# Package 'pomp'

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**Description** Inference methods for partially-observed Markov processes

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**License** GPL(>= 2)

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### **Description**

The **pomp** package provides facilities for inference on time series data using partially-observed Markov processes (AKA state-space models or nonlinear stochastic dynamical systems). One can use **pomp** to fit nonlinear, non-Gaussian dynamic models to time-series data. The first step in using **pomp** is to encode one's model and data in an object of class pomp. One does this via a call to pomp, which involves specifying the process and measurement components of the model in one or more of a variety of ways. Details on this are given in the documentation for the pomp function and examples are given in the 'intro\_to\_pomp' vignette.

Currently, **pomp** provides algorithms for (i) simulation of stochastic dynamical systems (see simulate), (ii) particle filtering (AKA sequential Monte Carlo or sequential importance sampling), see pfilter), (iii) the iterated filtering method of Ionides et al. (2006), see mif), (iv) the nonlinear forecasting algorithm of Kendall et al. (2005), see nlf), (v) the particle MCMC approach of Andrieu et al. (2010), see pmcmc, (vi) basic trajectory matching, see traj.match, (vi) the probe-matching method of Wood (2010) and Kendall et al. (1999), see probe.match, (vii) a spectral probe-matching method (Reuman et al., 2006), see spect.match. See the package website http://pomp.r-forge.r-project.org for these references. The package also provides various tools for plotting and extracting information on models and data as well as an API for algorithm development. Future support for additional algorithms in envisioned, and implementations of the Bayesian sequential Monte Carlo approach of Liu & West. Much of the work in **pomp** has been done under the auspices of a working group of the National Center for Ecological Analysis and Synthesis (NCEAS), "Inference for Mechanistic Models".

The package is provided under the GNU Public License (GPL). Contributions are welcome, as are comments, suggestions for improvements, and bug reports. See the package website <a href="http://pomp.r-forge.r-project.org">http://pomp.r-forge.r-project.org</a> for more information, access to the package mailing list, links to the authors' websites, and references to the literature.

# Classes

**pomp** makes extensive use of S4 classes. The basic class, pomp, encodes a partially-observed Markov process together with a uni- or multi-variate data set and (possibly) parameters.

# Vignettes

The vignette 'Introduction to pomp' illustrates the facilities of the package using familiar stochastic processes. Run vignette("intro\_to\_pomp") or look at the HTML documentation to view the vignette. Methods for accelerating your codes are discussed in the 'Advanced topics in pomp' vignette; run vignette("advanced\_topics\_in\_pomp") to view it.

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp, pfilter, simulate, trajectory, mif, nlf, probe.match, traj.match, bsmc, pmcmc

B-splines

# **Description**

These functions generate B-spline basis functions. bspline.basis gives a basis of spline functions. periodic.bspline.basis gives a basis of periodic spline functions.

# Usage

```
bspline.basis(x, nbasis, degree = 3, names = NULL)
periodic.bspline.basis(x, nbasis, degree = 3, period = 1, names = NULL)
```

# Arguments

X	Vector at which the spline functions are to be evaluated.
nbasis	The number of basis functions to return.
degree	Degree of requested B-splines.
period	The period of the requested periodic B-splines.
names	optional; the names to be given to the basis functions. These will be the column names of the matrix returned. If the names are specified as a format string (e.g., "basis%d"), sprintf will be used to generate the names from the column

names of the matrix returned. If the names are specified as a format string (e.g., "basis%d"), sprintf will be used to generate the names from the column number. If a single non-format string is specified, the names will be generated by paste-ing name to the column number. One can also specify each column name explicitly by giving a length-nbasis string vector. By default, no columnnames are given.

# **Details**

Direct access to the underlying C routines is available. See the header file "pomp.h" for details.

#### Value

```
bspline.basis Returns a matrix with length(x) rows and nbasis columns. Each column contains the values one of the spline basis functions.
```

periodic.bspline.basis

Returns a matrix with length(x) rows and nbasis columns. The basis functions returned are periodic with period period.

# Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

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# **Examples**

```
x <- seq(0,2,by=0.01)
y <- bspline.basis(x,degree=3,nbasis=9,names="basis")
matplot(x,y,type='1',ylim=c(0,1.1))
lines(x,apply(y,1,sum),lwd=2)

x <- seq(-1,2,by=0.01)
y <- periodic.bspline.basis(x,nbasis=5,names="spline%d")
matplot(x,y,type='1')</pre>
```

basic.probes

Some probes for partially-observed Markov processes

# **Description**

Several simple and configurable probes are provided in the package. These can be used directly and as examples for building custom probes.

## Usage

# Arguments

var, vars character; the name(s) of the observed variable(s).

trim the fraction of observations to be trimmed (see mean).

transform transformation to be applied to the data before the probe is computed.

na.rm if TRUE, remove all NA observations prior to computing the probe.

kernel.width width of modified Daniell smoothing kernel to be used in power-spectrum com-

putation: see kernel.

prob a single probability; the quantile to compute: see quantile.

lags In probe.ccf, a vector of lags between time series. Positive lags correspond to

x advanced relative to y; negative lags, to the reverse.

In probe.nlar, a vector of lags present in the nonlinear autoregressive model that will be fit to the actual and simulated data. See Details, below, for a precise

description.

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powers the powers of each term (corresponding to lags) in the the nonlinear autoregres-

sive model that will be fit to the actual and simulated data. See Details, below,

for a precise description.

type Compute autocorrelation or autocovariance?

ref empirical reference distribution. Simulated data will be regressed against the

values of ref, sorted and, optionally, differenced. The resulting regression coefficients capture information about the shape of the marginal distribution. A

good choice for ref is the data itself.

order order of polynomial regression.
diff order of differencing to perform.

... Additional arguments to be passed through to the probe computation.

#### **Details**

Each of these functions is relatively simple. See the source code for a complete understanding of what each does.

probe.mean, probe.median, probe.var, probe.sd return functions that compute the mean, median, variance, and standard deviation of variable var, respectively.

probe.period returns a function that estimates the period of the Fourier component of the var series with largest power.

probe.marginal returns a function that regresses the marginal distribution of variable var against the reference distribution ref. If diff>0, the data and the reference distribution are first differenced diff times and centered. Polynomial regression of order order is used. This probe returns order regression coefficients (the intercept is zero).

probe.nlar returns a function that fit a nonlinear (polynomial) autoregressive model to the univariate series (variable var). Specifically, a model of the form  $y_t = \sum \beta_k y_{t-\tau_k}^{p_k} + \epsilon_t$  will be fit, where  $\tau_k$  are the lags and  $p_k$  are the powers. The data are first centered. This function returns the regression coefficients,  $\beta_k$ .

probe.acf returns a function that, if type=="covariance", computes the autocovariance of variable var at lags lags; if type=="correlation", computes the autocorrelation of variable var at lags lags.

probe.ccf returns a function that, if type=="covariance", computes the cross covariance of the two variables named in vars at lags lags; if type=="correlation", computes the cross correlation.

probe.quantile returns a function that estimates the prob-th quantile of variable var.

## Value

A call to any one of these functions returns a probe function, suitable for use in probe or probe.match. That is, the function returned by each of these takes a data array (such as comes from a call to obs) as input and returns a single numerical value.

#### Author(s)

Daniel C. Reuman (d.reuman at imperial dot ac dot uk)

Aaron A. King (kingaa at umich dot edu)

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### References

B. E. Kendall, C. J. Briggs, W. M. Murdoch, P. Turchin, S. P. Ellner, E. McCauley, R. M. Nisbet, S. N. Wood Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches, Ecology, 80:1789–1805, 1999.

S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems, Nature, 466: 1102–1104, 2010.

#### See Also

pomp-class, pomp-methods

blowflies

Model for Nicholson's blowflies.

### **Description**

blowflies1 and blowflies2 are pomp objects encoding stochastic delay-difference models.

# Usage

data(blowflies)

#### **Details**

The data are from "population I", a control culture in one of A. J. Nicholson's experiments with the Australian sheep-blowfly *Lucilia cuprina*. The experiment is described on pp. 163–4 of Nicholson (1957). Unlimited quantities of larval food were provided; the adult food supply (ground liver) was constant at 0.4g per day. The data were taken from the table provided by Brillinger et al. (1980).

# References

- A. J. Nicholson (1957) The self-adjustment of populations to change. Cold Spring Harbor Symposia on Quantitative Biology, **22**, 153–173.
- Y. Xia and H. Tong (2011) Feature Matching in Time Series Modeling. *Statistical Science* **26**, 21–46.
- E. L. Ionides (2011) Discussion of "Feature Matching in Time Series Modeling" by Y. Xia and H. Tong. *Statistical Science* **26**, 49–52.
- S. N. Wood (2010) Statistical inference for noisy nonlinear ecological dynamic systems. *Nature* **466**, 1102–1104.
- W. S. C. Gurney, S. P. Blythe, and R. M. Nisbet (1980) Nicholson's blowflies revisited. *Nature* **287**, 17–21.
- D. R. Brillinger, J. Guckenheimer, P. Guttorp and G. Oster (1980) Empirical modelling of population time series: The case of age and density dependent rates. in G. Oster (ed.), Some Questions in Mathematical Biology, vol. 13, pp. 65–90. American Mathematical Society, Providence.

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# See Also

```
pomp-class and the vignettes
```

# **Examples**

```
data(blowflies)
plot(blowflies1)
plot(blowflies2)
```

bsmc

Liu and West Bayesian Particle Filter

# Description

Generates draws from the posterior distribution for the parameters using the Liu and West algorithm. bsmc gives draws from the posterior.

# Usage

```
## S4 method for signature 'pomp'
bsmc(object, params, Np, est, smooth = 0.1,
    ntries = 1, tol = 1e-17, lower = -Inf, upper = Inf, seed = NULL,
    verbose = getOption("verbose"), max.fail = 0,
    transform = FALSE, ...)
```

# Arguments

ntries

rguments		
object	An object of class pomp or inheriting class pomp.	
params	A npars x Np matrix (with rownames) containing the parameters corresponding to the initial state values in xstart. Np is the number of particles, i.e., each row should contain Np draws from the prior distribution for that parameter. It is permissible to supply params as a named numeric vector, i.e., without a dim attribute. In this case, all particles will inherit the same parameter values, which is equivalent to a degenerate prior.	
Np	If params is specified as a named vector, Np specifies the number of particles to use. If params is specified as a matrix, Np should not be specified; it is taken to be the number of columns of params.	
est	Names of the rows of params that are to be estimated. No updates will be made to the other parameters. If est is not specified, all parameters for which there is variation in params will be estimated.	
smooth	Kernel density smoothing parameters. The compensating shrinkage factor will be sqrt(1-smooth^2). Thus, smooth=0 means that no noise will be added to parameters. Generally, the value of smooth should be chosen close to 0 (i.e., shrink~0.1).	

Number of draws from rprocess per particle used to estimate the expected

value of the state process at time t+1 given the state and parameters at time t.

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tol Particles with log likelihood below tol are considered to be "lost". A filtering

failure occurs when, at some time point, all particles are lost. When all particles are lost, the conditional log likelihood at that time point is set to be log(tol).

lower, upper optional; lower and upper bounds on the priors. This is useful in case there are

box constraints satisfied by the priors. The posterior is guaranteed to lie within

these bounds.

seed optional; an object specifying if and how the random number generator should

be initialized ('seeded'). If seed is an integer, it is passed to set.seed prior to any simulation and is returned as the "seed" element of the return list. By default, the state of the random number generator is not changed and the value of .Random.seed on the call is stored in the "seed" element of the return list.

verbose logical; if TRUE, print diagnostic messages.

max.fail The maximum number of filtering failures allowed. If the number of filtering

failures exceeds this number, execution will terminate with an error.

transform logical; if TRUE, the algorithm operates on the transformed scale.

... currently ignored.

#### Value

An object of class "bsmcd.pomp". The slots of this class include:

post A matrix containing draws from the approximate posterior distribution.

prior A matrix containing draws from the prior distribution (identical to params on

call).

eff.sample.size

A vector containing the effective number of particles at each time point.

smooth The smoothing parameter used (see above).

seed The state of the random number generator at the time bsmc was called. If the

argument seed was specified, this is a copy; if not, this is the internal state of

the random number generator at the time of call.

nfail The number of filtering failures encountered.

cond.log.evidence

A vector containing the conditional log evidence scores at each time point.

log.evidence The estimated log evidence.

weights The resampling weights for each particle.

## Author(s)

Michael Lavine (lavine at math dot umass dot edu), Matthew Ferrari (mferrari at psu dot edu), Aaron A. King

# See Also

pomp-class

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# **Examples**

## See the vignettes for examples.

dacca

Model of cholera transmission for historic Bengal.

# **Description**

dacca is a pomp object containing census and cholera mortality data from the Dacca district of the former British province of Bengal over the years 1891 to 1940 together with a stochastic differential equation transmission model. The model is that of King et al. (2008). The parameters are the MLE for the SIRS model with seasonal reservoir.

Data are provided courtesy of Dr. Menno J. Bouma, London School of Tropical Medicine and Hygiene.

