

Section 3: Functions and loops

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1 Admin

Change in office hours **this week**: 10:30am–12pm in Giannini 236. (Apologies for the inconvenience; department-level scheduling issues...)

1.1 What you will need

Packages:

- Previously used: dplyr and haven

- New: lfe

Data: The auto.dta file.

1.2 Summary of last time

In Section 2, we covered the data structures of vectors and matrices.

1.2.1 Follow up: Numeric vs. double

Someone asked about *double* versus *numeric*. It turns out that *numeric* is a more general class/mode. Numeric objects come in different modes. Specifically, numeric objects can be either double-precision or integer (single-precision is not really an option in R, unless you are calling C or Fortran at a lower level).

In practice:

```
# Does as.numeric() create integers or doubles?
is.double(as.numeric(1))
## [1] TRUE
is.integer(as.numeric(1))
## [1] FALSE
# Are integers and doubles numeric?
is.numeric(as.double(1))
## [1] TRUE
is.numeric(as.integer(1))
## [1] TRUE
```

1.2.2 Follow up: Vectorized operations

I want to point out that I probably did not give vectors a fair shake. While seemingly simple, R allows you to do a lot of things with vectors that might be much more difficult in other languages. Specifically, R allows you to apply (most) functions to vectors, rather than individual elements of a vector.

For an underwhelming example, if you want to square each number in a vector `vec` in R, you can simply write `vec^2`. The alternative that many languages use requires iterating through the vector and squaring the individual elements while simultaneously storing the results.

```
# Define the vector
vec <- 1:5
# Square the elements of the vector
vec2 <- vec^2
# Look at the result
vec2
## [1] 1 4 9 16 25
```

1.3 Summary of this section

This section covers functions, loops, and some simulation. We will take what you have been covering in lecture—the ordinary least squares (OLS) estimator—and create our very own OLS function.¹ Then we will play around with our OLS function.

2 Cleaning up

You will occasionally need to clear up some space for memory in R (or just tidy up your environment). To see the objects you are currently storing in memory, you can either (1) look in the “Environment” pane of RStudio or (2) use the `ls()` function (the function does not need any inputs).

If you decide to clean up, the function `rm()` is your friend. Here are three uses:

```
# Remove a single object from memory
rm(item1)
# Remove to (or more) objects from memory
rm(list = c("item2", "item3"))
# Remove everything from memory
rm(list = ls())
```

You also can use the garbage control (`gc()`) function if you’ve loaded and removed several large datasets. It is not the same as `rm()`; `gc()` has more to do with space allocated for objects than the space actually used.²

3 Custom functions

Up to this point, we have written some lines of R code that rely upon already-defined functions. We are now going to try writing our own function.

There are a few reasons why you want to write your own function:

1. Max forbids you from doing your homeworks with the canned functions.
2. You have a task for which there is not a function.
3. You have a task that needs to be repeated, and you do not want to keep writing the same N lines of code over and over again.

More simply: if you need to do the same task more than twice, you should probably write a function for that task, rather than copying and pasting the code dozens of times.

¹Max has probably mentioned that you have to write your own functions in this class. While relying upon the canned R functions is prohibited, you can use them to check your work.

²Sorry if this garbage control function is not clear: I’m not a computer scientist.

3.1 Custom function basics

To write a custom function in R, you use a function named `function()`.³ The specific syntax for defining a function looks like

```
foo <- function(arg1, arg2) {  
  ...  
  return(final_stuff)  
}
```

which says that we are defining a new function named `foo` that takes the arguments `arg1` and `arg2` (your function can take as many or as few arguments as you like). The function then completes some tasks (you would have actual code where you currently see `...`), and then the function returns a value of `final_stuff` using the `return()` function.⁴ Notice that after you define the function's arguments, you open a curly bracket and immediately start a new line. You end function's definition by closing the curly bracket (on a line by itself).

For a quick example of a custom function, let's define a function that accepts three arguments and returns the product of the three arguments.

```
# Define the function (named 'triple_prod')  
triple_prod <- function(x, y, z) {  
  # Take the product of the three arguments  
  tmp_prod <- x * y * z  
  # Return 'tmp_prod'  
  return(tmp_prod)  
}  
  
# Test the function  
triple_prod(x = 2, y = 3, z = 5)  
## [1] 30
```

3.2 An OLS function

As discussed above, functions are very helpful when you have a task that you want to repeat many times. In this class,⁵ you will estimate $\hat{\beta}_{ols}$ **many** times. So let's write a function that calculates the OLS estimator for β .

