casal2.txt`. In this example, `casal2.txt` specifies all the files necessary to run your CASAL2 model from your current working directory. This is done using the `!include` command as follows.

```
!include "population.csl2"
!include "reports.csl2"
!include "Observation.csl2"
!include "estimation.csl2"
```

Breaking up a CASAL2 model into sections is recommended, as it aids in readability and error checking. `population.csl2` contains the population information. The model runs from 1975-2012 and is initialised over a 120 year period prior to 1975, which applies the following processes,

1. A Beverton-Holt recruitment process, recruiting a constant number of individuals to the first age class (i.e.,  $age = 1$ ).
2. A constant mortality process representing natural mortality( $M$ ). This process is repeated in all three time steps, so that each with its own time step proportion of  $M$  applied.
3. An ageing process, where all individuals are aged by one year, and with a plus group accumulator age class at  $age = 30$ .

Following initialisation, the model runs from the years 1975 to 2012 iterating through two time-steps. The first time-step applies processes of recruitment, and  $\frac{1}{2}M_1 + F + \frac{1}{2}M_1$  processes, where  $M_1$  is the proportion of  $M$  applied in the first time step. The exploitation process (fishing) is applied in the years 1975–2012. Catches are defined in the catches table and attribute information on each fishery such as selectivity and time-step they are implemented are in the fisheries table in the `@process` block.

The second time-step applies an age increment and the remaining natural mortality.

The first 28 lines of the main section of the `population.csl2` are,

```
## Model Block
@model
start_year 1975
final_year 2012
min_age 1
max_age 30
age_plus true
initialisation_phases iphase1
time_steps step1 step2

## Category Block
@categories
format
names stock
age_lengths age_size

## Initialisation block
@initialisation_phase iphase1
type iterative
years 120

## Annual Cycle definition
@time_step step1
processes Recruitment instant_mort

@time_step step2
processes Ageing instant_mort
```

To carry out a run of the model (to verify that the model runs without any syntax errors), use the command `casal2 -r`. Note that as CASAL2 looks for a file named `casal2.txt` by default, we can override this. Hypothetically speaking if our model was all written in `Mymodel.txt` we could call it using the `-c` command like `casal2 -r -c Mymodel.txt`.

To run an estimation, and hence estimate the parameters defined in the file `estimation.csl2` (the catchability constant  $q$ , recruitment  $R_0$ , and the selectivity parameters  $a_{50}$  and  $a_{t095}$ ), use `casal2 -e`. Here, we have piped the output to `estimate.log` using the command `casal2 -e > estimate.log`, reports the user defined reports `reports.csl2` from the final iteration of the estimation, and successful convergence printed to screen,

```
Total elapsed time: 1 second
Completed
```

The main part of the output from the estimation run is summarised in the file `estimate.log`, and the final MPD parameter values can be piped out as a separate report, in this case named `paramaters.out`, using the command `casal2 -e -o paramaters.out > estimate.log`.

A profile on the  $R_0$  parameter can also be run, using `casal2 -p > profile.log`. See the examples folder for an example of the output.

KATH note below, will be useful to copy that document across. Examples on Input file specification go to the file `Input File Specification.odt` found in `CASAL2/Documentation/Software Development`

### 13.2. In line declaration

In line declarations can help shorten models by passing @ blocks, for example

```
@observation chatCPUE
type biomass
```

```
catchability [q=6.52606e-005]
time_step one
categories male+female
selectivities chatFselMale chatFselFemale
likelihood lognormal
years 1992:2001
time_step_proportion 1.0
obs 1.50 1.10 0.93 1.33 1.53 0.90 0.68 0.75 0.57 1.23
error_value 0.35
```

```
@estimate
parameter catchability[chatTANbiomass.one].q
type uniform_log
lower_bound 1e-2
upper_bound 1
In line declaration tips
```

In the above code we are defining and estimating catchability without explicitly creating an `@catchability` block

When you do an inline declaration the new object will be created with the name of the creator's label.<index> where index will be the word if it's one-nine and the number if it's 10+, for example

```
@mortality halfm
selectivities [type=constant; c=1]
```

```
would create
@selectivity halfm.one
```

if there were 10 categories all with there own selectivity the 10<sup>th</sup> selectivity would be labelled;

```
@selectivity halfm.10
```



---

## 14. Post processing output using R

In the downloaded bundle is a R-package that reads CASAL2 output into R. The CASAL2 package has only one function `extract()`, which will read in the entire file. The output is written so that each @report will start with a '\*' and end with '\*end'. Users may wish to construct R or other package routines that read CASAL2output that identify and select individual reports in the output for post-processing.



---

## 15. Troubleshooting

### 15.1. Introduction

### 15.2. Reporting errors

When reporting a bug or problem to the CASAL2 development team at [casal@niwa.co.nz](mailto:casal@niwa.co.nz), please address the following points.

