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# Theory of Computation Notes

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[KMV (DU)]

## Computer Science Notes

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## Ch-2- Languages

$\lambda \rightarrow$  string with length 0

$\emptyset \rightarrow$  A lang. with no. words

$L_1 = \{\lambda\}$  - finite Lang.

$L_2 = \{0, 00, 000, 0000, \dots\}$  infinite Lang.

Lexicographic order - (increasing order of length)

## Theory of formal languages

The word formal refers to the fact that all the rules for lang. are explicitly stated in terms

of word string of symbols occur

The formal rules use here emphasize its form of symbols that we interested in not

the meaning

certain specific set of strings of char. from the alphabets

Ex - I eat one apple

I eat three books  $\rightarrow$

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In a formal languages, we must allow this string because it is grammatical correct.

Meaning is something that we don't refer to in formal languages.

For ex. palindrome  $\Sigma = \{a, b\}$   
over alphabet

$\lambda$  - NULL

a	a a	a a a
b	ab	bab
aa	ba	bbb
bb	ab	aaa

Kleene closure or Kleene star -

Given an alphabet  $\Sigma$  a lang. is define in which any strings of letters from  $\Sigma$  is a word if even the same lang. is closure of the alphabet.

$$\Sigma^* = \{\lambda, a, b, aa, ab, ba, bb, \dots\}$$

$$\Sigma = \{a\}$$

$$\Sigma^* = \{\lambda, a, aa, aaa, aaaa, \dots\}$$

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$$\Sigma = \{a, b\}$$

$$\Sigma^* = \{ \lambda, aa, ab, ba, bb, \dots \}$$

$$\Sigma = \emptyset$$

$$\Sigma^* = \{\lambda\}$$

$$\Sigma = \{a, b\}$$

$$\Sigma^* = \{ \lambda, ab, aa, ba, bb, \dots \}$$

It also a closure. The diff. is null  $\lambda$ .

$$S = \{a, ab\}$$

$$S^* = \{ \lambda, a, aa, ab, \dots \}$$

Consider a set  $S = \{ab, ba\}$

$$S^* = \{ \lambda, ab, ba, aa, bb, ba, aab, bab, abb, \dots \}$$

$$S^* = \{ \lambda, ab, aa, ab, ba, bb, aab, aab, aba, \\ ab, baa, bab, bba, bbb, \dots \}$$

Some you can write

$$S = \{0, 1, 01\}$$

$$S^* = \{ \lambda, 0, 1, 01, 00, 010, 10, 11, 000, 001, 0100, 0101, 100, 101, 110, 111, 0000, 0001, 0010, 0100, 0101, 1000, 1001, 1010, 1100, 1101, 1110, 1111, \dots \}$$

Theorem 1 → We have for any set  $S$  of strings we have

$$S^* = S^{*\infty}$$

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$$S^* = \{ \lambda \text{ } a \} aa ab ba bb \dots \}$$

$$S^{*k} = \{ \lambda \text{ } a^k a^k a^k b^k b^k b^k \dots \}$$

$$S^{**} \subset S^*$$

$$S^* \subset S^{**}$$

problem (to 6, 9, 11 (do by self))

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## Ch-4 Regular Expression -

Regular Exp.

$$L_1 = \{ x^n \mid n=0, 1, 2, 3, \dots \}$$

1, 3, 5, 7, ...      a

$$\{ \lambda \text{ } a \text{ } aa \text{ } aaa \dots \} \quad a^*$$

b

$$\Sigma = \{ a \} \quad a^*$$

$$\Sigma^* = \{ \lambda \text{ } a \text{ } aa \text{ } aaaa \dots \} \quad a^*$$

b\*

$$aa^* = \{ a \text{ } aa \text{ } aaaa \dots \} \quad a^*$$

a\*b

some [ it is compulsory in every part (a+b)\* ]

$$a^*a = \{ \dots \} \quad a^*$$

$$ab^* = \{ a \text{ } ab \text{ } abb \text{ } abbb \dots \}$$

$$ba^* = \{ a \text{ } ba \text{ } bba \text{ } bbba \dots \}$$

$$a^*b^* = \{ a \text{ } a \text{ } b \text{ } aa \text{ } ab \text{ } ba \text{ } bb \dots \}$$

$$b^*a^* = \{ a \text{ } b \text{ } aa \text{ } bba \text{ } bbb \dots \}$$

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$a+b \rightarrow$  either  $a$  or  $b$  not null

$$(a+b)(a+b) = aa ab ba bb$$

$\nwarrow$   $\nearrow$

$$aa+ab+ba+bb$$

$$(a+b)(a+b)(a+b) = aaaa aabb abbb baaa babb$$

... all combination of 3 }

$$(a+b)^* = \{ a, b, aa, ab, ba, bb, \dots \}$$

$$a(a+b)^* = \{ a, aa, ab, \dots \}$$

$$(a+b)^*a = \{ a, aa, ba, \dots \}$$

$$a^* b^* ] \text{ not same} = \{ a, b, ab, bb \}$$

$$(ab)^* = \{ a, ab, abb, abbab, \dots \}$$

complete string

$$ab^*a = \{ a, aa, ab, abba, abbb, \dots \}$$

$$a(aa)^* = \{ a, aaa, aaaa, \dots \}$$

$$(aa)^*a = \{ \dots \}$$

$$a(a+b)^*a =$$

$$a(a+b)^* + (a+b)^*a =$$

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$$\leq = \{ a, b, c \}$$

$$T = \{ a, c, ab, cb, abb, cbb, abb, \\ cbbb, \dots \}$$

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All the words in T begin with a & c and then are followed by some no. of b.

Some are written

$$(a+c) b^*$$

Consider a language

$$L = \{aaa, aab, aba, abb, baa, bab\}$$

Some expression on  $(a+b)(a+b)(a+b) \neq (a+b)^3$

All words that begin a and end with b

$a (a+b)^* b$	$a a^* b^* b$
ab	ab
aab	aab
abb	abb
aab	aab
abb	abb
bab	bab
bbb	bbb

All these expression are language defining expressions and these are regular expression.

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The corresponding languages that define are

Task should be to generalise this

3rd Periodic exam

 $\wedge$ 

a

b

+

c

)

\*

The symbols are appear in regular exp. are the letters of alphabet signs. The symbol ( $\wedge$ ) of  $\wedge$  sign ( ) operator and the + sign.

Set of reg. expression is defined by the foll. rules.

Rule-1 - Every letter of sigma can be made into a reg. expression.

NULL itself is a reg. expression.

Rule-2 - If  $\lambda_1$  and  $\lambda_2$  are reg. expression then  $\lambda_1$  and  $\lambda_2$

(i)  $(\lambda_1)$

(ii)  $\lambda_1 \lambda_2$

(iii)  $\lambda_1 + \lambda_2$

(iv)  $\lambda_1^*$

are reg. exp.

Rule-3 - Nothing else is a reg. expression.

An expression  $(a+b)^* a (a+b)^*$

all strings with  $a$  and all without  $a$

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$$(a+b)^*$$

$$(a+b)^* \cdot a \cdot (a+b)^* + b^*$$

The language of all words that have atleast 2 a

$$(a+b)^* \cdot a \cdot (a+b)^* \cdot a \cdot (a+b)^*$$

All the words with exactly two a's

$$b^* a a b^* \cdot b^* a b^* a b^*$$

$$(a+b)^* \cdot a a \cdot (a+b)^*$$

If S and T are sets of strings of letter whether they are finite or infinite then define the product ST here all combination of string from S concatenated with a string from T in that order

For exp -

Set S as {aa, aab, aabaa}

T = {bb, bbb}

then ST is

$\{aababb, aabb, aabbbb, aabbaabb, aabbaabbb\}$

Language associated with reg. expression

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Lang. is associated with regular expre.

Following rules define the language associated with any regular expre.

Rule-(1) The language associated with reg. expression that is just a single letter is that one letter was along. And the language associated with NULL symbol () is just NULL a word language.  $L = \{\lambda\}$

Rule-(2) If  $R_1$  is a reg. exp. associated with the language  $L_1$  and  $R_2$  associated with the language  $L_2$ .

then

(i) the Reg. expression  $(R_1)(R_2)$  is associated with the product language  $L_1 L_2$ , i.e., the language  $L_1$  times  $L_2$ .

(ii) the Reg. exp.  $(R_1 + R_2)$  is associated with the language form by the union of the sets  $L_1, L_2$ .

(iii) the language assoc. with reg. expression  $(R_1)^*$  give  $L_1$  Kleen closure of the set  $L_1$  as a set of words.

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 These collection of rules proves recursively  
 there is some language associated  
 with neg. expression.

If  $L$  is a finite language then  $L$  can  
 be define by a Reg. expression  
 in other words are all finite lang.  
 are regular.

$$L_1 = \{a, ab\} = a + ab$$

$$L_2 = \{ab, ba, bb\} = ab + ba + bb$$

Set of strings of A and B's that at a  
 some point contain a double letter

$$\Sigma = \{a, b\}$$

$$aa, (a+b)^*$$

$$(a+b)^* aa$$

$$(a+b)^* aa (a+b)^*$$

$$(a+b)^* bb (a+b)^*$$

$$(a+b)^* (aa+bb)(a+b)^*$$

$$Ex - (A+B^*)^* (a+b)^*$$

Both are same or diff.

$$(a+b)^* (a^* b^*)^*$$

Same

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The language of all words without a 'aa'. Your exp. must give a

$$b^* (abb^*)^* (a+a)$$

Q Aug -

\* Even-Even (Language)

$$[(aa+bb+(ab+ba)) (aa+bb)^* (ab+ba)]^*$$

$$(aa)^*$$

$$(bb)^*$$

$$(ab+ba)(aa+bb)^* (ab+ba)$$

baa

aaa

baab

aab

baba

aba

bab

abb

bbaa

baaa

bbab

bab

bba

bba

bbbb

bbbb

Ch-4 - Q-1 to 11 - Handwritten

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16 Aug Finite Automata / (Autonation) (FA)

Pc's are setup on a playing board. Dices are thrown and a no. is generated at random depending on the no. the pc's on the board must be rearranged in a fashion completely specified by the rules. Everything is determined by the dices. We know that PC's are finite.

State | Initial State

1st step 2nd step 3rd step

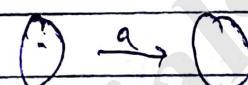
Finite Automata is also called Lang.

Accepting

read

read

read



initial  
state

final state

Accepting state

↓  
read → read

If we reach initial to final then input is accepted else rejected

Finite Automata - because no. of possible states and no. of letters are both finite. Automaton is closed if states is totally governed by the input.

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Finite Automata - A finite automata <sup>is</sup> a collection of 3 things -

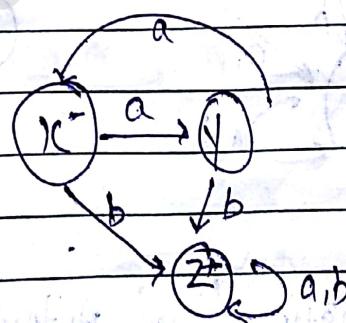
(1) A finite set of states, one of which is designated as initial state called the start state. and some (may be none) of which are designated as final states.

(2) An alphabet  $\Sigma$  of possible input letters

(3) A finite set of transitions that tell for each state and for each letter of the input alphabet which state to go to next.

Ex:- Consider

	a, b	set of alphabet
$x^-$	$y^-$	
set of state	$\Sigma$	$\Sigma^*$
$2^+$	$2^+$	Transition table



aaa	accepted
abb	
aaaab	

$$(a+b)^* \cap (a+b)^*$$

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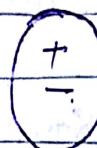
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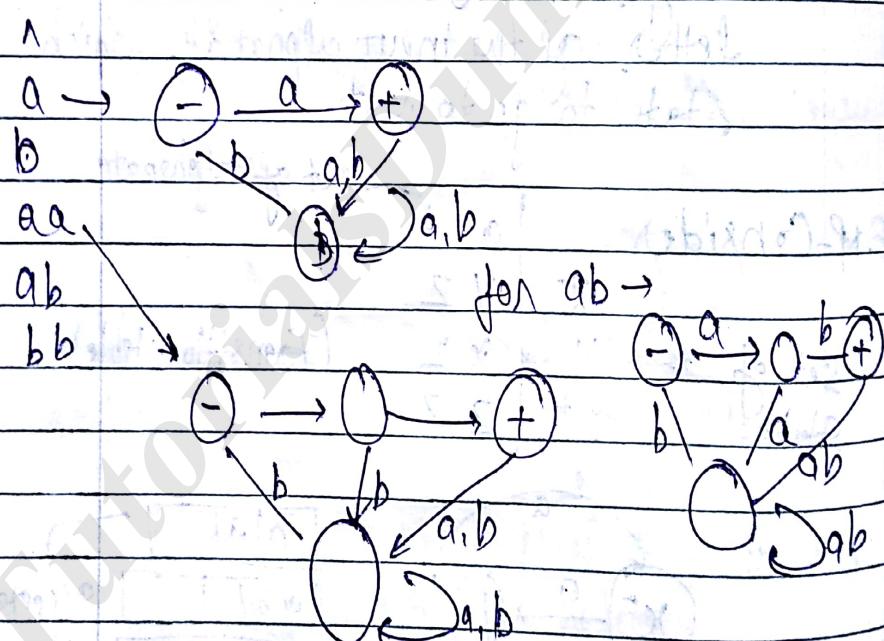
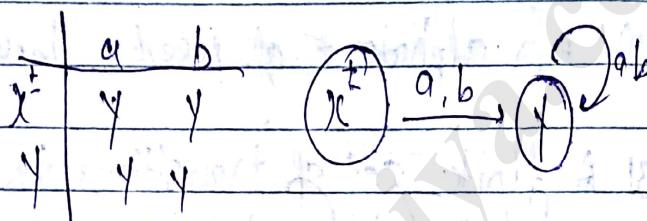
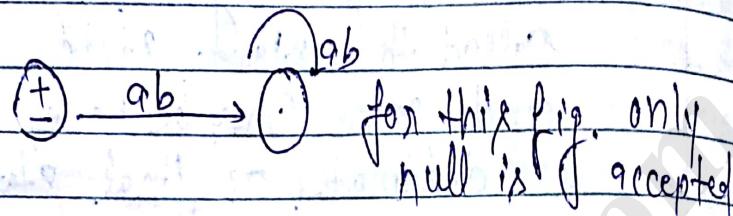
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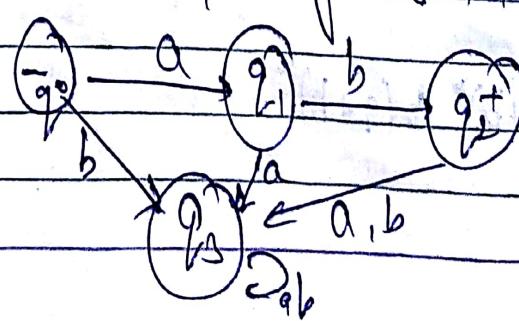
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→ Initial and final state is same mean null is accepted



DFA (Deterministic final Automata) →

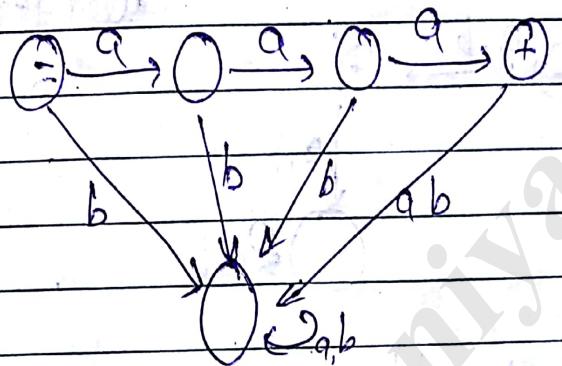


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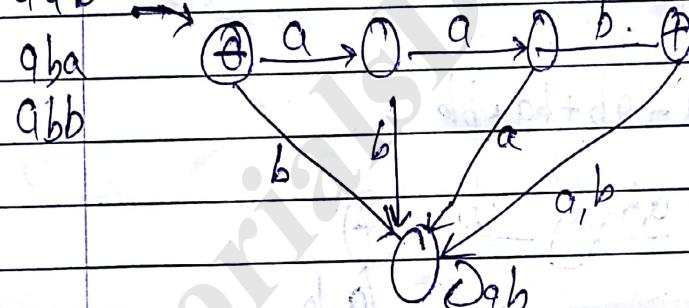
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	a	b
q0	q1 q3	
q1	q2 q2	
q2	q3 q3	
q3	q3 q1	

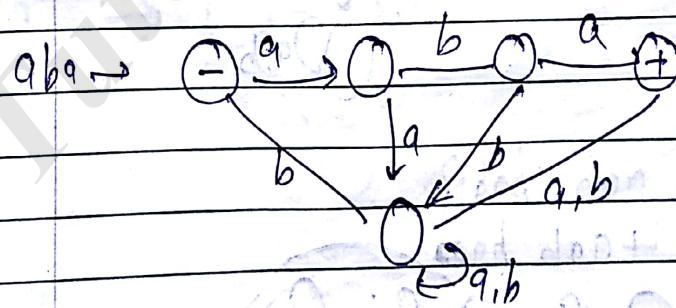
aaa -



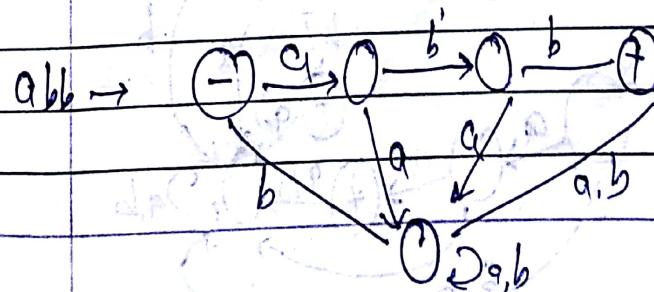
aab



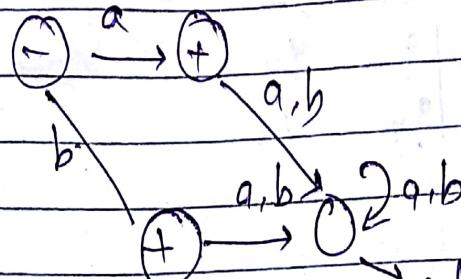
bab



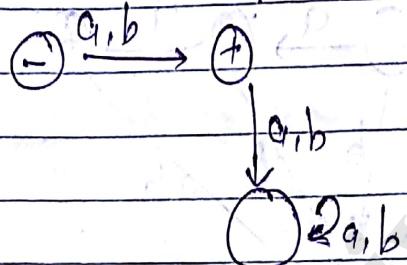
bbb



for  $a+b$



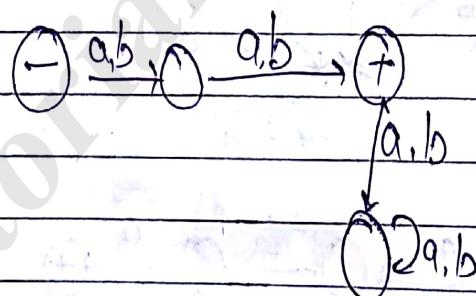
or



Called dead state

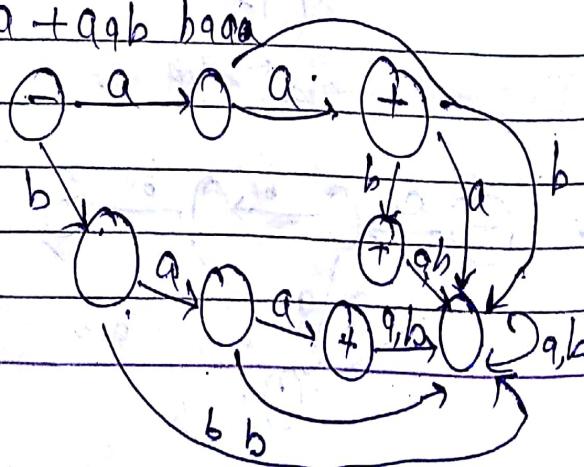
Try  $[aa+ab+ba+bb]$   
these  $(a+b)(a+b)$

8 Aug  $aa+ab+ba+bb$



{aa, aab, baa}

aa + aab baa



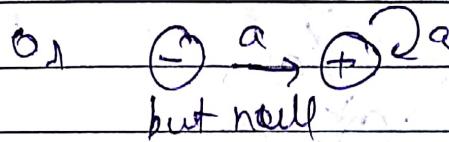
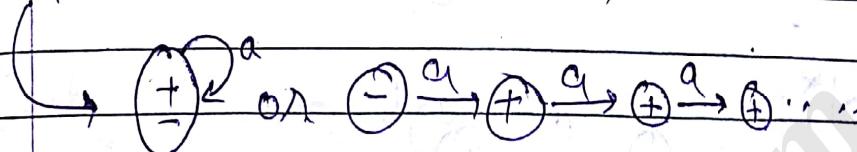
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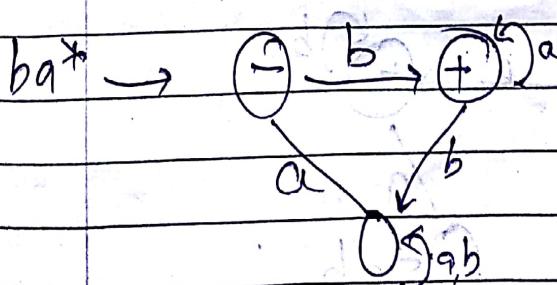
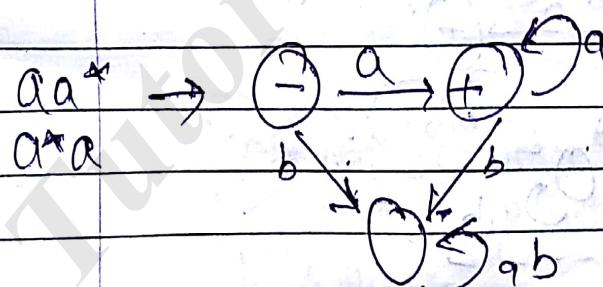
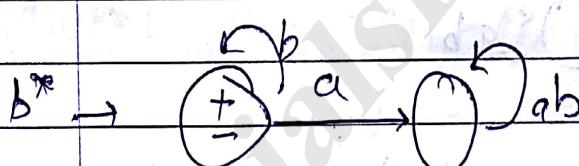
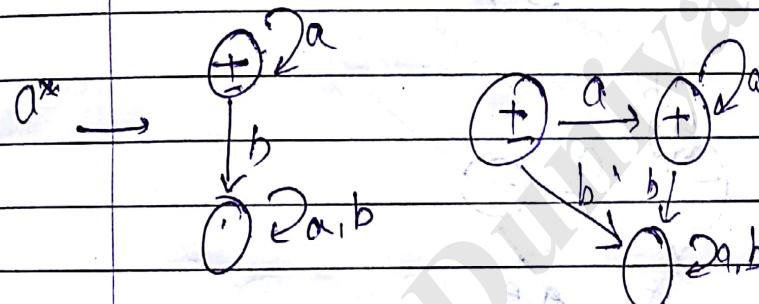
a

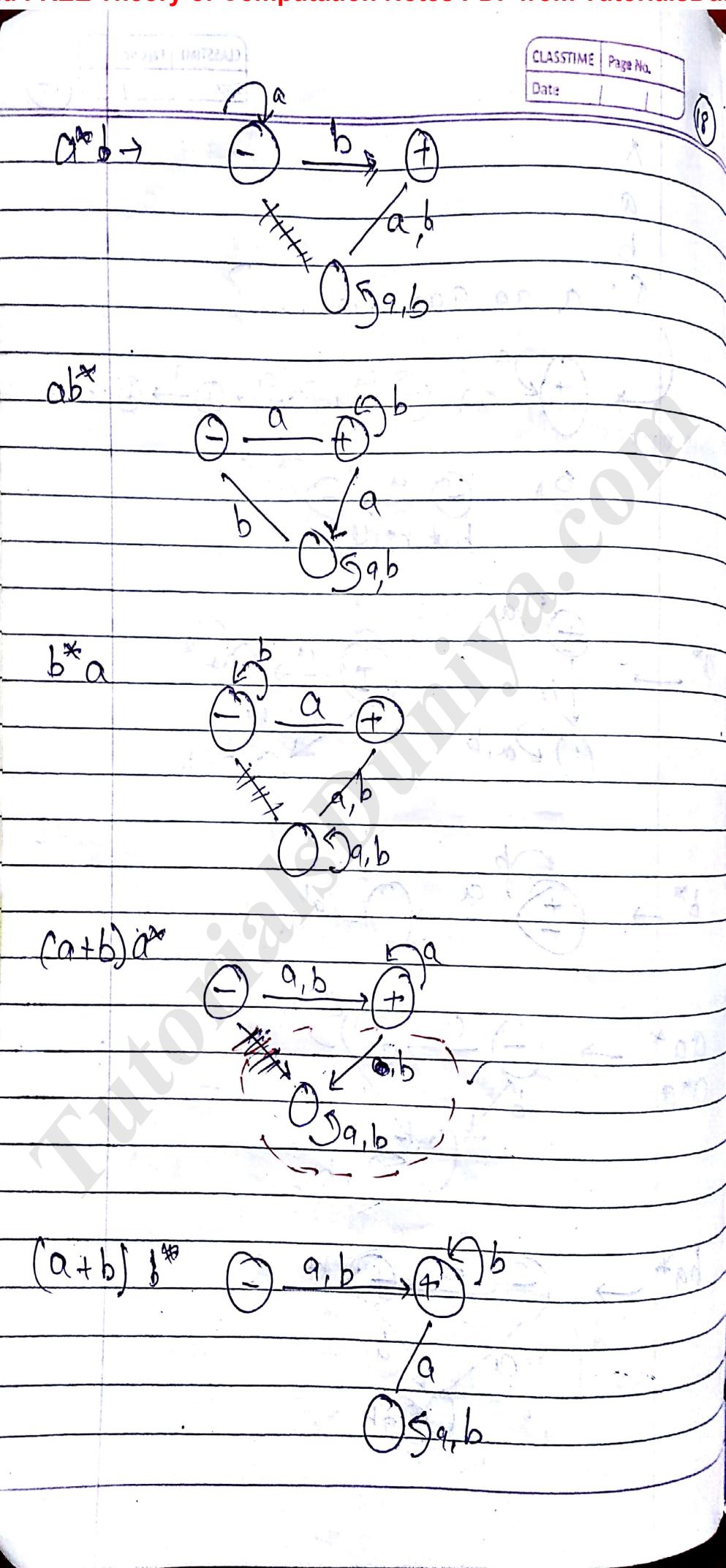
b

$\{1, 0, 0, 0, 0, 0, \dots\}$



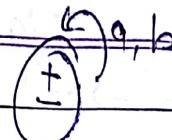
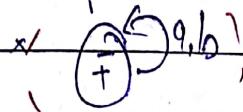
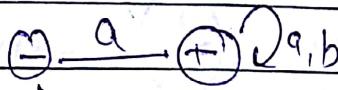
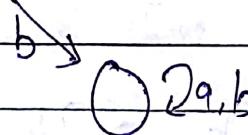
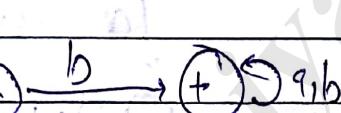
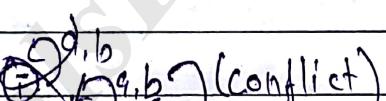
but now



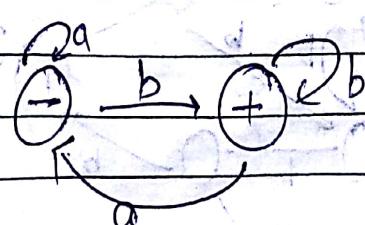


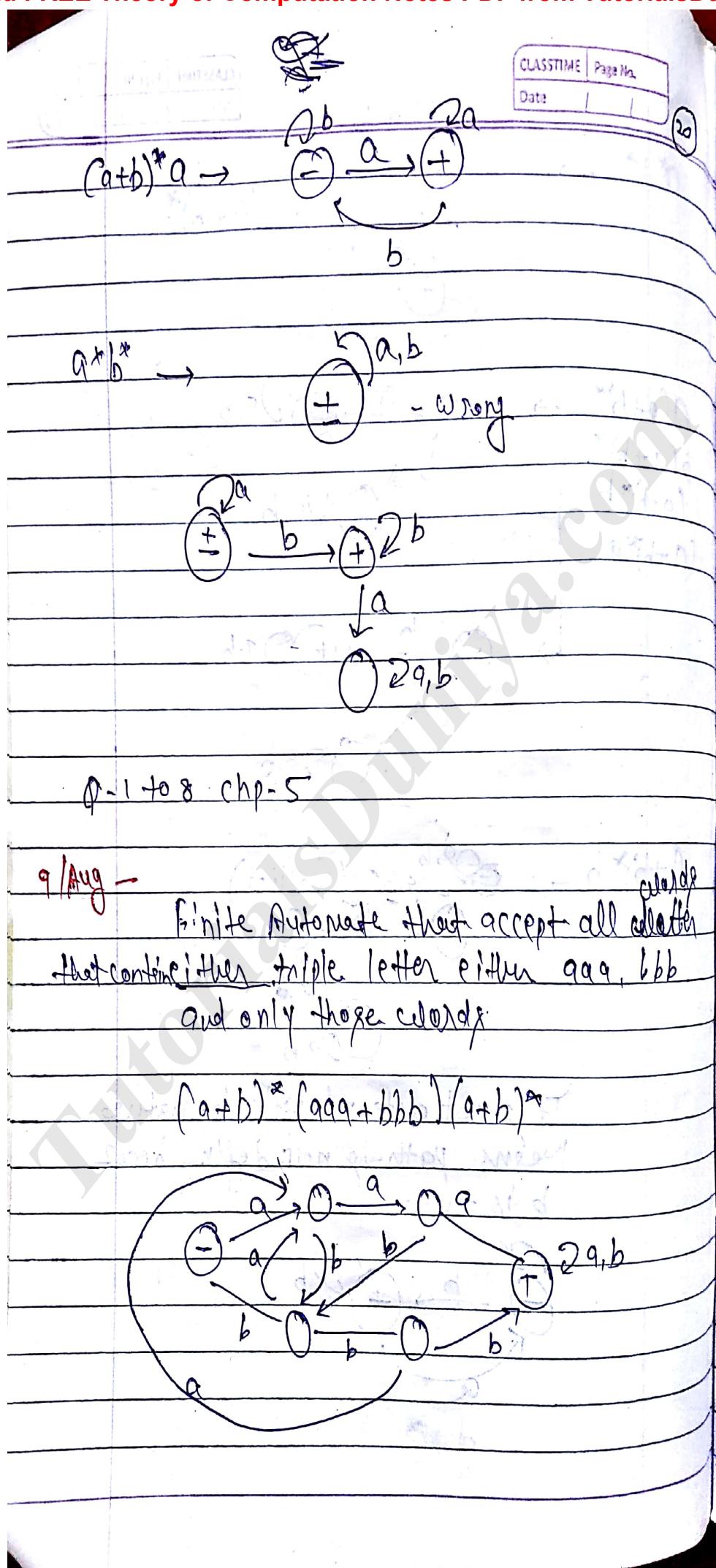
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 $a^* b^*$  $(a+b)^*$  $a(a+b)^*$  $b(a+b)^*$  $(a+b)^* b$  $(a+b)^* a$  $(a+b)^* b \rightarrow$ 

