```
In [1]: from keras.utils import np_utils from keras.datasets import mnist import seaborn as sns from keras.initializers import he_normal import matplotlib.pyplot as plt import numpy as np import time from keras.layers.normalization import BatchNormalization from keras.optimizers import Adam from keras.optimizers import KerasClassifier from keras.wrappers.scikit_learn import KerasClassifier from keras.models import Sequential from keras.models import Sequential from keras.layers import Dense, Activation,Dropout #from pactools.grid_search import GridSearchCVProgressBar
```

Using TensorFlow backend.

```
In [0]: # https://gist.github.com/greydanus/f6eee59eaf1d90fcb3b534a25362cea4

def plt_dynamic(x, vy, ty, ax, colors=['b']):
    ax.plot(x, vy, 'b', label="Validation Loss")
    ax.plot(x, ty, 'r', label="Train Loss")
    plt.legend()
    plt.grid(linestyle='-')
    fig.canvas.draw()
```

Load the data

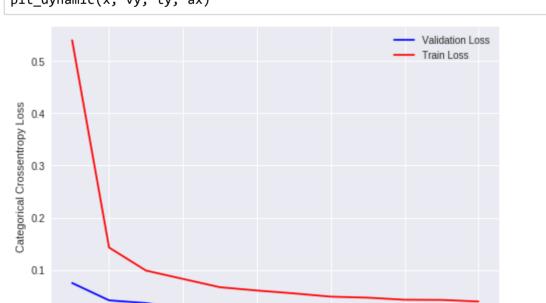
```
In [3]: # Credits: https://github.com/keras-team/keras/blob/master/examples/mnist_cnn.py
        from __future__ import print_function
        import keras
        from keras.datasets import mnist
        from keras.models import Sequential
        from keras.layers import Dense, Dropout, Flatten
        from keras.layers import Conv2D, MaxPooling2D
        from keras import backend as K
        batch_size = 120
        num_classes = 10
        epochs = 12
        # input image dimensions
        img_rows, img_cols = 28, 28
        # the data, split between train and test sets
        (x_train, y_train), (x_test, y_test) = mnist.load_data()
        if K.image_data_format() == 'channels_first':
           x_train = x_train.reshape(x_train.shape[0], 1, img_rows, img_cols)
           x_test = x_test.reshape(x_test.shape[0], 1, img_rows, img_cols)
           input_shape = (1, img_rows, img_cols)
        else:
           x_train = x_train.reshape(x_train.shape[0], img_rows, img_cols, 1)
           x_test = x_test.reshape(x_test.shape[0], img_rows, img_cols, 1)
           input_shape = (img_rows, img_cols, 1)
        x_train = x_train.astype('float32')
        x_test = x_test.astype('float32')
        x_train /= 255
        x_test /= 255
        print('The shape of train data is', x_train.shape)
        print(x_train.shape[0], 'train samples')
        print(x_test.shape[0], 'test samples')
       Downloading data from https://s3.amazonaws.com/img-datasets/mnist.npz (https://s3.amazonaws.com/img-datasets/mnist.npz)
       The shape of train data is (60000, 28, 28, 1)
       60000 train samples
```

3 Convolutional layers

With a ConvNet of (3, 3)

10000 test samples

```
In [9]: # convert class vectors to binary class matrices
     from keras.initializers import he_normal
     from keras.optimizers import Adam
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     model = Sequential()
     model.add(Conv2D(32, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal(), input_shape=input_shape))
     model.add(MaxPooling2D(pool size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(Dropout(0.5))
     model.add(BatchNormalization())
     model.add(Dense(num_classes, activation='softmax'))
     model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
     model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
     model_scores = model.evaluate(x_test, y_test, verbose=0)
     print('Test loss:', model_scores[0])
     print('Test accuracy:', model_scores[1])
     Train on 60000 samples, validate on 10000 samples
     Epoch 1/12
     Epoch 2/12
     Epoch 3/12
     Epoch 4/12
     Epoch 5/12
     Epoch 6/12
     Epoch 7/12
     Epoch 8/12
     Epoch 9/12
     Epoch 10/12
     Epoch 11/12
     Test loss: 0.018514532477124885
     Test accuracy: 0.9946
In [11]: import matplotlib.pyplot as plt
     fig,ax = plt.subplots(1,1)
     ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
     # list of epoch numbers
     x = list(range(1, epochs+1))
     vy = model_fit.history['val_loss']
     ty = model_fit.history['loss']
     plt_dynamic(x, vy, ty, ax)
```



6

10

Observations: This plot seems to perform good, no signs of overfit.

