Deep Generative Models

Lecture 5

Roman Isachenko

Moscow Institute of Physics and Technology

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Jacobian matrix

Let $f: \mathbb{R}^m \to \mathbb{R}^m$ be a differentiable function.

$$\mathbf{z} = f(\mathbf{x}), \quad \mathbf{J} = \frac{\partial \mathbf{z}}{\partial \mathbf{x}} = \begin{pmatrix} \frac{\partial z_1}{\partial x_1} & \cdots & \frac{\partial z_1}{\partial x_m} \\ \cdots & \cdots & \cdots \\ \frac{\partial z_m}{\partial x_1} & \cdots & \frac{\partial z_m}{\partial x_m} \end{pmatrix} \in \mathbb{R}^{m \times m}$$

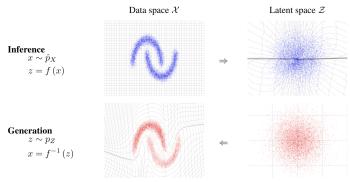
Change of variable theorem (CoV)

Let \mathbf{x} be a random variable with density function $p(\mathbf{x})$ and $f: \mathbb{R}^m \to \mathbb{R}^m$ is a differentiable, invertible function (diffeomorphism). If $\mathbf{z} = f(\mathbf{x})$, $\mathbf{x} = f^{-1}(\mathbf{z}) = g(\mathbf{z})$, then

$$p(\mathbf{x}) = p(\mathbf{z})|\det(\mathbf{J}_f)| = p(\mathbf{z})\left|\det\left(\frac{\partial \mathbf{z}}{\partial \mathbf{x}}\right)\right| = p(f(\mathbf{x}))\left|\det\left(\frac{\partial f(\mathbf{x})}{\partial \mathbf{x}}\right)\right|$$
$$p(\mathbf{z}) = p(\mathbf{x})|\det(\mathbf{J}_g)| = p(\mathbf{x})\left|\det\left(\frac{\partial \mathbf{x}}{\partial \mathbf{z}}\right)\right| = p(g(\mathbf{z}))\left|\det\left(\frac{\partial g(\mathbf{z})}{\partial \mathbf{z}}\right)\right|.$$

Definition

Normalizing flow is a *differentiable, invertible* mapping from data \mathbf{x} to the noise \mathbf{z} .



Log likelihood

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \log p(f_K \circ \cdots \circ f_1(\mathbf{x})) + \sum_{k=1}^K \log |\det(\mathbf{J}_{f_k})|$$

Forward KL for flow model

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \log p(f_{\boldsymbol{\theta}}(\mathbf{x})) + \log |\det(\mathbf{J}_f)|$$

Reverse KL for flow model

$$\mathit{KL}(p||\pi) = \mathbb{E}_{p(\mathbf{z})} \left[\log p(\mathbf{z}) - \log |\det(\mathbf{J}_g)| - \log \pi(g_{\boldsymbol{\theta}}(\mathbf{z})) \right]$$

Flow KL duality

$$\operatorname*{arg\,min}_{m{ heta}} \mathit{KL}(\pi(\mathbf{x})||p(\mathbf{x}|m{ heta})) = \operatorname*{arg\,min}_{m{ heta}} \mathit{KL}(p(\mathbf{z}|m{ heta})||p(\mathbf{z}))$$

- $ightharpoonup p(\mathbf{z})$ is a base distribution; $\pi(\mathbf{x})$ is a data distribution;
- ightharpoonup $\mathbf{z} \sim p(\mathbf{z}), \ \mathbf{x} = g_{\boldsymbol{\theta}}(\mathbf{z}), \ \mathbf{x} \sim p(\mathbf{x}|\boldsymbol{\theta});$
- $ightharpoonup \mathbf{x} \sim \pi(\mathbf{x}), \ \mathbf{z} = f_{\theta}(\mathbf{x}), \ \mathbf{z} \sim p(\mathbf{z}|\theta).$

Papamakarios G. et al. Normalizing flows for probabilistic modeling and inference, 2019

Flow log-likelihood

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \log p(f_{\boldsymbol{\theta}}(\mathbf{x})) + \log |\det(\mathbf{J}_f)|$$

The main challenge is a determinant of the Jacobian.