If is not deterministic in nature  
Means path is not define bcoz  
b is there





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## Definition of Transition Graph — (TG) —

Invented by John Myhill

A Transition Graph (TG) is a collection of three things —

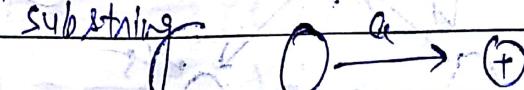
(i) A finite set of state at least one of which is designated as start state and some

(2) An alphabet ( $\Sigma$ )

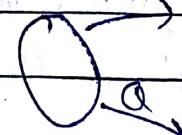
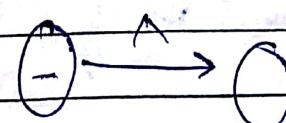
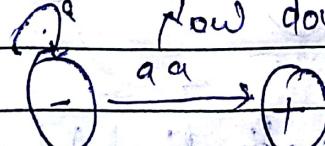
(3) A finite set of transition that show how to go from some states to some others based on reading specified sub string of input letters, (possibly even the null string)

$$\emptyset \subseteq S$$

sub string



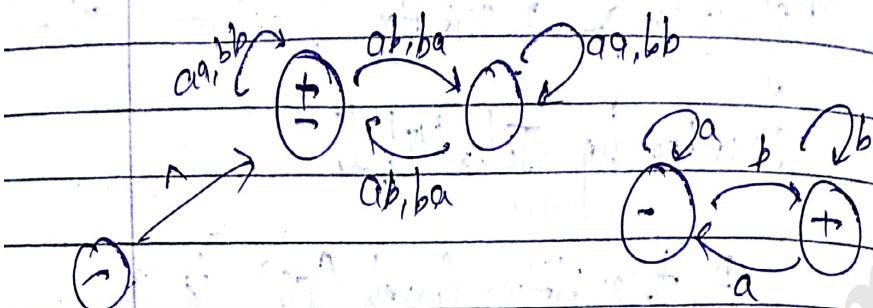
Now double element



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A TG like this



G.T.G. (Generalized Transition Graph) —

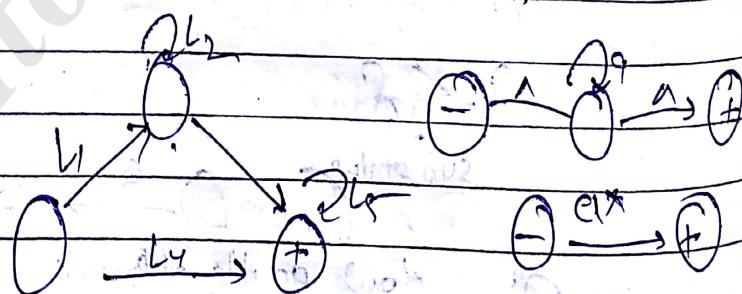
is a collection of three things

(1) A finite set of states in which at least one is start state and some (may be one or more) are final states

(2) An alphabet  $\Sigma$  of input letters

(3) Directed edges connecting some pair of states, each labeled with a regular expression.

For ex — It will allow



DFA (Deterministic Final Automata)

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## Chapter-7 (Kleen's theorem)

Any lang. can be defined by reg. expression, finite automata or TG  
can be define by all three methods.

R.E.

F.A.

T.G.

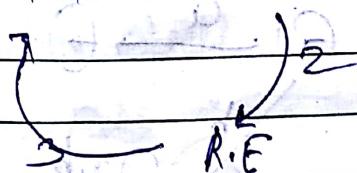
21/8/18 three parts —

part-1 - Every lang. can be define by finite automata and also by TG.

part-2 - Every lang. that can be define by TG can also be define by regular expression.

part-3 - Every lang. that can be define by regular expression that can be define by final automata.

F.A.  $\rightarrow$  T.G



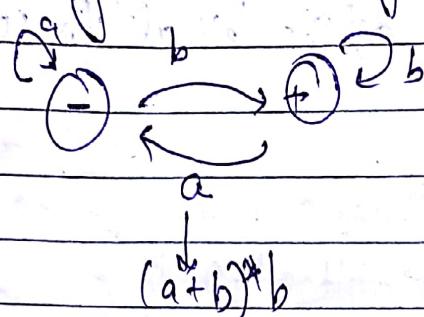
every finite automata is itself already  
isomorphic with TG.

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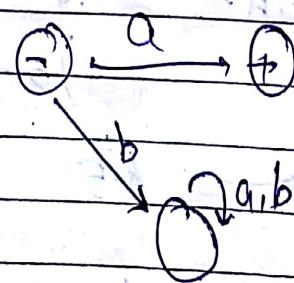
Any lang. that can be define F.A  
that already been defined by TG

Turning TG into regular expression



This part will be or proof done by  
converting - constructive algo. which  
means we represent a procedure  
that starts out a TG and end  
with a reg. expression, that  
define the same language

Any algo. must satisfy a criteria  
(+) It must work every conceivable  
TG. And it must guarantee to  
finish its job in a finite time

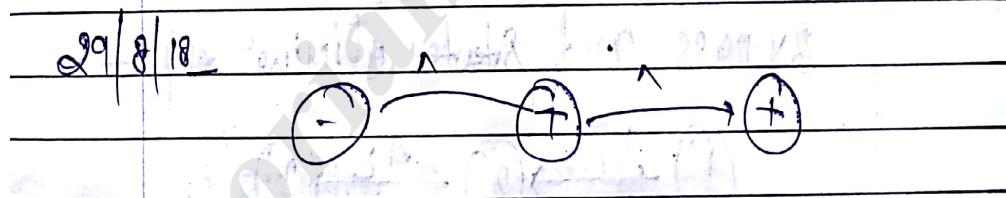
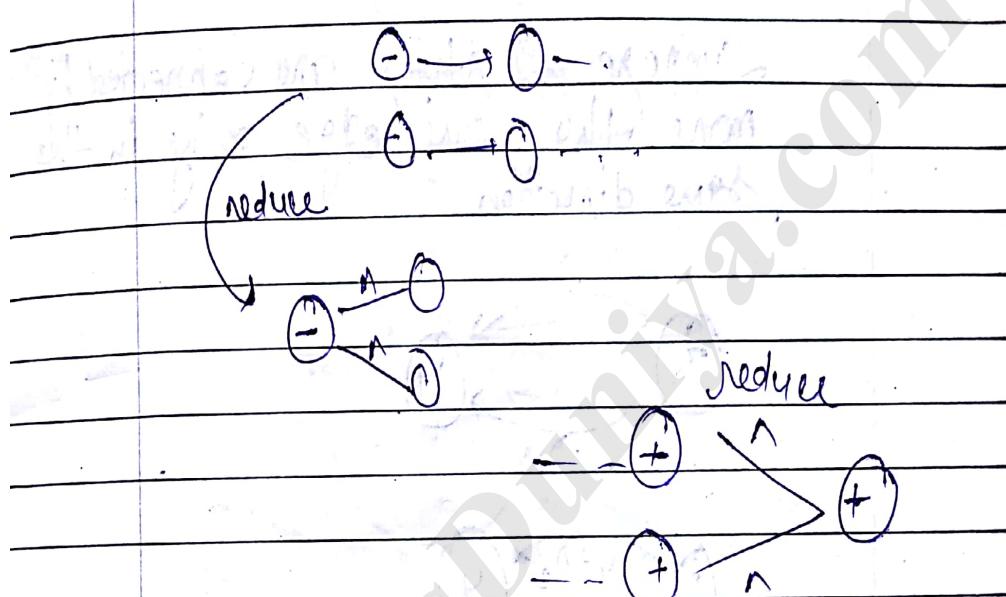
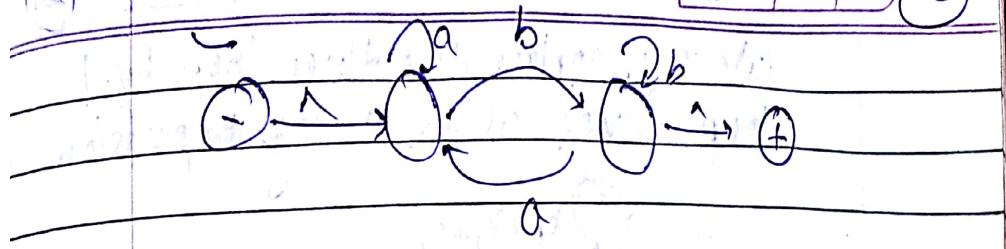


$\ominus (a+b)^*b \rightarrow \oplus$  (reduce graphs  
a/bone)

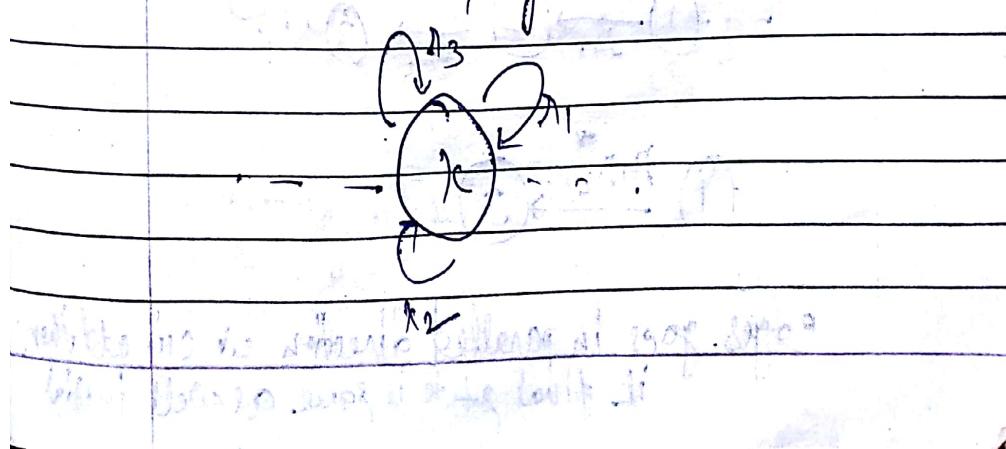
Page No. 106 (given an algo.)

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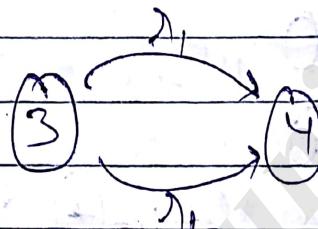
Suppose  $T$  has some state that has more than one loop circling back to itself.



We can replace the three loop by 1 loop level with a reg. expression

$$\rightarrow \text{--- } x \text{ ---} \xrightarrow{x_1 + x_2 + x_3}$$

Suppose 2 states are connected by more than one edge going in the same direction.

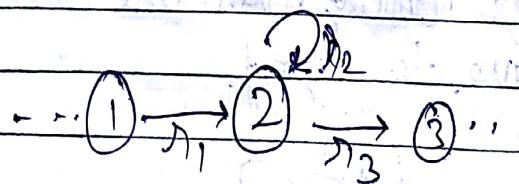


$$\xrightarrow{x_1 + x_2} \text{--- } 4 \text{ ---}$$

Bypass and state elimination exp -



$$\text{--- } 1 \xrightarrow{x_1} 2 \xrightarrow{x_2} 3 \text{ ---}$$

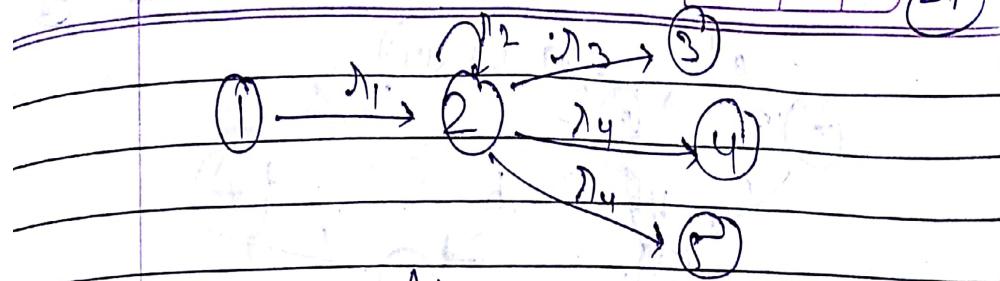


$$\text{--- } 1 \xrightarrow{x_1} 2 \xrightarrow{x_2} 3 \text{ ---}$$

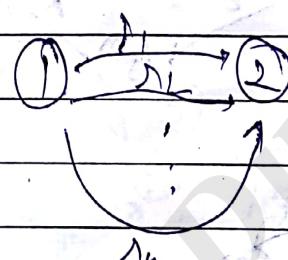
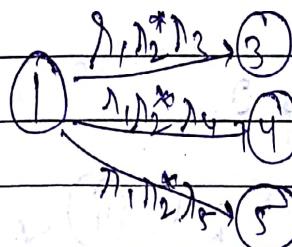
Edges goes in parallel direction we can add them if final state is same as well initial

We can eliminate anything as we want  
but the final result will agree

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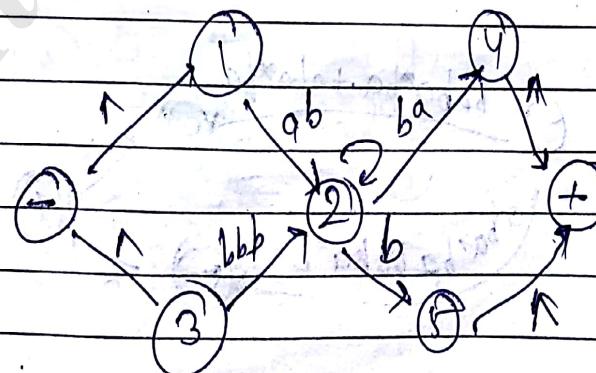


