dgswem-v2: User's Guide

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Introduction

This document aims to orient new users about the design of dgswem-v2. Before beginning to discuss what this document is, we will briefly preface what it is not. Firstly, this document does not contain installation instructions. Those can be found in the README.md file in the root directory of this repository. Secondly, this guide is not intended as an API reference. To see API documentation, we have annotated our functions using doxygen, which can be built via

```
cd ${dgswem-v2-root}/documentation
doxygen Doxyfile
```

Rather this document aims to achieve the following 3 goals:

- 1. Provide insight into the design philosophy of dgswem-v2,
- 2. Document input formats and intended usage through annotated examples.
- 3. Provide a reference for dgswem-users trying to get oriented in this new code.

1.1 Problems with dgswem

Before discussing the features of dgswem-v2, we will briefly dwell on the problems with the predecessor of this code. To quote George Santayana, "Those who cannot remember the past are condemned to repeat it".

1.1.1 Difficulty of Adding Features

The first two problems outline with dgswem center on issues surrounding developer productivity. The first issue is centered around the difficulty of adding features. This is partially centered around limitations of Fortran, but also partially a criticism of the code bases design.

The first point I would like to highlight is the difficulty associated with implementing new features is the difficulty in maintain old ones. One poignant

example of this can be found in src/DG_hydro_timestep.F. The code currently supports two timestepping mechanisms: Strong Stability Preserving Runge-Kutta (SSPRK) methods and Runge-Kutta Chebychev methods. In an attempt to preserve good performance, the methods can be swapped out at compile time using compiler macros. However, the SSPRK implementation spans roughly 170 lines of code, and the RKC implementation a similar number of lines. The issue now being that any modification that happens to one timestepping scheme needs to be duplicated below. This form of code duplication can be confusing and complicates supporting the full set of features in any given combination.

The second issue is a more underlying limitation of the use of Fortran. Steven Brus' work [?] demonstrates the drastic performance improvements made by the introduction of curvilinear elements. Due to the varying Jacobians, separate loops are required to update curvilinear elements. This would then require that two loops be written into dgswem. However, it is convievable that one might be interested in implementing quadratic elements as well. Now the number of loops grow in a comminatorial manner (linear/triangles, curved/triangles, linear/quadrilateral, and curved/quadrilaterals).

1.1.2 Not Testable

As a procedural code written in a traditional fortran manner. The data of the simulation are allocated as globally accessible structs of arrays. The global scoping of the structs obfuscates the actually dependencies. Developing a unit testing framework would require meticulous teasing out of explicit dependencies for a given function, and then furthermore require convoluted tests cases to achieve reasonable code coverage. In practice, previous attempts at implementing continuous integration testing for dgswem have centered around implementing correctness tests. While these would at least verify if adding a change to the code base doesn't compromise the correctness of the code, these tests fail to locate the source of the error.

1.1.3 Poor Fortran/C++ Interoperability

This problem has initially arisen out of the STORM project whose objective was to implement storm surge codes using HPX, an Asynchronous runtime system. One of the key difficulties in this project however, remains the interoperability of Fortran—what dgswem is written in – and C++—what HPX is written in. The works by Byerly et al. [?] illustrate some of the difficulties that go into this. However, this fix is places relatively restrictive limitations on what the code can do. Furthermore, the development of new C++ libraries present interesting solutions, which are currently not accessible to fortran based implementations. In particular, examples include explicit data parallel programming libraries such as Boost.simd and Vc, as well as novel GPU abstraction mechanisms such as Kokkos. While certainly pains have been taken to implement a dgswemhpx implementation. This is not really affordable, when looking at developer

cost. The choice of Fortran as a programming language restricts our abilities to explore novel solutions to HPC problems.

1.2 Proposed Solution

In an attempt to directly address the issues above dgswem-v2 has been design with the following features: written in C++14, object-oriented, and test driven design.

1.2.1 Written in C++14

The simplest solution to address issues with C++ interoperability is to write the application in C++. Additionally, we have chosen the C++14 standard. Typical reasons, for not using newer standards hinge around legacy support issues. However, since the code base is being rewritten in its entirety, we have no such limitations.

