BME 6310 - Homework 1

Problem 1

Here is my function new_matrices(). The function leverages the numpy package to handle basic matrix manipulation and concatenation:

```
def new_matrices(n: int) -> list[npt.ArrayLike, npt.ArrayLike]:
    # create ones array
A = np.ones(shape=(n,n), dtype="int")

# create equivalent zeros array
A_zeros = np.zeros(shape=(n,n), dtype="int")

# block arrays rogether
A_new = np.block(
    [
        [A, A_zeros],
        [A_zeros, A]
    ]
)

return [A, A_new]
```

Here is the following code used to test my function

```
[A, A_new] = new_matrices(6)

print(A)
print(A_new)
```

The following output is achieved when running the above test code

```
[[1 1 1 1 1 1 1]

[1 1 1 1 1 1]

[1 1 1 1 1 1]

[1 1 1 1 1 1]

[1 1 1 1 1 1]

[1 1 1 1 1 1]]

[[1 1 1 1 1 1 0 0 0 0 0 0]

[1 1 1 1 1 1 0 0 0 0 0 0]
```

```
[1 1 1 1 1 1 1 0 0 0 0 0 0 0]
[1 1 1 1 1 1 1 0 0 0 0 0 0 0]
[1 1 1 1 1 1 1 1 0 0 0 0 0 0 0]
[0 0 0 0 0 0 1 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 1 1 1 1 1 1 1]
[0 0 0 0 0 0 0 1 1 1 1 1 1 1]
```

Problem 2

To plot the function $f(x)=3xcos^2(x)-2x$ and its derivative (see below) I am using the matplotlib package here.

Equation 1

$$rac{d}{dx}f(x)=rac{d}{dx}[3xcos^2(x)-2x]=f'(x)=3cos^2(x)-6xsin(x)cos(x)-2$$

The following functions were written for f(x) and $f^{\prime}(x)$ respectively:

```
def f_x(x: float) -> float:
    """
    f(x) = 3xcos^2(x) - 2x
    """
    return 3*x*(math.cos(x)**2) - 2*x

def f_prime_x(x: float) -> float:
    """
    f'(x) = 3cos^2(x) - 6xsin(x)cos(x) - 2
    """
    return 3*(math.cos(x)**2) - 6*x*math.sin(x)*math.cos(x) - 2
```

Leveraging these functions I created a list of data points to be plotted with matplotlib:

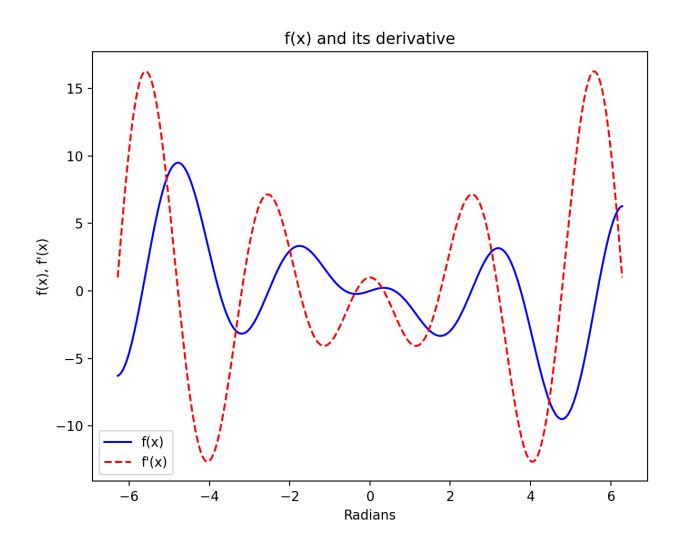
```
points = 10000 #Number of points
xmin = math.pi*-2
xmax = math.pi*2

# calculate
xlist = np.linspace(xmin, xmax, num=points)
ylist = [f_x(x) for x in xlist]
y_prime_list = [f_prime_x(x) for x in xlist]
```

```
# plot and annotate
plt.plot(xlist, ylist, 'b')
plt.plot(xlist, y_prime_list, 'r--')
plt.title("f(x) and its derivative")
plt.xlabel("Radians")
plt.ylabel("f(x), f'(x)")
plt.legend(['f(x)', "f'(x)"])
plt.show()
```

The following plot was generated:

Figure 1.