Here we can eliminate  $\lambda_2$



$$(1) \xrightarrow{\lambda_1 + \lambda_2 + \dots + \lambda_n} (2)$$

Consider a T-Graph



If we eliminate 1  
then result is

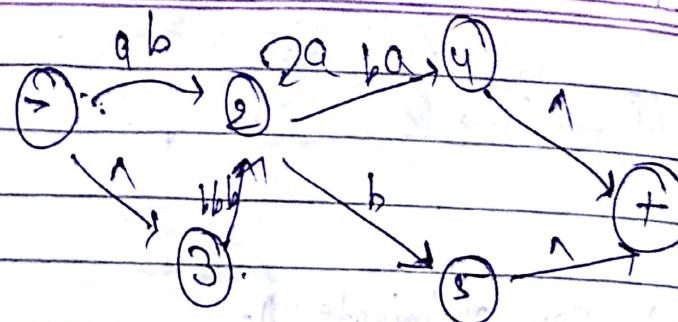
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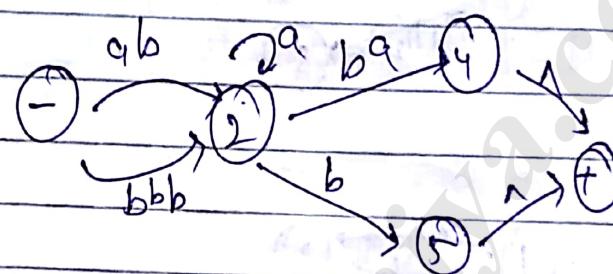
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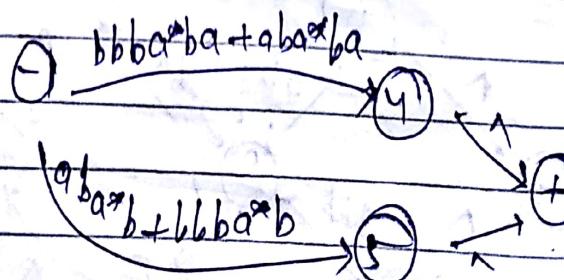
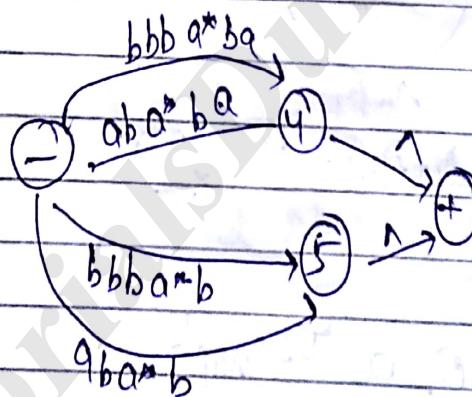




If we remove 3



Remove 4



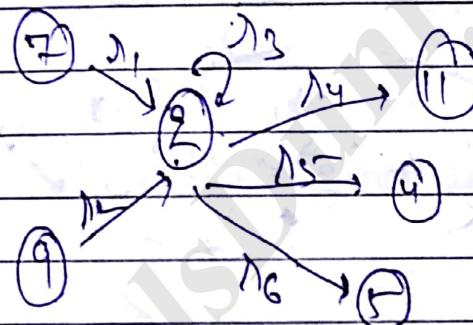
Remove 4 then 5  
then result is

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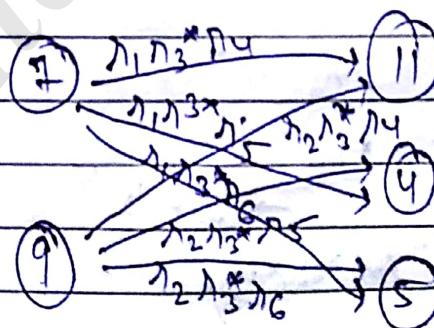
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 $bba^*ba + aba^*ba$ 
 $\oplus$   $a b a^* b + b b b a^* b$   $\oplus$ 
 $\oplus$   $bba^*ba + aba^*ba + a b a^* b + bbb a^* b$   $\oplus$ 

Consider another case

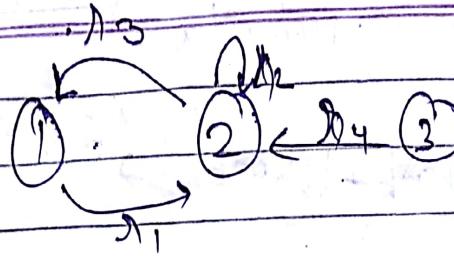


eliminate state 2



We have some special cases

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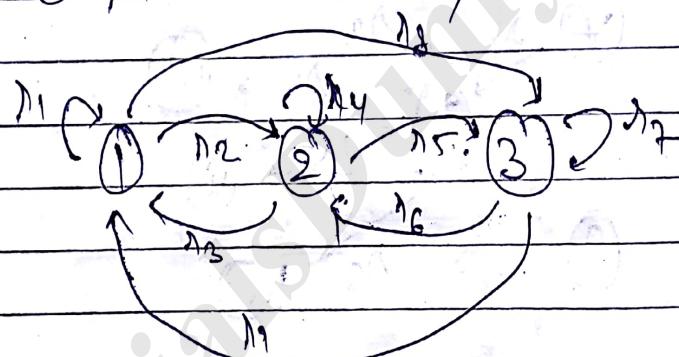


Remove 2 & state

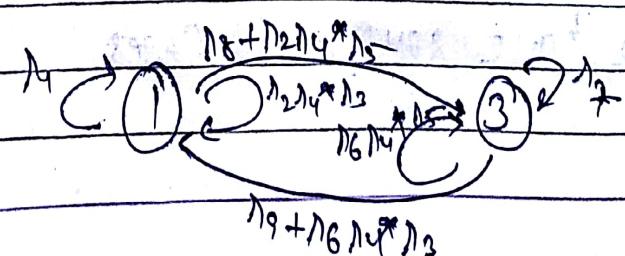
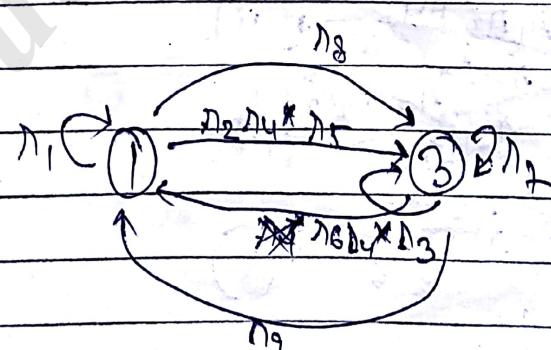
Connect incoming to outgoing edges

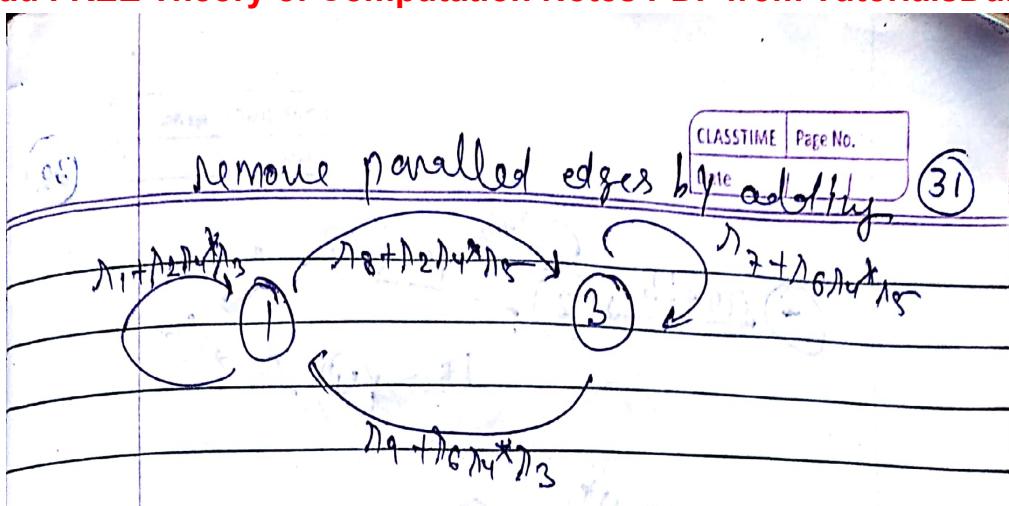


Consider another case

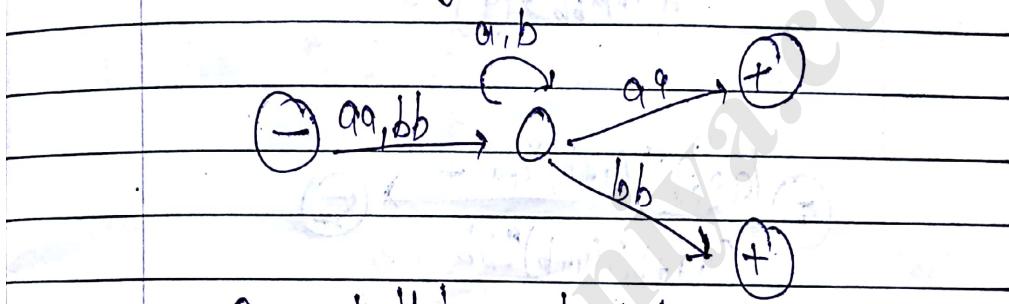


eliminate state 2



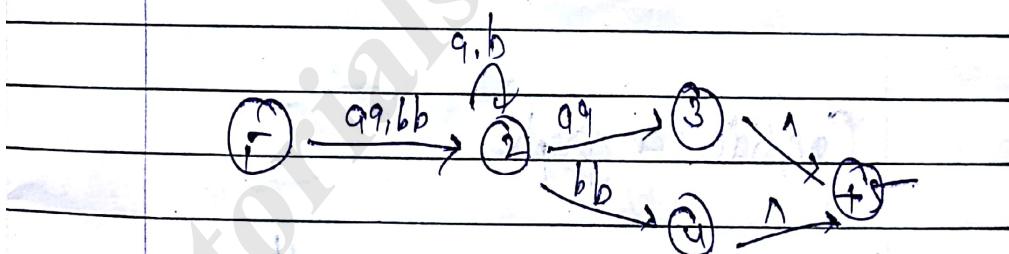


Consider a graph

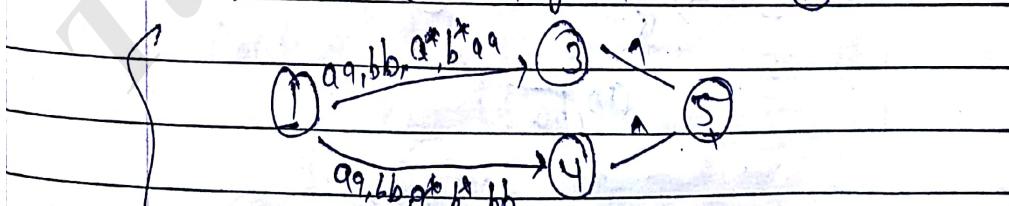


Convert this graph into regular exp.

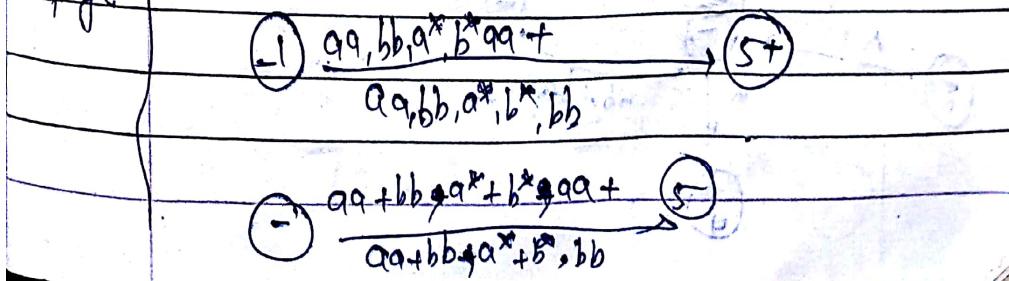
We can have only one final state. So add transition  
 $aa + bb + a^* + b^* + aa + bb$  edge



Remove 2 because we want final  $\textcircled{3} \rightarrow \textcircled{4}$

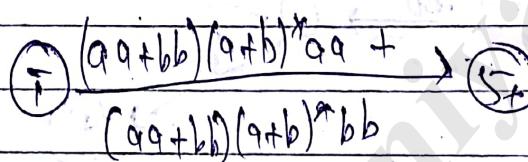
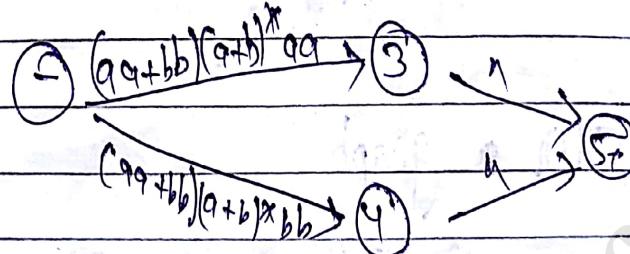
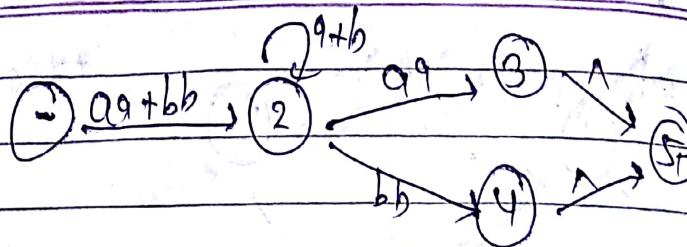


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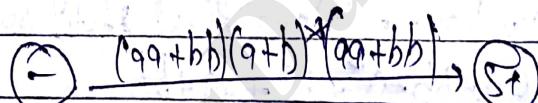


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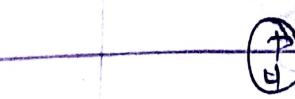
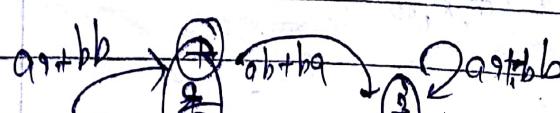
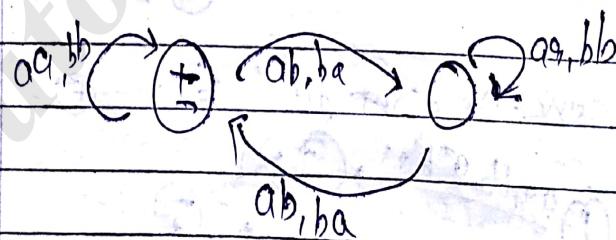
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Common



