

Not All Embeddings are Created Equal: Towards Robust Cross-domain Recommendation via Contrastive Learning

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ABSTRACT

Cross-domain recommendation (CDR) aims to leverage the rich information from the source domain to enhance recommendation performance in the target domain. However, the data imbalance problem inherent across different domains compromises the effectiveness of CDR approaches, posing a significant challenge to CDR. Most current CDR methodologies focus on creating better user embeddings for the target domain, yet usually neglect the inconsistency in user activities due to data imbalance. As a result, the process of creating user embeddings tends to prioritize users with more frequent interactions and leave less active users underserved, leading these CDR methods to struggle in making accurate recommendations for those with fewer interactions. Such bias in creating embeddings reveals the fact that "not all embeddings are created equal" in CDR, which serves as the primary motivation of this study. Inspired by the recent development of contrastive learning, this paper proposes User-aware Contrastive Learning for Robust cross-domain recommendation (UCLR), enhancing the

robustness of cross-domain recommendation. Specifically, our proposed method consists of two sub-modules: (i) pretrained global embedding, where the global user embeddings are pretrained across all the domains; (ii) contrastive dual-stream collaborative autoencoder, where more equal user embeddings are generated by optimizing contrastive loss with individualized temperatures. To further improve the performance of our method in each domain, we finetune the whole framework of UCLR based on Low-Rank Adaptation (LoRA). Theoretically, our method is equipped with a provable convergence guarantee during the contrastive learning stage. Furthermore, we also conduct comprehensive experiments on real-world datasets to validate the effectiveness of our proposed method.

CCS CONCEPTS

• Information systems \rightarrow Recommender systems.

KEYWORDS

Cross-domain recommendation, Contrastive learning

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1 INTRODUCTION

Recommendation systems (RS) have been effectively implemented in various real-world applications with the advent of the big data era, serving as essential tools for understanding user preferences.

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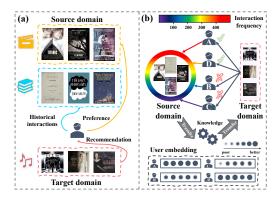


Figure 1: (a) An illustration of cross-domain recommendation. Based on the historical interactions, CDR methods recommend romantic music in target domain to a user who prefers to romantic movies and books in source domain. (b) In real-world applications, the frequency of interactions from different users can be extremely diverse. Most existing CDR methods tend to create poor embeddings for users with fewer interactions, e.g., User B and C, resulting in inaccurate recommendations for these users in the target domain.

Most of the existing RS methods follow the structure of collaborative filtering (CF), which make recommendations by creating user and item embeddings based on the historical interactions [10, 20, 21, 64, 65]. However, data sparsity has been a long-standing issue for recommendation systems, as some services find it challenging to collect sufficient data. Cross-domain recommendation (CDR) was introduced to alleviate this issue, aiming to transfer the rich information from the source domain to improve the recommendation performance in the target domain [74]. For example, as shown in Figure 1(a), CDR methods tend to recommend romantic music to a user based on his historical interactions in other domains. Essentially, CDR methods aim to learn user's preferences from rich domains to make accurate recommendations in sparse domains. In practical settings, AliExpress operates as a global e-commerce platform catering to consumers worldwide. The variations in consumer spending habits and levels across different countries contribute to the issue of sparsity in interactions between consumers and products in certain nations.

In recent years, many efforts have been made to improve the performance of cross-domain recommendations [2, 3, 12, 32, 35, 40, 71]. The commonality among these methods is to create better user embeddings based on the user-item interactions from the source domain. However, in real-world scenarios, the frequency of interactions from different users can be extremely diverse due to data imbalance [6, 46, 55, 62]. Taking the AliExpress business as a case study, the interaction frequency between the products on the e-commerce platform and users from different countries exhibits considerable variability, influenced by factors such as popularity, usage, and pricing. As demonstrated in Figure 1(b), User A and D exhibit frequent interactions in the source domain, in contrast to User B and C who have notably fewer. When creating user embeddings with such imbalanced interactions, deep learning based methods tend to focus more on users with frequent interactions

while overlooking those with fewer interactions, as the process of creating embeddings invariably leans towards gradient descent in directions that are easier to fit. Such biases will lead CDR methods to create poor embeddings for inactive users, resulting in inaccurate recommendations for these users in the target domain. We refer to this observation as "not all embeddings are created equal". Unfortunately, most existing CDR methods neglect the inconsistency in user activities, which is particularly unfriendly for users with fewer interactions or some newly started users in real-world applications.

Hence, the above discussions motivate us to ask the following question: "Can we develop a robust algorithm that is capable of mitigating the negative effects caused by data imbalance across different users?" This paper provides an affirmative answer by proposing a novel algorithm named User-aware Contrastive Learning for Robust cross-domain recommendation (UCLR). Our proposed algorithm consists of two sub-modules, including pretrained global embedding and contrastive dual-stream collaborative autoencoder.

Our study focuses on investigating the multi-target CDR problem, aiming to simultaneously enhance the performance across multiple domains. First, we adopt Matrix Factorization (MF) model with the Bayes Personalized Ranking (BPR) loss [47] to create user and item embeddings across all observable domains. We refer to this BPRMF model as "pretrained global embedding", where "global" means that the user preferences are captured from all domains. Second, we construct the dual-stream autoencoder that takes the pretrained global user embedding both in its original form and with random masking as inputs. After encoding the two input user embeddings, our goal is to push the similarity score between the user embeddings of the same user to be higher than that between the user embeddings of different users. However, due to the significant variation in the quality of created user embeddings, the technical challenge arises from the demand for varying degrees of force to obtain separable embedding space. With the inspiration of the recent development of contrastive learning [43], we propose user-aware contrastive learning with automatic temperature individualization to address this challenge. In contrast to conventional contrastive learning, user-aware contrastive learning introduces an optimizable individualized temperature for each user. This mechanism adaptively adjusts the penalty strength for negative samples, effectively dealing with the problem that "not all embeddings are created equal". We refer to this autoencoder as "contrastive dual-stream collaborative autoencoder".

To further enhance the performance of UCLR, we finetune the whole framework within each domain. Given that the pretrained global model is over-parameterized for each domain, i.e., the number of the pretrained model parameters across all domains is typically redundant for a single domain, we innovatively introduce Low-Rank Adaptation (LoRA) [22] to finetune the whole framework of UCLR within each domain for cross-domain recommendation. Domain-aware LoRA finetuning method offers the dual advantages of performance enhancement and efficiency improvement.

Our main contributions are summarized as follows:

 We propose a novel user-aware contrastive learning framework with automatic temperature individualization to handle the problem that "not all embeddings are created equal" in cross-domain recommendation. Besides, our proposed

- method is specially designed with justifications, rather than directly utilize the existing contrastive learning methods.
- We employ Low-Rank Adaption (LoRA) to finetune the whole framework, leading to a significant improvement for crossdomain recommendation.
- Theoretically, we provide a rigorous analysis to establish
 the convergence guarantee of our method during the contrastive learning stage. Furthermore, we also conduct comprehensive experiments on benchmark datasets to support
 our claims. Compared with the state-of-the-art methods for
 single-domain or cross-domain recommendation, our proposed method achieves superior performance.

2 RELATED WORK

In this section, we briefly introduce the recent studies on crossdomain recommendation and contrastive learning, which bear significance to our proposed method.

2.1 Cross-Domain Recommendation

Cross-domain recommendation aims to leverage the rich information from multiple source domains to enhance the recommendation performance in target domain. According to the number of source domains, cross-domain recommendation can be categorized into three types: single-target cross-domain recommendation (STCDR), dual-target cross-domain recommendation (DTCDR), and multitarget cross-domain recommendation (MTCDR). Both STCDR and DTCDR focus on just two domains. While STCDR leverages the abundant information from the source domain to make better recommendations within the target domain [14, 26, 27, 41, 53, 57, 66, 70], DTCDR utilizes the observed information from both domains to improve the recommendation performance across them at the same time [2, 3, 33, 35, 36, 39, 40, 49, 71–73, 76]. However, in realworld scenarios, we often have access to more than just two source domains, implying that STCDR and DTCDR methods cannot fully exploit the information from all source domains. Therefore, MTCDR has gained significant attention in recent years, as it presents a more general and challenging scenario. Multi-target cross-domain recommendation (MTCDR) seeks to improve the recommendation performance within all domains simultaneously. Existing studies focus on how to construct domain-shared information based on multiple domains, with the aim of leveraging such information to enhance the performance within each individual domain [12, 30, 32, 61, 75]. HeroGraph [12] constructs a domain-shared heterogeneous graph based on user-item interactions across all domains and creates graph embeddings to improve the performance. GA-MTCDR [75] combines user embeddings across all domains by element-wise attention to create better embeddings. Moreover, CAT-ART [32] utilizes contrastive loss to create global user embeddings, and enhances the performance within specific domain by combining global and local user embeddings. However, previous studies on MTCDR ignore the imbalanced user activities.

2.2 Contrastive Learning

Contrastive learning aims to ensure that the similarity scores for positive pairs exceed those of negative pairs, which is the cornerstone of most existing self-supervised models [9, 16, 18, 23, 45, 52].

