## R Code

```
## Machine Learning Project
#
                   Author: N. Murphy
## Version: Masters-Coursework-ML-ML-Project-NMURPHY.R
## Version Control:
# ~/R/ML/Assignents/Project/
# Problem Specification: This script implements Q1 of assignment 2
# Data Specification: None
# Configuration Control: userpath/MATLAB/Master/Coursework/ML
# Version Control: No version control
# References: None
## 1. Data Description
# None
## 2. Clear workspace
rm(list=ls()) # clear environment
## 3. Paths
# 3.1. setwd("<location of your dataset>")
rootp <- getwd()</pre>
setwd("..") # move up one level in the directory tree
# setwd(path.expand('~'))
filentrain <- "/Train_Digits_20171108.csv"
filentest <- "/Test_Digits_20171108.csv"
fpath <- "~/R/ML/Assignments/Project"</pre>
ffilentrain <- paste(fpath,filentrain,sep="")</pre>
ffilentest <- paste(fpath,filentest,sep="")</pre>
## 4. Load Train Data
traindata <- read.csv(ffilentrain)</pre>
testdata <- read.csv(ffilentest)</pre>
## 5. Load libraries
library(e1071)
library(randomForest)
library(neuralnet)
library(nnet)
library(rpart)
library(rattle)
library(gbm)
library(tree)
library(glm)
#####################
```

```
## Pre-processing ##
#####################
# true output
ytemp <- traindata[,1]</pre>
# Even/odd
is.even <- function(x) x\%2 == 0
is.odd <- function(x) x\%2 == 1
eveninds <- which(is.even(ytemp), arr.ind = TRUE)</pre>
oddinds <- which(is.odd(ytemp), arr.ind = FALSE)
# Convert y to +-1 for odd (-1) and even (+1)
y <- matrix(NA,nrow=length(ytemp),ncol=1)</pre>
y[eveninds,1] <- 1
y[oddinds,1] \leftarrow 0#-1
## Inputs
X <- traindata[,2:785]</pre>
## Split into training and validation (80:20 split)
\# N \leftarrow dim(X)[1]
# Xtrain <- X[1:(N*0.8),]
# Xval <- tail(X,N*0.2)
# ytrain <- y[1:(N*0.8)]
# yval <- tail(y,N*0.2)
N \leftarrow dim(X)[1]
# Xtrain <- X
ytrain <- y
## Reduced training set using Principal Component Analysis
Xtrain_cov <- var(X)</pre>
PC_Xtrain <- prcomp(Xtrain_cov)</pre>
## find number of principal components to use- use number of principal components that explain at least
eigs <- PC_Xtrain$sdev^2</pre>
fv <- rbind(Cumulative = cumsum(eigs)/sum(eigs))</pre>
numPC <- which(fv[1,]>0.99)[1]
## create reduced training set
Xtrain_PCA <- as.matrix(X)%*%PC_Xtrain$rotation[,1:numPC] #extract first numpc princ. comps</pre>
Xtrain <- Xtrain_PCA</pre>
## View some images from training set ##
# Create a 28*28 matrix with pixel colour values
m = matrix(unlist(traindata[10,-1]), nrow = 28, byrow = TRUE)
# Plot that matrix
image(m,col=grey.colors(255))
# reverses (rotates the matrix)
rotate <- function(x) t(apply(x, 2, rev))</pre>
# Plot the first 6 images
par(mfrow=c(2,3))
```

```
lapply(1:6,
       function(x) image(
         rotate(matrix(unlist(traindata[x,-1]),nrow = 28, byrow = FALSE)),
         col = grey.colors(256),
         xlab = traindata[x,1]
)
## Implement various classification methods
############################
# 1. Pocket Algorithm ##
#############################
\# Vectorized version to take in NxP matrix X
iter <- 1200
E_in_w_hat <- matrix(NA,iter,1)</pre>
E_in_w <- matrix(NA,iter,1)</pre>
PLA = function(X,y,w0)
  X = cbind(1, X)
  w_{hat} = matrix(w0, dim(X)[2], 1)
  misclass = (sign(as.matrix(X)%*%w_hat)!=y)
  for (i in 1:iter)
    pick = sample(which(misclass==TRUE),1)
    w = w_hat +X[pick,]*y[pick]
    #evaluate errors for updates w and w_hat which has given lower E_in so far
