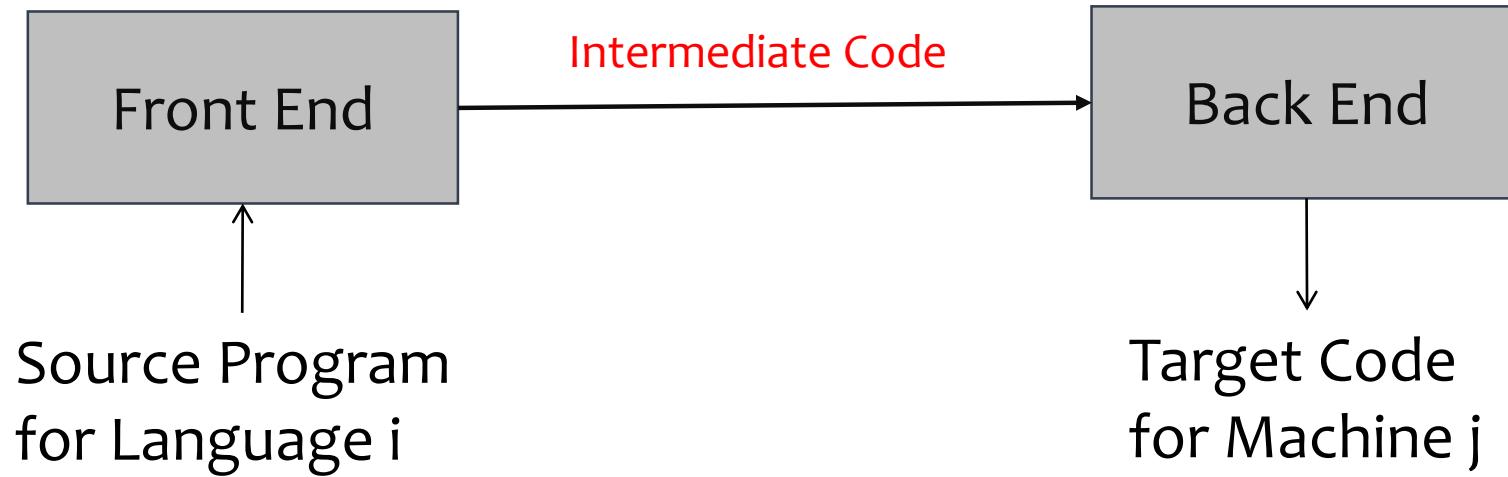


Chapter 6

Intermediate Code Generation

Intermediate Representation



Intermediate Representation

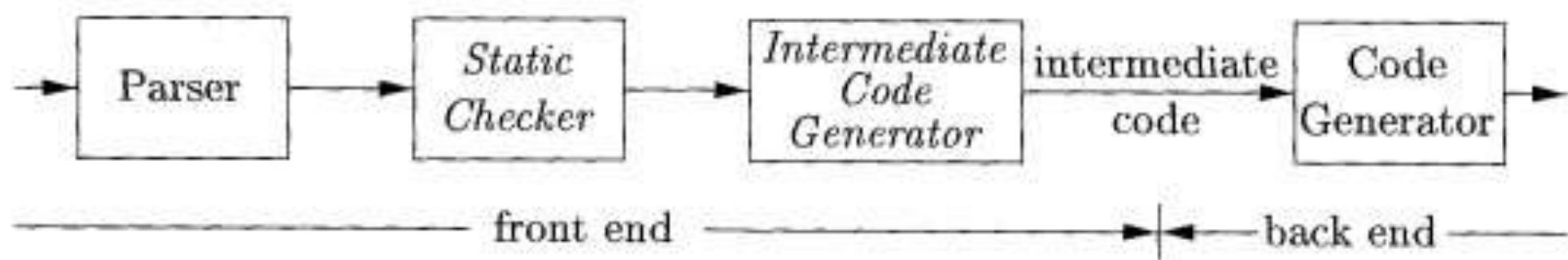


Figure 6.1: Logical structure of a compiler front end

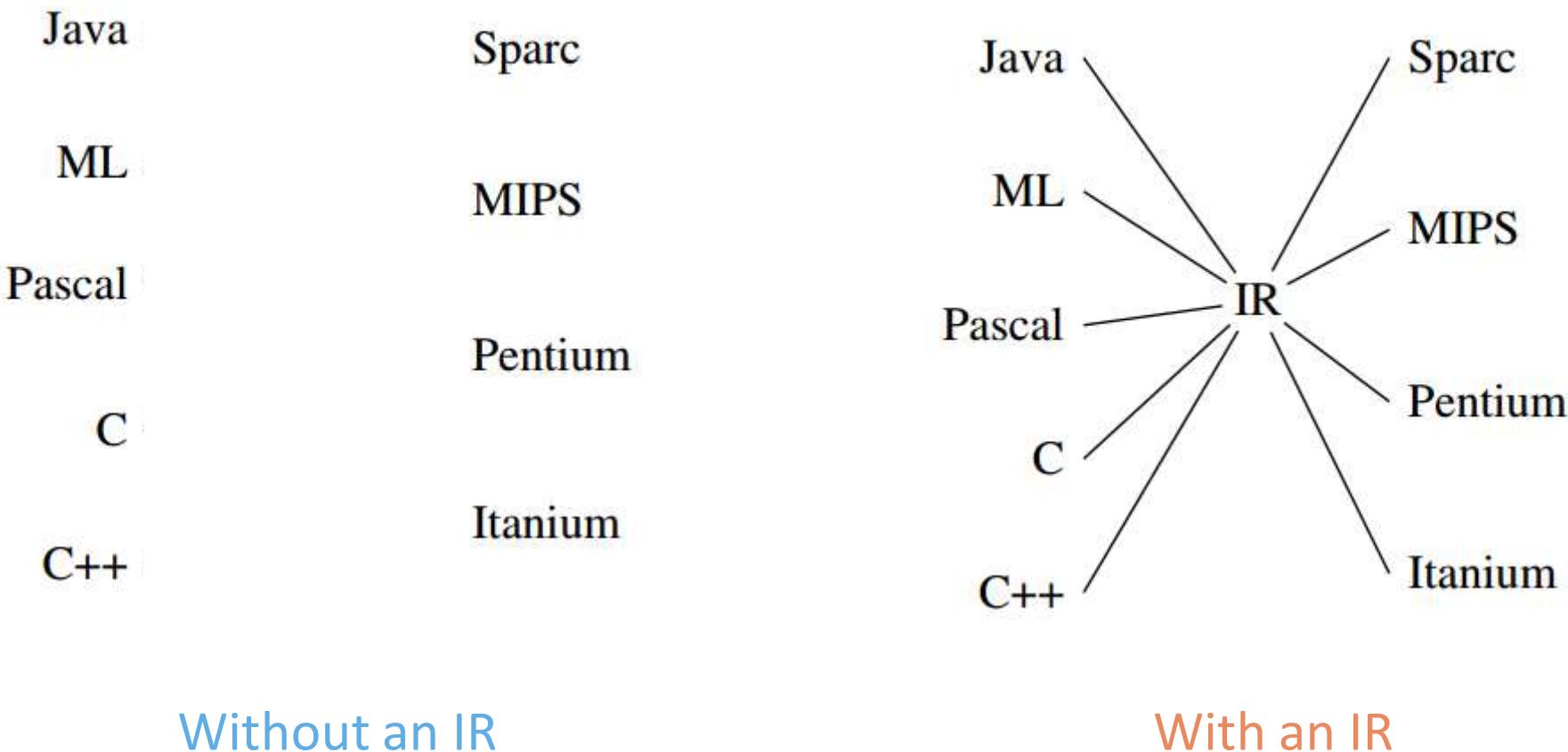
Intermediate Representation

- What is an **Intermediate Representation (IR)**?
 - Abstract Machine Language
 - Machine and Language independent version of source program
 - Can express target machine operation without committing too much machine specific details

Why Need IR?

- Modularity:
 - Front end is not complicated with machine specific details
 - Back end is not bothered with information specific to the source code
- Portability & Cross-Compilation:
 - For n source language and m machines, need only n front ends and m back ends
 - Without IR, a total of $n \times m$ compilers are required
- Simplify Certain Optimization:
 - Easier and clearer optimization tasks

Why Need IR?

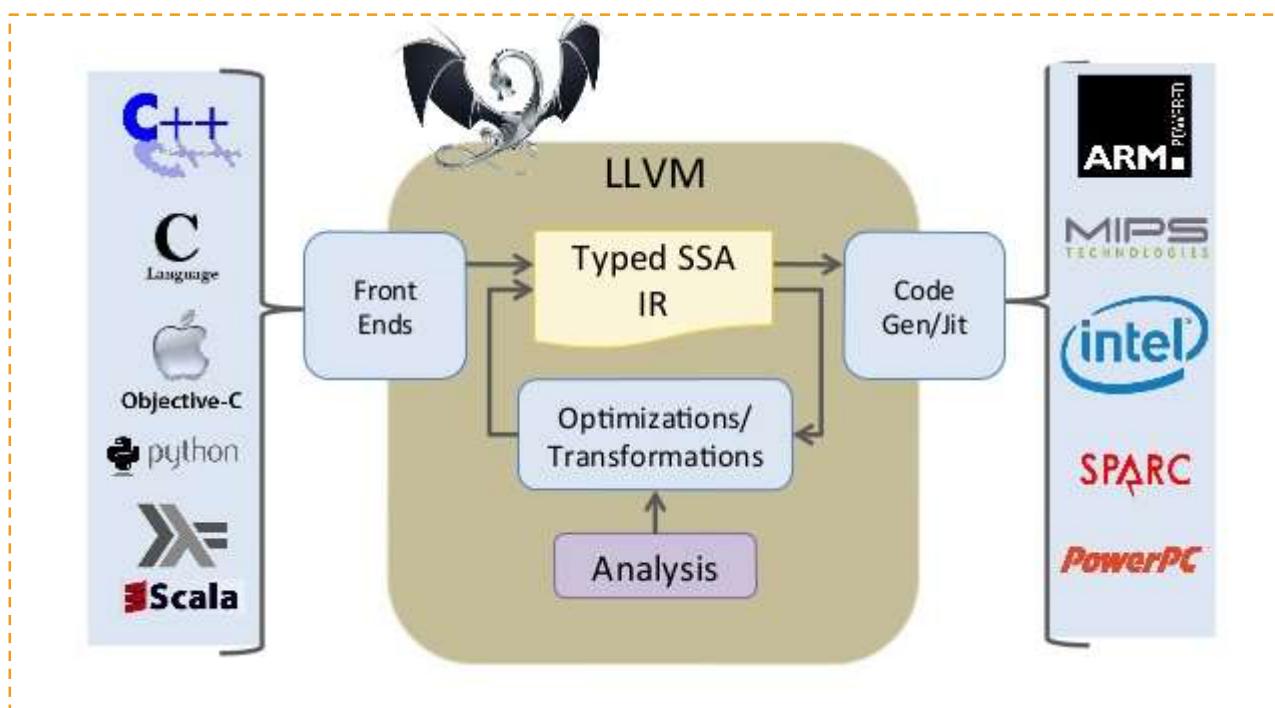
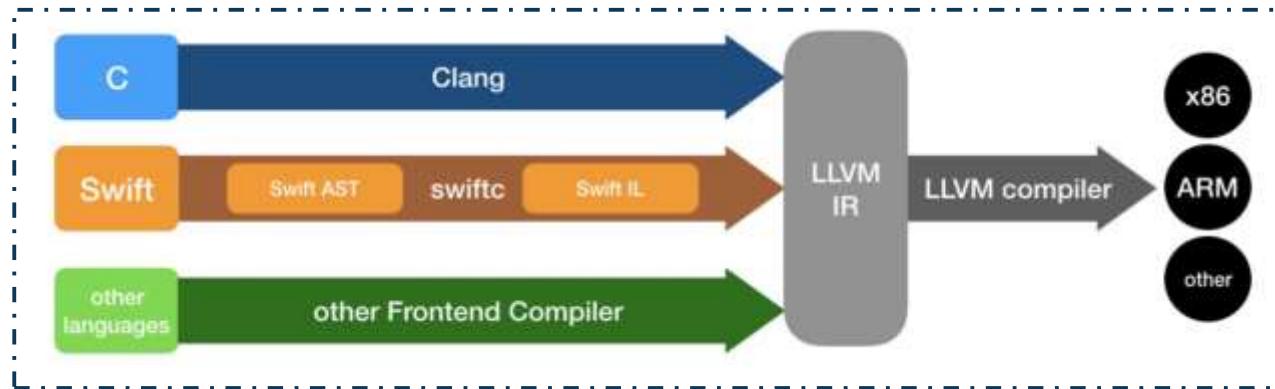


Without an IR

With an IR

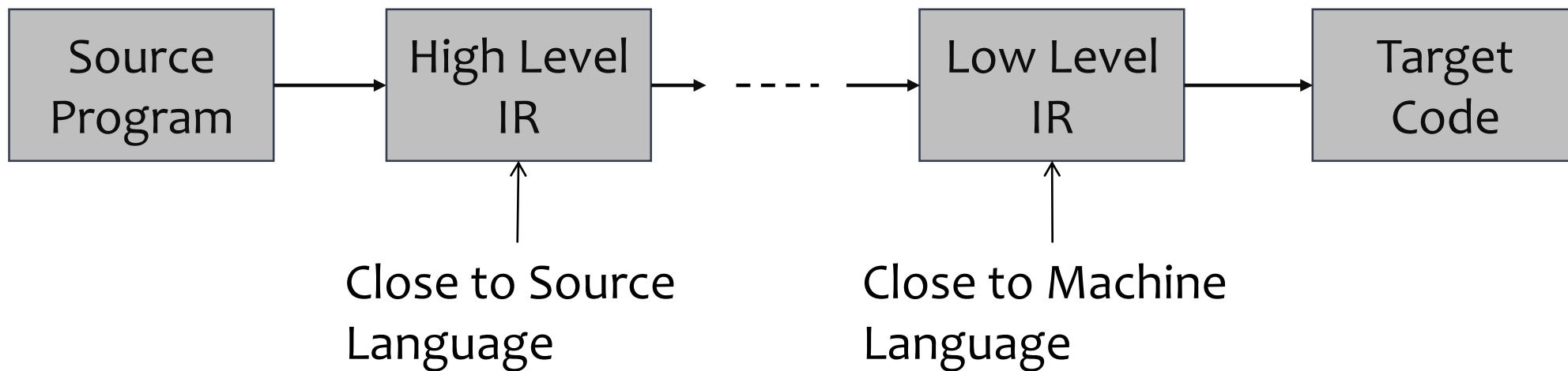
The LLVM Project

<https://www.llvm.org/>



Designing Good IR?

- Balance between high-level source language and low level machine language
- Often there are multiple IRs in a single compiler



Choice of an IR

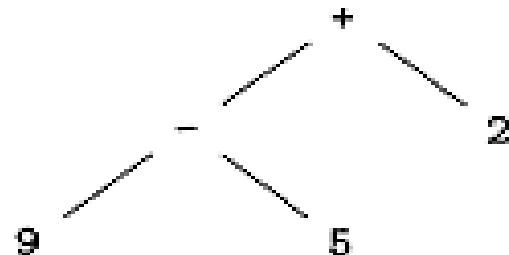
- The choice or design of an intermediate representation varies from compiler to compiler.
- An intermediate representation may either be
 - an actual language or
 - it may consist of internal data structures that are shared by phases of the compiler.
- C is a programming language, yet it is often used as an intermediate form because
 - it is flexible,
 - compiles into efficient machine code, and
 - its compilers are widely available.
- The original C + + compiler consisted of a front end that generated C, treating a C compiler as a back end.
- Another example: python compiler using C++ as an IR
(<https://github.com/Omyyyy/pycom>)

High and Low Level IRs

- High Level IRs:
 - Syntax Tree
 - DAG
 - Three Address Code with high level operators
- Low Level IRs:
 - Three Address Code with low level operators

Syntax Trees

- Syntax Tree:
 - Each node represents a construct of source program
 - Each children represent a meaningful component
 - Leaves correspond to atomic operands
 - Interior nodes correspond to operators

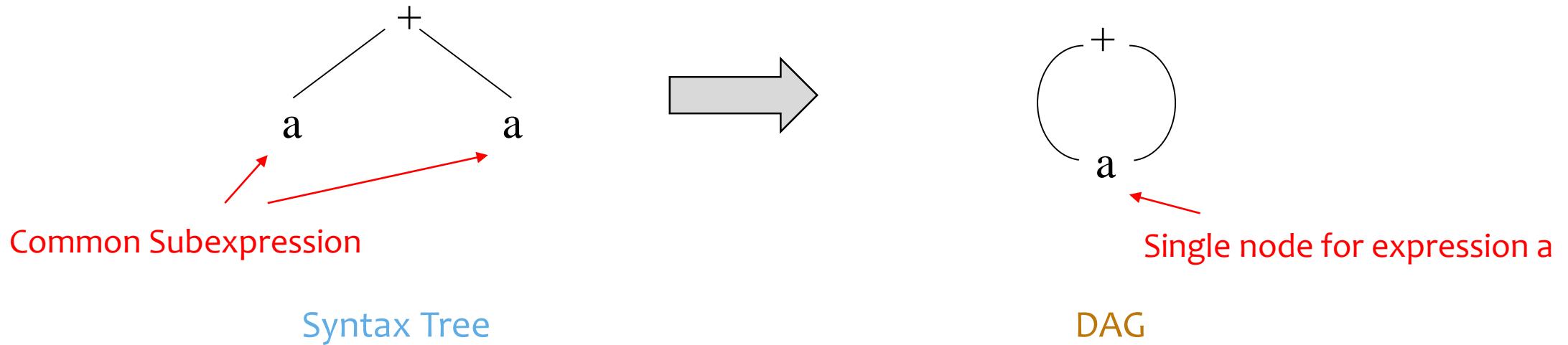


Syntax Tree for expression $9-5+2$

Directed Acyclic Graphs (DAG)

- Detect Common Subexpression

- Produce only one subtree for each subexpression
- Consider an expression: $a + a$

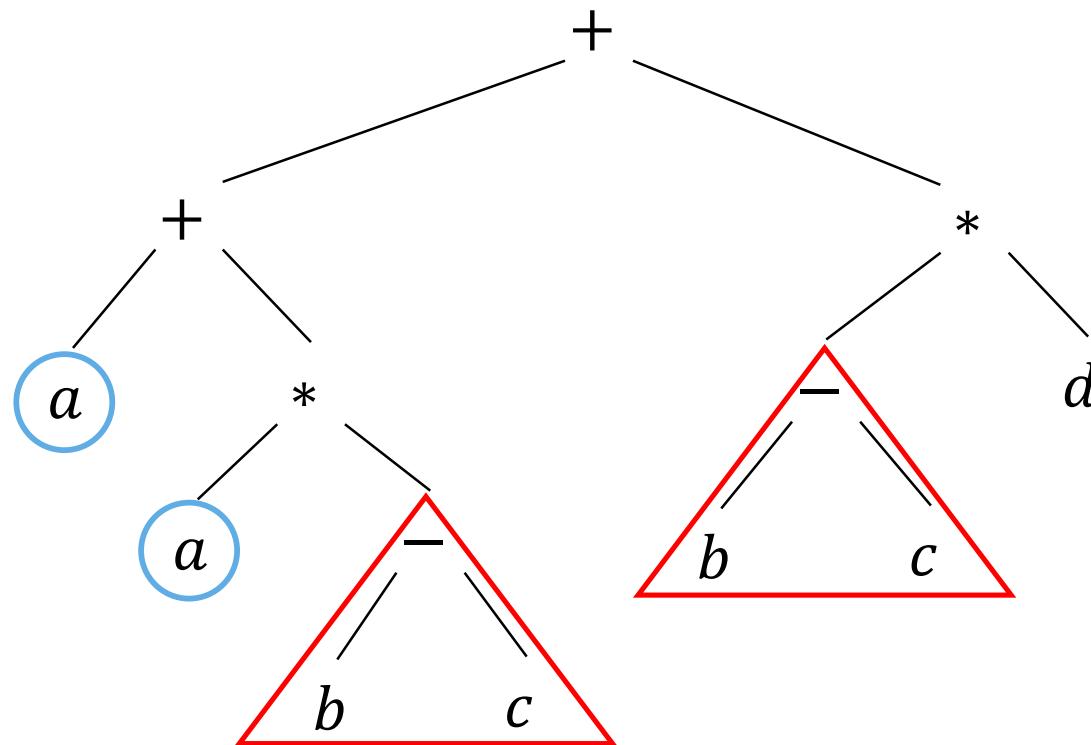


Directed Acyclic Graphs (DAG)

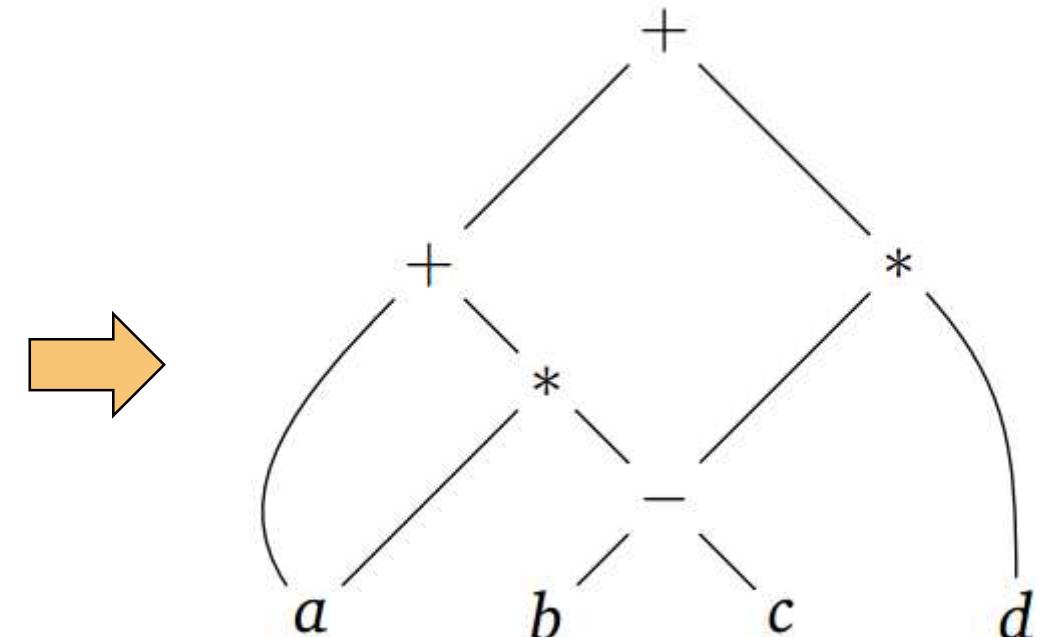
- A Node N can have more than one parent
 - If it represent a common subexpression
- Succinct Representation of Syntax Tree
- Provide clues for generating efficient code