For a given anchor point, a commonly used contrastive loss can be generally written as:

$$\mathcal{L}_i = -\log \frac{\exp(\operatorname{sim}(z_i, z_i^+)/\tau)}{\sum_{k \neq i} \exp(\operatorname{sim}(z_i, z_k)/\tau)} \tag{1}$$

where z_i is the feature of anchor point sample, z_i^+ is the feature of positive sample and $z_k (k \neq i)$ is the feature of negative sample, τ is the temperature parameter that controls the penalty strength on negative samples [54, 68], and $\operatorname{sim}(\cdot,\cdot)$ is the similarity function for two input vectors.

In the seminal studies of contrastive learning methods [9, 18], they directly optimize InfoNCE loss [42] to learn visual representations. To further enhance the effectiveness of contrastive learning, a series of studies dedicate to deal with hard negative samples [7, 11, 13, 25, 48, 58, 60, 68] or employ innovative contrasting techniques [4, 15, 34, 50, 51, 56]. Additionally, several recent studies aim to design novel contrastive losses to get better representations. For instance, spectral decomposition on the population augmentation graph is incorporated into contrastive learning, leading to the development of a new contrastive loss objective [17]. In order to enable most CL methods to break free from the dependency on large batch sizes, a global contrastive loss is introduced to attain provable guarantees [67]. Considering the long-tail distribution often observed in unsupervised learning, Qiu et al. [43] propose a novel contrastive loss with individualized temperatures and develop a mechanism for automatic temperature individualization. Inspired by Qiu et al. [43], this paper introduces a user-aware contrastive learning framework for cross-domain recommendation. Different from the contrastive learning in Qiu et al. [43], our proposed method necessitates the specially designed formulation of positive and negative sample pairs for each individual user. Consequently, this paper proposes a novel autoencoder structure coupled with a masking mechanism, aiming to mitigate the negative impact caused by imbalanced interactions across different users.

3 METHODOLOGY

In this section, we introduce our proposed method named User-aware Contrastive Learning for Robust cross-domain recommendation (UCLR). First, we elaborate the problem formulation of Multi-Target Cross-Domain Recommendation. Then, we provide an overview of UCLR framework. Furthermore, we give details of models consisted of UCLR and optimization methods. Finally, we also summarize the whole algorithm procedure and provide the convergence guarantee of user-aware contrastive learning in UCLR.

3.1 Problem Formulation

We focus on the MTCDR problem with a overlapped domain-shared user set U, and domain-specific item sets $\{V_1, \cdots, V_n\}$ for multiple domains, where n is the number of domains. For each domain d, user-item interactions are denoted by a matrix $R^d \in \mathbb{R}^{|U| \times |V_d|}$, where |U| and $|V_d|$ are the number of users and items respectively. Each element in matrix R^d is represented by $r^d_{ij} \in [0,1]$ indicating whether user i has interacted with item j, where $i \in \{1, \cdots, |U|\}$ and $j \in \{1, \cdots, |V_d|\}$. The goal of MTCDR problem is to enhance performance of recommendations over all domains simultaneously.

3.2 Overview of UCLR Framework

The illustration of UCLR framework is shown in Figure 2. First, we pretrain global user and item embedding matrices by adopting BPRMF model based on user-item interactions over all domains. Then, we develop contrastive dual-stream collaborative autoencoder, where one stream is to reconstruct the original global user embedding and the another stream is to generate user embedding that mitigate the effects from other users. In detail, the reconstruction stream takes the original global user embeddings as its input, while the generation stream works with randomly masked user embeddings. After encoding these two user embeddings, we apply user-aware contrastive loss with automatic temperature individualization to their latent representations of user embeddings, aiming to push the similarity score between the same users to be higher than that between different users. It is worth noting that individualized temperatures are able to control different degrees of the penalty strength for different users. Furthermore, we employ reconstruction loss to ensure the stability of autoencoders in two streams. Finally, to further enhance the performance within each domain, we adopt Low-Rank Adaption (LoRA) to finetune the whole framework of our method, as illustrated in Figure 2(b).

3.3 Pretrained Global Embedding

To fully exploit the rich information of different users across all domains, we integrate the historical user-item interactions from all domains and denote it as $R \in \mathbb{R}^{|U| \times (\sum_{i=1}^d |V_d|)}$. To factorize the interaction matrix R, we create two trainable embedding matrices $\mathbb{E} \in \mathbb{R}^{(|U|+1) \times m}$ and $\mathbb{I} \in \mathbb{R}^{(\sum_{i=1}^d |V_d|+1) \times m}$ to represent user and item embeddings, where m denotes the number of dimensions in the latent space. Given a user $u_i \in U$ and an item $v_j \in \{V_1, \cdots, V_n\}$, we can obtain a user embedding $E_i \in \mathbb{R}^m$ and an item embedding $I_j \in \mathbb{R}^m$ by adopting two embedding matrices. The preference score of the user u_i to the item v_j is computed by $r_{ij} = E_i^{\top} I_j$. Then, we employ the following BPR loss:

$$\mathcal{L}_{bpr} = -\sum_{i \in U} \sum_{j \in p_i} \sum_{k \notin p_i} \log \sigma(r_{ij} - r_{ik}) + \lambda_U \sum_{i \in U} ||E_i||_2 + \lambda_V \sum_{j \in \{V_1, \dots, V_n\}} ||I_j||_2,$$
(2)

where p_i is the set of items that user u_i has interacted, $\sigma(\cdot)$ represents the sigmoid function, λ_U and λ_V are the regularization terms. After pretraining two embedding matrices by BPRMF model, we can obtain global user and item embeddings that capture the user preferences across all domains.

3.4 Contrastive Dual-Stream Collaborative AutoEncoder

The pretrained global embeddings are derived from the interaction information of all users across multiple domains. Given the diverse interaction frequencies among different users in real-world scenarios, there arises a problem that not all embeddings are created equal. Such bias results in the BPR loss primarily enhancing the embeddings for users with frequent interactions, while neglecting those who are less active. To address this challenge, we develop contrastive dual-stream collaborative autoencoder.

The key idea is to ensure that the embeddings generated for the same user exhibit a higher similarity compared to those generated for different users, thereby mitigating the negative impact of imbalanced interaction frequencies among different users. To facilitate the understanding, we proceed to delve into the details. Given a global set of users U, we first obtain a pretrained global user embedding $\mathbf{E} \in \mathbb{R}^{|U| \times m}$, where E_i denotes user embedding for user i. More explicitly, $\mathbf{E} = [E_1, E_2, \cdots, E_{|U|}]^{\mathsf{T}}$. To eliminate the effect caused by different users, we randomly mask some of the user embeddings in \mathbf{E} by replacing the original embeddings with zero vectors according to mask ratio. The masked global user embedding is denoted as $\mathbf{E}' = [E_1, \mathbf{0}, \cdots, E_{|U|}]^{\mathsf{T}}$. For example, if we set mask ratio to 30%, it means that 30% of the user embeddings in \mathbf{E} will be replaced with zero vectors to obtain \mathbf{E}' .

In order to achieve the latent representations of global user embeddings, we employ a dual-stream autoencoder, with user embedding E and masked user embedding E' as its inputs. After encoding these two user embeddings, we denote their latent representations as **e** and **e**', respectively. Similarly, $\mathbf{e} = [e_1, e_2, \cdots, e_{|U|}]^{\mathsf{T}}$ where e_i is the latent representation of user embedding for user i. For each user i, we treat the embedding of the same user in the generation path as a positive sample, and those of other users as negative samples. Given the imbalanced interactions across different users, the pretrained global user embeddings necessitate varying penalty strengths for negative samples to ensure separable embedding space. Specifically, user embeddings created by rare interactions are more vulnerable to influences from other users, necessitating a smaller τ that can penalize much more on negative samples. Conversely, user embeddings created by frequent interactions are more readily influence others, demanding a larger τ that can treat all negative samples equally. Inspired by the recent study on contrastive learning [43], we propose a user-aware contrastive loss with individualized temperature, which is formulated as:

$$\mathcal{L}_{\text{con}}^{i} = -\tau_{i} \log \frac{\exp(\text{sim}(e_{i}, e_{i}^{\prime})/\tau_{i})}{\sum_{k \in U \setminus \{i\}} \exp(\text{sim}(e_{i}, e_{k}^{\prime})/\tau_{i})}, \tag{3}$$

where τ_i is an *individual* temperature for user i. Next, we decode the latent representations \mathbf{e} and $\mathbf{e'}$ in reconstructive and generative stream, respectively. The reconstructive stream autoencoder aims to enhance the ability of preserving the original pretrained global user embedding, while the generative stream strives to generate the user embeddings with random masking. We share the weights of dual-stream autoencoder to obtain better and more equal user embeddings based on the original ones. We denote the reconstructive user embeddings and generative user embeddings as $\hat{\mathbf{E}}$ and $\hat{\mathbf{E'}}$, where $\hat{\mathbf{E}} = [\hat{E}_1, \hat{E}_2, \cdots, \hat{E}_{|U|}]^{\top}$ and $\hat{\mathbf{E'}} = [\hat{E}_1', \hat{E}_2', \cdots, \hat{E}_{|U|}']^{\top}$. To ensure the stability of autoencoders, we also employ the following reconstructions loss for user i:

$$\mathcal{L}_{\text{rec}}^{i} = \|\hat{E}_{i} - E_{i}\|_{2}^{2} + \|\hat{E}_{i}' - E_{i}\|_{2}^{2}. \tag{4}$$

Finally, we jointly train our dual-stream autoencoder through the following combined loss:

$$\mathcal{L}_{\text{combined}} = \sum_{i \in U} \left(\mathcal{L}_{\text{con}}^{i} + \alpha \mathcal{L}_{\text{rec}}^{i} \right). \tag{5}$$

By minimizing the combined loss, we obtain better and more equal global user embedding for cross-domain recommendation.