    misclass_w = (sign(as.matrix(X)%*%w)!=y)
    misclass_w_hat = (sign(as.matrix(X)%*%w_hat)!=y)
    E_in_w[i,1] <- sum(misclass_w)</pre>
    E_in_w_hat[i,1] <- sum(misclass_w_hat)</pre>
    if (E_in_w_hat[i,1]>E_in_w[i,1] ){
       w_hat <- w
       misclass <- misclass_w
    } else {
       w_hat <- w_hat</pre>
       misclass <- misclass_w_hat</pre>
    }
   # err<- (sign(as.matrix(X)%*%t(w))-y)^2
  return(list(E_in_w_hat,E_in_w,w_hat,w))
## 5-fold Cross-validation
R <- 5
folds <- cut(seq(1,nrow(Xtrain)),breaks=10,labels=FALSE)</pre>
Ein_pocket <- cbind(rep(NA,R))</pre>
E_val_pock <- Ein_pocket</pre>
# ValData <- list()</pre>
```

```
# TrainData <- list()</pre>
## Split data into 10 folds
for(j in 1:R){
  #Segement your data by fold using the which() function
  Inds <- which(folds==j,arr.ind=TRUE) # indices of current validation fold
  ValData <- Xtrain[Inds,]</pre>
  TrainData <- Xtrain[-Inds,]</pre>
  ydatatrain <- ytrain[-Inds,]</pre>
  ydataval <- ytrain[Inds,]</pre>
  res = PLA(TrainData,ydatatrain,matrix(0,dim(TrainData)[2]+1,1))
  \#Ein\_percept[j] \leftarrow tail(res[[2]]/2500,1)
  Ein_pocket[j] <- tail(res[[1]]/dim(TrainData)[1],1)</pre>
  ## Validation error for pocket and perceptron
  E_val_pock[j] <- sum(sign(as.matrix(cbind(1,ValData))%*%res[[3]])!=ydataval)/250</pre>
  #E_val_perc[j] <- sum(sign(as.matrix(cbind(1,ValData)))%*%res[[4]])!=ydataval)/500
}
## Cross-val. error
E_CV_pock <- mean(E_val_pock)</pre>
##vector of in sample errors
Ein_pocket
## Plot insample error vs iter
plot(1:iter,res[[2]]/2500,type = "1") #Ein percept
plot(1:iter,res[[1]]/2500,type = "l") #Ein pocket
###############################
# 2. Logistic Regression ##
## 5-fold Cross-validation
folds <- cut(seq(1,nrow(Xtrain)),breaks=10,labels=FALSE)</pre>
Ein_pocket <- cbind(rep(NA,R))</pre>
E_val_pock <- Ein_pocket</pre>
# ValData <- list()</pre>
# TrainData <- list()</pre>
## Split data into 10 folds
for(j in 1:R){
  #Segement your data by fold using the which() function
  Inds <- which(folds==j,arr.ind=TRUE) # indices of current validation fold</pre>
  ValData <- Xtrain[Inds,]</pre>
  TrainData <- Xtrain[-Inds,]</pre>
  ydatatrain <- ytrain[-Inds,]</pre>
  ydataval <- ytrain[Inds,]</pre>
```

```
# Implement the glm model for logistic regression
  GLM <- glm(as.formula(paste('ydatatrain ~ ',paste(paste('Pixel_',1:784,sep=''), collapse='+'), sep='
  GLM <- glm(factor(ydatatrain)~.,data=TrainData ,family="binomial")</pre>
  ## Predict on validation data
  pred_glm <- predict.glm(GLM,newdata = ValData, type="response")</pre>
# ## Confusion matrix
# table(`Actual Class` = yval, `Predicted Class` = pred_glm)
  # Error and accuracy
  E_val_glm <- sum(ydataval != pred_glm)/nrow(ydataval)</pre>
  Acc_SVM = 1 - E_val_glm
}
# Fit a neural network 1 hidden layers
Xtrainglm <- X[1:(N*0.8),]</pre>
ytrainglm \leftarrow y[1:(N*0.8)]
Xval \leftarrow tail(X,N*0.2)
yval <- tail(ytrain,N*0.2)</pre>
GLM <- train(Xtrainglm ,factor(ytrainglm ),method = "glm" ,family = "binomial")
pred_glm <- predict(GLM,newdata = Xval)</pre>
E_val_glm <- sum(yval!= pred_glm)/length(yval)</pre>
## Test data prediciton
pred_glmtest <- predict(GLM,newdata = testdata[,2:785])</pre>
pred_glmtest <- ifelse(pred_glmtest,1,0)</pre>
##################################
# 3. Support Vector Machine ##
#####################################