# Usage

```
data(dacca)
```

#### **Details**

dacca is a pomp object containing the model, data, and MLE parameters. Parameters that naturally range over the positive reals are log-transformed; parameters that range over the unit interval are logit-transformed; parameters that are naturally unbounded or take integer values are not transformed.

#### References

King, A. A., Ionides, E. L., Pascual, M., and Bouma, M. J. Inapparent infections and cholera dynamics. Nature 454:877-880 (2008)

# See Also

```
euler.sir, pomp
```

# **Examples**

```
data(dacca)
plot(dacca)
#MLEs on the natural scale
coef(dacca)
#MLEs on the transformed scale
coef(dacca,transform=TRUE)
plot(simulate(dacca))
# now change 'eps' and simulate again
coef(dacca,"eps") <- 1
plot(simulate(dacca))</pre>
```

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Euler-multinomial death process

#### **Description**

Density and random-deviate generation for the Euler-multinomial death process with parameters size, rate, and dt.

# Usage

```
reulermultinom(n = 1, size, rate, dt)
deulermultinom(x, size, rate, dt, log = FALSE)
rgammawn(n = 1, sigma, dt)
```

# **Arguments**

n	integer; number of random variates to generate.
size	scalar integer; number of individuals at risk.
rate	numeric vector of hazard rates.
sigma	numeric scalar; intensity of the Gamma white noise process.
dt	numeric scalar; duration of Euler step.
X	matrix or vector containing number of individuals that have succumbed to each death process.
log	logical; if TRUE, return logarithm(s) of probabilities.

#### **Details**

If N individuals face constant hazards of death in k ways at rates  $r_1, r_2, \ldots, r_k$ , then in an interval of duration  $\Delta t$ , the number of individuals remaining alive and dying in each way is multinomially distributed:

$$(N - \sum_{i=1}^{k} \Delta n_i, \Delta n_1, \dots, \Delta n_k) \sim \text{multinomial}(N; p_0, p_1, \dots, p_k),$$

where  $\Delta n_i$  is the number of individuals dying in way i over the interval, the probability of remaining alive is  $p_0 = \exp(-\sum_i r_i \Delta t)$ , and the probability of dying in way j is

$$p_j = \frac{r_j}{\sum_i r_i} (1 - \exp(-\sum_i r_i \Delta t)).$$

In this case, we can say that

$$(\Delta n_1, \ldots, \Delta n_k) \sim \text{eulermultinom}(N, r, \Delta t),$$

where  $r=(r_1,\ldots,r_k)$ . Draw m random samples from this distribution by doing dn <- reulermultinom(n=m,size=N,rate=r,dt=dt),

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where r is the vector of rates. Evaluate the probability that  $x = (x_1, ..., x_k)$  are the numbers of individuals who have died in each of the k ways over the interval  $\Delta t = dt$ , by doing

```
deulermultinom(x=x,size=N,rate=r,dt=dt).
```

Breto & Ionides discuss how an infinitesimally overdispersed death process can be constructed by compounding a binomial process with a Gamma white noise process. The Euler approximation of the resulting process can be obtained as follows. Let the increments of the equidispersed process be given by

```
reulermultinom(size=N,rate=r,dt=dt).
```

In this expression, replace the rate r with  $r\Delta W/\Delta t$ , where  $\Delta W^{\sim}Gamma(dt/\sigma^2,\sigma^2)$  is the increment of an integrated Gamma white noise process with intensity  $\sigma$ . That is,  $\Delta W$  has mean  $\Delta t$  and variance  $\sigma^2\Delta t$ . The resulting process is overdispersed and converges (as  $\Delta t$  goes to zero) to a well-defined process. The following lines of R code accomplish this:

```
dW <- rgammawn(sigma=sigma,dt=dt)
dn <- reulermultinom(size=N,rate=r,dt=dW)
or
dn <- reulermultinom(size=N,rate=r*dW/dt,dt=dt).</pre>
```

He et al. use such overdispersed death processes in modeling measles.

For all of the functions described here, direct access to the underlying C routines is available: see the header file "pomp.h", included with the package.

#### Value

reulermultinom Returns a length(rate) by n matrix. Each column is a different random draw. Each row contains the numbers of individuals succumbed to the corresponding process.

deulermultinom Returns a vector (of length equal to the number of columns of x) containing

the probabilities of observing each column of x given the specified parameters (size, rate, dt).

Returns a vector of length n containing random increments of the integrated Gamma white noise process with intensity sigma.

# Author(s)

rgammawn

Aaron A. King <kingaa at umich dot edu>

### References

C. Bret\'o & E. L. Ionides, Compound Markov counting processes and their applications to modeling infinitesimally over-dispersed systems. Stoch. Proc. Appl., 121:2571–2591, 2011.

D. He, E. L. Ionides, & A. A. King, Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. J. R. Soc. Interface, 7:271–283, 2010.

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# **Examples**

```
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=0.1))
deulermultinom(x=dn,size=100,rate=c(1,2,3),dt=0.1)
## an Euler-multinomial with overdispersed transitions:
dt <- 0.1
dW <- rgammawn(sigma=0.1,dt=dt)
print(dn <- reulermultinom(5,size=100,rate=c(a=1,b=2,c=3),dt=dW))</pre>
```

gompertz

Gompertz model with log-normal observations.

# **Description**

gompertz is a pomp object encoding a stochastic Gompertz population model with log-normal measurement error.

# Usage

```
data(gompertz)
```

## **Details**

The state process is  $X_{t+1} = K^{(1-S)} X_t^S \varepsilon_t$ , where  $S = e^{-r}$  and the  $\varepsilon_t$  are i.i.d. lognormal random deviates with variance  $\sigma^2$ . The observed variables  $Y_t$  are distributed as  $\log (\log X_t, \tau)$ . Parameters include the per-capita growth rate r, the carrying capacity K, the process noise s.d. sigma, the measurement error s.d. tau, and the initial condition  $X_0$ . The model is parameterized internally by the logarithms of r, K,  $\sigma$ , and  $\tau$ ; the initial condition is parameterized directly. The pomp object includes parameter transformations to and from this internal parameterization.

#### See Also

```
pomp-class and the introductory vignette vignette("intro_to_pomp").
```

# **Examples**

```
data(gompertz)
plot(gompertz)
coef(gompertz)
coef(gompertz,transform=TRUE)
```

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LondonYorke

Historical childhood disease incidence data

# Description

LondonYorke is a data-frame containing the monthly number of reported cases of chickenpox, measles, and mumps from two American cities (Baltimore and New York) in the mid-20th century (1928–1972).

# Usage

```
data(LondonYorke)
```

#### References

W. P. London and J. A. Yorke, Recurrent Outbreaks of Measles, Chickenpox and Mumps: I. Seasonal Variation in Contact Rates, American Journal of Epidemiology, 98:453–468, 1973.

#### See Also

```
pomp-class and the vignettes
```

# **Examples**

```
data(LondonYorke)
plot(cases~time,data=LondonYorke,subset=disease=="measles",type='n',main="measles",bty='l')
lines(cases~time,data=LondonYorke,subset=disease=="measles"&town=="Baltimore",col="red")
lines(cases~time,data=LondonYorke,subset=disease=="measles"&town=="New York",col="blue")
legend("topright",legend=c("Baltimore","New York"),lty=1,col=c("red","blue"),bty='n')
plot(
     cases~time,
     data=LondonYorke,
     subset=disease=="chickenpox"&town=="New York",
     type='l',col="blue",main="chickenpox, New York",
    bty='l'
    )
plot(
     cases~time,
     data=LondonYorke,
     subset=disease=="mumps"&town=="New York",
     type='l',col="blue",main="mumps, New York",
    bty='l'
    )
```

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mif

The MIF algorithm

# **Description**

The MIF algorithm for estimating the parameters of a partially-observed Markov process.

# Usage

```
mif(object, ...)
## S4 method for signature 'pomp'
mif(object, Nmif = 1, start, pars, ivps = character(0),
    particles, rw.sd, Np, ic.lag, var.factor, cooling.factor,
    weighted, method = c("mif", "unweighted", "fp"),
    tol = 1e-17, max.fail = 0,
    verbose = getOption("verbose"), transform = FALSE, ...)
## S4 method for signature 'pfilterd.pomp'
mif(object, Nmif = 1, start, pars, ivps = character(0),
    particles, rw.sd, Np, ic.lag, var.factor, cooling.factor,
    weighted, method = c("mif", "unweighted", "fp"),
    tol, \max.fail = 0,
    verbose = getOption("verbose"), transform = FALSE, ...)
## S4 method for signature 'mif'
mif(object, Nmif, start, pars, ivps,
    particles, rw.sd, Np, ic.lag, var.factor, cooling.factor,
    weighted, method = c("mif", "unweighted", "fp"),
    tol, \max.fail = 0,
    verbose = getOption("verbose"), transform, ...)
## S4 method for signature 'mif'
continue(object, Nmif = 1, start, pars, ivps,
    particles, rw.sd, Np, ic.lag, var.factor, cooling.factor,
    weighted, method = c("mif", "unweighted", "fp"),
    tol, max.fail = 0, verbose = getOption("verbose"),
    transform, ...)
```

#### **Arguments**

object An object of class pomp.

Nmif The number of MIF iterations to perform.

start named numerical vector; the starting guess of the parameters.

pars optional character vector naming the ordinary parameters to be estimated. Every parameter named in pars must have a positive random-walk standard deviation specified in rw. sd. Leaving pars unspecified is equivalent to setting it equal to

the names of all parameters with a positive value of rw.sd that are not ivps.

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ivps

optional character vector naming the initial-value parameters (IVPs) to be estimated. Every parameter named in ivps must have a positive random-walk standard deviation specified in rw. sd. If pars is empty, i.e., only IVPs are to be estimated, see below ""Using MIF to estimate initial-value parameters only"".

particles

Function of prototype particles(Np,center,sd,...) which sets up the starting particle matrix by drawing a sample of size Np from the starting particle distribution centered at center and of width sd. If particles is not supplied by the user, the default behavior is to draw the particles from a multivariate normal distribution with mean center and standard deviation sd.

rw.sd

numeric vector with names; the intensity of the random walk to be applied to parameters. The random walk is only applied to parameters named in pars (i.e., not to those named in ivps). The algorithm requires that the random walk be nontrivial, so each element in rw.sd[pars] must be positive. rw.sd is also used to scale the initial-value parameters (via the particles function). Therefore, each element of rw.sd[ivps] must be positive. The following must be satisfied: names(rw.sd) must be a subset of names(start), rw.sd must be non-negative (zeros are simply ignored), the name of every positive element of rw.sd must be in either pars or ivps.

Np

the number of particles to use in filtering. This may be specified as a single positive integer, in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timestep, one may specify Np either as a vector of positive integers (of length length(time(object,t0=TRUE))) or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object,t0=TRUE)), Np(T) is the number of particles to sample at the end of the time-series.

ic.lag

a positive integer; the timepoint for fixed-lag smoothing of initial-value parameters. The mif update for initial-value parameters consists of replacing them by their filtering mean at time times[ic.lag], where times=time(object). It makes no sense to set ic.lag>length(times); if it is so set, ic.lag is set to length(times) with a warning.

var.factor

a positive number; the scaling coefficient relating the width of the starting particle distribution to rw.sd. In particular, the width of the distribution of particles at the start of the first MIF iteration will be random.walk.sd\*var.factor.

cooling.factor a positive number not greater than 1; the exponential cooling factor, alpha. method, weighted

method sets the update rule used in the algorithm. method="mif" uses the iterated filtering update rule (Ionides 2006, 2011); method="unweighted" updates the parameter to the unweighted average of the filtering means of the parameters at each time; method="fp" updates the parameter to the filtering mean at the end of the time series. weighted is logical. This argument is deprecated and will be removed in a future release. weighted=TRUE is equivalent to method="mif"; weighted=FALSE is equivalent to method="unweighted".

mif 17

numeric scalar; particles with log likelihood below tol are considered to be "lost". A filtering failure occurs when, at some time point, all particles are lost.

max.fail integer; maximum number of filtering failures permitted. If the number of failures exceeds this number, execution will terminate with an error.

verbose logical; if TRUE, print progress reports.

transform logical; if TRUE, optimization is performed on the transformed scale.

additional arguments. Currently, these are ignored.

# **Re-running MIF Iterations**

To re-run a sequence of MIF iterations, one can use the mif method on a mif object. By default, the same parameters used for the original MIF run are re-used (except for weighted, tol, max.fail, and verbose, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

# **Continuing MIF Iterations**

One can resume a series of MIF iterations from where one left off using the continue method. A call to mif to perform Nmif=miterations followed by a call to continue to perform Nmif=n iterations will produce precisely the same effect as a single call to mif to perform Nmif=m+n iterations. By default, all the algorithmic parameters are the same as used in the original call to mif. Additional arguments will override the defaults.