Linear flows

$$z = f_{\theta}(x) = Wx$$
, $W \in \mathbb{R}^{m \times m}$, $\theta = W$, $J_f = W^T$

► LU-decomposition

$$W = PLU$$
.

QR-decomposition

$$W = QR$$
.

Decomposition should be done only once in the beggining. Next, we fit decomposed matrices (P/L/U or Q/R).

Kingma D. P., Dhariwal P. Glow: Generative Flow with Invertible 1×1 Convolutions, 2018

Hoogeboom E., et al. Emerging convolutions for generative normalizing flows, 2019

Consider an autoregressive model

$$p(\mathbf{x}|\boldsymbol{\theta}) = \prod_{i=1}^{m} p(x_i|\mathbf{x}_{1:i-1},\boldsymbol{\theta}), \quad p(x_i|\mathbf{x}_{1:i-1},\boldsymbol{\theta}) = \mathcal{N}\left(\mu_j(\mathbf{x}_{1:i-1}), \sigma_j^2(\mathbf{x}_{1:i-1})\right).$$

Gaussian autoregressive NF

$$\mathbf{x} = g_{\theta}(\mathbf{z}) \quad \Rightarrow \quad x_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot z_j + \mu_j(\mathbf{x}_{1:j-1}).$$

$$\mathbf{z} = f_{\theta}(\mathbf{x}) \quad \Rightarrow \quad z_j = (x_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_i(\mathbf{x}_{1:j-1})}.$$

- We have an **invertible** and **differentiable** transformation from $p(\mathbf{z})$ to $p(\mathbf{x}|\theta)$.
- ▶ Jacobian of such transformation is triangular!

Generation function $g_{\theta}(\mathbf{z})$ is **sequential**. Inference function $f_{\theta}(\mathbf{x})$ is **not sequential**.

Papamakarios G., Pavlakou T., Murray I. Masked Autoregressive Flow for Density Estimation, 2017

Gaussian autoregressive NF

$$\mathbf{x} = g_{\theta}(\mathbf{z}) \quad \Rightarrow \quad x_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot z_j + \mu_j(\mathbf{x}_{1:j-1}).$$

$$\mathbf{z} = f_{\theta}(\mathbf{x}) \quad \Rightarrow \quad z_j = (x_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_j(\mathbf{x}_{1:j-1})}.$$

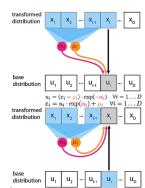
- ▶ Sampling is sequential, density estimation is parallel.
- ► Forward KL is a natural loss.

Forward transform: $f_{\theta}(\mathbf{x})$

$$z_j = (x_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_j(\mathbf{x}_{1:j-1})}$$

Inverse transform: $g_{\theta}(\mathbf{z})$

$$x_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot z_j + \mu_j(\mathbf{x}_{1:j-1})$$



1. RealNVP: coupling layer

2. Normalizing flows as VAE model

3. Discrete data vs continuous model
Discretization of continuous distribution
Dequantization of discrete data

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RealNVP

Let split x and z in two parts:

$$\mathbf{x} = [\mathbf{x}_1, \mathbf{x}_2] = [\mathbf{x}_{1:d}, \mathbf{x}_{d+1:m}]; \quad \mathbf{z} = [\mathbf{z}_1, \mathbf{z}_2] = [\mathbf{z}_{1:d}, \mathbf{z}_{d+1:m}].$$

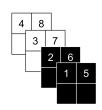
Coupling layer

$$\begin{cases} \mathbf{x}_1 = \mathbf{z}_1; & \left\{ \mathbf{z}_1 = \mathbf{x}_1; \\ \mathbf{x}_2 = \mathbf{z}_2 \odot \sigma_{\theta}(\mathbf{z}_1) + \mu_{\theta}(\mathbf{z}_1). & \left\{ \mathbf{z}_2 = (\mathbf{x}_2 - \mu_{\theta}(\mathbf{x}_1)) \odot \frac{1}{\sigma_{\theta}(\mathbf{x}_1)}. \right. \end{cases}$$

$$egin{cases} \mathbf{z}_1 = \mathbf{x}_1; \ \mathbf{z}_2 = (\mathbf{x}_2 - oldsymbol{\mu}_{oldsymbol{ heta}}(\mathbf{x}_1)) \odot rac{1}{\sigma_{oldsymbol{ heta}}(\mathbf{x}_1)} \end{cases}$$

Image partitioning





- Checkerboard ordering uses masking.
- Channelwise ordering uses splitting.