### Test different kernals using CV:
#different kernals
kern = c('polynomial','linear','radial')
\#C = 50
## R-fold Cross-validation
R <- 5
folds <- cut(seq(1,nrow(Xtrain)),breaks=R,labels=FALSE)</pre>
E_val_svm <- cbind(rep(NA,R))</pre>
E_CV_svmkern <- cbind(rep(NA,length(kern)))</pre>
### CV error for different cost parameters
C \leftarrow c(0.01,1,5,30,80)
## R-fold Cross-validation
R <- 5
folds <- cut(seq(1,nrow(Xtrain)),breaks=R,labels=FALSE)</pre>
E_val_svm <- cbind(rep(NA,R))</pre>
E_CV_svm <- matrix(NA,length(kern),length(C))</pre>
```

```
for (k in 1:length(kern)){
  for (i in 1:length(C)){
  ## Split data into R folds
  for(j in 1:R){
    #Segement your data by fold using the which() function
    Inds <- which(folds==j,arr.ind=TRUE) # indices of current validation fold
    ValData <- Xtrain[Inds,]</pre>
    TrainData <- Xtrain[-Inds,]</pre>
    ydatatrain <- ytrain[-Inds,]</pre>
    ydataval <- ytrain[Inds,]</pre>
    ## Using R's in-built function 'svm'
    SVM_fn <- svm(factor(ydatatrain) ~ ., data=TrainData, type='C-classification', kernel=kern[k], cost
    ## Predict on validation data
    predSVM <- predict(SVM_fn,newdata = ValData, type = "class")</pre>
    ## Confusion matrix
    table(`Actual Class` = ydataval, `Predicted Class` = predSVM)
    # Error and accuracy
    E_val_svm[j] <- sum(ydataval != predSVM)/length(ydataval)</pre>
    \#Acc\_SVM = 1 - E\_SVM
   }
  ## Cross-validation error SVM
 E_CV_svm[k,i] <- mean(E_val_svm)</pre>
 }
## find cost and kernal which gave lowest CV error
indssvm <- which(E_CV_svm==min(E_CV_svm))</pre>
# number of trees
print(kern[indssvm[1]])
print(C[indssvm[1]])
## data frame of results for svm CV
df_SVM <- data.frame(100*E_CV_svm)</pre>
rownames(df_SVM) <- kern</pre>
colnames(df_SVM) <- C</pre>
library(knitr)
kable(df_SVM)
## Predict on test data
SVM_fntest <- svm(factor(ytrain) ~ ., data=X, type='C-classification', kernel=kern[indssvm[1]], cost=C[
pred_svmtest <- as.matrix(predict(SVM_fntest,newdata = testdata[,2:785]))</pre>
#######################
# 4. Neural Network ##
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```
# Fit a neural network 1 hidden layers
XtrainNN <- X[1:(N*0.8),]</pre>
ytrainNN \leftarrow y[1:(N*0.8)]
Xval \leftarrow tail(X,N*0.2)
yval \leftarrow tail(y,N*0.2)
nnet_model <- nnet(XtrainNN ,ytrainNN, size = 40, MaxNWts=1000000 )</pre>
predresults <- predict(nnet_model,newdata=Xval)</pre>
results <- table(round(predresults),yval)</pre>
# ### gives sum(diag(results))/length(y) = 15.8% error
pred_NNtest <- predict(nnet_model,newdata=testdata[,2:785])</pre>
pred_NNtest <- round(pred_NNtest)</pre>
# #sum(round(Predicted)!=yval)
#results <- data.frame(actual = yval, predprob = predNN$net.result, prediction = round(predNN$net.resu</pre>
#
# ptm <- proc.time()</pre>
# NN <- neuralnet(as.formula(paste('ytrainNN ~ ',paste(paste('Pixel_',1:784,sep=''), collapse='+'), sep
# proc.time() - ptm
# ## Predictions on validation set
# predNN <- compute(NN, Xval)</pre>
# ## Confusion matrix
# CM_NN <- table(round(predNN$net.result),yval)</pre>
# ## Accuracy/Validation error
# (sum(diag(CM_NN)))/sum(CM_NN)
# ## predictions on test data
# NN <- neuralnet(as.formula(paste('ytrain ~ ',paste(paste('Pixel_',1:784,sep=''), collapse='+'), sep='
# pred_NNtest <- compute(NN, testdata[,2:785])</pre>
#########################
# 5. Random Forests ##
##########################