# Using MIF to estimate initial-value parameters only

One can use MIF's fixed-lag smoothing to estimate only initial value parameters (IVPs). In this case, pars is left empty and the IVPs to be estimated are named in ivps. If theta is the current parameter vector, then at each MIF iteration, Np particles are drawn from a distribution centered at theta and with width proportional to var.factor\*rw.sd, a particle filtering operation is performed, and theta is replaced by the filtering mean at time(object)[ic.lag]. Note the implication that, when mif is used in this way on a time series any longer than ic.lag, unnecessary work is done. If the time series in object is longer than ic.lag, consider replacing object with window(object,end=ic.lag).

#### **Details**

If particles is not specified, the default behavior is to draw the particles from a multivariate normal distribution. It is the user's responsibility to ensure that, if the optional particles argument is given, that the particles function satisfies the following conditions:

particles has at least the following arguments: Np, center, sd, and . . . . Np may be assumed to be a positive integer; center and sd will be named vectors of the same length. Additional arguments may be specified; these will be filled with the elements of the userdata slot of the underlying pomp object (see pomp-class).

particles returns a length(center) x Np matrix with rownames matching the names of center and sd. Each column represents a distinct particle.

The center of the particle distribution returned by particles should be center. The width of the particle distribution should vary monotonically with sd. In particular, when sd=0, the particles should return matrices with Np identical columns, each given by the parameters specified in center.

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# Author(s)

Aaron A. King <kingaa at umich dot edu>

#### References

E. L. Ionides, C. Bretl'o, & A. A. King, Inference for nonlinear dynamical systems, Proc. Natl. Acad. Sci. U.S.A., 103:18438–18443, 2006.

E. L. Ionides, A. Bhadra, Y. Atchad\'e, & A. A. King, Iterated filtering, Annals of Statistics, 39:1776–1802, 2011.

A. A. King, E. L. Ionides, M. Pascual, and M. J. Bouma, Inapparent infections and cholera dynamics, Nature, 454:877–880, 2008.

#### See Also

mif-methods, pomp, pomp-class, pfilter. See the "intro\_to\_pomp" vignette for examples.

mif-methods

Methods of the "mif" class

# **Description**

Methods of the "mif" class.

# Usage

```
## S4 method for signature 'mif'
logLik(object, ...)
## S4 method for signature 'mif'
conv.rec(object, pars, transform = FALSE, ...)
## S4 method for signature 'mif'
plot(x, y = NULL, ...)
compare.mif(z)
```

## **Arguments**

object	The mif object.
pars	Names of parameters.
x	The mif object.
У	Ignored.
z	A mif object or list of mif objects.
transform	optional logical; should the parameter transformations be applied? See coef for details.
	Further arguments (either ignored or passed to underlying functions).

nlf

# Methods

conv.rec conv.rec(object, pars = NULL) returns the columns of the convergence-record matrix corresponding to the names in pars. By default, all rows are returned.

logLik Returns the value in the loglik slot.

mif Re-runs the MIF iterations. See the documentation for mif.

**compare.mif** Given a mif object or a list of mif objects, compare.mif produces a set of diagnostic plots.

plot Plots a series of diagnostic plots. When x is a mif object, plot(x) is equivalent to compare.mif(list(x)).

predvarplot predvarplot(object, pars = NULL, mean = FALSE, ...) produces a plot of
 the scaled prediction variances for each parameter. This can be used to diagnose a good value
 of the mif parameters var.factor and ic.lag. If used in this way, one should run mif with
 Nmif=1 first. Additional arguments in ... will be passed to the actual plotting function.

**print** Prints a summary of the mif object.

show Displays the mif object.

# Author(s)

Aaron A. King <kingaa at umich dot edu>

#### References

E. L. Ionides, C. Bret\'o, & A. A. King, Inference for nonlinear dynamical systems, Proc. Natl. Acad. Sci. U.S.A., 103:18438–18443, 2006.

A. A. King, E. L. Ionides, M. Pascual, and M. J. Bouma, Inapparent infections and cholera dynamics, Nature, 454:877–880, 2008.

#### See Also

mif, pomp, pomp-class, pfilter

nlf

Fit Model to Data Using Nonlinear Forecasting (NLF)

# **Description**

Calls an optimizer to maximize the nonlinear forecasting (NLF) goodness of fit, by simulating data from a model, fitting a nonlinear autoregressive model to the simulated time series (which may be multivariate) and using the fitted model to predict some or all variables in the data time series. NLF is an 'indirect inference' method using a quasi-likelihood as the objective function.

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# Usage

```
nlf(object, start, est, lags, period = NA, tensor = FALSE,
    nconverge=1000, nasymp=1000, seed = 1066,
    transform = identity,
    nrbf = 4, method = "subplex", skip.se = FALSE,
    verbose = FALSE, gr = NULL,
    bootstrap=FALSE, bootsamp = NULL,
    lql.frac = 0.1, se.par.frac = 0.1, eval.only = FALSE,
    transform.params = FALSE, ...)
```

#### **Arguments**

object A pomp object, with the data and model to fit to it.
start Named numeric vector with guessed parameters.

est Vector containing the names or indices of parameters to be estimated.

lags A vector specifying the lags to use when constructing the nonlinear autoregres-

sive prediction model. The first lag is the prediction interval.

period numeric; period=NA means the model is nonseasonal. period>0 is the period of

seasonal forcing in 'real time'.

tensor logical; if FALSE, the fitted model is a generalized additive model with time

mod period as one of the predictors, i.e., a gam with time-varying intercept. If TRUE, the fitted model is a gam with lagged state variables as predictors and time-periodic coefficients, constructed using tensor products of basis functions

of state variables with basis functions of time.

nconverge Number of convergence timesteps to be discarded from the model simulation.

nasymp Number of asymptotic timesteps to be recorded from the model simulation.

seed Integer specifying the random number seed to use. When fitting, it is usually

best to always run the simulations with the same sequence of random numbers, which is accomplished by setting seed to an integer. If you want a truly random

simulation, set seed=NULL.

transform optional function. If specified, forecasting is performed using data and model

simulations transformed by this function. By default, transform is the identity function, i.e., no transformation is performed. The main purpose of transform is to achieve approximately multivariate normal forecasting errors. If data are univariate, transform should take a scalar and return a scalar. If data are multivariate, transform should assume a vector input and return a vector of the same

length.

nrbf A scalar specifying the number of radial basis functions to be used at each lag.

method Optimization method. Choices are subplex and any of the methods used by

optim.

skip.se Logical; if TRUE, skip the computation of standard errors.

verbose Logical; if TRUE, the negative log quasilikelihood and parameter values are

printed at each iteration of the optimizer.

gr optional; passed to optim if optim is used.

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bootstrap	Logical; if TRUE the indices in bootsamp will determine which of the conditional likelihood values be used in computing the quasi-loglikelihood.	
bootsamp	Vector of integers; used to have the quasi-loglikelihood evaluated using a bootstrap re-sampling of the data set.	
lql.frac	target fractional change in log quasi-likelihood for quadratic standard error estimate	
se.par.frac	initial parameter-change fraction for quadratic standard error estimate	
eval.only	logical; if TRUE, no optimization is attempted and the quasi-loglikelihood value is evaluated at the start parameters.	
transform.params		
	logical; if TRUE, parameters are optimized on the transformed scale.	

# Details

. . .

This is functionally a wrapper for nlf.objfun, which does the statistical heavy lifting and should be consulted for details.

Arguments that will be passed to optim or subplex in the control list.

# Value

A list corresponding to the output from the optimizer, except that the full parameter vector is returned (not just the ones fitted), the log quasilikelihood (LQL) (*not* -LQL) is reported, xstart is included, and asymptotic Wald standard errors based on M-estimator theory are returned for each fitted parameter.

#### Author(s)

Stephen P. Ellner <spe2 at cornell dot edu> and Bruce E. Kendall <kendall at bren dot ucsb dot edu>

#### References

The following papers describe and motivate the NLF approach to model fitting:

Ellner, S. P., Bailey, B. A., Bobashev, G. V., Gallant, A. R., Grenfell, B. T. and Nychka D. W. (1998) Noise and nonlinearity in measles epidemics: combining mechanistic and statistical approaches to population modeling. *American Naturalist* **151**, 425–440.

Kendall, B. E., Briggs, C. J., Murdoch, W. W., Turchin, P., Ellner, S. P., McCauley, E., Nisbet, R. M. and Wood S. N. (1999) Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches. *Ecology* **80**, 1789–1805. Available online at http://www2.bren.ucsb.edu/~kendall/pubs/1999Ecology.pdf

Kendall, B. E., Ellner, S. P., McCauley, E., Wood, S. N., Briggs, C. J., Murdoch, W. W. and Turchin, P. (2005) Population cycles in the pine looper moth (*Bupalus piniarius*): dynamical tests of mechanistic hypotheses. *Ecological Monographs* **75**, 259–276. Available online at http://repositories.cdlib.org/postprints/818/

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ou2

Two-dimensional discrete-time Ornstein-Uhlenbeck process

# Description

ou2 is a pomp object encoding a bivariate discrete-time Ornstein-Uhlenbeck process.

# Usage

data(ou2)

#### **Details**

If the state process is  $X(t) = (x_1(t), x_2(t))$ , then

$$X(t+1) = \alpha X(t) + \sigma \epsilon(t),$$

where  $\alpha$  and  $\sigma$  are 2x2 matrices,  $\sigma$  is lower-triangular, and  $\epsilon(t)$  is standard bivariate normal. The observation process is  $Y(t)=(y_1(t),y_2(t))$ , where  $y_i(t)\sim \operatorname{normal}(x_i(t),\tau)$ . The functions rprocess, dprocess, rmeasure, dmeasure, and skeleton are implemented using compiled C code for computational speed: see the source code for details. This object is demonstrated in the vignette "Advanced topics in pomp".

# See Also

pomp and the vignettes

# **Examples**

```
data(ou2)
plot(ou2)
coef(ou2)
x <- simulate(ou2)
plot(x)
pf <- pfilter(ou2,Np=1000)
logLik(pf)</pre>
```

parmat

Create a matrix of parameters

# **Description**

parmat is a utility that makes a vector of parameters suitable for use in **pomp** functions.

#### **Usage**

```
parmat(params, nrep = 1)
```

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## **Arguments**

params named numeric vector or matrix of parameters.

nrep number of replicates (columns) desired.

# Value

parmat returns a matrix consisting of nrep copies of params.

## Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

# **Examples**

```
## generate a bifurcation diagram for the Ricker map
data(ricker)
p <- parmat(coef(ricker),nrep=500)
p["log.r",] <- seq(from=1.5,to=4,length=500)
x <- trajectory(ricker,times=seq(from=1000,to=2000,by=1),params=p)
matplot(p["log.r",],x["N",,],pch='.',col='black',xlab="log(r)",ylab="N")</pre>
```

pfilter

Particle filter

# **Description**

Run a plain vanilla particle filter. Resampling is performed at each observation.

# Usage

```
## S4 method for signature 'pomp'
pfilter(object, params, Np, tol = 1e-17,
    max.fail = 0, pred.mean = FALSE, pred.var = FALSE,
    filter.mean = FALSE, save.states = FALSE,
    save.params = FALSE, seed = NULL,
    verbose = getOption("verbose"), ...)
## S4 method for signature 'pfilterd.pomp'
pfilter(object, params, Np, tol,
    max.fail = 0, pred.mean = FALSE, pred.var = FALSE,
    filter.mean = FALSE, save.states = FALSE,
    save.params = FALSE, seed = NULL,
    verbose = getOption("verbose"), ...)
```

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#### **Arguments**

object An object of class pomp or inheriting class pomp.

params A npars x Np numeric matrix containing the parameters corresponding to the

initial state values in xstart. This must have a 'rownames' attribute. If it desired that all particles should share the same parameter values, one one may

supply params as a named numeric vector.

Np the number of particles to use. This may be specified as a single positive integer,

in which case the same number of particles will be used at each timestep. Alternatively, if one wishes the number of particles to vary across timesteps, one may

specify Np either as a vector of positive integers (of length length(time(object,t0=TRUE)))

or as a function taking a positive integer argument. In the latter case, Np(k) must be a single positive integer, representing the number of particles to be used at the k-th timestep: Np(0) is the number of particles to use going from timezero(object) to time(object)[1], Np(1), from timezero(object) to time(object)[1], and so on, while when T=length(time(object, t0=TRUE)), Np(T) is the number of particles to sample at the end of the time-series. When object is of class mif, this is by default the same number of particles used in

the mif iterations.

tol positive numeric scalar; particles with likelihood less than tol are considered to

be "lost". A filtering failure occurs when, at some time point, all particles are lost. When all particles are lost, the conditional likelihood at that time point is

set to tol.

max.fail integer; the maximum number of filtering failures allowed. If the number of

filtering failures exceeds this number, execution will terminate with an error.

pred.mean logical; if TRUE, the prediction means are calculated for the state variables and

parameters.

pred.var logical; if TRUE, the prediction variances are calculated for the state variables

and parameters.

filter.mean logical; if TRUE, the filtering means are calculated for the state variables and

parameters.

save.states, save.params

logical. If save.states=TRUE, the state-vector for each particle at each time is saved in the saved.states slot of the returned pfilterd.pomp object. If save.params=TRUE, the parameter-vector for each particle at each time is saved

in the saved.params slot of the returned pfilterd.pomp object.

seed optional; an object specifying if and how the random number generator should

be initialized ('seeded'). If seed is an integer, it is passed to set.seed prior to any simulation and is returned as the "seed" element of the return list. By default, the state of the random number generator is not changed and the value

of .Random. seed on the call is stored in the "seed" element of the return list.

verbose logical; if TRUE, progress information is reported as pfilter works.