Directed Acyclic Graphs (DAG)

- An example: $a + a * (b - c) + (b - c) * d$



Syntax Tree



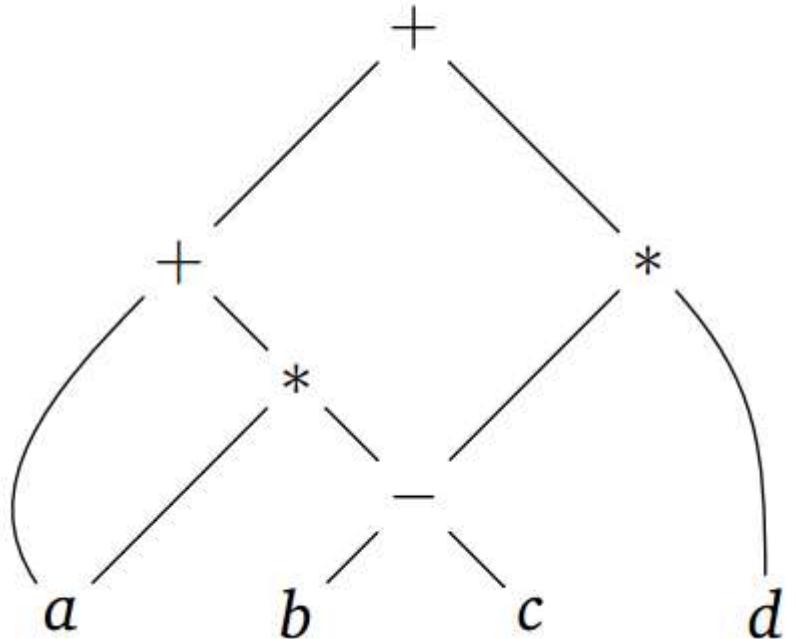
DAG

SDD for Constructing DAG

PRODUCTION	SEMANTIC RULES
1) $E \rightarrow E_1 + T$	
2) $E \rightarrow E_1 - T$	
3) $E \rightarrow T$	
4) $T \rightarrow (E)$	
5) $T \rightarrow \text{id}$	
6) $T \rightarrow \text{num}$	

- Wait!! What?? This SDD constructs Syntax Tree!
- The Leaf and Node functions will return a previously created identical node if exist, otherwise return a newly created one
- Identical Node means the subtree rooted at that node is same

SDD for constructing DAG

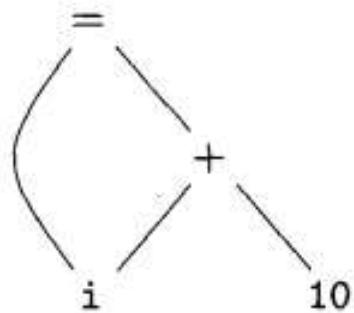


DAG for expression: $a + a * (b - c) + (b - c) * d$

- 1) $p_1 = \text{Leaf}(\text{id}, \text{entry-}a)$
- 2) $p_2 = \text{Leaf}(\text{id}, \text{entry-}a) = p_1$
- 3) $p_3 = \text{Leaf}(\text{id}, \text{entry-}b)$
- 4) $p_4 = \text{Leaf}(\text{id}, \text{entry-}c)$
- 5) $p_5 = \text{Node}(' - ', p_3, p_4)$
- 6) $p_6 = \text{Node}(' * ', p_1, p_5)$
- 7) $p_7 = \text{Node}(' + ', p_1, p_6)$
- 8) $p_8 = \text{Leaf}(\text{id}, \text{entry-}b) = p_3$
- 9) $p_9 = \text{Leaf}(\text{id}, \text{entry-}c) = p_4$
- 10) $p_{10} = \text{Node}(' - ', p_3, p_4) = p_5$
- 11) $p_{11} = \text{Leaf}(\text{id}, \text{entry-}d)$
- 12) $p_{12} = \text{Node}(' * ', p_5, p_{11})$
- 13) $p_{13} = \text{Node}(' + ', p_7, p_{12})$

Steps of constructing the left DAG

Value Number Method for Constructing DAG



(a) DAG

id	
num	10
+	1 2
=	1 3
...	

(b) Array.

First Field is an **operation code** (label of the node)

- Nodes of AST or DAG can be stored in array or records (structures)
- Each row represent one record (one node)
- Reference to a node is the index of the node in the array
 - The integer index is called the value number of the node
- The value number of + node is 3

Value Number Method

- Algorithm for constructing Nodes of DAG (Node and Leaf function)
 - **Input:** Label op , Node l and Node r (For leaf node $r = 0$)
 - **Output:** The value number of a node in the array with signature $< op, l, r >$
 - **Method:**
 - Search array for a node M with label op , left child l and right child r
 - If found return value number of M
 - Otherwise create in the array a new node N with label op , left child l and right child r
 - Return value number of N

Value Number Method

- Searching the entire array every time to check whether a node exists is expensive
- Use Hash Table
- Hash using $< op, l, r >$ as hash key

Three Address Code

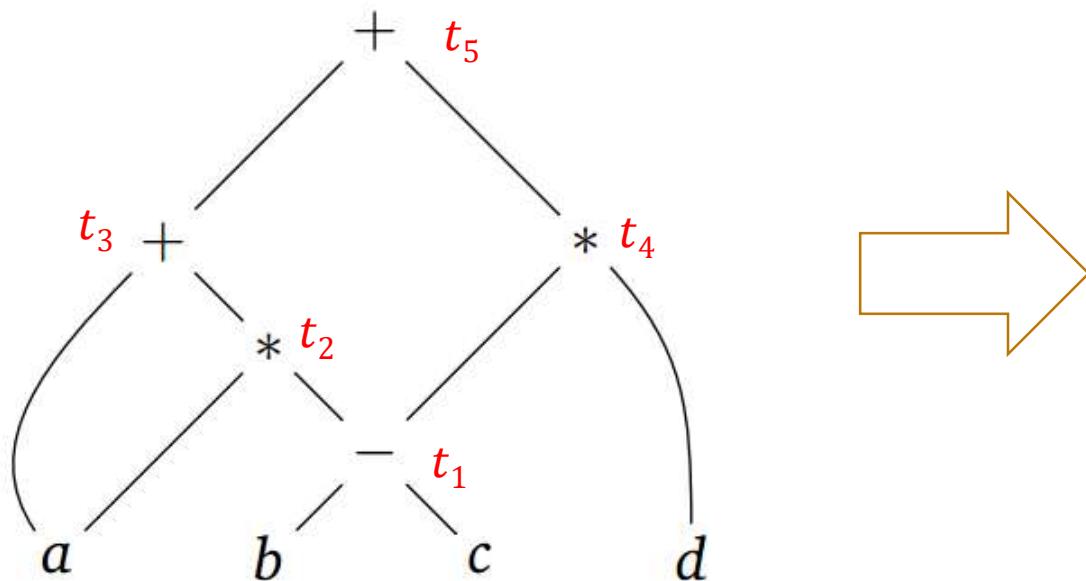
- At most one operator at the right side of an instruction
- For expression $x * y + z$ three address code is

$$\begin{aligned}t_1 &= x * y \\t_2 &= z + t_1\end{aligned}$$

- t_1 and t_2 are compiler generated names

Three Address Code

- Linearized representation for DAG
 - Explicit name corresponds to the interior nodes
 - Each instruction in the sequence has a label



DAG for expression: $a + a * (b - c) + (b - c) * d$

$t_1 = b - c$
 $t_2 = a * t_1$
 $t_3 = a + t_2$
 $t_4 = t_1 * d$
 $t_5 = t_3 + t_4$

Three Address Code

Three Address Code

- Based on Two concepts:
 - Address
 - What address can be used in the code
 - Instruction
 - What kind of instruction sets can be applied

Address

- Name
 - Name from source program
 - Example: x, y, z
 - May be replaced by pointer to symbol table entry in implementation
- Constant
 - Example: 2.3, 1
- Compiler generated temporary
 - Example: t_1, t_2

Instructions

- Assignment instructions
 - $x = y \ op \ z$ where x, y, z are addresses and op is a binary operator
 - $x = op \ y$ where op is a unary operation such as unary minus, logical negation and conversion operator
- Copy instruction: $x = y$
 - x is assigned the value of y
- An unconditional jump : *goto L*
 - Instruction with label L is executed next
- Conditional jumps:
 - *if x goto L*
 - *ifFalse x goto L*
 - *if x relop y goto L*

Instructions

- Procedure calls and returns:
 - *param x* for parameters
 - *call p, n* or *y = call p, n* for procedure/function calls
 - *return y* represent returning a value
 - For procedure *proc(x₁, x₂, ..., x_n)*
 - param x₁*
 - param x₂*
 - ...
 - param x_n*
 - call proc,n*

Instructions

- **Indexed copy instructions:**
 - $x = y[i]$ sets x to the value in the location i memory units beyond location y .
 - $x[i] = y$ sets the contents of the location i units beyond x to the value of y
- **Address and Pointers assignments:**
 - $x = \& y$
 - $x = * y$
 - $* x = y$

Assigning Labels

- Example: `do i = i + 1; while(a[i] < v);`

*L : t₁ = i + 1
i = t₁
t₂ = i * 8
t₃ = a[t₂]
if t₃ < v goto L*

Symbolic Labels

*100 : t₁ = i + 1
101 : i = t₁
102 : t₂ = i * 8
103 : t₃ = a[t₂]
104 : if t₃ < v goto 100*

Position Numbers

Choice of Operators

- The choice of allowable operators is an important issue
 - The operator set clearly must be rich enough to implement the operations in the source language.
 - Operators that are close to machine instructions make it easier to implement the intermediate form on a target machine.
 - However, if the front end must generate long sequences of instructions for some source-language operations, then the optimizer and code generator may have to work harder to rediscover the structure and generate good code for these operations.

Representing Three Address Code

- What is the suitable data structure to represent three address code?
- Can be represented using objects or record with operators and operands as fields
- Three representations:
 - Quadruples
 - Triples
 - Indirect Triples

Quadruples

- **Four Fields:**

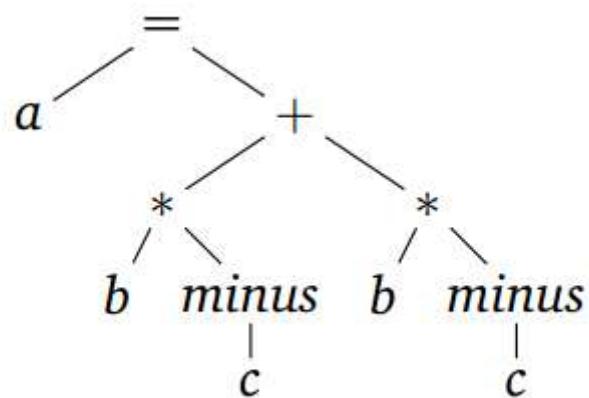
- *op* – represent operator
- *arg1, arg2* – holding operands
- *result* – hold result of the operation

- **Exceptions:**

- Unary Operators: no *arg2*
- param operator: no *arg2*, no *result*
- (Un)conditional jump: target label is the *result*

Quadruples

- Example: $a = b * -c + b * -c;$



$t_1 = \text{minus } c$
 $t_2 = b * t_1$
 $t_3 = \text{minus } c$
 $t_4 = b * t_3$
 $t_5 = t_2 + t_4$
 $a = t_5$

	OP	ARG1	ARG2	RESULT
0	minus	c		t_1
1	*	b	t_1	t_2
2	minus	c		t_3
3	*	b	t_3	t_4
4	+	t_2	t_4	t_5
5	=	t_5		a

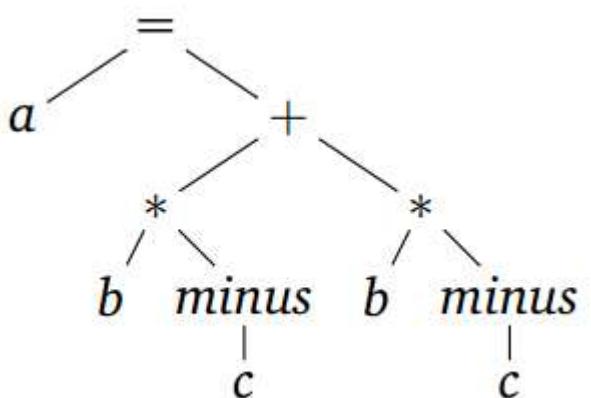
Syntax Tree

Three Address Code

Quadruples

Triples

- Three fields:
 - $op, arg1, arg2$
 - No result field
 - result referred by their position
- Example: $a = b * -c + b * -c;$



Syntax Tree

$$\begin{aligned} t_1 &= \text{minus } c \\ t_2 &= b * t_1 \\ t_3 &= \text{minus } c \\ t_4 &= b * t_3 \\ t_5 &= t_2 + t_4 \\ a &= t_5 \end{aligned}$$

Three Address Code

	OP	ARG1	ARG2
0	minus	c	
1	*	b	(0)
2	minus	c	
3	*	b	(2)
4	+	(1)	(3)
5	=	a	(4)

Triples

Triples

- Optimization by moving instructions is difficult in Triples, but easy in Quadruples
- Moving instructions forces to adjust the arguments where that position appear

	OP	ARG1	ARG2
0	<i>minus</i>	<i>c</i>	
1	*	<i>b</i>	(0)
2	<i>minus</i>	<i>c</i>	
3	*	<i>b</i>	(2)
4	+	(1)	(3)
5	=	<i>a</i>	(4)

Triples

Indirect Triples

- Listing pointers to the triples instead of triples
- Reorder the pointers instead of the tuples itself during code motion

	OP	ARG1	ARG2
0	<i>minus</i>	<i>c</i>	
1	*	<i>b</i>	(0)
2	<i>minus</i>	<i>c</i>	
3	*	<i>b</i>	(2)
4	+	(1)	(3)
5	=	<i>a</i>	(4)

Triples

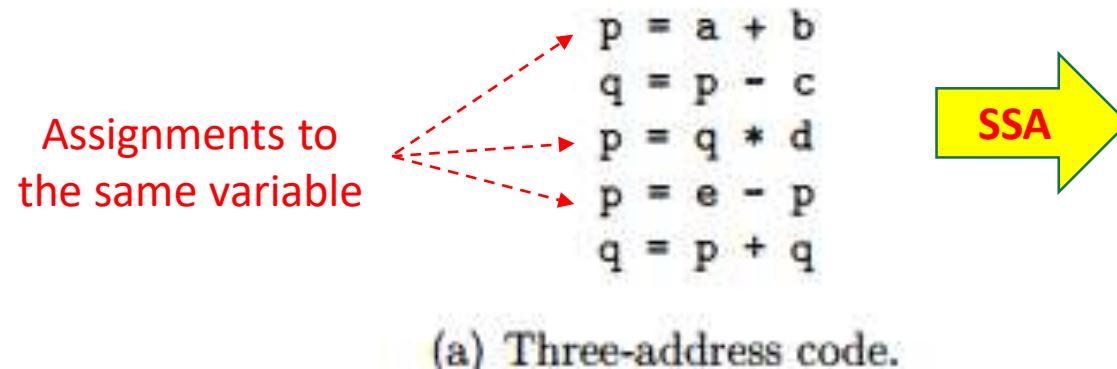
	INSTRUCTION
35	(0)
36	(1)
37	(2)
38	(3)
39	(4)
40	(5)

Indirect Triples

	OP	ARG1	ARG2
0	<i>minus</i>	<i>c</i>	
1	*	<i>b</i>	(0)
2	<i>minus</i>	<i>c</i>	
3	*	<i>b</i>	(2)
4	+	(1)	(3)
5	=	<i>a</i>	(4)

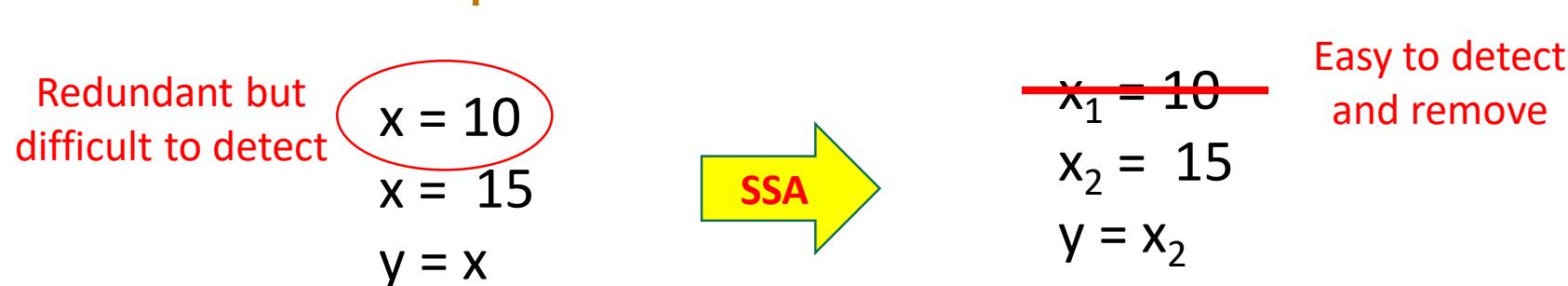
Static Single Assignment Form (SSA)

- Another form of IR
- All assignments are to variables with distinct names



(a) Three-address code.

- Facilitates code optimizations



Static Single Assignment Form (SSA)

- Converting ordinary code into SSA form
 - Replace the target of each assignment with a new variable
 - Replacing each use of a variable with the "version" of the variable reaching that point.
- What to do when branching is involved?

```
if (flag) x = -1  
else x = 1  
y = x*a
```



```
if (flag) x1 = -1  
else x2 = 1  
y = x?*a
```

- Φ functions to combine two definitions of the same variable x

```
if (flag) x = -1; else x = 1  
y = x*a
```



```
if (flag) x1 = -1; else x2 = 1  
x3 =  $\phi(x_1, x_2)$   
y = x3*a
```

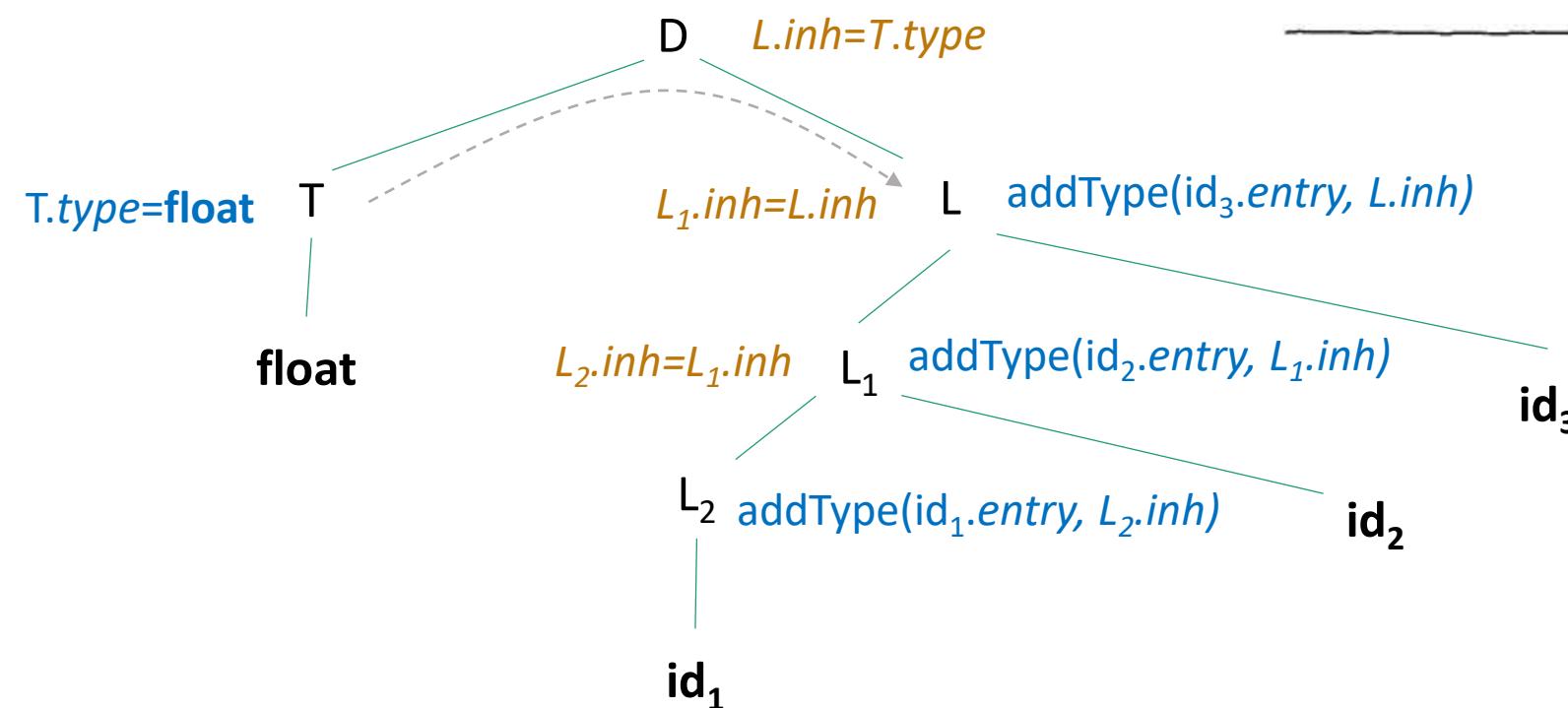
For further details see: https://en.wikipedia.org/wiki/Static_single-assignment_form

Types and Declarations

- Application of types
 - Type Checking
 - Uses logical rules to reason about the behavior of a program at run time
 - Ensures that the types of the operands match the type expected by an operator
 - **Example:** the `&&` operator in java expects its two operands to be booleans; the result type is also boolean
 - Translation Applications
 - From the type of a name, a compiler can determine its required storage at runtime
 - Type information is also needed
 - to calculate the address denoted by an array reference
 - to insert explicit type conversion
 - to choose the right version of an arithmetic operator

Computing Types

- Let us compute an SDD to support declarations like
 - int id1, id2, id3
 - float id1, id2, id3



PRODUCTION	SEMANTIC RULES

Parse tree for the declaration:
float id1, id2, id3

Type Expressions

- Type expressions are used to represent structures of types
- A type expression is either a basic type or is formed by applying an operator called a *type constructor* to a type expression
- The sets of basic types and constructors depend on the language to be checked

Example: The array type `int [2] [3]` can be

- read as “array of two arrays of 3 integers each”
- written as a type expression
`array(2,array(3,integer))`
 - the operator `array` takes two parameters, a number and a type

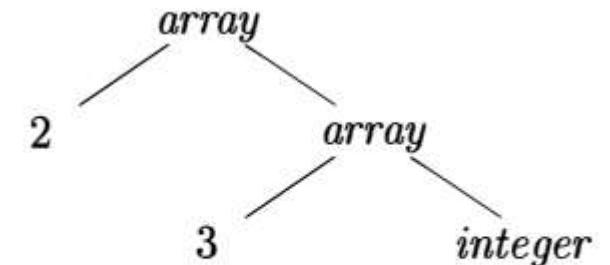


Figure 6.14: Type expression for `int [2] [3]`

- Type expressions can be represented using a graph and the **value-number method** can be used to store type expressions.