0.0

```
In [12]: import matplotlib.pyplot as plt
         import seaborn as sns
         w_after = model.get_weights()
         h1_w = w_after[0].flatten().reshape(-1,1)
         h2_w = w_after[2].flatten().reshape(-1,1)
         h3_w = w_after[4].flatten().reshape(-1,1)
         out_w = w_after[6].flatten().reshape(-1,1)
         fig = plt.figure(figsize = (15,6))
         plt.title("Weight matrices after model trained")
         plt.subplot(1, 4, 1)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h1_w,color='b')
         plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 4, 2)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h2_w, color='r')
         plt.xlabel('Hidden Layer 2 ')
         plt.subplot(1, 4, 3)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h3_w, color='g')
         plt.xlabel('Hidden Layer 3 ')
         plt.subplot(1, 4, 4)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=out_w,color='y')
         plt.xlabel('Output Layer ')
         plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)

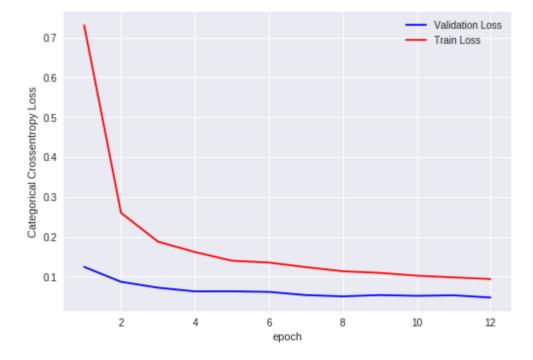
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use. violin_data = remove_na(group_data)



With a ConvNet of (5, 5)

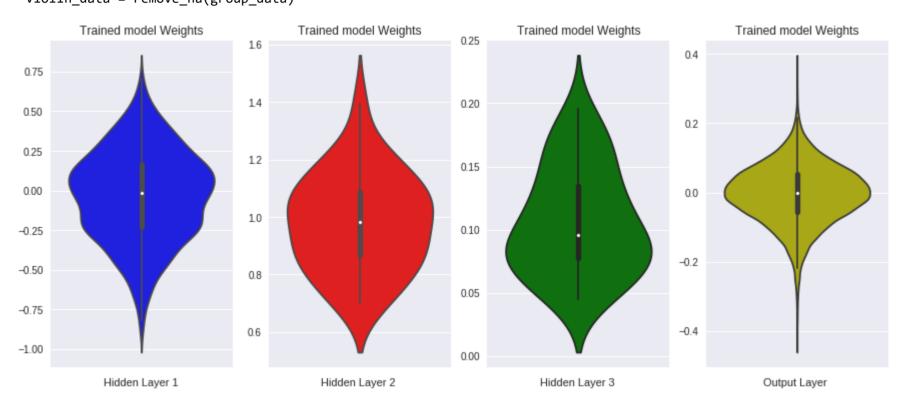
```
Various CNN networks on MNIST
In [16]: # convert class vectors to binary class matrices
     from keras.initializers import he_normal
     from keras.optimizers import Adam
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     model = Sequential()
     model.add(Conv2D(32, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(Dropout(0.5))
     model.add(BatchNormalization())
     model.add(Dense(num_classes, activation='softmax'))
     model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
     model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
     model_scores = model.evaluate(x_test, y_test, verbose=0)
     print('Test loss:', model_scores[0])
     print('Test accuracy:', model_scores[1])
     Train on 60000 samples, validate on 10000 samples
     Epoch 1/12
     Epoch 2/12
     Epoch 3/12
     Epoch 4/12
     Epoch 5/12
     Epoch 6/12
     Epoch 7/12
     Epoch 8/12
     Epoch 9/12
     Epoch 10/12
     Epoch 11/12
     Epoch 12/12
     Test loss: 0.04791659092535265
     Test accuracy: 0.9874
     fig,ax = plt.subplots(1,1)
     ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
     # list of epoch numbers
     x = list(range(1, epochs+1))
     vy = model_fit.history['val_loss']
     ty = model_fit.history['loss']
```





```
In [18]: import matplotlib.pyplot as plt
          import seaborn as sns
          w_after = model.get_weights()
          h1_w = w_after[0].flatten().reshape(-1,1)
          h2_w = w_after[2].flatten().reshape(-1,1)
         h3_w = w_after[4].flatten().reshape(-1,1)
          out_w = w_after[6].flatten().reshape(-1,1)
          fig = plt.figure(figsize = (15,6))
          plt.title("Weight matrices after model trained")
          plt.subplot(1, 4, 1)
          plt.title("Trained model Weights")
          ax = sns.violinplot(y=h1_w,color='b')
          plt.xlabel('Hidden Layer 1')
          plt.subplot(1, 4, 2)
          plt.title("Trained model Weights")
          ax = sns.violinplot(y=h2_w, color='r')
          plt.xlabel('Hidden Layer 2 ')
          plt.subplot(1, 4, 3)
          plt.title("Trained model Weights")
          ax = sns.violinplot(y=h3_w, color='g')
          plt.xlabel('Hidden Layer 3 ')
          plt.subplot(1, 4, 4)
          plt.title("Trained model Weights")
          ax = sns.violinplot(y=out_w,color='y')
          plt.xlabel('Output Layer ')
          plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use. violin data = remove_na(group_data)



Without Batch Normalization

```
In [24]: | # convert class vectors to binary class matrices
     from keras.initializers import he normal
     from keras.optimizers import Adam
    y_train = keras.utils.to_categorical(y_train, num_classes)
    y_test = keras.utils.to_categorical(y_test, num_classes)
    model = Sequential()
     model.add(Conv2D(32, (7, 7), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
    model.add(MaxPooling2D(pool_size=(2, 2)))
    model.add(Dropout(0.25))
     model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(Dropout(0.25))
     model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(Dropout(0.5))
    model.add(Dense(num_classes, activation='softmax'))
    model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
    model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
    model_scores = model.evaluate(x_test, y_test, verbose=0)
    print('Test loss:', model_scores[0])
    print('Test accuracy:', model_scores[1])
    Train on 60000 samples, validate on 10000 samples
    Epoch 1/12
    Epoch 2/12
    Epoch 3/12
    Epoch 4/12
    Epoch 5/12
    Epoch 6/12
    Epoch 7/12
    Epoch 8/12
    Epoch 9/12
    Epoch 10/12
    Epoch 11/12
    Epoch 12/12
```

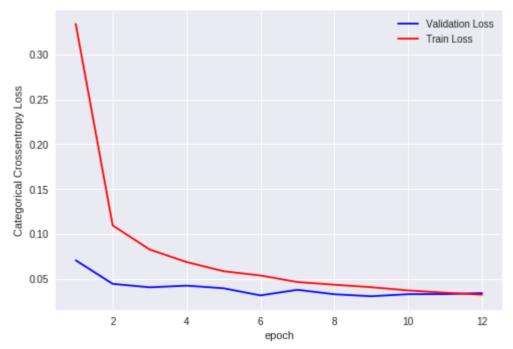
Test loss: 0.03397312323795263

Test accuracy: 0.9902

```
In [25]: import matplotlib.pyplot as plt
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')

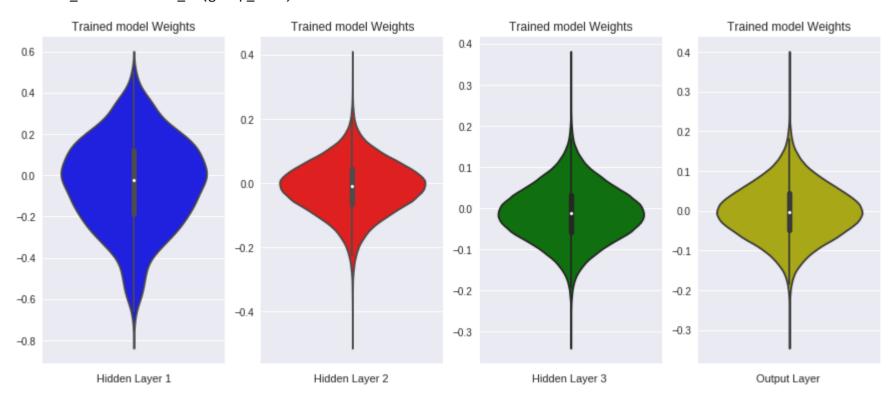
# List of epoch numbers
x = list(range(1, epochs+1))

vy = model_fit.history['val_loss']
ty = model_fit.history['loss']
plt_dynamic(x, vy, ty, ax)
```



