

# Deep Generative Models

## Lecture 5

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# Recap of previous lecture

## Jacobian matrix

Let  $f : \mathbb{R}^m \rightarrow \mathbb{R}^m$  be a differentiable function.

$$\mathbf{z} = f(\mathbf{x}), \quad \mathbf{J} = \frac{\partial \mathbf{z}}{\partial \mathbf{x}} = \begin{pmatrix} \frac{\partial z_1}{\partial x_1} & \cdots & \frac{\partial z_1}{\partial x_m} \\ \vdots & \ddots & \vdots \\ \frac{\partial z_m}{\partial x_1} & \cdots & \frac{\partial z_m}{\partial x_m} \end{pmatrix} \in \mathbb{R}^{m \times m}$$

## Change of variable theorem (CoV)

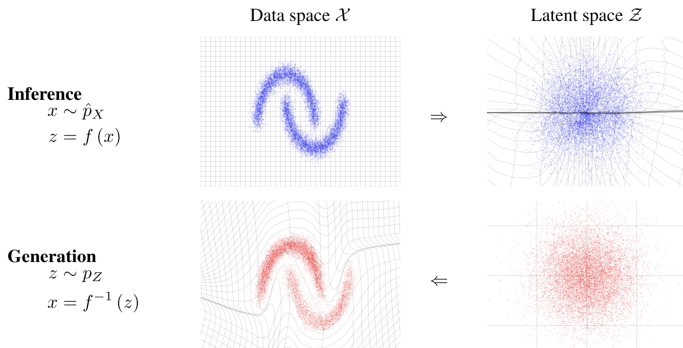
Let  $\mathbf{x}$  be a random variable with density function  $p(\mathbf{x})$  and  $f : \mathbb{R}^m \rightarrow \mathbb{R}^m$  is a differentiable, invertible function (diffeomorphism). If  $\mathbf{z} = f(\mathbf{x})$ ,  $\mathbf{x} = f^{-1}(\mathbf{z}) = g(\mathbf{z})$ , then

$$p(\mathbf{x}) = p(\mathbf{z}) |\det(\mathbf{J}_f)| = p(\mathbf{z}) \left| \det \left( \frac{\partial \mathbf{z}}{\partial \mathbf{x}} \right) \right| = p(f(\mathbf{x})) \left| \det \left( \frac{\partial f(\mathbf{x})}{\partial \mathbf{x}} \right) \right|$$
$$p(\mathbf{z}) = p(\mathbf{x}) |\det(\mathbf{J}_g)| = p(\mathbf{x}) \left| \det \left( \frac{\partial \mathbf{x}}{\partial \mathbf{z}} \right) \right| = p(g(\mathbf{z})) \left| \det \left( \frac{\partial g(\mathbf{z})}{\partial \mathbf{z}} \right) \right|.$$

# Recap of previous lecture

## Definition

Normalizing flow is a *differentiable, invertible* mapping from data  $\mathbf{x}$  to the noise  $\mathbf{z}$ .



## Log likelihood

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \log p(f_K \circ \dots \circ f_1(\mathbf{x})) + \sum_{k=1}^K \log |\det(\mathbf{J}_{f_k})|$$

# Recap of previous lecture

## Forward KL for flow model

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \log p(f(\mathbf{x}, \boldsymbol{\theta})) + \log |\det(\mathbf{J}_f)|$$

## Reverse KL for flow model

$$KL(p||\pi) = \mathbb{E}_{p(\mathbf{z})} [\log p(\mathbf{z}) - \log |\det(\mathbf{J}_g)| - \log \pi(g(\mathbf{z}, \boldsymbol{\theta}))]$$

## Flow KL duality

$$\arg \min_{\boldsymbol{\theta}} KL(\pi(\mathbf{x})||p(\mathbf{x}|\boldsymbol{\theta})) = \arg \min_{\boldsymbol{\theta}} KL(p(\mathbf{z}|\boldsymbol{\theta})||p(\mathbf{z}))$$

- ▶  $p(\mathbf{z})$  is a base distribution;  $\pi(\mathbf{x})$  is a data distribution;
- ▶  $\mathbf{z} \sim p(\mathbf{z})$ ,  $\mathbf{x} = g(\mathbf{z}, \boldsymbol{\theta})$ ,  $\mathbf{x} \sim p(\mathbf{x}|\boldsymbol{\theta})$ ;
- ▶  $\mathbf{x} \sim \pi(\mathbf{x})$ ,  $\mathbf{z} = f(\mathbf{x}, \boldsymbol{\theta})$ ,  $\mathbf{z} \sim p(\mathbf{z}|\boldsymbol{\theta})$ .

