

USING COMPILED CODE IN POMP

AARON A. KING

CONTENTS

1. A two-dimensional Ornstein-Uhlenbeck process. 1

1. A TWO-DIMENSIONAL ORNSTEIN-UHLENBECK PROCESS.

Let's look again at our example of the discrete-time 2-D Ornstein-Uhlenbeck process with normal measurement error. Recall that the unobserved Ornstein-Uhlenbeck (OU) process $X_t \in \mathbb{R}^2$ satisfies

$$X_t = A X_{t-1} + \xi_t.$$

The observation process is

$$Y_t = B X_t + \varepsilon_t.$$

In these equations, A and B are 2×2 constant matrices; ξ_t and ε_t are mutually-independent families of i.i.d. bivariate normal random variables. We let $\sigma\sigma^T$ be the variance-covariance matrix of ξ_t , where σ is lower-triangular; likewise, we let $\tau\tau^T$ be that of ε_t .

Since many of the methods we will use require us to simulate the process and/or measurement models many times, it is a good idea to use native (compiled) codes for the computational heavy lifting. This can result in many-fold speedup. The package includes some C codes that were written to implement the OU example. Read the source (file 'ou2.c') for details.

```
ou2.rprocess <- function(xstart, times, params,
  paramnames, ...) {
  nvar <- nrow(xstart)
  npar <- nrow(params)
  nrep <- ncol(xstart)
  ntimes <- length(times)
  parindex <- match(paramnames, rownames(params)) -
    1
  array(.C("ou2_adv", X = double(nvar * nrep *
    ntimes), xstart = as.double(xstart), par = as.double(params),
    times = as.double(times), n = as.integer(c(nvar,
      npar, nrep, ntimes)), parindex = as.integer(parindex),
    DUP = FALSE, NAOK = TRUE, PACKAGE = "pomp")$X,
    dim = c(nvar, nrep, ntimes), dimnames = list(rownames(xstart),
      NULL, NULL))
}
```

```
ou2.dprocess <- function(x, times, params, log,
  ...) {
  nvar <- nrow(x)
  npar <- nrow(params)
```

```

nrep <- ncol(x)
ntimes <- length(times)
parindex <- match(paramnames, rownames(params)) -
  1
array(.C("ou2_pdf", d = double(nrep * (ntimes -
  1)), X = as.double(x), par = as.double(params),
  times = as.double(times), n = as.integer(c(nvar,
    npar, nrep, ntimes)), parindex = as.integer(parindex),
  give_log = as.integer(log), DUP = FALSE,
  NAOK = TRUE, PACKAGE = "pomp")$d, dim = c(nrep,
  ntimes - 1))
}
ou2 <- pomp(times = seq(1, 100), data = rbind(y1 = rep(0,
  100), y2 = rep(0, 100)), t0 = 0, rprocess = ou2.rprocess,
  dprocess = ou2.dprocess, dmeasure = "normal_dmeasure",
  rmeasure = "normal_rmeasure", obsnames = c("y1",
  "y2"), paramnames = c("alpha.1", "alpha.2",
  "alpha.3", "alpha.4", "sigma.1", "sigma.2",
  "sigma.3", "tau"), statenames = c("x1",
  "x2"))

```

We'll specify some parameters:

```

p <- c(alpha.1 = 0.9, alpha.2 = 0, alpha.3 = 0,
  alpha.4 = 0.99, sigma.1 = 1, sigma.2 = 0,
  sigma.3 = 2, tau = 1, x1.0 = 50, x2.0 = -50)

tic <- Sys.time()
ou2 <- simulate(ou2, params = p, nsim = 1000,
  seed = 800733088)
toc <- Sys.time()
print(toc - tic)

```

Time difference of 3.835489 secs

Fig. 1 plots the data.

The `pomp` object we just created is included in the package: use `data(ou2)` to retrieve it.

A. A. KING, DEPARTMENTS OF ECOLOGY & EVOLUTIONARY BIOLOGY AND MATHEMATICS, UNIVERSITY OF MICHIGAN, ANN ARBOR, MICHIGAN 48109-1048 USA

E-mail address: kingaa at umich dot edu

URL: <http://www.umich.edu/~kingaa>

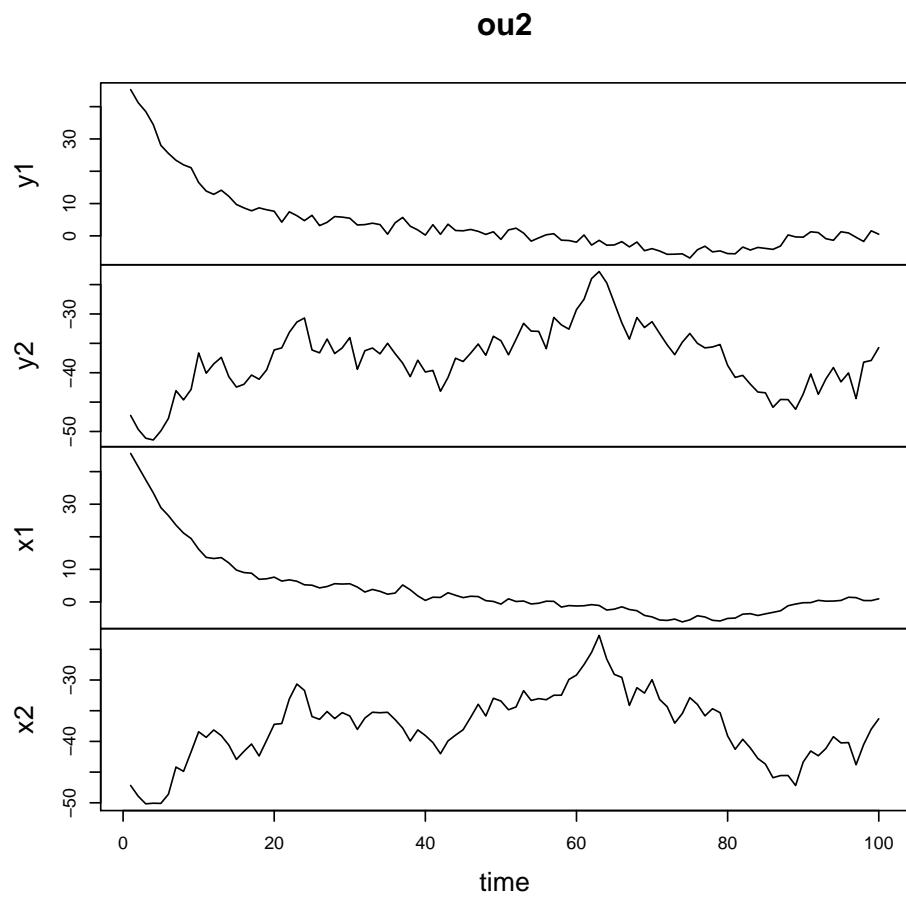


FIGURE 1. One realization of the two-dimensional OU process.