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Sear ch

1.1 Programming Model

This section under major construction.

Our study of algorithms is based upon implementing them as programs written in thortogramming language. Wdo so for several reasons:

- Our programs are concise, elegant, and complete descriptions of algorithms.
- You can run the programs to study properties of the algorithms.
- You can put the algorithms immediately to good use in applications.

Primitive data types and expressions.

A data type is a set of values and a set of operations on those valuethe following four primitive data types are the basis of the Java language:

- Integers, with arithmetic operations (t)
- Real numbers, again with arithmetic operations (uble)
- Booleans, the set of values \{rue, false\}\ with logical operations\(\phi\)olean)
- Characters, the alphanumeric characters and symbols that you typea(r)

A Java program manipulates*ariables* that are named with*identifiers*. Each variable is associated with a dataype and stores one of the permissible data-type values. We use *expressions* to apply the operations associated with each type.

term	examples		definition	
primitive data type	int double boolean char		a set of values and a set of operations on those values (built in to the Java language)	
identifier	a abc A	b\$ a_b ab123 lo hi	a sequence of letters, digits, _, and \$, the first of which is not a digit	
variable	[any identifier]		names a data-type value	
operator	+ - * /		names a data-type operation	
literal	int double boolean char	1 0 -42 2.0 1.0e-15 3.14 true false 'a' '+' '9' '\n'	source-code representation of a value	
expression	int double boolean	lo + (hi - lo)/2 1.0e-15 * t lo <= hi	a literal, a variable, or a sequence of operations on literals and/or variables that produces a value	

The following table summarizes the set of values and most common operations on those values fori tayalsuble, boolean, and char data types.

type	set of values	operators	typical expressions		
турс	Set of values	operators	expression	value	
	integers between -2^{31} and $+2^{31}-1$ (32-bit two's	+ (add)	5 + 3	8	
		- (subtract)	5 - 3	2	
int		* (multiply)	5 * 3	15	
		/ (divide)	5 / 3	1	
	complement)	% (remainder)	5 % 3	2	
	double-precision	+ (add)	3.14103	3.111	
double	real numbers	- (subtract)	2.0 - 2.0e-7	1.9999998	
gonpie	(64-bit IEEE 754	* (multiply)	100 * .015	1.5	
	standard)	/ (divide)	6.02e23 / 2.0	3.01e23	
	true Or false	&& (and)	true && false	false	
booloon		(or)	false true	true	
boolean		! (not)	!false	true	
		^ (xor)	true ^ true	false	
char	characters (16-bit)	[arithmet	ic operations, rarely u	sed]	

- Expressions. Typical expressions are infix. When an expression contains more than one operatone precedence order specifies the order in which they are applied the operators and / (and %) have higher precedence than (are applied beforthe + and operators; among logical operators, ! is the highest precedence, followed the and and then | |. Generally operators of the same precedence are deft associative (applied left to right You can use parentheses to override these rules.
- Type conversion. Numbers are automatically promoted to a more inclusive type ifinformation is lost. For example, in the expression 2.5, the 1 is promoted to the double value 1.0 and the expression evaluates to the double value 3.5. A cast is a directive to convert a value of one type into a value of another type. For example 1.7 is 3. Casting adouble to an int truncates toward zero.
- Comparisons. The following nixed-type operators compare two values of the same type and product open value:
 - equal (==)
 - not equal (!=)
 - less than (<)
 - less than or equal (<=)
 - o greater than (>)
 - greater than or equal (>=)
- Other primitive types. Java's int has a 32-bit representation; Java'souble type has a 64-bit representation. Java has five additional primitive data types:
 - o 64-bit integers, with arithmetic operations (g)
 - o 16-bit integers, with arithmetic operationsh(rt)
 - o 16-bit characters, with arithmetic operationsh(ar)
 - 8-bit integers, with arithmetic operationsy(te)
 - o 32-bit single-precision real numbers, with arithmetic operations (t)

Statements.

