# Package 'pomp'

May 28, 2015

Type Package

**Title** Statistical Inference for Partially Observed Markov Processes

**Version** 0.65-1 **Date** 2015-05-28

URL http://pomp.r-forge.r-project.org

**Description** Inference methods for partially observed Markov processes (AKA stochastic dynamical systems, state-space models).

**Depends** R(>= 3.0.0), methods

Imports stats, graphics, mytnorm, deSolve, coda, subplex, nloptr

License GPL(>= 2)

LazyData true

#### **MailingList**

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# Description

The **pomp** package provides facilities for inference on time series data using partially-observed Markov process (POMP) models. These models are also known as state-space models or nonlinear stochastic dynamical systems. One can use **pomp** to fit nonlinear, non-Gaussian dynamic models to time-series data. The package is both a set of tools for data analysis and a platform upon which statistical inference methods for POMP models can be implemented.

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# Data analysis using pomp

The first step in using **pomp** is to encode one's model(s) and data in objects of class pomp. One does this via a call to pomp, which involves specifying the unobserved state process and the measurement process of the model. Details on this are given in the documentation for the pomp constructor function. Examples are given in the tutorials on the package website, in the demos (demo(package=pomp)), and via the pompExample function.

**pomp** version 0.65-1 provides algorithms for

- 1. simulation of stochastic dynamical systems; see simulate
- 2. particle filtering (AKA sequential Monte Carlo or sequential importance sampling); see pfilter
- 3. the iterated filtering method of Ionides et al. (2006, 2011, 2015); see mif
- 4. the nonlinear forecasting algorithm of Kendall et al. (2005); see nlf
- 5. the particle MCMC approach of Andrieu et al. (2010); see pmcmc
- 6. the probe-matching method of Kendall et al. (1999, 2005); see probe.match
- 7. a spectral probe-matching method (Reuman et al. 2006, 2008); see spect.match
- 8. synthetic likelihood a la Wood (2010); see probe
- 9. approximate Bayesian computation (Toni et al. 2009); see abc
- 10. the approximate Bayesian sequential Monte Carlo scheme of Liu & West (2001); see bsmc
- 11. simple trajectory matching; see traj.match.

The package also provides various tools for plotting and extracting information on models and data.

#### Developing inference tools on the pomp platform

**pomp** provides a very general interface to the components of POMP models. All the inference algorithms in **pomp** interact with the models and data via this interface. One goal of the **pomp** project has been to facilitate the development of new algorithms in an environment where they can be tested and compared on a growing body of models and datasets.

The low-level interface relevant to developers is documented here.

# **Comments, bug reports, feature requests**

Contributions are welcome, as are comments, feature requests, and bug reports. See the package website <a href="http://pomp.r-forge.r-project.org">http://pomp.r-forge.r-project.org</a> for more information, access to the package mailing list, links to the authors' websites, references to the literature, and up-to-date versions of the package source and documentation.

#### Documentation

A number of tutorials, demonstrating the construction of pomp objects and the application of various inference algorithms, are available on the package homepage: <a href="http://pomp.r-forge.r-project.">http://pomp.r-forge.r-project.</a> org. Several examples of the construction of pomp objects are provided with the package and are documented in the help pages: to view a full list of these, execute pompExample(). In addition, there are a number of demos, which can be viewed by executing demo(package="pomp").

#### **History**

Much of the groundwork for **pomp** was laid by a working group of the National Center for Ecological Analysis and Synthesis (NCEAS), "Inference for Mechanistic Models".

#### License

**pomp** is provided under the GNU Public License (GPL).

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### References

See the package website, http://pomp.r-forge.r-project.org, for the references.

#### See Also

```
pomp, pomp low-level interface, pfilter, simulate, mif, nlf, probe, traj.match, bsmc2, pmcmc
```

Approximate Bayesian computation

Estimation by approximate Bayesian computation (ABC)

## **Description**

The approximate Bayesian computation (ABC) algorithm for estimating the parameters of a partially-observed Markov process.

## Usage

```
## S4 method for signature pomp
abc(object, Nabc = 1, start, proposal,
   pars, rw.sd, probes, scale, epsilon,
   verbose = getOption("verbose"), ...)
## S4 method for signature probed.pomp
abc(object, probes,
    verbose = getOption("verbose"), ...)
## S4 method for signature abc
abc(object, Nabc, start, proposal,
   probes, scale, epsilon,
   verbose = getOption("verbose"), ...)
## S4 method for signature abc
continue(object, Nabc = 1, ...)
## S4 method for signature abc
conv.rec(object, pars, ...)
## S4 method for signature abcList
```

```
conv.rec(object, ...)
## S4 method for signature abc
plot(x, y, pars, scatter = FALSE, ...)
## S4 method for signature abcList
plot(x, y, ...)
```

## **Arguments**

object An object of class pomp.

Nabc The number of ABC iterations to perform.

start named numeric vector; the starting guess of the parameters.

proposal optional function that draws from the proposal distribution. Currently, the pro-

posal distribution must be symmetric for proper inference: it is the user's responsibility to ensure that it is. Several functions that construct appropriate proposal function are provided: see MCMC proposal functions for more information.

rw. sd Deprecated. Will be removed in a future release. Specifying rw. sd is equivalent

to setting proposal=mvn.diag.rw(rw.sd).

probes List of probes (AKA summary statistics). See probe for details.

scale named numeric vector of scales.

epsilon ABC tolerance.

verbose logical; if TRUE, print progress reports.

pars Names of parameters.

scatter optional logical; If TRUE, draw scatterplots. If FALSE, draw traceplots.

x abc object.y Ignored.

.. Additional arguments. These are currently ignored.

#### **Running ABC**

abc returns an object of class abc. One or more abc objects can be joined to form an abcList object.

# **Re-running ABC iterations**

To re-run a sequence of ABC iterations, one can use the abc method on a abc object. By default, the same parameters used for the original ABC run are re-used (except for tol, max.fail, and verbose, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

## **Continuing ABC iterations**

One can continue a series of ABC iterations from where one left off using the continue method. A call to abc to perform Nabc=m iterations followed by a call to continue to perform Nabc=n iterations will produce precisely the same effect as a single call to abc to perform Nabc=m+n iterations. By default, all the algorithmic parameters are the same as used in the original call to abc. Additional arguments will override the defaults.

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## Methods

Methods that can be used to manipulate, display, or extract information from an abc object:

**conv.rec** conv.rec(object, pars) returns the columns of the convergence-record matrix corresponding to the names in pars. By default, all rows are returned.

c Concatenates abc objects into an abcList.

plot Diagnostic plots.

# Author(s)

Edward L. Ionides <ionides at umich dot edu>, Aaron A. King <kingaa at umich dot edu>

#### References

T. Toni and M. P. H. Stumpf, Simulation-based model selection for dynamical systems in systems and population biology, Bioinformatics 26:104–110, 2010.

T. Toni, D. Welch, N. Strelkowa, A. Ipsen, and M. P. H. Stumpf, Approximate Bayesian computation scheme for parameter inference and model selection in dynamical systems Journal of the Royal Society, Interface 6:187–202, 2009.

## See Also

pomp, probe, and the tutorials on the package website.

# **Description**

These functions generate B-spline basis functions. bspline.basis gives a basis of spline functions. periodic.bspline.basis gives a basis of periodic spline functions.

#### Usage

```
bspline.basis(x, nbasis, degree = 3, names = NULL)
periodic.bspline.basis(x, nbasis, degree = 3, period = 1, names = NULL)
```

# Arguments

X	Vector at which the spline functions are to be evaluated.
nbasis	The number of basis functions to return.
degree	Degree of requested B-splines.
period	The period of the requested periodic B-splines.

names

optional; the names to be given to the basis functions. These will be the columnnames of the matrix returned. If the names are specified as a format string (e.g., "basis%d"), sprintf will be used to generate the names from the column number. If a single non-format string is specified, the names will be generated by paste-ing name to the column number. One can also specify each column name explicitly by giving a length-nbasis string vector. By default, no columnnames are given.

## Value

bspline.basis Returns a matrix with length(x) rows and nbasis columns. Each column contains the values one of the spline basis functions.

periodic.bspline.basis

Returns a matrix with length(x) rows and nbasis columns. The basis functions returned are periodic with period period.

#### C API

Access to the underlying C routines is available: see the header file 'pomp.h' for definition and documentation of the C API. At an R prompt, execute

```
file.show(system.file("include/pomp.h",package="pomp"))
to view this file.
```

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

## **Examples**

```
x <- seq(0,2,by=0.01)
y <- bspline.basis(x,degree=3,nbasis=9,names="basis")
matplot(x,y,type=1,ylim=c(0,1.1))
lines(x,apply(y,1,sum),lwd=2)

x <- seq(-1,2,by=0.01)
y <- periodic.bspline.basis(x,nbasis=5,names="spline%d")
matplot(x,y,type=1)</pre>
```

Bayesian sequential Monte Carlo

The Liu and West Bayesian particle filter

# Description

Modified versions of the Liu and West (2001) algorithm.

#### Usage

```
## S4 method for signature pomp
bsmc2(object, params, Np, est, smooth = 0.1,
    tol = 1e-17, seed = NULL,
    verbose = getOption("verbose"), max.fail = 0,
    transform = FALSE, ...)
## S4 method for signature pomp
bsmc(object, params, Np, est, smooth = 0.1,
    ntries = 1, tol = 1e-17, lower = -Inf, upper = Inf, seed = NULL,
    verbose = getOption("verbose"), max.fail = 0,
    transform = FALSE, ...)
```

## **Arguments**

lower, upper

object An object of class pomp or inheriting class pomp.

params, Np Specifications for the prior distribution of particles. See details below.

est Names of the rows of params that are to be estimated. No updates will be made

to the other parameters. If est is not specified, all parameters for which there is

variation in params will be estimated.

smooth Kernel density smoothing parameters. The compensating shrinkage factor will

be sqrt(1-smooth^2). Thus, smooth=0 means that no noise will be added to parameters. Generally, the value of smooth should be chosen close to 0 (i.e.,

shrink~0.1).

ntries Number of draws from rprocess per particle used to estimate the expected

value of the state process at time t+1 given the state and parameters at time t.

tol Particles with log likelihood below tol are considered to be "lost". A filtering

failure occurs when, at some time point, all particles are lost. When all particles are lost, the conditional log likelihood at that time point is set to be log(tol).

optional; lower and upper bounds on the priors. This is useful in case there are box constraints satisfied by the priors. The posterior is guaranteed to lie within

these bounds.

seed optional; an object specifying if and how the random number generator should

be initialized ('seeded'). If seed is an integer, it is passed to set.seed prior to any simulation and is returned as the "seed" element of the return list. By default, the state of the random number generator is not changed and the value

of .Random. seed on the call is stored in the "seed" element of the return list.

verbose logical; if TRUE, print diagnostic messages.

max.fail The maximum number of filtering failures allowed. If the number of filtering

failures exceeds this number, execution will terminate with an error.

transform logical; if TRUE, the algorithm operates on the transformed scale.

... currently ignored.

#### **Details**

There are two ways to specify the prior distribution of particles. If params is unspecified or is a named vector, Np draws are made from the prior distribution, as specified by rprior. Alternatively, params can be specified as an npars x Np matrix (with rownames).

bsmc uses version of the original algorithm that includes a plug-and-play auxiliary particle filter. bsmc2 discards this auxiliary particle filter and appears to give superior performance for the same amount of effort.

## Value

An object of class "bsmcd.pomp". The "params" slot of this object will hold the parameter posterior medians. The slots of this class include:

post A matrix containing draws from the approximate posterior distribution.

prior A matrix containing draws from the prior distribution (identical to params on

call).

eff.sample.size

A vector containing the effective number of particles at each time point.

smooth The smoothing parameter used (see above).

seed The state of the random number generator at the time bsmc was called. If the

argument seed was specified, this is a copy; if not, this is the internal state of

the random number generator at the time of call.

nfail The number of filtering failures encountered.

cond.log.evidence

A vector containing the conditional log evidence scores at each time point.

log.evidence The estimated log evidence.

weights The resampling weights for each particle.

#### Author(s)

Michael Lavine (lavine at math dot umass dot edu), Matthew Ferrari (mferrari at psu dot edu), Aaron A. King (kingaa at umich dot edu), Edward L. Ionides (ionides at umich dot edu)

# References

Liu, J. and M. West. Combining Parameter and State Estimation in Simulation-Based Filtering. In A. Doucet, N. de Freitas, and N. J. Gordon, editors, Sequential Monte Carlo Methods in Practice, pages 197-224. Springer, New York, 2001.

## See Also

pomp, pfilter

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blowflies

Model for Nicholson's blowflies.

## Description

blowflies1 and blowflies2 are pomp objects encoding stochastic delay-difference models.

#### **Details**

The data are from "population I", a control culture in one of A. J. Nicholson's experiments with the Australian sheep-blowfly *Lucilia cuprina*. The experiment is described on pp. 163–4 of Nicholson (1957). Unlimited quantities of larval food were provided; the adult food supply (ground liver) was constant at 0.4g per day. The data were taken from the table provided by Brillinger et al. (1980).

The models are discrete delay equations:

$$R(t+1) \sim \text{Poisson}(PN(t-\tau) \exp{(-N(t-\tau)/N_0)}e(t+1)\Delta t)$$
  
$$S(t+1) \sim \text{binomial}(N(t), \exp{(-\delta\epsilon(t+1)\Delta t)})$$
  
$$N(t) = R(t) + S(t)$$

where e(t) and  $\epsilon(t)$  are Gamma-distributed i.i.d. random variables with mean 1 and variances  $\sigma_p^2/\Delta t$ ,  $\sigma_d^2/\Delta t$ , respectively. blowflies1 has a timestep ( $\Delta t$ ) of 1 day, and blowflies2 has a timestep of 2 days. The process model in blowflies1 thus corresponds exactly to that studied by Wood (2010). The measurement model in both cases is taken to be

$$y(t) \sim \operatorname{negbin}(N(t), 1/\sigma_y^2)$$

, i.e., the observations are assumed to be negative-binomially distributed with mean N(t) and variance  $N(t) + (\sigma_u N(t))^2$ .

Do

file.show(system.file("examples","blowflies.R",package="pomp")) to view the code that constructs these pomp objects.