Recall that for an outcome (dependent) variable \mathbf{y} and a matrix of independent variables \mathbf{X} (including a column of ones for the intercept), the OLS estimator for β in the equation

$$\mathbf{y} = \mathbf{X}\beta + \epsilon$$

is

$$\hat{\beta}_{ols} = (\mathbf{X}'\mathbf{X})^{-1} \mathbf{X}'\mathbf{y}$$

³So meta, right?

⁴You can get away with not using the `return()` function, but it is generally thought of as bad form.

⁵not to mention the life of an empirical economist

Part of writing a function is determining what you want and do not want the function to do. You have a lot of options. Should it accept matrices, tibbles, data frames, *etc.*? Should the function automatically add a row for the intercept? Should it calculate the R^2 or only $\hat{\beta}_{ols}$? ...

For now, let's assume the function will accept a tibble with the variables that we want for both y and \mathbf{X} . And let's name the function `b_ols`. In addition to the tibble (let's pass the tibble to the function through the argument `data`), the function will probably need (at least) two more arguments: `y` and `X`, which will be the name of the dependent variable and the names of the independent variables, respectively. Finally—for now—let's say the function will only return the OLS estimate for β .

The function should thus look something like

```
b_ols <- function(data, y, X) {  
  # Put some code here...  
  return(beta_hat)  
}
```

3.2.1 Aside: Load your data

Our OLS function will need some data. Load the `auto.dta` data from Section 1 (also in this section's zip file). (Remember: you will need the `haven` package to load the `.dta` file.) We're not loading the data inside our function because we'll probably want to use the function on different datasets.

```
# Setup ----  
# Options  
options(stringsAsFactors = F)  
# Packages  
library(haven)  
library(dplyr)  
# Set the directory  
setwd("/Users/edwardarubin/Dropbox/Teaching/ARE212/Section03/")  
  
# Load the data ----  
cars <- read_dta(file = "auto.dta")
```

3.2.2 required packages

Spoiler: Our function is going to make use of the `dplyr` package. So let's tell our function to make sure the `dplyr` package is loaded. The function `require()` is the standard way to have a function make sure a package is loaded. You use it just like the `library()` function. Since we know that we plan to use the `dplyr` package, let's require it within our function:

```
b_ols <- function(data, y, X) {  
  # Require the 'dplyr' package  
  require(dplyr)  
  # Put some code here...  
  return(beta_hat)  
}
```

3.2.3 select_ing variables

Let's take an inventory of which objects we have, once we are inside the function. We have `data`, which is a tibble with columns that represent various variables. We have `y`, the name of our outcome variable (e.g., `weight`). And we have `X`, a vector of the names of our independent variables (e.g. `c("mpg", "weight")`).⁶

The first step for our function is to grab the data for `y` and `X` from `data`. For this task, we will use a variation of the `select()` function introduced in Section 1: `select_()`. The difference between `select()` and `select_()` (besides the underscore) is that `select()` wants the variable names without quotes (*non-standard evaluation*), e.g. `select(cars, mpg, weight)`. This notation is pretty convenient except when you are writing your own function. Generally, you will have variable/column names in a character vector, and `select(cars, "mpg", "weight")` does not work. Here is where `select_()` comes in: it *wants* you to use characters (*standard evaluation*). There is one more complexity: while `select_(cars, "mpg", "weight")` works, `select_(cars, c("mpg", "weight"))` does not. So if you have a vector of variable names, like our `X`, you need a slightly different way to use `select_()`. The solution is the `.dots` argument in `select_()`: `select_(cars, .dots = c("mpg", "weight"))` works!

So... we now want to select the `y` and `X` variables from `data`. Let's do it.

```
# Select y variable data from 'data'
y_data <- select_(data, .dots = y)
# Select X variable data from 'data'
X_data <- select_(data, .dots = X)
```

This code should do the trick. To test it, you'll need to define `y` and `X` (e.g., `y = "price"` and `X = c("mpg", "weight")`).

3.2.4 Exercise: Finish the function

The function now looks like

```
b_ols <- function(data, y, X) {
  # Require the 'dplyr' package
  require(dplyr)
  # Select y variable data from 'data'
  y_data <- select_(data, .dots = y)
  # Select X variable data from 'data'
  X_data <- select_(data, .dots = X)
  # Put some code here...
  return(beta_hat)
}
```

Fill in the `# Put some code here...` section of our new function with the code needed to produce OLS estimates via matrix operations. More kudos for fewer lines.

⁶I guess I've asserted these definitions of `y` and `X`. You're free to do whatever you like.

3.2.4.1 Hints/reminders:

- The data objects `y_data` and `X_data` are still tibbles. You eventually want matrices.
- Don't forget the intercept.
- If you finish early, adapt the function to return centered R^2 , uncentered R^2 , and adjusted R^2 .

3.2.5 Matrices

We have a few tasks left:

1. Add an intercept (column of ones) to `X_data`
2. Convert the data objects to matrices
3. Calculate $\hat{\beta}_{ols}$ via matrix operations

First, let's add a column of ones to `X_data`. We will use `mutate_()`.⁷ The `mutate()` and `mutate_()` functions allow us to add new columns/variables to an existing data object. Often the new variables will be a combination of existing variables, but in our case, we just want a column of ones, so all we need to do is write `mutate_(X_data, "ones" = 1)`.

It is customary to have the intercept column be the first column in the matrix. We can use `select_()` again to change the order of the columns: `select_(X_data, "ones", .dots = X)`.

We will use the `as.matrix()` function to convert our tibbles to matrices.

Finally, once we have our matrices, we can use the basic matrix functions discussed in Section 2—namely `%*%`, `t()`, and `solve()`—to calculate $\hat{\beta}_{ols} = (\mathbf{X}'\mathbf{X})^{-1} \mathbf{X}'\mathbf{y}$.

Putting these steps together, we can finish our function:

```
b_ols <- function(data, y, X) {  
  # Require the 'dplyr' package  
  require(dplyr)  
  
  # Select y variable data from 'data'  
  y_data <- select_(data, .dots = y)  
  # Convert y_data to matrices  
  y_data <- as.matrix(y_data)  
  
  # Select X variable data from 'data'  
  X_data <- select_(data, .dots = X)  
  # Add a column of ones to X_data  
  X_data <- mutate_(X_data, "ones" = 1)  
  # Move the intercept column to the front  
  X_data <- select_(X_data, "ones", .dots = X)  
  # Convert X_data to matrices  
  X_data <- as.matrix(X_data)
```

⁷You could use `mutate()` too.

```

# Calculate beta hat
beta_hat <- solve(t(X_data) %*% X_data) %*% t(X_data) %*% y_data
# Change the name of 'ones' to 'intercept'
rownames(beta_hat) <- c("intercept", X)
# Return beta_hat
return(beta_hat)
}

```

3.3 Piping

Our OLS function is nice, but we redefined `y_data` and `X_data` a number of times. There's nothing wrong with these intermediate steps, but `dplyr` provides a fantastic tool `%>%` for bypassing these steps to clean up your code. The operator is known as the pipe or chain command.⁸

The way the pipe (`%>%`) works is by taking the output from one expression and plugging it into the next expression (defaulting to the first argument in the second expression). For example, rather than writing the two lines of code

```

# Select the variables
tmp_data <- select(cars, price, mpg, weight)
# Summarize the selected variables
summary(tmp_data)
##      price      mpg      weight
##  Min.   : 3291  Min.   :12.00  Min.   :1760
## 1st Qu.: 4220  1st Qu.:18.00  1st Qu.:2250
## Median : 5006  Median :20.00  Median :3190
## Mean   : 6165  Mean   :21.30  Mean   :3019
## 3rd Qu.: 6332  3rd Qu.:24.75  3rd Qu.:3600
## Max.   :15906  Max.   :41.00  Max.   :4840

```

we can do it in a single line (and without creating the unnecessary object `tmp_data`)

```

cars %>% select(price, mpg, weight) %>% summary()
##      price      mpg      weight
##  Min.   : 3291  Min.   :12.00  Min.   :1760
## 1st Qu.: 4220  1st Qu.:18.00  1st Qu.:2250
## Median : 5006  Median :20.00  Median :3190
## Mean   : 6165  Mean   :21.30  Mean   :3019
## 3rd Qu.: 6332  3rd Qu.:24.75  3rd Qu.:3600
## Max.   :15906  Max.   :41.00  Max.   :4840

```

What is going on here? We're plugging `cars` into the first argument of the `select()` expression, and then plugging the output from `select()` into `summary()`. If you want to save the result from the **last** expression (`summary()` here), use the normal method, *e.g.*

```
some_summaries <- cars %>% select(price, mpg, weight) %>% summary()
```

⁸See the package `magrittr` for even more pipe operators.

