Additional Plots

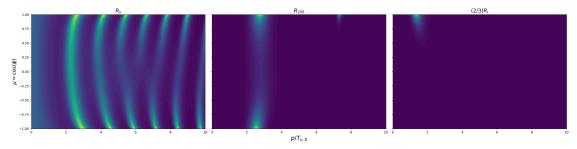
September 21, 2024

```
[1]: import numpy as np
  import matplotlib.pyplot as plt
  from src.input import *
  from src.distributions import f_FD
  from src.units import UNITS
  from scipy.interpolate import interp1d
  from matplotlib import cm
  from matplotlib.colors import Normalize
  from mpl_toolkits.axes_grid1.inset_locator import inset_axes
  from scipy.stats import linregress
```

0.0.1 Orbits and Contours

```
[2]: fig, axes = plt.subplots(1, 3, figsize=(24, 6), sharex=True, sharey=True)
     mu_integrands = np.load('paper_plots_notebook/mu_integrands.npy')
     mu_arr = np.cos(np.linspace(0, np.pi, 50))
     extended_p_arr = np.geomspace(0.01, 50, 1000)
     X_1, Y_1 = np.meshgrid(mu_arr, extended_p_arr)
     contour = axes[0].contourf(Y_1, X_1, mu_integrands[0, :, :], levels=50, __
      ⇔cmap='viridis')
     axes[0].set_ylabel(r'\mu = \cos(\phi)\$', fontsize = 16)
     axes[0].set xlim(0, 20)
     axes[0].set_title(r'$R_s$', fontsize = 16)
     contour = axes[1].contourf(Y_1, X_1, mu_integrands[1, :, :], levels=50,__
      ⇔cmap='viridis')
     axes[1].set_xlabel(r'$p / T_{\nu,0}$', fontsize=18)
     axes[1].set_xlim(0, 10)
     axes[1].set_title(r'$R_{200}$', fontsize = 16)
     contour = axes[2].contourf(Y_1, X_1, mu_integrands[2, :, :], levels=50,__
      ⇔cmap='viridis')
     axes[2].set_xlim(0, 10)
     axes[2].set_title(r'(2/3)$R_i$', fontsize = 16)
```

```
plt.tight_layout()
plt.savefig('plot_save_vehicle.png')
plt.show()
```



```
[3]: ### Chose momenta and mu values where the integrands peak, as indicated above
      ⇔###
     ## So all are mu = 1. First two are p/T_nu = 2.5, and Ri is p/T_nu = 1.5
     fig, axes = plt.subplots(1, 3, figsize=(24, 6))
     positions_mod_funcs = np.load('paper_plots_notebook/positions_mod_funcs.npy')
     # Subplot 1
     axes[0].scatter(positions_mod_funcs[0,0,:,0], positions_mod_funcs[0,0,:,1],__
      ⇔s=2, label = 'linear')
     axes[0].scatter(positions_mod_funcs[0,1,:,0], positions_mod_funcs[0,1,:,1],__
      \Rightarrows=2, color = 'red', label = '50')
     axes[0].scatter(positions_mod_funcs[0,2,:,0], positions_mod_funcs[0,2,:,1],_
      \Rightarrows=2, color = 'green', label = '1 / 50')
     circle = plt.Circle((0, 0), radius=3.026, alpha=0.9, edgecolor='blue',

¬facecolor='none', label='R_200')
     circ = plt.Circle((0, 0), radius=17.7, alpha=0.9, edgecolor='green',

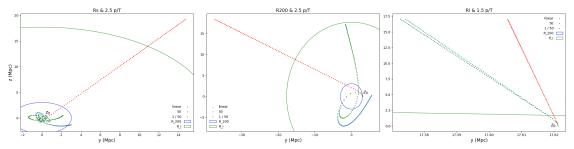
¬facecolor='none', label='R_i')
     axes[0].add artist(circle)
     axes[0].add_artist(circ)
     axes[0].set_xlabel('y (Mpc)', fontsize=14)
     axes[0].set_ylabel('z (Mpc)', fontsize=14)
     axes[0].legend(markerfirst = False, frameon = False)
     axes[0].set_title('Rs & 2.5 p/T', fontsize=14)
     axes[0].text(0.36, 0.8, $^{$z_0$}$', fontsize=14)
     # Subplot 2
     axes[1].scatter(positions_mod_funcs[1,0,:,0], positions_mod_funcs[1,0,:,1],
     ⇔s=2, label = 'linear')
     axes[1].scatter(positions_mod_funcs[1,1,:,0], positions_mod_funcs[1,1,:,1],__
      \Rightarrows=2, color = 'red', label = '50')
```

```
axes[1].scatter(positions_mod_funcs[1,2,:,0], positions_mod_funcs[1,2,:,1],_u
 \Rightarrows=2, color = 'green', label = '1 / 50')
circle = plt.Circle((0, 0), radius=3.026, alpha=0.9, edgecolor='blue',
⇔facecolor='none', label='R 200')
circ = plt.Circle((0, 0), radius=17.7, alpha=0.9, edgecolor='green', u

¬facecolor='none', label='R_i')

axes[1].add_artist(circle)
axes[1].add artist(circ)
axes[1].set_xlabel('y (Mpc)', fontsize=14)
axes[1].legend(frameon = False)
axes[1].set_title('R200 & 2.5 p/T', fontsize=14)
axes[1].text(3.2, 0.7, $^2_0$', fontsize=14)
# Subplot 3
axes[2].scatter(positions_mod_funcs[2,0,:,0], positions_mod_funcs[2,0,:,1],_u
 ⇔s=2, label = 'linear')
axes[2].scatter(positions_mod_funcs[2,1,:,0], positions_mod_funcs[2,1,:,1],_
 \Rightarrows=2, color = 'red', label = '50')
axes[2].scatter(positions_mod_funcs[2,2,:,0], positions_mod_funcs[2,2,:,1],__
\Rightarrows=2, color = 'green', label = '1 / 50')
circle = plt.Circle((0, 0), radius=3.026, alpha=0.9, edgecolor='blue', __
 ⇔facecolor='none', label='R 200')
circ = plt.Circle((0, 0), radius=17.7, alpha=0.9, edgecolor='green',

¬facecolor='none', label='R_i')
axes[2].add artist(circle)
axes[2].add_artist(circ)
axes[2].set_xlabel('y (Mpc)', fontsize=14)
axes[2].legend(markerfirst = False, frameon = False)
axes[2].set_title('Ri & 1.5 p/T', fontsize=14)
axes[2].text(17.619, -0.1, '$z_0$', fontsize=14)
plt.tight layout()
plt.savefig('plot_save_vehicle.png')
plt.show()
```