.. Additional arguments unused at present.

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#### Value

An object of class pfilterd.pomp. This class inherits from class pomp and contains the following additional slots:

**pred.mean, pred.var, filter.mean** matrices of prediction means, variances, and filter means, respectively. In each of these, the rows correspond to states and parameters (if appropriate), in that order, the columns to successive observations in the time series contained in object.

eff.sample.size numeric vector containing the effective number of particles at each time point.

cond.loglik numeric vector containing the conditional log likelihoods at each time point.

saved.states If pfilter was called with save.states=TRUE, this is the list of state-vectors at each time point, for each particle. It is a length-ntimes list of nvars-by-Np arrays. In particular, saved.states[[t]][,i] can be considered a sample from  $f[X_t|y_{1:t}]$ .

**saved.params** If pfilter was called with save.params=TRUE, this is the list of parameter-vectors at each time point, for each particle. It is a length-ntimes list of npars-by-Np arrays. In particular, saved.params[[t]][,i] is the parameter portion of the i-th particle at time t.

**seed** the state of the random number generator at the time pfilter was called. If the argument seed was specified, this is a copy; if not, this is the internal state of the random number generator at the time of call.

**Np, tol, nfail** the number of particles used, failure tolerance, and number of filtering failures, respectively.

loglik the estimated log-likelihood.

These can be accessed using the \$ operator as if the returned object were a list. In addition, logLik returns the log likelihood. Note that if the argument params is a named vector, then these parameters are included in the params slot of the returned pfilterd.pomp object. That is coef(pfilter(obj,params=theta))==theta if theta is a named vector of parameters.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### References

M. S. Arulampalam, S. Maskell, N. Gordon, & T. Clapp. A Tutorial on Particle Filters for Online Nonlinear, Non-Gaussian Bayesian Tracking. IEEE Trans. Sig. Proc. 50:174–188, 2002.

#### See Also

pomp-class

# **Examples**

## See the vignettes for examples.

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pfilter-methods

Methods of the "pfilterd.pomp" class

# Description

Methods of the "pfilterd.pomp" class.

# Usage

```
## S4 method for signature 'pfilterd.pomp'
logLik(object, ...)
## S4 method for signature 'pfilterd.pomp'
pred.mean(object, pars, ...)
## S4 method for signature 'pfilterd.pomp'
pred.var(object, pars, ...)
## S4 method for signature 'pfilterd.pomp'
filter.mean(object, pars, ...)
```

# Arguments

object An object of class pfilterd.pomp or inheriting class pfilterd.pomp.

pars Names of parameters.

... Additional arguments unused at present.

# Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

# See Also

```
pfilter, pomp-class
```

plugins

Plug-ins for dynamical models based on stochastic Euler algorithms

# Description

Plug-in facilities for implementing discrete-time Markov processes and continuous-time Markov processes using the Euler algorithm. These can be used in the rprocess and dprocess slots of pomp.

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# Usage

```
onestep.sim(step.fun, PACKAGE)
euler.sim(step.fun, delta.t, PACKAGE)
discrete.time.sim(step.fun, delta.t = 1, PACKAGE)
gillespie.sim(rate.fun, v, d, PACKAGE)
onestep.dens(dens.fun, PACKAGE)
```

# **Arguments**

step.fun

This can be either an R function or the name of a compiled, dynamically loaded native function containing the model simulator. It should be written to take a single Euler step from a single point in state space. If it is an R function, it should be of the form step.fun(x,t,params,delta.t,...). Here, x is a named numeric vector containing the value of the state process at time t, params is a named numeric vector containing parameters, and delta.t is the length of the Euler time-step. If step.fun is the name of a native function, it must be of type "pomp\_onestep\_sim" as defined in the header "pomp.h", which is included with the **pomp** package. For details on how to write such codes, see Details.

rate.fun

This can be either an R function or the name of a compiled, dynamically loaded native function that computes the transition rates. If it is an R function, it should be of the form rate.fun(j,x,t,params,...). Here, j is the number of the event, x is a named numeric vector containing the value of the state process at time t and params is a named numeric vector containing parameters. If rate.fun is a native function, it must be of type "pomp\_ssa\_rate\_fn" as defined in the header "pomp.h", which is included with the package. For details on how to write such codes, see Details.

v, d

Matrices that specify the continuous-time Markov process in terms of its elementary events. Each should have dimensions nvar x nevent, where nvar is the number of state variables and nevent is the number of elementary events. v describes the changes that occur in each elementary event: it will usually comprise the values 1, -1, and 0 according to whether a state variable is incremented, decremented, or unchanged in an elementary event. d is a binary matrix that describes the dependencies of elementary event rates on state variables: d[i,j] will have value 1 if event rate j must be updated as a result of a change in state variable i and 0 otherwise

dens.fun

This can be either an R function or a compiled, dynamically loaded native function containing the model transition log probability density function. If it is an R function, it should be of the form dens.fun(x1,x2,t1,t2,params,...). Here, x1 and x2 are named numeric vectors containing the values of the state process at times t1 and t2, params is a named numeric vector containing parameters. If dens.fun is the name of a native function, it should be of type "pomp\_onestep\_pdf" as defined in the header "pomp.h", which is included with the **pomp** package. This function should return the log likelihood of a transition from x1 at time t1 to x2 at time t2, assuming that no intervening transitions have occurred. For details on how to write such codes, see Details.

delta.t

Size of Euler time-steps.

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**PACKAGE** 

an optional argument that specifies to which dynamically loaded library we restrict the search for the native routines. If this is "base", we search in the R executable itself.

#### **Details**

onestep.sim is the appropriate choice when it is possible to simulate the change in state from one time to another, regardless of how large the interval between them is. To use onestep.sim, you must write a function step.fun that will advance the state process from one arbitrary time to another. euler.sim is appropriate when one cannot do this but can compute the change in state via a sequence of smaller steps. This is desirable, for example, if one is simulating a continuous time process but is willing to approximate it using an Euler approach. discrete.time.sim is appropriate when the process evolves in discrete time. In this case, by default, the intervals between observations are integers.

To use euler.sim or discrete.time.sim, you must write a function step.fun that will take a single Euler step, of size at most delta.t. euler.sim and discrete.time.sim will create simulators that take as many steps as needed to get from one time to another. See below for information on how euler.sim chooses the actual step size it uses.

gillespie.sim allows exact simulation of a continuous-time, discrete-state Markov process using Gillespie's algorithm. This is an "event-driven" approach: correspondingly, to use gillespie.sim, you must write a function rate.fun that computes the rates of each elementary event and specify two matrices (d, v) that describe, respectively, the dependencies of each rate and the consequences of each event.

onestep.dens will generate a suitable dprocess function when one can compute the likelihood of a given state transition simply by knowing the states at two times under the assumption that the state has not changed between the times. This is typically possible, for instance, when the rprocess function is implemented using onestep.sim, euler.sim, or discrete.time.sim. [NB: currently, there are no high-level algorithms in **pomp** that use dprocess. This function is provided for completeness only, and with an eye toward future development.]

If step. fun is written as an R function, it must have at least the arguments x, t, params, delta.t, and .... On a call to this function, x will be a named vector of state variables, t a scalar time, and params a named vector of parameters. The length of the Euler step will be delta.t. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t, of the covariates. This is accomplished via interpolation of the covariate table. Additional arguments may be given: these will be filled by the correspondingly-named elements in the userdata slot of the pomp object (see pomp). If step. fun is written in a native language, it must be a function of type "pomp\_onestep\_sim" as specified in the header "pomp.h" included with the package (see the directory "include" in the installed package directory).

If rate.fun is written as an R function, it must have at least the arguments j, x, t, params, and .... Here, j is the an integer that indicates which specific elementary event we desire the rate of. x is a named vector containing the value of the state process at time t, and params is a named vector containing parameters. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t, of the covariates. This is accomplished via interpolation of the covariate table. If rate.fun is a native function, it must be of type "pomp\_ssa\_rate\_fn" as defined in the header "pomp.h", which is included with the package.

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In writing dens. fun, you must assume that no state transitions have occurred between t1 and t2. If dens. fun is written as an R function, it must have at least the arguments x1, x2, t1, t2, params, and . . . . On a call to this function, x1 and x2 will be named vectors of state variables at times t1 and t2, respectively. The named vector params contains the parameters. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t1, of the covariates. If the argument covars is included and a covariate table has been included in the pomp object, then on a call to this function, covars will be filled with the values, at time t1, of the covariates. This is accomplished via interpolation of the covariate table. As above, any additional arguments will be filled by the correspondingly-named elements in the userdata slot of the pomp object (see pomp). If dens. fun is written in a native language, it must be a function of type "pomp\_onestep\_pdf" as defined in the header "pomp.h" included with the package (see the directory "include" in the installed package directory).

#### Value

onestep.sim, euler.sim, discrete.time.sim, and gillespie.sim each return functions suitable for use as the argument rprocess argument in pomp.

onestep. dens returns a function suitable for use as the argument dprocess in pomp.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

eulermultinom, pomp

# **Examples**

```
## examples showing how to use these functions
## are provided in the vignette "intro_to_pomp"
## Not run:
vignette("intro_to_pomp")
## End(Not run)
```

pmcmc

The PMCMC algorithm

# **Description**

The Particle MCMC algorithm for estimating the parameters of a partially-observed Markov process.

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### **Usage**

```
## S4 method for signature 'pomp'
pmcmc(object, Nmcmc = 1, start, pars,
    rw.sd, dprior, Np, hyperparams, tol = 1e-17, max.fail = 0,
    verbose = getOption("verbose"), transform = FALSE, ...)
## S4 method for signature 'pfilterd.pomp'
pmcmc(object, Nmcmc = 1, start, pars,
    rw.sd, dprior, Np, hyperparams, tol, max.fail = 0,
    verbose = getOption("verbose"), transform = FALSE, ...)
## S4 method for signature 'pmcmc'
pmcmc(object, Nmcmc, start, pars,
   rw.sd, dprior, Np, hyperparams, tol, max.fail = 0,
   verbose = getOption("verbose"), transform, ...)
## S4 method for signature 'pmcmc'
continue(object, Nmcmc = 1, start, pars,
   rw.sd, dprior, Np, hyperparams, tol, max.fail = 0,
   verbose = getOption("verbose"), transform, ...)
```

# **Arguments**

object	An object of class pomp.	

Nmcmc The number of PMCMC iterations to perform.

start named numeric vector; the starting guess of the parameters.

pars optional character vector naming the ordinary parameters to be estimated. Every

parameter named in pars must have a positive random-walk standard deviation specified in rw. sd. Leaving pars unspecified is equivalent to setting it equal to

the names of all parameters with a positive value of rw.sd.

dprior Function of prototype dprior(params, hyperparams, ..., log) that evaluates

the prior density. This defaults to an improper uniform prior.

rw. sd numeric vector with names; used to parameterize a Gaussian random walk MCMC

proposal. The random walk is only applied to parameters named in pars. The algorithm requires that the random walk be nontrivial, so each element in rw.sd[pars] must be positive. The following must be satisfied: names(rw.sd) must be a subset of names(start), rw.sd must be non-negative (zeros are simply ignored),

the name of every positive element of rw. sd must be in pars.

Np a positive integer; the number of particles to use in each filtering operation.

hyperparams optional list; parameters to be passed to dprior.

tol numeric scalar; particles with log likelihood below tol are considered to be

"lost". A filtering failure occurs when, at some time point, all particles are lost.

max.fail integer; maximum number of filtering failures permitted. If the number of fail-

ures exceeds this number, execution will terminate with an error.

verbose logical; if TRUE, print progress reports.

transform logical; if TRUE, optimization is performed on the transformed scale.

... Additional arguments. These are currently ignored.

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#### Value

An object of class pmcmc. This class inherits from class pfilterd.pomp and contains the following additional slots:

**pars, Nmcmc, dprior, hyperparams** These slots hold the values of the corresponding arguments of the call to pmcmc.

**random.walk.sd** a named numeric vector containing the random-walk variances used to parameterize a Gaussian random walk MCMC proposal.

**log.prior** a numeric value containing the log of the prior density evaluated at the parameter vector in the params slot.

# **Re-running PMCMC Iterations**

To re-run a sequence of PMCMC iterations, one can use the pmcmc method on a pmcmc object. By default, the same parameters used for the original PMCMC run are re-used (except for tol, max.fail, and verbose, the defaults of which are shown above). If one does specify additional arguments, these will override the defaults.