## References

- A. J. Nicholson (1957) The self-adjustment of populations to change. Cold Spring Harbor Symposia on Quantitative Biology, **22**, 153–173.
- Y. Xia and H. Tong (2011) Feature Matching in Time Series Modeling. *Statistical Science* 26, 21–46.
- E. L. Ionides (2011) Discussion of "Feature Matching in Time Series Modeling" by Y. Xia and H. Tong. *Statistical Science* **26**, 49–52.
- S. N. Wood (2010) Statistical inference for noisy nonlinear ecological dynamic systems. *Nature* **466**, 1102–1104.
- W. S. C. Gurney, S. P. Blythe, and R. M. Nisbet (1980) Nicholson's blowflies revisited. *Nature* **287**, 17–21.
- D. R. Brillinger, J. Guckenheimer, P. Guttorp and G. Oster (1980) Empirical modelling of population time series: The case of age and density dependent rates. in G. Oster (ed.), Some Questions in Mathematical Biology, vol. 13, pp. 65–90. American Mathematical Society, Providence.

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## See Also

pomp

#### **Examples**

```
pompExample(blowflies)
plot(blowflies1)
plot(blowflies2)
```

Csnippet

C code snippets for accelerating computations

# Description

For including snippets of C code in pomp objects.

## Usage

Csnippet(text)

# **Arguments**

text

character; a snippet of C code.

#### Value

An object of class Csnippet.

# Using C snippets to accelerate computations

From version 0.50, **pomp** provides a facility whereby users can define their model's components using inline C code. Furnishing one or more Csnippets as arguments to the pomp constructor causes them to be written to a C file stored in the R session's temporary directory, which is then compiled (via R CMD SHLIB) into a dynamically loadable shared object file. This is then loaded as needed.

**Note to Windows and Mac users:** By default, your R installation may not support R CMD SHLIB. Have a look at the tutorials on the package website for instructions on enabling this powerful feature of R.

In writing a Csnippet one must bear in mind both the *goal* of the snippet, i.e., what computation it is intended to perform, and the *context* in which it will be executed. Details of both of these are given below in the form of rules governing the use of Csnippets. Illustrative examples are given in the tutorials on the package website.

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## General rules for writing C snippets

1. C snippets must be valid C. They will embedded verbatim in a template file which will then be compiled by a call to R CMD SHLIB. If the resulting file does not compile, an error message wil be generated. No attempt is made by **pomp** to interpret this message. Typically, compilation errors are due to either invalid C syntax or undeclared variables.

- 2. State variables, parameters, observables, and covariates must be left undeclared in the snippet. State variables and parameters must be declared in either the statenames or paramnames argument to pomp, as appropriate. Compiler errors that complain about undeclared state variables or parameters are usually due to failure to include these parameters in the appropriate vector of names.
- 3. A C snippet can declare local variables. Be careful not to use names that match those of state variables, observables, or parameters. The latter must never be declared within a snippet.
- 4. Names of observables are determined by their names in the data. They must be referred to in measurement model snippets (rmeasure or dmeasure) by those names.
- 5. If the pomp object contains a table of covariates (see pomp), then the variables in the covariate table will be available, by their names, in the context within which the snippet is executed.
- 6. R variables with names containing dots ('.') are replaced in the C codes by variable names in which all dots have been replaced by underscores ('\_').
- 7. The header 'R.h', provided with R, will be included in the generated C file, making all of the R C API available for use in the snippet.
- 8. The header 'pomp.h', provided with **pomp**, will also be included, making all of the **pomp** C API available for use in every snippet. Do

```
file.show(system.file("include/pomp.h",package="pomp"))
to view this header file.
```

9. Snippets of C code passed to the globals argument of pomp will be included at the head of the generated C file. This can be used to declare global variables, define useful functions, and include arbitrary header files.

## Rules for writing rmeasure snippets

- 1. The goal of such a snippet is to fill the observables with random values drawn from the measurement model distribution. Accordingly, each observable should be assigned a new value.
- 2. In addition to the states, parameters, covariates (if any), and observables, the variable t, containing the time of the observation, will be defined in the context in which the snippet is executed.

# Rules for writing dmeasure snippets

- 1. The goal of such a snippet is to fill the lik variable with the likelihood of the data given the state. Alternatively, if give\_log=1, lik should be filled with the log likelihood.
- 2. In addition to the states, parameters, covariates (if any), and observables, the variable t, containing the time of the observation, will be defined in the context in which the snippet is executed.

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#### Rules for writing euler.sim and discrete.time.sim snippets

1. The goal of such a snippet is to replace the state variables with their new random values at the end of the time interval. Accordingly, each state variable should be over-written with its new value.

2. In addition to the states, parameters, covariates (if any), and observables, the variables t and dt, containing respectively the time at the beginning of the Euler step and the Euler step's duration, will be defined in the context in which the snippet is executed.

## Rules for writing skeleton snippets

- 1. For each state variable, there is a corresponding component of the deterministic skeleton. The goal of such a snippet is to compute all the components.
- 2. When the skeleton is a map, the component corresponding to state variable x is named Dx and is the new value of x after one iteration of the map.
- 3. When the skeleton is a vectorfield, the component corresponding to state variable x is named Dx and is the value of \$dx/dt\$.
- 4. As with the other C snippets, all states, parameters and covariates, as well as the current time, t, will be defined in the context within which the snippet is executed.

## Rules for writing rprior snippets

- 1. The goal of such a snippet is the replacement of parameters with values drawn from the prior distribution.
- 2. Within the context in which the snippet will be evaluated, only the parameters will be defined.
- 3. Hyperparameters can be included in the ordinary parameter list. Obviously, hyperparameters should not be replaced with random draws.

# Rules for writing dprior snippets

- 1. The goal of such a snippet is computation of the prior probability density, or the log of same, at a given point in parameter space. This scalar value should be returned in the variable lik. When give\_log=1, the user should return the log of the prior probability density.
- 2. Within the context in which the snippet will be evaluated, only the parameters and give\_log will be defined.
- 3. Hyperparameters can be included in the ordinary parameter list. Obviously, hyperparameters should not be replaced with random draws.

## Rules for writing parameter transformation snippets

- 1. The parameter transformation mapping a parameter vector from the scale defined by the model codes to another scale is specified as the parameter.inv.transform whilst the transformation mapping a parameter vector from the alternative scale to that on which the model is defined is specified as the parameter.transform.
- 2. The goal of a these snippets is the computation of the values of the transformed parameters. The value of transformed parameter x should be assigned to variable Tx.

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3. Time-, state-, and covariate-dependent transformations are not allowed. Therefore, neither the time, nor any state variables, nor any of the covariates will be available in the context within which a parameter transformation snippet is executed.

## Viewing the generated C code

It can be useful to view the C code generated by calling pomp with one or more Csnippet arguments. To do so, set options(verbose=TRUE) before calling pomp. A message giving the name of the generated C file (in the session temporary directory) will be printed.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp, plugins, and the tutorials on the package website.

dacca

Model of cholera transmission for historic Bengal.

## Description

dacca is a pomp object containing census and cholera mortality data from the Dacca district of the former British province of Bengal over the years 1891 to 1940 together with a stochastic differential equation transmission model. The model is that of King et al. (2008). The parameters are the MLE for the SIRS model with seasonal reservoir.

Data are provided courtesy of Dr. Menno J. Bouma, London School of Tropical Medicine and Hygiene.

#### **Details**

dacca is a pomp object containing the model, data, and MLE parameters. Parameters that naturally range over the positive reals are log-transformed; parameters that range over the unit interval are logit-transformed; parameters that are naturally unbounded or take integer values are not transformed.

## References

A. A. King, E. L. Ionides, M. Pascual, and M. J. Bouma, Inapparent infections and cholera dynamics, Nature, 454:877-880, 2008

## See Also

euler.sir, pomp

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# **Examples**

```
pompExample(dacca)
plot(dacca)
#MLEs on the natural scale
coef(dacca)
#MLEs on the transformed scale
coef(dacca,transform=TRUE)
plot(simulate(dacca))
# now change eps and simulate again
coef(dacca,"eps") <- 1
plot(simulate(dacca))</pre>
```

design

Design matrices for pomp calculations

# Description

These functions are useful for generating designs for the exploration of parameter space. sobolDesign generate a Latin hypercube design using the Sobol' low-discrepancy sequence. profileDesign generates a data-frame where each row can be used as the starting point for a profile likelihood calculation. sliceDesign generates points along slices through a specified point.

## Usage

## Arguments

lower, upper named numeric vectors giving the lower and upper bounds of the ranges, respec-

tively.

.. In profileDesign, additional arguments specify the parameters over which to

profile and the values of these parameters.

In sliceDesign, additional numeric vector arguments specify the locations of

points along the slices.

nseq Total number of points requested.

nprof The number of points per profile point.

stringsAsFactors

should character vectors be converted to factors?

center center is a named numeric vector specifying the point through which the slice(s)

is (are) to be taken.

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## Value

```
sobolDesign
```

profileDesign returns a data frame with nprof points per profile point. The other parameters in vars are sampled using sobol.

## Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

#### References

W. H. Press, S. A. Teukolsky, W. T. Vetterling, and B. P. Flannery, Numerical Recipes in C, Cambridge University Press, 1992

## **Examples**

```
## Sobol low-discrepancy design
plot(sobolDesign(lower=c(a=0,b=100),upper=c(b=200,a=1),100))
## A one-parameter profile design:
x \leftarrow profileDesign(p=1:10,lower=c(a=0,b=0),upper=c(a=1,b=5),nprof=20)
dim(x)
plot(x)
## A two-parameter profile design:
x \leftarrow profileDesign(p=1:10,q=3:5,lower=c(a=0,b=0),upper=c(b=5,a=1),nprof=20)
dim(x)
plot(x)
## A single 11-point slice through the point c(A=3,B=8,C=0) along the B direction.
x \leftarrow sliceDesign(center=c(A=3,B=8,C=0),B=seq(0,10,by=1))
dim(x)
plot(x)
## Two slices through the same point along the A and C directions.
x \leftarrow sliceDesign(c(A=3,B=8,C=0),A=seq(0,5,by=1),C=seq(0,5,length=11))
dim(x)
plot(x)
```

eulermultinom

The Euler-multinomial distributions and Gamma white-noise processes

# **Description**

This page documents both the Euler-multinomial family of distributions and the package's simulator of Gamma white-noise processes.

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#### Usage

```
reulermultinom(n = 1, size, rate, dt)
deulermultinom(x, size, rate, dt, log = FALSE)
rgammawn(n = 1, sigma, dt)
```

#### **Arguments**

n	integer; number of random variates to generate.
size	scalar integer; number of individuals at risk.
rate	numeric vector of hazard rates.
sigma	numeric scalar; intensity of the Gamma white noise process.
dt	numeric scalar; duration of Euler step.
X	matrix or vector containing number of individuals that have succumbed to each death process.
log	logical; if TRUE, return logarithm(s) of probabilities.

## **Details**

If N individuals face constant hazards of death in k ways at rates  $r_1, r_2, \ldots, r_k$ , then in an interval of duration  $\Delta t$ , the number of individuals remaining alive and dying in each way is multinomially distributed:

$$(N - \sum_{i=1}^{k} \Delta n_i, \Delta n_1, \dots, \Delta n_k) \sim \text{multinomial}(N; p_0, p_1, \dots, p_k),$$

where  $\Delta n_i$  is the number of individuals dying in way i over the interval, the probability of remaining alive is  $p_0 = \exp(-\sum_i r_i \Delta t)$ , and the probability of dying in way j is

$$p_j = \frac{r_j}{\sum_i r_i} (1 - \exp(-\sum_i r_i \Delta t)).$$

In this case, we say that

$$(\Delta n_1, \dots, \Delta n_k) \sim \text{eulermultinom}(N, r, \Delta t),$$

where  $r = (r_1, \dots, r_k)$ . Draw m random samples from this distribution by doing

dn <- reulermultinom(n=m, size=N, rate=r, dt=dt),</pre>

where r is the vector of rates. Evaluate the probability that  $x = (x_1, \dots, x_k)$  are the numbers of individuals who have died in each of the k ways over the interval  $\Delta t = dt$ , by doing

deulermultinom(x=x,size=N,rate=r,dt=dt).

Breto & Ionides (2011) discuss how an infinitesimally overdispersed death process can be constructed by compounding a binomial process with a Gamma white noise process. The Euler approximation of the resulting process can be obtained as follows. Let the increments of the equidispersed process be given by

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```
reulermultinom(size=N,rate=r,dt=dt).
```

In this expression, replace the rate r with  $r\Delta W/\Delta t$ , where  $\Delta W \sim \operatorname{Gamma}(\Delta t/\sigma^2, \sigma^2)$  is the increment of an integrated Gamma white noise process with intensity  $\sigma$ . That is,  $\Delta W$  has mean  $\Delta t$  and variance  $\sigma^2 \Delta t$ . The resulting process is overdispersed and converges (as  $\Delta t$  goes to zero) to a well-defined process. The following lines of R code accomplish this:

```
dW <- rgammawn(sigma=sigma,dt=dt)
dn <- reulermultinom(size=N,rate=r,dt=dW)
or
dn <- reulermultinom(size=N,rate=r*dW/dt,dt=dt).</pre>
```

He et al. use such overdispersed death processes in modeling measles.

For all of the functions described here, access to the underlying C routines is available: see below.

#### Value

reulermultinom Returns a length(rate) by n matrix. Each column is a different random draw.

Each row contains the numbers of individuals succumbed to the corresponding

process.

deulermultinom Returns a vector (of length equal to the number of columns of x) containing

the probabilities of observing each column of x given the specified parameters

(size, rate, dt).

rgammawn Returns a vector of length n containing random increments of the integrated

Gamma white noise process with intensity sigma.

## C API

An interface for C codes using these functions is provided by the package. At an R prompt, execute

```
file.show(system.file("include/pomp.h",package="pomp"))
```

to view the header file that defines and explains the API.

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

## References

C. Breto & E. L. Ionides, Compound Markov counting processes and their applications to modeling infinitesimally over-dispersed systems. Stoch. Proc. Appl., 121:2571–2591, 2011.

D. He, E. L. Ionides, & A. A. King, Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. J. R. Soc. Interface, 7:271–283, 2010.

Example pomp models

## **Examples**

```
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=0.1))
deulermultinom(x=dn,size=100,rate=c(1,2,3),dt=0.1)
## an Euler-multinomial with overdispersed transitions:
dt <- 0.1
dW <- rgammawn(sigma=0.1,dt=dt)
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=dW))</pre>
```

Example pomp models

Examples of the construction of POMP models

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# Description

pompExample loads pre-built example pomp objects.

## Usage