[]:

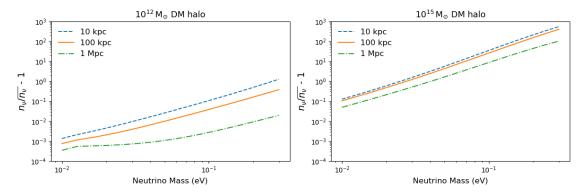
0.0.2 Mass-dependence of Neutrino Overdensity

```
[4]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(12, 4))
    mass_overdens = np.load('paper_plots_notebook/mass_overdens.npy')
    mass_arr = np.geomspace(0.01, 0.3, 15) #eV
    ax1.loglog(mass_arr, mass_overdens[0,5,:] - 1, label = '10 kpc', linestyle = _1

    dashed¹)

    ax1.loglog(mass_arr, mass_overdens[0,10,:] - 1, label = '100 kpc', linestyle = 1
      ⇔'solid')
    ax1.loglog(mass_arr, mass_overdens[0,14,:] - 1, label = '1 Mpc', linestyle = 1
      ax1.set_xlabel('Neutrino Mass (eV)', fontsize = 12)
    ax1.set_ylabel(r'$n_{\n} / verline{n_{\n}}, - 1', fontsize=14)
    ax1.set_title(r'$10^{12} \, \text{text}_{M}_{\odot}$ DM halo', fontsize = 13)
    ax1.set_ylim(1e-4,1e3)
    ax1.legend(loc = 'upper left', frameon = False, fontsize = 12)
    ax2.loglog(mass_arr, mass_overdens[1,5,:] - 1, label = '10 kpc', linestyle = __

¬'dashed')
    ax2.loglog(mass_arr, mass_overdens[1,10,:] - 1, label = '100 kpc', linestyle = 1
      ax2.loglog(mass_arr, mass_overdens[1,14,:] - 1, label = '1 Mpc', linestyle = 1
      ax2.set_xlabel('Neutrino Mass (eV)', fontsize = 12)
    ax2.set_ylabel(r'$n_{\n} / verline{n_{\n}}, - 1', fontsize=14)
    ax2.set_title(r'$10^{15} \, \text{text}M_{\odot}$ DM halo', fontsize = 13)
    ax2.set ylim(1e-4,1e3)
    ax2.legend(frameon = False, fontsize = 12)
    plt.tight_layout()
    plt.savefig('plot_save_vehicle.pdf')
    plt.show()
```



```
[5]: # Calculate the power law index for both halo masses with linear regression for mass_idx in range(2):
    data = mass_overdens[mass_idx, 5, :] - 1 # At 10 kpc
    log_mass = np.log10(mass_arr)
    log_data = np.log10(data)
    slope, _, _, _ = linregress(log_mass, log_data)
    print(f"Power law index for 10 kpc for 10^{12 + 3 * mass_idx} MSun: {slope:.

-2f}")
```