## Cv to choose number of trees for random forest
numtreerf <- c(10,30,60,100,200,300) #number of tress to use for random forest
## R-fold Cross-validation
R <- 5
folds <- cut(seq(1,nrow(Xtrain)),breaks=R,labels=FALSE)</pre>
E_val_rf <- cbind(rep(NA,R))</pre>
E_in_rf <- cbind(rep(NA,R))</pre>
E_CV_rf <- cbind(rep(NA,length(numtreerf)))</pre>
for (i in 1:length(numtreerf)){
## Split data into 10 folds
for(j in 1:R){
  #Segement your data by fold using the which() function
```

```
Inds <- which(folds==j,arr.ind=TRUE) # indices of current validation fold</pre>
  ValData <- Xtrain[Inds,]</pre>
  TrainData <- Xtrain[-Inds,]</pre>
  ydatatrain <- ytrain[-Inds,]</pre>
  ydataval <- ytrain[Inds,]</pre>
  ## Implement Random Forest using randomForest R package
  rf <- randomForest(factor(ydatatrain) ~ .,data=TrainData,type="class",ntree=numtreerf[i],importance=T
  ## In sample error
  E_in_rf <- tail(rf$err.rate,1)[1]</pre>
  ## Predict on the validation data
  rfPredval = predict(rf, newdata=ValData)
  # Confusion matrix- where predicted values agree and disagree with target y
  CM_rf = table(rfPredval, ydataval)
  ## acuracy and error of the prediction on val. data
  accuracy_rf = (sum(diag(CM_rf)))/sum(CM_rf)
  E_val_rf[j] = 100*(1-accuracy_rf) #validation error
 ## Cross-validation error RF
E_CV_rf[i] <- mean(E_val_rf)</pre>
nooftreerf <- which(E CV rf==min(E CV rf))</pre>
print(numtreerf[nooftreerf])
## data frame of results for svm CV
df_rf <- data.frame(E_CV_rf)</pre>
rownames(df_rf) <- numtreerf</pre>
colnames(df_rf) <- c("Trees", "Cross Validation Error")</pre>
library(knitr)
kable(df_rf)
## Train on all data using chosen number of trees
rffinal <- randomForest(factor(ytrain) ~ .,data=X,type="class",ntree=numtreerf[nooftreerf],importance=T.
## Predict on test data
Pred_rftest <- as.matrix(predict(rffinal, newdata=testdata[,2:785]))</pre>
## plot the mean square error of the forest object as function of no. of trees
plot(1:numtreerf[nooftreerf],rffinal$err.rate[,1],type="l",col="black",xlab = "No. of Trees",ylab="Error
lines(1:numtreerf[nooftreerf],rffinal$err.rate[,2],type="1",lty="dashed",col="green") #for classificati
lines(1:numtreerf[nooftreerf],rffinal$err.rate[,3],type="1",lty="dashed",col="red") #for classificatio
legend("top", cex =0.5,legend=c(0,"00B",1), colnames("Even","0dd"),lty=c(2,1,2), col=c("green","black",
# 6. Generalized Boosted Regression Models ##
```

```
# ## Implement R GBM function
# fitControl <- trainControl(method = "repeatedcv", number = 10, repeats = 1)
# GBM = train(Xtrain, ytrain, method= 'qbm', trControl=fitControl)
# ## Predict on the validation data
# pred_gbm = predict(GBM, newdata=Xval)
# ## Confusion matrix
# CM_GBM = table(round(pred_gbm), yval)
# ## acuracy and error of the prediction on val. data
# accuracy_GBM = (sum(diaq(CM_GBM)))/sum(CM_GBM)
# E_val_gbm = 100*(1-accuracy_GBM) #validation error
# ## Predict on test data
# Pred_qbm_test <- predict(GBM, newdata=testdata)</pre>
## USe CV to find number of trees
ptm <- proc.time()</pre>
numtrees_gbm <- c(100,400,800,1500)
shrinkparam = c(0.1, 0.01, 0.001)
## R-fold Cross-validation
R < -5
folds <- cut(seq(1,nrow(Xtrain)),breaks=R,labels=FALSE)</pre>
E_val_gbm <- cbind(rep(NA,R))</pre>
E_CV_gbm <- matrix(NA,length(numtrees_gbm),length(shrinkparam))</pre>
for (k in 1:length(shrinkparam)){
 for (i in 1:length(numtrees_gbm)){
  ## Split data into 10 folds
  for(j in 1:R){