Definition of Type Expressions

- A **basic type** is a **type expression** such as **boolean, float, char, integer and void**
- A **type name** is a **type expression** such as name of a record, structure or class
- A **type expression** can be formed by applying the **array** type constructor to a number and a type expression
- A **record** is a data structure with named fields. A type name can be formed by applying the **record** type constructor to the field names and their types
- A type expression can be formed by using the type constructor \rightarrow for function types.
 - $s \rightarrow t$ denotes “function from type s to type t”
- If s and t are **type expressions**, then their Cartesian product **$s \times t$** is a type expression.
 - Is used to represent a list or tuple of tuples (e.g., for function parameters)
- Type expressions may contain variables whose values are **type expressions**

Type Equivalence

- Many type-checking rules have the form, “if two type expressions are equal then return a certain type else error”
- When **type expressions** are represented by graphs, two types are **structurally equivalent** if and only if one of the following conditions hold
 - They are the same basic type.
 - They are formed by applying the same constructor to structurally equivalent types
 - One is a type name that denotes the other

Storage Layout for Local Names

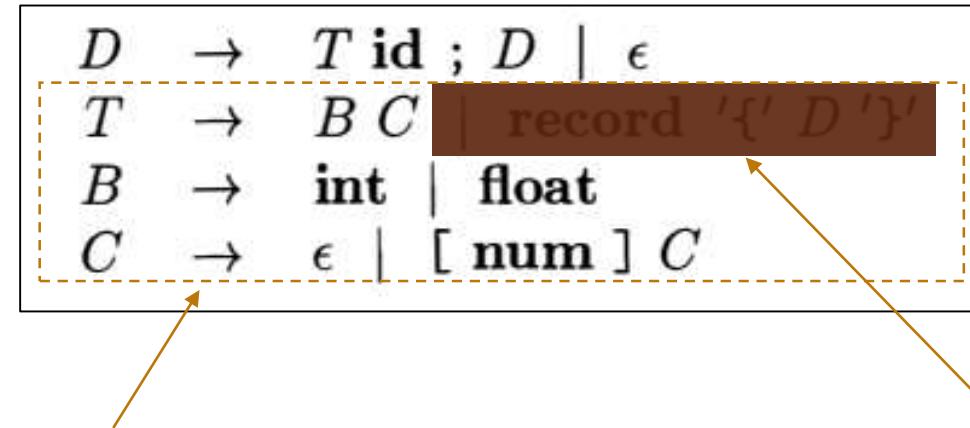
- From the type of a name, the amount of storage required for it during runtime can be determined
- At compile time, these amounts can be used to assign each name a relative address
- The type and relative address are saved in the symbol-table entry for the name
- Data of varying length, such as strings, dynamic arrays is handled by reserving a known fixed amount of storage for a pointer to the data

Storage Layout for Local Names (2)

- The **width** of a type is the number of storage units needed for objects of that type
 - we consider a byte as the smallest unit of addressable memory
- A basic type, such as a **character**, **integer**, or **float**, requires an integral number of bytes
- For easy access, storage for aggregates such as **arrays** and **classes** is allocated in one contiguous block of bytes

Computing Types and Their Widths

- A modified grammar
- Supports declarations like
 - **int id; float id;**
 - **int[2][3][3] id;**
 - **record { int id; int[2][3] id2 } id**

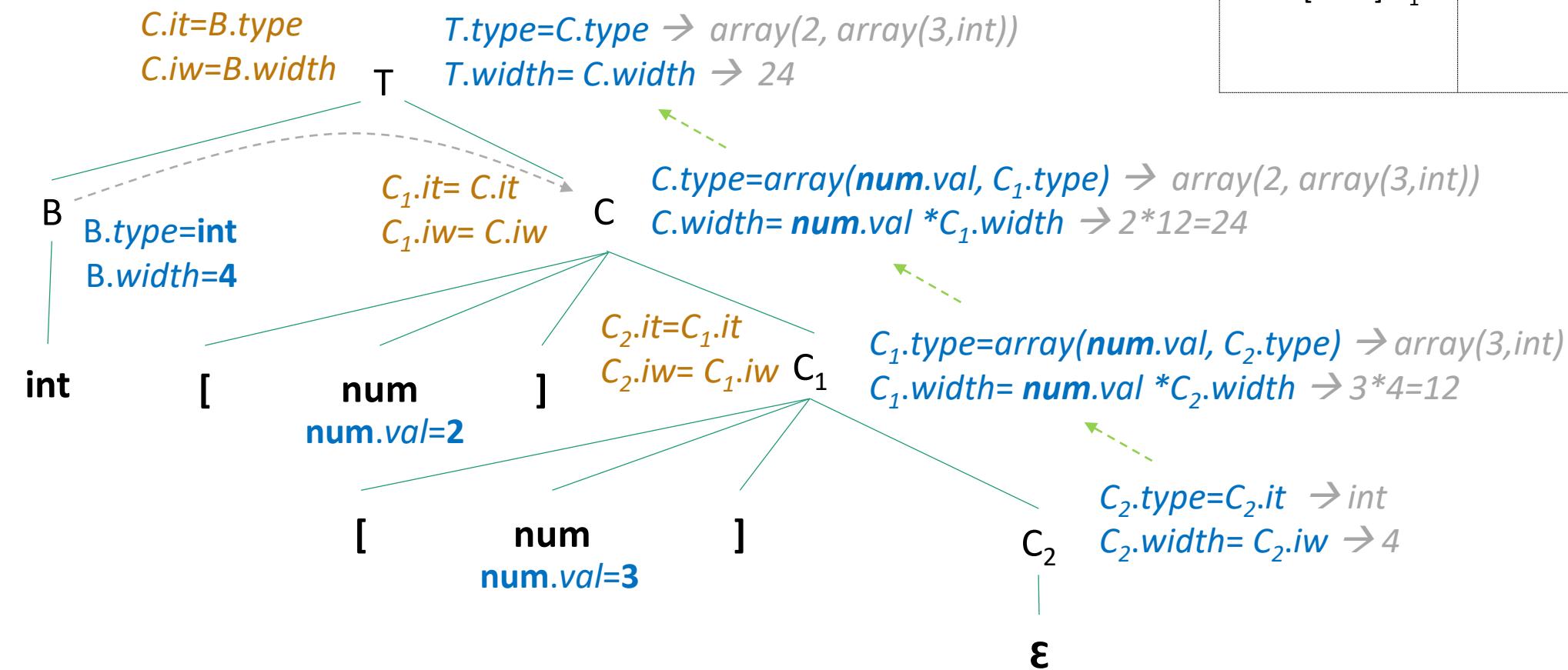


Let's start with the productions related to type definition

For the next example we omit the record part

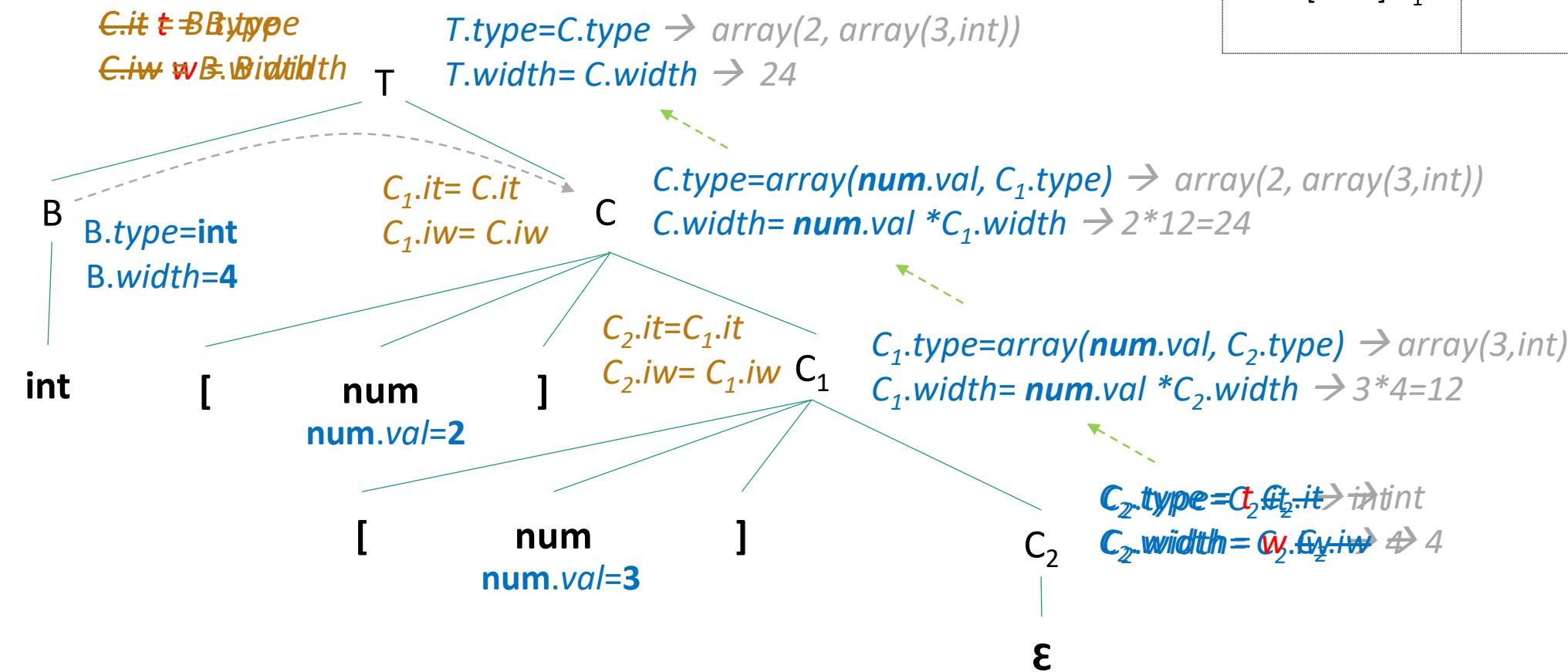
Prod.	Semantic Rules
$T \rightarrow BC$	
$B \rightarrow \text{int}$	
$B \rightarrow \text{float}$	
$C \rightarrow \epsilon$	
$C \rightarrow [\text{num}] C_1$	

Annotated Parse tree for $\text{int}[2][3]$



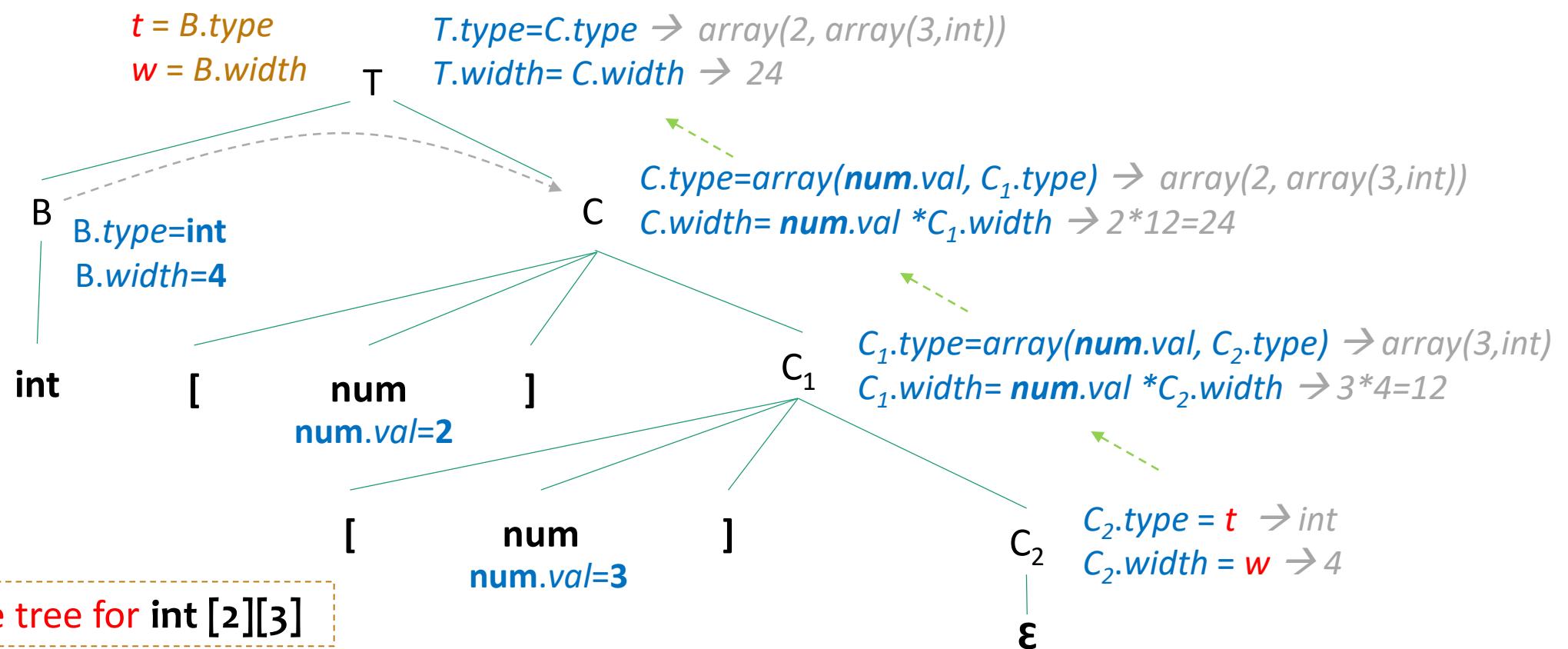
Prod.	Semantic Rules
$T \rightarrow BC$	
$B \rightarrow \text{int}$	
$B \rightarrow \text{float}$	
$C \rightarrow \epsilon$	
$C \rightarrow [\text{num}] C_1$	

Annotated Parse tree for $\text{int}[2][3]$



Use of global variables instead of inherited attributes

SDT for Computing Type and Width		Prod.	Semantic Rules
$T \rightarrow B$	{ $t = B.type$, $w = B.width$ }	$T \rightarrow B C$	$t = B.type$, $w = B.width$
C	{ $T.type = C.type$ $T.width = C.width$ }	$B \rightarrow int$	$T.type = C.type$ $T.width = C.width$
$B \rightarrow int$	{ $B.type = float$, $B.width = 4$ }	$B \rightarrow float$	$B.type = float$, $B.width = 4$
$B \rightarrow float$	{ $B.type = int$, $B.width = 8$ }	$C \rightarrow \epsilon$	$B.type = int$, $B.width = 8$
$C \rightarrow \epsilon$	{ $C.type = t$, $C.width = w$ }	$C \rightarrow [num] C_1$	$C.type = t$, $C.width = w$
$C \rightarrow [num] C_1$	{ $C.type = array(num.val, C_1.type)$ $C.width = num.val * C_1.width$ }		$C.type = array(num.val, C_1.type)$ $C.width = num.val * C_1.width$



Computing Relative Addresses

```
int main(){
    int a,b,c;
    a=1;
    b=2;
    c=1;
    return 0;
}
```

CPP

```
main:
    push    rbp
    mov     rbp, rsp
    mov     DWORD PTR [rbp-4], 1
    mov     DWORD PTR [rbp-8], 2
    mov     DWORD PTR [rbp-12], 1
    mov     eax, 0
    pop    rbp
    ret
```

ASM (x86-64 gcc 11.1)

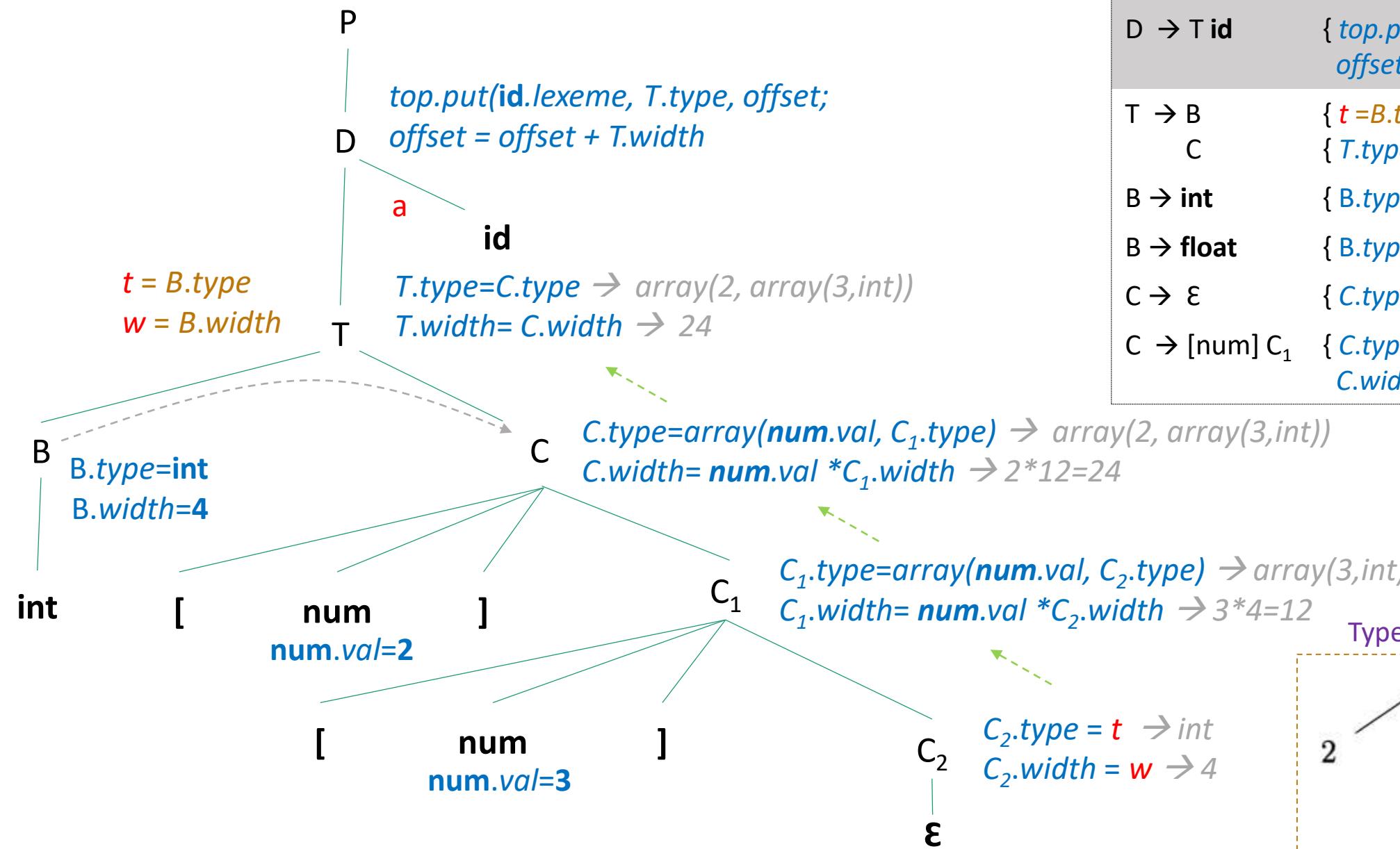
$$P \rightarrow \{ \text{offset} = 0; \} \ D$$
$$D \rightarrow T \text{id} ; \quad \{ \text{top.put(id.lexeme, T.type, offset);}$$
$$\text{offset} = \text{offset} + T.\text{width}; \}$$
$$D \rightarrow \epsilon$$