### 15.3. Guidelines for reporting a problem with CASAL2

1. Detail the version of CASAL2 are you using? e.g., CASAL2 v2016-06-03Microsoft Windows executable”
2. What operating system or environment are you using? e.g., “IBM-PC Intel CPU running Microsoft Windows 10 Enterprise, Service Pack 1”.
3. Give a brief one-line description of the problem, e.g., “a segmentation fault was reported”.
4. If the problem is reproducible, please list the exact steps required to cause it, remembering to include the relevant CASAL2 configuration file, other input files, and any out generated. Specify the *exact* command line arguments that were used, e.g., “Using the command `***. -* -*` reports a segmentation fault. The input configuration files are attached.”
5. If the problem is not reproducible (only happened once, or occasionally for no apparent reason), please describe the circumstances in which it occurred and the symptoms observed (but note it is much harder to reproduce and hence fix non-reproducible bugs, but if several reports are made over time that relate to the same thing, then this may help to track down the problem), e.g., “CASAL2 crashed, but I cannot reproduce how I did it. It seemed to be related to a local network crash but I cannot be sure.”
6. If the problem causes any error messages to appear, please give the *exact* text displayed, e.g., `segmentation fault (core dumped)`.
7. Remember to attach all relevant input and output files so that the problem can be reproduced (it can helpful to compress these into a single file). Without these, it is usually not possible to determine the cause of the problem, and we are unlikely to provide any assistance. Note that it is helpful to be as specific as possible when describing the problem.





---

## 16. Acknowledgements

We thank the developers of CASAL (Bull et al., 2012) for their ideas that led to the development of the CASAL2. The CASAL2 logo was designed by Ian Doonan and Erika Mackay (NIWA).

Much of the structure of CASAL2, equations, and documentation in this manual draw heavily on similar components of the fisheries population model CASAL (Bull et al., 2012) and the spatial model SPM (Dunn et al., 2015). We thank the authors of CASAL and SPM for their permission to use their work as the basis for parts of CASAL2 and allow the use of the definitions, concepts, and documentation.

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## 17. Quick reference

**@ageing\_error** *label*     Define an object type Ageing\_Error

*label*     Label

*type*     Type

**@ageing\_error[*label*].type=data**

**@ageing\_error[*label*].type=normal**

*cv*     CV for Misclassification matrix

*k*     TBA

**@ageing\_error[*label*].type=off\_by\_one**

*k*     The minimum age of fish which can be missclassified

*p1*     proprtion of misclassification up by a single age, i.e. Proportion of individuals at age 3 that are actually age 4

*p2*     proprtion of misclassification down by a single age

**@age\_length** *label*     Define an object type Age\_Length

*casal\_switch*     A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm

*cv\_first*     CV for the first age class

*cv\_last*     CV for last age class

*distribution*     TBA

*label*     Label

*time\_step\_proportions*     the proportion increase of age through the in each time step that corresponds to a length and thus weight increase

*type*     Type

**@age\_length[*label*].type=data**

*by\_length*     Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age

*casal\_switch*     A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm

*cv\_first*     CV for the first age class

*cv\_last*     CV for last age class

*distribution*     TBA

*external\_gaps*

*internal\_gaps*

*length\_weight*     TBA

*time\_step\_proportions*     the proportion increase of age through the in each time step that corresponds to a length and thus weight increase

**@age\_length[*label*].type=none**

*casal\_switch*     A switch to use CASAL Cumulative normal function, note CASAL2 uses the

recent BOOST function which differs from the previous CASAL algorithm

cv\_first CV for the first age class

cv\_last CV for last age class

distribution TBA

time\_step\_proportions the proportion increase of age through the in each time step that corresponds to a length and thus weight increase

**@age\_\_length[label].type=schnute**

a TBA

b TBA

by\_length TBA

casal\_switch A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm

cv\_first CV for the first age class

cv\_last CV for last age class

distribution TBA

length\_weight TBA

tau1 TBA

tau2 TBA

time\_step\_proportions the proportion increase of age through the in each time step that corresponds to a length and thus weight increase

y1 TBA

y2 TBA

**@age\_\_length[label].type=von\_bertalanffy**

by\_length Specifies if the linear interpolation of CV's is a linear function of mean length at age. Default is just by age

casal\_switch A switch to use CASAL Cumulative normal function, note CASAL2 uses the recent BOOST function which differs from the previous CASAL algorithm

cv\_first CV for the first age class

cv\_last CV for last age class

distribution TBA

k TBA

length\_weight TBA

linf TBA

t0 TBA

time\_step\_proportions the proportion increase of age through the in each time step that corresponds to a length and thus weight increase

**@catchability label** Define an object type Catchability

label Label

type

**@catchability[label].type=free**

q The catchability amount

**@derived\_quantity label** Define an object type Derived\_Quantity

categories The list of categories to use when calculating the derived quantity

---

label     **Label**  
time\_step\_proportion\_method  
selectivities     The list of selectivities to use when calculating the derived quantity. 1 per  
category  
time\_step     The time step to calculate the derived quantity after  
time\_step\_proportion  
type     **Type**