    #Segement your data by fold using the which() function
    Inds <- which(folds==j,arr.ind=TRUE) # indices of current validation fold</pre>
    ValData <- data.frame(Xtrain[Inds,])</pre>
    TrainData <- data.frame(Xtrain[-Inds,])</pre>
    ydatatrain <- ytrain[-Inds,]</pre>
    ydataval <- ytrain[Inds,]</pre>
    boost <- gbm(ydatatrain ~ ., data=TrainData, distribution="bernoulli", n.trees=numtrees_gbm[i],shri
    proc.time() - ptm
    pred_GBM = predict(boost, newdata=ValData,n.trees = numtrees_gbm[i],type = "response")
    CM_GBM = table(round(pred_GBM),ydataval)
    ## acuracy and error of the prediction on val. data
    accuracy_GBM = (sum(diag(CM_GBM)))/length(ydataval)
    E_val_gbm[j] = 100*(1-accuracy_GBM) #validation error
  ## Cross-validation error RF
  E_CV_gbm[i,k] <- mean(E_val_gbm)</pre>
```

```
proc.time() - ptm
## find lowest cv error for given number of trees
indsgbm <- which(E_CV_gbm==min(E_CV_gbm))</pre>
# number of trees
print(numtrees_gbm[indsgbm[2]])
#shrinkage
print(shrinkparam[indsgbm[1]])
## data frame of results for svm CV
df_gbm <- data.frame(E_CV_gbm)</pre>
rownames(df_gbm) <- numtrees_gbm</pre>
colnames(df_gbm) <- shrinkparam</pre>
library(knitr)
kable(df_gbm)
## Predict on test set using full training data with chosen number of trees from CV
boost <- gbm(as.formula(paste('ytrain ~ ',paste(paste('Pixel_',1:784,sep=''), collapse='+'), sep='')),
pred_GBMtest = as.matrix(round(predict(boost, newdata=testdata[,2:785],n.trees =numtrees_gbm[indsgbm[2]]
#############################
# 7. Classification trees ##
#############################
## Stopping criteria
stopcrit <- rpart.control(minbucket = 5, minsplit = 10)</pre>
## cross validation
R <- 5
E_val_tree <- cbind(rep(NA,R))</pre>
E_CV_tree <- cbind(rep(NA,R))</pre>
## Split data into R folds
for(j in 1:R){
  #Segement your data by fold using the which() function
  Inds <- which(folds==j,arr.ind=TRUE) # indices of current validation fold</pre>
  ValData <- data.frame(Xtrain[Inds,])</pre>
  TrainData <- data.frame(Xtrain[-Inds,])</pre>
  ydatatrain <- ytrain[-Inds,]</pre>
  ydataval <- ytrain[Inds,]</pre>
  ## Implement 'rpart' function
  fulltree <- rpart(ydatatrain ~ ., method = "class", data = TrainData,control = stopcrit)
  ## Predict on the validation data
  pred_tree <- predict(fulltree, newdata = ValData, type = "class")</pre>
  E_val_tree[j] <- sum(ydataval != pred_tree)/length(ydataval)</pre>
E_CV_tree <- 100*mean(E_val_tree)</pre>
## Implement 'rpart' function on full data set
```

```
stopcrit <- rpart.control(minbucket = 5, minsplit = 10)</pre>
fulltree <- rpart(ytrain ~ ., method = "class", data = X,control = stopcrit)</pre>
## Plot the tree
# plot(fulltree)
\# text(fulltree, cex = 0.5)
library(rattle)
fancyRpartPlot(fulltree, tweak=1.5,main="Recursive Partitioning Tree")
## Predict on test data
pred_treetest <- as.matrix(predict(fulltree, newdata = testdata[,2:785], type = "class"))</pre>
### Predictions on test data ##
Predictions <- cbind(pred_symtest,Pred_rftest,pred_GBMtest,pred_treetest,pred_NNtest,as.matrix(pred_glm
Pred <- data.frame(Predictions)</pre>
colnames(Pred) <- c("SVM","Random Forest","Boosting","Tree","Neural Network","Logistic Regression")</pre>
## Write to .csv
write.csv(Pred, "~/R/ML/Assignments/Project/Predictions.csv")
\#write.csv(pred\_sumtest, "~/R/ML/Assignments/Project/Predictions.csv")
### EOF
```