A Java program is composed of tatements, which define the computation by creating and manipulating variables, assigning data-type values to t and controlling the flow of execution of such operations.

- Declarations create variables of a specified type and name them with identifiers. Javainsonagly typed language because the Java compiler checks for consistencyThe scope of a variable is the part of the program where items.
- Assignments associate a data-type value (defined by an expression) with a variable.
- Initializing declarations combine a declaration with an assignment to initialize a variable at the same time it is declared.
- Implicit assignments. The following shortcuts are available when our purpose is to modify a variable's value relative to the current value:

- Increment/decrement operators: the code++ is shorthand for = i + 1. The code++i is the same except that the expression value is taken *after* the increment/decrement, not before.
- Other compound operators: the code /= 2 is shorthand for = i/2.
- Conditionals provide for a simple change in the flow of execution—executestatements in one of two blocks, depending on a specified condition.
- Loops provide for a more profound change in the flow of execution—execute the statements in a block as long as a given condition true refer to the statements in the block in a loop as the dy of the loop.
- Break and continue. Java supports two additional statements for use within while loops:
 - o The break statement, which immediately exits the loop
 - The continue statement, which immediately begins the next iteration of the loop
- For notation. Many loops follow this scheme: initialize an index variable to some value and then the loop to test a loop continuation condition involving the index variable, where the last statement in the loop increments the index variable or can express such loops compactly with Java's or notation.
- Single-statement blocks. If a block of statements in a conditional or a loop has only a single statement, the box may be omitted.

The following table illustratesfdrent kinds of Java statements.

statement	examples	definition	
declaration	<pre>int i; double c;</pre>	create a variable of a specified type, named with a given identifier	
assignment	<pre>a = b + 3; discriminant = b*b - 4.0*c;</pre>	assign a data-type value to a variable	
initializing declaration	<pre>int i = 1; double c = 3.141592625;</pre>	declaration that also assigns an initial value	
implicit assignment	i++; i += 1;	i = i + 1;	
conditional (if)	if $(x < 0) x = -x;$	execute a statement, depending on boolean expression	
conditional (if-else)	<pre>if (x > y) max = x; else</pre>	execute one or the other statement, depending on boolean expression	
loop (while)	<pre>int v = 0; while (v <= N) v = 2*v; double t = c; while (Math.abs(t - c/t) > 1e-15*t) t = (c/t + t) / 2.0;</pre>	execute statement until boolean expression is false	
loop (for)	<pre>for (int i = 1; i <= N; i++) sum += 1.0/i; for (int i = 0; i <= N; i++) StdOut.println(2*Math.PI*i/N);</pre>	compact version of while statement	
call	<pre>int key = StdIn.readInt();</pre>	invoke other methods (see page 22)	
return	return false;	return from a method (see page 24)	

Arrays.

An array stores a sequence of values that are all of the same type. If we havealues, we can use the notation[i] to refer to theith value for any value of from to N-1.

- Creating and initializing an array Making an array in a Java program involves three distinct steps:
 - Declare the array name and type.
 - · Create the array
 - o Initialize the array values.
- Default array initialization. For economy in code, we often take advantage of Java's default array initialization convention and combine a three steps into a single statement he default initial value is zero for numeric types that for typeboolean.
- *Initializing declaration*. We can specify the initialization values at compile time, by listing literal values between curly braces, separated t commas.

- Using an array. Once we create an array its size is fixedA program can refer to the length of an array] with the codea.length. Java does
 automatic bounds checking—if you access an array with an illegal index your program will terminate with an
 ArrayIndexOutOfBoundsException
- *Aliasing*. An array name refers to the whole array—if we assign one array name to anothen both refer to the same arrayas illustrated in the following code fragment.

```
int[] a = new int[N];
...
a[i] = 1234;
...
int[] b = a;
...
b[i] = 5678; // a[i] is now 5678.
```

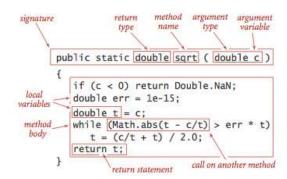
This situation is known adiasing and can lead to subtle bugs.