```
pompExample(example, ..., envir = .GlobalEnv)
```

# **Arguments**

example	example to load given as a name or literal character string. Evoked without an argument, pompExample lists all available examples.
• • •	additional arguments define symbols in the environment within which the example code is executed.
envir	the environment into which the objects should be loaded. If envir=NULL, then the created objects are returned in a list.

# **Details**

Directories listed in the global option pomp.examples (which can be changed using options()) are searched for file named '<example>.R'. If found, this file will be sourced in a temporary environment. Additional arguments to pompExample define variables within this environment and will therefore be available when the code in '<example>.R' is sourced.

The codes that construct these pomp objects can be found in the 'examples' directory in the installed package. Do system.file("examples", package="pomp")) to find this directory.

## Value

By default, pompExample has the side effect of creating one or more objects in the global workspace. If envir=NULL, there are no side effects; rather, the objects are returned as a list.

## Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

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## See Also

```
blowflies, dacca, gompertz, ou2, ricker, rw2, euler.sir, gillespie.sir, bbs
```

# **Examples**

```
pompExample()
pompExample(euler.sir)
pompExample("gompertz")
pompExample(ricker,envir=NULL)
## Not run:
file.show(system.file("examples/bbs.R",package="pomp"))
## End(Not run)
```

gompertz

Gompertz model with log-normal observations.

## **Description**

gompertz is a pomp object encoding a stochastic Gompertz population model with log-normal measurement error.

# **Details**

The state process is  $X_{t+1} = K^{1-S} X_t^S \epsilon_t$ , where  $S = e^{-r}$  and the  $\epsilon_t$  are i.i.d. lognormal random deviates with variance  $\sigma^2$ . The observed variables  $Y_t$  are distributed as  $\log (\log X_t, \tau)$ . Parameters include the per-capita growth rate r, the carrying capacity K, the process noise s.d.  $\sigma$ , the measurement error s.d.  $\tau$ , and the initial condition  $X_0$ . The pomp object includes parameter transformations that  $\log \tau$  transform the parameters for estimation purposes.

# See Also

```
pomp, ricker, and the tutorials at http://pomp.r-forge.r-project.org.
```

## **Examples**

```
pompExample(gompertz)
plot(gompertz)
coef(gompertz)
coef(gompertz,transform=TRUE)
```

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Iterated filtering

Maximum likelihood by iterated filtering

# Description

Iterated filtering algorithms for estimating the parameters of a partially-observed Markov process.

# Usage

```
## S4 method for signature pomp
mif(object, Nmif = 1, start, ivps = character(0),
    particles, rw.sd, Np, ic.lag, var.factor = 1,
    cooling.type, cooling.fraction.50,
   method = c("mif", "unweighted", "fp", "mif2"),
    tol = 1e-17, max.fail = Inf,
    verbose = getOption("verbose"), transform = FALSE, ...)
## S4 method for signature pfilterd.pomp
mif(object, Nmif = 1, Np, tol, ...)
## S4 method for signature mif
mif(object, Nmif, start, ivps,
    particles, rw.sd, Np, ic.lag, var.factor,
    cooling.type, cooling.fraction.50,
    method, tol, transform, ...)
## S4 method for signature mif
continue(object, Nmif = 1, ...)
## S4 method for signature mif
logLik(object, ...)
## S4 method for signature mif
conv.rec(object, pars, transform = FALSE, ...)
## S4 method for signature mifList
conv.rec(object, ...)
```

# **Arguments**

object Nmif start	An object of class pomp.  The number of filtering iterations to perform.  named numerical vector; the starting guess of the parameters.
ivps	optional character vector naming the initial-value parameters (IVPs) to be estimated. Every parameter named in ivps must have a positive random-walk standard deviation specified in rw.sd. If there are no non-IVP parameters with positive rw.sd, i.e., only IVPs are to be estimated, see below "Using mif to estimate initial-value parameters only".
particles	Function of prototype particles(Np,center,sd,) which sets up the starting particle matrix by drawing a sample of size Np from the starting particle distribution centered at center and of width sd. If particles is not supplied by the user, the default behavior is to draw the particles from a multivariate normal distribution with mean center and standard deviation sd.

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rw.sd

numeric vector with names; the intensity of the random walk to be applied to parameters. The random walk is only applied to parameters named in pars (i.e., not to those named in ivps). The algorithm requires that the random walk be nontrivial, so each element in rw.sd[pars] must be positive. rw.sd is also used to scale the initial-value parameters (via the particles function). Therefore, each element of rw.sd[ivps] must be positive. The following must be satisfied: names(rw.sd) must be a subset of names(start), rw.sd must be non-negative (zeros are simply ignored), the name of every positive element of rw.sd must be in either pars or ivps.

Np

the number of particles to use in filtering. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timestep, one may specify Np either as a vector of positive integers (of length length(time(object,t0=TRUE))) or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object,t0=TRUE)), Np(T) is the number of particles to sample at the end of the time-series.

ic.lag

a positive integer; the timepoint for fixed-lag smoothing of initial-value parameters. The mif update for initial-value parameters consists of replacing them by their filtering mean at time times[ic.lag], where times=time(object). It makes no sense to set ic.lag>length(times); if it is so set, ic.lag is set to length(times) with a warning.

For method="mif2", the default is ic.lag=length(times).

var.factor

a positive number; the scaling coefficient relating the width of the starting particle distribution to rw.sd. In particular, the width of the distribution of particles at the start of the first mif iteration will be random.walk.sd\*var.factor.

cooling.type, cooling.fraction.50

specifications for the cooling schedule, i.e., the manner in which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule.

When cooling.type="geometric", on the n-th mif iteration, the relative perturbation intensity is cooling.fraction.50^(n/50).

When cooling.type="hyperbolic", on the n-th mif iteration, the relative perturbation intensity is (s+1)/(s+n), where (s+1)/(s+50)=cooling.fraction.50. cooling.fraction.50 is the relative magnitude of the parameter perturbations after 50 mif iterations.

method

method sets the update rule used in the algorithm. method="mif" uses the iterated filtering update rule (Ionides 2006, 2011); method="unweighted" updates the parameter to the unweighted average of the filtering means of the parameters at each time; method="fp" updates the parameter to the filtering mean at the end of the time series. method="mif2" implements an incomplete version of the iterated Bayes map method of Ionides (2015). The latter method is, by every indication, both more efficient and more stable.

tol, max.fail See the description under pfilter.

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verbose logical; if TRUE, print progress reports.

transform logical; if TRUE, optimization is performed on the transformed scale, as defined

by the user-supplied parameter transformations (see pomp).

... additional arguments that override the defaults.

pars names of parameters.

## Re-running mif Iterations

To re-run a sequence of mif iterations, one can use the mif method on a mif object. By default, the same parameters used for the original mif run are re-used (except for weighted, tol, max.fail, and verbose, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

## **Continuing mif Iterations**

One can resume a series of mif iterations from where one left off using the continue method. A call to mif to perform Nmif=m iterations followed by a call to continue to perform Nmif=n iterations will produce precisely the same effect as a single call to mif to perform Nmif=m+n iterations. By default, all the algorithmic parameters are the same as used in the original call to mif. Additional arguments will override the defaults.

#### Using mif to estimate initial-value parameters only

One can use mif's fixed-lag smoothing to estimate only initial value parameters (IVPs). In this case, pars is left empty and the IVPs to be estimated are named in ivps. If theta is the current parameter vector, then at each mif iteration, Np particles are drawn from a distribution centered at theta and with width proportional to var.factor\*rw.sd, a particle filtering operation is performed, and theta is replaced by the filtering mean at time(object)[ic.lag]. Note the implication that, when mif is used in this way on a time series any longer than ic.lag, unnecessary work is done. If the time series in object is longer than ic.lag, consider replacing object with window(object,end=ic.lag).

#### Methods

Methods that can be used to manipulate, display, or extract information from a mif object:

**conv.rec** conv.rec(object, pars = NULL) returns the columns of the convergence-record matrix corresponding to the names in pars. By default, all rows are returned.

**logLik** Returns the value in the loglik slot. NB: this is *not* the same as the likelihood of the model at the MLE!

c Concatenates mif objects into an mifList.

**plot** Plots a series of diagnostic plots when applied to a mif or mifList object.

## **Details**

If particles is not specified, the default behavior is to draw the particles from a multivariate normal distribution. It is the user's responsibility to ensure that, if the optional particles argument is given, that the particles function satisfies the following conditions:

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particles has at least the following arguments: Np, center, sd, and . . . . Np may be assumed to be a positive integer; center and sd will be named vectors of the same length. Additional arguments may be specified; these will be filled with the elements of the userdata slot of the underlying pomp object (see pomp).

particles returns a length(center) x Np matrix with rownames matching the names of center and sd. Each column represents a distinct particle.

The center of the particle distribution returned by particles should be center. The width of the particle distribution should vary monotonically with sd. In particular, when sd=0, the particles should return matrices with Np identical columns, each given by the parameters specified in center.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### References

E. L. Ionides, C. Breto, & A. A. King, Inference for nonlinear dynamical systems, Proc. Natl. Acad. Sci. U.S.A., 103:18438–18443, 2006.

E. L. Ionides, A. Bhadra, Y. Atchad'e, & A. A. King, Iterated filtering, Annals of Statistics, 39:1776–1802, 2011.

E. L. Ionides, D. Nguyen, Y. Atchad\'e, S. Stoev, and A. A. King. Inference for dynamic and latent variable models via iterated, perturbed Bayes maps. Proc. Natl. Acad. Sci. U.S.A., 112:719–724, 2015.

A. A. King, E. L. Ionides, M. Pascual, and M. J. Bouma, Inapparent infections and cholera dynamics, Nature, 454:877–880, 2008.

#### See Also

pomp, pfilter

logmeanexp

The log-mean-exp trick

# **Description**

logmeanexp computes

$$\log \frac{1}{N} \sum_{n=1}^{N} e_i^x,$$

avoiding over- and under-flow in doing so.

#### **Usage**

logmeanexp(x, se = FALSE)

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## **Arguments**

x numeric

se logical; give approximate standard error?

## Value

log(mean(exp(x))) computed so as to avoid over- or underflow. If se = FALSE, the approximate standard error is returned as well.

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

# **Examples**

```
## generate a bifurcation diagram for the Ricker map
pompExample(ricker)
11 <- replicate(n=5,logLik(pfilter(ricker,Np=1000)))
## an estimate of the log likelihood:
logmeanexp(11)
## with standard error:
logmeanexp(11,se=TRUE)</pre>
```

LondonYorke

Historical childhood disease incidence data

# Description

LondonYorke is a data-frame containing the monthly number of reported cases of chickenpox, measles, and mumps from two American cities (Baltimore and New York) in the mid-20th century (1928–1972).

# Usage

data(LondonYorke)

#### References

W. P. London and J. A. Yorke, Recurrent Outbreaks of Measles, Chickenpox and Mumps: I. Seasonal Variation in Contact Rates, American Journal of Epidemiology, 98:453–468, 1973.

## **Examples**

```
data(LondonYorke)
plot(cases~time,data=LondonYorke,subset=disease=="measles",type=n,main="measles",bty=1)
lines(cases~time.data=LondonYorke.subset=disease=="measles"&town=="Baltimore".col="red")
lines(cases~time,data=LondonYorke,subset=disease=="measles"&town=="New York",col="blue")
legend("topright",legend=c("Baltimore","New York"),lty=1,col=c("red","blue"),bty=n)
plot(
     cases~time,
     data=LondonYorke,
     subset=disease=="chickenpox"&town=="New York".
     type=1,col="blue",main="chickenpox, New York",
    bty=1
    )
plot(
     cases~time,
     data=LondonYorke,
     subset=disease=="mumps"&town=="New York",
     type=1,col="blue",main="mumps, New York",
    bty=1
    )
```

Low-level-interface

pomp low-level interface

# **Description**

A pomp object implements a partially observed Markov process (POMP) model. Basic operations on this model (with shorthand terms) include:

- 1. simulation of the state process given parameters (rprocess)
- 2. evaluation of the likelihood of a given state trajectory given parameters (dprocess)
- 3. simulation of the observation process given the states and parameters (rmeasure)
- 4. evaluation of the likelihood of a set of observations given the states and parameters (dmeasure)
- 5. simulation from the prior probability distribution (rprior)
- 6. evaluation of the prior probability density (dprior)
- 7. simulation from the distribution of initial states, given parameters (init.state)
- 8. evaluation of the deterministic skeleton at a point in state space, given parameters (skeleton)
- 9. computation of a trajetory of the deterministic skeleton given parameters (trajectory)

**pomp** provides S4 methods that implement each of these basic operations. These operations can be combined to implement computations and statistical inference methods that depend only on a model's POMP structure. For convenience, parameter transformations may also be enclosed in a pomp object.

This page documents these elements.

## Usage

```
## S4 method for signature pomp
rprocess(object, xstart, times, params, offset = 0, ...)
## S4 method for signature pomp
dprocess(object, x, times, params, log = FALSE, ...)
## S4 method for signature pomp
rmeasure(object, x, times, params, ...)
## S4 method for signature pomp
dmeasure(object, y, x, times, params, log = FALSE, ...)
## S4 method for signature pomp
dprior(object, params, log = FALSE, ...)
## S4 method for signature pomp
rprior(object, params, ...)
## S4 method for signature pomp
init.state(object, params, t0, ...)
## S4 method for signature pomp
skeleton(object, x, t, params, ...)
## S4 method for signature pomp
trajectory(object, params, times, t0, as.data.frame = FALSE, ...)
## S4 method for signature pomp
pompLoad(object, ...)
## S4 method for signature pomp
pompUnload(object, ...)
```

# **Arguments**

object	an object of class pomp.
_	•
xstart	an nvar x nrep matrix containing the starting state of the system. Columns of xstart correspond to states; rows to components of the state vector. One independent simulation will be performed for each column. Note that in this case, params must also have nrep columns.
X	a rank-3 array containing states of the unobserved process. The dimensions of $x$ are nvars $x$ nrep $x$ ntimes, where nvars is the number of state variables, nrep is the number of replicates, and ntimes is the length of times.
У	a matrix containing observations. The dimensions of $y$ are nobs $x$ ntimes, where nobs is the number of observables and ntimes is the length of times.
times, t	a numeric vector (length ntimes) containing times. These must be in non-decreasing order.
params	a npar x nrep matrix of parameters. Each column is an independent parameter set and is paired with the corresponding column of x or xstart.
	In the case of init.state, params is a named vector of parameters.
offset	integer; the first offset times in times will not be returned.
t0	the initial time at which initial states are requested.
log	if TRUE, log probabilities are returned.
as.data.frame	logical; if TRUE, return the result as a data-frame.

... In trajectory, additional arguments are passed to the ODE integrator (if the skeleton is a vectorfield) and ignored if it is a map. See ode for a description of the additional arguments accepted.

In all other cases, additional arguments are ignored.

# rprocess

rprocess simulates the process-model portion of partially-observed Markov process.

When rprocess is called, the first entry of times is taken to be the initial time (i.e., that corresponding to xstart). Subsequent times are the additional times at which the state of the simulated processes are required.

rprocess returns a rank-3 array with rownames. Suppose x is the array returned. Then