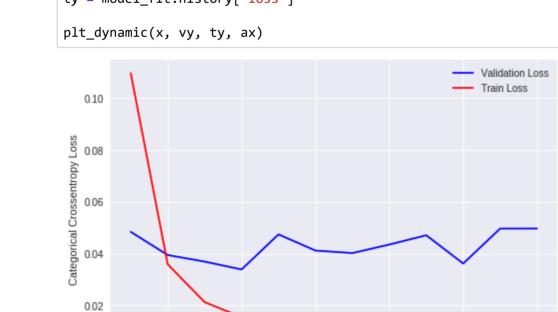
```
In [26]: import matplotlib.pyplot as plt
         import seaborn as sns
         w_after = model.get_weights()
         h1_w = w_after[0].flatten().reshape(-1,1)
         h2_w = w_after[2].flatten().reshape(-1,1)
         h3_w = w_after[4].flatten().reshape(-1,1)
         out_w = w_after[6].flatten().reshape(-1,1)
          fig = plt.figure(figsize = (15,6))
          plt.title("Weight matrices after model trained")
          plt.subplot(1, 4, 1)
         plt.title("Trained model Weights")
          ax = sns.violinplot(y=h1_w,color='b')
          plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 4, 2)
         plt.title("Trained model Weights")
          ax = sns.violinplot(y=h2_w, color='r')
          plt.xlabel('Hidden Layer 2 ')
          plt.subplot(1, 4, 3)
         plt.title("Trained model Weights")
          ax = sns.violinplot(y=h3_w, color='g')
          plt.xlabel('Hidden Layer 3 ')
          plt.subplot(1, 4, 4)
          plt.title("Trained model Weights")
          ax = sns.violinplot(y=out_w,color='y')
          plt.xlabel('Output Layer ')
          plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use. violin_data = remove_na(group_data)



Without Dropouts

```
Various CNN networks on MNIST
In [4]: # convert class vectors to binary class matrices
    from keras.initializers import he_normal
    from keras.optimizers import Adam
    y_train = keras.utils.to_categorical(y_train, num_classes)
    y_test = keras.utils.to_categorical(y_test, num_classes)
    model = Sequential()
    model.add(Conv2D(32, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
    model.add(MaxPooling2D(pool_size=(2, 2)))
    model.add(BatchNormalization())
    model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Flatten())
    model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Dense(num_classes, activation='softmax'))
    model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
    model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
    model_scores = model.evaluate(x_test, y_test, verbose=0)
    print('Test loss:', model_scores[0])
    print('Test accuracy:', model_scores[1])
    Train on 60000 samples, validate on 10000 samples
    Epoch 1/12
    Epoch 2/12
    Epoch 3/12
    Epoch 4/12
    Epoch 5/12
    Epoch 6/12
    Epoch 7/12
    Epoch 8/12
    Epoch 9/12
    Epoch 10/12
    Epoch 11/12
    Epoch 12/12
    Test loss: 0.049707786166346975
    Test accuracy: 0.9876
In [5]: import matplotlib.pyplot as plt
    fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
    # list of epoch numbers
    x = list(range(1, epochs+1))
    vy = model_fit.history['val_loss']
    ty = model_fit.history['loss']
    plt_dynamic(x, vy, ty, ax)
```



epoch

10

12

0.00

2

```
In [6]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        out_w = w_after[6].flatten().reshape(-1,1)
        fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 4, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 4, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 4, 3)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 4, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.

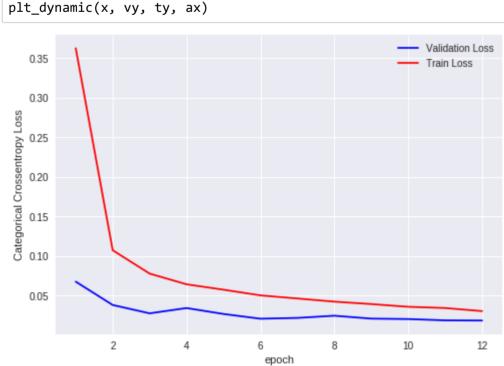
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use. violin_data = remove_na(group_data)



5 Convolutional layers

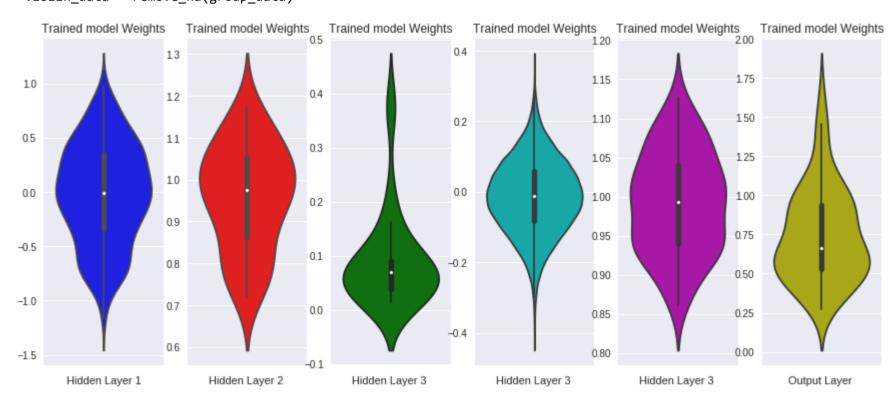
With a ConvNet of (3, 3)

```
Various CNN networks on MNIST
In [0]: # convert class vectors to binary class matrices
     from keras.initializers import he_normal
     from keras.optimizers import Adam
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     model = Sequential()
     model.add(Conv2D(32, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal(), input_shape=input_shape))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(Dropout(0.5))
     model.add(BatchNormalization())
     model.add(Dense(num_classes, activation='softmax'))
     model.compile(loss= 'categorical crossentropy', optimizer= 'Adam', metrics=['accuracy'])
     model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
     model_scores = model.evaluate(x_test, y_test, verbose=0)
     print('Test loss:', model_scores[0])
     print('Test accuracy:', model_scores[1])
    Train on 60000 samples, validate on 10000 samples
     Epoch 1/12
     Epoch 2/12
     Epoch 3/12
     Epoch 4/12
     Epoch 5/12
     Epoch 6/12
     Epoch 7/12
     Epoch 8/12
     Epoch 9/12
     Epoch 10/12
     Epoch 11/12
     Epoch 12/12
     Test loss: 0.01859951108721252
    Test accuracy: 0.9947
In [0]: import matplotlib.pyplot as plt
     fig,ax = plt.subplots(1,1)
     ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
     # list of epoch numbers
     x = list(range(1, epochs+1))
     vy = model_fit.history['val_loss']
     ty = model_fit.history['loss']
```