# Recap of previous lecture

## Flow log-likelihood

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \log p(f(\mathbf{x}, \boldsymbol{\theta})) + \log |\det(\mathbf{J}_f)|$$

The main challenge is a determinant of the Jacobian.

## Linear flows

$$\mathbf{z} = f(\mathbf{x}, \boldsymbol{\theta}) = \mathbf{W}\mathbf{x}, \quad \mathbf{W} \in \mathbb{R}^{m \times m}, \quad \boldsymbol{\theta} = \mathbf{W}, \quad \mathbf{J}_f = \mathbf{W}^T$$

- ▶ LU-decomposition

$$\mathbf{W} = \mathbf{P}\mathbf{L}\mathbf{U}.$$

- ▶ QR-decomposition

$$\mathbf{W} = \mathbf{Q}\mathbf{R}.$$

Decomposition should be done only once in the beginning. Next, we fit decomposed matrices (**P/L/U** or **Q/R**).

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*Kingma D. P., Dhariwal P. Glow: Generative Flow with Invertible 1x1 Convolutions, 2018*

*Hoogeboom E., et al. Emerging convolutions for generative normalizing flows, 2019*

# Recap of previous lecture

Consider an autoregressive model

$$p(\mathbf{x}|\boldsymbol{\theta}) = \prod_{j=1}^m p(x_j|\mathbf{x}_{1:j-1}, \boldsymbol{\theta}), \quad p(x_j|\mathbf{x}_{1:j-1}, \boldsymbol{\theta}) = \mathcal{N}(\mu_j(\mathbf{x}_{1:j-1}), \sigma_j^2(\mathbf{x}_{1:j-1})).$$

## Gaussian autoregressive NF

$$\mathbf{x} = g(\mathbf{z}, \boldsymbol{\theta}) \quad \Rightarrow \quad x_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot z_j + \mu_j(\mathbf{x}_{1:j-1}).$$

$$\mathbf{z} = f(\mathbf{x}, \boldsymbol{\theta}) \quad \Rightarrow \quad z_j = (x_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_j(\mathbf{x}_{1:j-1})}.$$

- ▶ We have an **invertible** and **differentiable** transformation from  $p(\mathbf{z})$  to  $p(\mathbf{x}|\boldsymbol{\theta})$ .
- ▶ Jacobian of such transformation is triangular!

Generation function  $g(\mathbf{z}, \boldsymbol{\theta})$  is **sequential**.

Inference function  $f(\mathbf{x}, \boldsymbol{\theta})$  is **not sequential**.

# Gaussian autoregressive NF

$$\mathbf{x} = g(\mathbf{z}, \boldsymbol{\theta}) \Rightarrow x_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot z_j + \mu_j(\mathbf{x}_{1:j-1}).$$

$$\mathbf{z} = f(\mathbf{x}, \boldsymbol{\theta}) \Rightarrow z_j = (x_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_j(\mathbf{x}_{1:j-1})}.$$

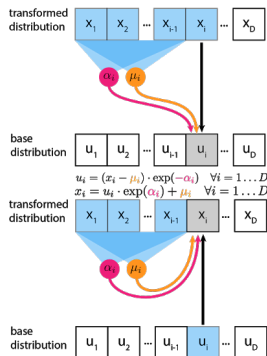
- ▶ Sampling is sequential, density estimation is parallel.
- ▶ Forward KL is a natural loss.

Forward transform:  $f(\mathbf{x}, \boldsymbol{\theta})$

$$z_j = (x_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_j(\mathbf{x}_{1:j-1})}$$

Inverse transform:  $g(\mathbf{z}, \boldsymbol{\theta})$

$$x_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot z_j + \mu_j(\mathbf{x}_{1:j-1})$$



# Outline

1. RealNVP: coupling layer
2. Normalizing flows as VAE model
3. Discrete data vs continuous model
  - Discretization of continuous distribution
  - Dequantization of discrete data



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# RealNVP

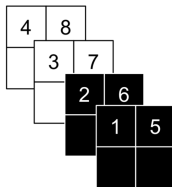
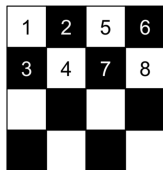
Let split  $\mathbf{x}$  and  $\mathbf{z}$  in two parts:

$$\mathbf{x} = [\mathbf{x}_1, \mathbf{x}_2] = [\mathbf{x}_{1:d}, \mathbf{x}_{d+1:m}]; \quad \mathbf{z} = [\mathbf{z}_1, \mathbf{z}_2] = [\mathbf{z}_{1:d}, \mathbf{z}_{d+1:m}].$$