RealNVP

Coupling layer

$$\begin{cases} \mathbf{x}_1 = \mathbf{z}_1; \\ \mathbf{x}_2 = \mathbf{z}_2 \odot \boldsymbol{\sigma}_{\boldsymbol{\theta}}(\mathbf{z}_1) + \boldsymbol{\mu}_{\boldsymbol{\theta}}(\mathbf{z}_1). \end{cases} \begin{cases} \mathbf{z}_1 = \mathbf{x}_1; \\ \mathbf{z}_2 = (\mathbf{x}_2 - \boldsymbol{\mu}_{\boldsymbol{\theta}}(\mathbf{x}_1)) \odot \frac{1}{\boldsymbol{\sigma}_{\boldsymbol{\theta}}(\mathbf{x}_1)}. \end{cases}$$

Estimating the density takes 1 pass, sampling takes 1 pass!

Jacobian

$$\det\left(\frac{\partial \mathbf{z}}{\partial \mathbf{x}}\right) = \det\left(\frac{\mathbf{I}_d}{\frac{\partial \mathbf{z}_2}{\partial \mathbf{x}_1}} \quad \frac{\mathbf{0}_{d \times m - d}}{\frac{\partial \mathbf{z}_2}{\partial \mathbf{x}_2}}\right) = \prod_{j=1}^{m-d} \frac{1}{\sigma_j(\mathbf{x}_1)}.$$

Gaussian AR NF

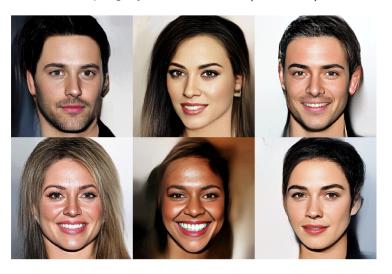
$$\mathbf{x} = g_{\theta}(\mathbf{z}) \quad \Rightarrow \quad x_j = \sigma_j(\mathbf{x}_{1:j-1}) \cdot z_j + \mu_j(\mathbf{x}_{1:j-1}).$$

$$\mathbf{z} = f_{\theta}(\mathbf{x}) \quad \Rightarrow \quad z_j = (x_j - \mu_j(\mathbf{x}_{1:j-1})) \cdot \frac{1}{\sigma_j(\mathbf{x}_{1:j-1})}.$$

How to get RealNVP coupling layer from gaussian AR NF?

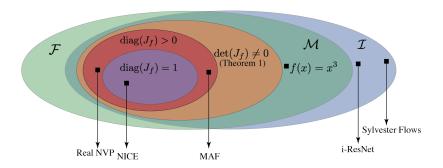
Glow samples

Glow model: coupling layer + linear flows (1x1 convs)



Kingma D. P., Dhariwal P. Glow: Generative Flow with Invertible 1x1 Convolutions, 2018

Venn diagram for Normalizing flows



- \triangleright \mathcal{I} invertible functions.
- ► F continuously differentiable functions whose Jacobian is lower triangular.
- $\triangleright \mathcal{M}$ invertible functions from \mathcal{F} .

Song Y., Meng C., Ermon S. Mintnet: Building invertible neural networks with masked convolutions, 2019

1. RealNVP: coupling layer

2. Normalizing flows as VAE model

Discrete data vs continuous model
 Discretization of continuous distribution
 Dequantization of discrete data