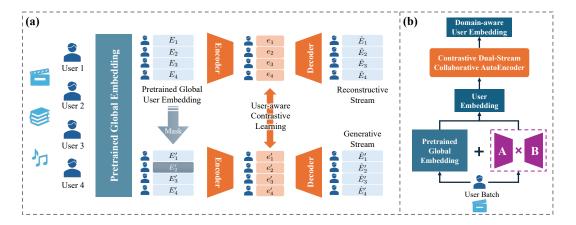


Figure 2: Overall framework of UCLR. (a) shows that UCLR consists of two sub-modules: pretrained global embedding and contrastive dual-stream collaborative autoencoder. (b) illustrates the method of domain-aware LoRA finetune in domain movie.

3.5 Domain-aware LoRA Finetune

To further improve the performance within each domain, we dedicate to finetune the framework of our method based on the user-item interations in each domain. For each domain d, we first adopt matrix factorization model with the BPR loss, which is formulated as:

$$\mathcal{L}_{\text{ft-bpr}}^{d} = -\sum_{i \in U} \sum_{j \in p_i^d} \sum_{k \notin p_i^d} \log \sigma(r_{ij} - r_{ik})$$

$$+ \lambda_U \sum_{i \in U} ||E_i||_2 + \lambda_V \sum_{j \in V_d} ||I_j||_2,$$

$$(6)$$

where p_i^d is the set of items that user u_i has interacted in domain d, $r_{ij} = E_i^{\mathsf{T}} I_j$ is the preference score, and λ_U and λ_V are the regularization terms. Then we construct the combined loss in (5) for contrastive dual-stream collaborative autoencoder. Therefore, the final finetuning loss for domain d can be concluded as:

$$\mathcal{L}_{\mathrm{ft}}^{d} = \mathcal{L}_{\mathrm{ft-bpr}}^{d} + \mathcal{L}_{\mathrm{combined}}.$$
 (7)

Nevertheless, directly optimizing model parameters with the finetune loss in (7) may encounter a issue that the pretrained model across all domains is over-parameterized for the finetuned model within one single domain. Following the hypothesis of previous studies [1, 31] that the learned over-parameterized models in fact reside on a low intrinsic dimension, we propose Low-Rank Adaption (LoRA) [22] to finetune the whole framework of UCLR. Domainaware LoRA finetuning method is illustrated in Fig 2(b). Specifically, we construct two trainable matrices $A \in \mathbb{R}^{r \times m}$ and $B \in \mathbb{R}^{|U| \times r}$, where r is the low rank that $r \ll |U|$. We denote the weight of pretrained global user embedding as $W_0 \in \mathbb{R}^{|U| \times m}$, and formulate the domain-aware LoRA finetuning update as, $W = W_0 + BA$. We fix the weight of pretrained global user embedding W_0 and optimize the weight of *A* and *B* by minimizing (7) during the finetuning stage. As a result, we can obtain the domain-aware finetuned embedding which is denoted as W.

Algorithm 1 User-aware contrastive learning for robust crossdomain recommendation

- 1: **Pretrain** user and item embeddings by adopting matrix factorization model with the BPR loss in (2) across all the domains
- 2: **Sample** a batch of users $\mathcal{B} \subset U$ and achieve pretrained global user embedding $\mathbf{E} \in \mathbb{R}^{|\mathcal{B}| \times m}$
- 3: Mask user embedding E to attain E'
- 4: **Encode** user embedding **E** and **E**' to obtain latent representations of user embeddings **e** and **e**'
- 5: **Compute** $\mathcal{L}_{\text{con}}^{i}$ in (3) for each user $E_{i} \in \mathbb{E}$ $(i = 1, \dots, |\mathcal{B}|)$
- 6: **Optimize** τ_i for each user $E_i \in E$ with the gradient of \mathcal{L}_{con}^i
- 7: **Decode** latent representations e and e' to achieve generative and reconstructive user embedding \hat{E} and \hat{E}'
- 8: Compute the combined loss $\mathcal{L}_{combined}$ in (5) for all users
- 9: **Optimize** the weight of contrastive dual-stream collaborative autoencoder with the gradient of $\mathcal{L}_{combined}$
- 10: **Finetune** the whole framework of two sub-modulues within specific domain d by employing LoRA with $\mathcal{L}_{\mathrm{ft}}^d$ in (7)

3.6 Algorithm Procedure

Our algorithm is summarized in Algorithm 1. To capture the user preferences across all the domains, we adopt BPRMF model to get pretrained global user and item embeddings in Step 1. To eliminate the negative effects from different users with diverse frequency of interactions, we employ user-aware contrastive learning. In Step 3, we first mask the pretrained global user embedding randomly. Then, we encoder two user embeddings in Step 4 and compute the user-aware contrastive loss of their latent representations in Step 5. Furthermore, we optimize the individualized temperature with the gradients of user-aware contrastive loss for each user. To control the structure of reconstructive and generative user embeddings, we utilize reconstruction loss to optimize the parameters of autoencoder in Step 9. Finally, we adopt domain-aware LoRA finetuning method to further enhance the performance of our method within each domain. Theoretically, we present the following convergence guarantee of user-aware contrastive learning.

Table 1: Statistics of Datasets

Dataset	Dataset Domain		#Items	#Interactions
Amazon	Books Movies Electronics	26507	102800 14912 26933	311539 153361 119342
Douban	Books Movies Music	1733	90096 33728 79179	206609 967475 176556

Theorem 1. Under the standard assumptions of stochastic optimization, by setting appropriate optimizer and learning rate, the user-aware contrastive learning can find an ϵ -stationary solution after $O\left(\frac{|U|}{|\mathcal{B}|^2 \epsilon^4}\right)$ iterations.

Remark 1. Theorem 1 indicates that our algorithm converges to a stationary solution for user-aware contrastive learning. The complexity $O\left(\frac{|U|}{|\mathcal{B}|^2\epsilon^4}\right)$ is same as the previous studies on contrastive learning [43, 67]. We highlight the differences between our theoretical analysis and theirs. Compared with Yuan et al. [67], our method employs individualized temperature instead of global temperature to address the problem that "not all embeddings are created equal". Compared with Qiu et al. [43], our negative samples in contrastive loss are from a deterministic set depending on the user embedding rather than a set independent from batch of samples.

4 EXPERIMENTS

To validate the effectiveness of our method, we conduct experiments to answer the following research questions (RQs):

- **RQ1**: How does our proposed method UCLR perform when compared with other baselines?
- RQ2: Does our proposed method UCLR address the problem that "not all embeddings are created equal"?
- RQ3: How do our proposed sub-modules contribute to the performance improvement?

4.1 Datasets

To make a fair comparison with existing work, we evaluate our method on two real-world datasets, including the Amazon dataset [19] and the Douban dataset. Additionally, we select three domains on each dataset to validate the effectiveness of our proposed MTCDR method. For the Amazon dataset, these domains are Books, Movies and Electronics; for the Douban dataset, they are Books, Movies, and Music. To validate the performance of the graph-based CDR method on the Amazon dataset, we preprocessed the raw Amazon dataset by randomly deleting 70% of the items. Table 1 provides concrete statistics of datasets with three domains. Furthermore, the motivation for this study is the observation that the interactions across different users are imbalanced in real-world scenarios. As illustrated in Figure 3, the phenomenon of data imbalance does exist in multiple domains of the Douban dataset, meaning that some users have frequent interactions with items while others have only a few. This phenomenon also appears in the Amazon dataset, which is illustrated in Appendix A.

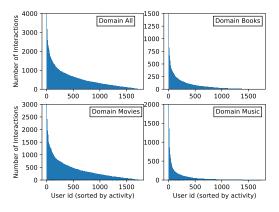


Figure 3: Illustration of imbalanced interactions across different users on the Douban dataset.

4.2 Experiment Setting

Evaluation. Following the previous studies [3, 29, 40], we adopt the widely used *leave-one-out* method to ensure a fair comparison. Specifically, during the testing stage, we construct a item set V_i^d by randomly sampling 1 positive item and 99 negative items for each user u_i in each domain d. A positive item refers to an item that the user u_i has interacted with in testing set. Conversely, negative items denote items that the user u_i has not interacted with across training, validation and testing sets. Subsequently, we rank 100 items in the item set V_i^d and evaluate the performance of *top-10/20* ranking results by employing three widely-used metrics, including Mean Reciprocal Rank (MRR) [44], Hit Ratio (HR), and Normalized Discounted Cumulative Gain (NDCG) [24].

Baselines. To demonstrate the effectiveness of our proposed CDR method, we compare UCLR with the following state-of-the-art methods, including (1) single-domain recommendation: BPRMF [47], NeuMF [21], and LightGCN [20]; (2) cross-domain recommendation: HeroGraph [12], GA-MTCDR [75], and CAT-ART [32].