SDT for computing relative addresses

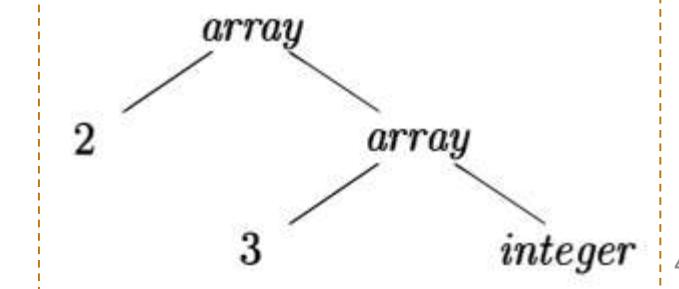
SDT for Computing Type and Width

$P \rightarrow$	{ $offset = 0;$ }
$D \rightarrow$	
$D \rightarrow T \text{id}$	{ $\text{top.put}(\text{id.lexeme}, T.type, offset);$ $offset = offset + T.width$ }
$T \rightarrow B$	{ $t = B.type, w = B.width$ }
C	{ $T.type = C.type, T.width = C.width$ }
$B \rightarrow \text{int}$	{ $B.type = \text{float}, B.width = 4$ }
$B \rightarrow \text{float}$	{ $B.type = \text{int}, B.width = 8$ }
$C \rightarrow \epsilon$	{ $C.type = t, C.width = w$ }
$C \rightarrow [\text{num}] C_1$	{ $C.type = \text{array}(\text{num.val}, C_1.type)$ $C.width = \text{num.val} * C_1.width$ }

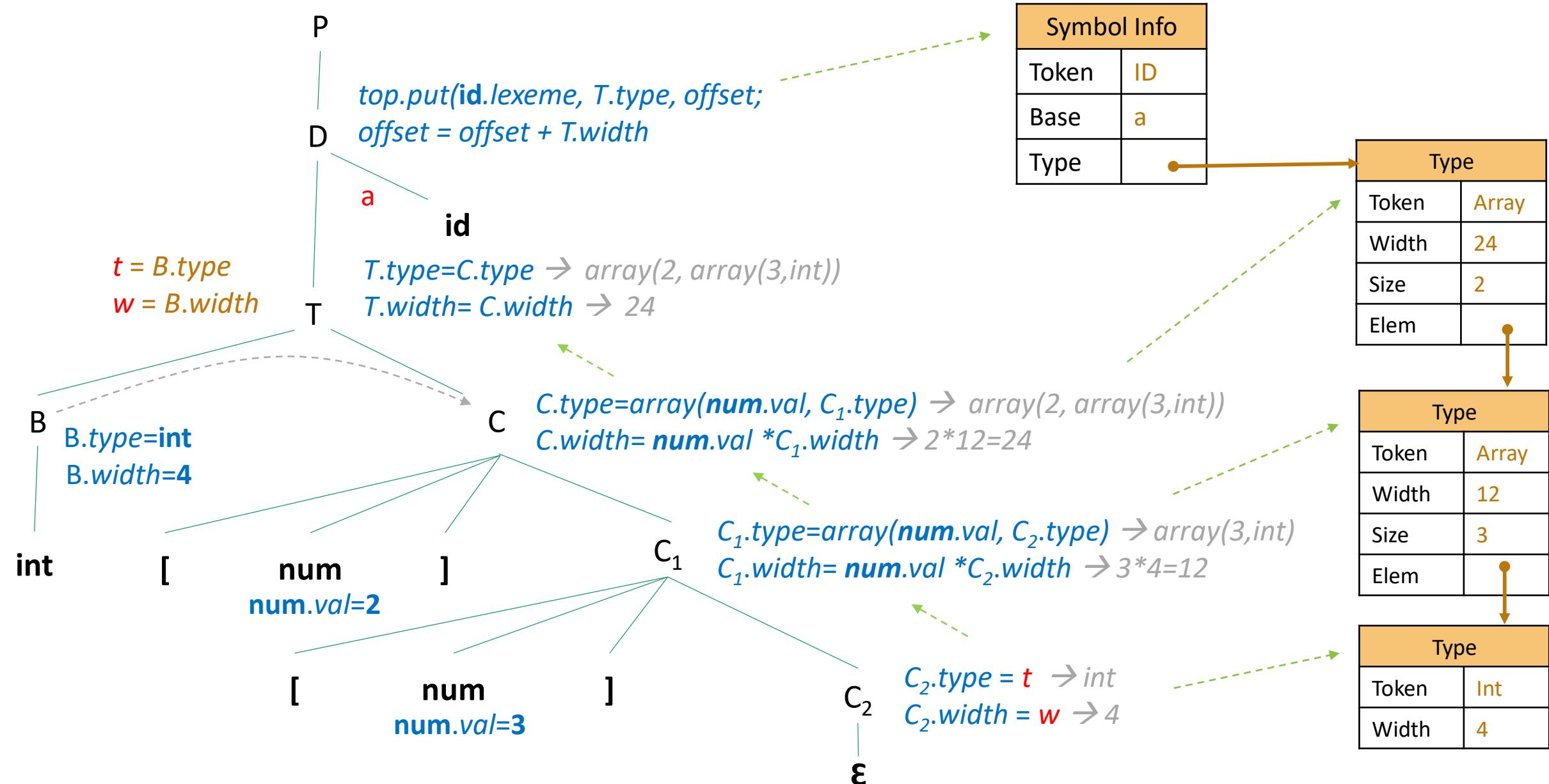
Annotated Parse tree for $\text{int}[2][3] \text{a}$



Type expression for $\text{int}[2][3]$



Annotated Parse tree for `int [2][3] a`



Fields in Records and Classes

```
struct Info {  
    int x, y, z;  
};  
int main(){  
    struct Info a;  
    struct Info b;  
    int x;  
    x=a.x+b.x;  
    return 0;  
}
```

CPP

```
main:  
    push    rbp  
    mov     rbp, rsp  
    mov     edx, DWORD PTR [rbp-16]  
    mov     eax, DWORD PTR [rbp-28]  
    add     eax, edx  
    mov     DWORD PTR [rbp-4], eax  
    mov     eax, 0  
    pop     rbp  
    ret
```

ASM (x86-64 gcc 11.1)

$T \rightarrow \text{record } \{ D \}$

$T \rightarrow \text{record } \{ \begin{array}{l} \text{Env.push}(top); top = \text{new Env}(); \\ \text{Stack.push}(offset); offset = 0; \end{array} \}$

$D \}$

$\{ T.type = \text{record}(top); T.width = offset; \\ top = \text{Env.pop}(); offset = \text{Stack.pop}(); \}$

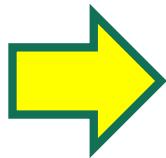
type constructor

symbol table object

Three Address Code Generation

An Example

```
1) {           // File test
2)   int i; int j; float v; float x; float[100] a;
3)   while( true ) {
4)     do i = i+1; while( a[i] < v );
5)     do j = j-1; while( a[j] > v );
6)     if( i >= j ) break;
7)     x = a[i]; a[i] = a[j]; a[j] = x;
8)   }
9) }
```



```
1) L1:L3:  i = i + 1
2) L5:      t1 = i * 8
3)          t2 = a [ t1 ]
4)          if t2 < v goto L3
5) L4:      j = j - 1
6) L7:      t3 = j * 8
7)          t4 = a [ t3 ]
8)          if t4 > v goto L4
9) L6:      iff false i >= j goto L8
10) L9:     goto L2
11) L8:     t5 = i * 8
12)          x = a [ t5 ]
13) L10:    t6 = i * 8
14)          t7 = j * 8
15)          t8 = a [ t7 ]
16)          a [ t6 ] = t8
17) L11:    t9 = j * 8
18)          a [ t9 ] = x
19)          goto L1
20) L2:
```

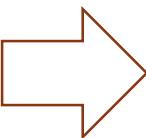
Translation of Expressions

- Need to convert an expression with more than one operator in source program to Three Address Codes with only one operator
 - $a * b + c$
- An array reference will expand in sequence of Three Address Codes that calculate the address for the reference
 - $A[i][j]$

Translation of Expressions

```
int initial = 32;  
float rate = .8;  
float position = initial + rate * 60 ;
```

Source code



```
int t1 = 32  
int initial = t1  
float t2 = .8  
float rate = t2  
int t3 = initial  
float t4 = rate  
int t5 = 60  
float t6 = (float) t3  
float t7 = t4 * t6  
float t8 = t6 + t7
```

E.code

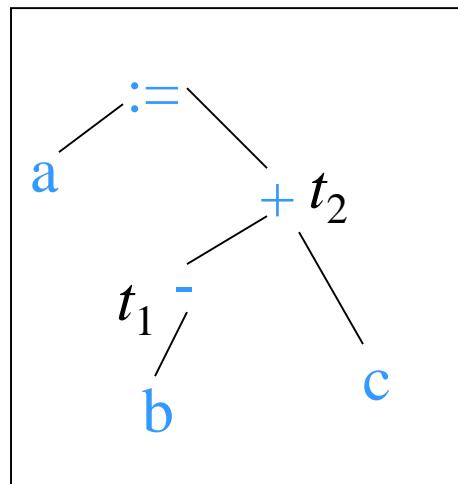
↓ *E.addr*

```
float position = t8
```

Corresponding Three Address Code

Translation of Expressions

An Example Expression: $a := -(b) + c$



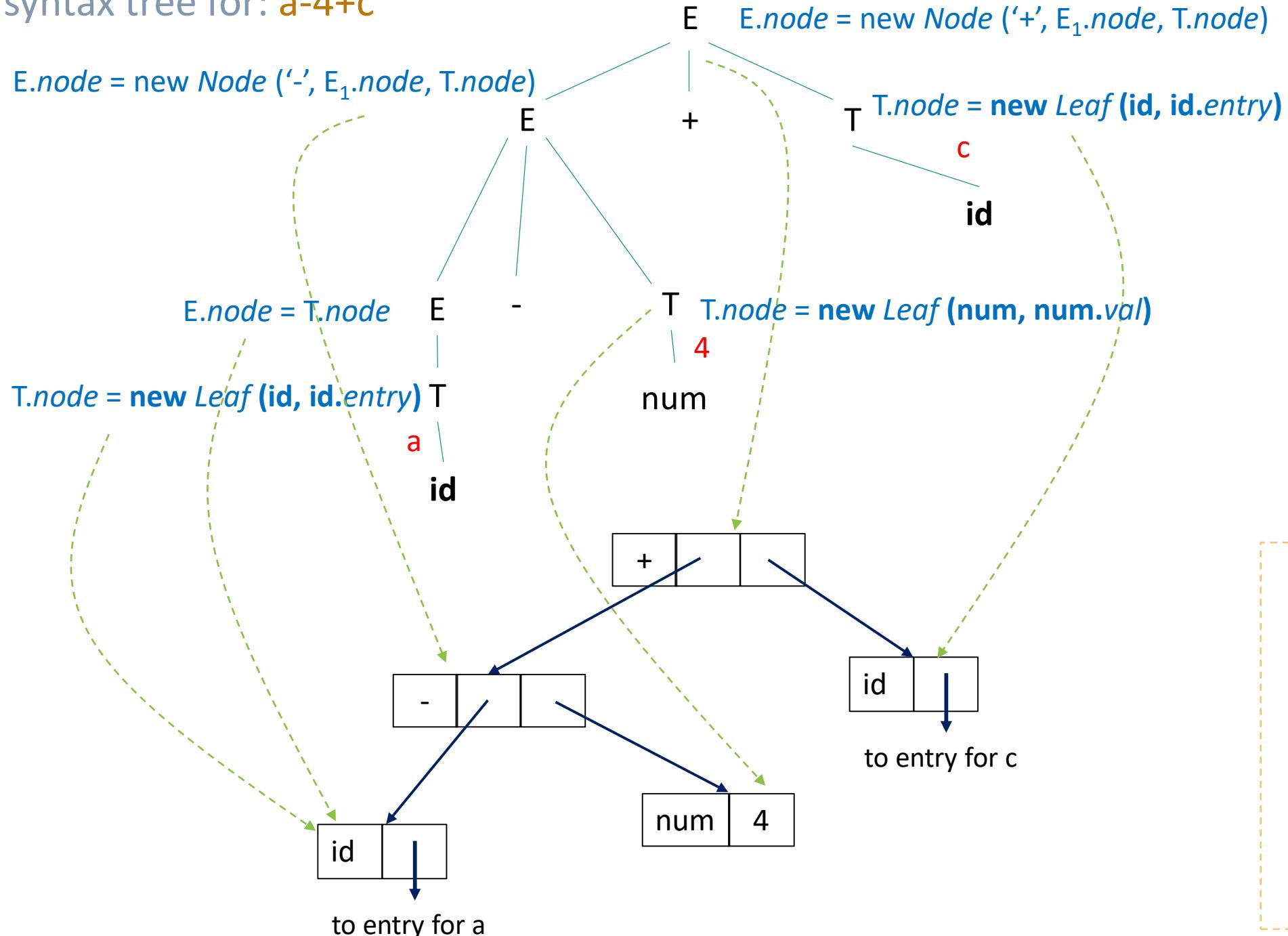
Syntax Tree



$t_1 = \text{minus } b$
 $t_2 = t_1 + c$
 $a = t_2$

Three Address Code

Construct syntax tree for: a-4+c



Production

$E \rightarrow E_1 + T$

$E \rightarrow E_1 - T$

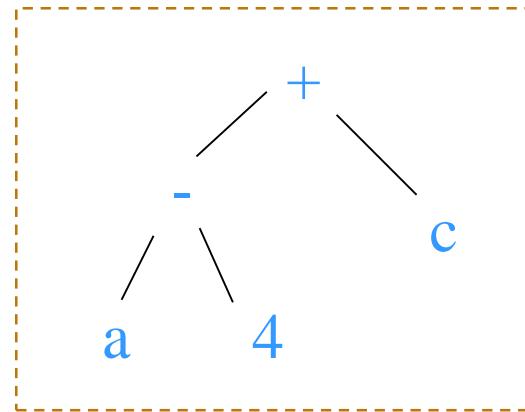
$E \rightarrow T$

$T \rightarrow (E)$

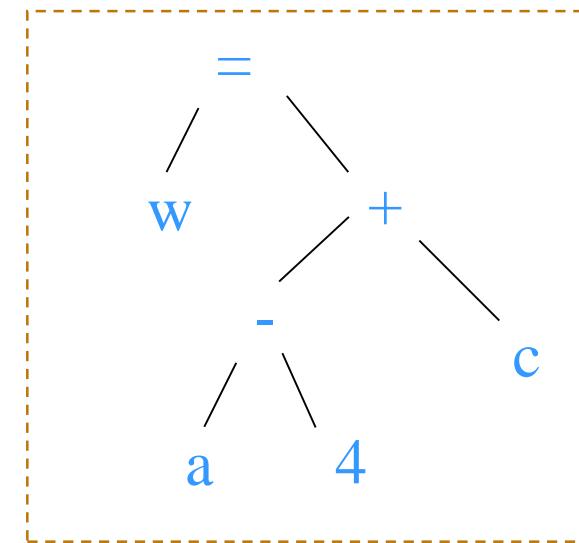
$T \rightarrow id$

$T \rightarrow num$

AST for $a-4+c$



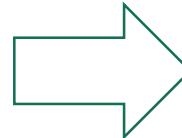
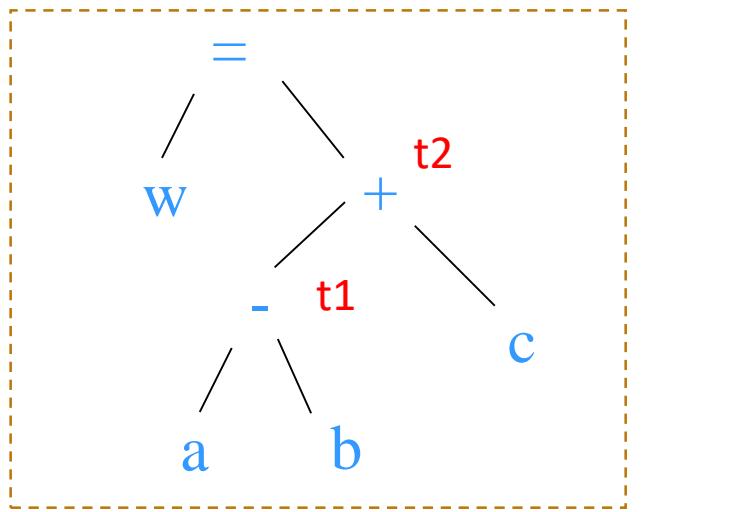
AST for $w=a-4+c$



Prod.	Semantic Rules
$E \rightarrow E_1 + T$	$E.\text{node} = \text{new Node} ('+', E_1.\text{node}, T.\text{node})$
$E \rightarrow E_1 - T$	$E.\text{node} = \text{new Node} ('-', E_1.\text{node}, T.\text{node})$
$E \rightarrow T$	$E.\text{node} = T.\text{node}$
$T \rightarrow (E)$	$E.\text{node} = E.\text{node}$
$T \rightarrow \text{id}$	$T.\text{node} = \text{new Leaf} (\text{id}, \text{id.entry})$
$T \rightarrow \text{num}$	$T.\text{node} = \text{new Leaf} (\text{num}, \text{num.val})$

Prod.	Semantic Rules
$S \rightarrow \text{id} = E$	$S.\text{node} = \text{new Node} (':=', \text{new Leaf} (\text{id}, \text{id.entry}), E.\text{node})$
$E \rightarrow E_1 + T$	$E.\text{node} = \text{new Node} ('+', E_1.\text{node}, T.\text{node})$
$E \rightarrow E_1 - T$	$E.\text{node} = \text{new Node} ('-', E_1.\text{node}, T.\text{node})$
$E \rightarrow T$	$E.\text{node} = T.\text{node}$
$T \rightarrow (E)$	$E.\text{node} = E.\text{node}$
$T \rightarrow \text{id}$	$T.\text{node} = \text{new Leaf} (\text{id}, \text{id.entry})$
$T \rightarrow \text{num}$	$T.\text{node} = \text{new Leaf} (\text{num}, \text{num.val})$

AST for $w := a - b + c$



Three address code for $w := a - b + c$

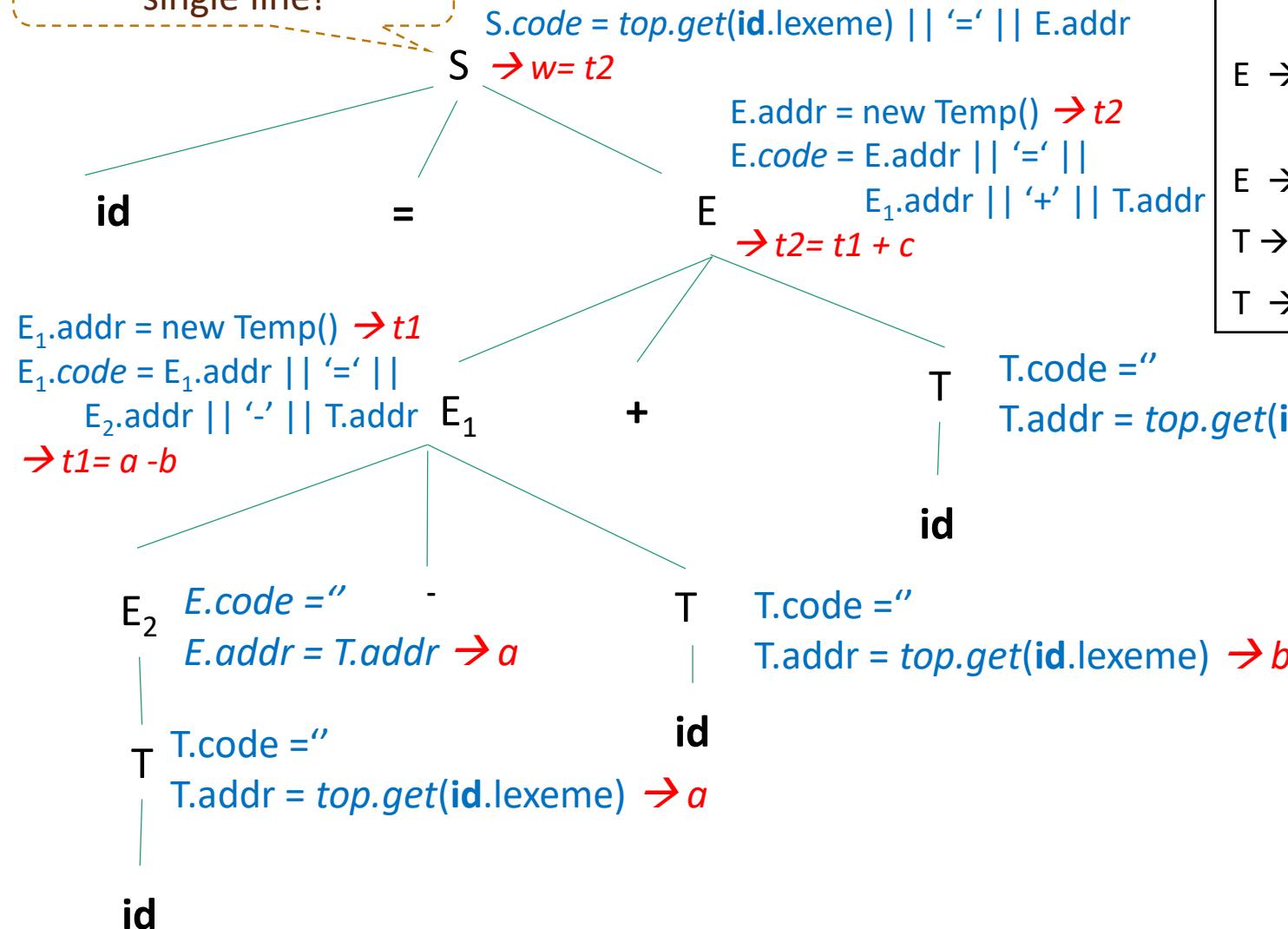
$t1 = a - b$
 $t2 = t1 + c$
 $w = t2$

Prod.	Semantic Rules for AST
$S \rightarrow id = E$	$S.node = new Node (':=', new Leaf (id, id.entry), E.node)$
$E \rightarrow E_1 + T$	$E.node = new Node ('+', E_1.node, T.node)$
$E \rightarrow E_1 - T$	$E.node = new Node ('-', E_1.node, T.node)$
$E \rightarrow T$	$E.node = T.node$
$T \rightarrow (E)$	$T.node = E.node$
$T \rightarrow id$	$T.node = new Leaf (id, id.entry)$

Prod.	Semantic Rules Three Address Code
$S \rightarrow id = E$	
$E \rightarrow E_1 + T$	
$E \rightarrow E_1 - T$	
$E \rightarrow T$	
$T \rightarrow (E)$	
$T \rightarrow id$	

Three address code for $w := a - b + c$

But S.code produces a single line!