If it helps you remember what a pipe is doing, you can use a period with a comma:⁹

```
# Four equivalent expressions
cars %>% select(price, mpg) %>% summary()
cars %>% select(., price, mpg) %>% summary()
select(cars, price, mpg) %>% summary()
summary(select(cars, price, mpg))
```

You can see that pipes also help you avoid situations with crazy parentheses.

Now let's apply these pipes to the OLS function above. Essentially any time you redefine an object, you could have used a pipe. Also note that pipes can extend to the next line and are uninterrupted by comments.

```
b_ols <- function(data, y, X) {
  # Require the 'dplyr' package
  require(dplyr)

  # Create the y matrix
  y_data <- data %>%
    # Select y variable data from 'data'
    select_(.dots = y) %>%
    # Convert y_data to matrices
    as.matrix()

  # Create the X matrix
  X_data <- data %>%
    # Select X variable data from 'data'
    select_(.dots = X) %>%
    # Add a column of ones to X_data
    mutate_("ones" = 1) %>%
    # Move the intercept column to the front
    select_("ones", .dots = X) %>%
    # Convert X_data to matrices
    as.matrix()

  # Calculate beta hat
  beta_hat <- solve(t(X_data) %*% X_data) %*% t(X_data) %*% y_data
  # Change the name of 'ones' to 'intercept'
  rownames(beta_hat) <- c("intercept", X)
  # Return beta_hat
  return(beta_hat)
}
```

3.4 Quality check

Let's check our function's results against one of R's canned regression functions. The base installation of R provides the function `lm()`, which works great. However, we are going to use the `fe_lm()` function from the

⁹Note: the period will actually allow you to shift the argument to which the prior expression's output is sent.

lfe package. The `felm()` function has some nice benefits over `lm()` that you will probably want at some point, namely the ability to deal with *many* fixed effects, instrumental variables, and multi-way clustered errors. (Don't worry if you do not know what that last sentence meant. You will soon.)

Install the lfe package.

```
install.packages("lfe")
```

Load it.

```
library(lfe)
```

Run the relevant regression with `felm()`:¹⁰

```
# Run the regression with 'felm'
canned_ols <- felm(formula = price ~ mpg + weight, data = cars)
# Summary of the regression
canned_ols %>% summary()
##
## Call:
##   felm(formula = price ~ mpg + weight, data = cars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3332  -1858   -504    1256    7507
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1946.0687   3597.0496   0.541  0.59019
## mpg         -49.5122    86.1560  -0.575  0.56732
## weight       1.7466     0.6414   2.723  0.00813 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2514 on 71 degrees of freedom
## Multiple R-squared(full model): 0.2934   Adjusted R-squared: 0.2735
## Multiple R-squared(proj model): 0.2934   Adjusted R-squared: 0.2735
## F-statistic(full model):14.74 on 2 and 71 DF, p-value: 4.425e-06
## F-statistic(proj model): 14.74 on 2 and 71 DF, p-value: 4.425e-06
```

Run the regression with our function `b_ols()`:

```
b_ols(data = cars, y = "price", X = c("mpg", "weight"))
##              price
## intercept 1946.06868
## mpg       -49.512221
## weight     1.746559
```

¹⁰ `felm()`, like most regression functions I've seen in R, uses a formula where the dependent variable¹¹ is separated from the independent variables with a tilde (~).

They match!

4 Loops

Loops are a very common programming tool. Just like functions, loops help us with repetitive tasks.

4.1 `for()` loops

`for` loops are classic. You give the program a list and then tell it to do something with each of the objects in the list. R's power with vectors obviates some uses of `for` loops, but there are still many cases in which you will need some type of loop. You will also hear people say that `for` loops are a bad idea in R. Don't entirely believe them. There are cases where you can do things much faster with other types of loops—particularly if you are going to parallelize and have access to a lot of computing resources—but `for` loops can still be very helpful.

In R, the `for` loop has the following structure

```
for (i in vec) {  
  # Complex computations go here  
}
```

Example of an actual (simple) `for` loop:

```
for (i in 1:5) {  
  print(paste("Hi", i))  
}
```

```
## [1] "Hi 1"  
## [1] "Hi 2"  
## [1] "Hi 3"  
## [1] "Hi 4"  
## [1] "Hi 5"
```

A final note on `for` loops in R: R keeps the last iteration's values in memory. This behavior can help with troubleshooting, but it can also sometimes lead to confusion.