Problem 3

To plot the equation $A_v=\frac{Q}{\sqrt{PG}}$ I used a similar approach as in problem 2. A user-defined function was created to calculate the area of the aortic valve:

```
def aoritc_valve_area(pg: float, Q: float) -> float:
    """
    Function to estimate the area of the aortic valve.

Av = Q/sqrt(PG), where

Q is the cardiac output and PG is the difference between the left ventricular systolic pressure and the aortic systolic pressure.
    """
    return Q/math.sqrt(pg)
```

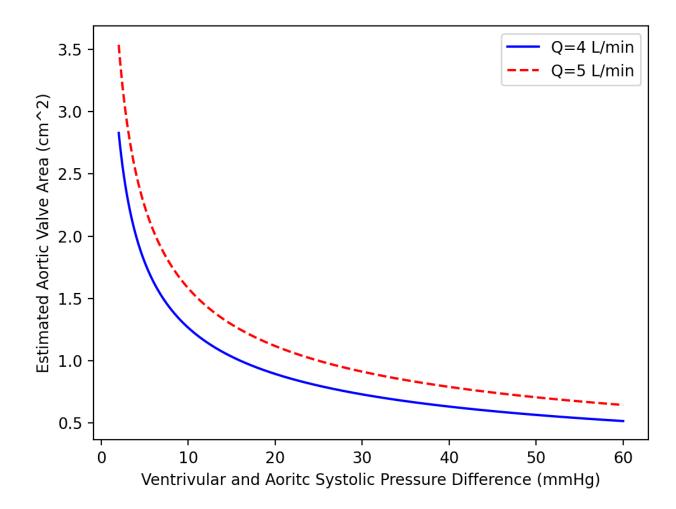
Similarly, points were calculated using this function be plugging in values for Q, the cardiac output:

```
points: int = 10000 #Number of points
PGmin: float = 2
PGmax: float = 60

# calculate
xlist = np.linspace(PGmin, PGmax, num=points)
q_4 = [aoritc_valve_area(pg, 4) for pg in xlist]
q_5 = [aoritc_valve_area(pg, 5) for pg in xlist]

# plot and annotate
plt.plot(xlist, q_4, 'b')
plt.plot(xlist, q_5, 'r--')
plt.xlabel("Ventrivular and Aoritc Systolic Pressure Difference (mmHg)")
plt.ylabel("Estimated Aortic Valve Area (cm^2)")
plt.legend(['Q=4 L/min', 'Q=5 L/min'])
plt.show()
```

This produced the following plots:



Problem 4

My lab is highly concerned with gene regulation and how the epigenome contributes to dysregulation and subsequent disease pathologies and progression. Of importance is a phenomenon known as **CpG Islands**. In brief, CpG islands are regions of DNA with a high G+C content and a high frequency of CpG dinucleotides relative to the bulk genome. These islands have great implications on gene expression and regulation. As such, their detection could prove highly useful. A definition for what constitutes a CpG islands was laid out in [@gardiner-gardenCpGIslandsVertebrate1987]. The authors define a CpG island as a sequence "window" that exhibits the following properties:

- 1. The GC Content of a sequence window must be greater than 50% ${N_{GC} \over N_{tot}} imes 100 > 50$
- 2. The ratio of observed CpG dimers to the expected number of CpG dimers must be greater than 0.6

$$rac{Obs}{Exp} > 0.6 = rac{N_{cg}}{N_c N_g} imes N_{tot} > 0.6$$

To this end, I wrote a function that will accept flasta files as an input and it will report on any sequence window's it detects to be a CpG island according to the above criterion. The function is quite simple and written below:

```
def cpg_island_detect(filename: str, window: int = 200, verbose: bool = False) ->
list[dict]:
    CpG island detector. Will take an input .fasta file and
    search the sequence space for CpG islands using the method
    described by Gardiner-Garden and Frommer (1987).
    Searches the sequence in windows of 200 bp moving forward in 1bp
    increments. CpG islands are defined as sequence ranges where the
    Obs/Exp value is greater than 0.6 and the GC content is greater
    than 50%.
    The expected number of CpG dimers in a window is calculated as the
    number of 'C's in the window multiplied by the number of 'G's in
    the window, divided by the window length. CpG islands are often
    found in the 5' regions of vertebrate genes, therefore this program
    can be used to highlight potential genes in genomic sequences.
    :param: - filename (str) - path to .fasta file
    :param: - window (int) - optional. window length to search
    :return: - list of dictionaries that contain CpG island location
               (start and end bp), GC content, and Obs/Exp value
    cpg_islands: list[dict] = []
    # extract sequence from file
    seq = read fasta file(filename)
    for i in range(len(seq)+1 - window):
        # get sequence window
        seq window = seq[i:i+window]
        # calc parameters
        obs exp =
seq_window.count('cg')/(seq_window.count('c')*seq_window.count('g'))*window
        gc content = (seq window.count('c') + seq window.count('g'))/window
        # check parameters
        if obs exp > 0.6 and gc content > 0.5:
            # append new detected CpG island detection
```

```
cpg_islands.append({
    'start': i+1,
    'end': i+window+1,
    'gc_content': gc_content,
    'obs_exp': obs_exp
})

# output results
if verbose:
    print('----> Cpg Island Detected!')
    print(f"----> \tStart: {i+1}")
    print(f"----> \tEnd: {i+window+1}")
    print(f"----> \tGC Content: {round(gc_content*100,2)}%")
    print(f"----> \tObs/Exp Val: {round(obs_exp,2)}")
    print("")
```