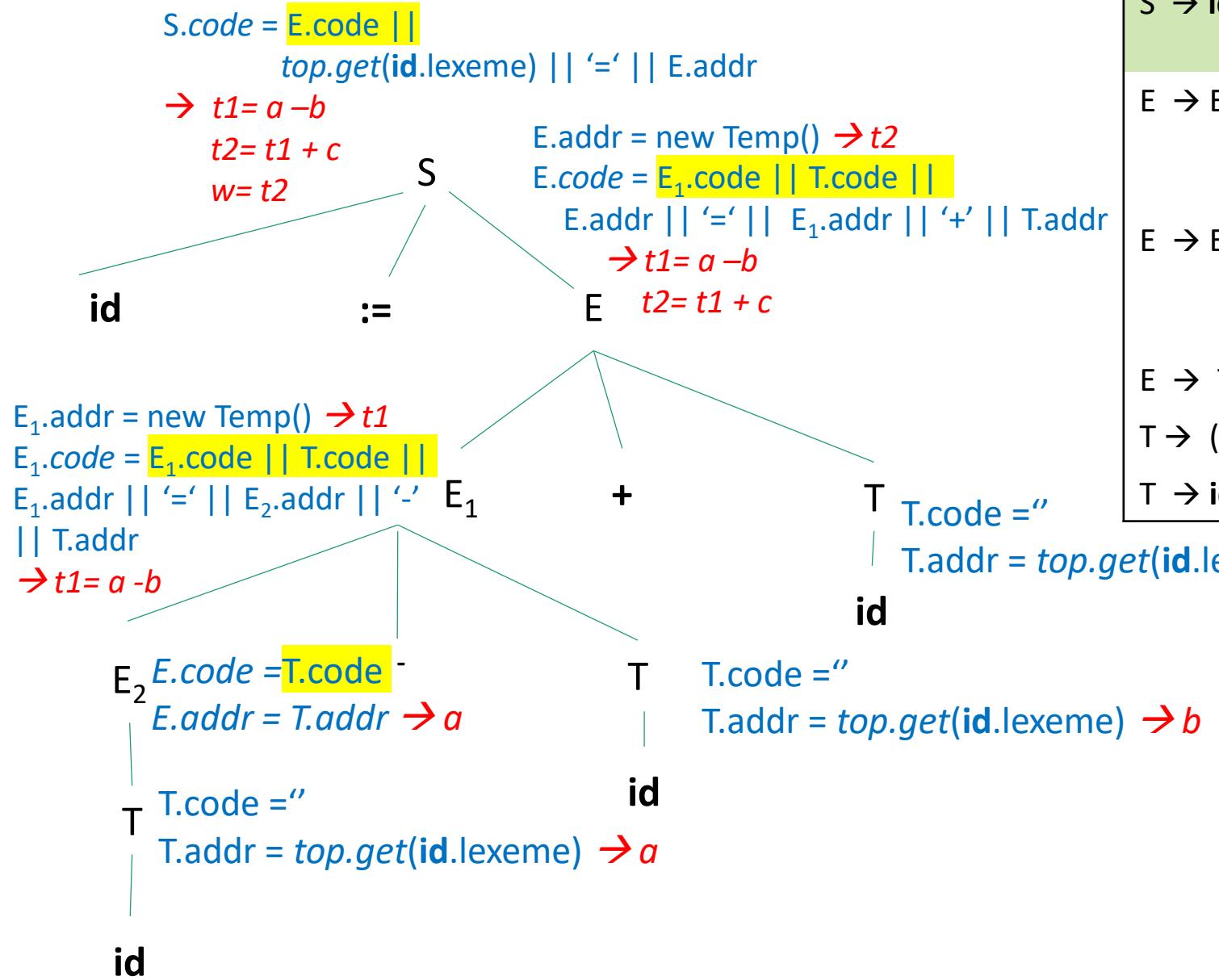


Prod.	Semantic Rules Three Address Code
$S \rightarrow \text{id} = E$	$S.\text{code} = \text{top.get(id.lexeme)} \mid\mid '=' \mid\mid E.\text{addr}$
$E \rightarrow E_1 + T$	$E.\text{addr} = \text{new Temp()}$, $E.\text{code} = E.\text{addr} \mid\mid '=' \mid\mid E_1.\text{addr} \mid\mid '+' \mid\mid T.\text{addr}$
$E \rightarrow E_1 - T$	$E.\text{addr} = \text{new Temp()}$, $E.\text{code} = E.\text{addr} \mid\mid '=' \mid\mid E_1.\text{addr} \mid\mid '-' \mid\mid T.\text{addr}$
$E \rightarrow T$	$E.\text{code} = ''$, $E.\text{addr} = T.\text{addr}$
$T \rightarrow (E)$	$T.\text{code} = ''$, $T.\text{addr} = E.\text{addr}$
$T \rightarrow \text{id}$	$T.\text{code} = ''$, $T.\text{addr} = \text{top.get(id.lexeme)}$

w := a - b + c →

t1 = a - b	t2 = t1 + c
w = t2	

Three address code for $w := a - b + c$



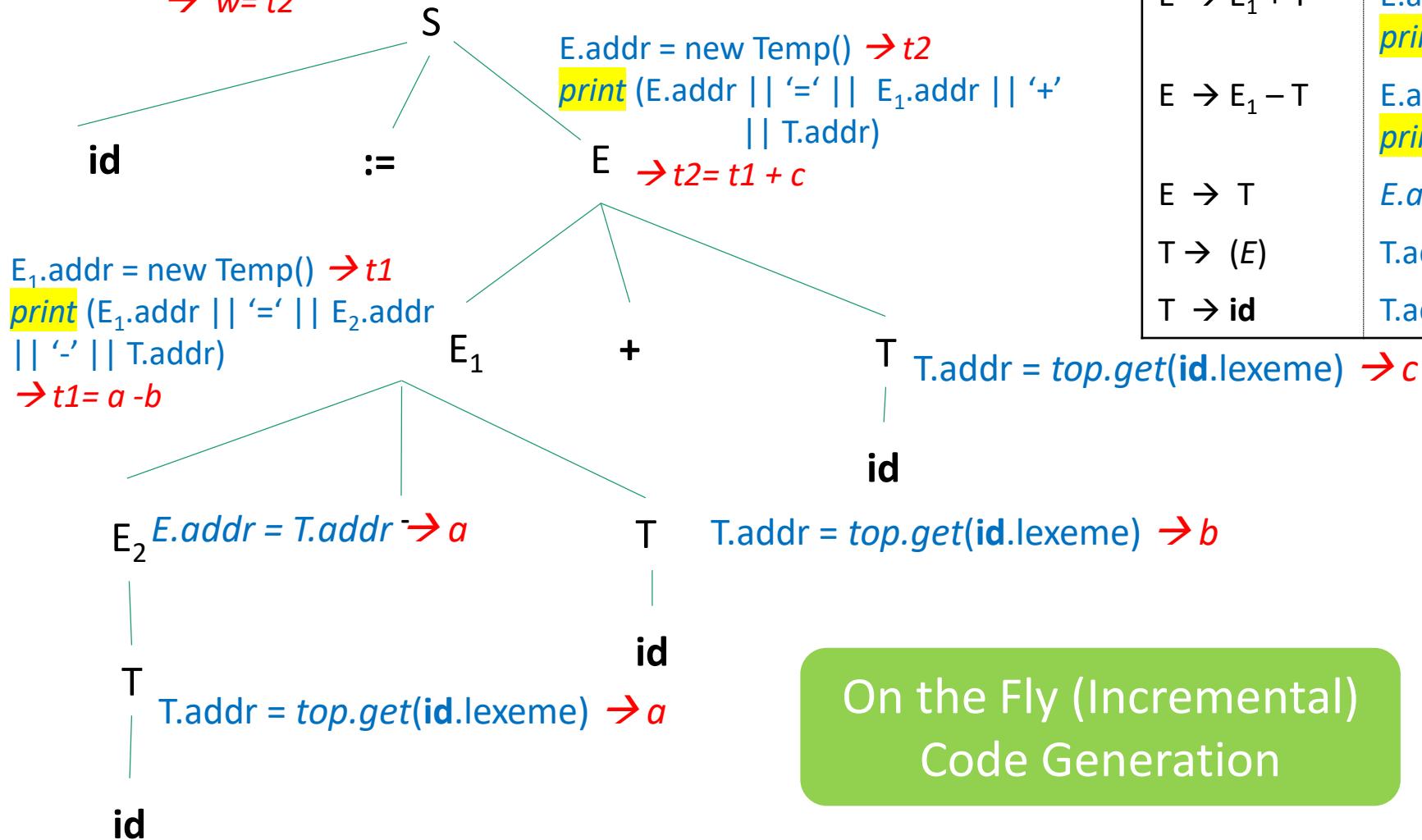
Prod.	Semantic Rules Three Address Code
$S \rightarrow id = E$	$S.code = E.code \mid\mid top.get(id.lexeme) \mid\mid '=' \mid\mid E.addr$
$E \rightarrow E_1 + T$	$E.addr = new Temp()$ $E.code = E_1.code \mid\mid T.code \mid\mid$ $E.addr \mid\mid '=' \mid\mid E_1.addr \mid\mid '+' \mid\mid T.addr$
$E \rightarrow E_1 - T$	$E.addr = new Temp()$ $E.code = E_1.code \mid\mid T.code \mid\mid$ $E.addr \mid\mid '=' \mid\mid E_1.addr \mid\mid '-' \mid\mid T.addr$
$E \rightarrow T$	$E.code = T.code, E.addr = T.addr$
$T \rightarrow (E)$	$T.code = E.code, T.addr = E.addr$
$T \rightarrow id$	$T.code = "", T.addr = top.get(id.lexeme)$

$w := a - b + c \rightarrow$

$t1 = a - b$
 $t2 = t1 + c$
 $w = t2$

Three address code for $w := a - b + c$

`print (top.get(id.lexeme) || '=' || E.addr)`
 $\rightarrow w = t2$



Prod.	Semantic Rules Three Address Code
$S \rightarrow id = E$	<code>print (top.get(id.lexeme) '=' E.addr)</code>
$E \rightarrow E_1 + T$	$E.addr = new \text{Temp}()$ <code>print (E.addr '=' E_1.addr '+' T.addr)</code>
$E \rightarrow E_1 - T$	$E.addr = new \text{Temp}()$ <code>print (E.addr '=' E_1.addr '-' T.addr)</code>
$E \rightarrow T$	$E.addr = T.addr$
$T \rightarrow (E)$	$T.addr = E.addr$
$T \rightarrow id$	$T.addr = top.get(id.lexeme)$

$w := a - b + c \rightarrow$

$t1 = a - b$
 $t2 = t1 + c$
 $w = t2$

Translation of Expressions

CFG and SDD from your text

PRODUCTION	SEMANTIC RULES
$S \rightarrow \text{id} = E ;$	$S.\text{code} = E.\text{code} $ $\text{gen}(\text{top.get(id.lexeme)} '=' E.\text{addr})$ ←
$E \rightarrow E_1 + E_2$	$E.\text{addr} = \text{new Temp}()$ $E.\text{code} = E_1.\text{code} E_2.\text{code} $ $\text{gen}(E.\text{addr} '=' E_1.\text{addr} '+' E_2.\text{addr})$
$ - E_1$	$E.\text{addr} = \text{new Temp}()$ $E.\text{code} = E_1.\text{code} $ $\text{gen}(E.\text{addr} '=' '\text{minus}' E_1.\text{addr})$
$ (E_1)$	$E.\text{addr} = E_1.\text{addr}$ $E.\text{code} = E_1.\text{code}$
$ \text{id}$	$E.\text{addr} = \text{top.get(id.lexeme)}$ $E.\text{code} = ''$

gen(...) builds an instruction and returns it

Incremental Translation

- Code attributes can be long strings, so they are usually generated incrementally
- Instead of building up $E.\text{code}$, generate only the new three address instructions
- The function $\text{gen}(\dots)$, in addition to constructing new instruction, append to the stream

PRODUCTION	SEMANTIC RULES
$S \rightarrow \text{id} = E ;$	$S.\text{code} = E.\text{code} $ $\text{gen}(top.\text{get}(\text{id}.lexeme) '=' E.\text{addr})$
$E \rightarrow E_1 + E_2$	$E.\text{addr} = \text{new Temp}()$ $E.\text{code} = E_1.\text{code} E_2.\text{code} $ $\text{gen}(E.\text{addr}'=' E_1.\text{addr}'+' E_2.\text{addr})$
$ - E_1$	$E.\text{addr} = \text{new Temp}()$ $E.\text{code} = E_1.\text{code} $ $\text{gen}(E.\text{addr}'=' '\text{minus}' E_1.\text{addr})$
$ (E_1)$	$E.\text{addr} = E_1.\text{addr}$ $E.\text{code} = E_1.\text{code}$
$ \text{id}$	$E.\text{addr} = top.\text{get}(\text{id}.lexeme)$ $E.\text{code} = ''$



$S \rightarrow \text{id} = E ;$	$\{ \text{gen}(top.\text{get}(\text{id}.lexeme) '=' E.\text{addr}); \}$
$E \rightarrow E_1 + E_2$	$\{ E.\text{addr} = \text{new Temp}();$ $\text{gen}(E.\text{addr}'=' E_1.\text{addr}'+' E_2.\text{addr}); \}$
$ - E_1$	$\{ E.\text{addr} = \text{new Temp}();$ $\text{gen}(E.\text{addr}'=' '\text{minus}' E_1.\text{addr}); \}$
$ (E_1)$	$\{ E.\text{addr} = E_1.\text{addr}; \}$
$ \text{id}$	$\{ E.\text{addr} = top.\text{get}(\text{id}.lexeme); \}$

Generating three-address code for expressions incrementally

Addressing Array Element

- In C and Java, array elements are numbered $0, 1, \dots, n-1$, for an array of n elements
- If the width of each array element is w , then the i -th element of array A begins in location

$$\text{base} + i \times w$$

Here base is the relative address of $A[0]$

- The above formula generalized to k -dimensions as

$$\text{base} + i_1 \times w_1 + i_2 \times w_2 + \dots + i_k \times w_k$$

- For the array, `int A[5][7][8]`, location of `A[2][3][4]` will be

$$\text{base} + 2 \times 224 + 3 \times 32 + 4 \times 4$$

Here size of integer is assumed as 4 byte

Translation of Array References

- The chief problem in generating code for array references is to relate the address calculation formulas to a grammar for array references
- For the array a declared as $\text{int}[2][3]$, three-address translation of the expression –

$c + a[i][j]$

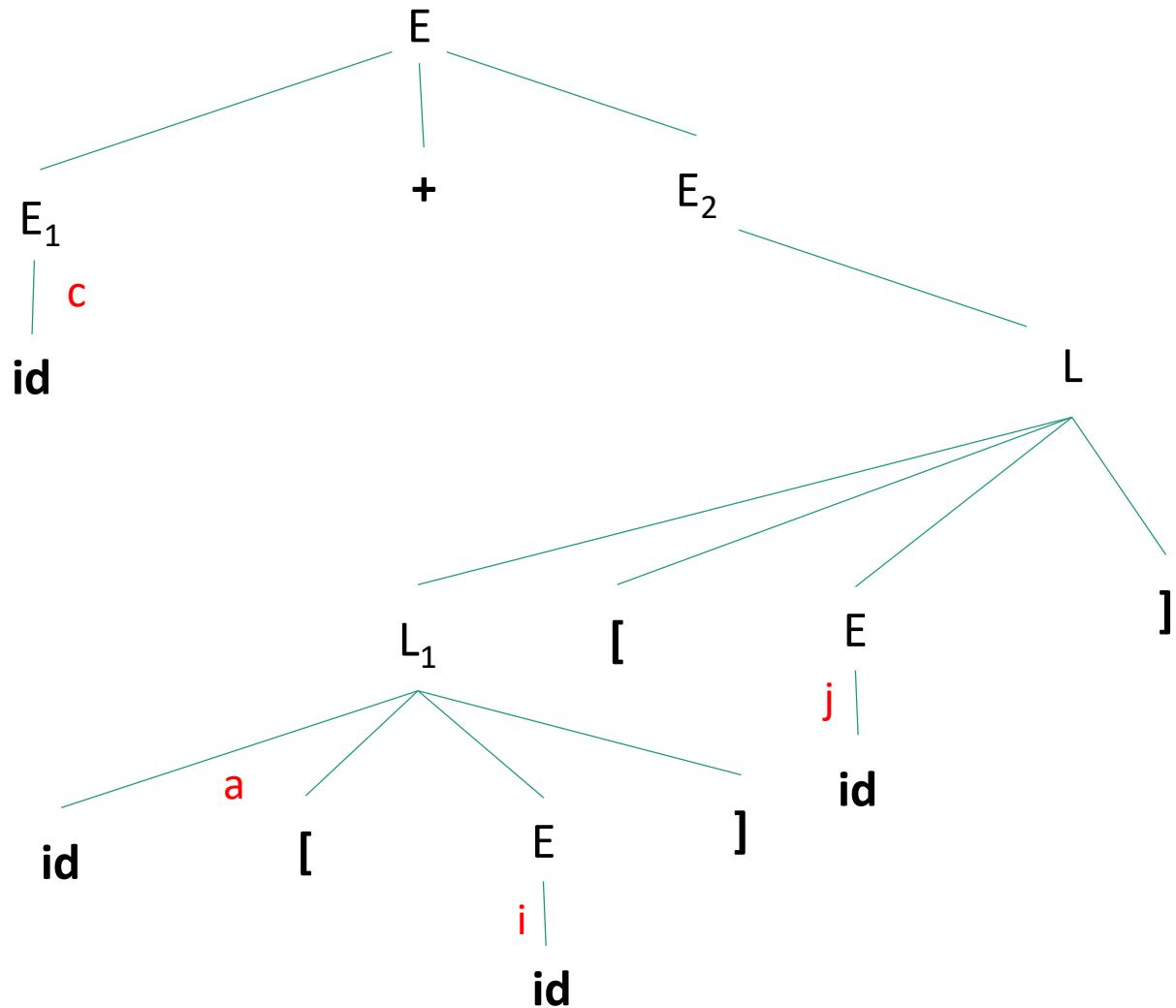


```
t1 = i * 12  
t2 = j * 4  
t3 = t1 + t2  
t4 = a [ t3 ]  
t5 = c + t4
```

- We will use the following grammar production rule where nonterminal L generates an array name followed by a sequence of index expression.

```
 $L \rightarrow L[E] \mid \text{id}[E]$ 
```

Translation of array references for $c+a[i][j]$

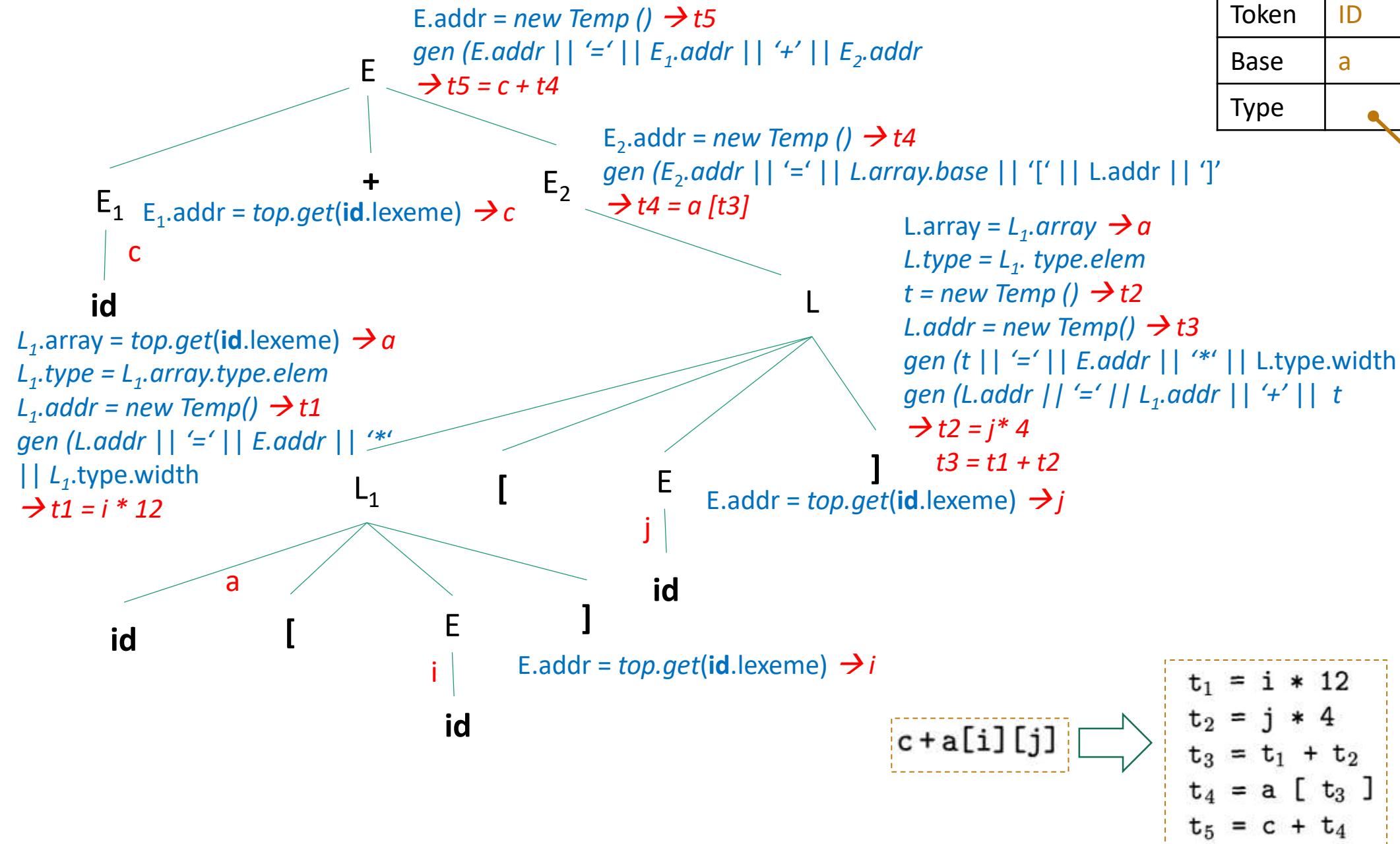


$c + a[i][j]$

```
t1 = i * 12
t2 = j * 4
t3 = t1 + t2
t4 = a [ t3 ]
t5 = c + t4
```