Implementation. For a fair comparison, we conduct all the experiments by using PyTorch with python 3.7 and train the whole pipeline of all the models on Tesla A10 GPUs. Furthermore, we set all the embedding size to m = 128 for both single-domain recommendation and cross-domain recommendation methods. During training optimization, we apply a mini-batch size N=2048and the Adam optimizer [28] with fixed learning rate $\eta = 10^{-3}$. Next, we elaborate the details on our proposed method. For the contrastive dual-stream collaborative autoencoder, we construct the Multi-Layer Perceptron (MLP) where the size of the hidden layer is [128, 32]. In the loss function $\mathcal{L}_{combined}$ defined in (5) , we set $\alpha = 10^{-3}$. In the loss function \mathcal{L}_{bpr} defined in (2), we set the regularization terms $\lambda_U = \lambda_V = 10^{-5}$. For the individualized temperature au_i for each user u_i in the loss functions $\mathcal{L}_{ ext{con}}^i$ defined in (3), we bound the temperature parameter τ_i in $[10^{-5}, 1]$ by applying clipping technique. For a more comprehensive comparison of the experimental results, we repeate each experiment five times by employing different random seeds and record the average and standard deviation of the experimental results.

	Model	Amazon Domain	MRR	Metric@10 HR	NDCG	Douban Domain	MRR	Metric@10 HR	NDCG
ain	BPRMF	Books Movies Electronics	19.01 ± 0.08 31.51 ± 0.11 15.13 ± 0.12	32.32 ± 0.08 58.55 ± 0.26 32.26 ± 0.38	21.73 ± 0.06 37.93 ± 0.14 19.14 ± 0.17	Books Movies Music	22.19 ± 1.23 38.42 ± 0.41 17.82 ± 0.58	37.58 ± 1.59 73.00 ± 0.88 33.56 ± 1.24	25.84 ± 1.31 46.99 ± 0.45 21.54 ± 0.72
Single-domain	NeuMF	Books Movies Electronics	$ \begin{array}{c} 19.01 \pm 0.10 \\ 31.19 \pm 0.68 \\ 22.68 \pm 0.22 \end{array} $	35.56 ± 0.26 60.57 ± 0.74 44.92 ± 0.36	22.90 ± 0.07 38.14 ± 0.69 27.91 ± 0.25	Books Movies Music	26.67 ± 0.58 39.95 ± 0.30 24.41 ± 0.13	46.66 ± 1.92 71.83 ± 1.21 46.67 ± 0.57	31.41 ± 0.77 47.50 ± 0.52 29.68 ± 0.04
0)	LightGCN	Books Movies Electronics	19.23 ± 0.41 21.26 ± 0.97 18.42 ± 0.29	36.50 ± 0.91 57.52 ± 0.31 38.57 ± 0.43	23.30 ± 0.53 29.74 ± 0.84 23.16 ± 0.31	Books Movies Music	21.19 ± 0.33 28.72 ± 1.16 15.12 ± 0.37	41.40 ± 0.61 70.69 ± 1.92 36.43 ± 0.87	25.94 ± 0.11 38.58 ± 1.29 20.11 ± 0.48
Cross-domain	HeroGraph	Books Movies Electronics	$ \begin{array}{c} 19.61 \pm 0.32 \\ 34.55 \pm 0.10 \\ 23.26 \pm 0.06 \end{array} $	35.73 ± 0.47 61.95 ± 0.11 43.21 ± 0.25	23.39 ± 0.35 41.07 ± 0.10 27.97 ± 0.10	Books Movies Music	19.63 ± 0.22 28.10 ± 0.99 17.45 ± 0.62	39.72 ± 0.58 67.58 ± 1.33 39.22 ± 0.45	24.34 ± 0.27 37.41 ± 1.05 22.54 ± 0.56
	GA-MTCDR	Books Movies Electronics	20.43 ± 0.22 36.92 ± 0.18 22.48 ± 0.19	37.14 ± 0.25 65.65 ± 0.07 42.79 ± 0.20	24.35 ± 0.22 43.76 ± 0.16 27.26 ± 0.19	Books Movies Music	24.10 ± 0.47 39.92 ± 0.42 23.12 ± 0.42	43.81 ± 0.69 71.80 ± 1.09 44.09 ± 0.68	28.76 ± 0.49 47.50 ± 0.60 28.06 ± 0.44
	CAT-ART	Books Movies Electronics	21.70 ± 0.28 37.47 ± 0.12 22.91 ± 0.11	36.82 ± 0.43 65.78 ± 0.18 43.51 ± 0.18	25.27 ± 0.31 44.22 ± 0.11 27.77 ± 0.13	Books Movies Music	27.88 ± 0.48 39.87 ± 0.63 23.15 ± 0.45	46.86 ± 1.07 73.92 ± 1.39 41.91 ± 0.12	32.40 ± 0.63 47.55 ± 0.77 27.59 ± 0.34
Ours	UCLR	Books Movies Electronics		42.19 ± 0.16 66.00 ± 0.11 46.36 ± 0.04	28.47 ± 0.20 43.12 ± 0.13 29.03 ± 0.05	Books Movies Music	29.75 ± 0.50 40.33 ± 0.19 27.10 ± 0.36	48.85 ± 0.87 73.28 ± 1.35 48.08 ± 0.56	34.29 ± 0.59 48.17 ± 0.45 31.95 ± 0.31

Table 2: Performance (%) comparison between our proposed method and baselines on two datasets.

4.3 Performance Comparisons (RQ1)

The performances of our proposed UCLR method and all the baseline methods over two datasets across three domains according to Metric@10 are summarized in Table 2. As can be seen, compared with the baseline methods, our method achieves superior performance across most of domains over two datasets. From the experimental results, we have the following insightful observations: (1) The performances of the three single-domain recommendation methods vary across different datasets. For instance, Light-GCN performs best on Amazon-Books, while NeuMF shines on Amazon-Electronics, and BPRMF stands out on Douban-Movies. (2) Compared with single-domain recommendation methods, CDR approaches indeed achieve improvements by leveraging knowledge from multiple domains. (3) Although our proposed CDR method does not achieve the best performance in domain Movies on the Amazon and Douban datasets, the performance of our proposed method is still highly competitive with the top-performing CAT-ART method. Next, we delve into the reasons why UCLR underperforms CAT-ART in domain Movies. Firstly, in domain Movies of the Douban dataset, we observe that UCLR slightly lags behind CAT-ART in terms of HR metric. It is highly probable that the number of interactions in domain Movies is significantly higher than the other two domains in the Douban dataset, resulting in our created equal embeddings exhibiting a less pronounced effect. Secondly, in domain Movies of the Amazon dataset, UCLR appears to fall marginally behind CAT-ART on the MRR and NDCG metrics, both indicative of recommendation ranking. This discrepancy stems from domain Movies of the Amazon dataset containing the fewest number of items, potentially limiting the efficacy of our created

equal embeddings in optimizing the ranking order among a small set of items. It is also observable that the three CDR methods have varying performances across different domains in both datasets. Meanwhile, our proposed method outperforms the baseline methods in most scenarios, demonstrating greater robustness.

4.4 Refined Analysis (RQ2)

Given the frequent issue of imbalanced user interactions in realworld scenarios, existing CDR methods tend to overly focus on users with higher interactions during the construction of user embeddings. Consequently, this often results in the inability to provide accurate recommendations for users with fewer interactions in the target domain during the testing stage. To validate the existence of such bias, we conduct detailed experiments accordingly. Specifically, we focus our recommendation on the users with only one or two interactions in the Amazon dataset. For these users with fewer interactions, the performances of our proposed UCLR method and other CDR baseline methods over the Amazon dataset across three domains according to Metric@10 are summarized in Table 3. Compared with other CDR methods, our proposed method achieves significant performance improvement for less active users. This underscores the capability of our method to effectively address the problem that "not all embeddings are created equal" across all domains. We attribute the success of the UCLR method to user-aware contrastive learning, which is specially designed to eliminate the negative effects across different users. Diverging from the global temperature employed in traditional contrastive learning, our proposed user-aware contrastive learning method creates individualized temperatures for each user. This allows for continual adaptive

Table 3: Refined performance (%) comparison of CDR methods on users with fewer interactions.

Model	Amazon Domain	MRR	Metric@10 HR	NDCG
Hero Graph	Books Movies Elec.	17.25 ± 0.17 31.08 ± 0.50 20.19 ± 0.35	31.66 ± 0.06 65.16 ± 0.91 38.55 ± 0.72	20.62 ± 0.14 39.20 ± 0.56 24.52 ± 0.13
GA-M TCDR	Books Movies Elec.	17.21 ± 0.49 34.50 ± 0.29 19.88 ± 0.14	34.56 ± 0.15 61.98 ± 0.31 40.41 ± 0.43	21.27 ± 0.41 41.03 ± 0.30 24.69 ± 0.18
CAT- ART	Books Movies Elec.	$ \begin{array}{c} 17.56 \pm 0.74 \\ 34.50 \pm 0.86 \\ 21.48 \pm 0.41 \end{array} $	30.53 ± 1.06 60.42 ± 1.35 41.28 ± 0.25	20.62 ± 0.76 40.68 ± 0.99 26.15 ± 0.35
UCLR	Books Movies Elec.	20.53 ± 0.28 35.77 ± 0.26 21.88 ± 0.26	38.52 ± 0.29 67.33 ± 0.19 43.27 ± 0.32	24.75 ± 0.28 43.25 ± 0.18 26.92 ± 0.26

adjustment of the penalty strength across different users during the embedding creation stage. In real-world scenarios, our proposed method attentively considers the interaction information of each user equally, thereby enhancing the attractiveness of the product platform to less active users.