```
dim(x)=c(nvars,nrep,ntimes-offset),
```

where nvars is the number of state variables (=nrow(xstart)), nrep is the number of independent realizations simulated (=ncol(xstart)), and ntimes is the length of the vector times. x[,j,k] is the value of the state process in the j-th realization at time times[k+offset]. The rownames of x must correspond to those of xstart.

## dprocess

dprocess evaluates the probability density of a sequence of consecutive state transitions.

dprocess returns a matrix of dimensions nrep x ntimes-1. If d is the returned matrix, d[j,k] is the likelihood of the transition from state x[,j,k-1] at time times[k-1] to state x[,j,k] at time times[k].

#### rmeasure

rmeasure simulate the measurement model given states and parameters.

rmeasure returns a rank-3 array of dimensions nobs x nrep x ntimes, where nobs is the number of observed variables.

#### dmeasure

dmeasure evaluates the probability density of observations given states.

dmeasure returns a matrix of dimensions nreps x ntimes. If d is the returned matrix, d[j,k] is the likelihood of the observation y[,k] at time times[k] given the state x[,j,k].

# dprior, rprior

dprior evaluates the prior probability density and rprior simulates from the prior.

## init.state

init.state returns an nvar x nrep matrix of state-process initial conditions when given an npar x nrep matrix of parameters, params, and an initial time t0. By default, t0 is the initial time defined when the pomp object ws constructed.

#### skeleton

The method skeleton evaluates the deterministic skeleton at a point or points in state space, given parameters. In the case of a discrete-time system, the skeleton is a map. In the case of a continuous-time system, the skeleton is a vectorfield. NB: skeleton just evaluates the deterministic skeleton; it does not iterate or integrate.

skeleton returns an array of dimensions nvar x nrep x ntimes. If f is the returned matrix, f[i,j,k] is the i-th component of the deterministic skeleton at time times[k] given the state x[,j,k] and parameters params[,j].

## trajectory

trajectory computes a trajectory of the deterministic skeleton of a Markov process. In the case of a discrete-time system, the deterministic skeleton is a map and a trajectory is obtained by iterating the map. In the case of a continuous-time system, the deterministic skeleton is a vector-field; trajectory uses the numerical solvers in **deSolve** to integrate the vectorfield.

trajectory returns an array of dimensions nvar x nrep x ntimes. If x is the returned matrix, x[i,j,k] is the i-th component of the state vector at time times[k] given parameters params[,j].

When the skeleton is a vectorfield, trajectory integrates it using ode. When the skeleton is a map, trajectory iterates it. By default, time is advanced 1 unit per iteration. The user can change this behavior by specifying the desired timestep using the argument skelmap.delta.t in the construction of the pomp object.

## **Parameter transformations**

User-defined parameter transformations enclosed in the pomp object can be accessed via partrans.

```
pompLoad, pompUnload
```

pompLoad and pompUnload cause compiled codes associated with object to be dynamically linked or unlinked, respectively. When Csnippets are used in the construction of a pomp object, the resulting shared-object library is dynamically loaded (linked) before each use, and unloaded afterward. These functions are provided because in some instances, greater control may be desired. These functions have no effect on shared-object libraries linked by the user.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

```
pomp, pomp methods
```

#### **Examples**

```
pompExample(ricker)
p <- parmat(c(r=42,phi=10,sigma=0.3,N.0=7,e.0=0),10)
t <- c(1:10,20,30)
t0 <- 0</pre>
```

```
x0 <- init.state(ricker,params=p,t0=t0)</pre>
x <- rprocess(ricker,xstart=x0,times=c(t0,t),params=p,offset=1)</pre>
y <- rmeasure(ricker,params=p,x=x,times=t)</pre>
11 <- dmeasure(ricker,y=y[,3,,drop=FALSE],x=x,times=t,params=p,log=TRUE)</pre>
apply(ll,1,sum)
f <- skeleton(ricker, x=x, t=t, params=p)</pre>
z <- trajectory(ricker,params=p,times=t,t0=t0)</pre>
## short arguments are recycled:
p <- c(r=42, phi=10, sigma=0.3, N.0=7, e.0=0)
t <- c(1:10,20,30)
t0 <- 0
x0 <- init.state(ricker,params=p,t0=t0)</pre>
x <- rprocess(ricker,xstart=x0,times=c(t0,t),params=p,offset=1)</pre>
y <- rmeasure(ricker,params=p,x=x,times=t)</pre>
11 <- dmeasure(ricker,y=y,x=x,times=t,params=p,log=TRUE)</pre>
f <- skeleton(ricker,x=x,t=t,params=p)</pre>
z <- trajectory(ricker,params=p,times=t,t0=t0)</pre>
```

MCMC proposal distributions

MCMC proposal distributions

# **Description**

Functions to construct proposal distributions for use with MCMC methods.

## Usage

```
mvn.diag.rw(rw.sd)
mvn.rw(rw.var)
```

## **Arguments**

rw.sd named numeric vector; random-walk SDs for a multivariate normal random-walk proposal with diagonal variance-covariance matrix.

rw.var square numeric matrix with row- and column-names. Specifies the variance-

covariance matrix for a multivariate normal random-walk proposal distribution.

# Value

Functions taking a single argument. Given a parameter vector, each returns a single draw from the corresponding proposal distribution.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

Nonlinear forecasting 31

## See Also

```
pmcmc, abc
```

Nonlinear forecasting Parameter estimation my maximum simulated quasi-likelihood (non-linear forecasting)

# **Description**

nlf calls an optimizer to maximize the nonlinear forecasting (NLF) goodness of fit. The latter is computed by simulating data from a model, fitting a nonlinear autoregressive model to the simulated time series, and quantifying the ability of the resulting fitted model to predict the data time series. NLF is an 'indirect inference' method using a quasi-likelihood as the objective function.

#### **Usage**

#### **Arguments**

object	A pomp object, with the data and model to fit to it.
start	Named numeric vector with guessed parameters.
est	Vector containing the names or indices of parameters to be estimated.
lags	A vector specifying the lags to use when constructing the nonlinear autoregressive prediction model. The first lag is the prediction interval.
period	numeric; period=NA means the model is nonseasonal. period>0 is the period of seasonal forcing in 'real time'.
tensor	logical; if FALSE, the fitted model is a generalized additive model with time mod period as one of the predictors, i.e., a gam with time-varying intercept. If TRUE, the fitted model is a gam with lagged state variables as predictors and time-periodic coefficients, constructed using tensor products of basis functions of state variables with basis functions of time.
nconverge	Number of convergence timesteps to be discarded from the model simulation.

nasymp Number of asymptotic timesteps to be recorded from the model simulation.

seed Integer specifying the random number seed to use. When fitting, it is usually

best to always run the simulations with the same sequence of random numbers, which is accomplished by setting seed to an integer. If you want a truly random

simulation, set seed=NULL.

transform.params

deprecated. Will be removed in a future version. Use transform instead.

transform logical; if TRUE, parameters are optimized on the transformed scale.

transform.data optional function. If specified, forecasting is performed using data and model

simulations transformed by this function. By default, transform.data is the identity function, i.e., no transformation is performed. The main purpose of transform.data is to achieve approximately multivariate normal forecasting errors. If data are univariate, transform.data should take a scalar and return a scalar. If data are multivariate, transform.data should assume a vector input

and return a vector of the same length.

nrbf A scalar specifying the number of radial basis functions to be used at each lag.

method Optimization method. Choices are subplex and any of the methods used by

optim.

skip.se Logical; if TRUE, skip the computation of standard errors.

verbose Logical; if TRUE, the negative log quasilikelihood and parameter values are

printed at each iteration of the optimizer.

bootstrap Logical; if TRUE the indices in bootsamp will determine which of the conditional

likelihood values be used in computing the quasi-loglikelihood.

bootsamp Vector of integers; used to have the quasi-loglikelihood evaluated using a boot-

strap re-sampling of the data set.

1q1. frac target fractional change in log quasi-likelihood for quadratic standard error esti-

mate

se.par.frac initial parameter-change fraction for quadratic standard error estimate

eval.only logical; if TRUE, no optimization is attempted and the quasi-loglikelihood value

is evaluated at the start parameters.

... Arguments that will be passed to optim or subplex in the control list.

#### **Details**

This runs an optimizer to maximize nlf. objfun.

#### Value

An object of class nlfd.pomp. logLik applied to such an object returns the log quasi likelihood. The \$ method allows extraction of arbitrary slots from the nlfd.pomp object.

## Author(s)

Stephen P. Ellner <spe2 at cornell dot edu>, Bruce E. Kendall <kendall at bren dot ucsb dot edu>, Aaron A. King <kingaa at umich dot edu>

ou2

#### References

The following papers describe and motivate the NLF approach to model fitting:

Ellner, S. P., Bailey, B. A., Bobashev, G. V., Gallant, A. R., Grenfell, B. T. and Nychka D. W. (1998) Noise and nonlinearity in measles epidemics: combining mechanistic and statistical approaches to population modeling. *American Naturalist* **151**, 425–440.

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Kendall, B. E., Briggs, C. J., Murdoch, W. W., Turchin, P., Ellner, S. P., McCauley, E., Nisbet, R. M. and Wood S. N. (1999) Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches. *Ecology* **80**, 1789–1805.

Kendall, B. E., Ellner, S. P., McCauley, E., Wood, S. N., Briggs, C. J., Murdoch, W. W. and Turchin, P. (2005) Population cycles in the pine looper moth (*Bupalus piniarius*): dynamical tests of mechanistic hypotheses. *Ecological Monographs* **75**, 259–276.

ou2

Two-dimensional discrete-time Ornstein-Uhlenbeck process

# **Description**

ou2 is a pomp object encoding a bivariate discrete-time Ornstein-Uhlenbeck process.

#### **Details**

If the state process is  $X(t) = (x_1(t), x_2(t))$ , then

$$X(t+1) = \alpha X(t) + \sigma \epsilon(t),$$

where  $\alpha$  and  $\sigma$  are 2x2 matrices,  $\sigma$  is lower-triangular, and  $\epsilon(t)$  is standard bivariate normal. The observation process is  $Y(t) = (y_1(t), y_2(t))$ , where  $y_i(t) \sim \operatorname{normal}(x_i(t), \tau)$ . The functions rprocess, dprocess, rmeasure, dmeasure, and skeleton are implemented using compiled C code for computational speed: see the source code for details.

#### See Also

pomp

# **Examples**

```
pompExample(ou2)
plot(ou2)
coef(ou2)
x <- simulate(ou2)
plot(x)
pf <- pfilter(ou2,Np=1000)
logLik(pf)</pre>
```

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parmat

Create a matrix of parameters

# **Description**

parmat is a utility that makes a vector of parameters suitable for use in pomp functions.

## Usage

```
parmat(params, nrep = 1)
```

# Arguments

params named numeric vector or matrix of parameters.

nrep number of replicates (columns) desired.

## Value

parmat returns a matrix consisting of nrep copies of params.

# Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

## **Examples**

```
## generate a bifurcation diagram for the Ricker map
pompExample(ricker)
p <- parmat(coef(ricker),nrep=500)
p["r",] <- exp(seq(from=1.5,to=4,length=500))
x <- trajectory(ricker,times=seq(from=1000,to=2000,by=1),params=p)
matplot(p["r",],x["N",,],pch=.,col=black,xlab="log(r)",ylab="N",log=x)</pre>
```

Particle filter

Particle filter

# **Description**

A plain vanilla sequential Monte Carlo (particle filter) algorithm. Resampling is performed at each observation.

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## Usage

```
## S4 method for signature pomp
pfilter(object, params, Np, tol = 1e-17,
   max.fail = Inf, pred.mean = FALSE, pred.var = FALSE,
   filter.mean = FALSE, save.states = FALSE,
   save.params = FALSE, seed = NULL,
   verbose = getOption("verbose"), ...)
## S4 method for signature pfilterd.pomp
pfilter(object, params, Np, tol, ...)
## S4 method for signature pfilterd.pomp
logLik(object, ...)
## S4 method for signature pfilterd.pomp
cond.logLik(object, ...)
## S4 method for signature pfilterd.pomp
eff.sample.size(object, ...)
## S4 method for signature pfilterd.pomp
pred.mean(object, pars, ...)
## S4 method for signature pfilterd.pomp
pred.var(object, pars, ...)
## S4 method for signature pfilterd.pomp
filter.mean(object, pars, ...)
```

## **Arguments**

object

An object of class pomp or inheriting class pomp.

params

A npars x Np numeric matrix containing the parameters corresponding to the initial state values in xstart. This must have a 'rownames' attribute. If it desired that all particles should share the same parameter values, one one may supply params as a named numeric vector.

Np

the number of particles to use. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may specify Np either as a vector of positive integers of length