VAE vs Normalizing flows

	VAE	NF
Objective	ELBO $\mathcal L$	Forward KL/MLE
Encoder	stochastic $\mathbf{z} \sim q(\mathbf{z} \mathbf{x}, oldsymbol{\phi})$	$\begin{aligned} deterministic \\ \mathbf{z} &= f_{\boldsymbol{\theta}}(\mathbf{x}) \\ q(\mathbf{z} \mathbf{x}, \boldsymbol{\theta}) &= \delta(\mathbf{z} - f_{\boldsymbol{\theta}}(\mathbf{x})) \end{aligned}$
Decoder	$\begin{aligned} &stochastic \\ &x \sim p(x z, \boldsymbol{\theta}) \end{aligned}$	$\begin{aligned} deterministic \\ \mathbf{x} &= g_{\boldsymbol{\theta}}(\mathbf{z}) \\ p(\mathbf{x} \mathbf{z}, \boldsymbol{\theta}) &= \delta(\mathbf{x} - g_{\boldsymbol{\theta}}(\mathbf{z})) \end{aligned}$
Parameters	$oldsymbol{\phi}, oldsymbol{ heta}$	$ heta \equiv \phi$

Theorem

MLE for normalizing flow is equivalent to maximization of ELBO for VAE model with deterministic encoder and decoder:

$$p(\mathbf{x}|\mathbf{z},\boldsymbol{\theta}) = \delta(\mathbf{x} - f^{-1}(\mathbf{z},\boldsymbol{\theta})) = \delta(\mathbf{x} - g_{\boldsymbol{\theta}}(\mathbf{z}));$$

$$q(\mathbf{z}|\mathbf{x}, \boldsymbol{\theta}) = p(\mathbf{z}|\mathbf{x}, \boldsymbol{\theta}) = \delta(\mathbf{z} - f_{\boldsymbol{\theta}}(\mathbf{x})).$$

Nielsen D., et al. SurVAE Flows: Surjections to Bridge the Gap between VAEs and Flows. 2020

Normalizing flow as VAE

Proof

1. Dirac delta function property

$$\mathbb{E}_{\delta(\mathbf{x}-\mathbf{y})}f(\mathbf{x}) = \int \delta(\mathbf{x}-\mathbf{y})f(\mathbf{x})d\mathbf{x} = f(\mathbf{y}).$$

2. CoV theorem and Bayes theorem:

$$p(\mathbf{x}|\boldsymbol{\theta}) = p(\mathbf{z})|\det(\mathbf{J}_f)|;$$

$$p(\mathbf{z}|\mathbf{x},\boldsymbol{\theta}) = \frac{p(\mathbf{x}|\mathbf{z},\boldsymbol{\theta})p(\mathbf{z})}{p(\mathbf{x}|\boldsymbol{\theta})}; \quad \Rightarrow \quad p(\mathbf{x}|\mathbf{z},\boldsymbol{\theta}) = p(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})|\det(\mathbf{J}_f)|.$$

3. Log-likelihood decomposition

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \mathcal{L}(\boldsymbol{\theta}) + \frac{KL(q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})||p(\mathbf{z}|\mathbf{x},\boldsymbol{\theta}))}{\mathcal{L}(\boldsymbol{\theta})} = \mathcal{L}(\boldsymbol{\theta}).$$

Normalizing flow as VAE

Proof

ELBO objective:

$$\mathcal{L} = \mathbb{E}_{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})} \left[\log p(\mathbf{x}|\mathbf{z},\boldsymbol{\theta}) - \log \frac{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})}{p(\mathbf{z})} \right]$$

$$= \mathbb{E}_{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})} \left[\log \frac{p(\mathbf{x}|\mathbf{z},\boldsymbol{\theta})}{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})} + \log p(\mathbf{z}) \right].$$

1. Dirac delta function property:

$$\mathbb{E}_{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})}\log p(\mathbf{z}) = \int \delta(\mathbf{z} - f_{\boldsymbol{\theta}}(\mathbf{x}))\log p(\mathbf{z})d\mathbf{z} = \log p(f_{\boldsymbol{\theta}}(\mathbf{x})).$$

2. CoV theorem and Bayes theorem:

$$\mathbb{E}_{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})}\log\frac{p(\mathbf{x}|\mathbf{z},\boldsymbol{\theta})}{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})} = \mathbb{E}_{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})}\log\frac{p(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})|\det(\mathbf{J}_f)|}{q(\mathbf{z}|\mathbf{x},\boldsymbol{\theta})} = \log|\det\mathbf{J}_f|.$$

3. Log-likelihood decomposition

$$\log p(\mathbf{x}|\boldsymbol{\theta}) = \mathcal{L}(\boldsymbol{\theta}) = \log p(f_{\boldsymbol{\theta}}(\mathbf{x})) + \log |\det \mathbf{J}_f|.$$

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Discrete data vs continuous model

Let our data \mathbf{y} comes from discrete distribution $\Pi(\mathbf{y})$ and we have continuous model $p(\mathbf{x}|\theta) = \mathsf{NN}(\mathbf{x},\theta)$.