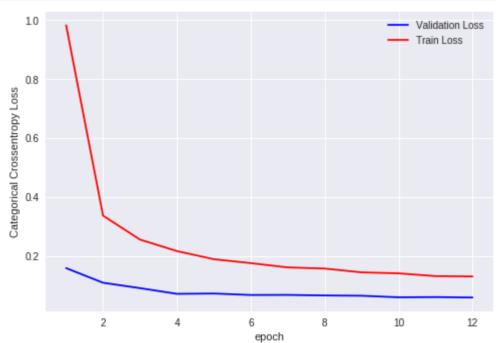
```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        out_w = w_after[10].flatten().reshape(-1,1)
        fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 6, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 6, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 6, 3)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4_w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use.
kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.
violin_data = remove_na(group_data)



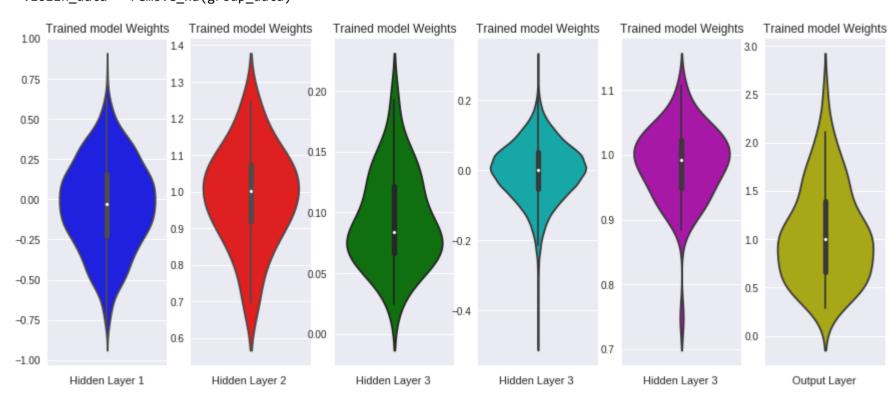
With a ConvNet of (5,5)

```
Various CNN networks on MNIST
In [0]: # convert class vectors to binary class matrices
     from keras.initializers import he_normal
     from keras.optimizers import Adam
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     model = Sequential()
     model.add(Conv2D(32, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel initializer = he normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(Dropout(0.5))
     model.add(BatchNormalization())
     model.add(Dense(num_classes, activation='softmax'))
     model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
     model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
     model_scores = model.evaluate(x_test, y_test, verbose=0)
     print('Test loss:', model_scores[0])
     print('Test accuracy:', model_scores[1])
    Train on 60000 samples, validate on 10000 samples
    Epoch 1/12
     Epoch 2/12
     Epoch 3/12
     Epoch 4/12
     Epoch 5/12
     Epoch 6/12
     Epoch 7/12
     Epoch 8/12
     Epoch 9/12
     Epoch 10/12
     Epoch 11/12
     Epoch 12/12
     Test loss: 0.0583803462437354
    Test accuracy: 0.9853
In [0]: import matplotlib.pyplot as plt
     fig,ax = plt.subplots(1,1)
     ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
     # list of epoch numbers
     x = list(range(1, epochs+1))
     vy = model fit.history['val loss']
     ty = model_fit.history['loss']
     plt_dynamic(x, vy, ty, ax)
```



```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        out_w = w_after[10].flatten().reshape(-1,1)
        fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 6, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 6, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 6, 3)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4_w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

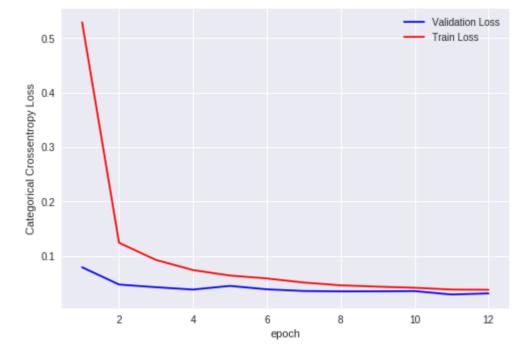
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use.
kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.
violin_data = remove_na(group_data)