# **Continuing PMCMC Iterations**

One can continue a series of PMCMC iterations from where one left off using the continue method. A call to pmcmc to perform Nmcmc=m iterations followed by a call to continue to perform Nmcmc=n iterations will produce precisely the same effect as a single call to pmcmc to perform Nmcmc=m+n iterations. By default, all the algorithmic parameters are the same as used in the original call to pmcmc. Additional arguments will override the defaults.

# **Details**

pmcmc implements an MCMC algorithm in which the true likelihood of the data is replaced by an unbiased estimate computed by a particle filter. This gives an asymptotically correct Bayesian procedure for parameter estimation (Andrieu and Roberts, 2009). An extension to give a correct Bayesian posterior distribution of unobserved state variables (Andrieu et al, 2010) has not yet been implemented.

# Author(s)

Edward L. Ionides <ionides at umich dot edu>, Aaron A. King <kingaa at umich dot edu>

### References

C. Andrieu, A. Doucet and R. Holenstein, Particle Markov chain Monte Carlo methods, J. R. Stat. Soc. B, to appear, 2010.

C. Andrieu and G.O. Roberts, The pseudo-marginal approach for efficient computation, Ann. Stat. 37:697-725, 2009.

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# See Also

pmcmc-class, pmcmc-methods, pomp, pomp-class, pfilter. See the "intro\_to\_pomp" vignette for an example [CURRENTLY, ONLY DEMONSTRATING THE MIF ALGORITHM, WHICH IS ALGORITHMICALLY VERY SIMILAR TO PMCMC SINCE THEY BOTH DEPEND CRITICALLY ON A PARTICLE FILTERING STEP].

pmcmc-methods

Methods of the "pmcmc" class

# **Description**

Methods of the "pmcmc" class.

# Usage

```
## S4 method for signature 'pmcmc'
logLik(object, ...)
## S4 method for signature 'pmcmc'
conv.rec(object, pars, ...)
## S4 method for signature 'pmcmc'
filter.mean(object, pars, ...)
## S4 method for signature 'pmcmc'
plot(x, y = NULL, ...)
## S4 method for signature 'pmcmc'
dprior(object, params, log = FALSE, ...)
compare.pmcmc(z)
```

# **Arguments**

object, x	The pmcmc object.
pars	Names of parameters.
у	Ignored.
z	A pmcmc object or list of pmcmc objects.
params	Named vector of parameters.
log	if TRUE, log probabilities are returned.
	Further arguments (either ignored or passed to underlying functions).

# Methods

**conv.rec** conv.rec(object, pars = NULL) returns the columns of the convergence-record matrix corresponding to the names in pars. By default, all rows are returned.

logLik Returns the value in the loglik slot.

**dprior** dprior(object,params,log) evaluates the prior density at params with values of the hyperparameters given by object@hyperparams.

**pmcmc** Re-runs the PMCMC iterations. See the documentation for pmcmc.

**compare.pmcmc** Given a pmcmc object or a list of pmcmc objects, compare.pmcmc produces a set of diagnostic plots.

plot Plots a series of diagnostic plots. When x is a pmcmc object, plot(x) is equivalent to compare.pmcmc(list(x)).

**filter.mean** filter.mean(object, pars = NULL) returns the rows of the filtering-mean matrix corresponding to the names in pars. By default, all rows are returned.

**print** Prints a summary of the pmcmc object.

show Displays the pmcmc object.

pfilter See pfilter.

#### Author(s)

Edward L. Ionides <ionides at umich dot edu>, Aaron A. King <kingaa at umich dot edu>

#### References

C. Andrieu, A. Doucet and R. Holenstein, Particle Markov chain Monte Carlo methods, J. Roy. Stat. Soc B, to appear, 2010.

C. Andrieu and G.O. Roberts, The pseudo-marginal approach for efficient computation, Ann Stat 37:697-725, 2009.

#### See Also

```
pmcmc, pomp, pomp-class, pfilter
```

pomp

Partially-observed Markov process object.

# **Description**

Create a new pomp object to hold a partially-observed Markov process model together with a unior multi-variate time series.

# **Usage**

```
skeleton = NULL, skeleton.type = c("map","vectorfield"), skelmap.delta.t = 1,
       initializer, covar, tcovar,
       obsnames, statenames, paramnames, covarnames, zeronames,
       PACKAGE, parameter.transform, parameter.inv.transform)
## S4 method for signature 'matrix'
pomp(data, times, t0, ..., rprocess, dprocess, rmeasure, dmeasure,
      measurement.model,
    skeleton = NULL, skeleton.type = c("map","vectorfield"), skelmap.delta.t = 1,
       initializer, covar, tcovar,
       obsnames, statenames, paramnames, covarnames, zeronames,
       PACKAGE, parameter.transform, parameter.inv.transform)
## S4 method for signature 'pomp'
pomp(data, times, t0, ..., rprocess, dprocess, rmeasure, dmeasure,
      measurement.model,
       skeleton, skeleton.type, skelmap.delta.t,
       initializer, covar, tcovar,
       obsnames, statenames, paramnames, covarnames, zeronames,
       PACKAGE, parameter.transform, parameter.inv.transform)
```

#### **Arguments**

data, times

The time series data and times at which observations are made. data can be specified as a vector, a matrix, a data-frame, or a pomp object.. If data is a numeric vector, times must be a numeric vector of the same length. If data is a matrix, it should have dimensions nobs x ntimes, where nobs is the number of observed variables and ntimes is the number of times at which observations were made (i.e., each column is a distinct observation of the nobs variables). In this case, times must be given as a numeric vector (of length ntimes). If data is a data-frame, times must name of the column of observation times. Note that, in this case, data is a data-frame, it will be internally coerced to an array with storage-mode 'double'. Note that the times must be numeric and strictly increasing.

t0

The zero-time. This must be no later than the time of the first observation, times[1]. The stochastic dynamical system is initialized at time t0.

rprocess

optional function; a function of prototype rprocess(xstart, times, params, ...) that simulates from the unobserved process. The easiest way to specify rprocess is to use one of the plugins provided as part of the **pomp** package. See below for details.

dprocess

optional function; a function of prototype dprocess(x, times,params,log,...) that evaluates the likelihood of a sequence of consecutive state transitions. The easiest way to specify dprocess is to use one of the plugins provided as part of the **pomp** package. It is not typically necessary (or even feasible) to define dprocess. See below for details.

rmeasure

optional; the measurement model simulator. This can be specified in one of three ways: (1) as a function of prototype rmeasure(x,t,params,...) that makes a draw from the observation process given states x, time t, and parameters params. (2) as the name of a native (compiled) routine with prototype "pomp\_measure\_model\_simulator" as defined in the header file "exam-

ples/pomp.h". In the above cases, if the measurement model depends on covariates, the optional argument covars will be filled with interpolated values at each call. (3) using the formula-based measurement.model facility (see below).

dmeasure

optional; the measurement model probability density function. This can be specified in one of three ways: (1) as a function of prototype dmeasure(y,x,t,params,log,...) that computes the p.d.f. of y given x, t, and params. (2) as the name of a native (compiled) routine with prototype "pomp\_measure\_model\_density" as defined in the header file "examples/pomp.h". In the above cases, if the measurement model depends on covariates, the optional argument covars will be filled with interpolated values at each call. (3) using the formula-based measurement.model facility (see below). As might be expected, if log=TRUE, this function should return the log likelihood.

measurement.model

optional; a formula or list of formulae, specifying the measurement model. These formulae are parsed internally and used to generate rmeasure and dmeasure functions. If measurement.model is given it overrides any specification of rmeasure or dmeasure. See below for an example. **NB:** it will typically be possible to acclerate measurement model computations by writing dmeasure and/or rmeasure functions directly.

skeleton, skeleton.type, skelmap.delta.t

The function skeleton specifies the deterministic skeleton of the unobserved Markov process. If we are dealing with a discrete-time Markov process, its deterministic skeleton is a map: indicate this by specifying skeleton.type="map". If we are dealing with a continuous-time Markov process, its deterministic skeleton is a vectorfield: indicate this by specifying skeleton.type="vectorfield". The skeleton function can be specified in one of two ways: (1) as an R function of prototype skeleton(x,t,params,...) that evaluates the deterministic skeleton at state x and time t given the parameters params, or (2) as the name of a native (compiled) routine with prototype "pomp\_skeleton" as defined in the header file "pomp.h". If the deterministic skeleton depends on covariates, the optional argument covars will be filled with interpolated values of the covariates at the time t.

With a discrete-time skeleton, the default assumption is that time advances 1 unit per iteration of the map; to change this, set skelmap.delta.t to the appropriate time-step.

initializer

optional function of prototype initializer(params, t0,...) that yields initial conditions for the state process when given a vector, params, of parameters. By default (i.e., if it is unspecified when pomp is called), the initializer assumes any parameters in params the names of which end in ".0" are initial values. These are simply copied over as initial conditions when init.state is called (see init.state-pomp). The names of the state variables are the same as the corresponding initial value parameters, but with the ".0" dropped.

covar, tcovar

An optional table of covariates: covar is the table (with one column per variable) and tcovar the corresponding times (one entry per row of covar). covar can be specified as either a matrix or a data frame. In either case the columns are taken to be distinct covariates. If covar is a data frame, tcovar can be either the name or the index of the time variable. If a covariate table is supplied,

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> then the value of each of the covariates is interpolated as needed, i.e., whenever rprocess, dprocess, rmeasure, dmeasure, or init.state is evaluated. The resulting interpolated values are passed to the corresponding functions as a numeric vector named covars.

obsnames, statenames, paramnames, covarnames

Optional character vectors specifying the names of observables, state variables, parameters, or covariates, respectively. These are only used in the event that one or more of the basic functions (rprocess, dprocess, rmeasure, dmeasure, skeleton) are defined using native routines. In that case, these name vectors are matched against the corresponding names and the indices of the names are passed to the native routines. Using this facility allows one to write one or more of rprocess, dprocess, rmeasure, dmeasure, skeleton in native code in a way that does not depend on the order of states, parameters, and covariates at run time. See the "Advanced topics in pomp" vignette for more on this topic and examples.

zeronames

Optional character vector specifying the names of accumulator variables. See the "Advanced topics in pomp" vignette for a discussion of this.

**PACKAGE** 

An optional string giving the name of the dynamically loaded library in which any native routines are to be found.

parameter.transform, parameter.inv.transform

Optional functions specifying parameter transformations. These functions must have arguments params and .... parameter.transform should transform parameters from the user's scale to the scale that rprocess, dprocess, rmeasure, dmeasure, skeleton, and initializer will use internally. parameter.inv.transform should be the inverse of parameter.transform. Note that it is the user's responsibility to make sure this holds. If obj is the constructed pomp object, and coef(obj) is non-empty, a simple check of this is x <- coef(obj, transform=TRUE); obj1 <- obj; coef(obj1,transform=TRUE) <- x; identical(coef(obj),coef(obj1))</pre> and identical(coef(obj1, transform=TRUE), x). By default, both functions are the identity transformation. See the "introduction\_to\_pomp" vignette for an example.

Any additional arguments given to pomp will be stored in the pomp object and . . . passed as arguments to each of the functions rprocess, dprocess, rmeasure, dmeasure, and initializer whenever they are evaluated.

# **Details**

It is not typically necessary (or desirable, or even feasible) to define all of the functions rprocess, dprocess, rmeasure, dmeasure, and skeleton in any given problem. Each algorithm makes use of a different subset of these functions. In general, the specification of processmodel codes rprocess and/or dprocess can be somewhat nontrivial: for this reason, plugins have been developed to streamline this process for the user. Currently, if one's process model evolves in discrete time or one is willing to make such an approximation (e.g., via an Euler approximation), then the euler. sim or onestep. sim plugin for rprocess and onestep, dens plugin for dprocess are available. For exact simulation of certain continuous-time Markov chains, an implementation of Gillespie's algorithm is available (see gillespie.sim). To use the plugins, consult the help documentation (?plugins) and the vignettes.

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It is anticipated that, in specific cases, it will be possible to obtain increased computational efficiency by writing custom versions of rprocess and/or dprocess. See the "Advanced topics in pomp" vignette for a discussion of this. If such custom versions are desired, the following describes how each of these functions should be written in this case.

rprocess In general, the specification of rprocess can be somewhat nontrivial: for this reason, plugins have been developed to streamline this process for the user. Currently, if one's process model evolves in discrete time or one is willing to make such an approximation (e.g., via an Euler approximation), then the euler.sim or onestep.sim plugin is available. For exact simulation of certain continuous-time Markov chains, an implementation of Gillespie's algorithm is available (see gillespie.sim). To use the plugins, consult the help documentation (?plugins) and the vignettes.

If the plugins are not used rprocess must have at least the following arguments: xstart, times, params, and . . . . It can also take additional arguments. It is guaranteed that these will be filled with the corresponding elements the user has included as additional arguments in the construction of the pomp object.