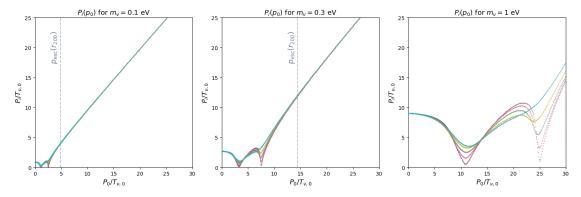
Power law index for 10 kpc for 10^12 MSun: 2.00 Power law index for 10 kpc for 10^15 MSun: 2.51

[]:

0.0.3 $P_i(p_0)$

```
[6]: fig, (ax1, ax2, ax3) = plt.subplots(1, 3, figsize=(15, 5))
     po_pi_data = np.load('paper_plots_notebook/po_pi_array.npy')
     po_pi_arr = np.geomspace(0.01, 40, 2000)
     for i in range(10):
        ax1.scatter(po_pi_arr, po_pi_data[0,i,:] * 0.1 * UNITS.eV / Tnu_0, s=0.1)
     ax1.set_xlim(0, 30)
     ax1.set_ylim(0, 25)
     ax1.set_xlabel(r'$P_0 / T_{\nu,0}$', fontsize=13)
     ax1.set_ylabel(r'$P_i / T_{\nu,0}$', fontsize=13)
     ax1.set_title(r'$P_i(p_0)$ for $m_{nu} = 0.1$ eV', fontsize=13)
     ax1.vlines(4.818, 0, 30, linestyle='dashed', alpha=0.5, color='slategrey')
     ax1.text(2.818, 20, r'p_{\text{esc}}(r_{200}), rotation=90, 
      overticalalignment='center', horizontalalignment='left', fontsize=14, ∪
      ⇔color='slategrey')
     for i in range(10):
         ax2.scatter(po_pi_arr, po_pi_data[1,i,:] * 0.3 * UNITS.eV / Tnu_0, s=0.1)
     ax2.set_xlabel(r'p / T_{nu,0}; size=12)
     ax2.set_xlim(0, 30)
     ax2.set_ylim(0, 25)
     ax2.set_xlabel(r'$P_0 / T_{nu,0}$', fontsize=13)
     ax2.set_ylabel(r'$P_i / T_{nu,0}$', fontsize=13)
     ax2.set_title(r'$P_i(p_0)$ for $m_{nu} = 0.3$ eV', fontsize=13)
     ax2.vlines(14.45, 0, 30, linestyle='dashed', alpha=0.5, color='slategrey')
     ax2.text(12.45, 20, r'p_{\text{esc}}(r_{200}))', rotation=90, 
      ⇔verticalalignment='center', horizontalalignment='left', fontsize=14, ⊔
      ⇔color='slategrey')
```

```
for i in range(10):
    ax3.scatter(po_pi_arr, po_pi_data[2,i,:] * 1 * UNITS.eV / Tnu_0, s=0.1)
ax3.set_xlabel(r'$p / T_{\nu,0}$', size=12)
ax3.set_xlim(0, 30)
ax3.set_ylim(0, 25)
ax3.set_xlabel(r'$P_0 / T_{\nu,0}$', fontsize=13)
ax3.set_ylabel(r'$P_i / T_{\nu,0}$', fontsize=13)
ax3.set_title(r'$P_i(p_0)$ for $m_{\nu} = 1$ eV', fontsize=13)
ax3.vlines(48.18, 0, 30, linestyle = 'dashed', alpha = 0.5)
plt.tight_layout()
#plt.savefig('plot_save_vehicle.pdf')
```



[]:

0.0.4 Concentration parameter

```
[8]: def concentration(redshift_array, Mh):
    # For redshift >= 4
    cond = redshift_array >= 4
    conc_high_z = 10 ** (
        1.3081
        - 0.1078 * (1 + redshift_array)
        + 0.00398 * (1 + redshift_array) ** 2
        + (0.0223 - 0.0944 * (1 + redshift_array) ** (-0.3907))
        * np.log10(Mh / UNITS.MSun)
)

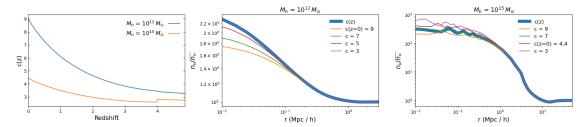
# For redshift < 4
    conc_low_z = 10 ** (
        1.7543
        - 0.2766 * (1 + redshift_array)</pre>
```

```
+ 0.02039 * (1 + redshift_array) ** 2
             + (0.2753 + 0.00351 * (1 + redshift_array) - 0.3038 * (1 + ____)
      →redshift_array) ** 0.0269)
             * np.log10(Mh / UNITS.MSun)
             * (
                  1.0
                  + (-0.01537 + 0.02102 * (1 + redshift_array) ** (-0.1475))
                  * (np.log10(Mh / UNITS.MSun)) ** 2
             )
         )
         conc = np.where(cond, conc_high_z, conc_low_z)
         return conc
     extended_z_arr = np.linspace(0, 4.85, 1000)
     conc_test_1e12 = concentration(extended_z_arr, 1e12 * UNITS.MSun)
     conc test 1e13 = concentration(extended z arr, 1e13 * UNITS.MSun)
     conc_test_1e14 = concentration(extended_z_arr, 1e14 * UNITS.MSun)
     conc_test_1e15 = concentration(extended_z_arr, 1e15 * UNITS.MSun)
[9]: fig, (ax1, ax2, ax3) = plt.subplots(1, 3, figsize=(18, 4))
     density_conc_vars = np.load('paper_plots_notebook/density_conc_vars.npy')
     extended_z_arr = np.linspace(0, 4.85, 1000)
     r_array_5e1 = np.geomspace(1e-2, 5e1, 50)
     # Subplot 1
     ax1.plot(extended_z_arr, conc_test_1e12, label=r'$M_h$ = $10^{12} \,_u
      \hookrightarrow M_{\odot}')
     \#ax1.plot(extended_z_arr, conc_test_1e13, label=r'$M_h$ = $10^{13} \,
      \hookrightarrow M \{ \setminus odot \}  \}')
     \#ax1.plot(extended_z_arr, conc_test_1e14, label=r'$M_h$ = $10^{14} \, \
      \hookrightarrow M_{(odot)}
     ax1.plot(extended\ z\ arr,\ conc\ test\ 1e15,\ label=r'$M\ h$ = $10^{15} \,
      \hookrightarrow M_{\odot}')
     ax1.set xlabel('Redshift', fontsize=14)
     ax1.set_xlim(0, 4.85)
     ax1.set_ylabel('c(z)', fontsize=14)
     ax1.tick_params(axis='y')
     ax1.tick_params(axis='y', which='both', direction='in', right=True)
     ax1.legend(markerfirst = False, frameon = False, fontsize = 13)
     # Subplot 2
     ax2.loglog(r_array_5e1, density_conc_vars[0, 0, :], label = 'c(z)', linewidth = __
```

 $ax2.loglog(r_array_5e1, density_conc_vars[1, 0, :], label = 'c(z=0) = 9')$ $ax2.loglog(r_array_5e1, density_conc_vars[2, 0, :], label = 'c = 7')$

→7)

```
ax2.loglog(r_array_5e1, density_conc_vars[3, 0, :], label = 'c = 5')
ax2.loglog(r_array_5e1, density_conc_vars[4, 0, :], label = 'c = 3')
ax2.legend(frameon = False, fontsize = 12)
ax2.set_xlabel('r (Mpc / h)', fontsize=14)
ax2.set_ylabel(r'$n {\nu} / verline{n {\nu}},}$', fontsize=15)
ax2.set_title(r'$M_h$ = $10^{12} \ , M_{\odot}$', fontsize=14)
ax2.set xlim(1e-2, 3)
#Subplot 3
ax3.loglog(r_array_5e1, density_conc_vars[0, 1, :], label = c(z), linewidth =
 →7)
ax3.loglog(r_array_5e1, density_conc_vars[1, 1, :], label = 'c = 9')
ax3.loglog(r_array_5e1, density_conc_vars[2, 1, :], label = 'c = 7')
ax3.loglog(r_array_5e1, density_conc_vars[3, 1, :], label = 'c(z=0) = 4.4')
ax3.loglog(r_array_5e1, density_conc_vars[4, 1, :], label = 'c = 3')
ax3.legend(frameon = False, fontsize = 12)
ax3.set_xlabel('r (Mpc / h)', fontsize=14)
ax3.set_ylabel(r'$n_{\langle nu} / verline{n_{\langle nu} \rangle,}$', fontsize=15)
ax3.set_title(r'$M_h$ = $10^{15} \ , M_{\odot}$', fontsize=14)
ax3.set_xlim(1e-2, 50)
plt.tight_layout()
#plt.savefig('plot_save_vehicle.pdf')
plt.show()
```



```
[]:
```