Prod.
$S \rightarrow id = E$
$S \rightarrow L = E$
$E \rightarrow E_1 + E_2$
$E \rightarrow id$
$E \rightarrow L$
$L \rightarrow id [E]$
$L \rightarrow L_1 [E]$

Translation of array references for $c+a[i][j]$



Symbol Info	
Token	ID
Base	a
Type	

Type	
Token	Array
Width	24
Size	2
Elem	

Type	
Token	Array
Width	12
Size	3
El	•

Type	
Token	Int
Width	4

Translation of Array References (2)

Attributes of L

$L.\text{addr}$ - a temporary that holds the sum of the terms $i_k \times w_k$

$L.\text{array}$ - a pointer to the symbol-table entry for the array name

$L.\text{type}$ - type of the subarray generated by L

$S \rightarrow \text{id} = E ;$	{ $\text{gen}(top.get(id.lexeme) '=' E.addr);$ }
$L = E ;$	{ $\text{gen}(L.addr.base '[' L.addr ']' '=' E.addr);$ }
$E \rightarrow E_1 + E_2$	{ $E.\text{addr} = \text{new Temp}();$ $\text{gen}(E.\text{addr} '=' E_1.\text{addr} '+' E_2.\text{addr});$ }
id	{ $E.\text{addr} = top.get(id.lexeme);$ }
L	{ $E.\text{addr} = \text{new Temp}();$ $\text{gen}(E.\text{addr} '=' L.array.base '[' L.addr ']');$ }
$L \rightarrow \text{id} [E]$	{ $L.\text{array} = top.get(id.lexeme);$ $L.\text{type} = L.array.type.elem;$ $L.\text{addr} = \text{new Temp}();$ $\text{gen}(L.\text{addr} '=' E.\text{addr} '*' L.type.width);$ }
$L_1 [E]$	{ $L.\text{array} = L_1.\text{array};$ $L.\text{type} = L_1.\text{type}.elem;$ $t = \text{new Temp}();$ $L.\text{addr} = \text{new Temp}();$ $\text{gen}(t '=' E.\text{addr} '*' L.type.width);$ } $\text{gen}(L.\text{addr} '=' L_1.\text{addr} '+' t);$ }

Translation of Array References (2)

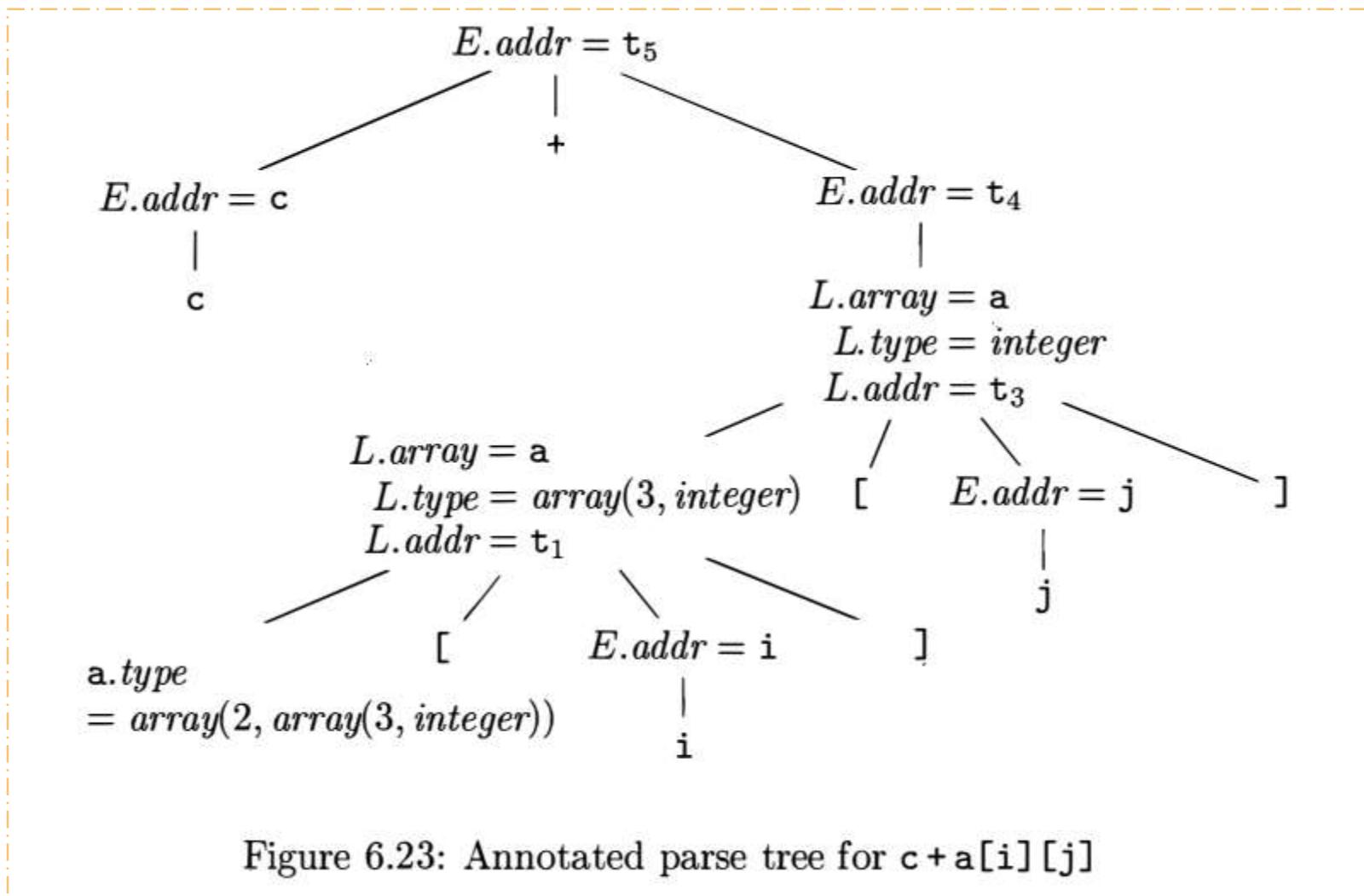


Figure 6.23: Annotated parse tree for $c + a[i][j]$

Control Flow

- We will translate control flow statements such as *if-else*, *while*
- Translation of control flow statements are tied with **Boolean expressions**
- **Boolean expressions** are composed of Boolean operators
- **Boolean operators** are applied to
 - Boolean variables
 - Relational expression with relational operator

Boolean Expression

- We consider **Boolean expressions** generated by following grammar

$$B \rightarrow B \text{ || } B \mid B \text{ && } B \mid !B \mid (B) \mid E \text{ rel } E \mid \text{true} \mid \text{false}$$

- **rel** is relational operator which is any one of `<`, `>`, `<=`, `>=`, `==`, `!=`
- We assume `&&`, `||` are **left associative** and precedence order is `!`, `&&` then `||`

Boolean Expression

- Boolean expressions are used to
 - Alter flow of control
 - If (B) then S: B must be true to reach S
 - To compute logical values
 - True or False as value

```
if ( x < 100 || x > 200 && x != y )  
    x = 0;
```

```
p = x<a && (x>b || y<a);
```

Short Circuit Code

- Also called **jumping code**
- `&&`, `||` and `!` are translated into **jumps**
- The operators don't appear in the code
- The value of a boolean expression is represented by a position in the code

Short Circuit Code

- Example:

A statement with Boolean expressions

```
if ( x < 100 || x > 200 && x != y )  
    x = 0;
```

Jumping Code

```
if x < 100 goto L2  
ifFalse x > 200 goto L1  
ifFalse x != y goto L1  
L2: x = 0  
L1:
```

Flow of Control Statements

- We will consider flow of control statements generated by following grammar

$$S \rightarrow if (B) S_1$$
$$S \rightarrow if (B) S_1 else S_2$$
$$S \rightarrow while (B) S_1$$

- B represent Boolean expression
- S represent Statements

Flow of Control Statements

- The Grammar

Productions	Semantic Rules
$P \rightarrow S$	
$S \rightarrow S_1 S_2$	
$S \rightarrow \text{assign}$	
$S \rightarrow \text{if } (B) S_1$	
$S \rightarrow \text{if } (B) S_1 \text{ else } S_2$	
$S \rightarrow \text{while } (B) S_1$	

assign is a Placeholder for
an assignment statement



We need to find out the Semantic Rules

Flow of Control Statements

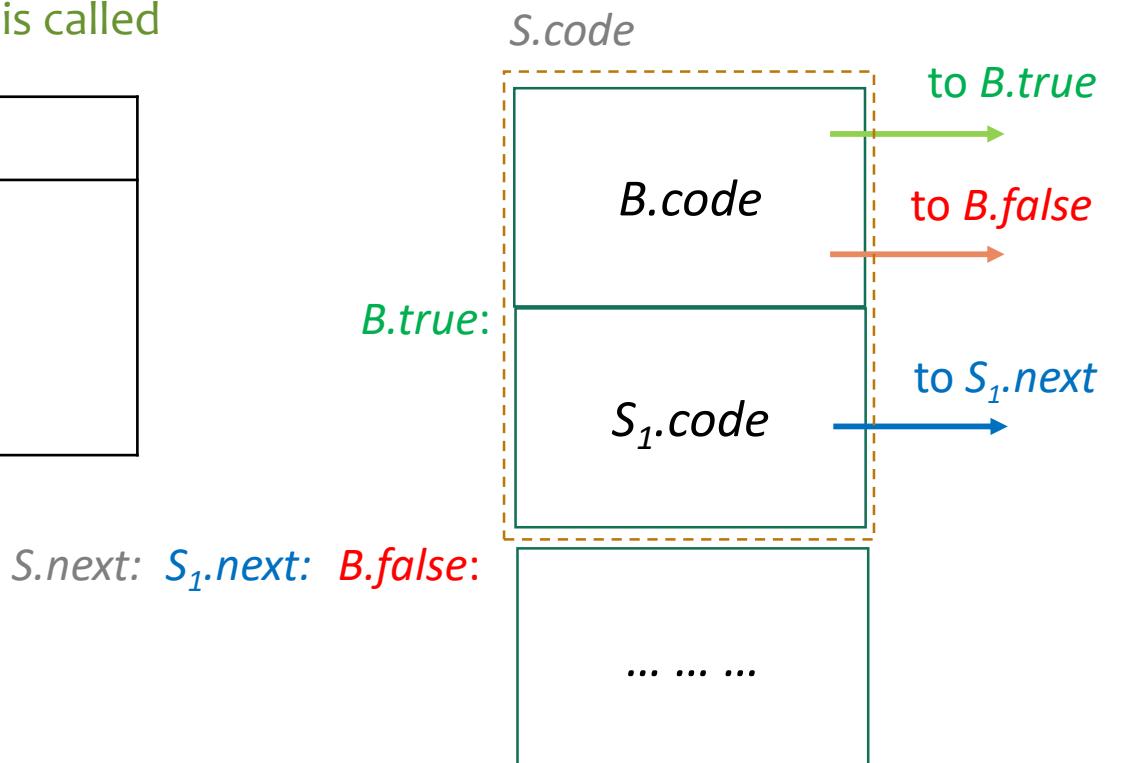
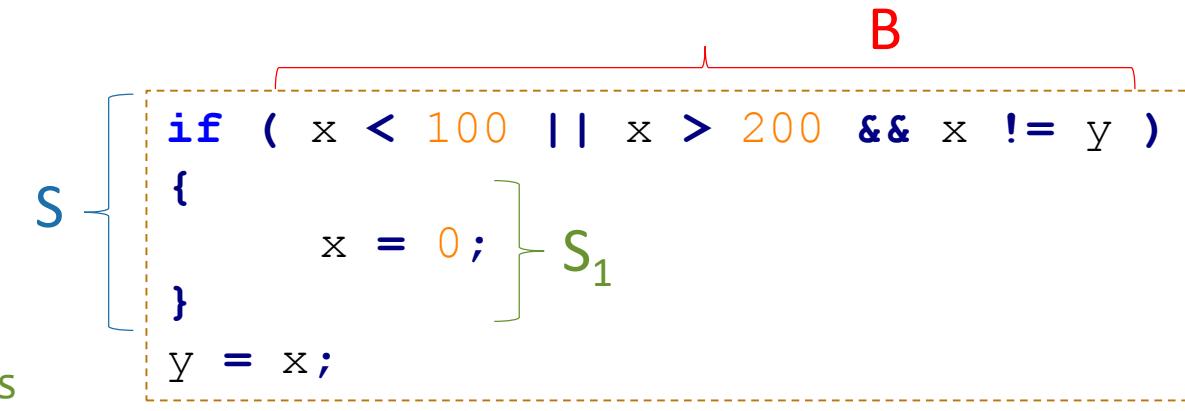
- Semantic Rules for the production

$$S \rightarrow if (B) S_1$$

newlabel() creates
new label each time it is called

Productions	Semantic Rules
$S \rightarrow if (B) S_1$	-

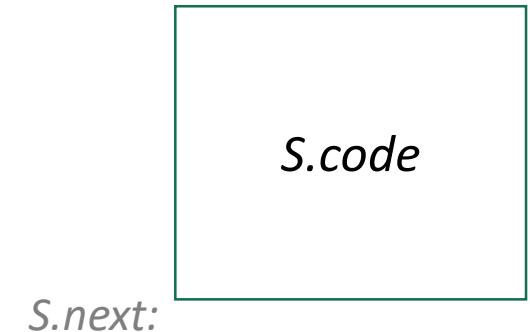
label(L) attaches label L to the
next instruction to be generated



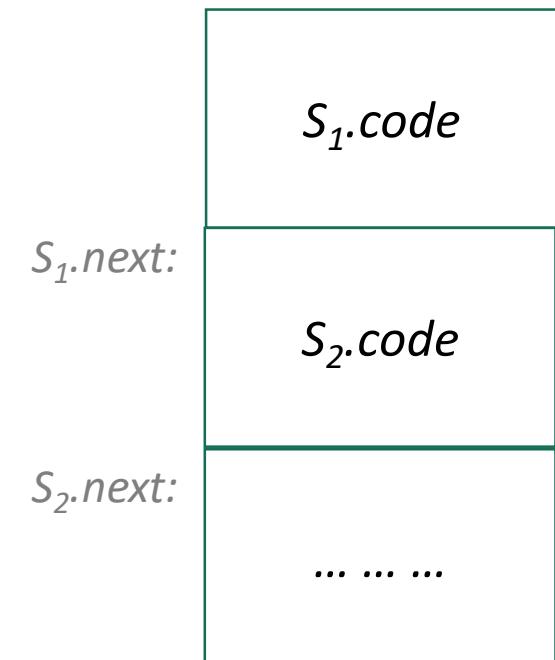
Flow of Control Statements

- Semantic Rules for the first two productions

Productions	Semantic Rules
$P \rightarrow S$	$S.next = newlabel()$ $P.code = S.code \mid\mid label(S.next)$



$S \rightarrow S_1 S_2$	$S_1.next = newlabel()$ $S_2.next = S.next$ $S.code = S_1.code \mid\mid label(S_1.next) \mid\mid S_2.code$
-------------------------	--



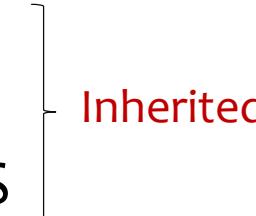
Flow of Control Statements

- Attributes of SDD:

- Codes are managed using

- B.code : contains codes of B
 - S.code : contains codes of S
- 
- Synthesized

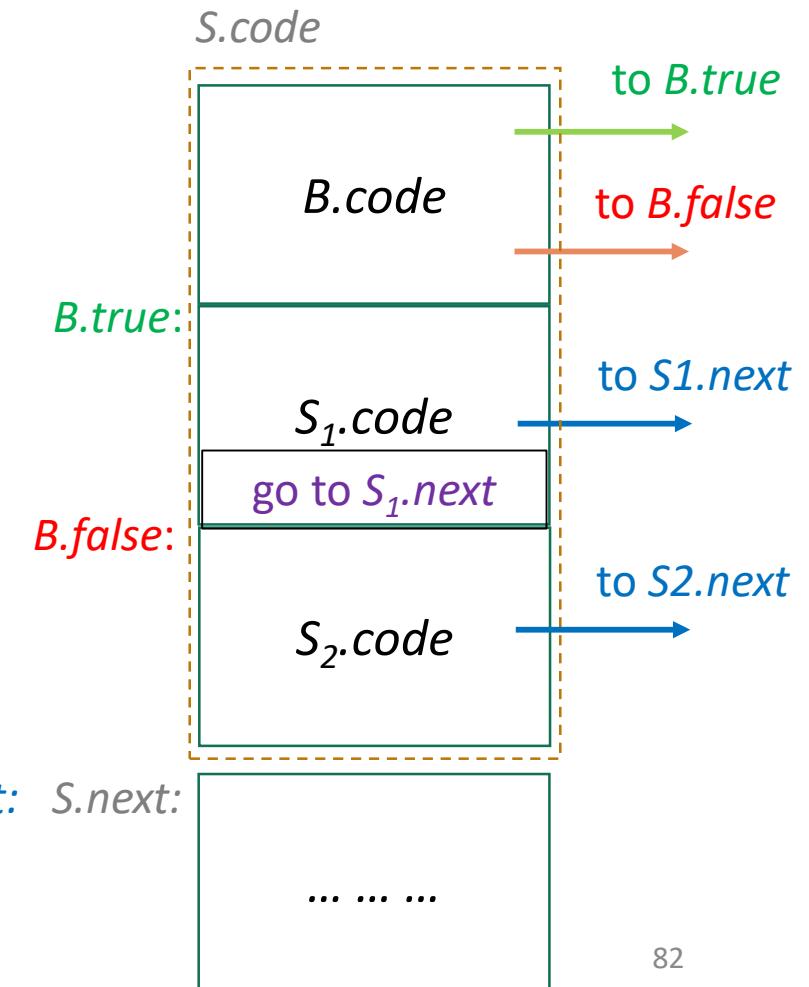
- Jumping Labels are managed using

- B.true : label to which control flows if B is true
 - B.false : label to which control flows if B is false
 - S.next : label of an instruction immediately after S
- 
- Inherited

Flow of Control Statements

- Semantic Rules for the production $S \rightarrow \text{if } (B) S_1 \text{ else } S_2$

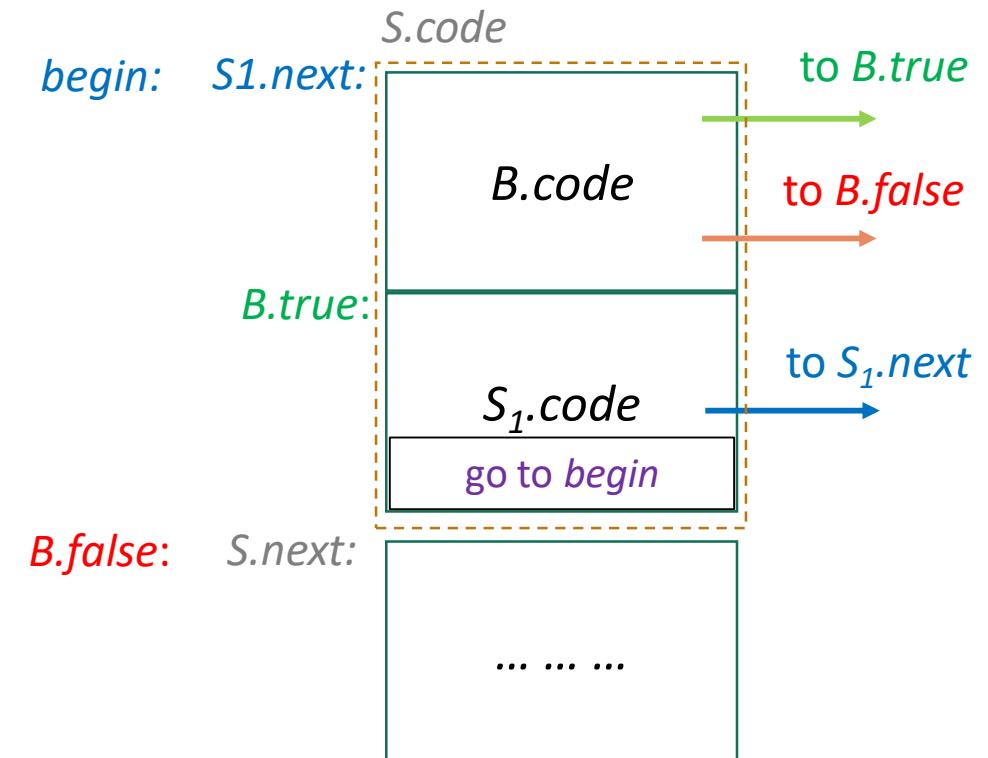
Productions	Semantic Rules
$S \rightarrow \text{if } (B) S_1 \text{ else } S_2$	-



Flow of Control Statements

- Semantic Rules for the production $S \rightarrow \text{while } (B) S_1$

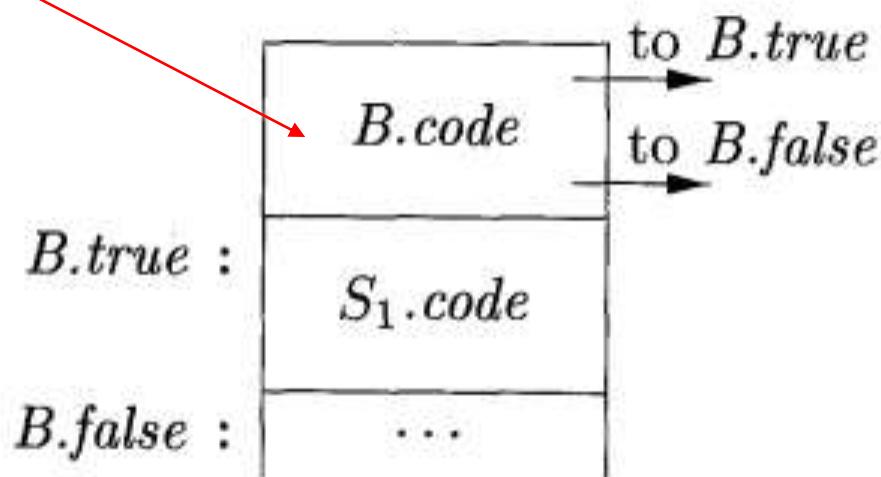
Productions	Semantic Rules
$S \rightarrow \text{while } (B) S_1$	



Translation of Boolean Expression

- Now we will consider productions containing B in their head
 - We want to know how we produce $B.\text{code}$

How to produce $B.\text{code}$?



Translation of Boolean Expression

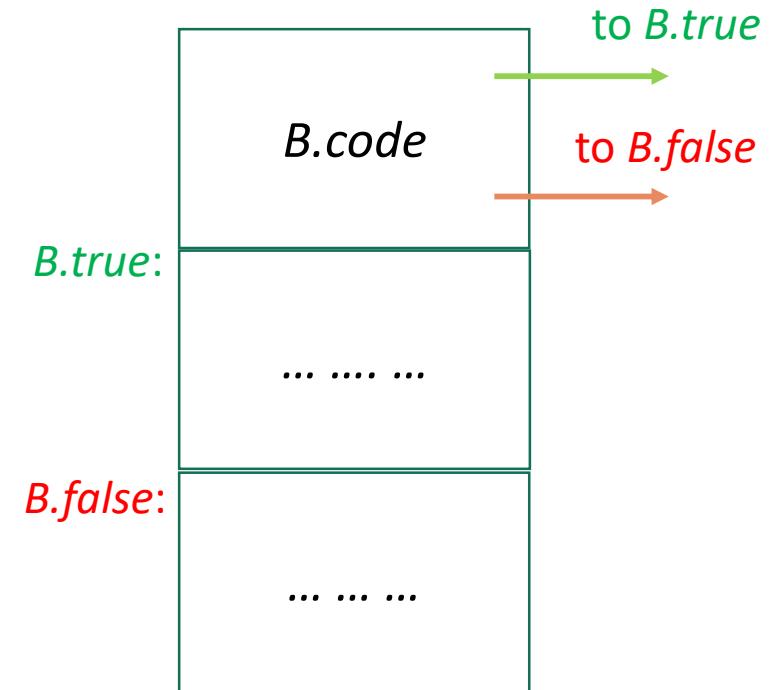
- The Grammar

Productions	Semantic Rules
$B \rightarrow B_1 \mid\mid B_2$	
$B \rightarrow B_1 \&\& B_2$	
$B \rightarrow !B_1$	
$B \rightarrow E_1 \text{ rel } E_2$	
$B \rightarrow \text{true}$	
$B \rightarrow \text{false}$	

Translation of Boolean Expression

- Semantic Rules for the production $B \rightarrow B_1 \parallel B_2$

PRODUCTION	SEMANTIC RULE
$B \rightarrow B_1 \parallel B_2$	

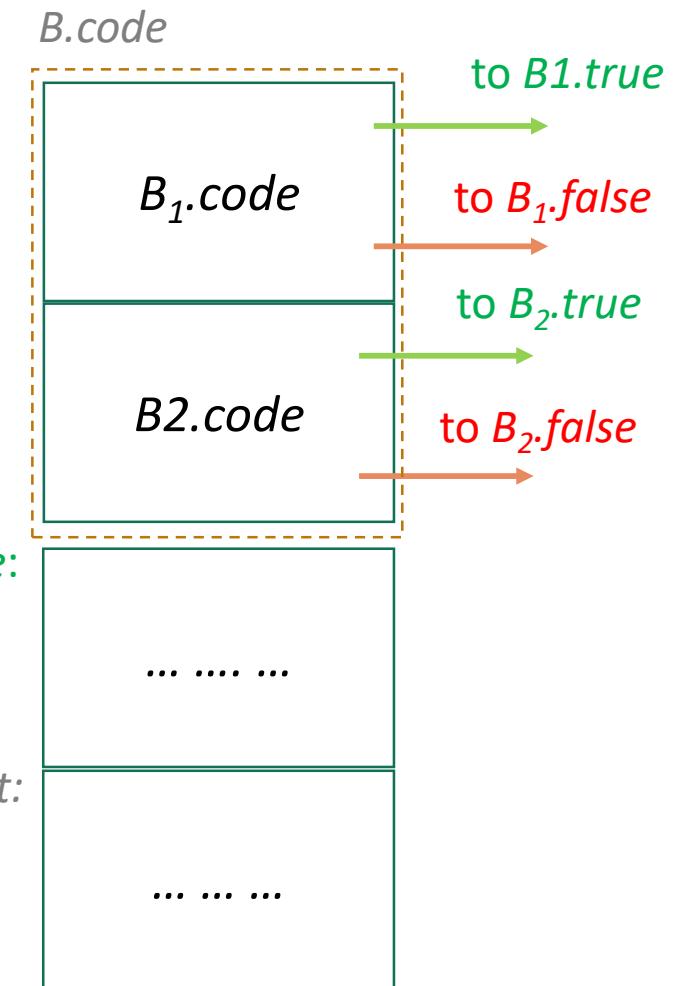


Translation of Boolean Expression

- Semantic Rules for the production $B \rightarrow B_1 \parallel B_2$

PRODUCTION	SEMANTIC RULE
$B \rightarrow B_1 \parallel B_2$	

$B_1.false:$
 $B_2.true: B1.true: B.true:$
 $B_2.false: B.false: S.next:$



Translation of Boolean Expression

- Consider $B \rightarrow B_1 \mid\mid B_2$
- If B_1 is true then B is also true. So label of $B_1.\text{true}$ is same as $B.\text{true}$
- If B_1 is false, then we need to evaluate B_2 . So label of $B_1.\text{false}$ is the label of first instruction of B_2
- $B_2.\text{true}$ is same as $B.\text{true}$
- $B_2.\text{false}$ is same as $B.\text{false}$

Translation of Boolean Expression

- Semantic Rules for the production $B \rightarrow B_1 \And B_2$

PRODUCTION	SEMANTIC RULE
$B \rightarrow B_1 \And B_2$	$B_1.true =$ $B_1.false =$ $B_2.true =$ $B_2.false =$ $B.code =$

Translation of Boolean Expression

- Semantic Rules for the production $B \rightarrow !B_1$

PRODUCTION	SEMANTIC RULE
$B \rightarrow !B_1$	

Translation of Boolean Expression

- Semantic Rules for the production $B \rightarrow E_1 \text{ rel } E_2$

PRODUCTION	SEMANTIC RULE
$B \rightarrow E_1 \text{ rel } E_2$	

Translation of Boolean Expression

- Semantic Rules for the productions $B \rightarrow \text{true}$ and $B \rightarrow \text{false}$

PRODUCTION	SEMANTIC RULE
$B \rightarrow \text{true}$	
$B \rightarrow \text{false}$	

SDD for Generating Three Address Code for Flow-of-Control Statements

PRODUCTION	SEMANTIC RULES
$P \rightarrow S$	$S.next = newlabel()$ $P.code = S.code \parallel label(S.next)$
$S \rightarrow \text{assign}$	$S.code = \text{assign}.code$
$S \rightarrow \text{if} (B) S_1$	$B.true = newlabel()$ $B.false = S_1.next = S.next$ $S.code = B.code \parallel label(B.true) \parallel S_1.code$
$S \rightarrow \text{if} (B) S_1 \text{ else } S_2$	$B.true = newlabel()$ $B.false = newlabel()$ $S_1.next = S_2.next = S.next$ $S.code = B.code$ $\quad \parallel label(B.true) \parallel S_1.code$ $\quad \parallel \text{gen('goto' } S.next)$ $\quad \parallel label(B.false) \parallel S_2.code$
$S \rightarrow \text{while} (B) S_1$	$begin = newlabel()$ $B.true = newlabel()$ $B.false = S.next$ $S_1.next = begin$ $S.code = label(begin) \parallel B.code$ $\quad \parallel label(B.true) \parallel S_1.code$ $\quad \parallel \text{gen('goto' } begin)$
$S \rightarrow S_1 S_2$	$S_1.next = newlabel()$ $S_2.next = S.next$ $S.code = S_1.code \parallel label(S_1.next) \parallel S_2.code$

SDD for Generating Three Address Code for Booleans

PRODUCTION	SEMANTIC RULES
$B \rightarrow B_1 \text{ } B_2$	$B_1.\text{true} = B.\text{true}$ $B_1.\text{false} = \text{newlabel}()$ $B_2.\text{true} = B.\text{true}$ $B_2.\text{false} = B.\text{false}$ $B.\text{code} = B_1.\text{code} \parallel \text{label}(B_1.\text{false}) \parallel B_2.\text{code}$
$B \rightarrow B_1 \&& B_2$	$B_1.\text{true} = \text{newlabel}()$ $B_1.\text{false} = B.\text{false}$ $B_2.\text{true} = B.\text{true}$ $B_2.\text{false} = B.\text{false}$ $B.\text{code} = B_1.\text{code} \parallel \text{label}(B_1.\text{true}) \parallel B_2.\text{code}$
$B \rightarrow ! B_1$	$B_1.\text{true} = B.\text{false}$ $B_1.\text{false} = B.\text{true}$ $B.\text{code} = B_1.\text{code}$
$B \rightarrow E_1 \text{ rel } E_2$	$B.\text{code} = E_1.\text{code} \parallel E_2.\text{code}$ $\parallel \text{gen('if' } E_1.\text{addr rel.op } E_2.\text{addr 'goto' } B.\text{true})$ $\parallel \text{gen('goto' } B.\text{false})$
$B \rightarrow \text{true}$	$B.\text{code} = \text{gen('goto' } B.\text{true})$
$B \rightarrow \text{false}$	$B.\text{code} = \text{gen('goto' } B.\text{false})$

Code Generation

SDD for Flow-of-Control and Booleans (*partial*)

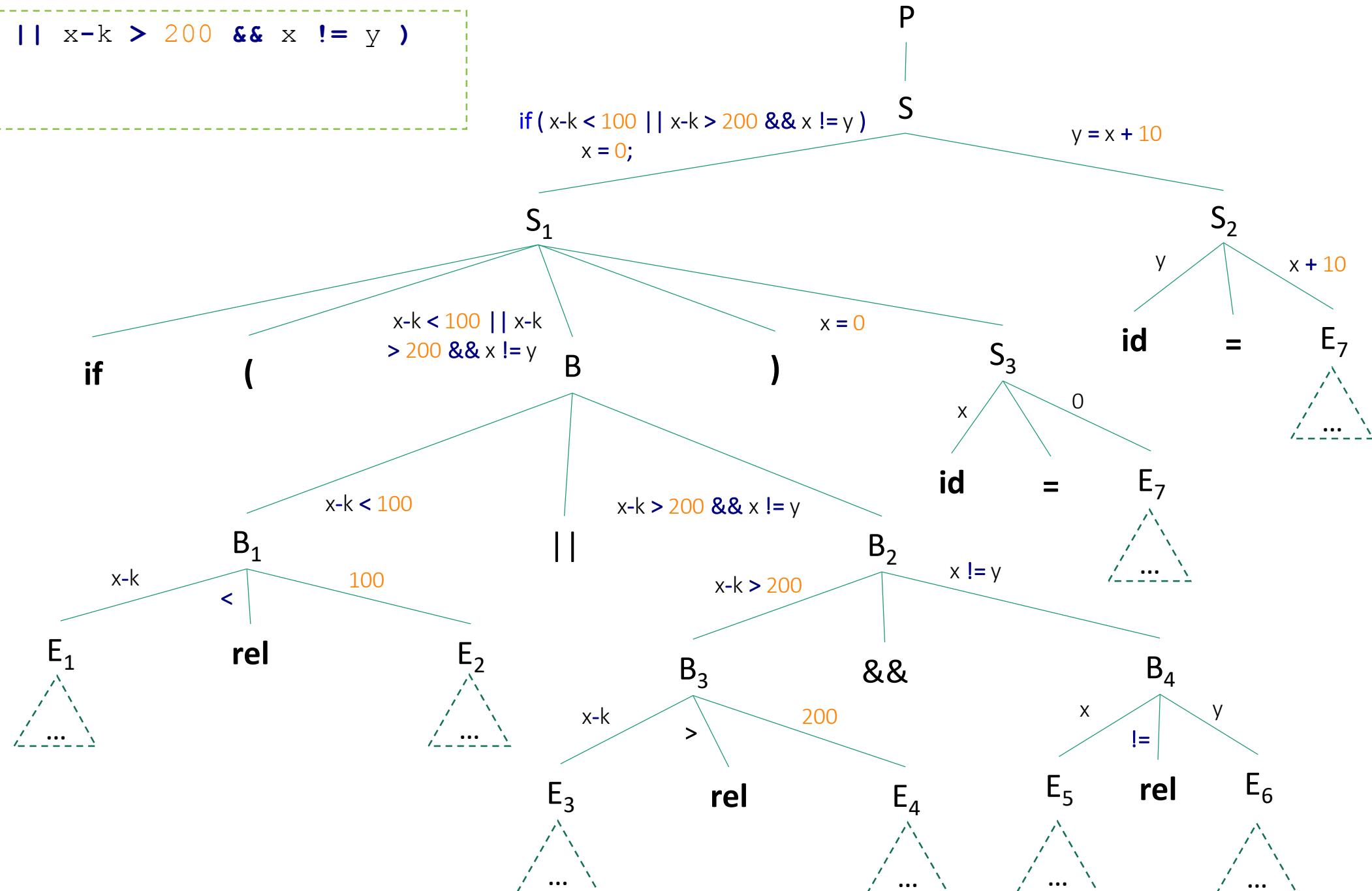
Production	Semantic Action
$P \rightarrow S$	$S.\text{next}=\text{newlabel}()$ $P.\text{code}=S.\text{code} \mid\mid \text{label}(S.\text{next})$
$S \rightarrow S_1 S_2$	$S_1.\text{next}=\text{newlabel}()$ $S_2.\text{next}=S.\text{next}$ $S.\text{code}=S_1.\text{code} \mid\mid \text{label}(S_1.\text{next}) \mid\mid S_2.\text{code}$
$S \rightarrow \text{if } (B) S_1$	$B.\text{true}=\text{newlabel}()$ $B.\text{false}=S_1.\text{next}=S.\text{next}$ $S.\text{code}=B.\text{code} \mid\mid \text{label}(B.\text{true}) \mid\mid S_1.\text{code}$
$B \rightarrow B_1 \mid\mid B_2$	$B_1.\text{true}=B.\text{true}$ $B_1.\text{false}=\text{newlabel}()$ $B_2.\text{true}=B.\text{true}$ $B_2.\text{false}=B.\text{false}$ $B.\text{code}=B_1.\text{code} \mid\mid \text{label}(B_1.\text{false}) \mid\mid B_2.\text{code}$
$B \rightarrow E_1 \text{ rel } E_2$	$B.\text{code}=E_1.\text{code} \mid\mid E_2.\text{code}$ $\mid\mid \text{gen}(\text{'if'} E_1.\text{addr} \text{ rel } E_2.\text{addr} \text{ ' goto } B.\text{true}')$ $\mid\mid \text{gen}(\text{' goto } B.\text{false}')$

SDT for Flow-of-Control and Booleans (on the fly)

Translation of statement

```
if ( x-k < 100 || x-k > 200 && x != y )
    x = 0;
y = x + 10;
```

Prod.
$P \rightarrow S$
$S \rightarrow id = E;$
$S \rightarrow S_1 S_2$
$S \rightarrow if(B) S_1$
$B \rightarrow B_1 B_2$
$B \rightarrow B_1 \&\& B_2$
$B \rightarrow E_1 rel E_2$
$E \rightarrow ...$



Translation of statement

$t1 = x-k$

$t2=100$

if $t1 < t2$ go to L2

go to L1

L3: $t3 = x-k$

$t4=200$

if $t3 < t4$ go to L4

go to L1

L4: if $x \neq y$ go to L2

go to L1

L2: $t5=0$

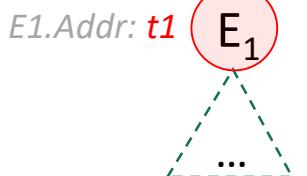
$x = t5$

L1: $t6 = x+10$

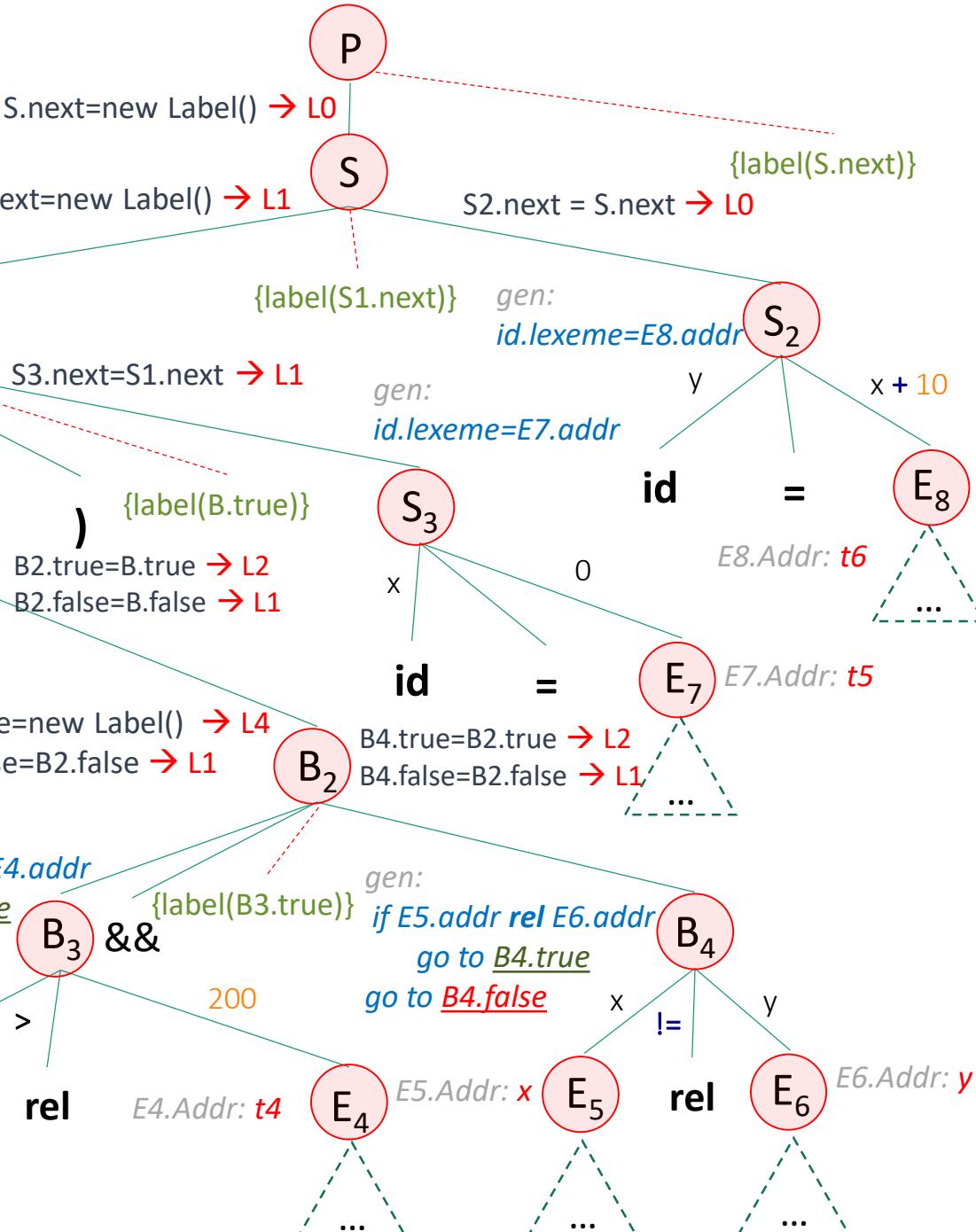
$y = t6$

L0:

TAC

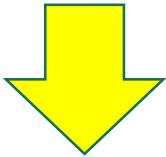


```
if ( x-k < 100 || x-k > 200 && x != y )
    x = 0;
y = x + 10;
```



Avoiding Redundant Gotos

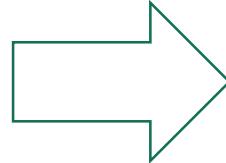
```
if( x < 100 || x > 200 && x != y ) x = 0;
```



Redundant

```
if x < 100 goto L2
goto L3
L3: if x > 200 goto L4
     goto L1
L4: if x != y goto L2
     goto L1
L2: x = 0
L1:
```

Code with redundant goto



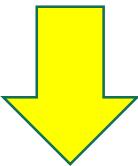
```
if x < 100 goto L2
ifFalse x > 200 goto L1
ifFalse x != y goto L1
L2: x = 0
L1:
```

Code without redundant goto

Avoiding Redundant Gotos

$S \rightarrow \text{if} (B) S_1$

$B.\text{true} = \text{newlabel}()$
 $B.\text{false} = S_1.\text{next} = S.\text{next}$
 $S.\text{code} = B.\text{code} \parallel \text{label}(B.\text{true}) \parallel S_1.\text{code}$