1.2.2 Object Oriented

One of the key features of C++ is it's support of object oriented programming. The main principal of object oriented programming is to partition the program into objects that are responsible for discrete tasks. This modularization allows users to work on one part of the code without having to worry about unintended effects in the rest of the code base. This is hopefully shorten the amount of time required for a new user to become productive. Additionally, it allows us to reasonably partition up the timesteppers. In terms of the previous example regarding the Runge-Kutta timesteppers, each time stepper would be implemented as a unique class, and its arguments would contain all the functionality required for function evaluations. This would allow a user to make a change in the code, and have it automatically propagated to both timesteppers, and expose an API that the user could use two develop a third timestepper.

1.2.3 Test driven design

The other advantage of object oriented programming is that it strictly scopes the data it's working on. This allows us to write tests for small units of code, e.g. integration or polynomial basis implementations. These changes will then hopefully indicate where and when code breaks greatly simplifying debugging. Additionally, existing continuous integration software allows us to run these unit tests for each commit. Allowing developers to precisely pinpoint the commit that broke functionality.

1.3 Target Audience

There certainly already exist a vast set of finite element libraries out there, e.g. deal.ii, dune, feel++. Certainly, there are a lot of arguments for using on of these libraries. However, ultimately we have settled on implementing their functionality ourselves. We are aiming to solve a much smaller subset of the problems these libraries attempt to solve. Libraries like deal.ii have quite intense dependencies, which we simply are not interested in at the moment. Furthermore, it is worth mentioning that dgswem-v2 isn't even library, but rather an application. Our target audience really falls into two user groups:

- 1. People who are interesting in modeling shallow water equations. In the same, spirit as addirc, we hope to provide the functionality, that might allow a coastal engineer to supply the code with a mesh geometry, and run a simulation.
- People who are interested in developing new numerical methods. The barebones API has been designed to expose hooks that mirror the numerical algorithms as closely as possible. The hope being that these hooks allow users to rapidly explore new algorithms.

1.3.1 Limitations

While attempts have been made to leave dgswem-v2's API as open as possible. It is important to list some of the governing principles. These principals dictate limitations with what can be naturally achieved with the code.

- 1. Adding new features should be more important than maintaining the best performance. While we certainly are not ignore performance in the design of dgswem-v2, it is of note that we should prefer flexibility of the code over diehard performance.
- 2. The code is centered around solving conservation laws using the discontinuous Galerkin Method. The main ramifications of this item, is that all of our solvers are set-up as explicit. Presumably, there would have to be significant refactoring to incorporate implicit solvers.

1.4 Remainder of the Guide

The remainder of this guide aims to underscore the design of dgswem-v2. The two main abstractions are the Mesh and Problem class. The Mesh class abstracting the underlying mesh, and the Problem abstracting the PDE/ discretization thereof. These two concepts are the intellectual pillars upon which dgswem-v2 is based. Thereafter, we include annotated examples, which will hopefully get users started.

This is followed-up with a description of the input format, and a chapter describing where dgswem functionality can be found in the new code.

Mesh class

2.1 Motivation

To understand, the design behind the Mesh class, we would like to begin by discussing one of the key problems currently faced in dgswem. The issue comes from Steven Brus' dissertation [?]. Brus goes on to show that the addition of curvilinear elements plays a significant role in obtaining high-order accuracy for real world problems. Simultaneously, these curvilinear elements incur a significantly higher computational cost. Thus in the interior of the finite element domain, where the solution doesn't exhibit mesh geometry to more computationally efficient standard affine elements suffice. While computationally straight forward, this approach provides a software engineering challenge. Namely, something like the volume kernel now needs to be split up into two loops, i.e.

Listing 2.1: Naïve implementation of curved and linear finite element kernel

```
for ( auto& elt : linear_elements ) {
   //Evaluate volume kernel for each linear element
}

for ( auto& elt : curved_elements ) {
   //Evaluate volume kernel for each curved element
}
```

This can quickly provide a software engineering headache. For instance, the addition of quadrilateral elements, would suddenly require that each time step cover 4 loops. The addition of more features will lead to more code bloat ultimately resulting in maintainable code. The main goal of the Mesh class is to address specifically the problem, mentioned above.

2.2 The Element Class

The object-oriented solution approach is based on the fact that the discontinuous Galerkin algorithm ultimately, simply applies integrals over the elements, remaining mathematically agnostic to the actually implementation of the approximation. This lends itself to a polymorphic implementation. The idea behind polymorphism being that functionally all elements should behave identically. Thus, if we can agree to an interface that we would like to expose. We should be able to accomplish everything in one loop over the elements without having to worry about what's happening under the hood.

Regardless of the type of element, we assume that for any given element, the approximated solution u^h is given in the form

$$u^h(x,t) = \sum_{i=0}^{N} u_n(t)\phi_n(x),$$

where ϕ_n is some basis. The approximated solution is determined by the evolution of the functions $u_n(t)$. For the Galerkin Method, this evolution is ultimately determined by ensuring that the residuals of the approximate solution is orthogonal to the space spanned by $\{\phi_n\}$. Thus the key functionality that every element must possess is that ability to compute integrals of the form

$$\int_{\Omega} f \phi_n \mathbf{x}$$

for an arbitrary function f. In practice these integrations are approximated by quadrature rules. However, this provides the basis for the interface, we would like to expose from a generic element class.

Listing 2.2: Generic Element API

That is to say if every element satisfied this API, we would be able to write the discontinuous Galerkin kernel with only one loop regardless of the element.

2.2.1 Strong Typing

C++ is a strongly typed language. Thus, in exposing any kind of polymorphism there are two options. (1) Dynamic polymorphism and (2) Static polymorphism. Dynamic polymorphism is typically achieved through the use of the virtual keyword. This approach is typically considered the most readable, and typically be preferred in a first attempt at an implementation. However, virtual objects typically can't be resolved by the compiler at runtime. This means that when the executable is running, the compiler maintains a virtual look-up table, which it uses to determine which implementation to call, when provided one of these virtual calls. The cost of this is that there is a virtual overhead associated with each of these calls. Additionally, the compiler may have trouble inlining and optimizing virtual function calls. Typically, when the function execution is large enough this overhead may be treated as negligible. But for our applications, these function calls are expensive enough that virtualization would seriously degrade performance.

The other typical approach is the use of static polymorphism. The idea being that we still maintain a unified API exposed by the class. However, now we specify the order in which we loop through the elements. That way the compiler is able to determine each of the function calls. Although ultimately, we will be able to get away with still only having one loop. The binary code generated should be equivalent to the code in Listing 2.1. Thus, static polymorphism provides us with the usage of dynamic polymorphism without the additional overhead. The downsides include a code base that is more difficult to maintain. However, given the performance critical nature of these function calls, this is a downside we've decided to accept.

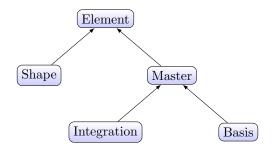


Figure 2.1: Composition of the Element classes.

2.2.2 Class Hierarchy of Element

The last subsection describes the exact decomposition of the element. In designing dgswem-v2, we attempted to think of all possible features that one might want to implement and provide encapsulation to allow for adding of new features without having to be familiar with the entire code base. Figure 2.1 describes the major constituents of the element class.

- Shape: The shape class deals with deformations from the master element to the actual orientation within the mesh. Here features such as curvature of the mesh (e.g. solving in spherical coordinates) or the element (e.g. isoparametric or isogeometric) should be implemented.
- Master: The master element is rather similar to the generic element class. It exposes integration hooks over the master element.
- Basis: This class encapsulates all basis information. Potentially additional choices of basis include Bernstein, modal, and bases on quadrilateral elements.
- Quadrature: This class contains all information required to approximate an integral over the master element.

In addition to adding features by providing new instances of these classes. There also still remains the ability to add classes through template specialization and SFINAE. These techniques allow for special implementations to be written in certain element compositions. For example, one of the large advantages of a Bernstein basis is the fast matrix inversion formula. Since this formula drastically deviates from linear elements, one might want to write a specific implementation for linear triangles using the Bernstein basis.

2.3 Mesh Class

With the decision to strongly type the elements in the Mesh class, the next task is to develop a container, which represents the mesh. This requires the ability to

iterate over interfaces, boundaries, elements, and distributed boundaries. The key object in allowing this to are the heterogeneous containers in the **Utilities** namespace. To explain, what in particular is happening in these containers assume we have three types of elements in our mesh: EltA, EltB, EltC. Morally, the heterogeneous vector can be written out as:

Now assuming, we have a function we would like to execute on each element regardless of type. We emulate the std::for_each API. So we will define a hook in the Mesh class, which will execute that function for every element in the Heterogeneous Vector. We have demonstrated what specifically we would like in Listing 2.3.

Listing 2.3: Moral implementation of iterating over Heterogeneous Vector

In dgswem-v2, this type of implementation can be generalized to arbitrary Hetereogeneous vectors through the use of template metaprogramming. However, ultimately, the code is effectively executing the above code. Allowing the compiler to generate these loops is precisely the issue we wanted to address. The definition of the kernels to be passed into the mesh class are problem specific and will be addressed in the next chapter. This mechanism is used for boundaries, internal interfaces, and distributed interfaces, in addition to elements. In understanding, this key concept the Mesh class becomes nothing more than a container. Detailed API descriptions are provided in the doxygen documentation.

Problem Class

Annontated Examples

Input Format

dgswem to dgswem-v2 Look-up Table

This chapter is aimed at helping users proficient with dgswem orient themselves in dgswem-v2. Table provides means to look up subroutines from dgswem and determine the location in dgswemv2. Certain functionality is not present at all in dgswem-v2. These files and subroutines therein have been omitted from the table. If you are searching for a subroutine from:

- \bullet dg.F
- Diff45_41.F
- flow_edge_sed.F
- fparser.F90
- fparser.F90
- global_3dvs.F
- globalio.F
- \bullet harm.F
- mkodal2nodal.F
- nodalattr.F
- parameters.f90
- pdg_debug.F
- sizes.F
- slopelimiter.F

- \bullet wind.F
- $\bullet \ write_output.F$

the desired functionality has not been implemented in dgswem-v2.

dgswem subroutine	dgswem-v2 equivalent function	Location in Repository
calc_normal	Shape::StraightTriangle::GetSurfaceNormal	source/shape/shapes_2D/shape_straighttriangle.cpp
check_errors	Not supported	
coldstart	Not supported	
create_edge_data	initialize_mesh_interfaces_boundaries	source/preprocessor/initialize_mesh.hpp
dg_hydro_timestep	Inlined	source/simulation/simulation.hpp
		source/hpx_simulation.hpp
		source/simulation/ompi_simulation.hpp
dg_timestep	Inlined	source/simulation/simulation.hpp
		source/hpx_simulation.hpp
		source/simulation/ompi_simulation.hpp
dgswem	main	source/simulation/simulation.hpp
		source/hpx_simulation.hpp source/simulation/ompi_simulation.hpp
abannian adam bardan	Not our out od	source/simulation/ompi_simulation.npp
ebarrier_edge_hydro edge_int_ldg_hydro	Not supported Not supported	
edge_int_ldg_sediment	Not supported Not supported	
errorelevsum		
	Not supported	
flow_edge_hydro	SWE::Flow::GetEX [†]	source/problem/SWE/swe_kernels_boundary_conditions.hpp
flow_edge_ldg_hydro	Not supported	
fort_dg_setup	Not supported	
Hllc_flux	Not supported	
hotstart	Not supported Not supported	
ibarrier_edge_hydro ibarrier_fluxes		
	Not supported	/ 11 /CXXID / 1 1
internal_edge_hydro	SWE::Problem::interface_kernel [†]	source/problem/SWE/swe_kernels_processor.hpp
internal_edge_ldg_hydro	Not supported	/ 12 /022777 / 12 / 12 / 12 / 12 / 12 / 12 / 12
land_edge_hydro	SWE::Land::GetEX [†]	source/problem/SWE/swe_kernels_boundary_conditions.hpp
land_edge_ldg_hydro	Not supported	
LDG_hydro	Not supported	
llf_flux	SWE::LLF_flux	source/problem/SWE/swe_LLF_flux.hpp
Message_abort	Not supported	
Message_fini	Inlined	source/problem/SWE/ompi_main_swe.cpp
message_init	Inlined	source/problem/SWE/ompi_main_swe.cpp
met_forcing	Not supported	
msg_blocksync_finish	Not supported	
msg_blocksync_start	Not supported	
msg_start_elem msg_table_elem	OMPICommunicator:InitializeCommunication OMPICommunicator::OMPICommunicator	source/communication/ompi_communicator.cpp
		source/communication/ompi_communicator.cpp
msg_types_elem	Not supported	
ncp_flux numerical_flux	Not supported Inlined	
nws112interp_region nws12get	Not supported Not supported	
nws12get nws12init	Not supported Not supported	
	Not supported Not supported	
nws12interp_basin ocean_edge_hydro	Not supported Not supported	
ocean_edge_hydro_post	Not supported Not supported	
ocean_edge_hydro_strict	Not supported Not supported	
ocean_edge_lldg_hydro	Not supported Not supported	
ocean_flow_edge_hydro	Not supported Not supported	
orthobasis	Basis::Dubiner_2D::GetPhi	source/basis/bases_2D/basis_dubiner_2D.cpp
ormobasis	Basis::Dubiner_2D::GetPhi Basis::Dubiner_2D::GetDPhi	source/ basis/ bases_2D/ basis_dubilier_2D.cpp
orthobasis_area	Basis::Dubiner_2D::GetPhi	source/basis/bases_2D/basis_dubiner_2D.cpp
OI tilobasis_area	Basis::Dubiner_2D::GetPhi	source/ basis/ bases_2D/ basis_dubilier_2D.cpp
	DanisDaniici_2DGctD1 iii	
orthobasis edge	Basis: Dubiner 2D: CetPhi	source/basis/bases 2D/basis dubiner 2D con
orthobasis_edge p_enrichment	Basis::Dubiner_2D::GetPhi Not supported	source/basis/bases_2D/basis_dubiner_2D.cpp

para_min	Not supported	
para_sum	Not supported	
prep_DG	initialize_mesh	source/preprocessor/initialize_mesh.hpp
prep_slopelim	Not supported	
quad_pts_area	Integration::Dunabant_2D::GetRule	source/integration/integrations_2D/integration_dunavant_2D.cpp
quad_pts_edge	Integration::GaussLegendre_1D::GetRule	source/integration/integrations_1D/integration_gausslegendre_1D.cpp
radiation_edge_hydro	Not supported	
radiation_edge_ldg_hydro	Not supported	
read_fixed_fort_dg	Not supported	
read_input	InputParameters::InputParameters	source/preprocessor/input_parameters.hpp
read_keyword_fort_dg	Not supported	, , , , , , , , , , , , , , , , , , , ,
rhs_dg_hydro	SWE::Problem::volume_kernel [†]	source/problem/SWE/swe_kernels_processor.hpp
3 %	SWE::Problem::source::kernel [†]	
rhs_ldg_hydro	Not supported	
rk_time	Stepper::Stepper	source/simulation/stepper.cpp
roe_flux	Not supported	/ / ** **
scrutinize_solution	SWE::Problem::scrutinize_solution_kernel [†]	source/problem/SWE/swe_kernels_processor.hpp
sta_basis	Integration::Dunabant_2D::GetRule	source/integration/integrations_2D/integration_dunavant_2D.cpp
sta_location	Not supported	
tidal_potential	Not supported	
updatei_elem	Not supported	
updatelz_elem	Not supported	
updatemz_elem	Not supported	
updater_elem	Not supported	
updater_elem_mod	OMPICommunicator::SendAll	source/communication/ompi_communicator.hpp
<u>r</u>	OMPICommunicator::ReceiveAll	Tr
	OMPICommunicator::WaitAllSends	
	OMPICommunicator::WaitAllReceives	
updater_elem_mod2	OMPICommunicator::SendAll	source/communication/ompi_communicator.hpp
•	OMPICommunicator::ReceiveAll	
	OMPICommunicator::WaitAllSends	
	OMPICommunicator::WaitAllReceives	
updater_elem_mod3	OMPICommunicator::SendAll	source/communication/ompi_communicator.hpp
	OMPICommunicator::ReceiveAll	
	OMPICommunicator::WaitAllSends	
	OMPICommunicator::WaitAllReceives	
wetdry	Not supported	
write_results	SWE::Problem::extract_VTK_data_kernel	source/problem/SWE/swe_kernels_postprocessor.hpp
	SWE::Problem::extract_modal_data_kernel	

Table 6.1: The names of Fortran subroutines with the corresponding dgswem-v2 function calls and the location of their implementation. Not supported routines are not implemented in dgswem-v2. The dagger (†) signifies that a given implementation is defined element-wise, whereas typical dgswem implementations loop over the entire mesh.