Without Batch Normalization

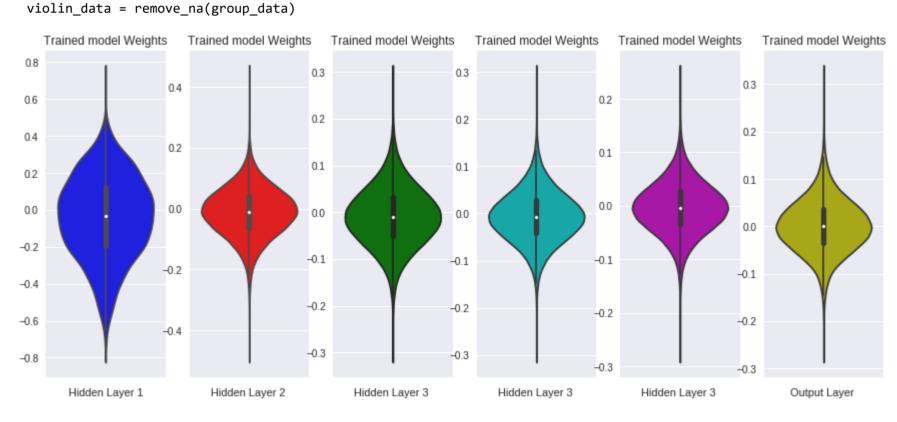
```
Various CNN networks on MNIST
In [0]: # convert class vectors to binary class matrices
    from keras.initializers import he_normal
    from keras.optimizers import Adam
    y_train = keras.utils.to_categorical(y_train, num_classes)
    y_test = keras.utils.to_categorical(y_test, num_classes)
    model = Sequential()
    model.add(Conv2D(32, (7, 7), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
    model.add(MaxPooling2D(pool size=(2, 2)))
    model.add(Dropout(0.25))
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(Dropout(0.25))
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(Dropout(0.25))
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(Dropout(0.25))
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(Dropout(0.25))
    model.add(Flatten())
    model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
    model.add(Dropout(0.5))
    model.add(BatchNormalization())
    model.add(Dense(num classes, activation='softmax'))
    model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
    model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
    model_scores = model.evaluate(x_test, y_test, verbose=0)
    print('Test loss:', model_scores[0])
    print('Test accuracy:', model_scores[1])
    Train on 60000 samples, validate on 10000 samples
    Epoch 1/12
    Epoch 2/12
    Epoch 3/12
    Epoch 4/12
    Epoch 5/12
    Epoch 6/12
    Epoch 7/12
    Epoch 8/12
    Epoch 9/12
    Epoch 10/12
    Epoch 11/12
    Epoch 12/12
    Test loss: 0.031549876034964106
    Test accuracy: 0.9914
In [0]: import matplotlib.pyplot as plt
    fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
    # list of epoch numbers
    x = list(range(1, epochs+1))
    vy = model_fit.history['val_loss']
```





```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        out_w = w_after[10].flatten().reshape(-1,1)
        fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 6, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 6, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 6, 3)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4_w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.



Without Dropouts

```
In [0]: # convert class vectors to binary class matrices
    from keras.initializers import he_normal
    from keras.optimizers import Adam
    y_train = keras.utils.to_categorical(y_train, num_classes)
    y_test = keras.utils.to_categorical(y_test, num_classes)
    model = Sequential()
    model.add(Conv2D(32, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
    model.add(MaxPooling2D(pool_size=(2, 2)))
    model.add(BatchNormalization())
    model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Flatten())
    model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
    model.add(BatchNormalization())
    model.add(Dense(num_classes, activation='softmax'))
    model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
    model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
    model_scores = model.evaluate(x_test, y_test, verbose=0)
    print('Test loss:', model_scores[0])
    print('Test accuracy:', model_scores[1])
    Train on 60000 samples, validate on 10000 samples
    Epoch 1/12
    Epoch 2/12
    Epoch 3/12
    Epoch 4/12
    Epoch 5/12
    Epoch 6/12
    Epoch 7/12
    Epoch 8/12
    Epoch 9/12
    Epoch 10/12
    Epoch 11/12
    Epoch 12/12
    Test loss: 0.04222672743776784
    Test accuracy: 0.9894
In [0]: import matplotlib.pyplot as plt
    fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
    # list of epoch numbers
    x = list(range(1, epochs+1))
    vy = model_fit.history['val_loss']
    ty = model_fit.history['loss']
```



12

10

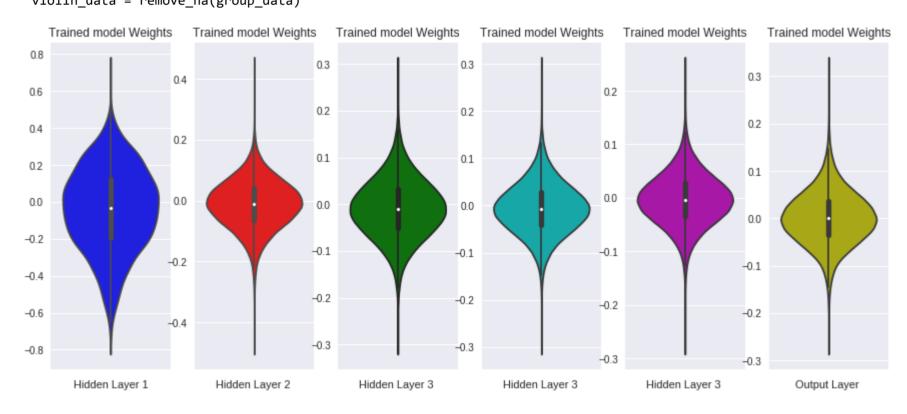
0.02

0.00

2

```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        out_w = w_after[10].flatten().reshape(-1,1)
        fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 6, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 6, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 6, 3)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4 w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 6, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use.
kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.
violin data = remove_na(group_data)



7 Convolutional layers

With a ConvNet of (3, 3)

```
In [0]: # convert class vectors to binary class matrices
     from keras.initializers import he normal
     from keras.optimizers import Adam
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     model = Sequential()
     model.add(Conv2D(32, (3, 3), activation='relu', padding= 'same', kernel initializer = he normal(), input shape=input shape))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (3, 3), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(Dropout(0.5))
     model.add(BatchNormalization())
     model.add(Dense(num_classes, activation='softmax'))
     model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
     model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
     model_scores = model.evaluate(x_test, y_test, verbose=0)
     print('Test loss:', model_scores[0])
     print('Test accuracy:', model_scores[1])
     Train on 60000 samples, validate on 10000 samples
     Epoch 1/12
     Epoch 2/12
     Epoch 3/12
     Epoch 4/12
     Epoch 5/12
     Epoch 6/12
     Epoch 7/12
     Epoch 8/12
     Epoch 9/12
     Epoch 10/12
     Epoch 11/12
     Epoch 12/12
     Test loss: 0.019338892967464563
     Test accuracy: 0.9953
In [0]: import matplotlib.pyplot as plt
     fig,ax = plt.subplots(1,1)
     ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
     # List of epoch numbers
     x = list(range(1, epochs+1))
     vy = model_fit.history['val_loss']
     ty = model_fit.history['loss']
     plt_dynamic(x, vy, ty, ax)

    Validation Loss

    Train Loss

       0.5
     SS 0.4
      0.3
```

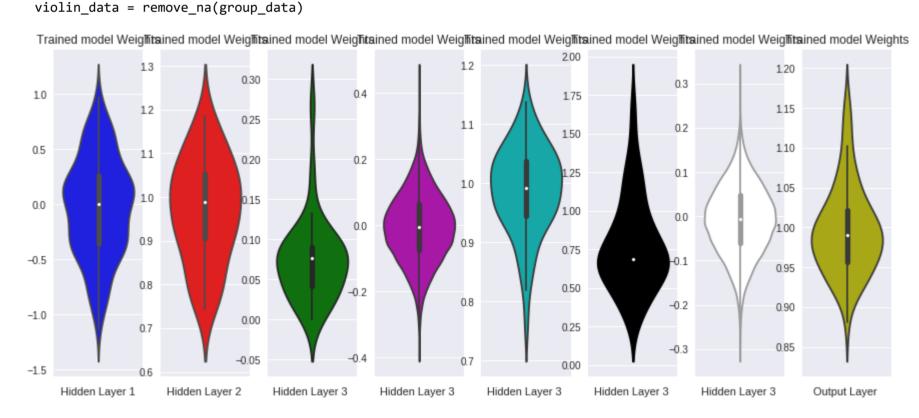
Categorical C

0.1

0.0

```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        h6_w = w_after[10].flatten().reshape(-1,1)
        h7_w = w_after[12].flatten().reshape(-1,1)
        out_w = w_after[14].flatten().reshape(-1,1)
         fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 8, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 8, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 8, 3)
        plt.title("Trained model Weights")
         ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
         plt.subplot(1, 8, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h6_w, color='k')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 7)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h7_w, color='w')
        plt.xlabel('Hidden Layer 3 ')
         plt.subplot(1, 8, 8)
         plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use.
kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.



With a ConvNet of (5, 5)

```
In [0]: # convert class vectors to binary class matrices
     from keras.initializers import he_normal
     from keras.optimizers import Adam
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     model = Sequential()
     model.add(Conv2D(32, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', strides= 2, padding= 'valid', kernel initializer = he normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(Dropout(0.25))
     model.add(BatchNormalization())
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(Dropout(0.5))
     model.add(BatchNormalization())
     model.add(Dense(num_classes, activation='softmax'))
     model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
     model fit = model.fit(x train, y train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
     model_scores = model.evaluate(x_test, y_test, verbose=0)
     print('Test loss:', model_scores[0])
     print('Test accuracy:', model_scores[1])
     Train on 60000 samples, validate on 10000 samples
     Epoch 1/12
     Epoch 2/12
     Epoch 3/12
     Epoch 4/12
     Epoch 5/12
     Epoch 6/12
     Epoch 7/12
     Epoch 8/12
     Epoch 9/12
     Epoch 10/12
     Epoch 11/12
     Epoch 12/12
     Test loss: 0.06989532590415329
     Test accuracy: 0.9838
In [0]: import matplotlib.pyplot as plt
     fig,ax = plt.subplots(1,1)
     ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
     # list of epoch numbers
     x = list(range(1, epochs+1))
     vy = model_fit.history['val_loss']
     ty = model_fit.history['loss']
     plt_dynamic(x, vy, ty, ax)

    Validation Loss

       14

    Train Loss

       12
       10
      0.8
      0.6
     0.4
Cate
```

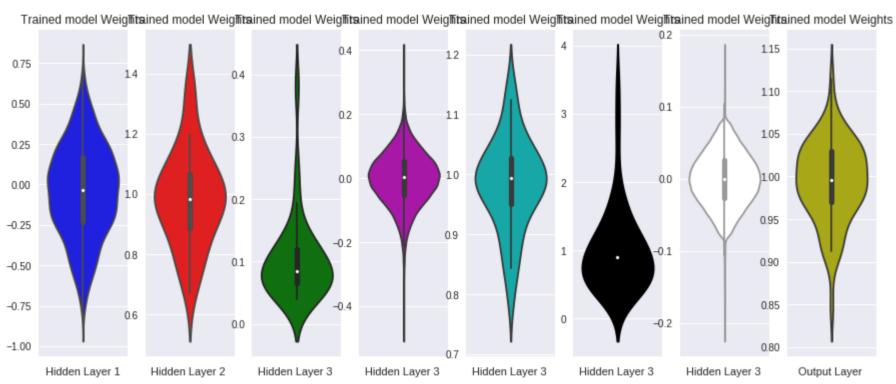
0.2

0.0

```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        h6_w = w_after[10].flatten().reshape(-1,1)
        h7_w = w_after[12].flatten().reshape(-1,1)
        out_w = w_after[14].flatten().reshape(-1,1)
         fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 8, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 8, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 8, 3)
        plt.title("Trained model Weights")
         ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
         plt.subplot(1, 8, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h6_w, color='k')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 7)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h7_w, color='w')
        plt.xlabel('Hidden Layer 3 ')
         plt.subplot(1, 8, 8)
         plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

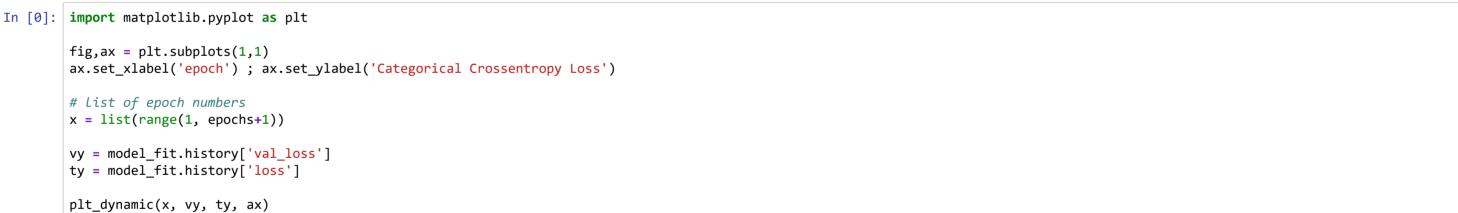
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.