**@derived\_quantity[label].type=abundance**

categories     The list of categories to use when calculating the derived quantity  
time\_step\_proportion\_method  
selectivities     The list of selectivities to use when calculating the derived quantity. 1 per  
category  
time\_step     The time step to calculate the derived quantity after  
time\_step\_proportion

**@derived\_quantity[label].type=biomass**

categories     The list of categories to use when calculating the derived quantity  
time\_step\_proportion\_method  
selectivities     The list of selectivities to use when calculating the derived quantity. 1 per  
category  
time\_step     The time step to calculate the derived quantity after  
time\_step\_proportion

**@estimate label**     Define an object type Estimate

estimation\_phase     **TBA**  
label     **Label**  
lower\_bound     The lowest value the parameter is allowed to have  
mcmc     **TBA**  
parameter     The name of the variable to estimate in the model  
prior     The name of the prior to use for the parameter  
same     A list of parameters that are bound to the value of this estimate  
type     **Type**  
upper\_bound     The highest value the parameter is allowed to have

**@estimate[label].type=beta**

a     **A**  
b     **B**  
estimation\_phase     **TBA**  
lower\_bound     The lowest value the parameter is allowed to have  
mcmc     **TBA**  
mu     **Mu**  
parameter     The name of the variable to estimate in the model  
prior     The name of the prior to use for the parameter  
same     A list of parameters that are bound to the value of this estimate  
sigma     **Sigma**  
upper\_bound     The highest value the parameter is allowed to have

**@estimate[label].type=lognormal**

cv Cv  
estimation\_phase TBA  
lower\_bound The lowest value the parameter is allowed to have  
mcmc TBA  
mu Mu  
parameter The name of the variable to estimate in the model  
prior The name of the prior to use for the parameter  
same A list of parameters that are bound to the value of this estimate  
upper\_bound The highest value the parameter is allowed to have

**@estimate[label].type=normal**

cv Cv  
estimation\_phase TBA  
lower\_bound The lowest value the parameter is allowed to have  
mcmc TBA  
mu Mu  
parameter The name of the variable to estimate in the model  
prior The name of the prior to use for the parameter  
same A list of parameters that are bound to the value of this estimate  
upper\_bound The highest value the parameter is allowed to have

**@estimate[label].type=normal by stdev**

estimation\_phase TBA  
lower\_bound The lowest value the parameter is allowed to have  
mcmc TBA  
mu Mu  
parameter The name of the variable to estimate in the model  
prior The name of the prior to use for the parameter  
same A list of parameters that are bound to the value of this estimate  
sigma Sigma  
upper\_bound The highest value the parameter is allowed to have

**@estimate[label].type=normal log**

estimation\_phase TBA  
lower\_bound The lowest value the parameter is allowed to have  
mcmc TBA  
mu Mu  
parameter The name of the variable to estimate in the model  
prior The name of the prior to use for the parameter  
same A list of parameters that are bound to the value of this estimate  
sigma Sigma  
upper\_bound The highest value the parameter is allowed to have

**@estimate[label].type=uniform**

estimation\_phase TBA

---

lower\_bound     The lowest value the parameter is allowed to have  
mcmc     TBA  
parameter     The name of the variable to estimate in the model  
prior     The name of the prior to use for the parameter  
same     A list of parameters that are bound to the value of this estimate  
upper\_bound     The highest value the parameter is allowed to have

**@estimate[label].type=uniform\_log**

estimation\_phase     TBA  
lower\_bound     The lowest value the parameter is allowed to have  
mcmc     TBA  
parameter     The name of the variable to estimate in the model  
prior     The name of the prior to use for the parameter  
same     A list of parameters that are bound to the value of this estimate  
upper\_bound     The highest value the parameter is allowed to have  
**@initialisation\_phase label**     Define an object type Initialisation.Phase  
label     Label  
type     Type

**@initialisation\_phase[label].type=cinitial**

categories     List of categories to use

**@initialisation\_phase[label].type=derived**

casal\_initialisation\_switch     Reset the partition after running an extra annual cycle to take on equilibrium SSB's. Warning should only be set to true if comparing with previous CASAL models  
exclude\_processes     The processes to exclude from all time steps  
insert\_processes     The processes to insert in to target time steps

**@initialisation\_phase[label].type=iterative**

convergence\_years     The years to test for convergence  
exclude\_processes     The processes to exclude from all time steps  
insert\_processes     The processes to insert in to target time steps  
lambda     Lambda  
years     The number of iterations to execute this phase for

**@initialisation\_phase[label].type=state\_category\_by\_age**

categories     List of categories to use  
max\_age     Maximum age to use for this process  
min\_age     Minimum age to use for this process  
**@likelihood label**     Define an object type Likelihood  
label  
type