0.0.5 Enclosed mass for mass conservation

```
[10]: def compute_enclosed_mass(radii, density_profile, radius_index):
    if radius_index < 0 or radius_index >= len(radii):
        raise ValueError("Radius index out of range")
# Compute enclosed mass
enclosed_mass_profile = 0
for i in range(radius_index + 1):
    if i == 0:
        r1 = 0
```

```
else:
                  r1 = radii[i - 1]
              r2 = radii[i]
              volume = (4/3) * np.pi * (r2**3 - r1**3)
              enclosed_mass_profile += density_profile[i] * volume
          return enclosed_mass_profile
      def compute enclosed mass background(radii, radius index):
          if radius index < 0 or radius index >= len(radii):
              raise ValueError("Radius index out of range")
          # Compute enclosed mass
          enclosed mass background = 0
          for i in range(radius_index + 1):
              if i == 0:
                  r1 = 0
              else:
                  r1 = radii[i - 1]
              r2 = radii[i]
              volume = (4/3) * np.pi * (r2**3 - r1**3)
              enclosed_mass_background += volume # Density is 1 for the background
          return enclosed_mass_background
[11]: dens 4halos 4nu = np.load('paper plots notebook/dens 4halos 4nu.npy')
      dm_mass_count = dens_4halos_4nu.shape[0] # Number of DM halo masses
      nu_mass_count = dens_4halos_4nu.shape[2] # Number of neutrino masses
      radii = r_array_5e1.copy()
      # Compute the background enclosed mass for all radii
      background_encl = []
      for radius_index in range(50):
          enclosed mass_background = compute_enclosed_mass_background(radii,__
       →radius index)
          background_encl.append(enclosed_mass_background)
```

Extract the density profile for the current combination of DM mass \sqcup

Convert the background enclosed mass list to a numpy array

for nu_idx in range(4): # 4 different neutrino mass values

background_encl = np.array(background_encl)

 \hookrightarrow and neutrino mass

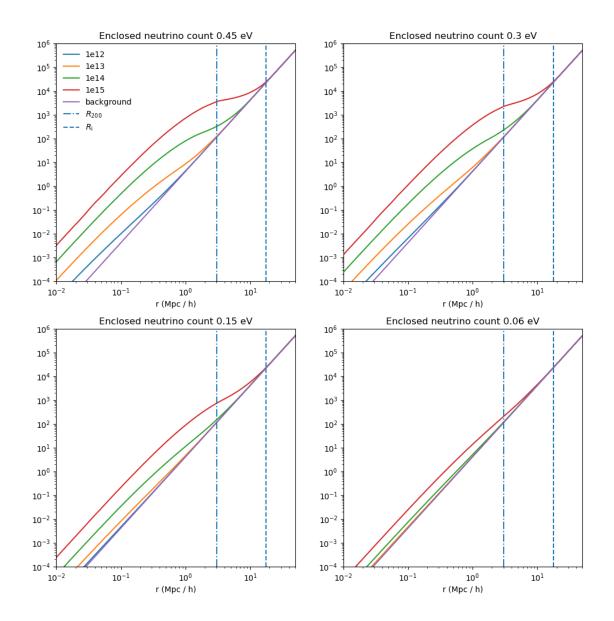
Loop over DM and neutrino mass combinations