In calls to rprocess, xstart can be assumed to be a rank-2 array (matrix) with rows corresponding to state variables and columns corresponding to independent realizations of the process. params will similarly be a rank-2 array with rows corresponding to parameters and columns corresponding to independent realizations. The columns of params correspond to those of xstart; in particular, they will agree in number. Both xstart and params will have rownames, which are available for use by the user.

rprocess must return a rank-3 array with rownames. Suppose x is the array returned. Then  $\dim(x)=c(\text{nvars},\text{nreps},\text{ntimes})$ , where nvars (=nrow(xstart)) is the number of state variables, nreps (=ncol(xstart)) is the number of independent realizations simulated, and ntimes is the length of the vector times. x[,j,k] is the value of the state process in the j-th realization at time times[k]. In particular, x[,,1] must be identical to xstart. The rownames of x must correspond to those of xstart.

At present, the following methods make use of rprocess:

- simulate
- pfilter
- mif
- nlf
- probe
- probe.match

dprocess In general, the specification of dprocess can be somewhat nontrivial: for this reason, plugins have been developed to streamline this process for the user. Currently, if one's process model evolves in discrete time or one is willing to make such an approximation (e.g., via an Euler approximation), then the onestep.dens plugin for dprocess is available. To use the plugins, consult the help documentation (?plugins) and the vignettes.

If the plugins are not used, dprocess must have at least the following arguments: x, times, params, log, and .... It may take additional arguments. It is guaranteed that these will be filled with the corresponding elements the user has included as additional arguments in the construction of the pomp object.

In calls to dprocess, x may be assumed to be an nvars x nreps x ntimes array, where these terms have the same meanings as above. params will be a rank-2 array with rows corresponding to individual parameters and columns corresponding to independent realizations. The

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columns of params correspond to those of x; in particular, they will agree in number. Both x and params will have rownames, available for use by the user.

dprocess must return a rank-2 array (matrix). Suppose d is the array returned. Then  $\dim(d)=c(nreps,ntimes-1)$ . d[j,k] is the probability density of the transition from state x[,j,k-1] at time times[k-1] to state x[,j,k] at time times[k]. If  $\log=TRUE$ , then the log of the pdf is returned.

In writing this function, you may assume that the transitions are consecutive. It should be quite clear that, but for this assumption, it would be quite difficult in general to write the transition probabilities. In fact, from one perspective, the algorithms in **pomp** are designed to overcome just this difficulty.

At present, no methods in pomp make use of dprocess.

The measurement-model, deterministic skeleton, and initializer components are easily specified without the use of plugins. The following is a guide to writing these components.

rmeasure if provided, must take at least the arguments x, t, params, and .... It may take additional arguments, which will be filled with user-specified data as above. x may be assumed to be a named numeric vector of length nvars, (which has the same meanings as above). t is a scalar quantity, the time at which the measurement is made. params may be assumed to be a named numeric vector of length npars.

rmeasure must return a named numeric vector. If y is the returned vector, then length(y)=nobs, where nobs is the number of observable variables.

At present, the following methods make use of rmeasure:

- simulate
- nlf
- probe
- probe.match

dmeasure if provided, must take at least the arguments y, x, t, params, log, and .... y may be assumed to be a named numeric vector of length nobs containing (actual or simulated) values of the observed variables; x will be a named numeric vector of length nvar containing state variables params, a named numeric vector containing parameters; and t, a scalar, the corresponding observation time. It may take additional arguments which will be filled with user-specified data as above. dmeasure must return a single numeric value, the pdf of y given x at time t. If log=TRUE, then the log of the pdf is returned.

At present, the following methods make use of dmeasure:

- pfilter
- mif

skeleton If skeleton is an R function, it must have at least the arguments x, t, params, and . . . . x is a numeric vector containing the coordinates of a point in state space at which evaluation of the skeleton is desired. t is a numeric value giving the time at which evaluation of the skeleton is desired. Of course, these will be irrelevant in the case of an autonomous skeleton. params is a numeric vector holding the parameters. The optional argument covars is a numeric vector containing the values of the covariates at the time t. covars will have one value for each column of the covariate table specified when the pomp object was created. covars is constructed from the covariate table (see covar, below) by interpolation. skeleton may take additional arguments, which will be filled, as above, with user-specified data. skeleton must return a numeric vector of the same length as x. The return value is interpreted as the

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vectorfield (if the dynamical system is continuous) or the value of the map (if the dynamical system is discrete), at the point x at time t.

If skeleton is the name of a native routine, this routine must be of prototype "pomp\_skeleton" as defined in the header "pomp.h" (see the "include" directory in the installed package directory).

At present, the following methods make use of skeleton:

- trajectory
- traj.match

initializer if provided, must have at least the arguments params, t0, and .... params is a named numeric vector of parameters. t0 will be the time at which initial conditions are desired. initializer must return a named numeric vector of initial states.

#### Value

An object of class pomp. If data is an object of class pomp, then by default the returned pomp object is identical to data. If additional arguments are given, these override the defaults.

#### Warning

Some error checking is done by pomp, but complete error checking is impossible. If the user-specified functions do not conform to the above specifications (see Details), then the results may be invalid. In particular, if both rmeasure and dmeasure are specified, the user should verify that these two functions correspond to the same model and if skeleton is specified, the user is responsible for verifying that it corresponds to the true deterministic skeleton of the model. Each **pomp**-package algorithm uses some subset of the five basic components (rprocess, dprocess, rmeasure, dmeasure, skeleton). If an algorithm requires a component that was not given in the construction of the pomp object, an error is generated.

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

```
pomp-methods, plugins, time, time<-, timezero, timezero<-, coef, coef<-, obs, states, window,
as.data.frame.pomp</pre>
```

#### **Examples**

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```
header=paste("=====",pomp.examples,"======")
)

## End(Not run)
```

pomp-methods

Methods of the "pomp" class

# Description

Methods of the pomp class.

#### Usage

```
## S3 method for class 'pomp'
as.data.frame(x, row.names, optional, ...)
## S4 method for signature 'pomp'
coef(object, pars, transform = FALSE, ...)
## S4 replacement method for signature 'pomp'
coef(object, pars, transform = FALSE, ...) <- value</pre>
## S4 method for signature 'pomp'
obs(object, vars, ...)
## S4 method for signature 'pomp'
data.array(object, vars, ...)
## S4 method for signature 'pomp'
partrans(object, params, dir = c("forward", "inverse"), ...)
## S4 method for signature 'pomp'
plot(x, y, variables, panel = lines,
      nc = NULL, yax.flip = FALSE,
      mar = c(0, 5.1, 0, if (yax.flip) 5.1 else 2.1),
      oma = c(6, 0, 5, 0), axes = TRUE, ...)
## S4 method for signature 'pomp'
print(x, ...)
## S4 method for signature 'pomp'
show(object)
## S4 method for signature 'pomp'
states(object, vars, ...)
## S4 method for signature 'pomp'
time(x, t0 = FALSE, ...)
## S4 replacement method for signature 'pomp'
time(object, t0 = FALSE, ...) <- value</pre>
## S4 method for signature 'pomp'
timezero(object, ...)
## S4 replacement method for signature 'pomp'
timezero(object, ...) <- value
## S4 method for signature 'pomp'
window(x, start, end, ...)
```

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```
## S4 method for signature 'pomp'
as(object, class)
## S4 method for signature 'pomp,data.frame'
coerce(from, to = "data.frame", strict = TRUE)
```

## **Arguments**

object, x The pomp object.

pars optional character; names of parameters to be retrieved or set.

vars optional character; names of observed variables to be retrieved.

transform optional logical; should the parameter transformations be applied?

value numeric; values to be assigned.

params a vector or matrix of parameters to be transformed.

dir direction of the transformation. dir="forward" applies the transformation from

the "natural" scale to the "internal" scale. This is the transformation specified by the parameter.transform argument to pomp; it is stored in the 'par.trans' slot of object. dir="inverse" applies the inverse transformation (stored in the

'par.untrans' slot).

to logical; if TRUE on a call to time, the zero time is prepended to the time vector;

if TRUE on a call to time<-, the first element in value is taken to be the initial

time.

start, end start and end times of the window.

class character; name of the class to which object should be coerced.

from, to the classes between which coercion should be performed.

strict ignored.
y ignored.

variables optional character; names of variables to plot.

panel a function of prototype panel(x, col, bg, pch, type, ...) which gives

the action to be carried out in each panel of the display.

nc the number of columns to use. Defaults to 1 for up to 4 series, otherwise to 2.

yax.flip logical; if TRUE, the y-axis (ticks and numbering) should flip from side 2 (left)

to 4 (right) from series to series.

mar, oma the 'par' settings for 'mar' and 'oma' to use. Modify with care!

axes logical; indicates if x- and y- axes should be drawn.

row.names, optional

ignored.

... Further arguments (either ignored or passed to underlying functions).

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#### **Details**

coef coef(object) returns the contents of the params slot of object. coef(object,pars) returns only those parameters named in pars. coef(object,transform=TRUE) returns parameter.inv.transform(coe
where parameter.inv.transform is the user parameter inverse transformation function specified when object was created. Likewise, coef(object,pars,transform=TRUE) returns
parameter.inv.transform(coef(object))[pars].

- coef<- Assigns values to the params slot of the pomp object. coef(object) <- value has the effect of replacing the parameters of object with value. If coef(object) exists, then coef(object,pars) <- value replaces those parameters of object named in pars with the elements of value; the names of value are ignored. If some of the names in pars do not already name parameters in coef(object), then they are concatenated. If coef(object) does not exist, then coef(object,pars) <- value assigns value to the parameters of object; in this case, the names of object will be pars and the names of value will be ignored. coef(object,transform=TRUE) <- value assigns parameter.transform(value) to the params slot of object. Here, parameter.transform is the parameter transformation function specified when object was created. coef(object,pars,transform=TRUE) <- value first, discards any names the value may have, sets names(value) <- pars, and then replaces the elements of object's params slot parameter.transform(value). In this case, if some of the names in pars do not already name parameters in coef(object,transform=TRUE), then they are concatenated.</p>
- **obs**, **data.array** These functions are synonymous. obs(object) returns the array of observations. obs(object, vars) gives just the observations of variables named vars. vars may specify the variables by position or by name.
- **states** states(object) returns the array of states. states(object, vars) gives just the state variables named in vars. vars may specify the variables by position or by name.
- **time** time(object) returns the vector of observation times. time(object,t0=TRUE) returns the vector of observation times with the zero-time t0 prepended.
- time<- time(object) <- value replaces the observation times slot (times) of object with value. time(object,t0=TRUE) <- value has the same effect, but the first element in value is taken to be the initial time. The second and subsequent elements of value are taken to be the observation times. Those data and states (if they exist) corresponding to the new times are retained.</p>
- timezero, timezero<- timezero(object) returns the zero-time t0. timezero(object) <- value
   sets the zero-time to value.</pre>
- window window(x,start=t1,end=t2 returns a new pomp object, identical to x but with only the data in the window between times t1 and t2 (inclusive). By default, start is the time of the first observation and end is the time of the last.
- show Displays the pomp object.
- **plot** Plots the data and state trajectories (if the latter exist). Additional arguments are passed to the low-level plotting routine.
- **print** Prints the pomp object in a nice way.
- as, coerce The coerce method should typically not be used directly. It is defined by setAs as a method to be used by as. A pomp object can be coerced to a data frame via as (object, "data.frame"). The data frame contains the times, the data, and the state trajectories, if they exist.

rprocess simulates the process model. See rprocess-pomp.

**dprocess** evaluates the process model density. See dprocess-pomp.

**rmeasure** simulates the measurement model. See rmeasure-pomp.

**dmeasure** evaluates the measurement-model density. See dmeasure-pomp.

**skeleton** evaluates the deterministic skeleton (be it a vector field or a map). See skeleton-pomp.

init.state returns a vector of initialial conditions. See init.state-pomp.

**simulate** simulate can be used to simulate state and observation trajectories. See documentation under simulate-pomp.

## Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp, pomp-class, rprocess, dprocess, rmeasure, dmeasure, init.state, simulate

probe

Probe a partially-observed Markov process.

# Description

probe applies one or more "probes" to time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for "probe-matching", a generalized method-of-moments approach to parameter estimation. probe.match calls an optimizer to adjust model parameters to do probe-matching, i.e., to minimize the discrepancy between simulated and actual data. This discrepancy is measured using the "synthetic likelihood" as defined by Wood (2010). probe.match.objfun constructs an objective function for probe-matching suitable for use in optim-like optimizers.

#### Usage

# **Arguments**

object An object of class pomp.

probes A single probe or a list of one or more probes. A probe is simply a scalar- or

vector-valued function of one argument that can be applied to the data array of a pomp. A vector-valued probe must always return a vector of the same size. A number of basic examples are provided with the package (see basic.probes).

params optional named numeric vector of model parameters. By default, params=coef(object).

nsim The number of model simulations to be computed.

seed optional; if non-NULL, the random number generator will be initialized with this

seed for simulations. See simulate-pomp.

start named numeric vector; the initial guess of parameters.

est character vector; the names of parameters to be estimated.

weights optional numeric vector of relative weights. Must be of the same length as

probes.

method Optimization method. Choices are subplex and any of the methods used by

optim.

verbose logical; print diagnostic messages?

eval.only logical; if TRUE, no optimization is attempted. Instead, the probe-mismatch

value is simply evaluated at the start parameters.

fail.value optional scalar; if non-NA, this value is substituted for non-finite values of the

objective function. It should be a large number (i.e., bigger than any legitimate

values the objective function is likely to take).

transform logical; if TRUE, optimization is performed on the transformed scale.

... Additional arguments. In the case of probe, these are currently ignored. In the

case of probe.match, these are passed to optim or subplex in the control list.

#### **Details**

A call to probe results in the evaluation of the probe(s) in probes on the data. Additionally, nsim simulated data sets are generated (via a call to simulate) and the probe(s) are applied to each of these. The results of the probe computations on real and simulated data are stored in an object of class probed.pomp.

A call to probe match results in an attempt to optimize the agreement between model and data, as measured by the specified probes, over the parameters named in est. The results, including coefficients of the fitted model and values of the probes for data and fitted-model simulations, are stored in an object of class probe matched.pomp.

The objective function minimized by probe.match — in a form suitable for use with optim-like optimizers — is created by a call to probe.match.objfun. Specifically, probe.match.objfun will return a function that takes a single numeric-vector argument that is assumed to cotain the parameters named in est, in that order. This function will return the negative synthetic log likelihood for the probes specified.

#### Value

probe returns an object of class probed.pomp. probed.pomp is derived from the pomp class and therefore have all the slots of pomp. In addition, a probed.pomp class has the following slots:

**probes** list of the probes applied.

datvals, simvals values of each of the probes applied to the real and simulated data, respectively.

quantiles fraction of simulations with probe values less than the value of the probe of the data.

pvals two-sided p-values: fraction of the simvals that deviate more extremely from the mean of the simvals than does datavals.

**synth.loglik** the log synthetic likelihood (Wood 2010). This is the likelihood assuming that the probes are multivariate-normally distributed.

probe.match returns an object of class probe.matched.pomp, which is derived from class probed.pomp. probe.matched.pomp objects therefore have all the slots above plus the following:

est, weights, fail.value values of the corresponding arguments in the call to spect.match.

value value of the objective function.

evals number of function and gradient evaluations by the optimizer. See optim.

convergence, msg Convergence code and message from the optimizer. See optim.

probe.match.objfun returns a function suitable for use as an objective function in an optim-like optimizer.

#### Author(s)

Daniel C. Reuman (d.reuman at imperial dot ac dot uk)

Aaron A. King (kingaa at umich dot edu)

#### References

B. E. Kendall, C. J. Briggs, W. M. Murdoch, P. Turchin, S. P. Ellner, E. McCauley, R. M. Nisbet, S. N. Wood Why do populations cycle? A synthesis of statistical and mechanistic modeling approaches, Ecology, 80:1789–1805, 1999.

S. N. Wood Statistical inference for noisy nonlinear ecological dynamic systems, Nature, 466: 1102–1104, 2010.

#### See Also

pomp-class, pomp-methods, basic.probes, probe.match

#### **Examples**

```
data(ou2)
good <- probe(</pre>
              ou2,
              probes=list(
                y1.mean=probe.mean(var="y1"),
                y2.mean=probe.mean(var="y2"),
                y1.sd=probe.sd(var="y1"),
                y2.sd=probe.sd(var="y2"),
                extra=function(x)max(x["y1",])
                ),
              nsim=500
              )
summary(good)
plot(good)
bad <- probe(</pre>
             params=c(alpha.1=0.1,alpha.4=0.2,x1.0=0,x2.0=0,
                       alpha.2=-0.5,alpha.3=0.3,
                       sigma.1=3, sigma.2=-0.5, sigma.3=2,
                       tau=1),
             probes=list(
               y1.mean=probe.mean(var="y1"),
               y2.mean=probe.mean(var="y2"),
               y1.sd=probe.sd(var="y1"),
               y2.sd=probe.sd(var="y2"),
               extra=function(x)range(x["y1",])
               ),
             nsim=500
summary(bad)
plot(bad)
```

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## **Description**

Methods of the probed.pomp, probe.matched.pomp, spect.pomp, and spect.matched.pomp classes

## Usage

```
## S4 method for signature 'probed.pomp'
summary(object, ...)
## S4 method for signature 'probed.pomp'
plot(x, y, ...)
## S4 method for signature 'probe.matched.pomp'
summary(object, ...)
## S4 method for signature 'probe.matched.pomp'
plot(x, y, ...)
## S4 method for signature 'spect.pomp'
summary(object, ...)
## S4 method for signature 'probed.pomp'
logLik(object, ...)
## S4 method for signature 'spect.pomp'
plot(x, y, max.plots.per.page = 4,
          plot.data = TRUE,
          quantiles = c(.025, .25, .5, .75, .975),
          quantile.styles = list(lwd=1, lty=1, col="gray70"),
          data.styles = list(lwd=2, lty=2, col="black"))
## S4 method for signature 'spect.matched.pomp'
summary(object, ...)
## S4 method for signature 'spect.matched.pomp'
plot(x, y, ...)
## S4 method for signature 'probed.pomp'
as(object, class)
```

## **Arguments**

```
object, x the object to be summarized or plotted.

y ignored.

max.plots.per.page
 maximum number of plots per page

plot.data plot the data spectrum?

quantiles quantiles to plot

quantile.styles

plot style parameters for the quantiles
```

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data.styles plot style parameters for the data spectrum
class character; name of the class to which object should be coerced.
... Further arguments (either ignored or passed to underlying functions).

#### Methods

plot displays diagnostic plots.

summary displays summary information.

**logLik** returns the synthetic likelihood for the probes. NB: in general, this is not the same as the likelihood.

**as** when a 'probed.pomp' is coerced to a 'data.frame', the first row gives the probes applied to the data; the rest of the rows give the probes evaluated on simulated data. The rownames of the result can be used to distinguish these.

#### Author(s)

Daniel C. Reuman (d.reuman at imperial dot ac dot uk)

Aaron A. King (kingaa at umich dot edu)

#### See Also

probe, probed.pomp, probe.matched.pomp, probe.match

profileDesign Design matrices for likelihood profile calculations.

## Description

profileDesign generates a data-frame where each row can be used as the starting point for a profile likelihood calculation.

#### Usage

```
profileDesign(..., lower, upper, nprof)
```

#### **Arguments**

... Specifies the parameters over which to profile.

lower, upper Named numeric vectors, specifying the range over which the other parameters

are to be sampled.

nprof The number of starts per profile point.

#### Value

profileDesign returns a data frame with nprof points per profile point. The other parameters in vars are sampled using sobol.

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#### Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

## See Also

sobol

## **Examples**

```
## A one-parameter profile design:
x <- profileDesign(p=1:10,lower=c(a=0,b=0),upper=c(a=1,b=5),nprof=20)
dim(x)
plot(x)
## A two-parameter profile design:
x <- profileDesign(p=1:10,q=3:5,lower=c(a=0,b=0),upper=c(b=5,a=1),nprof=20)
dim(x)
plot(x)</pre>
```

ricker

Ricker model with Poisson observations.

# Description

ricker is a pomp object encoding a stochastic Ricker model with Poisson measurement error.

#### Usage

```
data(ricker)
```

#### **Details**

The state process is  $N_{t+1} = rN_t \exp(-N_t + e_t)$ , where the  $e_t$  are i.i.d. normal random deviates with variance  $\sigma^2$ . The observed variables  $y_t$  are distributed as  $Poisson(\phi N_t)$ .

## See Also

```
pomp-class and the vignettes
```

## **Examples**

```
data(ricker)
plot(ricker)
coef(ricker)
```

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rw2

Two-dimensional random-walk process

# Description

rw2 is a pomp object encoding a 2-D normal random walk.

# Usage

```
data(rw2)
```

## **Details**

The random-walk process is fully but noisily observed.

# See Also

```
pomp-class and the vignettes
```

# **Examples**

```
data(rw2)
plot(rw2)
x <- simulate(rw2,nsim=10,seed=20348585L,params=c(x1.0=0,x2.0=0,s1=1,s2=3,tau=1))
plot(x[[1]])</pre>
```

sannbox

Simulated annealing with box constraints.

# Description

sannbox is a straightforward implementation of simulated annealing with box constraints.

# Usage

```
sannbox(par, fn, control = list(), ...)
```

# Arguments

par	Initial values for the parameters to be optimized over.
fn	A function to be minimized, with first argument the vector of parameters over which minimization is to take place. It should return a scalar result.
control	A named list of control parameters. See 'Details'.
	ignored.

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#### **Details**

The control argument is a list that can supply any of the following components:

trace Non-negative integer. If positive, tracing information on the progress of the optimization is produced. Higher values may produce more tracing information.

fnscale An overall scaling to be applied to the value of fn during optimization. If negative, turns the problem into a maximization problem. Optimization is performed on fn(par)/fnscale.

parscale A vector of scaling values for the parameters. Optimization is performed on par/parscale and these should be comparable in the sense that a unit change in any element produces about a unit change in the scaled value.

maxit The total number of function evaluations: there is no other stopping criterion. Defaults to 10000.

temp starting temperature for the cooling schedule. Defaults to 1.

tmax number of function evaluations at each temperature. Defaults to 10.

candidate.dist function to randomly select a new candidate parameter vector. This should be a function with three arguments, the first being the current parameter vector, the second the temperature, and the third the parameter scaling. By default, candidate.dist is function(par,temp,scale) rnorm(n=length(par),mean=par,sd=scale\*temp).

sched cooling schedule. A function of a three arguments giving the temperature as a function of iteration number and the control parameters temp and tmax. By default, sched is function(k, temp, tmax) temp/log(((k-1)%/%tmax)\*tmax+exp(1)).

Alternatively, one can supply a numeric vector of temperatures. This must be of length at least maxit.

## Value

sannbox returns a list with components:

**counts** two-element integer vector. The first number gives the number of calls made to fn. The second number is provided for compatibility with optim and will always be NA.

**convergence** provided for compatibility with optim; will always be 0.

final.params last tried value of par.

**final.value** value of fn corresponding to final.params.

par best tried value of par.

value value of fn corresponding to par.

## Author(s)

Daniel Reuman, Imperial College London and Aaron A. King <kingaa at umich dot edu>

## See Also

traj.match, probe.match.

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simulate-pomp	Running simulations of a partially-observed Markov process	

# Description

simulate can be used to generate simulated data sets and/or to simulate the state process.

# Usage

# Arguments

object	An object of class pomp.
nsim	The number of simulations to perform. Note that the number of replicates will be nsim times ncol(xstart).
seed	optional; if set, the pseudorandom number generator (RNG) will be initialized with seed. the random seed to use. The RNG will be restored to its original state afterward.
params	either a named numeric vector or a numeric matrix with rownames. The parameters to use in simulating the model. If params is not given, then the contents of the params slot of object will be used, if they exist.
states	Do we want the state trajectories?
obs	Do we want data-frames of the simulated observations?
times, t0	times specifies the times at which simulated observations will be made. to specifies the start time (the time at which the initial conditions hold). The default for times is is times=time(object,t0=FALSE) and t0=timezero(object), respectively.
as.data.frame	logical; if TRUE, return the result as a data-frame.
	further arguments that are currently ignored.

## **Details**

Simulation of the state process and of the measurement process are each accomplished by a single call to the user-supplied rprocess and rmeasure functions, respectively. This makes it possible for the user to write highly optimized code for these potentially expensive computations.

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#### Value

If states=FALSE and obs=FALSE (the default), a list of nsim pomp objects is returned. Each has a simulated data set, together with the parameters used (in slot params) and the state trajectories also (in slot states). If times is specified, then the simulated observations will be at times times.

If nsim=1, then a single pomp object is returned (and not a singleton list).

If states=TRUE and obs=FALSE, simulated state trajectories are returned as a rank-3 array with dimensions nvar x (ncol(params)\*nsim) x ntimes. Here, nvar is the number of state variables and ntimes the length of the argument times. The measurement process is not simulated in this case.

If states=FALSE and obs=TRUE, simulated observations are returned as a rank-3 array with dimensions nobs x (ncol(params)\*nsim) x ntimes. Here, nobs is the number of observables.

If both states=TRUE and obs=TRUE, then a named list is returned. It contains the state trajectories and simulated observations as above.

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

#### See Also

pomp-class

### **Examples**

```
data(ou2)
x <- simulate(ou2,seed=3495485,nsim=10)
x <- simulate(ou2,seed=3495485,nsim=10,states=TRUE,obs=TRUE)</pre>
```

sir

Seasonal SIR model implemented using two stochastic simulation algorithms.

## **Description**

euler.sir is a pomp object encoding a simple seasonal SIR model. Simulation is performed using an Euler multinomial approximation. gillespie.sir has the same model implemented using Gillespie's algorithm.

## Usage

```
data(euler.sir)
data(gillespie.sir)
```

#### **Details**

The codes that construct these pomp objects can be found in the "data-R" directory in the installed package. Do file.show(system.file("data-R/sir.R",package="pomp")) to view these codes.