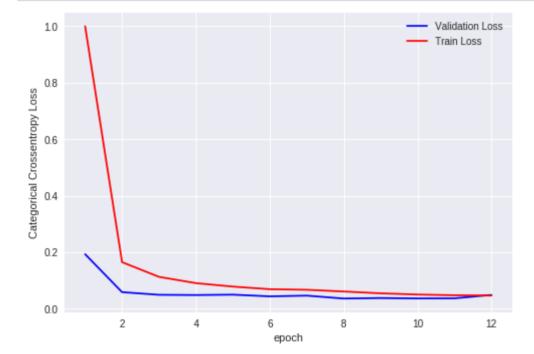
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use violin_data = remove_na(group_data)



Without Batch Normalization

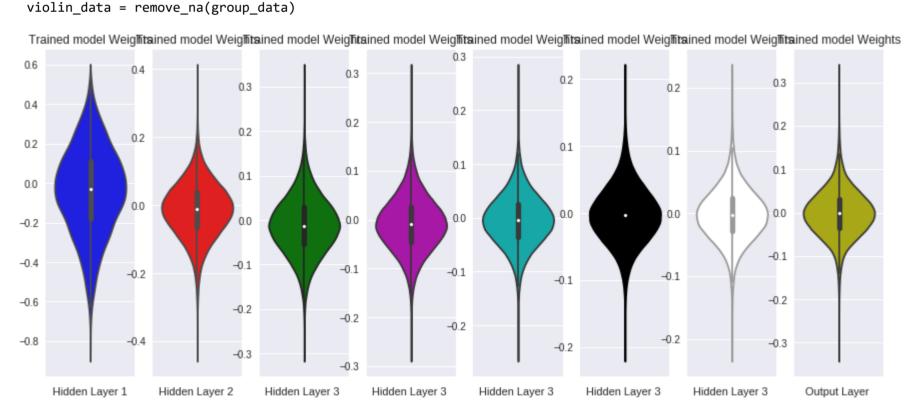
```
1/16/2019
                                                       Various CNN networks on MNIST
   In [0]: # convert class vectors to binary class matrices
        from keras.initializers import he_normal
        from keras.optimizers import Adam
        y_train = keras.utils.to_categorical(y_train, num_classes)
        y_test = keras.utils.to_categorical(y_test, num_classes)
        model = Sequential()
        model.add(Conv2D(32, (7, 7), activation='relu', strides= 2, padding= 'valid', kernel initializer = he normal(), input shape=input shape))
        model.add(MaxPooling2D(pool_size=(2, 2)))
        model.add(Dropout(0.25))
        model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
        model.add(Dropout(0.25))
        model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
        model.add(Dropout(0.25))
        model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
        model.add(Dropout(0.25))
        model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
        model.add(Dropout(0.25))
        model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
        model.add(Dropout(0.25))
        model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
        model.add(Dropout(0.25))
        model.add(Flatten())
        model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
        model.add(Dropout(0.5))
        model.add(BatchNormalization())
        model.add(Dense(num_classes, activation='softmax'))
        model.compile(loss= 'categorical crossentropy', optimizer= 'Adam', metrics=['accuracy'])
        model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
        model_scores = model.evaluate(x_test, y_test, verbose=0)
        print('Test loss:', model_scores[0])
        print('Test accuracy:', model_scores[1])
        Train on 60000 samples, validate on 10000 samples
        Epoch 1/12
        Epoch 2/12
        Epoch 3/12
        Epoch 4/12
        Epoch 5/12
        Epoch 6/12
        Epoch 7/12
        Epoch 8/12
        Epoch 9/12
        Epoch 10/12
        Epoch 11/12
        Epoch 12/12
        Test loss: 0.048573660604926405
        Test accuracy: 0.9888
        fig,ax = plt.subplots(1,1)
        ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
```





```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        h6_w = w_after[10].flatten().reshape(-1,1)
        h7_w = w_after[12].flatten().reshape(-1,1)
        out_w = w_after[14].flatten().reshape(-1,1)
         fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 8, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 8, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 8, 3)
        plt.title("Trained model Weights")
         ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
         plt.subplot(1, 8, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h6_w, color='k')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 7)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h7_w, color='w')
        plt.xlabel('Hidden Layer 3 ')
         plt.subplot(1, 8, 8)
         plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.

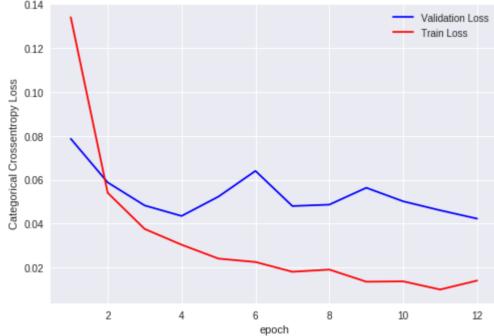


Without Dropouts

```
In [0]: # convert class vectors to binary class matrices
     from keras.initializers import he_normal
     from keras.optimizers import Adam
     y_train = keras.utils.to_categorical(y_train, num_classes)
     y_test = keras.utils.to_categorical(y_test, num_classes)
     model = Sequential()
     model.add(Conv2D(32, (3, 3), activation='relu', strides= 2, padding= 'valid', kernel_initializer = he_normal(), input_shape=input_shape))
     model.add(MaxPooling2D(pool_size=(2, 2)))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (5, 5), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(BatchNormalization())
     model.add(Conv2D(64, (7, 7), activation='relu', padding= 'same', kernel_initializer = he_normal()))
     model.add(BatchNormalization())
     model.add(Flatten())
     model.add(Dense(128, activation='relu', kernel_initializer = he_normal()))
     model.add(BatchNormalization())
     model.add(Dense(num_classes, activation='softmax'))
     model.compile(loss= 'categorical_crossentropy', optimizer= 'Adam', metrics=['accuracy'])
     model_fit = model.fit(x_train, y_train, batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
     model_scores = model.evaluate(x_test, y_test, verbose=0)
     print('Test loss:', model_scores[0])
     print('Test accuracy:', model_scores[1])
     Train on 60000 samples, validate on 10000 samples
     Epoch 1/12
     Epoch 2/12
     Epoch 3/12
     Epoch 4/12
     Epoch 5/12
     Epoch 6/12
     Epoch 7/12
     Epoch 8/12
     Epoch 9/12
     Epoch 10/12
     Epoch 11/12
     Epoch 12/12
     Test loss: 0.04224848728413344
     Test accuracy: 0.988
In [0]: import matplotlib.pyplot as plt
     fig,ax = plt.subplots(1,1)
     ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
     # list of epoch numbers
     x = list(range(1, epochs+1))
     vy = model_fit.history['val_loss']
     ty = model_fit.history['loss']
     plt_dynamic(x, vy, ty, ax)
      0.14
                                    Validation Loss