for dm_idx in range(4): # 4 different DM mass values

```
density_profile = dens_4halos_4nu[dm_idx, :, nu_idx] # [50] profile_
       ⇔for this combination
              mass_conservation_check = []
              profile encl = []
              for i in range(50):
                  radius index = i
                  # Compute the enclosed mass for the profile
                  enclosed_mass_profile = compute_enclosed_mass(radii,__

→density_profile, radius_index)
                  profile encl.append(enclosed mass profile)
                  ratio = enclosed_mass_profile / background_encl[i] # Use the_
       →precomputed background
                  mass_conservation_check.append(ratio)
              # Convert lists to numpy arrays
              profile_encl = np.array(profile_encl)
              mass_conservation_check = np.array(mass_conservation_check)
              # Assign the arrays to dynamically named variables
              suffix = f' dm{dm idx} nu{nu idx}'
              globals()['profile_encl' + suffix] = profile_encl
              globals()['mass_conservation_check' + suffix] = mass_conservation_check
[12]: fig, axes = plt.subplots(2, 2, figsize=(12, 12))
      axes[0, 0].loglog(radii, profile_encl_dm0_nu3, label='1e12')
      axes[0, 0].loglog(radii, profile_encl_dm1_nu3, label='1e13')
      axes[0, 0].loglog(radii, profile_encl_dm2_nu3, label='1e14')
      axes[0, 0].loglog(radii, profile_encl_dm3_nu3, label='1e15')
      axes[0, 0].loglog(radii, background_encl, label='background')
      axes[0, 0].set_xlabel('r (Mpc / h)')
      axes[0, 0].set_title('Enclosed neutrino count 0.45 eV')
      axes[0, 0].vlines(3.026, 1e-4, 1e6, linestyle='dashdot', u
       \Rightarrowlabel=r'$R_{\mathrm{200}}$')
      axes[0, 0].vlines(17.7, 1e-4, 1e6, linestyle='dashed',__
       ⇔label=r'$R_{\mathrm{i}}$')
      axes[0, 0].legend(frameon=False, loc='upper left')
      axes[0, 1].loglog(radii, profile_encl_dm0_nu2, label='1e12')
      axes[0, 1].loglog(radii, profile_encl_dm1_nu2, label='1e13')
      axes[0, 1].loglog(radii, profile_encl_dm2_nu2, label='1e14')
      axes[0, 1].loglog(radii, profile_encl_dm3_nu2, label='1e15')
      axes[0, 1].loglog(radii, background_encl)
      axes[0, 1].set_xlabel('r (Mpc / h)')
```

```
axes[0, 1].set_title('Enclosed neutrino count 0.3 eV')
axes[0, 1].vlines(3.026, 1e-4, 1e6, linestyle='dashdot', ___
 ⇔label=r'$R_{\mathrm{200}}$')
axes[0, 1].vlines(17.7, 1e-4, 1e6, linestyle='dashed',_
 ⇔label=r'$R {\mathrm{i}}$')
axes[1, 0].loglog(radii, profile_encl_dm0_nu1, label='1e12')
axes[1, 0].loglog(radii, profile_encl_dm1_nu1, label='1e13')
axes[1, 0].loglog(radii, profile_encl_dm2_nu1, label='1e14')
axes[1, 0].loglog(radii, profile_encl_dm3_nu1, label='1e15')
axes[1, 0].loglog(radii, background_encl)
axes[1, 0].set xlabel('r (Mpc / h)')
axes[1, 0].set_title('Enclosed neutrino count 0.15 eV')
axes[1, 0].vlines(3.026, 1e-4, 1e6, linestyle='dashdot',__
 →label=r'$R_{\mathrm{200}}$')
axes[1, 0].vlines(17.7, 1e-4, 1e6, linestyle='dashed',
 ⇔label=r'$R_{\mathrm{i}}$')
axes[1, 1].loglog(radii, profile_encl_dm0_nu0, label='1e12')
axes[1, 1].loglog(radii, profile encl dm1 nu0, label='1e13')
axes[1, 1].loglog(radii, profile_encl_dm2_nu0, label='1e14')
axes[1, 1].loglog(radii, profile encl dm3 nu0, label='1e15')
axes[1, 1].loglog(radii, background_encl)
axes[1, 1].set_xlabel('r (Mpc / h)')
axes[1, 1].set_title('Enclosed neutrino count 0.06 eV')
axes[1, 1].vlines(3.026, 1e-4, 1e6, linestyle='dashdot', u
 ⇔label=r'$R_{\mathrm{200}}$')
axes[1, 1].vlines(17.7, 1e-4, 1e6, linestyle='dashed', __
 ⇔label=r'$R {\mathrm{i}}$')
for ax in axes.flatten():
   ax.set_xlim(1e-2, 5e1)
   ax.set_ylim(1e-4, 1e6)
plt.tight_layout
#plt.savefig('plot_save_vehicle.pdf')
plt.show()
```



[]: