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Started on Tuesday, October 18, 2022, 7:49 PM

State Finished

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Time taken 12 mins 9 secs

Points 21.00/21.00

Grade 10.00 out of 10.00 (100%)

Question **1**

Correct

1.00 points out of 1.00

For any vector space V , the set containing only its zero vector is a subspace of V .

Select one:

☒ True ✓

☐ False

Question **2**

Correct

2.00 points out of 2.00

Consider the vector space of all $n \times n$ matrices with standard addition and scalar multiplication. The subset of $n \times n$ matrices for which all entries are greater than or equal to zero is a subspace of this vector space.

Select one:

☐ True

☒ False ✓

Question 3

Correct

2.00 points out of 2.00

The vector $(4, 4, 5)$ is a linear combination of the vectors $(1, 2, 1)$ and $(2, 0, 3)$.

Select one:

- ☒ True ✓
- ☐ False

Question 4

Correct

1.00 points out of 1.00

What is required to verify that a subset W of a vector space V is a subspace?

- ☐ Verify that W satisfies the commutative and associative properties.
- ☐ Verify all 10 properties from the definition of a vector space.
- ☐ Verify that W has a zero vector and a negative vector.
- ☐ Verify that W is in fact a subset of V .
- ☒ Verify that the two closure properties hold. ✓

Question 5

Correct

2.00 points out of 2.00

W is the subset of \mathbb{R}^3 consisting of vectors of the form (a, b, c) where $c = ab$, with standard addition and scalar multiplication. Is W a subspace of \mathbb{R}^3 ?

Select one:

- ☒ No. W is not closed under either vector addition or scalar multiplication. ✓
- ☐ Yes, because W is closed under both vector addition and scalar multiplication.
- ☐ No. While W is closed under vector addition, it is not closed under scalar multiplication.
- ☐ Yes, because W is not closed under either vector addition or scalar multiplication.
- ☐ No. While W is closed under scalar multiplication, it is not closed under scalar addition.

Question **6**

Correct

2.00 points out of 2.00

W is the subset of R^3 consisting of vectors of the form (a, b, c) where $c = a + b$, with standard addition and scalar multiplication. Is W a subspace of R^3 ?

Select one:

- ☐ No. While W is closed under vector addition, it is not closed under scalar multiplication.
- ☐ Yes, because W is not closed under either vector addition or scalar multiplication.
- ☒ Yes, because W is closed under both vector addition and scalar multiplication. ✓
- ☐ No. W is not closed under either vector addition or scalar multiplication.
- ☐ No. While W is closed under scalar multiplication, it is not closed under scalar addition.

Question **7**

Correct

1.00 points out of 1.00

If $S = \{w_1, w_2, \dots, w_r\}$ is a nonempty set of vectors in a vector space V , then the set W of all possible linear combinations of the vectors in S is a subspace of V .

Select one:

- ☒ True ✓
- ☐ False

Question **8**

Correct

1.00 points out of 1.00

Consider the vector space of all $n \times n$ matrices with standard addition and scalar multiplication. The subset of $n \times n$ matrices whose trace is zero is a subspace of this vector space.

Select one:

- ☒ True ✓
- ☐ False

Question 9

Correct

2.00 points out of 2.00

The vectors $(1, -1, 1)$, $(1, 0, 1)$, and $(0, 0, 2)$ span \mathbb{R}^3 .

Select one:

☒ True ✓☐ False

Question 10

Correct

2.00 points out of 2.00

The matrix $\begin{bmatrix} 7 & 10 \\ 0 & -2 \end{bmatrix}$ is a linear combination of the matrices $\begin{bmatrix} 1 & 2 \\ 0 & 0 \end{bmatrix}$ and $\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$ because

$$\begin{bmatrix} 7 & 10 \\ 0 & -2 \end{bmatrix} = \boxed{5} \checkmark \begin{bmatrix} 1 & 2 \\ 0 & 0 \end{bmatrix} + \boxed{-2} \checkmark \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}.$$

Question 11

Correct

2.00 points out of 2.00

The polynomial $p = 2x^2 + 11x + 1$ is a linear combination of $p_1 = 2 - x$, $p_2 = 1 + x^2$, and $p_3 = 3x - x^2$ because

$$p = \boxed{-2} \checkmark p_1 + \boxed{5} \checkmark p_2 + \boxed{3} \checkmark p_3.$$

Question 12

Correct

1.00 points out of 1.00

The solution set of a homogeneous linear system $Ax = 0$ of m equations in n unknowns is a subspace of \mathbb{R}^n .

Select one:

☒ True ✓☐ False

Question **13**

Correct

2.00 points out of 2.00

Suppose V is the set of all ordered pairs with standard addition and scalar multiplication. Let W be the subset of V that just contains points on a certain line. W will be a subspace of V if which of the following is true?

Select one:

- ☐ The line has a positive y-intercept.
- ☐ The line has a positive slope.
- ☐ The line is vertical.
- ☒ The line goes through the origin.
- ☐ The line is horizontal.

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