Consider a graph



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eliminate 2 and 3

$$\rightarrow (aa+bb)^*(ab+ba) \xrightarrow{aa+bb} (3)$$

(4)

eliminate 3 first

aa+bb

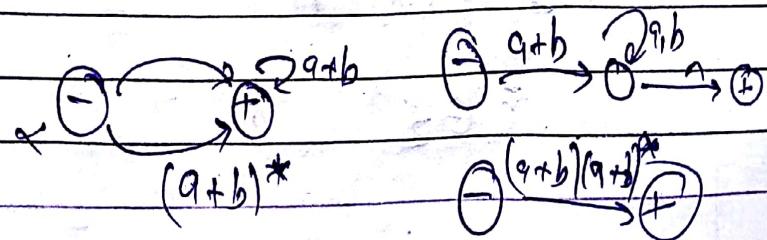
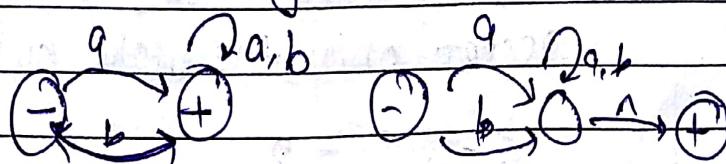
$$\rightarrow \xrightarrow{aa+bb} (ab+ba)(aa+bb)^*(ab+ba)$$

(4)

$$\rightarrow (aa+bb)^*((ab+ba)(aa+bb)^*(ab+ba))^*$$

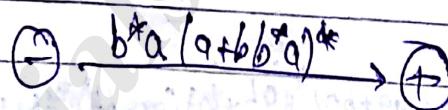
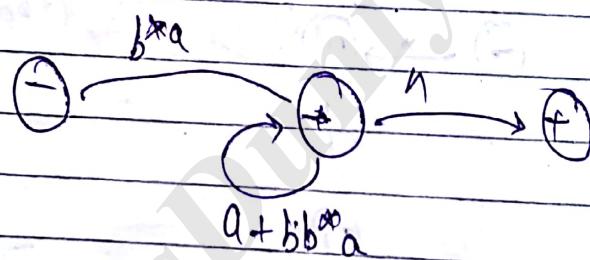
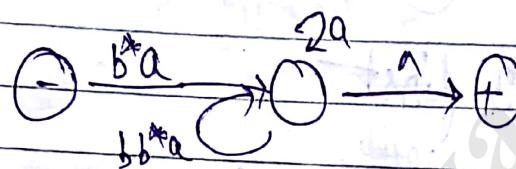
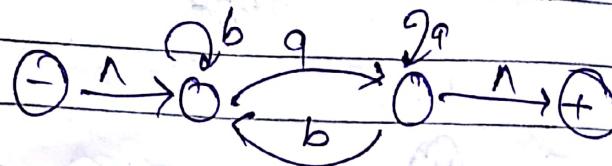
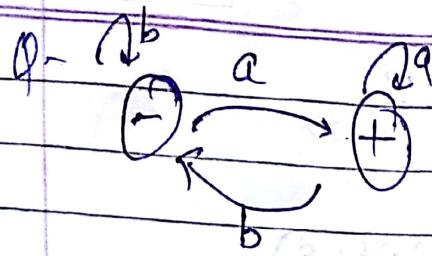
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Consider this graph into Reg. Exp.



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Kleene's theorem

Part 3 - Rule No - 1 - If there is a F.A that accept only particular letter of the alphabet, there is F.A that accept only the word null,

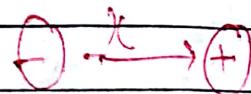
$$\Sigma = \{ \dots \}$$

$X \in \Sigma^*$

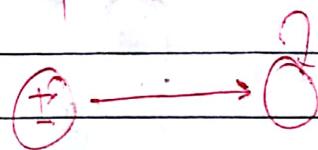
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You can draw a F.A that accept x  
other inputs are invalid



F.A accept null. i.e.,  $\{\}$  Not of  
string. You can draw one that

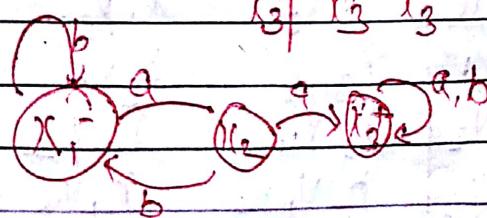


Rule No-2 - If there is a F.A called FA1  
that accept the language define  
by Reg. Exp. that is  $R_1$  and  
there is a F.A called FA2  
that accept the language define by  
Reg. Exp. is  $R_2$ , then if there is a  
finite Au. that we shall call  
FA3 that accept lang. define  
by Reg. Exp.  $R_1 + R_2$

Q. Consider FA1

$$\Sigma = \{a, b\}$$

	a	b
FA1	$x_1$	$x_2$
	$x_2$	$x_1$
	$x_3$	$x_3$

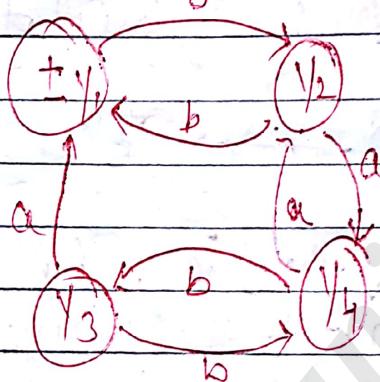


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$FA_2$  | a b

$y_1^+$	$y_3$	$y_2$
$y_2$	$y_4$	$y_1$
$y_3$	$y_1$	$y_4$
$y_4$	$y_2$	$y_3$

b



The lang. the new machine accept  
will be union of those langs  
 $L_1 \cup L_2$

$$L_1 + L_2 = FA_1 + FA_2$$

$FA_3$

$2(x_1, y_1, z)^{\pm}$  | a b

$(x_1, y_1)$	$x_2 y_3$	$x_1 y_2$
$(x_1, y_2)$	$x_2 y_1$	$x_1 y_1$

$x_2 y_3$	$x_3 y_1$	$x_1 y_4$
-----------	-----------	-----------

$x_1 y_4$	$x_2 y_2$	$x_1 y_3$
-----------	-----------	-----------

$x_3 y_1^+$	$x_3 y_3$	$x_3 y_2$
-------------	-----------	-----------

$x_2 y_2$	$x_3 y_4$	$x_1 y_1$
-----------	-----------	-----------

$x_1 y_3$	$x_2 y_1$	$x_1 y_4$
-----------	-----------	-----------

		$\{ \text{have already}\}$
--	--	----------------------------

		$\{ \text{have}\}$
--	--	--------------------

$$\text{Max Rows} = 4 \times 3 = 12$$

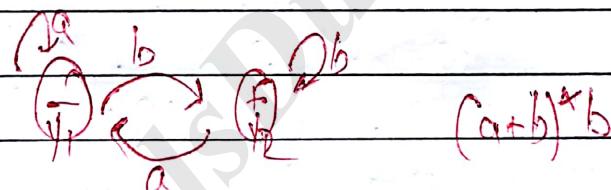
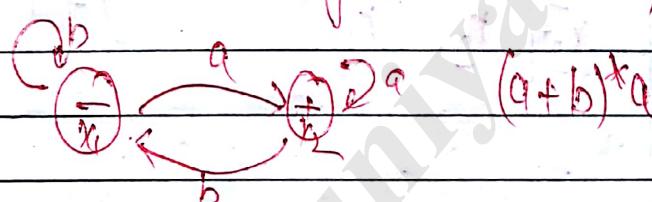
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	a	b
$x_3 y_3^+$	$x_3 y_1$	$x_3 y_4$
$x_3 y_2^+$	$x_3 y_4$	$x_3 y_1$
$x_3 y_1^+$	$x_3 y_2$	$x_3 y_3$
$x_2 y_1^+$	$x_2 y_3$	$x_1 y_2$
$x_2 y_4^+$	$x_3 y_2$	$x_1 y_2$

make graph of this table (self)

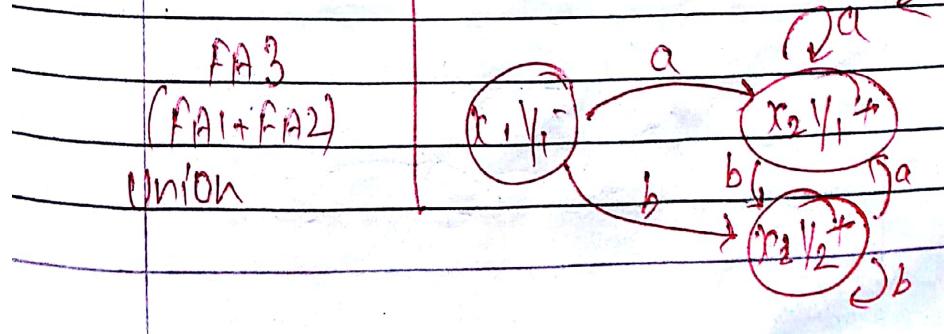
Q FA1 and FA2 are given (FA1 + FA2)

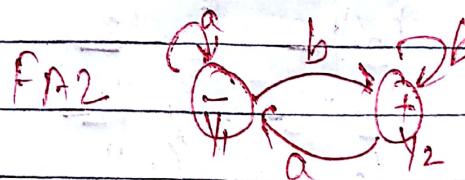


	a	b		a	b
$x_1^+ r_2$	$r_2$	$x_1$	$y_1^+ y_1$	$y_1$	$y_2$
$x_2^+ r_2$	$r_2$	$x_1$	$y_2^+ y_1$	$y_1$	$y_2$

	a	b
$x_1 y_1^-$	$x_2 y_1^+$	$y_1 y_2$
$y_1 y_2^+$	$x_2 y_1^+$	$x_1 y_2$
$x_2 y_1^+$	$x_2 y_1^-$	$x_1 y_2$

Graph





Find Union.

	a	b		a	b
x1	x2	x1	y1	y1	y2
x2	x3	x1	y2	y1	y2
x3	x3	x3			

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Rule No. 3 = If there is a finite Auto. FA1  
that accept the lang. define by Reg.  
Exp.  $R_1$  and FA is FA2 then if FA1  
lang. define by Reg. Exp.  $R_2$  then there  
is FA FA3 then lang. define by  
concatenation  $R_1 R_2$  with the product lang

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regular languages

All finite languages are regular, but only regular are not every lang. is not regular.

It is not Reg.

Finite - R.L.  $\{a^n b^n \mid n=0,1,2,3,\dots\}$ 

gab ab aabb aaabb...?

Reg.  $a^* b^* = \{ a \ b \ aa \ ab \ bb \dots \}$ 

A language that can be defined by a reg. Exp. is called a reg. Language

Some infinite lang. are regular.

If  $L_1$  &  $L_2$  are reg. languages then  $L_1 + L_2$ ,  $L_1 L_2$ ,  $(L_1 L_2)^*$  are also reg. languages.  
We know that  $L_1 + L_2$  means the lang. of all words if either  $L_1$  or  $L_2$ .

$L_1^*$  means string concatenation of arbitrarily many factors from  $L_1$

Set of reg. Lang. is closed under union, concat. and Kleen closure.

all these	$L_1$	$\lambda_1$	$L_1 + L_2 = \lambda_1 + \lambda_2$
Conj. are	$L_2$	$\lambda_2$	$L_1 L_2 = \lambda_1 \lambda_2$
regular	$L_1 + L_2$		$L_1^* = \lambda_1^*$

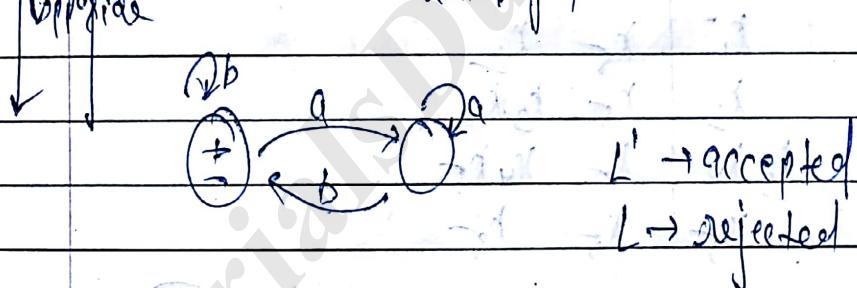
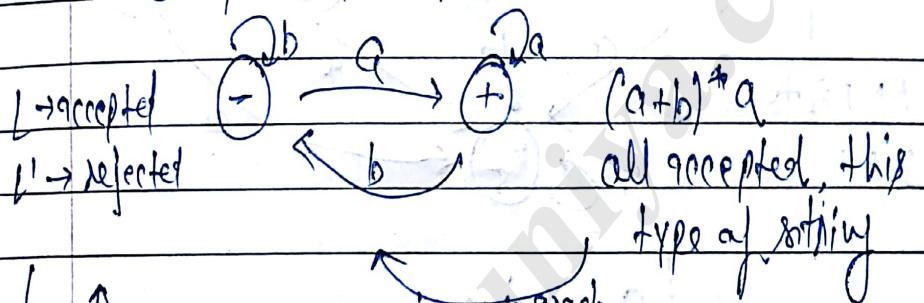
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L<sub>1</sub>L<sub>2</sub>

L'

L'

if L is a reg. lang. then L' is also  
a reg. language. In other words  
the set of reg. lang. is closed under  
Complementation.



If L is a reg. lang. then there is some finite Auto. that accept L. Some of the states of this f.A. are final states or most atleast not. Let us reverse the final status of each states.

i.e., if it was a final state make it non final state and nonfinal make a final state it becomes Complement.

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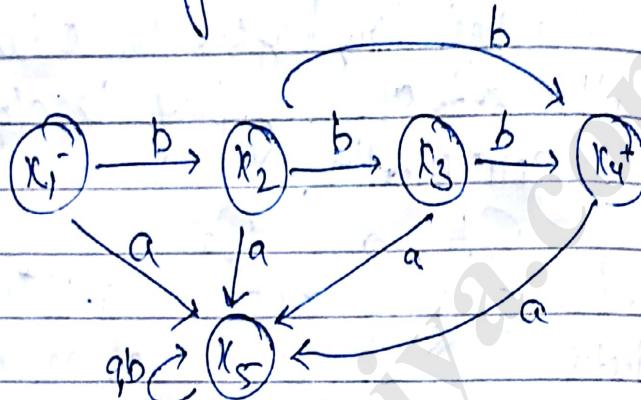
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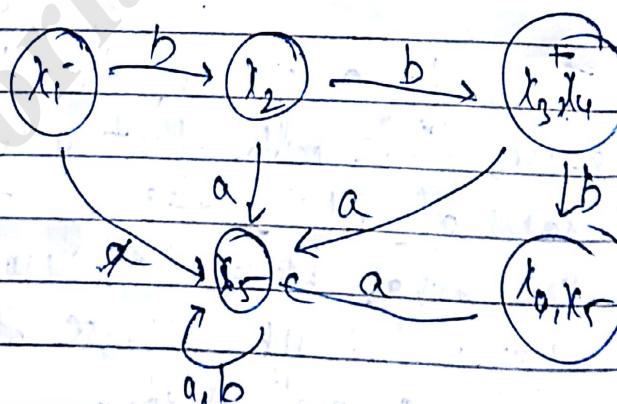
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If an input string formerly ended in  
its final state it now ends in its  
initial state and vice-versa.  
Therefore, this Machine accepts exactly  
the lang.  $E^*$ .

