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**Started on** Sunday, November 6, 2022, 4:22 PM

**State** Finished

**Completed on** Sunday, November 6, 2022, 5:44 PM

**Time taken** 1 hour 21 mins

**Points** 8.00/13.50

**Grade** 5.93 out of 10.00 (59.26%)

Question **1**

Correct

1.00 points out of 1.00

Suppose  $A$  is an invertible  $n \times n$  matrix. Which of the following is NOT an equivalent statement?

Select one:

- ☐ The reduced row echelon form of  $A$  is  $I_n$ .
- ☐  $A$  has nullity 0.
- ☒ The column vectors of  $A$  are linearly dependent. ✓
- ☐ The row vectors of  $A$  form a basis for  $\mathbb{R}^n$ .
- ☐ The determinant of  $A$  is not zero.

Question **2**

Correct

0.50 points out of 0.50

If  $A$  is an  $m \times n$  matrix, then the column space of  $A$  is a subspace of:

Select one:

- ☐  $\mathbb{R}$
- ☐  $\mathbb{R}^{m-n}$
- ☐  $\mathbb{R}^{mn}$
- ☒  $\mathbb{R}^m$  ✓
- ☐  $\mathbb{R}^n$

Question 3

Correct

0.50 points out of 0.50

If  $A$  is an  $m \times n$  matrix, then the row space of  $A$  is a subspace of:

Select one:

- ☐  $\mathbb{R}$
- ☐  $\mathbb{R}^{m-n}$
- ☐  $\mathbb{R}^{mn}$
- ☒  $\mathbb{R}^n$  ✓
- ☐  $\mathbb{R}^m$

Question 4

Correct

0.50 points out of 0.50

Elementary row operations do not change the null space of a matrix.

Select one:

- ☒ True ✓
- ☐ False

Question 5

Incorrect

0.00 points out of 0.50

Elementary row operations do not change the column space of a matrix.

Select one:

- ☒ True ✗
- ☐ False

Question 6

Partially correct

1.00 points out of 1.50

Suppose  $A$  is an  $8 \times 7$  matrix with rank 5. Then the rank of  $A^T$  is  ✓, the nullity of  $A$  is  ✓, and the nullity of  $A^T$  is  ✗.

Question **7**

Incorrect

0.00 points out of 1.00

What is the maximum rank of a  $6 \times 4$  matrix?

Select one:

- ☒ 6 ✖
- ☐ 5
- ☐ 4
- ☐ 2
- ☐ 10

Question **8**

Correct

1.00 points out of 1.00

The general solution of  $Ax = 0$  has 2 leading variables and 3 parameters. What is the rank of  $A$ ?

Select one:

- ☐ 1
- ☐ 5
- ☐ 6
- ☐ 3
- ☒ 2 ✔

Question **9**

Correct

1.50 points out of 1.50

What could be the size of the nullity of a  $5 \times 7$  matrix?

Select one:

- ☐ Exactly 2
- ☐ More than 2
- ☐ Less than 2
- ☒ At least 2 ✔
- ☐ At most 2

## Question 10

Correct

1.00 points out of 1.00

Consider the matrix  $A = \begin{bmatrix} 1 & 3 & 1 & 3 \\ 0 & 1 & 1 & 0 \\ -3 & 0 & 6 & -1 \\ 3 & 4 & -2 & 1 \\ 2 & 0 & -4 & -2 \end{bmatrix}$ . Its rank is  ✓ and its nullity is  ✓.

## Question 11

Incorrect

0.00 points out of 2.50

Consider the set of vectors  $S = \{(2, 0, -4), (-3, 0, 6), (1, 2, 1), (-2, 2, 7), (4, 4, -2)\}$  in  $\mathbb{R}^3$ . Find a subset of these vectors that forms a basis for  $\text{span}(S)$ .

Select one:

- ☒  $\{(2, 0, -4), (-3, 0, 6)\}$  ✗
- ☐  $\{(2, 0, -4), (1, 2, 1)\}$
- ☐  $\{(1, 2, 1), (-2, 2, 7), (4, 4, -2)\}$
- ☐  $\{(2, 0, -4), (1, 2, 1), (-2, 2, 7), (4, 4, -2)\}$
- ☐  $\{(2, 0, -4), (-3, 0, 6), (1, 2, 1)\}$

## Question 12

Correct

0.50 points out of 0.50

If a matrix has more rows than columns, then its row space will have a larger dimension than its column space.

Select one:

- ☐ True
- ☒ False ✓

## Question 13

Correct

0.50 points out of 0.50

Elementary row operations do not change the row space of a matrix.

Select one:

- ☒ True ✓
- ☐ False

Question **14**

Incorrect

0.00 points out of 1.00

The general solution of  $Ax = 0$  has 5 leading variables and 4 parameters. What is the nullity of  $A$  ?

Select one:

- ☐ 20
- ☐ 1
- ☒ 9 ✖
- ☐ 5
- ☐ 4

◀ (Sect. 4.8) Rank and Nullity of a Matrix

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