    Train Loss

      0.12
```

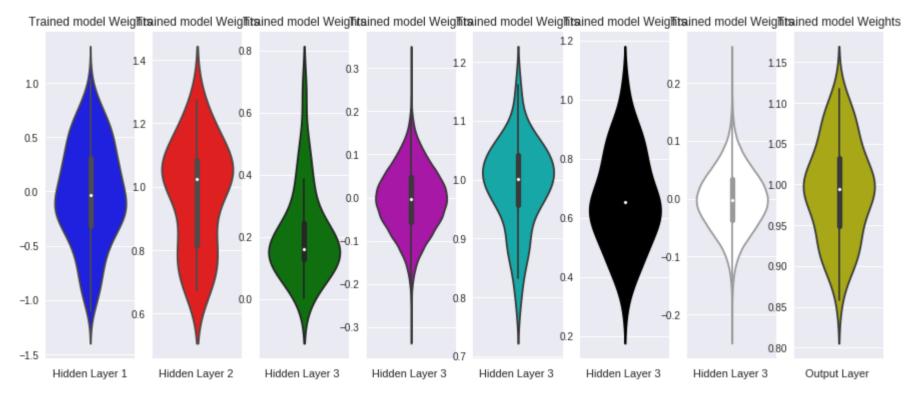


```
In [0]: import matplotlib.pyplot as plt
        import seaborn as sns
        w_after = model.get_weights()
        h1_w = w_after[0].flatten().reshape(-1,1)
        h2_w = w_after[2].flatten().reshape(-1,1)
        h3_w = w_after[4].flatten().reshape(-1,1)
        h4_w = w_after[6].flatten().reshape(-1,1)
        h5_w = w_after[8].flatten().reshape(-1,1)
        h6_w = w_after[10].flatten().reshape(-1,1)
        h7_w = w_after[12].flatten().reshape(-1,1)
        out_w = w_after[14].flatten().reshape(-1,1)
        fig = plt.figure(figsize = (15,6))
        plt.title("Weight matrices after model trained")
        plt.subplot(1, 8, 1)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h1_w,color='b')
        plt.xlabel('Hidden Layer 1')
        plt.subplot(1, 8, 2)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h2_w, color='r')
        plt.xlabel('Hidden Layer 2 ')
        plt.subplot(1, 8, 3)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h3_w, color='g')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 4)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h4_w, color='m')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 5)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h5_w, color='c')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 6)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h6_w, color='k')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 7)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=h7_w, color='w')
        plt.xlabel('Hidden Layer 3 ')
        plt.subplot(1, 8, 8)
        plt.title("Trained model Weights")
        ax = sns.violinplot(y=out_w,color='y')
        plt.xlabel('Output Layer ')
        plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarning: remove_na is deprecated and is a private function. Do not use. kde_data = remove_na(group_data)

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use.

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarning: remove_na is deprecated and is a private function. Do not use. violin_data = remove_na(group_data)



Conclusions

- 1) Models with Batch normalization and dropouts or just seems to perform better than others.
- 2) Models without dropouts seem to perform terribly as they become overfit.
- 3) Models without batch normalization seems to perform okay but chances of overfitting as number of epochs increase.
- 4) Models with **only Batch normalization** takes a **lot of time** to compute compared to models with **only Dropouts**.
- 5) Model seems to **perform best** when number of **convolutional layers is 7 with (3, 3)** and an **accuracy of 99.53%**.

```
In [7]: from prettytable import PrettyTable

x = PrettyTable()
x.field_names = ["Number of Convolutional layers", "Optimizations", "Accuracy", "Train error", "Test error", "Performance"]
x.add_row([3, "With ConvNet (3, 3)", "99.46%", "0.0396", "0.0185", "Good performance"])
x.add_row(["", "With ConvNet (5, 5)", "98.74%", "0.0942", "0.0479", "Good performance"])
x.add_row(["", "Without Dropouts", "98.76%", "0.0867", "0.0497", "Severely overfit"])
x.add_row(["", "Without BN", "99.02%", "0.0323", "0.0340", "Chances of overfit as epochs increase"])
x.add_row(["", "", "", "", "", "", ""])
x.add_row(["", "With ConvNet (3, 3)", "99.47%", "0.0305", "0.0186", "Good performance"])
x.add_row(["", "Without BN", "99.14%", "0.0315", "Chances of overfit as epochs increase"])
x.add_row(["", "Without BN", "99.14%", "0.0315", "Chances of overfit as epochs increase"])
x.add_row(["", "Without BN", "99.14%", "0.0328", "0.0315", "Chances of overfit as epochs increase"])
x.add_row(["", "With ConvNet (3, 3)", "99.53%", "0.0382", "0.0193", "Good performance"])
x.add_row(["", "With ConvNet (5, 5)", "98.38%", "0.1694", "0.0699", "Good performance"])
x.add_row(["", "With ConvNet (5, 5)", "98.38%", "0.1694", "0.0699", "Good performance"])
x.add_row(["", "With ConvNet (5, 5)", "98.38%", "0.1694", "0.0699", "Good performance"])
x.add_row(["", "With ConvNet (5, 5)", "98.38%", "0.1694", "0.0699", "Good performance"])
x.add_row(["", "With ConvNet (5, 5)", "98.38%", "0.1694", "0.0699", "Good performance"])
x.add_row(["", "Without BN", "99.1000", "0.0422", "Severely overfit"])
x.add_row(["", "Without BN", "99.1000", "0.0420", "Severely overfit"])
x.add_row(["", "Without BN", "98.88%", "0.0465", "0.0422", "Severely overfit as epochs increase"])
print(x.get_string())
```

Number of Convolutional layers	Optimizations	Accuracy	Train error	Test error	Performance
3	With ConvNet (3, 3)	99.46%	0.0396	0.0185	Good performance
	With ConvNet (5, 5)	98.74%	0.0942	0.0479	Good performance
	Without Dropouts	98.76%	0.0067	0.0497	Severely overfit
	Without BN	99.02%	0.0323	0.0340	Chances of overfit as epochs increase
5 	With ConvNet (3, 3)	 99.47%	 0.0305	 0.0186	 Good performance
	With ConvNet (5, 5)	98.53%	0.1300	0.0584	Good performance
	Without Dropouts	98.94%	0.0049	0.0422	Severely overfit
	Without BN	99.14%	0.0382	0.0315	Chances of overfit as epochs increase
7 	With ConvNet (3, 3)	 99.53%	 0.0382	 0.0193	 Good performance
	With ConvNet (5, 5)	98.38%	0.1694	0.0699	Good performance
	Without Dropouts	98.80%	0.0140	0.0422	Severely overfit
	Without BN	98.88%	0.0465	0.0486	Chances of overfit as epochs increase