While `for` loops are great, we're going to focus on a different type of loop today...

4.2 `lapply()`

The `lapply()` function is part of a family of `apply()` functions in R (`apply()`, `lapply()`, `sapply()`, `mapply()`, etc.). Each function takes slightly different inputs and/or generates slightly different outputs, but the idea is generally the same. And the idea is very similar to that of a loop: you give `lapply()` a list or vector `X` and a

function FUN, and `lapply()` will then apply the function FUN to each of the elements in X. `lapply()` returns a *list*¹² of the results generated by FUN for each of the elements of X.

Finally, it is worth noting that `lapply()` sticks the elements of X into the first argument of the function FUN (you can still define other arguments of FUN) in a way very similar to the pipe operator (`%>%`).

Here is a simplistic example of `lapply()`:

```
lapply(X = 0:4, FUN = sqrt)
```

```
## [[1]]
## [1] 0
##
## [[2]]
## [1] 1
##
## [[3]]
## [1] 1.414214
##
## [[4]]
## [1] 1.732051
##
## [[5]]
## [1] 2
```

Notice the slightly different notation of the list, relative to the vectors we previously discussed.

Unlike for loops, nothing done inside of an `lapply()` call is kept in memory after the function finishes (aside from the final results, if you assign them to an object).

4.2.1 `lapply()` meets `b_ols()`

What if we want to regress each of the numerical variables in the `cars` data on `mpg` and `weight` (with the exception of `rep78`, because I don't really understand what "Repair Record 1978" means)? Surprise, surprise: we can use `lapply()`.

What should our X value be? The numeric variables excluding `rep78`, `mpg`, and `weight`. Let's create a vector for it.

```
target_vars <- c("price", "headroom", "trunk", "length", "turn",
  "displacement", "gear_ratio", "foreign")
```

With respect to the FUN argument, keep in mind that `lapply()` plugs the X values into the first argument of the function. For `b_ols()`, the first argument is `data`, which is not what we currently want to vary. We want to vary `y`, which is the second argument. Rather than redefining the `b_ols()` function, we can augment it by wrapping another function around it. For example,

¹²This is our first time meeting a list. Lists are yet another way to store data in R—like vectors, matrices, data.frames, and tibbles. You can create lists with the `list()` function much like you create vectors with the `c()` function: `my_list <- list("a", 1, c(1,2,3))`. Lists differ in that they do not require a uniform data type, as demonstrated in the list in the preceding sentence. Lists also utilize a slightly different indexing: you access the third element of the list `my_list` via `my_list[[3]]`. Notice the extra set of square brackets.

```
function(i) b_ols(data = cars, y = i, X = c("mpg", "weight"))
```

This line of code creates a new, unnamed function with one argument `i`. The argument `i` is then fed to our `b_ols()` function as its `y` argument. Let's put it all together...

```
# The 'lapply' call
results_list <- lapply(
  X = target_vars,
  FUN = function(i) b_ols(data = cars, y = i, X = c("mpg", "weight"))
)
# The results
results_list

## [[1]]
##           price
## intercept 1946.068668
## mpg       -49.512221
## weight     1.746559
##
## [[2]]
##           headroom
## intercept  1.7943225731
## mpg        -0.0098904309
## weight     0.0004668253
##
## [[3]]
##           trunk
## intercept  5.849262628
## mpg        -0.082739270
## weight     0.003202433
##
## [[4]]
##           length
## intercept 120.11619444
## mpg        -0.35546594
## weight     0.02496695
##
## [[5]]
##           turn
## intercept 27.323996368
## mpg        -0.059092537
## weight     0.004498541
##
## [[6]]
##           displacement
## intercept -151.9910285
## mpg         0.7604918
```

```
## weight      0.1103151
##
## [[7]]
##           gear_ratio
## intercept  4.3311476331
## mpg        0.0007521123
## weight     -0.0004412382
##
## [[8]]
##           foreign
## intercept  2.1235056112
## mpg        -0.0194295266
## weight     -0.0004677698
```