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ANFA to  
DFA

	a	b
$x_1$	$x_5 \rightarrow x_2$	
$x_2$	$x_5 \rightarrow x_3, x_4$	
$x_3, x_4$	$x_5 \rightarrow x_4, x_5$	
$x_5$	$x_5 \rightarrow x_5$	



Convert each of foll. NFA into FA

Reg. languages -

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### Complement & intersection

If  $L$  is lang. over the alph.  $\Sigma$   
define its complement  $L'$

to be the lang. of all strings of letters  
 $\Sigma$  will not words in  $L$ .

E.g. If  $L$  is the lang. over the alph.  
 $\Sigma$  then have AA in them

$L'$  is lang. of all words that do  
not have AA

$$L = (a+b)^* aa(a+b) \text{ reg. lang}$$

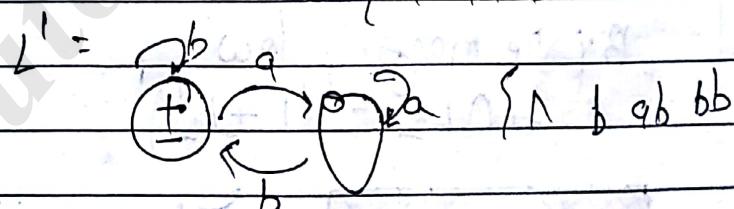
$$L' = \text{is not a reg. lang. (not compulsory)}$$

If  $L$  is a reg. lang. then  $L'$  is also  
reg. lang.



$$L = \text{accepting } (a+b)^* a$$

↓  
a aa ba



If  $L$  is a reg. lang. and then  
there is some FA that accept  
lang.  $L$  some of the state of this  
FA final states and most likely  
some are not.

To do complement of a lang. remove  $(\dagger)$  and add their initial state e.g.

$$\text{Initial State} \xrightarrow{a} (\dagger) \Rightarrow (\dagger) \xrightarrow{a} \text{Initial State}$$

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(44)

Let us reverse the final states of each state, i.e., if it was  $\dagger$ , final state make it a non-final stage and if it is a non-final stage make it a final state.

This new machine accept all input strings which were not accepted by original final Auto.  
(All words in  $L'$ )

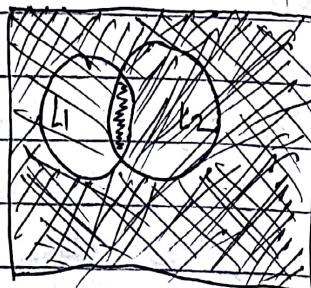
Theorem-2- If  $L_1$  and  $L_2$  are reg. languages then  $L_1 \cap L_2$  also a Reg. Lang  
In other words a set of closed lang. with closed intersection.

$$L_1 = (a+b)^*a$$

$$L_2 = (a+b)^*$$

By De Morgan's law

$$L_1 \cap L_2 = (L_1' + L_2')$$



If  $L_1, L_2$  are reg.  
then  $L_1 \cap L_2$  is  
also reg.

$\cap \rightarrow$  string with 0 length

$\emptyset \rightarrow$  string with no string

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$$\text{Q4/18} \quad L_1 \cap L_2 \\ (L_1' + L_2')$$

$\lambda_1 \quad \lambda_2$

$FA_1 \quad FA_2$

$FA_1' \quad FA_2'$

$FA_1' + FA_2'$

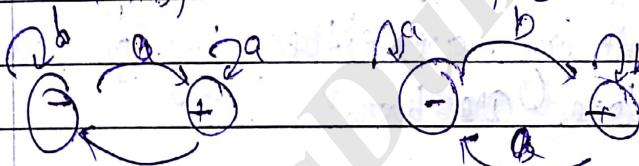
$(FA_1' + FA_2')'$

R.E (Reg. Exp.)

Q - Consider  $L_1 = (a+b)^* a \& L_2 = (a+b)^* b$

$L_1 \quad L_2 \quad \text{find } L_1 \cap L_2$

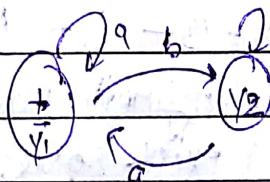
$(a+b)^* a \quad (a+b)^* b \quad F.A, RF$



FA1

FA2

FA1'



	a    b		a    b	
$x_1 \vdash$	$x_2 \cdot x_1$		$y_1 \vdash$	$y_1 \cdot y_2$
$x_2 \dashv$	$x_2 \cdot x_1$		$y_2 \dashv$	$y_1 \cdot y_2$

16

8:30  
T.O

$FA_1' + FA_2'$

a    b

make a graph

$x_1 y_1 \mid x_2 y_1 \mid x_1 y_2$   
 $x_2 y_2 \mid x_2 y_1 \mid x_1 y_2$

$L_1 \cap L_2 = \emptyset$

Ch-9 Page-185

Q- first 10 Q. TAY

CLASSTIME \_\_\_\_\_  
Page No. \_\_\_\_\_Q- Consider find  $L_1 \cap L_2$  $L_1$  $L_2$  $(a+b)^*$  $b(a+b)^*$ 

98

Non-Regular Languages

A lang. cannot be defined by a reg. exp.  
is called a non-reg. lang.

by construction F.A is not possible for N.R.L. as  
by well as Transition Graph.

All lang. are either reg. or non-reg.  
None are both.

25/9/18

Theorem-13 - Let  $L$  be any reg. lang. that has  
infinitely many words. Then there  
exist some three strings  $x, y$  and  $z$   
~~such that~~  $y \neq \lambda$  not the null string  
i.e., all strings are the form  
 $x^ny^z$  where  $n=1, 2, 3, \dots$  are  
words in  $L$ .

 $x^ny^z \in L$ 

Consider if  $L$  is reg. lang. then  
F.A that accepts words in  $L$ .

Now Consider,

 $w \in L$

47

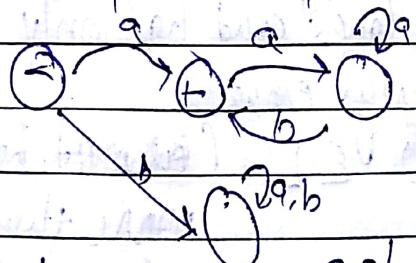
that have some words in L that  
has more letters in it there are some  
states in machine

When this word generate the path to the machine. The path cannot visit a new state for a new letter. i.e., it must at some point revisit a state that it has been before.

Now, let's break it into three parts

(ii) Call parts x : start letter with w starting with beginning that lead up to first state that is revisited.

(ii) Starting the letter after the substring  $x$  let  $y$  denote the substring the  $w$  that travels around the ckt. Coming back to the same state the ckt begins because there must be substring  $y$  cannot be the null string  $y$  contains the letters of  $w$  for exactly one loop around the ckt.



aaaab      abab

Kybernetik und Systemtheorie

(iii) Let  $\gamma$  be the rest of  $w$ , starting with the letter after the substring  $y$  and  $y$  to the end of string  $w$ .

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M8

$z$  should be null. partly  $\{0\}^n z$  could also possibly loop along

a a a a b

x y z

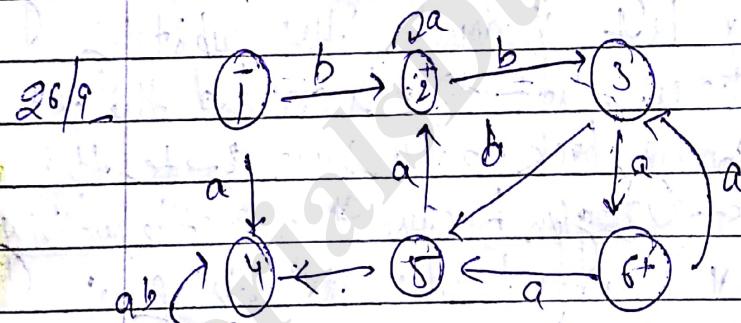
a a a a a b

x y y z

$xy^n z \in L$

This idea of pumping of  $y$  substring is called pumping lemma. We are repeating  $y$  we are pumping substring  $y$ .

$a^n b^n \cdot n = 1 2 3 4 \dots$



Consider a graph this machine accepts infinite lang and has only 6 states and pumping lemma

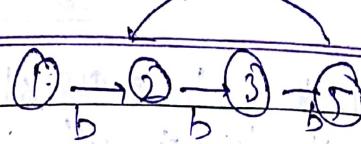
$w \in L$  (all must have at least  
more than 6 words)

Consider  $w$  to be bbbababa

break  $w$  into three parts  $x, y, z$

bbbababa  
x y z

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bb bababa

$x \downarrow y \downarrow z$

before 2nd 'b' it's just of string in 2  
(minimizing)

$\text{xyz}^2 \epsilon L$

$\text{xyz}^2 \epsilon L$

$\text{xyz}^2 \epsilon L$

(pumping lemma)  $\text{xyz}^n \epsilon L$ ,  $n = 1, 2, 3, 4, \dots$

pumping Lemma is only valid on Reg. exp.

Q. Consider another lang —

$a^n b a^n$

$y = q$

$a^{10} b a^{10}$

$a^{10} b a^{10} \notin L$  ? because we should

$a^{10} b a^{10} \in L$  be equal  $a^{10} b a^{10}$

We cannot have  $y$  that can be pumped into  
the string is not there for not reg.

Q.  $a^n b a^n b a^{n+1}$ ,  $n = 1, 2, 3, \dots$

let  $L$  be an infinite lang excepted  
by FA with  $n$  no. of states then  
for all strings  $w$  in  $L$  that have

Ch-10 is not in syllabus

Ch-11 " "

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more than h letters there are strings  $x, y$  &  $z$  where  $y$  is not null

$$|x| + |y| \leq n$$

length of  $y$  does not exceed  $n$

s.t.  $vw = xy^2$  and all strings of the form  $xy^n z \in L$  for  $n=1,2,3, \dots$

Ex-195

Show that lang. pallindrome is not reg.

Q- Consider the lang. prime

$$\text{prime} = \{a^p \mid p \text{ is prime}\}$$

(if not regular)

Q. Show the lang. is non-regular

(i)  $a^nb^{n+1}$

(ii)  $a^nb^nc^n$

(iii)  $a^nb^{2n}$

(iv)  $a^nb^m a^m$

Part-2

## Push Down Automata Theory

Ch-12 Context free Grammer

Syntax of a method for defining

lang

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(51)

Consider an exp.

$$\frac{1}{2} + 9$$



$$4 + 8$$

$$\frac{21}{2} + \frac{5}{2}$$

Consider arithmetic. exp.(AE) You are given some rule

- Rule-(i) Any no. is in the set of AE  
 (ii) If  $x$  and  $y$  are in AE then so are

$$x, y \in AE$$

$$(x)$$

$$(x)$$

$$(x+y)$$

$$(x-y)$$

$$(x \cdot y)$$

$$(x/y)$$

$$(x * y)$$

$$(3+4*5)$$

$$(3+4)*5 \quad (3+(4*5))$$

Terminals (T)

Non-Terminals (NT)

A Context-free Grammar is a collection of three things -

- (i) An alphabet  $\Sigma$  of letters called terminals from which we are going to make strings that will words of lang.

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(52)

(i) A set of symbols called non-terminals.

One of symbol which is capital S

Acting for start here.

(ii) If finite set of production of a form  
One NT into finite strings of terminals

or non-terminals (NT) where the  
strings of T & NT can consist of  
only T or of only NT or any  
mixture of T and NT or even the  
empty string.

1/10/19 Consider rules for the formal arithmetic

exp.

Start  $\rightarrow$  AE

AE  $\rightarrow$  (AE + AE)

AE  $\rightarrow$  (AE - AE)

AE  $\rightarrow$  (AE \* AE)

AE  $\rightarrow$  (AE/AE)

AE  $\rightarrow$  (AE \*\* AE)

AE  $\rightarrow$  (AE)

AE  $\rightarrow$  -(AE)

AE  $\rightarrow$  any number

Any Number

Rule 1: Any no  $\rightarrow$  FD

Rule 2: FD  $\rightarrow$  FOD

Rule 3: FD  $\rightarrow$  123-9

Rule 4: OD  $\rightarrow$  0 123-9

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$$(S + (4 \times 5))$$

$$\text{start} \rightarrow (AE)$$

$$\vdash ((AE + AE))$$

$$\vdash ((AE + (AD * AE)))$$

$$\vdash ((\text{Any no.} + (\text{Any no.} * \text{Any no.}))$$

$$\vdash ((3 + (4 \times 5)))$$

$$\text{Any no.} \rightarrow FD$$

$$3 \rightarrow 3$$

$$\text{Any no.} \rightarrow FD$$

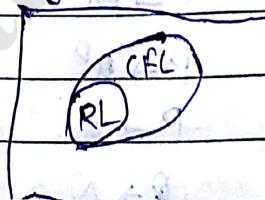
$$\vdash F_0 D$$

$$\rightarrow 20$$

all printing of

The lang. generated by CFG is a set of terminal  
that can be produced from the start symbol  
using the product as

A lang. generated by CFG is called CFL



Every RL is CFL

$$(\text{Start}) S \rightarrow A \quad \{A\}$$

$$S \rightarrow a \quad \{a\}$$

$$S \rightarrow b \quad \{b\}$$

$$S \rightarrow A \quad \{n\}$$

$$S \rightarrow a$$

$$S \rightarrow b$$

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(54)

All finite Lg's are CFL

 $\alpha^*$  $b^*$  $S \rightarrow aS$  $S \rightarrow bS$  $S \rightarrow A$  $S \rightarrow A$  $S \rightarrow aS$  $S \rightarrow A$  $\rightarrow a$  $S \rightarrow aS$  $S \rightarrow aS$  $S \rightarrow aA$  $\rightarrow aaS$  $S \rightarrow aA$  $\rightarrow aa$  $A \rightarrow aA$  $A \rightarrow A$  $A \rightarrow A$  $A \rightarrow A$  $A \rightarrow A$  $ab^*$  $(a+b)^*$  $S \rightarrow aB$  $S \rightarrow aS$  $B \rightarrow bB$  $S \rightarrow bS$  $B \rightarrow A$  $S \rightarrow A$  $a(a+b)^*$  $(a+b)^*a$  $S \rightarrow aS$  $S \rightarrow Pa$  $S \rightarrow aS$  $P \rightarrow aP$  $S \rightarrow bS$  $P \rightarrow bP$  $S \rightarrow A$  $P \rightarrow A$  $(a+b)^*a(a+b)^*$  $(aa+bb)^*$  $S \rightarrow PaP$  $a^*b^*$  $P \rightarrow aP$  $(aa+b)^*$  $P \rightarrow bP$  $(aa+b)^*$  $P \rightarrow A$ { }  
from here

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(55)