```
length(time(object,t0=TRUE))
```

or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object, t0=TRUE)), Np(T) is the number of particles to sample at the end of the time-series. When object is of class mif, this is by default the same number of particles used in the mif iterations.

tol

positive numeric scalar; particles with likelihood less than tol are considered to be "lost". A filtering failure occurs when, at some time point, all particles are lost. When all particles are lost, the conditional likelihood at that time point is set to tol.

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max.fail integer; the maximum number of filtering failures allowed. If the number of filtering failures exceeds this number, execution will terminate with an error. By default, max.fail is set to infinity, so no error can be triggered. logical; if TRUE, the prediction means are calculated for the state variables and pred.mean parameters. pred.var logical; if TRUE, the prediction variances are calculated for the state variables and parameters. logical; if TRUE, the filtering means are calculated for the state variables and filter.mean parameters. save.states, save.params logical. If save.states=TRUE, the state-vector for each particle at each time is saved in the saved.states slot of the returned pfilterd.pomp object. If save.params=TRUE, the parameter-vector for each particle at each time is saved in the saved.params slot of the returned pfilterd.pomp object. optional; an object specifying if and how the random number generator should seed be initialized ('seeded'). If seed is an integer, it is passed to set. seed prior to any simulation and is returned as the "seed" element of the return list. By default, the state of the random number generator is not changed and the value of .Random. seed on the call is stored in the "seed" element of the return list. logical; if TRUE, progress information is reported as pfilter works. verbose Names of parameters. pars additional arguments that override the defaults.

#### Value

An object of class pfilterd.pomp. This class inherits from class pomp and contains the following additional slots:

**pred.mean, pred.var, filter.mean** matrices of prediction means, variances, and filter means, respectively. In each of these, the rows correspond to states and parameters (if appropriate), in that order, the columns to successive observations in the time series contained in object.

eff.sample.size numeric vector containing the effective number of particles at each time point.

cond.loglik numeric vector containing the conditional log likelihoods at each time point.

saved.states If pfilter was called with save.states=TRUE, this is the list of state-vectors at each time point, for each particle. It is a length-ntimes list of nvars-by-Np arrays. In particular, saved.states[[t]][,i] can be considered a sample from  $f[X_t|y_{1:t}]$ .

**saved.params** If pfilter was called with save.params=TRUE, this is the list of parameter-vectors at each time point, for each particle. It is a length-ntimes list of npars-by-Np arrays. In particular, saved.params[[t]][,i] is the parameter portion of the i-th particle at time t.

**seed** the state of the random number generator at the time pfilter was called. If the argument seed was specified, this is a copy; if not, this is the internal state of the random number generator at the time of call.

**Np, tol, nfail** the number of particles used, failure tolerance, and number of filtering failures, respectively.

loglik the estimated log-likelihood.

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These can be accessed using the \$ operator as if the returned object were a list. Note that if the argument params is a named vector, then these parameters are included in the params slot of the returned pfilterd.pomp object.

#### Methods

**logLik** Extracts the estimated log likelihood.

cond.logLik Extracts the estimated conditional log likelihood

$$\ell_t(\theta) = \operatorname{Prob}[y_t | y_1, \dots, y_{t-1}],$$

where  $y_t$  are the data, at time t.

eff.sample.size Extracts the (time-dependent) estimated effective sample size, computed as

$$\left(\sum_{i} w_{it}^{2}\right)^{-1},$$

where  $w_{it}$  is the normalized weight of particle i at time t.

**pred.mean, pred.var** Extract the mean and variance of the approximate prediction distribution. This prediction distribution is that of

$$X_t|y_1,\ldots,y_{t-1},$$

where  $X_t$ ,  $y_t$  are the state vector and data, respectively, at time t.

filter.mean Extract the mean of the filtering distribution, which is that of

$$X_t|y_1,\ldots,y_t,$$

where  $X_t$ ,  $y_t$  are the state vector and data, respectively, at time t.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

## References

M. S. Arulampalam, S. Maskell, N. Gordon, & T. Clapp. A Tutorial on Particle Filters for Online Nonlinear, Non-Gaussian Bayesian Tracking. IEEE Trans. Sig. Proc. 50:174–188, 2002.

## See Also

pomp, mif, pmcmc, bsmc2, and the tutorials on the package website.

# **Examples**

```
pompExample(gompertz)
pf <- pfilter(gompertz,Np=1000) ## use 1000 particles
plot(pf)
logLik(pf)
cond.logLik(pf) ## conditional log-likelihoods</pre>
```

```
eff.sample.size(pf)  ## effective sample size
logLik(pfilter(pf))  ## run it again with 1000 particles
## run it again with 2000 particles
pf <- pfilter(pf,Np=2000,filter.mean=TRUE)
fm <- filter.mean(pf)  ## extract the filtering means</pre>
```

Particle Markov Chain Monte Carlo

The particle Markov chain Metropolis-Hastings algorithm

# **Description**

The Particle MCMC algorithm for estimating the parameters of a partially-observed Markov process.

# Usage

# **Arguments**

object	An object of class pomp.
--------	--------------------------

Nmcmc The number of PMCMC iterations to perform.

start named numeric vector; the starting guess of the parameters.

proposal optional function that draws from the proposal distribution. Currently, the pro-

posal distribution must be symmetric for proper inference: it is the user's responsibility to ensure that it is. Several functions that construct appropriate proposal function are provided: see MCMC proposal functions for more information.

pars, rw.sd Deprecated. Will be removed in a future release.

Np a positive integer; the number of particles to use in each filtering operation.

tol numeric scalar; particles with log likelihood below tol are considered to be

"lost". A filtering failure occurs when, at some time point, all particles are lost.

max.fail integer; maximum number of filtering failures permitted. If the number of fail-

ures exceeds this number, execution will terminate with an error.

verbose logical; if TRUE, print progress reports.

. . . Additional arguments. These are currently ignored.

#### Value

An object of class pmcmc.

## **Re-running PMCMC Iterations**

To re-run a sequence of PMCMC iterations, one can use the pmcmc method on a pmcmc object. By default, the same parameters used for the original PMCMC run are re-used (except for tol, max.fail, and verbose, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

# **Continuing PMCMC Iterations**

One can continue a series of PMCMC iterations from where one left off using the continue method. A call to pmcmc to perform Nmcmc=m iterations followed by a call to continue to perform Nmcmc=n iterations will produce precisely the same effect as a single call to pmcmc to perform Nmcmc=m+n iterations. By default, all the algorithmic parameters are the same as used in the original call to pmcmc. Additional arguments will override the defaults.

#### **Details**

pmcmc implements an MCMC algorithm in which the true likelihood of the data is replaced by an unbiased estimate computed by a particle filter. This gives an asymptotically correct Bayesian procedure for parameter estimation (Andrieu and Roberts, 2009). An extension to give a correct Bayesian posterior distribution of unobserved state variables (as in Andrieu et al, 2010) has not yet been implemented.

#### Methods

**conv.rec** conv.rec(object, pars) returns the columns of the convergence-record matrix corresponding to the names in pars as an object of class mcmc or mcmc.list.

plot Diagnostic plots.

logLik Returns the value in the loglik slot.

c Concatenates pmcmc objects into a pmcmcList.

# Author(s)

Edward L. Ionides <ionides at umich dot edu>, Aaron A. King <kingaa at umich dot edu>

#### References

C. Andrieu, A. Doucet and R. Holenstein, Particle Markov chain Monte Carlo methods, J. R. Stat. Soc. B, to appear, 2010.

C. Andrieu and G.O. Roberts, The pseudo-marginal approach for efficient computation, Ann. Stat. 37:697-725, 2009.

# See Also

pomp, pfilter, and the tutorials on the package website.

pomp constructor

Constructor of the basic POMP object

## **Description**

This function constructs a pomp object, encoding a partially-observed Markov process model together with a uni- or multivariate time series. One implements the model by specifying its *components*, each of which can be written as R functions or, for much greater computational efficiency, using C code. The preferred way to specify most components (as detailed below) is through the use of Csnippets, snippets of C that are compiled and linked into a running R session.

# Usage

```
## S4 method for signature data.frame
pomp(data, times, t0, ..., rprocess, dprocess, rmeasure, dmeasure,
       measurement.model,
       skeleton, skeleton.type = c("map","vectorfield"), skelmap.delta.t = 1,
       initializer, rprior, dprior, params, covar, tcovar,
       obsnames, statenames, paramnames, covarnames, zeronames,
       PACKAGE, fromEstimationScale, toEstimationScale, globals)
## S4 method for signature numeric
pomp(data, times, t0, ..., rprocess, dprocess, rmeasure, dmeasure,
       measurement.model,
       skeleton, skeleton.type = c("map","vectorfield"), skelmap.delta.t = 1,
       initializer, rprior, dprior, params, covar, tcovar,
       obsnames, statenames, paramnames, covarnames, zeronames,
       PACKAGE, fromEstimationScale, toEstimationScale, globals)
## S4 method for signature matrix
pomp(data, times, t0, ..., rprocess, dprocess, rmeasure, dmeasure,
       measurement.model,
       skeleton, skeleton.type = c("map","vectorfield"), skelmap.delta.t = 1,
       initializer, rprior, dprior, params, covar, tcovar,
       obsnames, statenames, paramnames, covarnames, zeronames,
       PACKAGE, fromEstimationScale, toEstimationScale, globals)
## S4 method for signature pomp
pomp(data, times, t0, ..., rprocess, dprocess, rmeasure, dmeasure,
       measurement.model, skeleton, skeleton.type, skelmap.delta.t,
       initializer, rprior, dprior, params, covar, tcovar,
       obsnames, statenames, paramnames, covarnames, zeronames,
       PACKAGE, fromEstimationScale, toEstimationScale, globals)
```

# Arguments

data, times

The time series data and times at which observations are made. data can be specified as a vector, a matrix, a data-frame. Alternatively, a pomp object can be supplied in the data argument.

If data is a numeric vector, times must be a numeric vector of the same length.

If data is a matrix, it should have dimensions nobs x ntimes, where nobs is the number of observed variables and ntimes is the number of times at which observations were made (i.e., each column is a distinct observation of the nobs variables). In this case, times must be given as a numeric vector (of length ntimes).

If data is a data-frame, times must name the column of observation times. Note that, in this case, data will be internally coerced to an array with storage-mode 'double'.

times must be numeric and strictly increasing.

t0

The zero-time, at which the stochastic dynamical system is to be initialized. This must be no later than the time of the first observation, i.e., t0 <= times[1].

rprocess

optional function; a function of prototype

```
rprocess(xstart,times,params,...)
```

that simulates from the unobserved process. The form of this function is given below. **pomp** provides a number of plugins that construct appropriate rprocess arguments corresponding to several common stochastic simulation algorithms. See below for more details.

dprocess

optional function; a function of prototype

```
dprocess(x,times,params,log,...)
```

that evaluates the likelihood of a sequence of consecutive state transitions. The form of this function is given below. It is not typically necessary (or even feasible) to define dprocess. This functionality is provided to support future algorithm development.

rmeasure

optional; the measurement model simulator. This can be specified in one of four ways:

1. as a function of prototype

```
rmeasure(x,t,params,...)
```

that makes a draw from the observation process given states x, time t, and parameters params.

2. as the name of a native (compiled) routine with prototype pomp\_measure\_model\_simulator as defined in the header file 'pomp.h'. (To view the header file, execute

```
file.show(system.file("include/pomp.h",package="pomp"))
in an R session.)
```

- 3. using the formula-based measurement.model facility (see below).
- 4. as a snippet of C code (via Csnippet) that draws from the observation process as above. The last is typically the preferred option, as it results in much faster code execution.

dmeasure

optional; the measurement model probability density function. This can be specified in one of four ways:

 as a function of prototype dmeasure(y,x,t,params,log,...) that computes the p.d.f. of y given x, t, and params.

2. as the name of a native (compiled) routine with prototype pomp\_measure\_model\_density as defined in the header file 'pomp.h'. (To view the header file, execute file.show(system.file("include/pomp.h",package="pomp")) in an R session.)

- 3. using the formula-based measurement.model facility (see below).
- 4. as a snippet of C code (via Csnippet) that computes the p.d.f. as above.

The last is typically the preferred option, as it results in much faster code execution. As might be expected, if log=TRUE, this function should return the log likelihood.

#### measurement.model

optional; a formula or list of formulae, specifying the measurement model. These formulae are parsed internally to generate rmeasure and dmeasure functions. If measurement model is given it overrides any specification of rmeasure or dmeasure. **NB:** This is a convenience function, primarily designed to facilitate exploration; it will typically be possible to acclerate measurement model computations by writing dmeasure and/or rmeasure using Csnippets.

skeleton, skeleton.type, skelmap.delta.t

The function skeleton specifies the deterministic skeleton of the unobserved Markov process. If we are dealing with a discrete-time Markov process, its deterministic skeleton is a map: indicate this by specifying skeleton.type="map". In this case, the default assumption is that time advances 1 unit per iteration of the map; to change this, set skelmap.delta.t to the appropriate time-step. If we are dealing with a continuous-time Markov process, its deterministic skeleton is a vectorfield: indicate this by specifying skeleton.type="vectorfield".

The skeleton function can be specified in one of three ways:

- as an R function of prototype skeleton(x,t,params,...) that evaluates the deterministic skeleton at state x and time t given the parameters params,
- 2. as the name of a native (compiled) routine with prototype pomp\_skeleton as defined in the header file 'pomp.h'. (To view the header file, execute file.show(system.file("include/pomp.h",package="pomp")) in an R session.)
- 3. as a snippet of C code (via Csnippet) that performs this evaluation. The latter is typically the preferred option, for reasons of computational efficiency.

initializer

optional function of prototype

```
initializer(params, t0,...)
```

that yields initial conditions for the state process when given a vector, params, of parameters.

By default, any parameters in params, the names of which end in ".0", are assumed to be initial values of states. To initialize the unobserved state process, these are simply copied over as initial conditions. The names of the resulting state variables are obtained by dropping the ".0" suffix.

rprior

optional; function drawing a sample from a prior distribution on parameters. This can be specified in one of three ways:

1. as an R function of prototype

```
rprior(params,...)
```

that makes a draw from the prior distribution given params,

2. as the name of a native (compiled) routine with prototype pomp\_rprior as defined in the header file 'pomp.h', or (To view the header file, execute file.show(system.file("include/pomp.h",package="pomp")) in an R session.)

3. as a snippet of C code (via Csnippet).

As above, the latter is typically preferable.

optional; function evaluating the prior distribution. This can be specified in one of three ways:

- 1. as an R function of prototype dprior(params,log=FALSE,...) that evaluates the prior probability density,
- 2. as the name of a native (compiled) routine with prototype pomp\_dprior as defined in the header file 'pomp.h', or (To view the header file, execute file.show(system.file("include/pomp.h",package="pomp")) in an R session.)
- 3. as a snippet of C code (via Csnippet).

As above, the latter is typically preferable.

params

optional named numeric vector of parameters. This will be coerced internally to storage mode double.

covar, tcovar

An optional matrix or data frame of covariates: covar is the table of covariates (one column per variable); tcovar the corresponding times (one entry per row of covar).

covar can be specified as either a matrix or a data frame. In either case the columns are taken to be distinct covariates. If covar is a data frame, tcovar can be either the name or the index of the time variable.

If a covariate table is supplied, then the value of each of the covariates is interpolated as needed. The resulting interpolated values are passed to the corresponding functions as a numeric vector named covars; see below.

obsnames, statenames, paramnames, covarnames

Optional character vectors specifying the names of observables, state variables, parameters, and covariates, respectively. These are only used in the event that one or more of the basic functions (rprocess, dprocess, rmeasure, dmeasure, skeleton, rprior, dprior) are defined using Csnippet or native routines.

zeronames

optional character vector specifying the names of accumulator variables (see below).

**PACKAGE** 

An optional string giving the name of the dynamically loaded library in which any native routines are to be found.

dprior

fromEstimationScale, toEstimationScale

Optional functions specifying parameter transformations. Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. toEstimationScale and fromEstimationScale are transformations from the model scale to the estimation scale, and vice versa, respectively. These functions must have arguments params and .... toEstimationScale should transform parameters from the scale that rprocess, dprocess, rmeasure, dmeasure, skeleton, and initializer use internally to the scale used in estimation. fromEstimationScale should be the inverse of toEstimationScale. The parameter transformations can be defined (as above) using either R functions, native routines, or Csnippets.

Note that it is the user's responsibility to make sure that these transformations are mutually inverse. If obj is the constructed pomp object, and coef(obj) is non-empty, a simple check of this property is