These results are a bit of a mess. Let's change the list into a more legible data structure. We will use `lapply()` to apply the function `data.frame()` to each of the results (each of the elements of `results_list`). Finally, we will use the `bind_cols()` function from `dplyr` to bind all of the results together (so we don't end up with another list).¹³

```
# Cleaning up the results list
results_df <- lapply(X = results_list, FUN = data.frame) %>% bind_cols()
# We lose the row names in the process; add them back
rownames(results_df) <- c("intercept", "mpg", "weight")
# Check out results_df
results_df

##           price      headroom      trunk      length      turn
## intercept 1946.068668  1.7943225731  5.849262628 120.11619444 27.323996368
## mpg       -49.512221 -0.0098904309 -0.082739270  -0.35546594 -0.059092537
## weight     1.746559  0.0004668253  0.003202433   0.02496695  0.004498541
##           displacement  gear_ratio      foreign
## intercept -151.9910285  4.3311476331  2.1235056112
## mpg         0.7604918  0.0007521123 -0.0194295266
## weight     0.1103151 -0.0004412382 -0.0004677698
```

4.2.2 Exercise: Check your work

Check the results in `results_df` using `lapply()` and `feIm()`. *Hint:* remember to check the class of the object returned by `feIm()`. You might want to try the `coef()` function on the object returned by `feIm()`.

¹³We could alternatively try `sapply()`, which attempts to return nicely formatted objects. However, you never know if it is going to succeed in nicely formatting your results. If it doesn't, then it returns a list. This sort of inconsistency is not very helpful in programming, so I generally avoid `sapply()`.

5 Simulation

One of the main reasons to learn the `apply()` family of functions is that they are very flexible (and easily parallelized).¹⁴ This flexibility lends them to use in simulation, which basically means we want to generate random numbers and to test/observe properties of estimators. And repeat many times.

5.1 Examining bias in one sample

We often examine the (finite-sample) properties of estimators through simulation.

Let's start with a function that generates some data, estimates coefficients via OLS, and calculates the bias.

```
# A function to calculate bias
data_baker <- function(sample_n, true_beta) {
  # First generate x from N(0,1)
  x <- rnorm(sample_n)
  # Now the error from N(0,1)
  e <- rnorm(sample_n)
  # Now combine true_beta, x, and e to get y
  y <- true_beta[1] + true_beta[2] * x + e
  # Define the data matrix of independent vars.
  X <- cbind(1, x)
  # Force y to be a matrix
  y <- matrix(y, ncol = 1)
  # Calculate the OLS estimates
  b_ols <- solve(t(X) %*% X) %*% t(X) %*% y
  # Convert b_ols to vector
  b_ols <- b_ols %>% as.vector()
  # Calculate bias, force to 2x1 data.frame()
  the_bias <- (true_beta - b_ols) %>%
    matrix(ncol = 2) %>% data.frame()
  # Set names
  names(the_bias) <- c("bias_intercept", "bias_x")
  # Return the bias
  return(the_bias)
}
```

This function will calculate the bias of the OLS estimator for a single sample,

```
# Set seed
set.seed(12345)
# Run once
data_baker(sample_n = 100, true_beta = c(1, 3))
```

¹⁴Parallelization basically means that you run things at the same time—instead of waiting until one thing finishes to start the next. Thus some tasks can be parallelized—simulations for unbiased estimators—while other tasks that depend upon the output from previous iterations are more difficult to parallelize. We'll talk more about parallelization next time.

```
##      bias_intercept      bias_x
## 1      -0.02205339 -0.09453503
```