- ▶ Images (and not only images) are discrete data, pixels lie in the integer domain ({0, 255}).
- ▶ By fitting a continuous density model $p(\mathbf{x}|\theta)$ to discrete data $\Pi(\mathbf{y})$, one can produce a degenerate solution with all probability mass on discrete values.

Discrete model

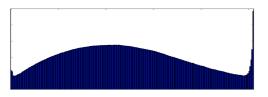
- ▶ Use **discrete** model (e.x. $P(\mathbf{y}|\theta) = \mathsf{Cat}(\pi(\theta))$).
- ▶ Minimize any suitable divergence measure $D(\Pi, P)$.
- ► NF works only with continuous data **x** (there are discrete NF, see papers below).
- ▶ If pixel value is not presented in the train data, it won't be predicted.

Discrete data vs continuous model

Continuous model

- Use **continuous** model (e.x. $p(\mathbf{x}|\theta) = \mathcal{N}(\mu_{\theta}(\mathbf{x}), \sigma_{\theta}^2(\mathbf{x}))$), but
 - **discretize** model (make the model outputs discrete): transform $p(\mathbf{x}|\theta)$ to $P(\mathbf{y}|\theta)$;
 - **dequantize** data (make the data continuous): transform $\Pi(y)$ to $\pi(x)$.
- Continuous distribution knows numerical relationships.

CIFAR-10 pixel values distribution



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Discretization of continuous distribution

Model discretization through CDF

$$F(\mathbf{x}|\boldsymbol{\theta}) = \int_{-\infty}^{\mathbf{x}} p(\mathbf{x}'|\boldsymbol{\theta}) d\mathbf{x}'; \quad P(\mathbf{y}|\boldsymbol{\theta}) = F(\mathbf{y} + 0.5|\boldsymbol{\theta}) - F(\mathbf{y} - 0.5|\boldsymbol{\theta})$$

Mixture of logistic distributions

$$p(x|\mu,s) = \frac{\exp^{-(x-\mu)/s}}{s(1+\exp^{-(x-\mu)/s})^2}; \quad p(x|\pi,\mu,s) = \sum_{k=1}^K \pi_k p(x|\mu_k,s_k).$$

PixelCNN++

$$p(\mathbf{x}|\boldsymbol{\theta}) = \prod_{j=1}^{m} p(x_j|\mathbf{x}_{1:j-1},\boldsymbol{\theta}); \quad p(x_j|\mathbf{x}_{1:j-1},\boldsymbol{\theta}) = \sum_{k=1}^{K} \pi_k p(x|\mu_k,s_k).$$

Here, $\pi_k = \pi_{k,\theta}(\mathbf{x}_{1:j-1}), \ \mu_k = \mu_{k,\theta}(\mathbf{x}_{1:j-1}), \ s_k = s_{k,\theta}(\mathbf{x}_{1:j-1}).$

For the pixel edge cases of 0, replace y-0.5 by $-\infty$, and for 255 replace y+0.5 by $+\infty$.

Salimans T. et al. PixelCNN++: Improving the PixelCNN with Discretized Logistic Mixture Likelihood and Other Modifications, 2017

1. RealNVP: coupling layer

2. Normalizing flows as VAE model

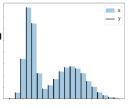
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Uniform dequantization

Let dequantize discrete distribution $\Pi(\mathbf{y})$ to continuous distribution $\pi(\mathbf{x})$ in the following way: $\mathbf{x} = \mathbf{y} + \mathbf{u}$, where $\mathbf{u} \sim U[0,1]$.