**@likelihood[label].type=binomial**

**@likelihood[label].type=binomial\_approx**

**@likelihood[label].type=dirichlet**

**@likelihood[label].type=log\_normal**

**@likelihood[label].type=log\_normal\_with\_q**

**@likelihood[label].type=multinomial**

**@likelihood[label].type=normal**

**@likelihood[label].type=pseudo**

**@derived\_quantity label** Define an object type `Derived_Quantity`

categories The list of categories to use when calculating the derived quantity

label Label

time\_step\_proportion\_method

selectivities The list of selectivities to use when calculating the derived quantity. 1 per

category

time\_step The time step to calculate the derived quantity after

time\_step\_proportion

type Type

**@derived\_quantity[label].type=abundance**

categories The list of categories to use when calculating the derived quantity

time\_step\_proportion\_method

selectivities The list of selectivities to use when calculating the derived quantity. 1 per

category

time\_step The time step to calculate the derived quantity after

time\_step\_proportion

**@derived\_quantity[label].type=biomass**

categories The list of categories to use when calculating the derived quantity

time\_step\_proportion\_method

selectivities The list of selectivities to use when calculating the derived quantity. 1 per

category

time\_step The time step to calculate the derived quantity after

time\_step\_proportion

**@mcmc label** Define an object type `MCMC`

active Is this the active MCMC algorithm

label Label

length The number of chain links to create

print\_default\_reports

type Type

**@mcmc[label].type=independence\_metropolis**

active Is this the active MCMC algorithm

adapt\_stepsize\_at Iterations in the chain to check and resize the MCMC stepsize

correlation\_adjustment\_diff TBA

covariance\_adjustment\_method Method for adjusting small variances in the covariance



---

proposal matrix  
df      Degrees of freedom of the multivariate t proposal distribution  
keep     Spacing between recorded values in the chain  
length    The number of chain links to create  
max\_correlation      Maximum absolute correlation in the covariance matrix of the proposal distribution  
print\_default\_reports  
proposal\_distribution      The shape of the proposal distribution (either t or normal  
start      Covariance multiplier for the starting point of the Markov chain  
step\_size      Initial stepsize (as a multiplier of the approximate covariance matrix  
**@minimiser label**      Define an object type Minimiser  
active      True if this minimiser is active  
covariance      True if a covariance matrix should be created  
label      Label  
type      Type of minimiser to use

**@minimiser[label].type=adolc**

active      True if this minimiser is active  
covariance      True if a covariance matrix should be created  
tolerance      Tolerance of the gradient for convergence  
evaluations      Maximum number of evaluations  
iterations      Maximum number of iterations  
step\_size      Minimum Step-size before minimisation fails

**@minimiser[label].type=beta.diff**

active      True if this minimiser is active  
covariance      True if a covariance matrix should be created  
tolerance      Tolerance of the gradient for convergence  
evaluations      Maximum number of evaluations  
iterations      Maximum number of iterations

**@minimiser[label].type=cppad**

active      True if this minimiser is active  
covariance      True if a covariance matrix should be created

**@minimiser[label].type=de\_solver**

active      True if this minimiser is active  
covariance      True if a covariance matrix should be created  
crossover\_probability      TBA  
difference\_scale      The scale to apply to new solutions when comparing candidates  
max\_generations      The maximum number of iterations to run  
method      The type of candidate generation method to use  
population\_size      The number of candidate solutions to have in the population  
tolerance      The total variance between the population and best candidate before acceptance

**@minimiser[label].type=d.lib**

active      True if this minimiser is active  
covariance      True if a covariance matrix should be created

**@minimiser[label].type=gamma\_diff**

active      True if this minimiser is active  
covariance      True if a covariance matrix should be created  
tolerance      Tolerance of the gradient for convergence  
evaluations      Maximum number of evaluations  
iterations      Maximum number of iterations  
step\_size      Minimum Step-size before minimisation fails  
**@model label**      Define an object type Model  
age\_plus      Define the oldest age as a plus group  
final\_year      Define the final year of the model, excluding years in the projection period  
initialisation\_phases      Define the labels of the phases of the initialisation  
label  
length\_bins  
max\_age      Maximum age of individuals in the population  
min\_age      Minimum age of individuals in the population  
projection\_final\_year      Define the final year of the model in projection mode  
start\_year      Define the first year of the model, immediately following initialisation  
time\_steps      Define the labels of the time steps, in the order that they are applied, to form the  
annual cycle  
type      Type of model (the partition structure). Either age, length or hybrid  
**@observation label**      Define an object type Observation  
categories      Category labels to use  
error\_value\_multiplier      Error value multiplier for likelihood  
label      Label  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      Type of likelihood to use  
simulation\_likelihood      Simulation likelihood to use  
type      Type of observation

**@observation[label].type=process\_abundance**

catchability      Abundance catchability

---

categories     Category labels to use  
delta     Delta value for error values  
error\_value\_multiplier     Error value multiplier for likelihood  
error\_value     The error values to use against the observation values  
likelihood\_multiplier     Likelihood score multiplier  
likelihood     Type of likelihood to use  
obs     Observation values  
process\_error     Process error  
process     Process label  
process\_proportion     Process proportion  
selectivities     Selectivity labels to use  
simulation\_likelihood     Simulation likelihood to use  
time\_step     Time step to execute in  
years     Years to execute in

**@observation[label].type=time\_step\_abundance**

catchability     TBA  
categories     Category labels to use  
delta     Delta value for error values  
error\_value\_multiplier     Error value multiplier for likelihood  
error\_value     The error values to use against the observation values  
likelihood\_multiplier     Likelihood score multiplier  
likelihood     Type of likelihood to use  
obs     Observation values  
process\_error     Process error  
selectivities     Selectivity labels to use  
simulation\_likelihood     Simulation likelihood to use  
time\_step     Time step to execute in  
time\_step\_proportion     Proportion through the time step to analyse the partition from  
years     Years to execute in

**@observation[label].type=process\_biomass**

catchability     Catchability of Biomass  
categories     Category labels to use  
delta     Delta value for error values  
error\_value\_multiplier     Error value multiplier for likelihood  
error\_value     The error values to use against the observation values  
likelihood\_multiplier     Likelihood score multiplier  
likelihood     Type of likelihood to use  
obs     Observation values  
process\_error     Process error  
process     Process label  
process\_proportion     Process proportion  
selectivities     Selectivity labels to use  
simulation\_likelihood     Simulation likelihood to use  
time\_step     Time step to execute in  
years     Years to execute in

**@observation[label].type=time\_step\_biomass**

catchability    Catchability of Biomass  
categories    Category labels to use  
delta    Delta value for error values  
error\_value\_multiplier    Error value multiplier for likelihood  
error\_value    The error values to use against the observation values  
likelihood\_multiplier    Likelihood score multiplier  
likelihood    Type of likelihood to use  
obs    Observation values  
process\_error    Process error  
selectivities    Selectivity labels to use  
simulation\_likelihood    Simulation likelihood to use  
time\_step    Time step to execute in  
time\_step\_proportion    Proportion through the time step to analyse the partition from  
years    Years to execute in

**@observation[label].type=process\_proportions\_at\_age**

age\_plus    Use age plus group  
ageing\_error    Label of ageing error to use  
categories    Category labels to use  
delta    Delta  
error\_value\_multiplier    Error value multiplier for likelihood  
likelihood\_multiplier    Likelihood score multiplier  
likelihood    Type of likelihood to use  
max\_age    Maximum age  
min\_age    Minimum age  
process\_errors    Process error  
process    Process label  
process\_proportion    Process proportion  
selectivities    Selectivity labels to use  
simulation\_likelihood    Simulation likelihood to use  
time\_step    Time step to execute in  
tolerance    Tolerance  
years    Year to execute in

**@observation[label].type=time\_step\_proportions\_at\_age**

age\_plus    Use age plus group

---

ageing\_error      Label of ageing error to use  
categories      Category labels to use  
delta      Delta  
error\_value\_multiplier      Error value multiplier for likelihood  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      Type of likelihood to use  
max\_age      Maximum age  
min\_age      Minimum age  
process\_errors      Process error  
selectivities      Selectivity labels to use  
simulation\_likelihood      Simulation likelihood to use  
time\_step      Time step to execute in  
time\_step\_proportion      Proportion through the time step to analyse the partition from  
tolerance      Tolerance  
years      Year to execute in

**@observation[label].type=proportions\_at\_age\_for\_fishery**

age\_plus      Use age plus group  
ageing\_error      Label of ageing error to use  
categories      Category labels to use  
delta      Delta  
error\_value\_multiplier      Error value multiplier for likelihood  
fishery      Label of fishery the observation is from  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      Type of likelihood to use  
max\_age      Maximum age  
min\_age      Minimum age  
process\_errors      Process error  
process      Process label  
simulation\_likelihood      Simulation likelihood to use  
time\_step      Time steps that the fisheries are in  
tolerance      Tolerance  
years      Year to execute in

**@observation[label].type=process\_proportions\_at\_length**

categories      Category labels to use

delta      **Delta**  
error\_value\_multiplier      Error value multiplier for likelihood  
length\_bins      **Length bins**  
length\_plus\_group      Is the last bin a plus group  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      **Type of likelihood to use**  
process\_errors      Process error  
process      **Process label**  
process\_proportion      Process proportion  
selectivities      Selectivity labels to use  
simulation\_likelihood      Simulation likelihood to use  
time\_step      Time step to execute in  
tolerance      Tolerance for rescaling proportions  
years      Year to execute in

**@observation[label].type=time\_step\_proportions\_at\_length**

categories      Category labels to use  
delta      **Delta**  
error\_value\_multiplier      Error value multiplier for likelihood  
length\_bins      **Length bins**  
length\_plus\_group      Is the last bin a plus group  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      **Type of likelihood to use**  
process\_errors      Process error  
selectivities      Selectivity labels to use  
simulation\_likelihood      Simulation likelihood to use  
time\_step      Time step to execute in  
time\_step\_proportion      Proportion through the time step to analyse the partition from  
tolerance      Tolerance for rescaling proportions  
years      Year to execute in

**@observation[label].type=proportions\_at\_length\_for\_fishery**

categories      Category labels to use  
delta      **Delta**  
error\_value\_multiplier      Error value multiplier for likelihood  
fishery      **Label of fishery the observation is from**  
length\_bins      **Length bins**  
length\_plus\_group      Is the last bin a plus group  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      **Type of likelihood to use**  
process\_errors      Process error  
process      **Process label**  
process\_proportion      Process proportion  
simulation\_likelihood      Simulation likelihood to use  
time\_step      Time step to execute in  
tolerance      Tolerance for rescaling proportions  
years      Year to execute in

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**@observation[label].type=process\_proportions\_by\_category**

age\_plus      Use age plus group  
categories    Category labels to use  
delta        Delta  
error\_value\_multiplier    Error value multiplier for likelihood  
likelihood\_multiplier    Likelihood score multiplier  
likelihood    Type of likelihood to use  
max\_age      Maximum age  
min\_age      Minimum age  
process\_errors    Process error  
process       Process label  
process\_proportion    Process proportion  
selectivities    Selectivity labels to use  
simulation\_likelihood    Simulation likelihood to use  
categories2    Target Categories  
selectivities2    Target Selectivities  
time\_step    Time step to execute in  
years        Year to execute in

**@observation[label].type=time\_step\_proportions\_by\_category**

age\_plus      Use age plus group  
categories    Category labels to use  
delta        Delta  
error\_value\_multiplier    Error value multiplier for likelihood  
likelihood\_multiplier    Likelihood score multiplier  
likelihood    Type of likelihood to use  
max\_age      Maximum age  
min\_age      Minimum age  
process\_errors    Process error  
selectivities    Selectivity labels to use  
simulation\_likelihood    Simulation likelihood to use  
categories2    Target Categories  
selectivities2    Target Selectivities  
time\_step    Time step to execute in  
time\_step\_proportion    Proportion through the time step to analyse the partition from  
years        Year to execute in

**@observation[label].type=proportions\_migrating**

age\_plus      Use age plus group

ageing\_error      Label of ageing error to use  
categories      Category labels to use  
delta      Delta  
error\_value\_multiplier      Error value multiplier for likelihood  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      Type of likelihood to use  
max\_age      Maximum age  
min\_age      Minimum age  
process\_errors      Process error  
process      Process label  
process\_proportion      Process proportion  
simulation\_likelihood      Simulation likelihood to use  
time\_step      Time step to execute in  
years      Year to execute in

**@observation[label].type=tag\_recapture\_by\_age**

age\_plus      Use age plus group  
categories      Category labels to use  
delta      Delta  
detection      Detection probability  
error\_value\_multiplier      Error value multiplier for likelihood  
likelihood\_multiplier      Likelihood score multiplier  
likelihood      Type of likelihood to use  
max\_age      Maximum age  
min\_age      Minimum age  
process\_errors      Process error  
selectivities      Selectivity labels to use  
simulation\_likelihood      Simulation likelihood to use  
categories2      Target Categories  
selectivities2      Target Selectivities  
time\_step      Time step to execute in  
time\_step\_proportion      Proportion through the time step to analyse the partition from  
years      Year to execute in

**@observation[label].type=tag\_recapture\_by\_length**

categories      Category labels to use



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delta      **Delta**  
detection      **Detection probability**  
error\_value\_multiplier      **Error value multiplier for likelihood**  
length.bins      **Length Bins**  
likelihood\_multiplier      **Likelihood score multiplier**  
likelihood      **Type of likelihood to use**  
plus\_group      **Last length bin a plus group**  
process\_errors      **Process error**  
selectivities      **Selectivity labels to use**  
simulation\_likelihood      **Simulation likelihood to use**  
categories2      **Target Categories**  
selectivities2      **Target Selectivities**  
time\_step      **Time step to execute in**  
time\_step\_proportion      **Proportion through the time step to analyse the partition from**  
years      **Year to execute in**  
**@penalty** *label*      **Define an object type Penalty**  
  
label      **Label**  
type      **Type**

**@penalty[label].type=process**

log\_scale      **Log scale**  
multiplier      **Multiplier**  
**@process** *label*      **Define an object type Process**  
  
print\_report      **Generate parameter report**  
label      **Label**  
type      **Type**