## Coupling layer

$$\begin{cases} \mathbf{x}_1 = \mathbf{z}_1; \\ \mathbf{x}_2 = \mathbf{z}_2 \odot \sigma(\mathbf{z}_1, \theta) + \mu(\mathbf{z}_1, \theta). \end{cases} \quad \begin{cases} \mathbf{z}_1 = \mathbf{x}_1; \\ \mathbf{z}_2 = (\mathbf{x}_2 - \mu(\mathbf{x}_1, \theta)) \odot \frac{1}{\sigma(\mathbf{x}_1, \theta)}. \end{cases}$$

## Image partitioning



- ▶ Checkerboard ordering uses masking.
- ▶ Channelwise ordering uses splitting.

# RealNVP

## Coupling layer

$$\begin{cases} \mathbf{x}_1 = \mathbf{z}_1; \\ \mathbf{x}_2 = \mathbf{z}_2 \odot \sigma(\mathbf{z}_1, \theta) + \mu(\mathbf{z}_1, \theta). \end{cases} \quad \begin{cases} \mathbf{z}_1 = \mathbf{x}_1; \\ \mathbf{z}_2 = (\mathbf{x}_2 - \mu(\mathbf{x}_1, \theta)) \odot \frac{1}{\sigma(\mathbf{x}_1, \theta)}. \end{cases}$$

Estimating the density takes 1 pass, sampling takes 1 pass!

## Jacobian

$$\det \left( \frac{\partial \mathbf{z}}{\partial \mathbf{x}} \right) = \det \begin{pmatrix} \mathbf{I}_d & 0_{d \times m-d} \\ \frac{\partial \mathbf{z}_2}{\partial \mathbf{x}_1} & \frac{\partial \mathbf{z}_2}{\partial \mathbf{x}_2} \end{pmatrix} = \prod_{j=1}^{m-d} \frac{1}{\sigma_j(\mathbf{x}_1, \theta)}.$$

## Gaussian AR NF

$$\mathbf{x} = g(\mathbf{z}, \theta) \quad \Rightarrow \quad \mathbf{x}_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot \mathbf{z}_j + \mu_j(\mathbf{x}_{1:j-1}).$$

$$\mathbf{z} = f(\mathbf{x}, \theta) \quad \Rightarrow \quad \mathbf{z}_j = (\mathbf{x}_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_j(\mathbf{x}_{1:j-1})}.$$

How to get RealNVP coupling layer from gaussian AR NF?

## Glow samples

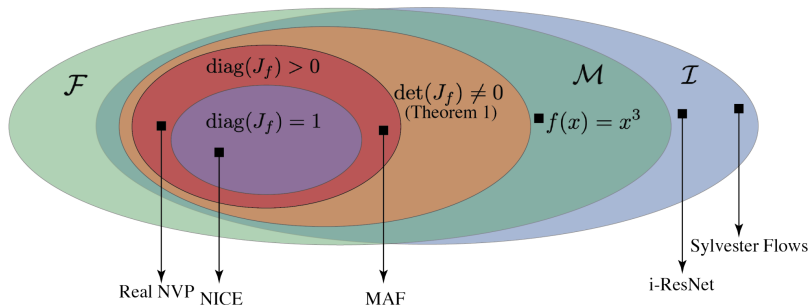
Glow model: coupling layer + linear flows (1x1 convs)



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Kingma D. P., Dhariwal P. *Glow: Generative Flow with Invertible 1x1 Convolutions*, 2018

# Venn diagram for Normalizing flows



- ▶  $\mathcal{I}$  – invertible functions.
- ▶  $\mathcal{F}$  – continuously differentiable functions whose Jacobian is lower triangular.
- ▶  $\mathcal{M}$  – invertible functions from  $\mathcal{F}$ .

# Outline

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2. Normalizing flows as VAE model
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# VAE vs Normalizing flows

	VAE	NF
Objective	ELBO $\mathcal{L}$	Forward KL/MLE
Encoder	stochastic $\mathbf{z} \sim q(\mathbf{z} \mathbf{x}, \phi)$	deterministic $\mathbf{z} = f(\mathbf{x}, \theta)$ $q(\mathbf{z} \mathbf{x}, \theta) = \delta(\mathbf{z} - f(\mathbf{x}, \theta))$
Decoder	stochastic $\mathbf{x} \sim p(\mathbf{x} \mathbf{z}, \theta)$	deterministic $\mathbf{x} = g(\mathbf{z}, \theta)$ $p(\mathbf{x} \mathbf{z}, \theta) = \delta(\mathbf{x} - g(\mathbf{z}, \theta))$
Parameters	$\phi, \theta$	$\theta \equiv \phi$

## Theorem

MLE for normalizing flow is equivalent to maximization of ELBO for VAE model with deterministic encoder and decoder:

$$p(\mathbf{x}|\mathbf{z}, \theta) = \delta(\mathbf{x} - f^{-1}(\mathbf{z}, \theta)) = \delta(\mathbf{x} - g(\mathbf{z}, \theta));$$

$$q(\mathbf{z}|\mathbf{x}, \theta) = p(\mathbf{z}|\mathbf{x}, \theta) = \delta(\mathbf{z} - f(\mathbf{x}, \theta)).$$

# Normalizing flow as VAE

## Proof

1. Dirac delta function property

$$\mathbb{E}_{\delta(\mathbf{x}-\mathbf{y})} f(\mathbf{x}) = \int \delta(\mathbf{x}-\mathbf{y}) f(\mathbf{x}) d\mathbf{x} = f(\mathbf{y}).$$

2. CoV theorem and Bayes theorem:

$$p(\mathbf{x}|\boldsymbol{\theta}) = p(\mathbf{z}) |\det(\mathbf{J}_f)|;$$

$$p(\mathbf{z}|\mathbf{x}, \boldsymbol{\theta}) = \frac{p(\mathbf{x}|\mathbf{z}, \boldsymbol{\theta}) p(\mathbf{z})}{p(\mathbf{x}|\boldsymbol{\theta})}; \quad \Rightarrow \quad p(\mathbf{x}|\mathbf{z}, \boldsymbol{\theta}) = p(\mathbf{z}|\mathbf{x}, \boldsymbol{\theta}) |\det(\mathbf{J}_f)|.$$

3. Log-likelihood decomposition

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \mathcal{L}(\boldsymbol{\theta}) + KL(q(\mathbf{z}|\mathbf{x}, \boldsymbol{\theta}) || p(\mathbf{z}|\mathbf{x}, \boldsymbol{\theta})) = \mathcal{L}(\boldsymbol{\theta}).$$



# Normalizing flow as VAE

## Proof

ELBO objective:

$$\begin{aligned}\mathcal{L} &= \mathbb{E}_{q(\mathbf{z}|\mathbf{x},\theta)} \left[ \log p(\mathbf{x}|\mathbf{z},\theta) - \log \frac{q(\mathbf{z}|\mathbf{x},\theta)}{p(\mathbf{z})} \right] \\ &= \mathbb{E}_{q(\mathbf{z}|\mathbf{x},\theta)} \left[ \log \frac{p(\mathbf{x}|\mathbf{z},\theta)}{q(\mathbf{z}|\mathbf{x},\theta)} + \log p(\mathbf{z}) \right].\end{aligned}$$

1. Dirac delta function property:

$$\mathbb{E}_{q(\mathbf{z}|\mathbf{x},\theta)} \log p(\mathbf{z}) = \int \delta(\mathbf{z} - f(\mathbf{x},\theta)) \log p(\mathbf{z}) d\mathbf{z} = \log p(f(\mathbf{x},\theta)).$$

2. CoV theorem and Bayes theorem:

$$\mathbb{E}_{q(\mathbf{z}|\mathbf{x},\theta)} \log \frac{p(\mathbf{x}|\mathbf{z},\theta)}{q(\mathbf{z}|\mathbf{x},\theta)} = \mathbb{E}_{q(\mathbf{z}|\mathbf{x},\theta)} \log \frac{p(\mathbf{z}|\mathbf{x},\theta) |\det(\mathbf{J}_f)|}{q(\mathbf{z}|\mathbf{x},\theta)} = \log |\det \mathbf{J}_f|.$$

3. Log-likelihood decomposition

$$\log p(\mathbf{x}|\theta) = \mathcal{L}(\theta) = \log p(f(\mathbf{x},\theta)) + \log |\det \mathbf{J}_f|.$$

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## Discrete data vs continuous model

Let our data  $\mathbf{y}$  comes from discrete distribution  $\Pi(\mathbf{y})$  and we have continuous model  $p(\mathbf{x}|\theta) = \text{NN}(\mathbf{x}, \theta)$ .