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## See Also

```
pomp-class and the vignettes
```

# **Examples**

```
data(euler.sir)
plot(euler.sir)
plot(simulate(euler.sir,seed=20348585))

data(gillespie.sir)
plot(gillespie.sir)
plot(simulate(gillespie.sir,seed=20348585))
```

sliceDesign

Design matrices for likelihood slices.

## **Description**

sliceDesign generates a data-frame representing points taken along one or more slices through a point in a multidimensional space.

#### Usage

```
sliceDesign(center, ...)
```

## **Arguments**

center center is a named numeric vector specifying the point through which the slice(s)

is (are) to be taken.

... Additional numeric vector arguments specify the slices.

#### Value

sliceDesign returns a data frame with one row per point along a slice. The column slice is a factor that tells which slice each point belongs to.

#### Author(s)

```
Aaron A. King <kingaa at umich dot edu>
```

## See Also

```
profileDesign
```

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#### **Examples**

```
## A single 11-point slice through the point c(A=3,B=8,C=0) along the B direction. x <- sliceDesign(center=c(A=3,B=8,C=0), B=seq(0,10,by=1)) dim(x) plot(x) ## Two slices through the same point along the A and C directions. x <- sliceDesign(c(A=3,B=8,C=0), A=seq(0,5,by=1), C=seq(0,5,length=11)) dim(x) plot(x)
```

sobol

Sobol' low-discrepancy sequence

## **Description**

Generate a data-frame containing a Sobol' low-discrepancy sequence.

#### Usage

```
sobol(vars, n)
sobolDesign(lower, upper, nseq)
```

#### **Arguments**

vars Named list of ranges of variables.

lower, upper named numeric vectors giving the lower and upper bounds of the ranges, respec-

tively.

n, nseq Number of vectors requested.

#### Value

sobol Returns a data frame with n 'observations' of the variables in vars.

sobolDesign Returns a data frame with nseq 'observations' of the variables over the range

specified.

#### Author(s)

Aaron A. King <kingaa at umich dot edu>

## References

W. H. Press, S. A. Teukolsky, W. T. Vetterling, \& B. P. Flannery, Numerical Recipes in C, Cambridge University Press, 1992

#### See Also

```
sliceDesign, profileDesign
```

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#### **Examples**

```
plot(sobol(vars=list(a=c(0,1),b=c(100,200)),100))
plot(sobolDesign(lower=c(a=0,b=100),upper=c(b=200,a=1),100))
```

spect

Power spectrum computation for partially-observed Markov processes.

## **Description**

spect estimates the power spectrum of time series data and model simulations and compares the results. It can be used to diagnose goodness of fit and/or as the basis for frequency-domain parameter estimation (spect.match).

spect.match tries to match the power spectrum of the model to that of the data. It calls an optimizer to adjust model parameters to minimize the discrepancy between simulated and actual data.

## Usage

#### **Arguments**

object	An object of class pomp.
params	optional named numeric vector of model parameters. By default, params=coef(object).
vars	optional; names of observed variables for which the power spectrum will be computed. This must be a subset of rownames(obs(object)). By default, the spectrum will be computed for all observables.
kernel.width	width parameter for the smoothing kernel used for calculating the estimate of the spectrum.
nsim	number of model simulations to be computed.

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seed	optional; if non-NULL, the random number generator will be initialized with this seed for simulations. See simulate-pomp.
transform	function; this transformation will be applied to the observables prior to estimation of the spectrum, and prior to any detrending.
detrend	de-trending operation to perform. Options include no detrending, and subtraction of constant, linear, and quadratic trends from the data. Detrending is applied to each data series and to each model simulation independently.
weights	optional. The mismatch between model and data is measured by a weighted average of mismatch at each frequency. By default, all frequencies are weighted equally. weights can be specified either as a vector (which must have length equal to the number of frequencies) or as a function of frequency. If the latter, weights(freq) must return a nonnegative weight for each frequency.
start	named numeric vector; the initial guess of parameters.
est	character vector; the names of parameters to be estimated.
method	Optimization method. Choices are subplex and any of the methods used by optim.
verbose	logical; print diagnostic messages?
eval.only	logical; if TRUE, no optimization is attempted. Instead, the probe-mismatch value is simply evaluated at the start parameters.
fail.value	optional scalar; if non-NA, this value is substituted for non-finite values of the
	objective function.

#### **Details**

A call to spect results in the estimation of the power spectrum for the (transformed, detrended) data and nsim model simulations. The results of these computations are stored in an object of class spect.pomp.

A call to spect.match results in an attempt to optimize the agreement between model and data spectrum over the parameters named in est. The results, including coefficients of the fitted model and power spectra of fitted model and data, are stored in an object of class spect.matched.pomp.

#### Value

spect returns an object of class spect.pomp, which is derived from class pomp and therefore has all the slots of that class. In addition, spect.pomp objects have the following slots:

kernel.width width parameter of the smoothing kernel used.

transform transformation function used.

freq numeric vector of the frequencies at which the power spectrum is estimated.

datspec, simspec estimated power spectra for data and simulations, respectively.

**pvals** one-sided p-values: fraction of the simulated spectra that differ more from the mean simulated spectrum than does the data. The metric used is  $L^2$  distance.

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detrend detrending option used.

spect.match returns an object of class spect.matched.pomp, which is derived from class {spect.pomp}
and therefore has all the slots of that class. In addition, spect.matched.pomp objects have the following slots:

est, weights, fail.value values of the corresponding arguments in the call to spect.match.

evals number of function and gradient evaluations by the optimizer. See optim.

value Value of the objective function.

convergence, msg Convergence code and message from the optimizer. See optim.

#### Author(s)

Daniel C. Reuman (d.reuman at imperial dot ac dot uk)

Cai GoGwilt

Aaron A. King (kingaa at umich dot edu)

#### References

D.C. Reuman, R.A. Desharnais, R.F. Costantino, O. Ahmad, J.E. Cohen (2006) Power spectra reveal the influence of stochasticity on nonlinear population dynamics. *Proceedings of the National Academy of Sciences* **103**, 18860-18865.

D.C. Reuman, R.F. Costantino, R.A. Desharnais, J.E. Cohen (2008) Color of environmental noise affects the nonlinear dynamics of cycling, stage-structured populations. *Ecology Letters*, **11**, 820-830.

#### See Also

pomp-class, pomp-methods, probe, probe.match

## **Examples**

```
data(ou2)
good <- spect(</pre>
               ou2,
               vars=c("y1","y2"),
               kernel.width=3,
               detrend="mean",
               nsim=500
summary(good)
plot(good)
ou2.bad <- ou2
coef(ou2.bad, c("x1.0", "x2.0", "alpha.1", "alpha.4")) <- c(0,0,0.1,0.2)
bad <- spect(</pre>
              ou2.bad,
              vars=c("y1","y2"),
              kernel.width=3,
              detrend="mean",
```

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```
nsim=500
)
summary(bad)
plot(bad)
```

traj.match

Trajectory matching

# Description

Facilities for matching trajectories to data. Trajectory matching is equivalent to maximum likelihood estimation under the assumption that process noise is entirely absent, i.e., that all stochasticity is measurement error.

# Usage

# Arguments

object	A pomp object. If object has no skeleton slot, an error will be generated.
start	named numeric vector containing an initial guess for parameters. By default start=coef(object) if the latter exists.
params	optional named numeric vector of parameters. This should contain all parameters needed by the skeleton and dmeasure slots of object. In particular, any parameters that are to be treated as fixed should be present here. Parameter values given in params for parameters named in est will be ignored. By default, params=coef(object) if the latter exists.
est	character vector containing the names of parameters to be estimated. In the case of traj.match.objfun, the objective function that is constructed will assume that its argument contains the parameters in this order.
method	Optimization method. Choices are subplex, "sannbox", and any of the methods used by optim.
gr	Passed to optim.
eval.only	logical; if TRUE, no optimization is attempted and the log likelihood value is evaluated at the start parameters.
transform	logical; if TRUE, optimization is performed on the transformed scale.
	Arguments that will be passed to optim, subplex or sannbox, via their control lists.

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#### **Details**

In **pomp**, trajectory matching is the term used for maximizing the likelihood of the data under the assumption that there is no process noise. Specifically, traj.match calls an optimizer (optim, subplex, and sannbox are the currently supported options) to minimize an objective function. For any value of the model parameters, this objective function is calculated by

- computing the deterministic trajectory of the model given the parameters. This is the trajectory returned by trajectory, which relies on the model's deterministic skeleton as specified in the construction of the pomp object object.
- evaluating the negative log likelihood of the data under the measurement model given the
  deterministic trajectory and the model parameters. This is accomplished via the model's
  dmeasure slot. The negative log likelihood is the objective function's value.

The objective function itself — in a form suitable for use with optim-like optimizers — is created by a call to traj.match.objfun. Specifically, traj.match.objfun will return a function that takes a single numeric-vector argument that is assumed to cotain the parameters named in est, in that order.

#### Value

traj.match returns an object of class traj.matched.pomp. This class inherits from class pomp and contains the following additional slots:

transform, est the values of these arguments on the call to traj.match.

evals number of function and gradient evaluations by the optimizer. See optim.

**value** value of the objective function. Larger values indicate better fit (i.e., traj.match attempts to maximize this quantity.

convergence, msg convergence code and message from the optimizer. See optim.

Available methods for objects of this type include summary and logLik. The other slots of this object can be accessed via the \$ operator.

traj.match.objfun returns a function suitable for use as an objective function in an optim-like optimizer.

# See Also

trajectory, pomp, optim, subplex

## **Examples**

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```
res <- traj.match(</pre>
 simdata,
 start=guess.p,
  est=c('alpha.1', 'alpha.3', 'alpha.4', 'x1.0', 'x2.0', 'tau'),
 maxit=2000,
 method="Nelder-Mead",
 reltol=1e-8
summary(res)
plot(range(time(res)),range(c(obs(res),states(res))),type='n',xlab="time",ylab="x,y")
points(y1~time,data=as(res,"data.frame"),col='blue')
points(y2~time,data=as(res,"data.frame"),col='red')
lines(x1~time,data=as(res,"data.frame"),col='blue')
lines(x2~time,data=as(res,"data.frame"),col='red')
data(ricker)
ofun <- traj.match.objfun(ricker,est=c("log.r","log.phi"),transform=TRUE)</pre>
optim(fn=ofun,par=c(2,0),method="BFGS")
```

trajectory

Compute trajectories of the determinstic skeleton.

## **Description**

The method trajectory computes a trajectory of the deterministic skeleton of a Markov process. In the case of a discrete-time system, the deterministic skeleton is a map and a trajectory is obtained by iterating the map. In the case of a continuous-time system, the deterministic skeleton is a vector-field; trajectory integrates the vectorfield to obtain a trajectory.

## Usage

```
## S4 method for signature 'pomp'
trajectory(object, params, times, t0, as.data.frame = FALSE, ...)
```

#### **Arguments**

object	an object of class pomp.
params	a rank-2 array of parameters. Each column of params is a distinct parameter vector.
times, t0	times is a numeric vector specifying the times at which a trajectory is desired. to specifies the start time (the time at which the initial conditions hold). The default for times is times=time(object, t0=FALSE) and t0=timezero(object), respectively.
as.data.frame	logical; if TRUE, return the result as a data-frame.
	additional arguments are passed to the ODE integrator if the skeleton is a vectorfield and ignored if it is a map. See ode for a description of the additional arguments accepted.

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#### **Details**

This function makes repeated calls to the user-supplied skeleton of the pomp object. For specifications on supplying this, see pomp.

When the skeleton is a vectorfield, trajectory integrates it using ode.

When the skeleton is a map, trajectory iterates it. By default, time is advanced 1 unit per iteration. The user can change this behavior by specifying the desired timestep using the argument skelmap.delta.t in the construction of the pomp object.

#### Value

Returns an array of dimensions nvar x nreps x ntimes. If x is the returned matrix, x[i,j,k] is the i-th component of the state vector at time times[k] given parameters params[,j].

#### Author(s)

```
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```

#### See Also

```
pomp, traj.match, ode
```

## **Examples**

```
data(euler.sir)
x <- trajectory(euler.sir)
plot(time(euler.sir),x["I",1,],type='1',xlab='time',ylab='I')
lines(time(euler.sir),x["cases",1,],col='red')

coef(euler.sir,c("gamma")) <- log(12)
x <- trajectory(euler.sir)
plot(time(euler.sir),x["I",1,],type='1',xlab='time',ylab='I')
lines(time(euler.sir),x["cases",1,],col='red')

x <- trajectory(euler.sir,as.data.frame=TRUE)</pre>
```

verhulst

Simple Verhulst-Pearl (logistic) model.

#### Description

verhulst is a pomp object encoding a univariate stochastic logistic model with measurement error.

#### **Usage**

```
data(verhulst)
```

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## **Details**

The model is written as an Ito diffusion,  $dn = rn(1 - n/K)dt + \sigma ndW$ , where W is a Wiener process. It is implemented using the euler.sim plug-in.

# See Also

```
pomp-class and the vignettes
```

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