**@process[label].type=ageing**

categories      **Categories**  
print\_report      **Generate parameter report**

**@process[label].type=growth**

print\_report      **Generate parameter report**

**@process[label].type=maturation**

print\_report      **Generate parameter report**  
from      **List of categories to mature from**  
rates      **The rates to mature for each year**  
selectivities      **List of selectivities to use for maturation**  
to      **List of categories to mature too**  
years      **The years to be associated with rates**

**@process[label].type=mortality\_constant\_rate**

categories      **List of categories**

print\_report    Generate parameter report  
m    Mortality rates  
time\_step\_ratio    Time step ratios for M  
selectivities    Selectivities

**@process[label].type=mortality\_event**

catches    Catches  
categories    Categories  
print\_report    Generate parameter report  
penalty    Penalty label  
selectivities    List of selectivities  
u\_max    U Max  
years    Years

**@process[label].type=mortality\_event\_biomass**

catches    Catches for each year  
categories    Category labels  
print\_report    Generate parameter report  
penalty    Penalty label  
selectivities    Selectivity labels  
u\_max    U Max  
units    Unit of weight that the Catches table are expressed in  
years    Years to apply mortality

**@process[label].type=mortality\_holling\_rate**

a    parameter a  
b    parameter b  
print\_report    Generate parameter report  
penalty    Label of penalty to be applied  
predator\_categories    Predator Categories labels  
predator\_selectivities    Selectivities for predator categories  
prey\_categories    Prey Categories labels  
prey\_selectivities    Selectivities for prey categories  
u\_max    Umax  
x    parameter x  
years    Year to execute in

**@process[label].type=mortality\_instantaneous**

categories    Categories for natural mortality  
print\_report    Generate parameter report  
m    Mortality rates  
selectivities    Selectivities for Natural Mortality  
time\_step\_ratio    Time step ratios for M  
units    Unit of weight that the Catches table are expressed in

**@process[label].type=mortality\_prey\_suitability**

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consumption\_rate    Predator consumption rate  
 print\_report        Generate parameter report  
 electivities        Prey Electivities  
 penalty            Label of penalty to be applied  
 predator\_categories    Predator Categories labels  
 predator\_selectivities    Selectivities for predator categories  
 prey\_categories      Prey Categories labels  
 prey\_selectivities    Selectivities for prey categories  
 u\_max              Umax  
 years              Year that process occurs

**@process[label].type=nop**

print\_report        Generate parameter report

**@process[label].type=recruitment\_beverton\_holt**

age            Age to recruit at  
 b0            B0  
 units        Units of B0, if initialising model using B0  
 categories    Category labels  
 print\_report    Generate parameter report  
 b0\_initialisation\_phase    Initialisation phase Label that b0 is from  
 prior\_standardised\_ycs    Priors for year class strength on ycs values (not standardised ycs values)  
 proportions    Proportions  
 r0            R0  
 ssb          SSB Label (derived quantity)  
 ssb\_offset    Spawning biomass year offset  
 standardise\_ycs\_years    Years that are included for year class standardisation  
 steepness    Steepness  
 ycs\_values    YCS Values

**@process[label].type=recruitment\_constant**

age            Age  
 categories    Categories  
 print\_report    Generate parameter report  
 proportions    Proportions  
 r0            R0

**@process[label].type=tag\_by\_age**

print\_report        Generate parameter report

from     Categories to transition from  
initial\_mortality  
initial\_mortality\_selectivity  
loss\_rate  
loss\_rate\_selectivities  
max\_age     Maximum age to transition  
min\_age     Minimum age to transition  
n  
penalty     Penalty label  
selectivities  
to     Categories to transition to  
u\_max     U Max  
years     Years to execute the transition in

**@process[label].type=tag\_by\_length**

print\_report     Generate parameter report  
from     Categories to transition from  
initial\_mortality  
initial\_mortality\_selectivity  
maximum\_length     The upper length when there is no plus group  
n  
penalty     Penalty label  
plus\_group     Use plus group for last length bin  
selectivities  
to     Categories to transition to  
u\_max     U Max  
years     Years to execute the transition in

**@process[label].type=tag\_loss**

categories     List of categories  
print\_report     Generate parameter report  
time\_step\_ratio     Time step ratios for Tag Loss  
selectivities     Selectivities  
tag\_loss\_rate     Tag Loss rates  
tag\_loss\_type     Type of tag loss  
year     The year the first tagging release process was executed

**@process[label].type=transition\_category**

print\_report     Generate parameter report  
from     From  
proportions     Proportions  
selectivities     Selectivity names  
to     To