```
x <- coef(obj,transform=TRUE)
obj1 <- obj
coef(obj1,transform=TRUE) <- x
identical(coef(obj),coef(obj1))
identical(coef(obj1,transform=TRUE),x).</pre>
```

By default, both functions are the identity transformation. See the demos,

```
demo(package="pomp"),
```

pompExample, and the tutorials on the package website for examples.

globals

optional character; C code that will be included in the source for (and therefore hard-coded into) the shared-object library created when the call to pomp uses Csnippets. If no Csnippets are used, globals has no effect.

Any additional arguments given to pomp will be stored in the pomp object and passed as arguments to each of the basic functions whenever they are evaluated.

#### Value

pomp returns an object of class pomp. If data is an object of class pomp, then by default the returned pomp object is identical to data. If additional arguments are given, these override the defaults.

## Important note

It is not typically necessary (or even feasible) to define all of the components rprocess, dprocess, rmeasure, dmeasure, and skeleton in any given problem. Each algorithm makes use of only a subset of these components. Any algorithm requiring a component that has not been defined will return an informative error.

## The state process model

Specification of process-model codes rprocess and/or dprocess in most cases is facilitated by **pomp**'s so-called **plugins**, which have been developed to handle common use-cases. Currently, if one's process model evolves in discrete time or one is willing to make such an approximation

(e.g., via an Euler approximation), then the euler.sim, discrete.time.sim, and onestep.sim plugins for rprocess and onestep.dens plugin for dprocess are available. In addition, for exact simulation of certain continuous-time Markov chains, an implementation of Gillespie's algorithm is available (see gillespie.sim). To learn more about the use of plugins, consult the help documentation (plugins) and the tutorials on the package website. Several of the demos and examples make use of these as well.

In specific cases, it may be possible to obtain increased computational efficiency by writing custom versions of rprocess and/or dprocess instead of using the plugins. If such custom versions are desired, the following describes how these functions should be written.

rprocess If the plugins are not used rprocess must be an R function with at least the following arguments: xstart, times, params, and .... It can also take additional arguments. It is guaranteed that these will be filled with the corresponding elements the user has included as additional arguments in the construction of the pomp object.

In calls to rprocess, xstart can be assumed to be an nvar x nrep matrix; its rows correspond to components of the state vector and columns correspond to independent realizations of the process. params will similarly be an npar x nrep matrix with rows corresponding to parameters and columns corresponding to independent realizations. Note that the columns of params correspond to those of xstart; in particular, they will agree in number. Both xstart and params are guaranteed to have rownames.

rprocess must return a rank-3 array with rownames. Suppose x is the array returned. Then  $\dim(x)=c(\text{nvars},\text{nrep},\text{ntimes})$ , where ntimes is the length of the vector times. x[,j,k] is the value of the state process in the j-th realization at time times[k]. In particular, x[,,1] must be identical to xstart. The rownames of x must correspond to those of xstart.

dprocess If the plugins are not used, dprocess must have at least the following arguments: x, times, params, log, and .... It may take additional arguments: again, these will be filled with the corresponding elements the user defines when the pomp object is constructed.

In calls to dprocess, x may be assumed to be an nvars x nrep x ntimes array, where these terms have the same meanings as above. params will be a matrix with rows corresponding to individual parameters and columns corresponding to independent realizations. The columns of params correspond to those of x; in particular, they will agree in number. Both x and params are guaranteed to have rownames.

dprocess must return a nrep x ntimes-1 matrix. Suppose d is the array returned. d[j,k] is the probability density of the transition from state x[,j,k-1] at time times[k-1] to state x[,j,k] at time times[k]. If log=TRUE, then the log of the pdf must be returned.

In writing this function, you may assume that the transitions are consecutive. It should be clear that, but for this assumption, it will in general be impossible to write the transition probabilities explicitly. In such cases, algorithms that make no use of dprocess, which are said to have the "plug and play" property, are useful. Most of the algorithms in **pomp** have this property. In particular, at present, no methods in pomp make use of dprocess.

## The observation process model

The following is a guide to writing the measurement model components as R functions. For a description on how to write these components using Csnippets, see the tutorials on the package website.

rmeasure if provided, must take at least the arguments x, t, params, and .... It may take additional arguments, which will be filled with user-specified data as above. x will be a named

numeric vector of length nvars (which has the same meaning as above). t will be a scalar quantity, the time at which the measurement is made. params will be a named numeric vector of length npars. The rmeasure function may take additional arguments which will be filled with user-specified data as above.

rmeasure must return a named numeric vector of length nobs, the number of observable variables.

dmeasure if provided, must take at least the arguments y, x, t, params, log, and .... y will be a named numeric vector of length nobs containing (actual or simulated) values of the observed variables; x will be a named numeric vector of length nvar containing state variables; params will be a named numeric vector containing parameters; and t will be a scalar, the corresponding observation time. The dmeasure function may take additional arguments which will be filled with user-specified data as above.

dmeasure must return a single numeric value, the probability density of y given x at time t. If log=TRUE, then dmeasure should return the log of the probability density.

#### The deterministic skeleton

The following describes how to specify the deterministic skeleton as an R function. For a description on how to write this component using Csnippets, see the tutorials on the package website.

If skeleton if provided, must have at least the arguments x, t, params, and .... x is a numeric vector containing the coordinates of a point in state space at which evaluation of the skeleton is desired. t is a numeric value giving the time at which evaluation of the skeleton is desired. Of course, these will be irrelevant in the case of an autonomous skeleton. params is a numeric vector holding the parameters. skeleton may take additional arguments, which will be filled, as above, with user-specified data.

skeleton must return a numeric vector of the same length as x, which contains the value vectorfield (if the dynamical system is continuous) or the value of the map (if the dynamical system is discrete), at the point x at time t.

## The state-process initializer

if provided, must have at least the arguments params, t0, and . . . . params will be a named numeric vector of parameters. t0 will be the time at which initial conditions are desired. initializer must return a named numeric vector of initial states.

# **Covariates**

If the pomp object contains covariates (via the covar argument; see above), then whenever any of the R functions described above are called, they will each be supplied with an additional argument covars. This will be a named numeric vector containing the (interpolated) values of the covariates at the time t. In particular, covars will have one value for each column of the covariate table.

# **Accumulator variables**

In formulating models, one often wishes to define a state variable that will accumulate some quantity over the interval between successive observations. **pomp** provides a facility to make such features more convenient. Specifically, variables named in the pomp's zeronames argument will be set to zero immediately following each observation. See euler.sir and the tutorials on the package website for examples.

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## Warning

Some error checking is done by pomp, but complete error checking is impossible. If the user-specified functions do not conform to the above specifications, then the results may be invalid. In particular, if both rmeasure and dmeasure are specified, the user should verify that these two functions correspond to the same probability distribution. If skeleton is specified, the user is responsible for verifying that it corresponds to a deterministic skeleton of the model. Each **pomp**-package algorithm uses some subset of the five basic functions (rprocess, dprocess, rmeasure, dmeasure, skeleton). If an algorithm requires a component that has not been specified, an informative error will be generated.

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp methods, pomp low-level interface, process model plugins

## **Examples**

pomp methods

Functions for manipulating, displaying, and extracting information from objects of the pomp class

## **Description**

This page documents the various methods that allow one to extract information from, display, plot, and modify pomp objects.

# Usage

```
## S4 method for signature pomp
coef(object, pars, transform = FALSE, ...)
## S4 replacement method for signature pomp
coef(object, pars, transform = FALSE, ...) <- value
## S4 method for signature pomp
obs(object, vars, ...)</pre>
```

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```
## S4 method for signature pomp
partrans(object, params, dir = c("fromEstimationScale",
      "toEstimationScale", "forward", "inverse"), ...)
## S4 method for signature pomp
plot(x, y, variables, panel = lines,
      nc = NULL, yax.flip = FALSE,
      mar = c(0, 5.1, 0, if (yax.flip) 5.1 else 2.1),
      oma = c(6, 0, 5, 0), axes = TRUE, ...)
## S4 method for signature pomp
print(x, ...)
## S4 method for signature pomp
show(object)
## S4 method for signature pomp
states(object, vars, ...)
## S4 method for signature pomp
time(x, t0 = FALSE, ...)
## S4 replacement method for signature pomp
time(object, t0 = FALSE, ...) <- value
## S4 method for signature pomp
timezero(object, ...)
## S4 replacement method for signature pomp
timezero(object, ...) <- value</pre>
## S4 method for signature pomp
window(x, start, end, ...)
## S4 method for signature pomp
as(object, class)
```

## **Arguments**

object,	X	The pomp	object.

pars optional character; names of parameters to be retrieved or set.

vars optional character; names of observed variables to be retrieved.

transform optional logical; should the parameter transformations be applied?

value numeric; values to be assigned.

params a vector or matrix of parameters to be transformed.

dir direction of the transformation. dir="forward" applies the transformation from the "natural" scale to the "internal" scale. This is the transformation specified by the parameter, transform argument to parameter the parameter.

by the parameter.transform argument to pomp; it is stored in the 'par.trans' slot of object. dir="inverse" applies the inverse transformation (stored in the

'par.untrans' slot).

to logical; if TRUE on a call to time, the zero time is prepended to the time vector;

if TRUE on a call to time<-, the first element in value is taken to be the initial

time.

start, end start and end times of the window.

class character; name of the class to which object should be coerced.

y ignored.

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variables optional character; names of variables to plot.

panel a function of prototype panel(x, col, bg, pch, type, ...) which gives the action to be carried out in each panel of the display.

nc the number of columns to use. Defaults to 1 for up to 4 series, otherwise to 2.

yax.flip logical; if TRUE, the y-axis (ticks and numbering) should flip from side 2 (left) to 4 (right) from series to series.

mar, oma the 'par' settings for 'mar' and 'oma' to use. Modify with care!

axes logical; indicates if x- and y- axes should be drawn.

Further arguments (either ignored or passed to underlying functions).

#### **Details**

coef coef(object) returns the contents of the params slot of object. coef(object,pars) returns only those parameters named in pars.

```
coef(object,transform=TRUE)
returns
parameter.inv.transform(coef(object))
, where parameter.inv.transform is the user parameter inverse transformation function specified when object was created. Likewise,
coef(object,pars,transform=TRUE)
returns
parameter.inv.transform(coef(object))[pars]
```

coef<- Assigns values to the params slot of the pomp object. coef(object) <- value has the
 effect of replacing the parameters of object with value. If coef(object) exists, then
 coef(object,pars) <- value replaces those parameters of object named in pars with the
 elements of value; the names of value are ignored. If some of the names in pars do not al ready name parameters in coef(object), then they are concatenated. If coef(object) does
 not exist, then coef(object,pars) <- value assigns value to the parameters of object;
 in this case, the names of object will be pars and the names of value will be ignored.
 coef(object,transform=TRUE) <- value assigns parameter.transform(value) to the
 params slot of object. Here, parameter.transform is the parameter transformation func tion specified when object was created. coef(object,pars,transform=TRUE) <- value
 first, discards any names the value may have, sets names(value) <- pars, and then replaces
 the elements of object's params slot parameter.transform(value). In this case, if some
 of the names in pars do not already name parameters in coef(object,transform=TRUE),
 then they are concatenated.</pre>

**obs** obs(object) returns the array of observations. obs(object, vars) gives just the observations of variables named in vars. vars may specify the variables by position or by name.

**states** states(object) returns the array of states. states(object, vars) gives just the state variables named in vars. vars may specify the variables by position or by name.

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**time** time(object) returns the vector of observation times. time(object,t0=TRUE) returns the vector of observation times with the zero-time t0 prepended.

time<- time(object) <- value replaces the observation times slot (times) of object with value. time(object,t0=TRUE) <- value has the same effect, but the first element in value is taken to be the initial time. The second and subsequent elements of value are taken to be the observation times. Those data and states (if they exist) corresponding to the new times are retained.</p>

timezero, timezero<- timezero(object) returns the zero-time t0. timezero(object) <- value
 sets the zero-time to value.</pre>

window window(x,start=t1,end=t2 returns a new pomp object, identical to x but with only the data in the window between times t1 and t2 (inclusive). By default, start is the time of the first observation and end is the time of the last.

show Displays the pomp object.

**plot** Plots the data and state trajectories (if the latter exist). Additional arguments are passed to the low-level plotting routine.

**print** Prints the pomp object in a nice way.

as A pomp object can be coerced to a data frame via

```
as(object, "data.frame").
```

The data frame contains the times, the data, and the state trajectories, if they exist.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp, pomp low-level interface, simulate, pfilter, probe.

POMP simulation

Simulations of a partially-observed Markov process

# Description

simulate generates simulations of the state and measurement processes.

## Usage

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#### **Arguments**

object An object of class pomp.

nsim The number of simulations to perform. Note that the number of replicates will

be nsim times ncol(xstart).

seed optional; if set, the pseudorandom number generator (RNG) will be initialized

with seed. the random seed to use. The RNG will be restored to its original

state afterward.

params either a named numeric vector or a numeric matrix with rownames. The param-

eters to use in simulating the model. If params is not given, then the contents of

the params slot of object will be used, if they exist.

states Do we want the state trajectories?

obs Do we want data-frames of the simulated observations?

times, t0 times specifies the times at which simulated observations will be made. t0

specifies the start time (the time at which the initial conditions hold). The default

for times is is times=time(object, t0=FALSE) and t0=timezero(object),

respectively.

as.data.frame, include.data

logical; if as.data.frame=TRUE, the results are returned as a data-frame. A factor variable, 'sim', distinguishes one simulation from another. If, in addition,

include.data=TRUE, the original data are included as an additional 'simula-

tion'. If as.data.frame=FALSE, include.data is ignored.

... further arguments that are currently ignored.

## **Details**

Simulation of the state process and of the measurement process are each accomplished by a single call to the user-supplied rprocess and rmeasure functions, respectively. This makes it possible for the user to write highly optimized code for these potentially expensive computations.

#### Value

If states=FALSE and obs=FALSE (the default), a list of nsim pomp objects is returned. Each has a simulated data set, together with the parameters used (in slot params) and the state trajectories also (in slot states). If times is specified, then the simulated observations will be at times times.

If nsim=1, then a single pomp object is returned (and not a singleton list).

If states=TRUE and obs=FALSE, simulated state trajectories are returned as a rank-3 array with dimensions nvar x (ncol(params)\*nsim) x ntimes. Here, nvar is the number of state variables and ntimes the length of the argument times. The measurement process is not simulated in this case.

If states=FALSE and obs=TRUE, simulated observations are returned as a rank-3 array with dimensions nobs x (ncol(params)\*nsim) x ntimes. Here, nobs is the number of observables.

If both states=TRUE and obs=TRUE, then a named list is returned. It contains the state trajectories and simulated observations as above.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp

# **Examples**

Power spectrum computation and matching

Power spectrum computation and spectrum-matching for partiallyobserved Markov processes

# **Description**

spect estimates the power spectrum of time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for frequency-domain parameter estimation (spect.match).

spect.match tries to match the power spectrum of the model to that of the data. It calls an optimizer to adjust model parameters to minimize the discrepancy between simulated and actual data.

## Usage

## **Arguments**

٠	•	
	object	An object of class pomp.
	params	$optional\ named\ numeric\ vector\ of\ model\ parameters.\ By\ default, \verb"params=coef" (object").$
	vars	optional; names of observed variables for which the power spectrum will be computed. This must be a subset of rownames(obs(object)). By default, the spectrum will be computed for all observables.
	kernel.width	width parameter for the smoothing kernel used for calculating the estimate of the spectrum.
	nsim	number of model simulations to be computed.
	seed	optional; if non-NULL, the random number generator will be initialized with this seed for simulations. See simulate.
	transform	function; this transformation will be applied to the observables prior to estimation of the spectrum, and prior to any detrending.
	detrend	de-trending operation to perform. Options include no detrending, and subtraction of constant, linear, and quadratic trends from the data. Detrending is applied to each data series and to each model simulation independently.
	weights	optional. The mismatch between model and data is measured by a weighted average of mismatch at each frequency. By default, all frequencies are weighted equally. weights can be specified either as a vector (which must have length equal to the number of frequencies) or as a function of frequency. If the latter, weights(freq) must return a nonnegative weight for each frequency.
	start	named numeric vector; the initial guess of parameters.
	est	character vector; the names of parameters to be estimated.
	method	Optimization method. Choices are subplex and any of the methods used by optim.
	verbose	logical; print diagnostic messages?
	eval.only	logical; if TRUE, no optimization is attempted. Instead, the probe-mismatch value is simply evaluated at the start parameters.
	fail.value	optional scalar; if non-NA, this value is substituted for non-finite values of the objective function.

# **Details**

. . .

A call to spect results in the estimation of the power spectrum for the (transformed, detrended) data and nsim model simulations. The results of these computations are stored in an object of class spect.pomp.

Additional arguments. In the case of spect, these are currently ignored. In the

case of spect.match, these are passed to optim or subplex in the control list.

A call to spect.match results in an attempt to optimize the agreement between model and data spectrum over the parameters named in est. The results, including coefficients of the fitted model and power spectra of fitted model and data, are stored in an object of class spect.matched.pomp.

#### Value

spect returns an object of class spect.pomp, which is derived from class pomp and therefore has all the slots of that class. In addition, spect.pomp objects have the following slots:

kernel.width width parameter of the smoothing kernel used.

transform transformation function used.

freq numeric vector of the frequencies at which the power spectrum is estimated.

datspec, simspec estimated power spectra for data and simulations, respectively.

**pvals** one-sided p-values: fraction of the simulated spectra that differ more from the mean simulated spectrum than does the data. The metric used is  $L^2$  distance.

detrend detrending option used.

spect.match returns an object of class spect.matched.pomp, which is derived from class {spect.pomp} and therefore has all the slots of that class. In addition, spect.matched.pomp objects have the following slots:

est, weights, fail.value values of the corresponding arguments in the call to spect.match.

evals number of function and gradient evaluations by the optimizer. See optim.

value Value of the objective function.

convergence, msg Convergence code and message from the optimizer. See optim.

#### Author(s)

Daniel C. Reuman, Cai GoGwilt, Aaron A. King

## References

D.C. Reuman, R.A. Desharnais, R.F. Costantino, O. Ahmad, J.E. Cohen (2006) Power spectra reveal the influence of stochasticity on nonlinear population dynamics. *Proceedings of the National Academy of Sciences* **103**, 18860-18865.

D.C. Reuman, R.F. Costantino, R.A. Desharnais, J.E. Cohen (2008) Color of environmental noise affects the nonlinear dynamics of cycling, stage-structured populations. *Ecology Letters*, **11**, 820-830.

# See Also

```
pomp, probe
```

## **Examples**

Probe functions 55

Probe functions

Some useful probes for partially-observed Markov processes

## **Description**

Several simple and configurable probes are provided with in the package. These can be used directly and as templates for custom probes.

# Usage

# Arguments

var, vars	character; the name(s) of the observed variable(s).
trim	the fraction of observations to be trimmed (see mean).
transform	transformation to be applied to the data before the probe is computed.
na.rm	if TRUE, remove all NA observations prior to computing the probe.
kernel.width	width of modified Daniell smoothing kernel to be used in power-spectrum computation: see kernel.
prob	a single probability; the quantile to compute: see quantile.

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lags In probe.ccf, a vector of lags between time series. Positive lags correspond to x advanced relative to y; negative lags, to the reverse. In probe.nlar, a vector of lags present in the nonlinear autoregressive model that will be fit to the actual and simulated data. See Details, below, for a precise description. powers the powers of each term (corresponding to lags) in the the nonlinear autoregressive model that will be fit to the actual and simulated data. See Details, below, for a precise description. Compute autocorrelation or autocovariance? type ref empirical reference distribution. Simulated data will be regressed against the values of ref, sorted and, optionally, differenced. The resulting regression coefficients capture information about the shape of the marginal distribution. A

> good choice for ref is the data itself. order of polynomial regression. order of differencing to perform.

... Additional arguments to be passed through to the probe computation.

#### **Details**

order diff

Each of these functions is relatively simple. See the source code for a complete understanding of what each does.

probe.mean, probe.median, probe.var, probe.sd return functions that compute the mean, median, variance, and standard deviation of variable var, respectively.

probe.period returns a function that estimates the period of the Fourier component of the var series with largest power.

probe.marginal returns a function that regresses the marginal distribution of variable var against the reference distribution ref. If diff>0, the data and the reference distribution are first differenced diff times and centered. Polynomial regression of order order is used. This probe returns order regression coefficients (the intercept is zero).

probe.nlar returns a function that fit a nonlinear (polynomial) autoregressive model to the univariate series (variable var). Specifically, a model of the form  $y_t = \sum \beta_k y_{t-\tau_k}^{p_k} + \epsilon_t$  will be fit, where  $\tau_k$  are the lags and  $p_k$  are the powers. The data are first centered. This function returns the regression coefficients,  $\beta_k$ .

probe.acf returns a function that, if type=="covariance", computes the autocovariance of variable var at lags lags; if type=="correlation", computes the autocorrelation of variable var at lags lags.

probe.ccf returns a function that, if type=="covariance", computes the cross covariance of the
 two variables named in vars at lags lags; if type=="correlation", computes the cross
 correlation.

probe quantile returns a function that estimates the prob-th quantile of variable var.

## Value

A call to any one of these functions returns a probe function, suitable for use in probe or probe.match. That is, the function returned by each of these takes a data array (such as comes from a call to obs) as input and returns a single numerical value.

## Author(s)

Daniel C. Reuman (d.reuman at imperial dot ac dot uk)

Aaron A. King (kingaa at umich dot edu)

#### References

- B. E. Kendall, C. J. Briggs, W. M. Murdoch, P. Turchin, S. P. Ellner, E. McCauley, R. M. Nisbet, S. N. Wood Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches, Ecology, 80:1789–1805, 1999.
- S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems, Nature, 466: 1102–1104, 2010.

#### See Also

pomp

Probes and synthetic likelihood

Probe a partially-observed Markov process by computing summary statistics and the synthetic likelihood.

# Description

probe applies one or more "probes" to time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for "probe-matching", a generalized method-of-moments approach to parameter estimation. probe.match calls an optimizer to adjust model parameters to do probe-matching, i.e., to minimize the discrepancy between simulated and actual data. This discrepancy is measured using the "synthetic likelihood" as defined by Wood (2010). probe.match.objfun constructs an objective function for probe-matching suitable for use in optim-like optimizers.

# Usage

#### **Arguments**

object	An object of class pomp.
Object	All object of class pollip.

probes A single probe or a list of one or more probes. A probe is simply a scalar- or

vector-valued function of one argument that can be applied to the data array of a pomp. A vector-valued probe must always return a vector of the same size. A number of useful examples are provided with the package: see probe functions).

params optional named numeric vector of model parameters. By default, params=coef(object).

nsim The number of model simulations to be computed.

seed optional; if non-NULL, the random number generator will be initialized with this

seed for simulations. See simulate-pomp.

start named numeric vector; the initial guess of parameters.

est character vector; the names of parameters to be estimated.

method Optimization method. Choices refer to algorithms used in optim, subplex, and

nloptr.

verbose logical; print diagnostic messages?

fail.value optional numeric scalar; if non-NA, this value is substituted for non-finite values

of the objective function. It should be a large number (i.e., bigger than any

legitimate values the objective function is likely to take).

transform logical; if TRUE, optimization is performed on the transformed scale.

... Additional arguments. In the case of probe, these are currently ignored. In the

case of probe.match, these are passed to the optimizer (one of optim, subplex, nloptr, or sannbox). These are passed via the optimizer's control list (in the case of optim, subplex, and sannbox) or the opts list (in the case of nloptr).

#### **Details**

A call to probe results in the evaluation of the probe(s) in probes on the data. Additionally, nsim simulated data sets are generated (via a call to simulate) and the probe(s) are applied to each of these. The results of the probe computations on real and simulated data are stored in an object of class probed.pomp.

A call to probe match results in an attempt to optimize the agreement between model and data, as measured by the specified probes, over the parameters named in est. The results, including coefficients of the fitted model and values of the probes for data and fitted-model simulations, are stored in an object of class probe matched pomp.

The objective function minimized by probe.match — in a form suitable for use with optim-like optimizers — is created by a call to probe.match.objfun. Specifically, probe.match.objfun will return a function that takes a single numeric-vector argument that is assumed to cotain the parameters named in est, in that order. This function will return the negative synthetic log likelihood for the probes specified.

#### Value

probe returns an object of class probed.pomp. probed.pomp is derived from the pomp class and therefore have all the slots of pomp. In addition, a probed.pomp class has the following slots:

**probes** list of the probes applied.

**datvals, simvals** values of each of the probes applied to the real and simulated data, respectively. **quantiles** fraction of simulations with probe values less than the value of the probe of the data.

**pvals** two-sided p-values: fraction of the simvals that deviate more extremely from the mean of the simvals than does datavals.

**synth.loglik** the log synthetic likelihood (Wood 2010). This is the likelihood assuming that the probes are multivariate-normally distributed.

probe.match returns an object of class probe.matched.pomp, which is derived from class probed.pomp. probe.matched.pomp objects therefore have all the slots above plus the following:

**est, transform, fail.value** values of the corresponding arguments in the call to probe.match.

**value** value of the objective function at the optimum.

evals number of function and gradient evaluations by the optimizer. See optim.

convergence, msg Convergence code and message from the optimizer. See optim and nloptr.

probe.match.objfun returns a function suitable for use as an objective function in an optim-like optimizer.

# Methods

plot displays diagnostic plots.

summary displays summary information.

**values** extracts the realized values of the probes on the data and on the simulations as a data frame in long format. The variable . id indicates whether the probes are from the data or simulations.

logLik returns the synthetic likelihood for the probes. NB: in general, this is not the same as the likelihood.

**as, as.data.frame** when a 'probed.pomp' is coerced to a 'data.frame', the first row gives the probes applied to the data; the rest of the rows give the probes evaluated on simulated data. The rownames of the result can be used to distinguish these.

In addition, slots of this object can be accessed via the \$ operator.

## Author(s)

Daniel C. Reuman, Aaron A. King

#### References

- B. E. Kendall, C. J. Briggs, W. M. Murdoch, P. Turchin, S. P. Ellner, E. McCauley, R. M. Nisbet, S. N. Wood Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches, Ecology, 80:1789–1805, 1999.
- S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems, Nature, 466: 1102–1104, 2010.

## See Also

pomp, probe functions, spect, and the tutorials on the package website.

## **Examples**

```
pompExample(ou2)
good <- probe(</pre>
              ou2,
              probes=list(
                y1.mean=probe.mean(var="y1"),
                y2.mean=probe.mean(var="y2"),
                y1.sd=probe.sd(var="y1"),
                y2.sd=probe.sd(var="y2"),
                extra=function(x)max(x["y1",])
                ),
              nsim=500
summary(good)
plot(good)
bad <- probe(</pre>
             params=c(alpha.1=0.1,alpha.4=0.2,x1.0=0,x2.0=0,
                       alpha.2=-0.5,alpha.3=0.3,
                       sigma.1=3, sigma.2=-0.5, sigma.3=2,
                       tau=1),
             probes=list(
               y1.mean=probe.mean(var="y1"),
               y2.mean=probe.mean(var="y2"),
               y1.sd=probe.sd(var="y1"),
               y2.sd=probe.sd(var="y2"),
               extra=function(x)range(x["y1",])
               ),
             nsim=500
summary(bad)
plot(bad)
```

Process model plugins Plug-ins for state-process models

## **Description**

The functions documented here can be used to specify the rprocess and dprocess slots for a pomp model. There are options for discrete- and continuous-time Markov processes.

## Usage

```
onestep.sim(step.fun, PACKAGE)
euler.sim(step.fun, delta.t, PACKAGE)
discrete.time.sim(step.fun, delta.t = 1, PACKAGE)
gillespie.sim(rate.fun, v, d, PACKAGE)
onestep.dens(dens.fun, PACKAGE)
```

## **Arguments**

step.fun

This can be either an R function, the name of a compiled, dynamically loaded native function containing the model simulator, or a Csnippet. The latter is the preferred option. It should be written to take a single Euler step from a single point in state space.

For an explanation and examples on the use of Csnippet to write fast simulators, see the tutorials on the package website.

If it is an R function, it should have prototype

```
step.fun(x,t,params,delta.t,...).
```

Here, x is a named numeric vector containing the value of the state process at time t, params is a named numeric vector containing parameters, and delta.t is the length of the Euler time-step.