4.5 Ablation Study (RQ3)

We conduct ablation experiments to demonstrate the effectiveness of each proposed sub-modules. To illustrate the impact of different sub-modules, we conduct experiments on the following models:

- PGE: We adopt the pretrained global embedding model.
- PGE + AE: We further add the single-stream autoencoder with reconstruction loss.
- PGE + CL-AE: We employ dual-stream autoencoder with reconstruction loss and contrastive loss. For the contrastive loss here, we adopt a global temperature parameter.
- PGE + UCL: We further incorporate user-aware contrastive learning with individualized temperatures.
- UCLR: Finally, we employ domain-aware LoRA finetuning method within each domain.

The ablation results over two datasets are summarized in Table 4 and Table 5. From the ablation results, we have the following insightful observations: (1) We pretrain the BPRMF model across all domains to obtain the pretrained global embedding. Compared with the BPRMF model trained individually on each single domain as shown in Table 2, the performance of the PGE model improve in domain Books and Electronics on both datasets. (2) After incorporating the AutoEncoder, the model can mitigate the negative impact between different domains through the reconstruction process. However, performance issues still persist in domain Movies of the Douban dataset. (3) With the dual-stream AutoEncoder based on contrastive learning, we improve the performance across all domains. However, there are still two issues: the enhancement is not pronounced, and there is a decline in performance on domain Movies of the Amazon dataset. (4) We refine the contrastive learning by introducing a novel user-aware contrastive loss objective, where we transition from a global temperature to automatically

Table 4: Ablation results (%) on the Amazon dataset.

Model	Amazon Domain	MRR	Metric@10 HR	NDCG
PGE	Books Movies Elec.	19.34 ± 0.41 31.03 ± 0.49 18.98 ± 0.18	34.98 ± 0.54 59.32 ± 0.64 38.22 ± 0.44	23.03 ± 0.44 37.75 ± 0.53 23.50 ± 0.23
PGE+ AE	Books Movies Elec.	19.40 ± 0.06 33.55 ± 0.08 22.18 ± 0.04	36.52 ± 0.18 63.18 ± 0.08 43.99 ± 0.14	23.42 ± 0.09 40.58 ± 0.07 27.30 ± 0.06
PGE+ CL-AE	Books Movies Elec.	20.06 ± 0.36 32.84 ± 0.17 22.99 ± 0.32	37.41 ± 0.44 63.74 ± 0.11 45.17 ± 0.43	23.91 ± 0.39 40.18 ± 0.12 28.22 ± 0.34
PGE+ UCL-AE	Books Movies Elec.	22.46 ± 0.17 35.48 ± 0.04 23.63 ± 0.09	40.97 ± 0.06 65.34 ± 0.09 45.20 ± 0.07	26.83 ± 0.14 42.59 ± 0.02 29.03 ± 0.09
UCLR	Books Movies Elec.		42.19 ± 0.16 66.00 ± 0.11 46.36 ± 0.04	28.47 ± 0.20 43.12 ± 0.13 29.03 ± 0.05

optimized individual temperatures for all users. This overall lead to a noticeable improvement in performance across all domains. (5) Lastly, we adopt domain-aware LoRA finetuning method to tackle the over-parameterization problem arising from transferring from the global model to the domain-specific model. As can be seen, it is evident that LoRA plays a crucial role in improving the performance of UCLR. These observations underscore the pivotal role each sub-module of the UCLR method plays in cross-domain recommendation.

5 CONCLUSION

This paper investigates the multi-target cross-domain recommendation (MTCDR) problem. In real-world scenarios, the frequency of interactions from different users can be extremely diverse. The bias in creating embeddings hinders most CDR methods from making accurate recommendations for less active users. To address the problem that "not all embeddings are created equal", we propose User-aware Contrastive Learning for Robust cross-domain recommendation (UCLR) in this paper. First, we develop pretrained global embedding to capture user preferences from all observable domains. Second, we build contrastive dual-stream collaborative autoencoder, where one stream is to reconstruct the original user embedding and another stream is to generate more equal user embedding by optimizing the user-aware contrastive loss with individualized temperatures. Third, we adopt low-rank adaption (LoRA) to finetune the whole framework of UCLR. Compared with the previous CDR studies, our proposed model effectively handles the issue of imbalanced interactions across different users, leading to a significant performance enhancement.

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REFERENCES

- Armen Aghajanyan, Sonal Gupta, and Luke Zettlemoyer. 2021. Intrinsic Dimensionality Explains the Effectiveness of Language Model Fine-Tuning. In Proceedings of the 59th Annual Meeting of the Association for Computational Linguistics and the 11th International Joint Conference on Natural Language Processing. 7319–7328.
- [2] Jiangxia Cao, Shaoshuai Li, Bowen Yu, Xiaobo Guo, Tingwen Liu, and Bin Wang. 2023. Towards Universal Cross-Domain Recommendation. In Proceedings of the Sixteenth ACM International Conference on Web Search and Data Mining. 78–86.
- [3] Jiangxia Cao, Xixun Lin, Xin Cong, Jing Ya, Tingwen Liu, and Bin Wang. 2022. DisenCDR: Learning Disentangled Representations for Cross-Domain Recommendation. In Proceedings of the 45th International ACM SIGIR Conference on Research and Development in Information Retrieval. 267–277.
- [4] Mathilde Caron, Ishan Misra, Julien Mairal, Priya Goyal, Piotr Bojanowski, and Armand Joulin. 2020. Unsupervised Learning of Visual Features by Contrasting Cluster Assignments. In Advances in Neural Information Processing Systems. 9912– 9924.
- [5] Jianxin Chang, Chenbin Zhang, Yiqun Hui, Dewei Leng, Yanan Niu, Yang Song, and Kun Gai. 2023. PEPNet: Parameter and Embedding Personalized Network for Infusing with Personalized Prior Information. In Proceedings of the 29th ACM SIGKDD Conference on Knowledge Discovery and Data Mining. 3795–3804.
- [6] Jiawei Chen, Hande Dong, Xiang Wang, Fuli Feng, Meng Wang, and Xiangnan He. 2023. Bias and Debias in Recommender System: A Survey and Future Directions. ACM Transactions on Information Systems (2023).
- [7] Junya Chen, Zhe Gan, Xuan Li, Qing Guo, Liqun Chen, Shuyang Gao, Tagyoung Chung, Yi Xu, Belinda Zeng, Wenlian Lu, et al. 2021. Simpler, faster, stronger: Breaking the log-k curse on contrastive learners with flatnce. arXiv preprint arXiv:2107.01152 (2021).
- [8] Ling-Hao Chen, JiaWei Zhang, Yewen Li, Yiren Pang, Xiaobo Xia, and Tongliang Liu. 2023. HumanMAC: Masked Motion Completion for Human Motion Prediction. In Proceedings of the IEEE/CVF International Conference on Computer Vision. 9544–9555.
- [9] Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. 2020. A Simple Framework for Contrastive Learning of Visual Representations. In Proceedings of the 37th International Conference on Machine Learning. 1597–1607.
- [10] Heng-Tze Cheng, Levent Koc, Jeremiah Harmsen, Tal Shaked, Tushar Chandra, Hrishi Aradhye, Glen Anderson, Greg Corrado, Wei Chai, Mustafa Ispir, Rohan Anil, Zakaria Haque, Lichan Hong, Vihan Jain, Xiaobing Liu, and Hemal Shah. 2016. Wide & deep learning for recommender systems. In Proceedings of the 1st Workshop on Deep Learning for Recommender Systems. 7–10.
- [11] Ching-Yao Chuang, Joshua Robinson, Yen-Chen Lin, Antonio Torralba, and Stefanie Jegelka. 2020. Debiased Contrastive Learning. In Advances in Neural Information Processing Systems. 8765–8775.
- [12] Qiang Cui, Tao Wei, Yafeng Zhang, and Qing Zhang. 2020. HeroGRAPH: A heterogeneous graph framework for multi-target cross-domain recommendation. Proceedings of the 3rd Workshop on Online Recommender Systems and User Modeling co-located with the 14th ACM Conference on Recommender Systems (2020).
- [13] Debidatta Dwibedi, Yusuf Aytar, Jonathan Tompson, Pierre Sermanet, and Andrew Zisserman. 2021. With a little help from my friends: Nearest-neighbor contrastive learning of visual representations. In Proceedings of the IEEE/CVF International Conference on Computer Vision. 9588–9597.
- [14] Ali Mamdouh Elkahky, Yang Song, and Xiaodong He. 2015. A Multi-View Deep Learning Approach for Cross Domain User Modeling in Recommendation Systems. In Proceedings of the 24th International Conference on World Wide Web. 278–288
- [15] Songwei Ge, Shlok Mishra, Chun-Liang Li, Haohan Wang, and David Jacobs. 2021. Robust Contrastive Learning Using Negative Samples with Diminished Semantics. In Advances in Neural Information Processing Systems. 27356–27368.
- [16] Priya Goyal, Mathilde Caron, Benjamin Lefaudeux, Min Xu, Pengchao Wang, Vivek Pai, Mannat Singh, Vitaliy Liptchinsky, Ishan Misra, Armand Joulin, et al. 2021. Self-supervised pretraining of visual features in the wild. arXiv preprint arXiv:2103.01988 (2021).
- [17] Jeff Z. HaoChen, Colin Wei, Adrien Gaidon, and Tengyu Ma. 2021. Provable Guarantees for Self-Supervised Deep Learning with Spectral Contrastive Loss. In Advances in Neural Information Processing Systems. 5000–5011.
- [18] Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. 2020. Momentum Contrast for Unsupervised Visual Representation Learning. In Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition. 9729–9738.
- [19] Ruining He and Julian McAuley. 2016. Ups and Downs: Modeling the Visual Evolution of Fashion Trends with One-Class Collaborative Filtering. In Proceedings of the 25th International Conference on World Wide Web. 507–517.
- [20] Xiangnan He, Kuan Deng, Xiang Wang, Yan Li, Yongdong Zhang, and Meng Wang. 2020. Lightgcn: Simplifying and powering graph convolution network for recommendation. In Proceedings of the 43rd International ACM SIGIR Conference on Research and Development in Information Retrieval. 639–648.
- [21] Xiangnan He, Lizi Liao, Hanwang Zhang, Liqiang Nie, Xia Hu, and Tat-Seng Chua. 2017. Neural collaborative filtering. In Proceedings of the 26th International Conference on World Wide Web. 173–182.

- [22] Edward J Hu, yelong shen, Phillip Wallis, Zeyuan Allen-Zhu, Yuanzhi Li, Shean Wang, Lu Wang, and Weizhu Chen. 2022. LoRA: Low-Rank Adaptation of Large Language Models. In International Conference on Learning Representations.
- [23] Zhicheng Huang, Xiaojie Jin, Chengze Lu, Qibin Hou, Ming-Ming Cheng, Dongmei Fu, Xiaohui Shen, and Jiashi Feng. 2022. Contrastive masked autoencoders are stronger vision learners. arXiv preprint arXiv:2207.13532 (2022).
- [24] Kalervo Järvelin and Jaana Kekäläinen. 2002. Cumulated Gain-Based Evaluation of IR Techniques. ACM Transaction on Information Systems (2002), 422–446.
- [25] Yannis Kalantidis, Mert Bulent Sariyildiz, Noe Pion, Philippe Weinzaepfel, and Diane Larlus. 2020. Hard Negative Mixing for Contrastive Learning. In Advances in Neural Information Processing Systems. 21798–21809.
- [26] Heishiro Kanagawa, Hayato Kobayashi, Nobuyuki Shimizu, Yukihiro Tagami, and Taiji Suzuki. 2019. Cross-Domain Recommendation via Deep Domain Adaptation. In European Conference on Information Retrieval. 20–29.
- [27] SeongKu Kang, Junyoung Hwang, Dongha Lee, and Hwanjo Yu. 2019. Semi-Supervised Learning for Cross-Domain Recommendation to Cold-Start Users. In Proceedings of the 28th ACM International Conference on Information and Knowledge Management. 1563–1572.
- [28] Diederik P. Kingma and Jimmy Lei Ba. 2015. Adam: A Method for Stochastic Optimization. In International Conference on Learning Representations.
- [29] Walid Krichene and Steffen Rendle. 2020. On Sampled Metrics for Item Recommendation. In Proceedings of the 26th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining. 1748–1757.
- [30] Adit Krishnan, Mahashweta Das, Mangesh Bendre, Hao Yang, and Hari Sundaram. 2020. Transfer Learning via Contextual Invariants for One-to-Many Cross-Domain Recommendation. In Proceedings of the 43rd International ACM SIGIR Conference on Research and Development in Information Retrieval. 1081–1090.
- [31] Chunyuan Li, Heerad Farkhoor, Rosanne Liu, and Jason Yosinski. 2018. Measuring the Intrinsic Dimension of Objective Landscapes. In International Conference on Learning Representations.
- [32] Chenglin Li, Yuanzhen Xie, Chenyun Yu, Bo Hu, Zang Li, Guoqiang Shu, Xiaohu Qie, and Di Niu. 2023. One for All, All for One: Learning and transferring user embeddings for cross-domain recommendation. In Proceedings of the 16th ACM International Conference on Web Search and Data Mining. 366–374.
- [33] Chenglin Li, Mingjun Zhao, Huanming Zhang, Chenyun Yu, Lei Cheng, Guoqiang Shu, BeiBei Kong, and Di Niu. 2022. RecGURU: Adversarial Learning of Generalized User Representations for Cross-Domain Recommendation. In Proceedings of the Fifteenth ACM International Conference on Web Search and Data Mining. 571–581.
- [34] Junnan Li, Pan Zhou, Caiming Xiong, and Steven Hoi. 2021. Prototypical Contrastive Learning of Unsupervised Representations. In International Conference on Learning Representations.
- [35] Pan Li and Alexander Tuzhilin. 2020. DDTCDR: Deep dual transfer cross domain recommendation. In Proceedings of the 13rd ACM International Conference on Web Search and Data Mining. 331–339.
- 36] Pan Li and Alexander Tuzhilin. 2023. Dual Metric Learning for Effective and Efficient Cross-Domain Recommendations. IEEE Transactions on Knowledge and Data Engineering (2023), 321–334.
- [37] Siqing Li, Liuyi Yao, Shanlei Mu, Wayne Xin Zhao, Yaliang Li, Tonglei Guo, Bolin Ding, and Ji-Rong Wen. 2021. Debiasing Learning based Cross-domain Recommendation. In Proceedings of the 27th ACM SIGKDD Conference on Knowledge Discovery & Data Mining. 3190–3199.
- [38] Xiaopeng Li, Fan Yan, Xiangyu Zhao, Yichao Wang, Bo Chen, Huifeng Guo, and Ruiming Tang. 2023. HAMUR: Hyper Adapter for Multi-Domain Recommendation. In Proceedings of the 32nd ACM International Conference on Information and Knowledge Management. 1268–1277.
- [39] Jian Liu, Pengpeng Zhao, Fuzhen Zhuang, Yanchi Liu, Victor S. Sheng, Jiajie Xu, Xiaofang Zhou, and Hui Xiong. 2020. Exploiting Aesthetic Preference in Deep Cross Networks for Cross-Domain Recommendation. In *Proceedings of The Web Conference* 2020. 2768–2774.
- [40] Meng Liu, Jianjun Li, Guohui Li, and Peng Pan. 2020. Cross domain recommendation via bi-directional transfer graph collaborative filtering networks. In Proceedings of the 29th ACM International Conference on Information and Knowledge Management. 885–894.
- [41] Tong Man, Huawei Shen, Xiaolong Jin, and Xueqi Cheng. 2017. Cross-Domain Recommendation: An Embedding and Mapping Approach. In Proceedings of the Twenty-Sixth International Joint Conference on Artificial Intelligence. 2464–2470.
- [42] Aaron van den Oord, Yazhe Li, and Oriol Vinyals. 2018. Representation learning with contrastive predictive coding. arXiv preprint arXiv:1807.03748 (2018).
- [43] Zi-Hao Qiu, Quanqi Hu, Zhuoning Yuan, Denny Zhou, Lijun Zhang, and Tianbao Yang. 2023. Not All Semantics are Created Equal: Contrastive Self-supervised Learning with Automatic Temperature Individualization. In Proceedings of the 40th International Conference on Machine Learning. 28389–28421.
- [44] Dragomir R. Radev, Hong Qi, Harris Wu, and Weiguo Fan. 2002. Evaluating Web-based Question Answering Systems. In Proceedings of the Third International Conference on Language Resources and Evaluation.
- [45] Alec Radford, Jong Wook Kim, Chris Hallacy, Aditya Ramesh, Gabriel Goh, Sandhini Agarwal, Girish Sastry, Amanda Askell, Pamela Mishkin, Jack Clark,