5.2 Examining bias in many samples

But what if you want to run 10,000 simulations? Should you just copy and paste 10,000 times? Probably not.¹⁵ Use `lapply()` (or `replicate()`). And let's write one more function wrapped around `data_baker()`.

```
# A function to run the simulation
bias_simulator <- function(n_sims, sample_n, true_beta) {

  # A function to calculate bias
  data_baker <- function(sample_n, true_beta) {
    # First generate x from N(0,1)
    x <- rnorm(sample_n)
    # Now the error from N(0,1)
    e <- rnorm(sample_n)
    # Now combine true_beta, x, and e to get y
    y <- true_beta[1] + true_beta[2] * x + e
    # Define the data matrix of independent vars.
    X <- cbind(1, x)
    # Force y to be a matrix
    y <- matrix(y, ncol = 1)
    # Calculate the OLS estimates
    b_ols <- solve(t(X) %*% X) %*% t(X) %*% y
    # Convert b_ols to vector
    b_ols <- b_ols %>% as.vector()
    # Calculate bias, force to 2x1 data.frame()
    the_bias <- (true_beta - b_ols) %>%
      matrix(ncol = 2) %>% data.frame()
    # Set names
    names(the_bias) <- c("bias_intercept", "bias_x")
    # Return the bias
    return(the_bias)
  }

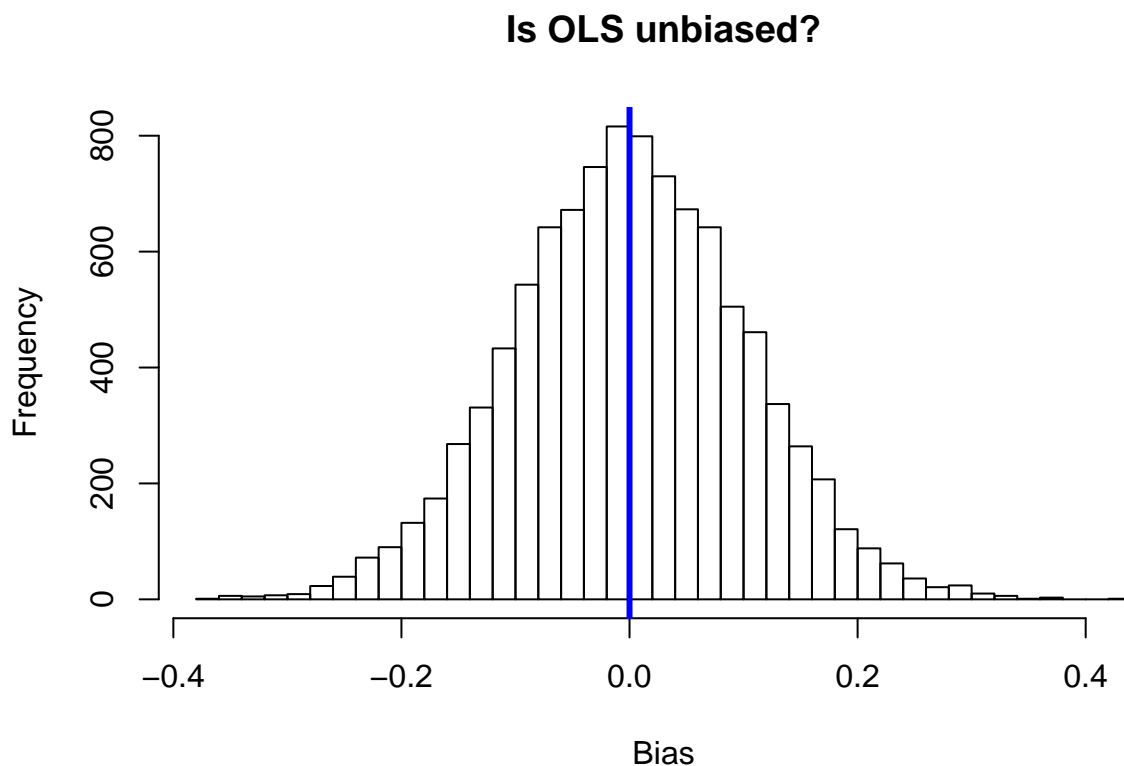
  # Run data_baker() n_sims times with given parameters
  sims_dt <- lapply(
    X = 1:n_sims,
    FUN = function(i) data_baker(sample_n, true_beta)) %>%
    # Bind the rows together to output a nice data.frame
    bind_rows()

  # Return sim_dt
  return(sims_dt)
}
```

¹⁵Definitely not.

To run the simulation 10,000 times, use the code (can take a little while):

```
# Set seed
set.seed(12345)
# Run it
sim_dt <- bias_simulator(n_sims = 1e4, sample_n = 100, true_beta = c(1,3))
# Check the results with a histogram
hist(sim_dt[,2],
     breaks = 30,
     main = "Is OLS unbiased?",
     xlab = "Bias")
# Emphasize the zero line
abline(v = 0, col = "blue", lwd = 3)
```



Next section we'll talk a bit about parallelization, which can greatly reduce the time of your simulations.

6 Extensions/challenges

1. How few characters can you use to write a function that estimates coefficients via OLS? Can you keep this function parsimonious while expanding its flexibility (allowing it to take different data structures with and without intercepts)?
2. Can you find any speed/efficiency improvements over my `data_baker()` and `bias_simulator()` functions? Feel free to include parallelization.
3. How would you generate vectors of two random variables that are correlated (i.e. x and ε are not independent)? Does this correlation affect anything in your bias simulations?