- ▶ Images (and not only images) are discrete data, pixels lie in the integer domain  $\{0, 255\}$ .
- ▶ By fitting a continuous density model  $p(\mathbf{x}|\theta)$  to discrete data  $\Pi(\mathbf{y})$ , one can produce a degenerate solution with all probability mass on discrete values.

## Discrete model

- ▶ Use **discrete** model (e.x.  $P(\mathbf{y}|\theta) = \text{Cat}(\pi(\theta))$ ).
- ▶ Minimize any suitable divergence measure  $D(\Pi, P)$ .
- ▶ NF works only with continuous data  $\mathbf{x}$  (there are discrete NF, see papers below).
- ▶ If pixel value is not presented in the train data, it won't be predicted.

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*Hoogeboom E. et al. Integer discrete flows and lossless compression, 2019*

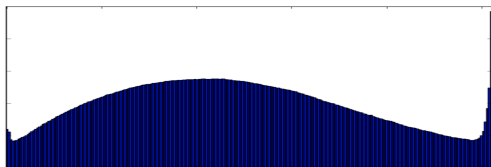
*Tran D. et al. Discrete flows: Invertible generative models of discrete data, 2019*

# Discrete data vs continuous model

## Continuous model

- ▶ Use **continuous** model (e.x.  $p(\mathbf{x}|\theta) = \mathcal{N}(\mu_{\theta}(\mathbf{x}), \sigma_{\theta}^2(\mathbf{x}))$ ), but
  - ▶ **discretize** model (make the model outputs discrete): transform  $p(\mathbf{x}|\theta)$  to  $P(\mathbf{y}|\theta)$ ;
  - ▶ **dequantize** data (make the data continuous): transform  $\Pi(\mathbf{y})$  to  $\pi(\mathbf{x})$ .
- ▶ Continuous distribution knows numerical relationships.

## CIFAR-10 pixel values distribution



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# Discretization of continuous distribution

## Model discretization through CDF

$$F(\mathbf{x}|\theta) = \int_{-\infty}^{\mathbf{x}} p(\mathbf{x}'|\theta) d\mathbf{x}'; \quad P(\mathbf{y}|\theta) = F(\mathbf{y} + 0.5|\theta) - F(\mathbf{y} - 0.5|\theta)$$

## Mixture of logistic distributions

$$p(x|\mu, s) = \frac{\exp^{-(x-\mu)/s}}{s(1 + \exp^{-(x-\mu)/s})^2}; \quad p(x|\pi, \mu, \mathbf{s}) = \sum_{k=1}^K \pi_k p(x|\mu_k, s_k).$$

## PixelCNN++

$$p(\mathbf{x}|\theta) = \prod_{j=1}^m p(x_j|\mathbf{x}_{1:j-1}, \theta); \quad p(x_j|\mathbf{x}_{1:j-1}, \theta) = \sum_{k=1}^K \pi_k p(x|\mu_k, s_k).$$

Here,  $\pi_k = \pi_{k,\theta}(\mathbf{x}_{1:j-1})$ ,  $\mu_k = \mu_{k,\theta}(\mathbf{x}_{1:j-1})$ ,  $s_k = s_{k,\theta}(\mathbf{x}_{1:j-1})$ .

For the pixel edge cases of 0, replace  $y - 0.5$  by  $-\infty$ , and for 255 replace  $y + 0.5$  by  $+\infty$ .

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Salimans T. et al. *PixelCNN++: Improving the PixelCNN with Discretized Logistic Mixture Likelihood and Other Modifications*, 2017

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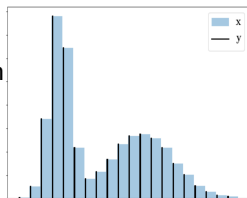
# Uniform dequantization

Let dequantize discrete distribution  $\Pi(\mathbf{y})$  to continuous distribution  $\pi(\mathbf{x})$  in the following way:  $\mathbf{x} = \mathbf{y} + \mathbf{u}$ , where  $\mathbf{u} \sim U[0, 1]$ .