- Gretchen Krueger, and Ilya Sutskever. 2021. Learning Transferable Visual Models From Natural Language Supervision. In *Proceedings of the 38th International Conference on Machine Learning*. 8748–8763.
- [46] Weijieying Ren, Lei Wang, Kunpeng Liu, Ruocheng Guo, Lim Ee Peng, and Yanjie Fu. 2022. Mitigating Popularity Bias in Recommendation with Unbalanced Interactions: A Gradient Perspective. In *IEEE International Conference on Data Mining*. 438–447.
- [47] Steffen Rendle, Christoph Freudenthaler, Zeno Gantner, and Lars Schmidt-Thieme. 2009. BPR: Bayesian personalized ranking from implicit feedback. In Proceedings of the 25th Conference on Uncertainty in Artificial Intelligence. 452–461.
- [48] Joshua David Robinson, Ching-Yao Chuang, Suvrit Sra, and Stefanie Jegelka. 2021. Contrastive Learning with Hard Negative Samples. In International Conference on Learning Representations.
- [49] Ashish Kumar Sahu and Pragya Dwivedi. 2020. Knowledge transfer by domainindependent user latent factor for cross-domain recommender systems. Future Generation Computer Systems (2020), 320–333.
- [50] Alex Tamkin, Mike Wu, and Noah Goodman. 2021. Viewmaker Networks: Learning Views for Unsupervised Representation Learning. In *International Conference on Learning Representations*. https://openreview.net/forum?id=enoVQWLsfyL
- [51] Yonglong Tian, Chen Sun, Ben Poole, Dilip Krishnan, Cordelia Schmid, and Phillip Isola. 2020. What Makes for Good Views for Contrastive Learning?. In Advances in Neural Information Processing Systems. 6827–6839.
- [52] Nenad Tomasev, Ioana Bica, Brian McWilliams, Lars Buesing, Razvan Pascanu, Charles Blundell, and Jovana Mitrovic. 2022. Pushing the limits of self-supervised ResNets: Can we outperform supervised learning without labels on ImageNet? arXiv preprint arXiv:2201.05119 (2022).
- [53] Cheng Wang, Mathias Niepert, and Hui Li. 2020. RecSys-DAN: Discriminative Adversarial Networks for Cross-Domain Recommender Systems. IEEE Transactions on Neural Networks and Learning Systems 8 (2020), 2731–2740.
- [54] Feng Wang and Huaping Liu. 2021. Understanding the behaviour of contrastive loss. In Proceedings of the IEEE/CVF conference on computer vision and pattern recognition. 2495–2504.
- [55] Lei Wang, Ee-Peng Lim, Zhiwei Liu, and Tianxiang Zhao. 2022. Explanation Guided Contrastive Learning for Sequential Recommendation. In Proceedings of the 31st ACM International Conference on Information & Knowledge Management. 2017–2027.
- [56] Xiao Wang and Guo-Jun Qi. 2022. Contrastive learning with stronger augmentations. IEEE transactions on pattern analysis and machine intelligence (2022), 5549–5560.
- [57] Yaqing Wang, Chunyan Feng, Caili Guo, Yunfei Chu, and Jenq-Neng Hwang. 2019. Solving the Sparsity Problem in Recommendations via Cross-Domain Item Embedding Based on Co-Clustering. In Proceedings of the Twelfth ACM International Conference on Web Search and Data Mining. 717–725.
- [58] Mike Wu, Milan Mosse, Chengxu Zhuang, Daniel Yamins, and Noah Goodman. 2021. Conditional Negative Sampling for Contrastive Learning of Visual Representations. In *International Conference on Learning Representations*.
- [59] Xiaobo Xia, Wenhao Yang, Jie Ren, Yewen Li, Yibing Zhan, Bo Han, and Tongliang Liu. 2022. Pluralistic Image Completion with Gaussian Mixture Models. In Advances in Neural Information Processing Systems, Vol. 35. 24087–24100.
- [60] Jiahao Xie, Xiaohang Zhan, Ziwei Liu, Yew-Soon Ong, and Chen Change Loy. 2022. Delving into inter-image invariance for unsupervised visual representations. International Journal of Computer Vision (2022), 2994–3013.
- [61] Huan Yan, Chunfeng Yang, Donghan Yu, Yong Li, Depeng Jin, and Dah Ming Chiu. 2021. Multi-Site User Behavior Modeling and Its Application in Video Recommendation. IEEE Transactions on Knowledge and Data Engineering (2021), 180–193.

- [62] Longqi Yang, Yin Cui, Yuan Xuan, Chenyang Wang, Serge Belongie, and Deborah Estrin. 2018. Unbiased Offline Recommender Evaluation for Missing-Notat-Random Implicit Feedback. In Proceedings of the 12th ACM Conference on Recommender Systems. 279–287.
- [63] Dong Yao, Zhou Zhao, Shengyu Zhang, Jieming Zhu, Yudong Zhu, Rui Zhang, and Xiuqiang He. 2022. Contrastive Learning with Positive-Negative Frame Mask for Music Representation. In Proceedings of the ACM Web Conference 2022. 2906–2915.
- [64] Jinfeng Yi, Cho-Jui Hsieh, Kush R. Varshney, Lijun Zhang, and Yao Li. 2017. Scalable Demand-Aware Recommendation. In Advance in Neural Information Processing Systems 30. 2409–2418.
- [65] Rex Ying, Ruining He, Kaifeng Chen, Pong Eksombatchai, William L. Hamilton, and Jure Leskovec. 2018. Graph Convolutional Neural Networks for Web-Scale Recommender Systems. In Proceedings of the 24th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining. 974–983.
- [66] Feng Yuan, Lina Yao, and Boualem Benatallah. 2019. DARec: Deep Domain Adaptation for Cross-Domain Recommendation via Transferring Rating Patterns. In Proceedings of the Twenty-Eighth International Joint Conference on Artificial Intelligence. 4227–4233.
- [67] Zhuoning Yuan, Yuexin Wu, Zi-Hao Qiu, Xianzhi Du, Lijun Zhang, Denny Zhou, and Tianbao Yang. 2022. Provable Stochastic Optimization for Global Contrastive Learning: Small Batch Does Not Harm Performance. In Proceedings of the 39th International Conference on Machine Learning. 25760–25782.
- [68] Chaoning Zhang, Kang Zhang, Trung X Pham, Axi Niu, Zhinan Qiao, Chang D Yoo, and In So Kweon. 2022. Dual temperature helps contrastive learning without many negative samples: Towards understanding and simplifying moco. In Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition. 14441–14450.
- [69] Yang Zhang, Yue Shen, Dong Wang, Jinjie Gu, and Guannan Zhang. 2023. Connecting Unseen Domains: Cross-Domain Invariant Learning in Recommendation. In Proceedings of the 46th International ACM SIGIR Conference on Research and Development in Information Retrieval. 1894–1898.
- [70] Cheng Zhao, Chenliang Li, Rong Xiao, Hongbo Deng, and Aixin Sun. 2020. CATN: Cross-Domain Recommendation for Cold-Start Users via Aspect Transfer Network. In Proceedings of the 43rd International ACM SIGIR Conference on Research and Development in Information Retrieval. 229–238.
- [71] Chuang Zhao, Hongke Zhao, Ming HE, Jian Zhang, and Jianping Fan. 2023. Cross-Domain Recommendation via User Interest Alignment. In Proceedings of the ACM Web Conference 2023. 887–896.
- [72] Feng Zhu, Chaochao Chen, Yan Wang, Guanfeng Liu, and Xiaolin Zheng. 2019. DTCDR: A Framework for Dual-Target Cross-Domain Recommendation. In Proceedings of the 28th ACM International Conference on Information and Knowledge Management. 1533–1542.
- [73] Feng Zhu, Yan Wang, Chaochao Chen, Guanfeng Liu, and Xiaolin Zheng. 2020. A Graphical and Attentional Framework for Dual-Target Cross-Domain Recommendation. In Proceedings of the Twenty-Ninth International Joint Conference on Artificial Intelligence. 3001–3008.
- [74] Feng Zhu, Yan Wang, Chaochao Chen, Jun Zhou, Longfei Li, and Guanfeng Liu. 2021. Cross-domain recommendation: challenges, progress, and prospects. In Proceedings of the 30th International Joint Conference on Artificial Intelligence. 950–958.
- [75] Feng Zhu, Yan Wang, Jun Zhou, Chaochao Chen, Longfei Li, and Guanfeng Liu. 2023. A Unified Framework for Cross-Domain and Cross-System Recommendations. IEEE Transactions on Knowledge and Data Engineering (2023), 1171–1184.
- [76] Yongchun Zhu, Zhenwei Tang, Yudan Liu, Fuzhen Zhuang, Ruobing Xie, Xu Zhang, Leyu Lin, and Qing He. 2022. Personalized Transfer of User Preferences for Cross-Domain Recommendation. In Proceedings of the Fifteenth ACM International Conference on Web Search and Data Mining. 1507–1515.

A ADDITIONAL EXPERIMENTS

A.1 Illustration of the Amazon Dataset

As illustrated in Figure 4, data imbalance problem also exists in multiple domains of the Amazon dataset, meaning that some users have frequent interactions with items while others have only a few.

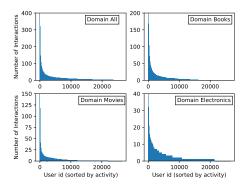


Figure 4: Illustration of imbalanced interactions across different users on the Amazon dataset.

A.2 More Performance Comparison

In Table 8, we provide the additional performances of our proposed UCLR method and all the baseline methods over two datasets across three domains according to Metric@20. We introduce an additional baseline, named as Recycs-DAN [53], which addresses both cross-domain and within-domain data imbalance.

A.3 Ablation Study

We provide the ablation study on the Douban dataset in Table 5.

Table 5: Ablation results (%) on the Douban dateset.