• Two-dimensional arrays. A two-dimensional array in Java is an array of one-dimensional arrayswo-dimensional array may bragged (its arrays may all be of differing lengths), but we most often work w(fbr appropriate parameters M and N) M-by-N two-dimensional arraysor refer to the entry in row and columnj of a two-dimensional arrays[][], we use the notations[i][j].

Static methods.

Static methods are callegiunctions in many programming languages, since they can behave like mathematical fun Exichsstatic method is a sequence of statements that are executed, one after the otherhen the static method is alled.

• Defining a static method. A method encapsulates a computation that is defined as a sequence of statemeAtsmethod takes arguments (values of given data types) and computes aturn value of some data type or causes aide effect. Each static method is composed of a signature and a body.



- Invoking a static method. A call on a static method is its name followed by expressions that specifigraent values in parentheses, separated by commas. When a method is called, its grument variables are initialized that the values of the corresponding expressions in the called the static method is to compute a value must be specified in a return statement.
- Properties of methods. Java methods have the following features:
 - Arguments are passed by value. When calling a function, the garment value is fully evaluated and the resulting value into argument variable. Array (and other object) references are also passed by value: the method cannot change the reference, but it can change the entries in the array (or value of the object).
 - *Method names can be overloaded.* Methods within a class can have the same name, provided they have defit signatures. This features is known as *overloading*.
 - A method has a single return value but may have multiple return statements. A Java method can provide only one return value. Control goes back to the calling program as soon as the streturn statement is reached.
 - A method can have side effects. A method may use the keywordoid as its return type, to indicate that it has no return value and produces side effects (consume input, produce output, change entries in an arrayotherwise change the state of the system).
- *Recursion*. A *recursive* method is a method that calls itself either directly or indirectly or indirectly are three important rules of thumb in developing recursive programs:
 - The recursion has abase case.
 - Recursive calls must address subproblems that annualler in some sense, so that recursive calls congerto the base case.
 - Recursive calls should not address subproblems that erlap.
- Basic programming model. A library of static methods is a set of static methods thatre defined in a Java classA basic model for Java programming is to develop a program that dresses a specific computational task by creating a library of static methods, one of which is na main().
- *Modular programming*. Libraries of static methods enablaodular programming, where static methods in one library can call static method defined in other libraries. This approach has many important advantages.
 - Work with modules of reasonable size
 - Share and reuse code without having to reimplement it
 - Substitute improved implementations
 - Develop appropriate abstract models for addressing programming problems
 - Localize debugging
- Unit testing. A best practice in Java programming is to include atn() in every library of static methods that tests the methods in the library
- External libraries. We use static methods from four diefent kinds of libraries, each requiring (slightly) rdiff procedures for code reuse.
 - o Standard system libraries inava.lang, includingjava.lang.Math, java.lang.Integer, and java.lang.Double
 - Imported system libraries such apava.util.Arrays. An import statement at the beginning of the programmeded to use such libraries.
 - Other libraries in this book to use such a program, download the source from the booksite into your working directory or following instructions for adding algs4.jarto your classpath.
 - The standard libraries that we have developed for use in this bolk use such a program, download the source from the booksite into your working directory or followhese instruction for addingstdlib.jarto your classpath.

To invoke a method from another library prepend the library name to the method name for each callth.sqrt(), Arrays.sort(), BinarySearch.rank(), and StdIn.readInt().

APIs.

- Java libraries.
- Our standard libraries.
- Your own libraries.