Theorem

Fitting continuous model $p(\mathbf{x}|\boldsymbol{\theta})$ on uniformly dequantized data is equivalent to maximization of a lower bound on log-likelihood for a discrete model:

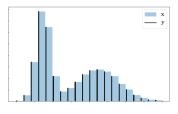


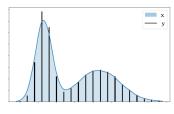
$$P(\mathbf{y}|\boldsymbol{\theta}) = \int_{U[0.1]} p(\mathbf{y} + \mathbf{u}|\boldsymbol{\theta}) d\mathbf{u}$$

Proof

$$\begin{split} \mathbb{E}_{\pi} \log p(\mathbf{x}|\boldsymbol{\theta}) &= \int \pi(\mathbf{x}) \log p(\mathbf{x}|\boldsymbol{\theta}) d\mathbf{x} = \sum \Pi(\mathbf{y}) \int_{U[0,1]} \log p(\mathbf{y} + \mathbf{u}|\boldsymbol{\theta}) d\mathbf{u} \leq \\ &\leq \sum \Pi(\mathbf{y}) \log \int_{U[0,1]} p(\mathbf{y} + \mathbf{u}|\boldsymbol{\theta}) d\mathbf{u} = \\ &= \sum \Pi(\mathbf{y}) \log P(\mathbf{y}|\boldsymbol{\theta}) = \mathbb{E}_{\Pi} \log P(\mathbf{y}|\boldsymbol{\theta}). \end{split}$$

Variational dequantization





- ▶ $p(\mathbf{x}|\boldsymbol{\theta})$ assign uniform density to unit hypercubes $\mathbf{y} + U[0,1]$ (left fig).
- Smooth dequantization is more natural (right fig).
- Neural network density models are smooth function approximators.

Introduce variational dequantization noise distribution $q(\mathbf{u}|\mathbf{y})$, which tells what kind of noise we have to add to our discrete data. Treat it as an approximate posterior as in VAE model.

Variational dequantization

Variational lower bound

$$egin{aligned} \log P(\mathbf{y}|oldsymbol{ heta}) &= \left[\log \int q(\mathbf{u}|\mathbf{y}) rac{p(\mathbf{y}+\mathbf{u}|oldsymbol{ heta})}{q(\mathbf{u}|\mathbf{y})} d\mathbf{u}
ight] \geq \ &\geq \int q(\mathbf{u}|\mathbf{y}) \log rac{p(\mathbf{y}+\mathbf{u}|oldsymbol{ heta})}{q(\mathbf{u}|\mathbf{y})} d\mathbf{u} = \mathcal{L}(q,oldsymbol{ heta}). \end{aligned}$$

Uniform dequantization is a special case of variational dequantization $(q(\mathbf{u}|\mathbf{y}) = U[0,1])$.

Flow++: flow-based variational dequantization

Let $\mathbf{u} = g_{\lambda}(\epsilon, \mathbf{y})$ is a flow model with base distribution $\epsilon \sim p(\epsilon)$:

$$q(\mathbf{u}|\mathbf{y}) = p(f_{\lambda}(\mathbf{u},\mathbf{y})) \cdot \left| \det \frac{\partial f_{\lambda}(\mathbf{u},\mathbf{y})}{\partial \mathbf{u}} \right|.$$

$$\log P(\mathbf{y}|oldsymbol{ heta}) \geq \mathcal{L}(oldsymbol{\lambda},oldsymbol{ heta}) = \int p(oldsymbol{\epsilon}) \log \left(rac{p(\mathbf{y}+g_{oldsymbol{\lambda}}(oldsymbol{\epsilon},\mathbf{y})|oldsymbol{ heta})}{p(oldsymbol{\epsilon})\cdot \left|\det \mathbf{J}_{oldsymbol{arepsilon}}
ight|^{-1}}
ight) doldsymbol{\epsilon}.$$

Ho J. et al. Flow++: Improving Flow-Based Generative Models with Variational Dequantization and Architecture Design, 2019

Summary

- ► Gaussian autoregressive flow is an autoregressive model with triangular Jacobian. It has fast inference function and slow generation function. Forward KL is a natural loss function.
- The RealNVP coupling layer is an effective type of flow (special case of AR flows) that has fast inference and generation modes.
- ▶ NF models could be treated as VAE model with deterministic encoder and decoder.
- Lots of data are discrete. We able to discretize the model or to dequantize our data to use continuous model.
- Uniform dequantization is the simplest form of dequantization. Variational dequantization is a more natural type that uses variational inference.