 $(a+bb)^*$  $a^*b^*$  $S \rightarrow aS$  $S \rightarrow pS$  $S \rightarrow bS$  $p \rightarrow qp$  $S \rightarrow \lambda$  $p \rightarrow \lambda$  $q \rightarrow bq$  $q \rightarrow \lambda$  $(a^*b^*)^*$  $S \rightarrow pS$  $p \rightarrow (qp+b)R$ 

Q10

RE

RL

CFL

finite  
Infinite $(a+b)^* \cap (a+b)^*$  $(a+b)^* a (a+b)^* ab$  $S \rightarrow X a a X$  $S \rightarrow X a X a b$  $X \rightarrow aX$  $X \rightarrow aX$  $X \rightarrow bX$  $X \rightarrow bX$  $X \rightarrow \lambda$  $X \rightarrow \lambda$  $a^*b^* \rightarrow AB$  $(a^*b^*)^*$  $S \rightarrow aS$  $S \rightarrow \lambda$  $S \rightarrow \lambda$  $A \rightarrow \lambda$  $(AB)^*$  $S \rightarrow bS$  $B \rightarrow bB$  $A \rightarrow aA$  $S \rightarrow \lambda$  $B \rightarrow \lambda$  $A \rightarrow \lambda$  $B \rightarrow bB$  $B \rightarrow \lambda$  $S \rightarrow ABS$  $S \rightarrow \lambda$

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$$(a^* + ab)^*$$

$$S \rightarrow AS$$

for Non-Reg. Languages

$$S \rightarrow BS$$

 $a^n b^n \quad n = 1, 2, 3, \dots$ 

$$S \rightarrow A$$

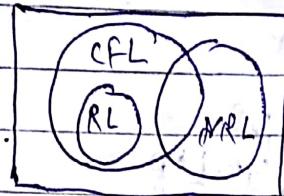
$$S \rightarrow aSb$$

$$A \rightarrow AA$$

$$S \rightarrow ab$$

$$A \rightarrow a$$

$$B \rightarrow ab$$



$$(NRL) \quad a^n b^n c^n \quad n = 1, 2, 3, \dots$$

$$S \rightarrow aXbYc$$

$$X \rightarrow ab$$

$$Y \rightarrow bc$$

Consider a CFG

$$\begin{array}{l} \text{all even} \quad S \rightarrow aSa \\ a \quad S \rightarrow a \end{array}$$

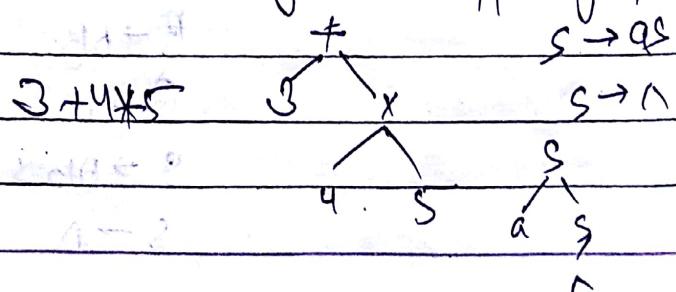
$$\begin{array}{l} S \rightarrow bSb \quad \text{all even} \\ S \rightarrow a \quad b \end{array}$$

$$\begin{array}{l} S \rightarrow aSa \\ \text{odd length} \quad S \rightarrow bSb \\ \text{palindrome} \quad S \rightarrow a \\ S \rightarrow b \end{array}$$

$$\begin{array}{l} S \rightarrow aSa \quad \text{even either a or b} \\ S \rightarrow bSb \quad \text{odd palindrome} \\ S \rightarrow a \quad (\text{even length}) \end{array}$$

If we add  $S \rightarrow \lambda$ 

it will give all types of palindrome

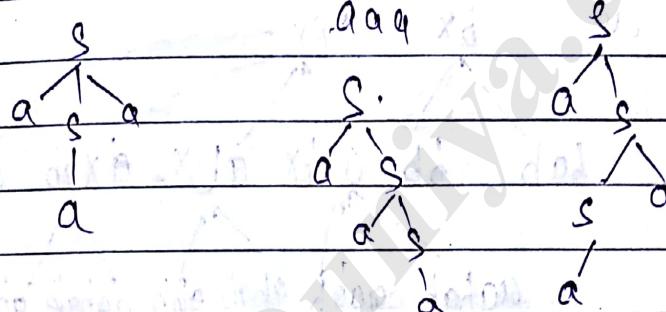


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(57)

If CFG is called ambiguous. If for atleast one word in the lang. that is generated there are 2 or more derivations of the word that correspond to diff. syntax trees. If CFG is not ambiguous it is called unambiguous.

$$S \rightarrow aSa \quad S \rightarrow a$$



10/10

### The Total lang. tree (TLT)

It is possible to depict the gen. of all the words in the lang. of CFG simultaneously in one big tree (possibly infinite tree). In the lang. infinite. For a given CFG we define a tree with the \* symbol (\*) as a root whose nodes are working strings of terminal and non-terminals. The dependents of each node are all the possible results of applying every applicable string rule at a time.

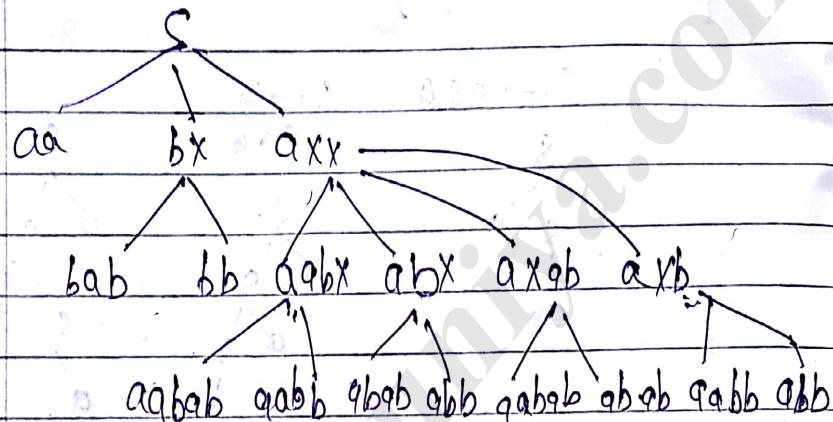
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If a string of all terminals is a terminal node in a tree, the resulting tree is called TLT

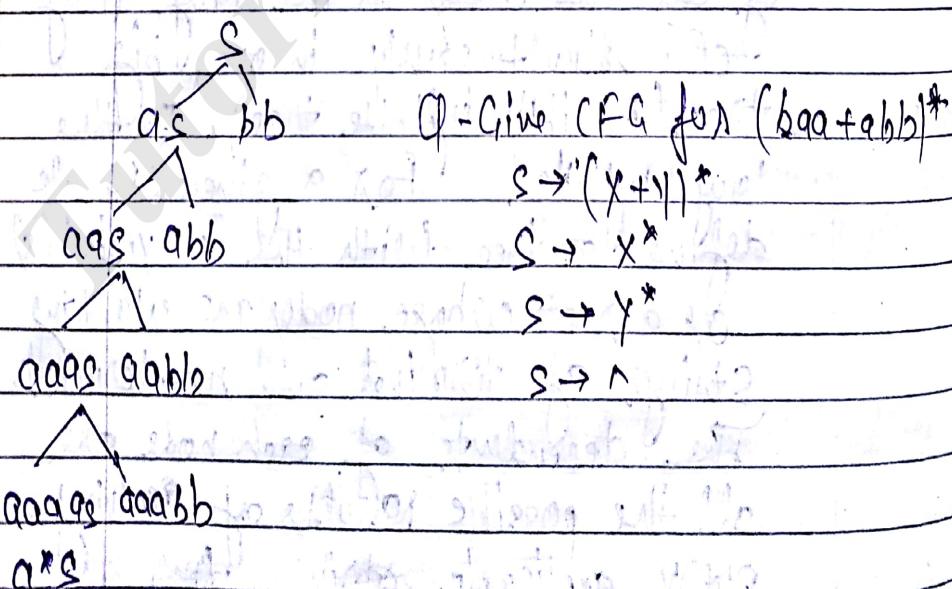
$$S \rightarrow aa \mid bx \mid axx$$

$$X \rightarrow ab \mid b$$



Q- 1, 2, 3, 4, 5, 7, 8, 11, 13, 16, 17

$$\text{Q- } S \rightarrow aS \mid bb \quad a^*bb$$



Ch-13 is not in syllabus

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{S is left-linear}  $\neq S(a+b)^*$  }

a a

b a

aa aa

ab aa

ba aa

bb aa

aa aa

b a

a b

aa aa

ab aa

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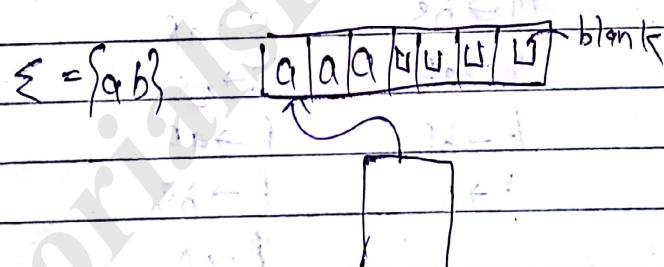
of 1 all of rules production are of one  
of the Chg's form

 $N T \rightarrow \text{str. only NPs}$ 
 $N T \rightarrow T$ 

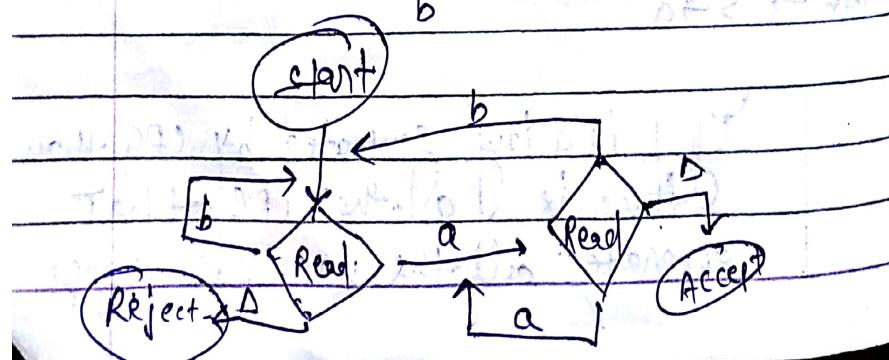
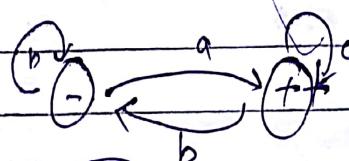
If a CFG has only production of form  
 $N T \rightarrow \text{str. of exactly two NT's}$

 $N P \rightarrow T$ 
 $S \rightarrow A B C$ 
 $R_1 \rightarrow A B$ 
 $S \rightarrow R_1 C$ 
 $R_1 \rightarrow A B$ 
 $S \rightarrow a a$ 
 $S \rightarrow A A$ 
 $A \rightarrow a$ 

Push Down Automata (PDA)



Consider a finite automata that accept  
all words in the letter ending a



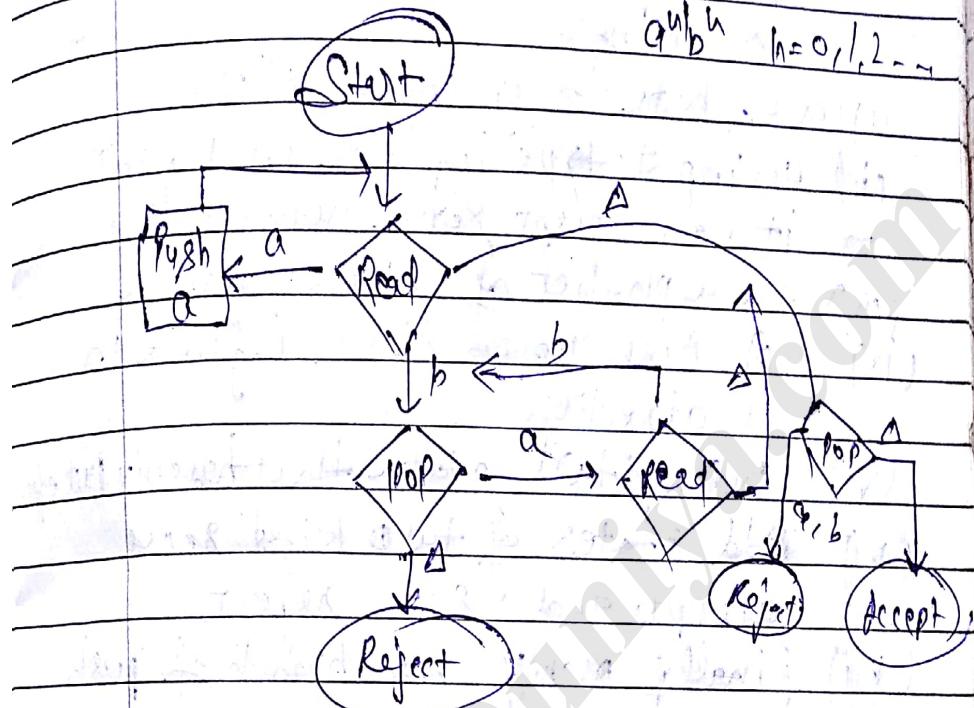
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PDA -

Consider a PDA

$$a_n b_n \quad n=0, 1, 2, \dots$$



$a_n f^{2^n}$        $a a a \ b b \ b b \ b b$

$g^{2n} h^n$

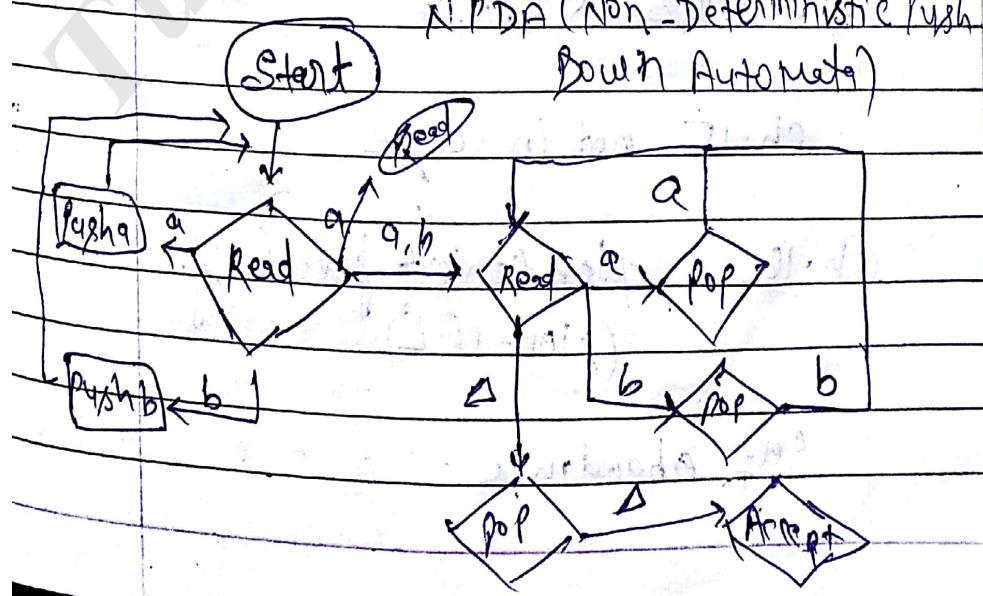
$$q^n \mid b^{2n+1}$$

for every CFL = PDA

$$a^{n+1} : b^n$$

11/10 Consider a PDA

NPDA (Non-Deterministic Push  
Down Automata)



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Fig. given on page no - 302

→ PDA

A pull down Automata collection of  
8 things.

