

ENGR 212: Programming Practice

Week 13

Optimization

- Optimization finds the best solution to a problem by trying many different solutions and scoring them to determine their quality.
- Optimization is typically used in cases where there are too many possible solutions to try them all.
- The simplest but least effective method of searching for solutions is just trying a few thousand random guesses and seeing which one is best.

Group Travel Planning

- Have you ever planned a trip for a group of people?
- You must have thought about total cost, time spent waiting at airports, and time taken off work.

Group Travel Planning

- Let's plan a trip for a group of people (the Glass family in this example) from different locations all arriving at NewYork, La Guardia Airport.

Group Travel Planning



Group Travel Planning

```
import time
import random
import math

people = [('Seymour', 'BOS'),
           ('Franny', 'DAL'),
           ('Zooey', 'CAK'),
           ('Walt', 'MIA'),
           ('Buddy', 'ORD'),
           ('Les', 'OMA')]

# LaGuardia airport in New York
destination='LGA'
```

Group Travel Planning

- schedule.txt
 - This file contains origin, destination, departure time, arrival time, and price for a set of flights

LGA, MIA, 20:27, 23:42, 169

MIA, LGA, 19:53, 22:21, 173

LGA, BOS, 6:39, 8:09, 86

BOS, LGA, 6:17, 8:26, 89

LGA, BOS, 8:23, 10:28, 149

Group Travel Planning

- Let's prepare a flights dictionary:

```
flights = {}  
  
for line in file('schedule.txt'):  
    origin, dest, depart, arrive, price = line.strip().split(',')  
    flights.setdefault((origin, dest), [])  
  
    # Add details to the list of possible flights  
    flights[(origin, dest)].append((depart, arrive, int(price)))
```


Representing Solutions

- There may be different alternatives.
- Should be generic enough so that any optimization algorithm may be used.
- List of numbers is a common representation.
 - Each number represents the flight a person takes

Example: [1, 4, 3, 2, 7, 3, 6, 3, 2, 4, 5, 3]



Printing a Solution

[illegible]

Printing a Solution

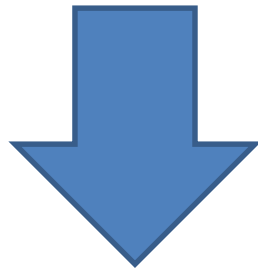
```
import optimization
```

```
s=[1, 4, 3, 2, 7, 3, 6, 3, 2, 4, 5, 3]
```

```
optimization.printschedule(s)
```

Printing a Solution

```
import optimization
s=[1, 4, 3, 2, 7, 3, 6, 3, 2, 4, 5, 3]
optimization.printschedule(s)
```



```
[1, 4, 3, 2, 7, 3, 6, 3, 2, 4, 5, 3]
Seymour      BOS   8:04-10:11  $ 95  12:08-14:05  $142
Franny       DAL  12:19-15:25  $342  10:51-14:16  $256
Zooney       CAK  10:53-13:36  $189   9:58-12:56  $249
Walt         MIA   9:15-12:29  $225  16:50-19:26  $304
Buddy        ORD  16:43-19:00  $246  10:33-13:11  $132
Les          OMA  11:08-13:07  $175  15:07-17:21  $129
```

The cost function

- **Price:** The total price of all the plane tickets, or possibly a weighted average.
- **Travel time:** The total time that everyone has to spend on a plane.
- **Waiting time:** Time spent at the airport waiting for the other members of the party to arrive.

The cost function

- **Departure time:** Flights that leave too early in the morning may impose an additional cost by requiring travelers to miss out on sleep.
- **Car rental period:** If the party rents a car, they must return it earlier in the day than when they rented it, or be forced to pay for a whole extra day.

The cost function

- After choosing some variables that impose costs, you'll need to determine how to combine them into a single number.
- How much money that time on the plane or time waiting in the airport is worth?

The cost function

- You might decide that:
 - it's worth spending \$1 for every minute saved on air travel (this translates into spending an extra \$90 for a direct flight that saves an hour and a half).
 - it's worth \$0.50 for every minute saved waiting in the airport.
- You could also add the cost of an extra day of car rental if everyone returns to the airport at a later time of the day than when they first rented the car.

Computing the Cost (Part 1)

```
def schedulecost(sol):  
    totalprice = 0  
    latestarrival = 0  
    earliestdep = 24 * 60  
    for d in range(len(sol) / 2):  
        # Get the inbound and outbound flights  
        origin = people[d][1]  
        outbound = flights[(origin, destination)][int(sol[2 * d])]  
        returnf = flights[(destination, origin)][int(sol[2 * d + 1])]  
  
        # Total price is the price of all outbound and return flights  
        totalprice += outbound[2]  
        totalprice += returnf[2]  
  
        # Each minute of flight duration costs $1  
        totalprice += getminutes(outbound[1]) - getminutes(outbound[0])  
        totalprice += getminutes(returnf[1]) - getminutes(returnf[0])  
  
        # Track the latest arrival and earliest departure  
        if latestarrival < getminutes(outbound[1]):  
            latestarrival = getminutes(outbound[1])  
        if earliestdep > getminutes(returnf[0]):  
            earliestdep = getminutes(returnf[0])
```

Computing the Cost (Part 2)

```
# Every person must wait at the airport until the latest person arrives.  
# They also must arrive at the same time and wait for their flights.  
totalwait = 0  
for d in range(len(sol) / 2):  
    origin = people[d][1]  
    outbound = flights[(origin, destination)][int(sol[2 * d])]  
    returnf = flights[(destination, origin)][int(sol[2 * d + 1])]  
    totalwait += latestarrival - getminutes(outbound[1])  
    totalwait += getminutes(returnf[0]) - earliestdep  
  
# Does this solution require an extra day of car rental? That'll be $50!  
if latestarrival < earliestdep:  
    totalprice += 50  
  
return totalprice + totalwait
```

The cost function

```
>>> reload(optimization)
```

```
>>> optimization.schedulecost(s)
```

Educated Optimization

- **Random Searching**
- Hill Climbing
- Genetic Algorithms
- Simulated Annealing

Random Search

```
def randomoptimize(domain, costf):  
    best = 9999999999  
    bestr = None  
    for i in range(1000):  
        # Create a random solution  
        r = [random.randint(domain[i][0], domain[i][1])  
              for i in range(len(domain))]  
        # Get the cost  
        cost = costf(r)  
  
        # Compare it to the best one so far  
        if cost < best:  
            best = cost  
            bestr = r  
  
    return bestr
```

Random Searching

- This function randomly generates 1,000 guesses and computes the schedule cost for each.
- It keeps track of the best guess (the one with the lowest cost) and returns it.

Random Searching

```
>>> reload(optimization)
```

```
>>> domain = [(0,9)]*(len(optimization.people)*2)
```

```
>>> s = optimization.randomoptimize(domain, optimization.schedulecost)
```

```
>>> optimization.schedulecost(s)
```

```
>>> optimization.printschedule(s)
```