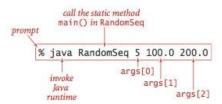
Strings.

type	set of values	typical literals	operators	typical expressions	
				expression	value
String	character	"AB" "Hello"	+ (concatenate)	"Hi, " + "Bob" "12" + "34"	"Hi, Bob" "1234"
	sequences	sequences "2.5"		"1" + "+" + "2"	"1+2"

- Concatenation.
- Conversion.
- Automatic conversion.
- Command-line arguments.

Input and output.

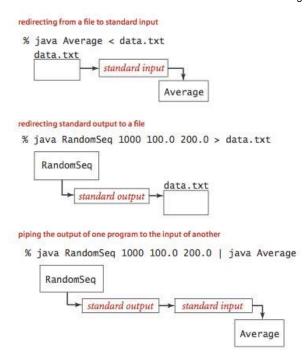
• Commands and arguments.



- Standard output.
- Formatted output.

type	code	typical literal	sample format strings	converted string values for output
int	d	512	"%14d" "%-14d"	" 512" "512 "
double	f e	1595.1680010754388	"%14.2f" "%.7f" "%14.4e"	" 1595.17" "1595.1680011" " 1.5952e+03"
String	S	"Hello, World"	"%14s" "%-14s" "%-14.5s"	" Hello, World" "Hello, World " "Hello"

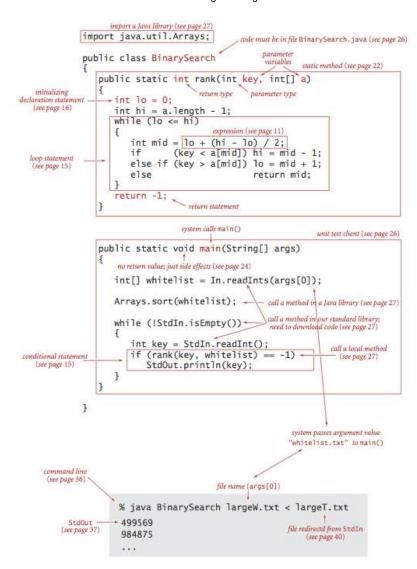
- Standard input.
- Redirection and piping.



- Input and output from a file.
- Standard drawing.

Binary search.

Below is a complete Java programming model. It implement a classic algorithm known abinary search and tests it for an application known abinary search.



The static method ank() takes an integer key and a orted array of int values as aguments and returns the index of the key if it is present in the array of the return value in it is in the array hen entering into a loop that tests the middle entry in the interval (at index). If the key is equal to [mid], the return value in id; otherwise the method cuts the interval size about in half, looking at the left half if the key is less a [name] and at the right half if the key is greater that [mid]. The process terminates when the key is found or the interval is empty

```
successful search for 23
 10 11 12 16 18 23 29 33 48 54 57 68 77 84 98
 10
          mid
                     hi
 10 11 12 16 18 23 29 33 48 54 57 68 77 84 98
               10
 10 11 12 16 18 23 29 33 48 54 57 68 77 84 98
unsuccessful search for 50
 10 11 12 16 18 23 29 33 48 54 57 68 77 84 98
 10 11 12 16 18 23 29 33
                            48 54 57 68 77 84 98
                            To mid hi
 10 11 12 16 18 23 29 33 48 54 57 68 77 84 98
                         10 mid hi
33 48 54
                           hi lo
 10 11 12 16 18 23 29 33 48 54 57 68 77 84 98
```

- Development client.
- Whitelisting.
- Performance.

Input and output libraries.

Here is a list of the input and output libraries that we use throughout the textbook and beyond.