- (i) a alphabet  $\Sigma$  of input letters
- (ii) an input tape infinite in 1 direction  
→ it can accept some non-reg. lang.
- (iii) An alphabet of stack char.
- (iv) A push down stack infinite in 1 direction.
- (v) One start state that has only Out edge.
- (vi) All states of two kind some accept and some reject.
- (vii) Finally many non-branching push states
- (viii) Finally many branching states of two type one read, one pop.

Theorem For every lang. L there is some PDA that accept it.

$$\varnothing = \{1, 2, 3, 4, 5, 6, 7, 8\}$$

Ch-15 not in course

Ch-16 Non Context free lang.  
(Non-CFL)

Self abundance -

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Now consider CFG which is in CNF  
all is producible of 2 forms

$$NT \rightarrow NTNT$$

$$NT \rightarrow T$$

Let G be a CFG in CNF and let's  
call production  $NT \rightarrow NTNT$  as  
live production and  $NT \rightarrow T$  as  
dead production. Every time we  
apply a live production we increase  
no. of NT by 1 and ..., dead we  
decrease no. of NT by 1.

Consider for e.g.

$$S \rightarrow b \text{ (dead)}$$

Suppose G has p-live prod^n

$q \rightarrow$  dead prod^n

by any definition that defined genre  
live prod^n must have atmost p+1  
live prod^n

Now consider a case

$$S \rightarrow A2$$

$$2 \rightarrow BB$$

$$B \rightarrow ZA$$

$$A \rightarrow a$$

$$B \rightarrow b$$



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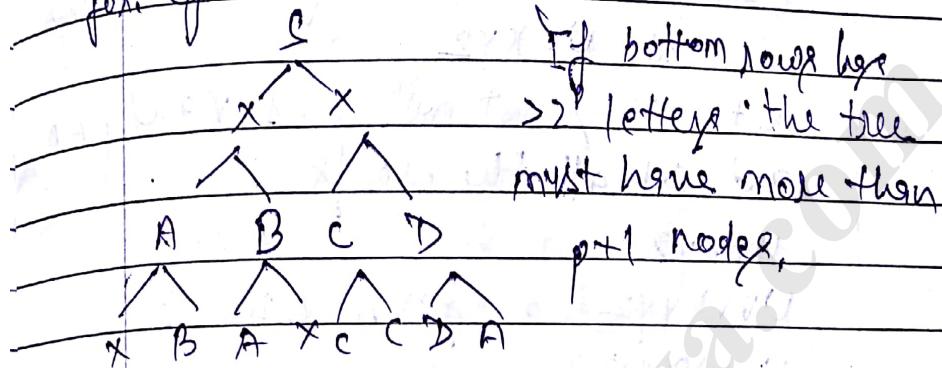


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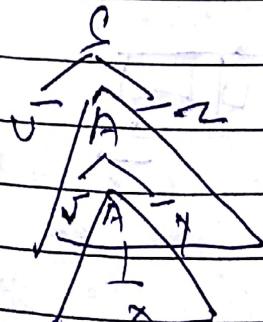
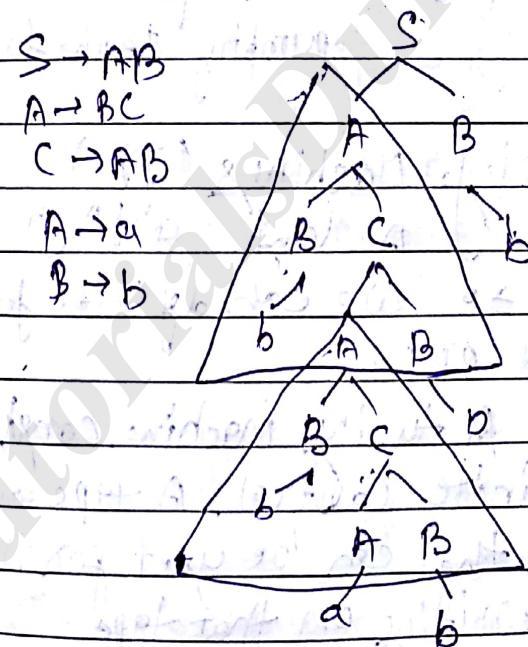
Some AT call it 2 being wed twice  
where the 2nd z is descended  
from first z.

~~for. 9g.~~



Now consider a CFG

$$100' > 2'$$



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66

If  $G$  is any CFG in CNF with  $p$  line prodn and  $w$  is any word generated by  $G$  with length  $\geq 2^p$  then we can break up  $w$  into five sub strings

$$w = U V X Y Z$$

$s + sc$  is not null and  $v$  and  $y \in \Sigma$  and  $s + t$  all the words

$$U V X Y Z$$

$$U V V X Y Y Z \quad \text{for } n = 1, 2, \dots, 3$$

$$U V V V X Y Y Y Z$$

$\vdots \quad C_n$  also be generated

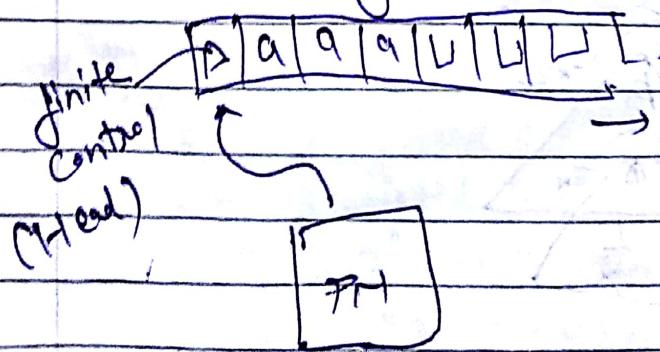
$$U V^n X Y^n Z$$

$\vdots \quad$  by  $G$ . This is pumping lemma for CNF.

## 29/10 Turing Machines (Tm)

A tape  $a^n b^n c^n$  where  $n \geq 0$  we can definite for it FA and PDA.

A turing machine consist of a finite control, A tape and a Head that can be used for reading and writing on that tape.



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The TM seem to form a suitable and maximal class of computer devices in terms of computers they can perform. The idea of an algo. must be equiv. to the (natively).

TMs are design to generally satisfy the foll. three criteria -

(i) They should be automata i.e., there funct. and cons.

as the devices previously studied.

(ii) They should be as simple as possible to describe formally and rigorously.

(iii) They should be as general as possible in terms of comput. of they carried out.

Definition of TM -

TM is a Quintuple  $(K, \Sigma, \delta, S, H)$

$K$  - is finite set of states

$\Sigma$  - is an alphabet containing blank symbol ( $\sqcup$ ), left end symbol ( $\Delta$ ) but not containing the symbol ( $\rightarrow \leftarrow$ )

$S \in K$  is the initial state

$H \subseteq K$  set of halting states (final)

If,  $\delta : (Q \times \Sigma) \rightarrow Q$ , The trans. func. is a fun.

from  $(K-H) \times \Sigma \rightarrow K \times (\Sigma \cup \{\leftarrow, \rightarrow\})$

s.t.

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(8)

(a)  $q \in k-H$ , if  $s(q, b) = (p, b)$  then  $b = \rightarrow$

(b)  $q \in k-H$  and  
 $a \in \Sigma$ , if  $s(q, a) = (p, b)$  then  $b \neq \rightarrow$

Consider

$\boxed{D \ a \ q \ a \ u \ u \ u \ u \ u \ u}$

$\rightarrow a \underline{bab} u u u \rightarrow (q, \rightarrow)$

$\rightarrow u \underline{bab} u u \rightarrow (q, \rightarrow)$

$\rightarrow u \underline{bab} u \rightarrow (q, \rightarrow)$

$\rightarrow u \underline{ab} u$

$\rightarrow u \underline{u a b} u$  - represent position

$\rightarrow u \underline{u b} \underline{b} u$  of head

$\rightarrow u \underline{u u b} u$

$\rightarrow u \underline{u u u} b u$

then bottom

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(6)

24/10

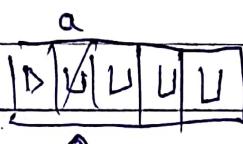
### A notation of TM -

Tabular form of a TM are quite complex and hard to interrupt when a annotation is needed for TM i.e., for graphic and transparent. We using <sup>more</sup> Hanoi cell notation, etc.

- The basic machines are
- Symbol writing machines
  - Head moving machines

A writing machine

$$\Sigma = \{a, b\}$$



The TM's will be combined in a way suggesting of a structure of a FA. Initially machines are like the states of F.A

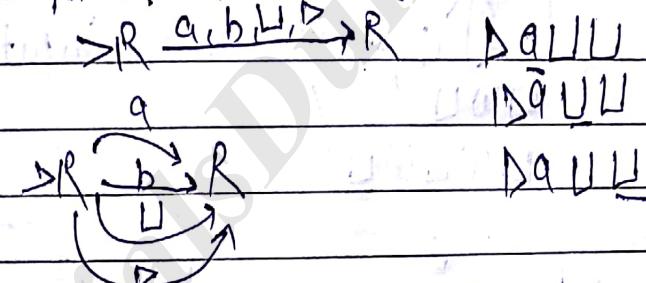
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The machines may be connected to each other in the way that the states of FA connected together.

The connection of one machine to another is not pursued until the first machine halts. Another machine is then started from its initial state with the tape and the head position as they will left by the first machine.

Consider a machine



$$g. \quad \text{DaaVU} \rightarrow \text{RR} \quad g. \quad \text{DaaULLI} \rightarrow \text{RLR}^q \rightarrow \text{R}$$

bag bag bag

Dad will be home at 7pm

~~OUR PICTURE BOOKS. D. BROWNE LTD.~~

~~BRUNNEN~~ ~~BRUNNEN~~

~~Mark it on the slide first blank~~

Maintain the chain  
1. Add oil 2. Lubricate

~~sq. to the right~~ : it means more

~~aaaaalll~~ ~~are~~ ~~the~~ ~~new~~ ~~one~~  
~~black~~ ~~white~~

~~Do not sign off on blank papers~~

same  $R_H \rightarrow 1$

P

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Dag Uaq U > L<sup>2</sup>U

A machine which find first Non-blanks  
sq. to the Right

S U U U U U U

> R<sup>2</sup>U → to move right until non-  
blank symbol.

→ L<sup>2</sup>U → to move left

OR L<sup>2</sup>

Copying Machine — (C)

C starts with input w

U W U

U W U U W U

> L<sup>2</sup>U → R → U R<sup>2</sup> U A L<sup>2</sup> U A

R<sup>2</sup>U  
R U

U Q Q Q W Q U W

U Q Q Q W U

U Q U Q U Q U W

U Q Q Q W U W

U Q U Q U Q U W

U U Q Q W U W

U Q U Q W U W

U U Q Q W U W

U Q U Q W U W

U U Q Q W U W

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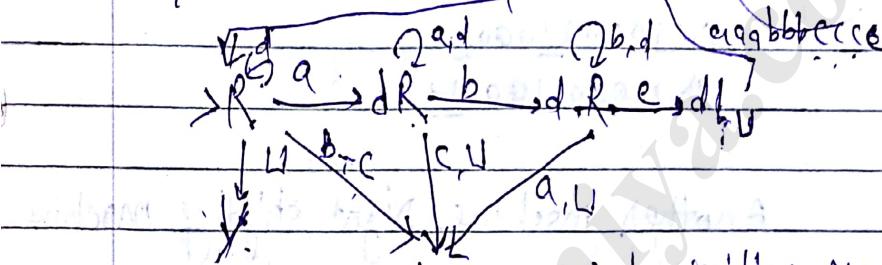
D babcc L abc ✓  
babcc  
babcc  
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$\Rightarrow R^q \rightarrow L$   $\Rightarrow L \underline{aabbcc} L$

Consider the lang.  $a^n b^n c^n$  which has evaluated all types of lang.  
 recognized

NFCL

TM  $\{a^n b^n c^n \mid n \geq 0\}$



$\rightarrow$  d writing machine  
 because we writing  
 it will accept all  $a^n b^n c^n$

$\Rightarrow R^q \rightarrow L(a^n)$   $\rightarrow R^q a \rightarrow R^q a, R^q \rightarrow \gamma$

$b, c, \gamma$   $a, b$

$a^* b \rightarrow R^q b \rightarrow \gamma$

$\Delta \underline{aabbcc} \downarrow \gamma$

$$\text{succ}(n) = n + 1$$

out

0	1	$\Delta \underline{n} \gamma$
01	10	$\Delta \underline{n+1} \gamma$
10	11	
11	100	
100	101	
101	110	

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## Recursive Functions

Q. Let  $M$  be a TM

$M = \{ R, \Sigma, S, S, H \}$ , and let  
 $\{0, 1\} \subseteq \Sigma \subseteq \Sigma - \{ \text{blank} \}$

$\{0, 1\} \cup \Sigma^* \subseteq \Sigma$

Now, suppose that  $M$  halts on input  
 $w$

$(S, D \sqcup w) \xrightarrow[M]{*} (h, D \sqcup y)$

then  $y$  is called the output of  $M$  on  
 Input  $w$

$m(w) = y$

meaning  $m(w)$  is defined only if  $M$  halts  
 on input  $w$ .

$x \in \Sigma^*$

Now let  $f : \Sigma^* \rightarrow \Sigma^*$

We say that  $M$  computes fun.  $f$  if  
 for all  $w \in \Sigma^*$

$m(w) = f(w)$  (input)

i.e., whenever  $f$  holds for all  $w$   
 and when it does hold its tape  
 contain the string  $\sqcup \sqcup f(w) \sqcup$

A func.  $f$  is called recursive if there  
 is a TM  $M$  that computes  $f$ .

Ex - 4.2.2

\* any way we have TM for that that is  
recursively how -

11P > 166WL C 8LWLWL

O/P DATA S

We want

~~1 → 0      succ(n) = n+1~~

$$> R_{WL} \xrightarrow{\text{O}}$$

$\text{ded. } \alpha \vdash \xi_L$

▷ 11 010101L

## Recursively Enumerable Languages

If a TM decides a lang. and computes a function it can't be negligible

- thought of S and algo. that performs correctly and reliably some computation
- 1985

Let  $M$  a TM. Let  $\Sigma$ .

Let  $L$  a subject of  $S^t$

We say that  $\Sigma$  semi decide  $E$  iff if for any string  $w \in \Sigma^*$  the foll. is true.  $w \in E$   $\rightarrow$

If and only if  $m$  holds on input  $w$

A large L is decisively winnable if and only if there is a firm M that semi decides L.

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