## Theorem

Fitting continuous model  $p(\mathbf{x}|\theta)$  on uniformly dequantized data is equivalent to maximization of a lower bound on log-likelihood for a discrete model:

$$P(\mathbf{y}|\theta) = \int_{U[0,1]} p(\mathbf{y} + \mathbf{u}|\theta) d\mathbf{u}$$

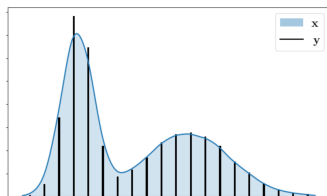
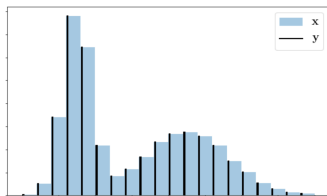


## Proof

$$\begin{aligned} \mathbb{E}_{\pi} \log p(\mathbf{x}|\theta) &= \int \pi(\mathbf{x}) \log p(\mathbf{x}|\theta) d\mathbf{x} = \sum \Pi(\mathbf{y}) \int_{U[0,1]} \log p(\mathbf{y} + \mathbf{u}|\theta) d\mathbf{u} \leq \\ &\leq \sum \Pi(\mathbf{y}) \log \int_{U[0,1]} p(\mathbf{y} + \mathbf{u}|\theta) d\mathbf{u} = \\ &= \sum \Pi(\mathbf{y}) \log P(\mathbf{y}|\theta) = \mathbb{E}_{\Pi} \log P(\mathbf{y}|\theta). \end{aligned}$$



# Variational dequantization



- ▶  $p(\mathbf{x}|\boldsymbol{\theta})$  assign uniform density to unit hypercubes  $\mathbf{y} + U[0, 1]$  (left fig).
- ▶ Smooth dequantization is more natural (right fig).
- ▶ Neural network density models are smooth function approximators.

Introduce variational dequantization noise distribution  $q(\mathbf{u}|\mathbf{y})$ , which tells what kind of noise we have to add to our discrete data. Treat it as an approximate posterior as in VAE model.

# Variational dequantization

## Variational lower bound

$$\begin{aligned}\log P(\mathbf{y}|\boldsymbol{\theta}) &= \left[ \log \int q(\mathbf{u}|\mathbf{y}) \frac{p(\mathbf{y} + \mathbf{u}|\boldsymbol{\theta})}{q(\mathbf{u}|\mathbf{y})} d\mathbf{u} \right] \geq \\ &\geq \int q(\mathbf{u}|\mathbf{y}) \log \frac{p(\mathbf{y} + \mathbf{u}|\boldsymbol{\theta})}{q(\mathbf{u}|\mathbf{y})} d\mathbf{u} = \mathcal{L}(q, \boldsymbol{\theta}).\end{aligned}$$

Uniform dequantization is a special case of variational dequantization ( $q(\mathbf{u}|\mathbf{y}) = U[0, 1]$ ).

## Flow++: flow-based variational dequantization

Let  $\mathbf{u} = g(\boldsymbol{\epsilon}, \mathbf{y}, \boldsymbol{\lambda})$  is a flow model with base distribution  $\boldsymbol{\epsilon} \sim p(\boldsymbol{\epsilon})$ :

$$q(\mathbf{u}|\mathbf{y}) = p(f(\mathbf{u}, \mathbf{y}, \boldsymbol{\lambda})) \cdot \left| \det \frac{\partial f(\mathbf{u}, \mathbf{y}, \boldsymbol{\lambda})}{\partial \mathbf{u}} \right|.$$

$$\log P(\mathbf{y}|\boldsymbol{\theta}) \geq \mathcal{L}(\boldsymbol{\lambda}, \boldsymbol{\theta}) = \int p(\boldsymbol{\epsilon}) \log \left( \frac{p(\mathbf{y} + g(\boldsymbol{\epsilon}, \mathbf{y}, \boldsymbol{\lambda})|\boldsymbol{\theta})}{p(\boldsymbol{\epsilon}) \cdot |\det \mathbf{J}_g|^{-1}} \right) d\boldsymbol{\epsilon}.$$

# Summary

- ▶ Gaussian autoregressive flow is an autoregressive model with triangular Jacobian. It has fast inference function and slow generation function. Forward KL is a natural loss function.
- ▶ The RealNVP coupling layer is an effective type of flow (special case of AR flows) that has fast inference and generation modes.
- ▶ NF models could be treated as VAE model with deterministic encoder and decoder.
- ▶ Lots of data are discrete. We able to discretize the model or to dequantize our data to use continuous model.
- ▶ Uniform dequantization is the simplest form of dequantization. Variational dequantization is a more natural type that uses variational inference.