If step. fun is the name of a native function, it must be of type pomp\_onestep\_sim as defined in the header file 'pomp.h', which is included with the **pomp** package. Do

```
file.show(system.file("include/pomp.h",package="pomp"))
```

to view this header file. For details on how to write such codes, see Details.

rate.fun

This can be either an R function, a Csnippet, or the name of a compiled, dynamically loaded native function that computes the transition rates. If it is an R function, it should be of the form rate.fun(j,x,t,params,...). Here, j is the number of the event, x is a named numeric vector containing the value of the state process at time t and params is a named numeric vector containing parameters.

For examples on the use of Csnippet to write fast simulators easily, see tutorials on the package website.

If rate.fun is a native function, it must be of type pomp\_ssa\_rate\_fn as defined in the header 'pomp.h', which is included with the package. For details on how to write such codes, see Details.

v, d

Matrices that specify the continuous-time Markov process in terms of its elementary events. Each should have dimensions nvar x nevent, where nvar is the number of state variables and nevent is the number of elementary events. v describes the changes that occur in each elementary event: it will usually comprise the values 1, -1, and 0 according to whether a state variable is incremented, decremented, or unchanged in an elementary event. d is a binary matrix that describes the dependencies of elementary event rates on state variables: d[i,j] will have value 1 if event rate j must be updated as a result of a change in state variable i and 0 otherwise

dens.fun

This can be either an R function, a Csnippet, or a compiled, dynamically loaded native function containing the model transition log probability density function. If it is an R function, it should be of the form

dens.fun(x1, x2, t1, t2, params, ...).

Here, x1 and x2 are named numeric vectors containing the values of the state process at times t1 and t2, params is a named numeric vector containing parameters.

If dens. fun is the name of a native function, it should be of type pomp\_onestep\_pdf as defined in the header 'pomp.h', which is included with the **pomp** package. This function should return the log likelihood of a transition from x1 at time t1 to x2 at time t2, assuming that no intervening transitions have occurred. For details on how to write such codes, see Details.

delta.t

Size of Euler time-steps.

**PACKAGE** 

an optional argument that specifies to which dynamically loaded library we restrict the search for the native routines. If this is "base", we search in the R executable itself. This argument is ignored if step. fun, rate. fn, or dens. fun is provided as an R function or a Csnippet.

# **Details**

onestep.sim is the appropriate choice when it is possible to simulate the change in state from one time to another, regardless of how large the interval between them is. To use onestep.sim, you must write a function step. fun that will advance the state process from one arbitrary time to another. euler.sim is appropriate when one cannot do this but can compute the change in state via a sequence of smaller steps. This is desirable, for example, if one is simulating a continuous time process but is willing to approximate it using an Euler approach. discrete.time.sim is appropriate when the process evolves in discrete time.

To use euler.sim or discrete.time.sim, you must write a function step.fun that will take a single Euler step, of size at most delta.t. The functions euler.sim and discrete.time.sim will create simulators that take as many steps as needed to get from one time to another. See below for information on how euler.sim chooses the actual step size it uses.

gillespie.sim allows exact simulation of a continuous-time, discrete-state Markov process using Gillespie's algorithm. This is an "event-driven" approach: correspondingly, to use gillespie.sim, you must write a function rate. fun that computes the rates of each elementary kind of event and specify two matrices (d, v) that describe, respectively, the dependencies of each rate and the consequences of each event.

onestep.dens will generate a suitable dprocess function when one can compute the likelihood of a given state transition simply by knowing the states at two times under the assumption that the state has not changed between the times. This is typically possible, for instance, when the rprocess function is implemented using onestep.sim, euler.sim, or discrete.time.sim. [NB: currently, there are no high-level algorithms in **pomp** that use dprocess. This function is provided for completeness only, with an eye toward future development.]

If step. fun is written as an R function, it must have at least the arguments x, t, params, delta.t, and .... On a call to this function, x will be a named vector of state variables, t a scalar time, and params a named vector of parameters. The length of the Euler step will be delta.t. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t, of the covariates. This is accomplished via interpolation of the user-supplied covariate table. Additional arguments may be given: these will be filled by the correspondingly-named elements in the userdata slot of the pomp object (see pomp).

If step.fun is written in a native language, it must be a function of type pomp\_onestep\_sim as specified in the header 'pomp.h' included with the package. Execute

```
file.show(system.file("include/pomp.h",package="pomp.h"))
```

to view this file.

If rate fun is written as an R function, it must have at least the arguments j, x, t, params, and . . . . Here, j is the an integer that indicates for which of the elementary events the current rate is desired. x is a named vector containing the value of the state process at time t, and params is a named vector containing parameters. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t, of the covariates. This is accomplished via interpolation of the covariate table. If rate fun is a native function, it must be of type pomp\_ssa\_rate\_fn as defined in the header 'pomp.h'; see above for instructions on how to view this file.

In writing dens.fun, you must assume that no state transitions have occurred between t1 and t2. If dens.fun is written as an R function, it must have at least the arguments x1, x2, t1, t2, params, and .... On a call to this function, x1 and x2 will be named vectors of state variables at times t1 and t2, respectively. The named vector params contains the parameters. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t1, of the covariates. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t1, of the covariates. This is accomplished via interpolation of the covariate table. As above, any additional arguments will be filled by the correspondingly-named elements in the userdata slot of the pomp object (see pomp). If dens.fun is written in a native language, it must be a function of type pomp\_onestep\_pdf as defined in the header 'pomp.h' included with the package; see above for instructions on how to view this file.

#### Value

onestep.sim, euler.sim, discrete.time.sim, and gillespie.sim each return functions suitable for use as the argument rprocess argument in pomp.

onestep. dens returns a function suitable for use as the argument dprocess in pomp.

64 rw2

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp and the tutorials on the package website.

ricker

Ricker model with Poisson observations.

# Description

ricker is a pomp object encoding a stochastic Ricker model with Poisson measurement error.

## **Details**

The state process is  $N_{t+1} = rN_t \exp(-N_t + e_t)$ , where the  $e_t$  are i.i.d. normal random deviates with zero mean and variance  $\sigma^2$ . The observed variables  $y_t$  are distributed as  $Poisson(\phi N_t)$ .

#### See Also

pomp, gompertz, and the tutorials on the package website.

# **Examples**

```
pompExample(ricker)
plot(ricker)
coef(ricker)
```

rw2

Two-dimensional random-walk process

# Description

rw2 is a pomp object encoding a 2-D normal random walk.

# **Details**

The random-walk process is fully but noisily observed.

## See Also

pomp, ou2

Simulated annealing 65

## **Examples**

```
pompExample(rw2)
plot(rw2)
x <- simulate(rw2,nsim=10,seed=20348585L,params=c(x1.0=0,x2.0=0,s1=1,s2=3,tau=1))
plot(x[[1]])</pre>
```

Simulated annealing

Simulated annealing with box constraints.

## **Description**

sannbox is a straightforward implementation of simulated annealing with box constraints.

# Usage

```
sannbox(par, fn, control = list(), ...)
```

# **Arguments**

par Initial values for the parameters to be optimized over.

fn A function to be minimized, with first argument the vector of parameters over

which minimization is to take place. It should return a scalar result.

control A named list of control parameters. See 'Details'.

... ignored.

#### **Details**

The control argument is a list that can supply any of the following components:

trace Non-negative integer. If positive, tracing information on the progress of the optimization is produced. Higher values may produce more tracing information.

fnscale An overall scaling to be applied to the value of fn during optimization. If negative, turns the problem into a maximization problem. Optimization is performed on fn(par)/fnscale.

parscale A vector of scaling values for the parameters. Optimization is performed on par/parscale and these should be comparable in the sense that a unit change in any element produces about a unit change in the scaled value.

maxit The total number of function evaluations: there is no other stopping criterion. Defaults to 10000.

temp starting temperature for the cooling schedule. Defaults to 1.

tmax number of function evaluations at each temperature. Defaults to 10.

candidate.dist function to randomly select a new candidate parameter vector. This should be a function with three arguments, the first being the current parameter vector, the second the temperature, and the third the parameter scaling. By default, candidate.dist is

```
function(par,temp,scale) rnorm(n=length(par),mean=par,sd=scale*temp)
```

66 sir

sched cooling schedule. A function of a three arguments giving the temperature as a function of iteration number and the control parameters temp and tmax. By default, sched is

```
function(k, temp, tmax) temp/log(((k-1)%/%tmax)*tmax+exp(1))
```

.

Alternatively, one can supply a numeric vector of temperatures. This must be of length at least maxit.

#### Value

sannbox returns a list with components:

**counts** two-element integer vector. The first number gives the number of calls made to fn. The second number is provided for compatibility with optim and will always be NA.

**convergence** provided for compatibility with optim; will always be 0.

final.params last tried value of par.

final.value value of fn corresponding to final.params.

par best tried value of par.

value value of fn corresponding to par.

#### Author(s)

Daniel Reuman, Imperial College London and Aaron A. King <kingaa at umich dot edu>

## See Also

traj.match, probe.match.

sir

Compartmental epidemiological models

# **Description**

euler.sir is a pomp object encoding a simple seasonal SIR model. Simulation is performed using an Euler multinomial approximation. gillespie.sir has the same model implemented using Gillespie's algorithm. bbs is a nonseasonal SIR model together with data from a 1978 outbreak of influenza in a British boarding school.

## **Details**

This and similar examples are discussed and constructed in tutorials available on the package website.

The boarding school influenza outbreak is described in Anonymous (1978).

Trajectory matching 67

## References

Anonymous (1978). Influenza in a boarding school. British Medical Journal 1:587

#### See Also

pomp and the tutorials on the package website.

## **Examples**

```
pompExample(euler.sir)
plot(euler.sir)
plot(simulate(euler.sir,seed=20348585))
coef(euler.sir)

pompExample(gillespie.sir)
plot(gillespie.sir)
plot(simulate(gillespie.sir,seed=20348585))
coef(gillespie.sir)

pompExample(bbs)
plot(bbs)
coef(bbs)
```

Trajectory matching

Parameter estimation by fitting the trajectory of a model's deterministic skeleton to data

# Description

This function attempts to match trajectories of a model's deterministic skeleton to data. Trajectory matching is equivalent to maximum likelihood estimation under the assumption that process noise is entirely absent, i.e., that all stochasticity is measurement error. Accordingly, this method uses only the skeleton and dmeasure components of a POMP model.

## Usage

#### **Arguments**

object A pomp object. If object has no skeleton slot, an error will be generated.

start named numeric vector containing an initial guess for parameters. By default

start=coef(object) if the latter exists.

params optional named numeric vector of parameters. This should contain all parame-

ters needed by the skeleton and dmeasure slots of object. In particular, any parameters that are to be treated as fixed should be present here. Parameter values given in params for parameters named in est will be ignored. By default,

params=coef(object) if the latter exists.

est character vector containing the names of parameters to be estimated. In the case

of traj.match.objfun, the objective function that is constructed will assume

that its argument contains the parameters in this order.

method Optimization method. Choices are subplex, "sannbox", and any of the methods

used by optim.

transform logical; if TRUE, optimization is performed on the transformed scale.

... Extra arguments that will be passed either to the optimizer (optim, subplex,

nloptr, or sannbox, via their control (optim, subplex, sannbox) or opts (nloptr) lists) or to the ODE integrator. In traj.match, extra arguments will be passed to the optimizer. In traj.match.objfun, extra arguments are passed to trajectory. If extra arguments are needed by both optimizer and trajectory, construct an objective function first using traj.match.objfun, then give this

objective function to the optimizer.

## Details

In **pomp**, trajectory matching is the term used for maximizing the likelihood of the data under the assumption that there is no process noise. Specifically, traj.match calls an optimizer (optim, subplex, and sannbox are the currently supported options) to minimize an objective function. For any value of the model parameters, this objective function is calculated by

- 1. computing the deterministic trajectory of the model given the parameters. This is the trajectory returned by trajectory, which relies on the model's deterministic skeleton as specified in the construction of the pomp object object.
- 2. evaluating the negative log likelihood of the data under the measurement model given the deterministic trajectory and the model parameters. This is accomplished via the model's dmeasure slot. The negative log likelihood is the objective function's value.

The objective function itself — in a form suitable for use with optim-like optimizers — is created by a call to traj.match.objfun. Specifically, traj.match.objfun will return a function that takes a single numeric-vector argument that is assumed to cotain the parameters named in est, in that order.

## Value

traj.match returns an object of class traj.matched.pomp. This class inherits from class pomp and contains the following additional slots:

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**transform, est** the values of these arguments on the call to traj.match.

evals number of function and gradient evaluations by the optimizer. See optim.

**value** value of the objective function. Larger values indicate better fit (i.e., traj.match attempts to maximize this quantity.

convergence, msg convergence code and message from the optimizer. See optim.

Available methods for objects of this type include summary and logLik. The other slots of this object can be accessed via the \$ operator.

traj.match.objfun returns a function suitable for use as an objective function in an optim-like optimizer.

#### See Also

```
trajectory, pomp, optim, subplex
```

## **Examples**

```
pompExample(ou2)
true.p <- c(
    alpha.1=0.9, alpha.2=0, alpha.3=-0.4, alpha.4=0.99,
    sigma.1=2, sigma.2=0.1, sigma.3=2,
    tau=1,
            x1.0=50,x2.0=-50
    )
simdata <- simulate(ou2,nsim=1,params=true.p,seed=43553)</pre>
guess.p <- true.p</pre>
res <- traj.match(</pre>
  simdata,
  start=guess.p,
  est=c(alpha.1,alpha.3,alpha.4,x1.0,x2.0,tau),
  maxit=2000,
  method="Nelder-Mead",
  reltol=1e-8
summary(res)
plot(range(time(res)),range(c(obs(res),states(res))),type=n,xlab="time",ylab="x,y")
points(y1~time,data=as(res,"data.frame"),col=blue)
points(y2~time,data=as(res,"data.frame"),col=red)
lines(x1~time,data=as(res,"data.frame"),col=blue)
lines(x2~time,data=as(res,"data.frame"),col=red)
pompExample(ricker)
ofun <- traj.match.objfun(ricker,est=c("r","phi"),transform=TRUE)</pre>
optim(fn=ofun,par=c(2,0),method="BFGS")
pompExample(bbs)
## some options are passed to the ODE integrator
ofun <- traj.match.objfun(bbs,est=c("beta","gamma"),transform=TRUE,hmax=0.001,rtol=1e-6)
optim(fn=ofun,par=c(0,-1),method="Nelder-Mead",control=list(reltol=1e-10))
```

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