**@process[label].type=transition\_category\_by\_age**

print\_report     Generate parameter report

---

from      Categories to transition from  
max\_age    Maximum age to transition  
min\_age    Minimum age to transition  
penalty    Penalty label  
to      Categories to transition to  
u\_max      U Max  
years      Years to execute the transition in  
**@profile** *label*      Define an object type Profile  
  
label      Label  
lower\_bound    The lower bounds  
parameter    The system parameter to profile  
steps      The number of steps to take between the lower and upper bound  
type  
upper\_bound    The upper bounds  
**@report** *label*      Define an object type Report  
  
file\_name    File Name  
label      Label  
type      Type  
write\_mode    Write mode

**@report [label] .type=ageing\_error\_matrix**

ageing\_error    Ageing Error label  
file\_name    File Name  
write\_mode    Write mode

**@report [label] .type=category\_info**

file\_name    File Name  
write\_mode    Write mode

**@report [label] .type=category\_list**

file\_name    File Name  
write\_mode    Write mode

**@report [label] .type=covariance\_matrix**

file\_name    File Name  
write\_mode    Write mode

**@report [label] .type=derived\_quantity**

file\_name    File Name  
units      Unit of weight output expressed in  
write\_mode    Write mode

**@report [label] .type=estimable**

file\_name    File Name

parameter     Parameter to print  
time\_step     Time Step label  
write\_mode     Write mode  
years     Years to print the estimable for

**@report[label].type=estimate\_summary**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=estimate\_value**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=initialisation\_partition**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=mcmc\_covariance**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=mcmc\_objective**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=mcmc\_sample**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=m\_p\_d**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=objective\_function**

file\_name     File Name  
write\_mode     Write mode

**@report[label].type=observation**

file\_name     File Name  
observation     Observation label  
write\_mode     Write mode

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**@report[label].type=output\_parameters**

file\_name     File Name  
write\_mode    Write mode

**@report[label].type=partition**

file\_name     File Name  
time\_step     Time Step label  
write\_mode    Write mode  
years        Years

**@report[label].type=partition\_biomass**

file\_name     File Name  
time\_step     Time Step label  
units        Units (Default Kgs  
write\_mode    Write mode  
years        Years

**@report[label].type=partition\_mean\_weight**

file\_name     File Name  
time\_step     Time Step label  
write\_mode    Write mode  
years        Years

**@report[label].type=process**

file\_name     File Name  
process       Process label that is reported  
write\_mode    Write mode

**@report[label].type=random\_number\_seed**

file\_name     File Name  
write\_mode    Write mode

**@report[label].type=selectivity**

file\_name     File Name  
selectivity    Selectivity name  
write\_mode    Write mode

**@report[label].type=simulated\_observation**

file\_name     File Name  
observation    Observation label  
write\_mode    Write mode

**@report[label].type=standard\_header**

file\_name     File Name  
write\_mode    Write mode

**@report[label].type=time\_varying**

file\_name     File Name  
write\_mode    Write mode

**@selectivity label**     Define an object type Selectivity

label     Label  
length\_based     Is the selectivity length based  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
type     Type

**@selectivity[label].type=all\_values**

length\_based     Is the selectivity length based  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
v     V

**@selectivity[label].type=all\_values\_bounded**

h     H  
length\_based     Is the selectivity length based  
l     L  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
v     V

**@selectivity[label].type=constant**

c     C  
length\_based     Is the selectivity length based  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution

**@selectivity[label].type=double\_exponential**

alpha     Alpha  
length\_based     Is the selectivity length based  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
x0     X0  
x1     X1  
x2     X2  
y0     Y0  
y1     Y1  
y2     Y2



---

**@selectivity[label].type=double\_normal**

alpha     Alpha  
length\_based     Is the selectivity length based  
mu     Mu  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
sigma\_l     Sigma L  
sigma\_r     Sigma R

**@selectivity[label].type=increasing**

alpha     Alpha  
h     High  
length\_based     Is the selectivity length based  
l     Low  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution  
v     V

**@selectivity[label].type=inverse\_logistic**

a50     A50  
alpha     Alpha  
ato95     aTo95  
length\_based     Is the selectivity length based  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution

**@selectivity[label].type=knife\_edge**

alpha     Alpha  
e     Edge  
length\_based     Is the selectivity length based  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution

**@selectivity[label].type=logistic**

a50     A50  
alpha     Alpha  
ato95     Ato95  
length\_based     Is the selectivity length based  
intervals     Number of quantiles to evaluate a length based selectivity over the age length  
distribution

**@selectivity[label].type=logistic\_producing**

a50     A50

alpha     Alpha  
ato95     Ato95  
h     High  
length\_based     Is the selectivity length based  
l     Low  
intervals     Number of quantiles to evaluate a length based selectivity over the age length distribution  
**@length\_weight** *label*     Define an object type Length\_Weight  
label     Label  
type     Type

**@length\_weight[label].type=basic**

a     A  
b     B  
units     Units of measure (tonnes, kgs, grams)

**@length\_weight[label].type=none**

**@time\_step** *label*     Define an object type Time\_Step  
label     Label  
processes     Processes  
type

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