§	PROGRAM	DESCRIPTION / JAVADOC
<u>1.5</u>	StdIn.java	read numbers and text from standard input
<u>1.5</u>	StdOut.java	write numbers and text to standard output
<u>1.5</u>	<u>StdDraw.java</u>	draw geometric shapes in a window
1.5	StdAudio.java	create, play and manipulate sound
<u>2.2</u>	StdRandom.java	generate random numbers
2.2	StdStats.java	compute statistics
2.2	StdArrayIO.java	read and write 1D and 2D arrays
<u>3.1</u>	<u>In.java</u>	read numbers and text from files and URLs
<u>3.1</u>	<u>Out.java</u>	write numbers and text to files
<u>3.1</u>	<u>Draw.java</u>	draw geometric shapes
<u>3.1</u>	Picture.java	process digital images
3.2	Stopwatch.java	measure running time
Ξ	BinaryStdIn.java	read bits from standard input
Ξ	BinaryStdOut.java	write bits to standard output
Ξ	BinaryIn.java	read bits from files and URLs
Ξ	BinaryOut.java	write bits to files

We briefly describe the input and output libraries and include a sample client.

Standard input and standard output.

StdIn.java and StdOut.java are libraries for reading in numbers and text from standard input and printing out numbers and text to standard output versions have a simpler interface than the corresponding Java ones (and provide a few technical improver Rents) in Seq.javagenerates random numbers in a given range verage.javareads in a sequence of real numbers from standard input and prints their average on standard output.

% java Average
10.0 5.0 6.0 3.0 7.0 32.0
3.14 6.67 17.71
<Ctrl-d>
Average is 10.0577777777778

In. java and Out. java are object-oriented versions that support multiple input and output streams, including reading from a file or URL and writin file.

Standard drawing.

StdDraw.java is an easy-to-use library for drawing geometric shapes, such as points, lines, and circlest Fiangle.javadraws a right triangle and a circumscribing circle.

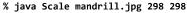
<u>Draw.java</u> is an object-oriented versions that support drawing in multiple windows.

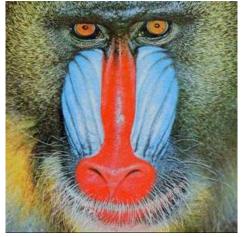
Standard audio.

<u>StdAudio.java</u>is an easy-to-use library for synthesizing sou<u>ffdne.java</u>reads in a frequency and duration from the command line, and it sonifies a wave of the given frequency for the given duration.

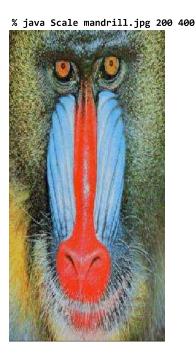
Image processing.

<u>Picture.java</u>is an easy-to-use library for image processing cale.javatakes the name of a picture file and two integers (width w and height h) as command-line agruments and scales the image to w-by-h.









Q + A

Q. How important is it to use a good shilling algorithm?

A. Here's an <u>amusing anecdot</u> of what happens when you don't do it correctly (and you're business is online poker!). If you're running an online casino, here's the recommended approach for shifting a deck of cards: (i) get a cryptographically secure pseudo-random number gene(ait) assign a random 64-bit number to each card, (iii) sort the cards according to their number

Creative Problems

27. **Binomial distribution**Estimate the number of recursive calls that would be used by method calbinomial1(100, 50, .25) in Binomial.javaDevelop a better implementation that is based on saving computed values in an array

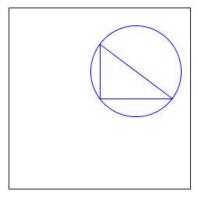
Web Exercises

- 1. Sattolo's algorithm. Write a program Sattolo.java that generates a unifomly distributed cycle of length N uSittplo's algorithm
- 2. Wget. Write a programWget.javathat reads indata from the URL specified on the command line and saves it in a file with the same name.

% java Wget http://introcs.cs.princeton.edu/data/codes.csv
% more codes.csv
United States,USA,00
Alabama,AL,01
Alaska,AK,02

3. **Right triangle.** Write a client Right Fiangle. jay athat draws a right triangle and a circumscribing circle.

% java RightTriangle



4. **Bouncing ball.**Write a programBouncingBall.jaythat illustrates the motion of a bouncing ball.

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