Model	Douban		Metric@10	
	Domain	MRR	HR	NDCG
	Books	25.75 ± 0.68	43.79 ± 0.87	28.73 ± 0.72
PGE	Movies	32.54 ± 0.31	68.26 ± 0.38	40.97 ± 0.34
	Music	22.11 ± 0.31	43.39 ± 0.88	27.15 ± 0.40
PGE+	Books	26.47 ± 1.13	44.54 ± 1.74	30.09 ± 1.28
PGE+ AE	Movies	35.24 ± 0.25	69.82 ± 1.53	43.43 ± 0.55
AL	Music	22.52 ± 0.19	43.27 ± 0.76	27.43 ± 0.24
PGE+	Books	26.91 ± 0.73	44.76 ± 1.10	31.16 ± 0.80
CL-AE	Movies	38.44 ± 0.51	71.37 ± 1.40	46.27 ± 0.70
CL-AE	Music	23.86 ± 0.12	43.41 ± 0.18	28.49 ± 0.11
PGE+	Books	28.97 ± 0.56	47.80 ± 0.72	33.46 ± 0.59
UCL-AE	Movies	40.24 ± 0.35	73.12 ± 1.62	48.07 ± 0.63
UCL-AE	Music	26.75 ± 0.47	47.88 ± 0.44	31.74 ± 0.43
	Books	29.75 ± 0.50	48.85 ± 0.87	34.29 ± 0.59
UCLR	Movies	40.33 ± 0.19	73.28 ± 1.35	48.17 ± 0.45
	Music	27.10 ± 0.36	$\textbf{48.08} \pm 0.56$	31.95 ± 0.31

A.4 More Baselines for Pretrained Embedding

Within the framework of UCLR, we choose BPRMF as pretrained global embeddings. In the literature, there exist other baselines caplable of learning better user representations, such as LightGCN [20] and PEPNet [5]. We conduct experiments that incorporate these baselines into our framework on the Amazon dataset, with results presented in the Table 6.

Table 6: Performance (%) comparison on pretrained models.

Model	Amazon Domain	Metric@10 MRR HR		NDCG
UCLR with LightGCN	Books Movies Elec.	22.66 ± 0.10 34.42 ± 0.12 23.11 ± 0.05	40.13 ± 0.25 62.21 ± 0.11 43.41 ± 0.11	26.29 ± 0.13 41.03 ± 0.09 27.90 ± 0.12
UCLR with PEPNet	Books Movies Elec.	20.41 ± 0.48 32.67 ± 0.58 24.30 ± 0.41	37.12 ± 0.66 64.74 ± 0.45 46.09 ± 0.51	24.35 ± 0.52 40.33 ± 0.55 29.46 ± 0.43
UCLR with BPRMF	Books Movies Elec.	24.17 ± 0.22 35.97 ± 0.14 23.68 ± 0.07	42.19 ± 0.16 66.00 ± 0.11 46.36 ± 0.04	28.47 ± 0.20 43.12 ± 0.13 29.03 ± 0.05

A.5 Illustration of User Temperatures

Regarding the Amazon dataset, we categorize its 26,507 users into 9 groups based on the number of interactions, arranging them from the most to the least active, and calculate the average and standard deviation of their temperatures for each group (See Figure 5).

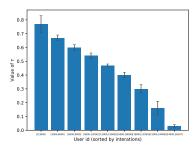


Figure 5: Illustration of user temperatures.

A.6 Running Time of UCLR

We summarize the running time of our proposed UCLR and other three CDR baselines in Table 7.

Table 7: Running time comparison.

Method	GA-MTCDR	HeroGraph	CAT-ART	UCLR
Training	1172s	1260s	1255s	1563s
Inference	153s	151s	157s	164s

Metric@20 Amazon Metric@20 Douban Model Domain MRR HR NDCG Domain MRR HR NDCG **Books** 19.09 ± 0.07 41.54 ± 0.38 24.04 ± 0.07 Books 22.92 ± 1.20 48.14 ± 1.14 28.50 ± 1.19 **BPRMF** Movies 32.28 ± 0.11 69.46 ± 0.16 40.69 ± 0.09 39.33 ± 0.37 85.30 ± 0.32 50.29 ± 0.28 Movies Single-domain Electronics 14.07 ± 0.05 35.93 ± 0.26 18.87 ± 0.10 Music 18.56 ± 0.52 44.25 ± 1.03 24.23 ± 0.55 25.47 ± 0.05 Books 19.71 ± 0.09 45.78 ± 0.28 Books 27.29 ± 0.58 54.12 ± 1.36 33.71 ± 0.71 Movies NeuMF Movies 32.05 ± 0.67 72.87 ± 0.59 41.26 ± 0.65 40.87 ± 0.26 84.96 ± 0.40 50.84 ± 0.33 Electronics 23.50 ± 0.24 56.74 ± 0.55 30.90 ± 0.30 Music 25.09 ± 0.13 56.15 ± 0.55 32.19 ± 0.03 29.00 ± 0.06 Books 19.97 ± 0.42 47.35 ± 1.06 26.03 ± 0.57 **Books** 22.02 ± 0.30 53.54 ± 1.19 LightGCN Movies 22.17 ± 0.92 70.48 ± 0.38 33.04 ± 0.70 29.71 ± 1.11 42.14 ± 1.05 Movies 84.63 ± 0.73 19.19 ± 0.28 16.12 ± 0.34 Electronics 49.63 ± 0.20 25.96 ± 0.27 Music 50.98 ± 0.37 23.78 ± 0.36 **Books** 20.34 ± 0.31 46.49 ± 0.25 26.10 ± 0.30 Books 20.45 ± 0.16 51.58 ± 0.68 27.34 ± 0.17 HeroGraph Movies 35.31 ± 0.10 72.85 ± 0.16 43.83 ± 0.09 29.16 ± 0.97 82.33 ± 0.88 41.18 ± 0.97 Movies Electronics 24.05 ± 0.06 54.69 ± 0.11 30.86 ± 0.07 Music 18.29 ± 0.57 51.62 ± 0.59 25.66 ± 0.38 29.64 ± 0.50 **Books** 22.34 ± 0.16 49.91 ± 0.03 28.44 ± 0.13 Books 57.79 ± 0.75 36.06 ± 0.53 Cross-domain Recycs-DAN 35.68 ± 0.13 76.99 ± 0.08 45.10 ± 0.11 85.05 ± 0.98 44.40 ± 0.66 Movies Movies 32.44 ± 0.63 Electronics 24.08 ± 0.13 57.64 ± 0.07 31.58 ± 0.10 Music 24.43 ± 0.33 54.34 ± 0.88 31.22 ± 0.44 **Books** 21.17 ± 0.21 47.79 ± 0.35 27.04 ± 0.21 24.77 ± 0.50 31.21 ± 0.60 Books 53.56 ± 1.07 **GA-MTCDR** 37.70 ± 0.17 76.77 ± 0.15 46.58 ± 0.11 Movies Movies 40.78 ± 0.40 84.16 ± 0.88 50.63 ± 0.54 Electronics 23.30 ± 0.19 54.69 ± 0.20 30.26 ± 0.19 Music 23.84 ± 0.41 54.56 ± 0.47 30.70 ± 0.40 34.57 ± 0.59 Books 22.31 ± 0.27 45.83 ± 0.31 27.54 ± 0.28 **Books** 28.48 ± 0.47 55.46 ± 0.92 CAT-ART 38.19 ± 0.12 Movies 76.05 ± 0.10 46.82 ± 0.11 Movies 40.73 ± 0.59 84.37 ± 1.01 51.54 ± 0.65 Electronics 23.65 ± 0.10 54.19 ± 0.16 30.47 ± 0.08 Music 23.88 ± 0.38 52.35 ± 1.09 30.23 ± 0.16 Books $\textbf{52.23} \pm 0.21$ 30.52 ± 0.33 24.29 ± 0.36 Books 30.27 ± 0.63 55.70 ± 0.54 36.19 ± 0.61 Ours **UCLR** Movies 36.98 ± 0.27 77.26 ± 0.40 46.16 ± 0.30 Movies 41.19 ± 0.18 85.46 ± 0.61 51.26 ± 0.31

 31.82 ± 0.05

Music

Table 8: More performance (%) comparison between our proposed method and baselines on two datasets.

B MORE DISCUSSIONS

B.1 More Related Works

Many existing CDR methods also focus on data imbalance problem, such as Recycs-DAN for single-target CDR [53]. They aim to address both cross-domain imbalance and within-domain imbalance. In contrast, the goal of our study is to address the imbalanced interactions among different users. Furthermore, recent work [38] also applies LoRA to the research of CDR. They construct domain-specific adapter cell external to the pretrained embedding layer. In contrast, our proposed algorithm employs LoRA to finetune the whole model framework, aiming to decrease the scale of parameters of pretrained global embedding.

Electronics

 24.37 ± 0.07

 57.70 ± 0.03

B.2 Masking Strategy

The fundamental idea of the mask strategy is to obscure information in specified areas, thereby ensuring that such information does not affect other regions. Most methodologies utilize a 0-1 mask

[8, 59, 63], i.e., mask_value $\in \{0, 1\}$, as this proves more effective in eliminating irrelevant information.

 56.41 ± 0.31

 33.85 ± 0.33

B.3 Domain-Variant and Invariant Representation Learning

 27.26 ± 0.37

The purpose of this study is to leverage contrastive learning to eliminate the influence among users, thereby learning fair domain-shared representations to accurately capture user preferences (domain invariant representations). As for domain-specific/variant representations [14, 37, 69], our proposed method can also be directly applied to each domain. Delving further into methods for enhancing domain-(in)variant representations is worthwhile to explore in the future. It may require specially designed modifications to our proposed framework, such as the incorporation of an attention module.

C CONVERGENCE ANALYSIS

Due to page limit, the analysis is organized in a separate *document*.