$B.\text{true} = \text{fall}$
 $B.\text{false} = S_1.\text{next} = S.\text{next}$
 $S.\text{code} = B.\text{code} \parallel S_1.\text{code}$

Avoiding Redundant Gotos

$B \rightarrow B_1 \parallel B_2$

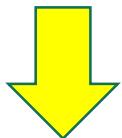
$B_1.\text{true} = B.\text{true}$

$B_1.\text{false} = \text{newlabel}()$

$B_2.\text{true} = B.\text{true}$

$B_2.\text{false} = B.\text{false}$

$B.\text{code} = B_1.\text{code} \parallel \text{label}(B_1.\text{false}) \parallel B_2.\text{code}$



$B_1.\text{true} = \mathbf{if } B.\text{true} \neq \text{fall} \mathbf{then } B.\text{true} \mathbf{else } \text{newlabel}()$

$B_1.\text{false} = \text{fall}$

$B_2.\text{true} = B.\text{true}$

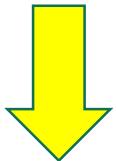
$B_2.\text{false} = B.\text{false}$

$B.\text{code} = \mathbf{if } B.\text{true} \neq \text{fall} \mathbf{then } B_1.\text{code} \parallel B_2.\text{code}$
 $\mathbf{else } B_1.\text{code} \parallel B_2.\text{code} \parallel \text{label}(B_1.\text{true})$

Avoiding Redundant Gotos

$B \rightarrow E_1 \text{ rel } E_2$

$B.code = E_1.code \parallel E_2.code$
 $\parallel \text{gen('if' } E_1.\text{addr rel.op } E_2.\text{addr 'goto' } B.\text{true})$
 $\parallel \text{gen('goto' } B.\text{false})$



$test = E_1.\text{addr rel.op } E_2.\text{addr}$

$s = \text{if } B.\text{true} \neq \text{fall and } B.\text{false} \neq \text{fall then}$
 $\quad \text{gen('if' } test \text{'goto' } B.\text{true}) \parallel \text{gen('goto' } B.\text{false})$
 $\text{else if } B.\text{true} \neq \text{fall then gen('if' } test \text{'goto' } B.\text{true})$
 $\text{else if } B.\text{false} \neq \text{fall then gen('iffalse' } test \text{'goto' } B.\text{false})$
 else ''

$B.code = E_1.code \parallel E_2.code \parallel s$

Boolean Values and Jumping Code

- So far, we have used boolean expressions to **alter the flow of control** in statements
- A boolean expression may also be **evaluated** for its value such as

x = a < b && c < d



```
if ( a < b && c < d )
    x=true;
else x=false;
```

ifFalse a < b goto L₁

ifFalse c > d goto L₁

t = true

goto L₂

L₁: t = false

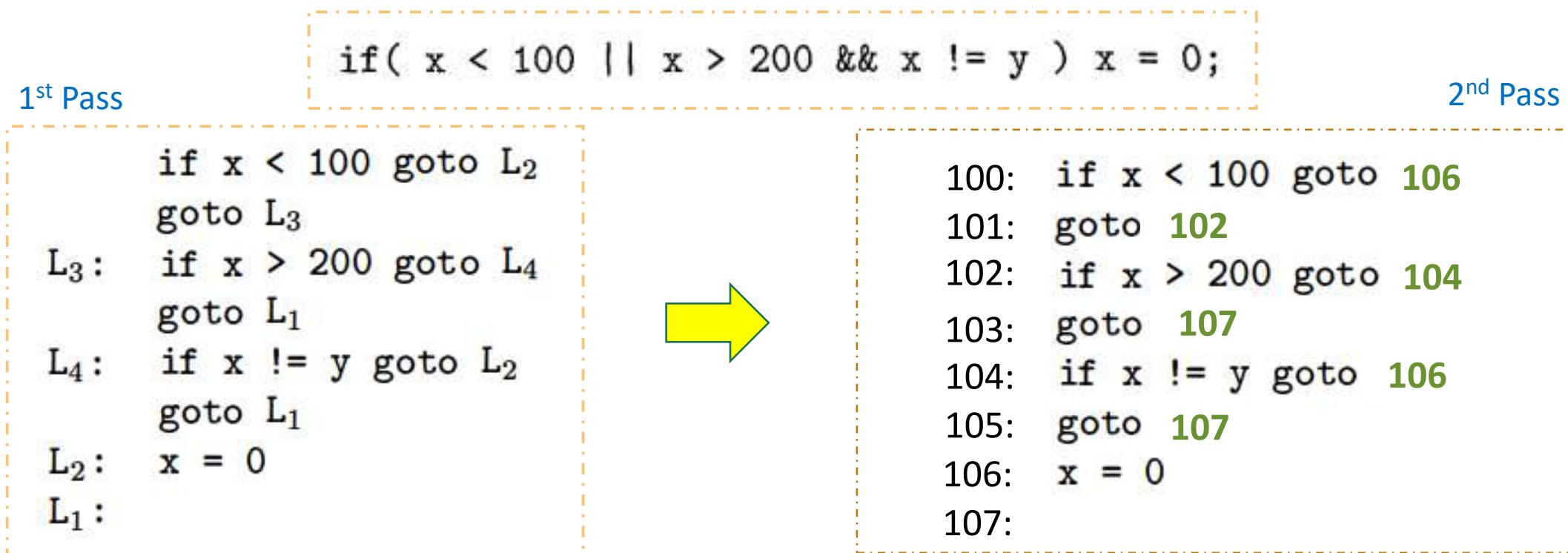
L₂: x = t

Boolean Values and Jumping Code

- A clean way of handling both roles of boolean expressions is to **first build a syntax tree for expressions**, using either of the following approaches
 - Use two passes
 - Construct a complete **syntax tree** for the input, and
 - then traverse in **depth-first order** computing the translations specified by the semantic rule
 - Use one pass for statements, but two passes for expressions
 - In the approach, we would first translate E in **while (E) S_1** before S_1 is examined.
 - The translation of E , however would be done by building its **syntax tree** and then walking the tree
- Use separate code generation functions for expressions
 - One for generating jumping code
 - The other for **computing the value**

Backpatching

- A key problem when generating code for boolean expression and flow-of-control statement is that of matching a jump instruction with the target of the jump
- The SDD we have used earlier generates symbolic labels
- A separate pass is needed to bind labels to address



Backpatching

- Backpatching is used to generate code for boolean expressions and flow-of-control statements in one pass
- In Backpatching, list of jumps are passed as synthesized attributes
- Specifically, when a jump is generated, the target of the jump label is left unspecified
- Each such jump is put on a list of jumps whose labels are to be filled in when proper label can be determined
- All of the jumps on a list have the same target label

Code Generation Using Backpatching

- Two synthesized attributes for boolean expression B
 - $B.\text{truelist}$ – a list of jumps or conditional jumps into which we must insert the label to which control goes if B is true
 - $B.\text{falselist}$ – a list of jumps or conditional jumps into which we must insert the label to which control goes if B is false
- A synthesized attribute for statement S
 - $S.\text{nextlist}$ – a list of jumps to the instruction immediately following the code for S
- Three functions
 - $\text{makelist}(i)$ – creates a new list containing only i , an index into the array of instructions.
Returns a pointer to the newly created array
 - $\text{merge}(p_1, p_2)$ – concatenates the lists pointed to by p_1 and p_2 , and returns a pointer to the concatenated list
 - $\text{backpatch}(p, i)$ – inserts i as the target label for each of the instructions on the list pointed to by p

Code Generation Using Backpatching

SDT for Flow-of-Control and Booleans (on the fly)

SDT for Backpatching

$L \rightarrow \{ L_1.next = newlabel(); \}$
 $L_1 \{ S.next = L.next; label(L_1.next); \}$
 S

$L \rightarrow \{ S.next = L.next; \}$
 S

$S \rightarrow if(\{ B.true = newlabel(); B.false = S_1.next = S.next; \}$
 $B) \{ label(B.true); \}$
 S_1

$B \rightarrow \{ B_1.true = B.true; B_1.false = newlabel(); \}$
 $B_1 || \{ B_2.true = B.true; B_2.false = B.false; label(B_1.false); \}$
 B_2

$B \rightarrow E_1 \text{ rel } E_2 \{ gen('if' E_1.addr \text{ rel } E_2.addr ' goto B.true');$
 $gen(' goto B.false'); \}$

Backpatching for Boolean Expression

1) $B \rightarrow B_1 \text{ || } M B_2$ { $\text{backpatch}(B_1.\text{falselist}, M.\text{instr});$
 $B.\text{truelist} = \text{merge}(B_1.\text{truelist}, B_2.\text{truelist});$
 $B.\text{falselist} = B_2.\text{falselist};$ }

2) $B \rightarrow B_1 \text{ && } M B_2$

3) $B \rightarrow ! B_1$

4) $B \rightarrow (B_1)$

5) $B \rightarrow E_1 \text{ rel } E_2$ { $B.\text{truelist} = \text{makelist}(nextinstr);$
 $B.\text{falselist} = \text{makelist}(nextinstr + 1);$
 $\text{emit('if' } E_1.\text{addr rel.op } E_2.\text{addr 'goto '});$
 $\text{emit('goto '});$ }

6) $B \rightarrow \text{true}$

7) $B \rightarrow \text{false}$

8) $M \rightarrow \epsilon$ { $M.\text{instr} = nextinstr;$ }

Backpatching for Flow-of-Control Statements

1) $S \rightarrow \text{if}(B) M S_1 \{ \text{backpatch}(B.\text{truelist}, M.\text{instr}); S.\text{nextlist} = \text{merge}(B.\text{falselist}, S_1.\text{nextlist}); \}$

2) $S \rightarrow \text{if}(B) M_1 S_1 N \text{ else } M_2 S_2$

3) $S \rightarrow \text{while } M_1 (B) M_2 S_1$

6) $M \rightarrow \epsilon \quad \{ M.\text{instr} = \text{nextinstr}; \}$

7) $N \rightarrow \epsilon$

Backpatching for Flow-of-Control Statements

4) $S \rightarrow \{ L \}$

5) $S \rightarrow A ;$

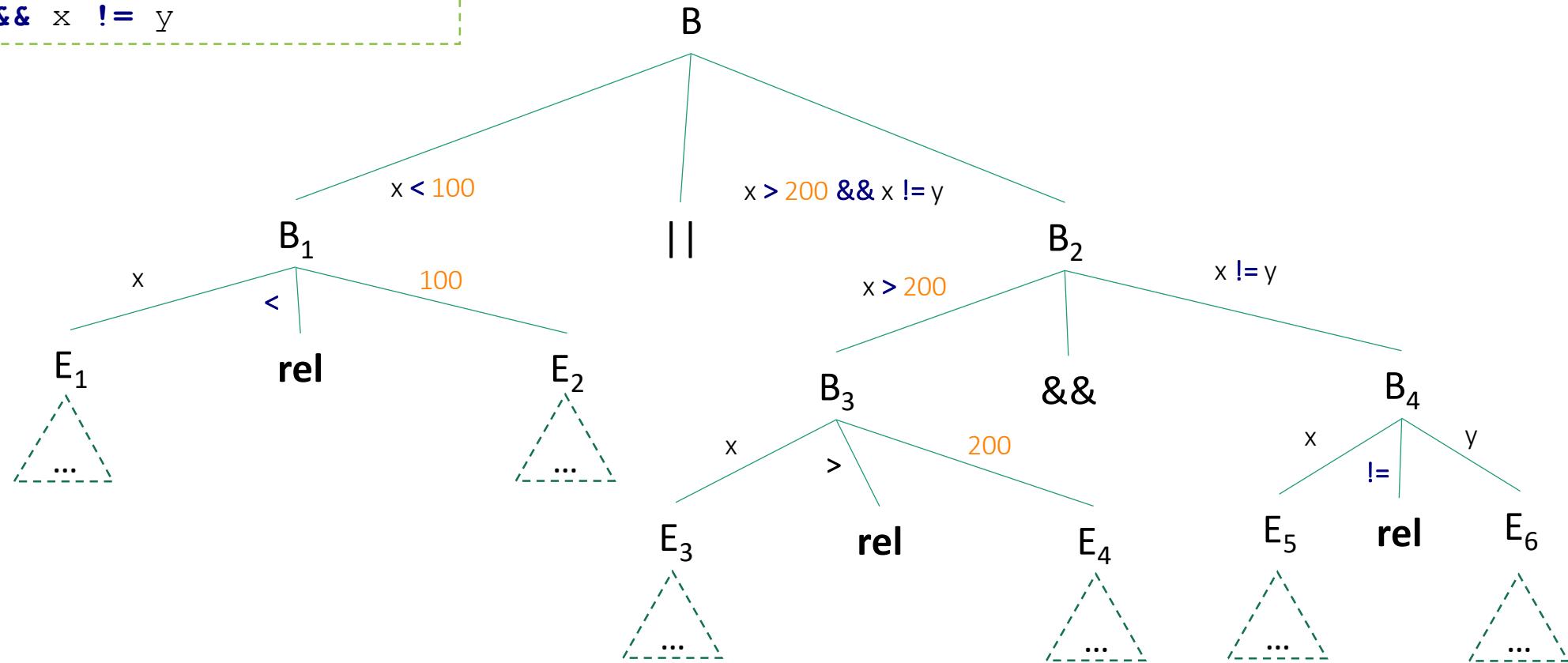
8) $L \rightarrow L_1 M S \quad \{ \text{backpatch}(L_1.\text{nextlist}, M.\text{instr});$
 $\quad L.\text{nextlist} = S.\text{nextlist}; \}$

9) $L \rightarrow S \quad \{ L.\text{nextlist} = S.\text{nextlist}; \}$

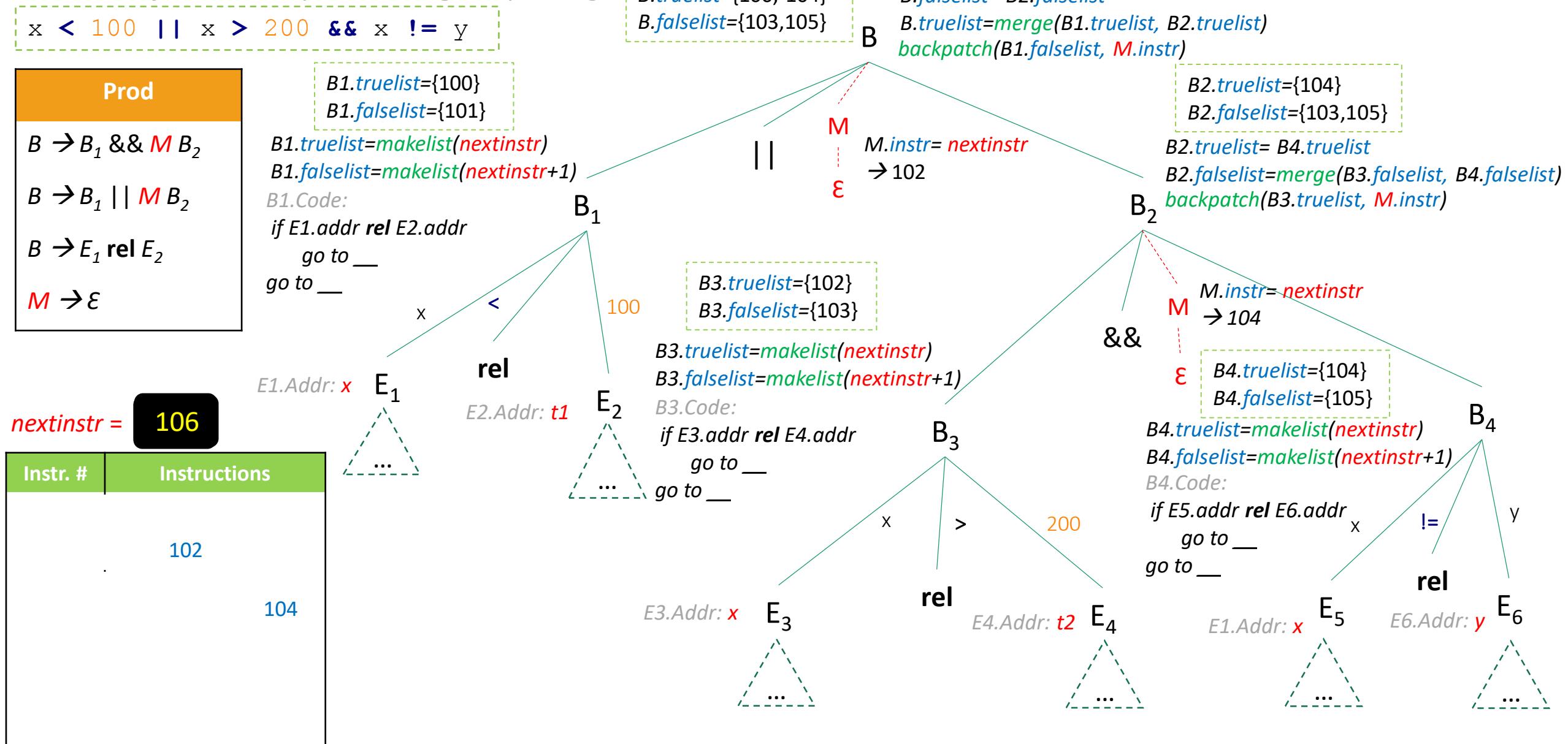
Translation of a boolean expression using backpatching

$x < 100 \quad || \quad x > 200 \quad \&\& \quad x \neq y$

Prod
$B \rightarrow B_1 \&\& B_2$
$B \rightarrow B_1 B_2$
$B \rightarrow E_1 \text{ rel } E_2$



Translation of a boolean expression using backpatching



Translation of Boolean Captured states in terms of backpatching

```

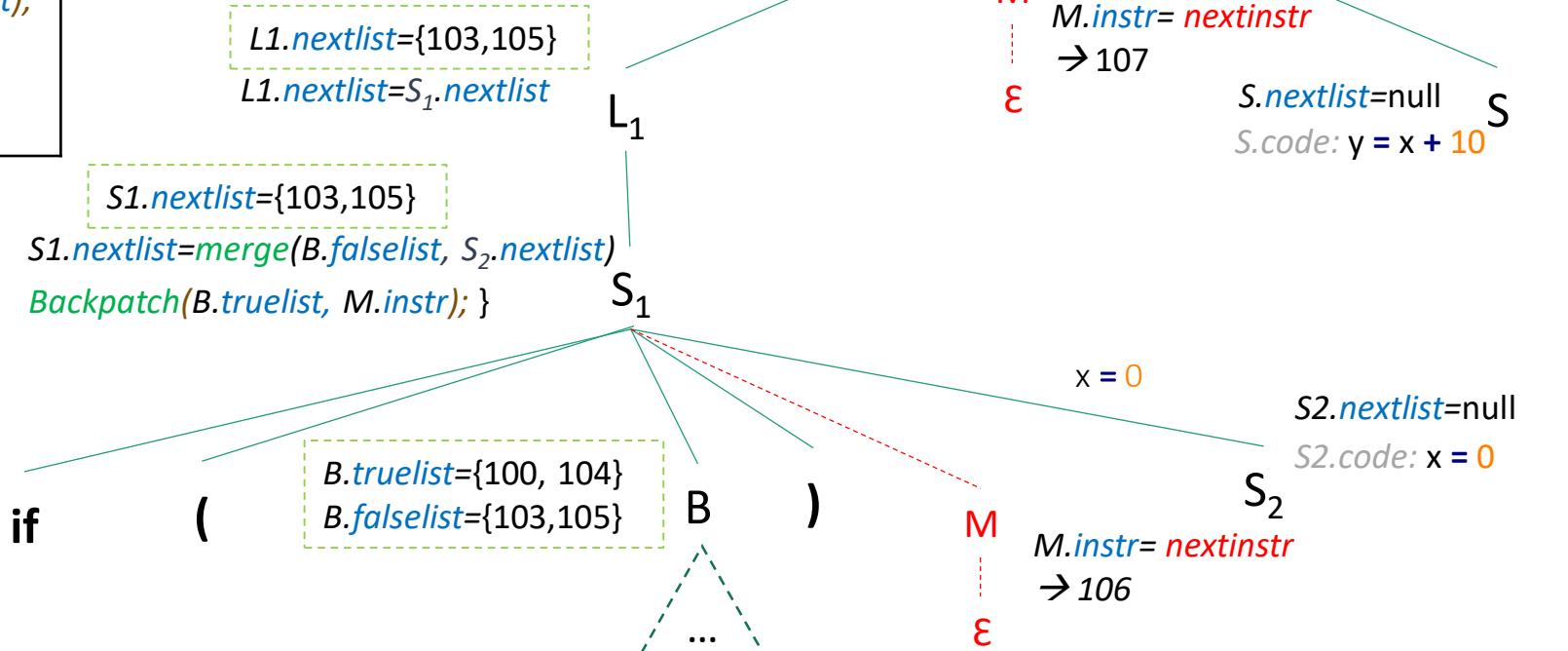
if<(1<|10>||2>&&0< && x != y)
    x = 0;
    y = x + 10;

```

$L \rightarrow L_1 M S$	{ Backpatch(L_1 .nextlist, $M.instr$); }
	$L.nextlist=S.nextlist;$ }
$L \rightarrow S$	{ $L.nextlist=S.nextlist$; }
$S \rightarrow A$	{ $S.nextlist=null$ }
$S \rightarrow if(B) M S_1$	{ $S.nextlist=merge(B.falselist, S_1.nextlist)$; Backpatch($B.truelist$, $M.instr$); }
$M \rightarrow \epsilon$	{ $M.instr=nextinstr$; }

nextinstr = 108

Instr. #	Instructions
100	if $x < 100$ go to 106
101	go to 102
102	if $x > 200$ go to 104
103	go to 107
104	if $x \neq y$ go to 106
105	go to 107



Break- and Continue- Statements

```
1) for ( ; ; readch() ) {  
2)     if( peek == ' ' || peek == '\t' ) continue;  
3)     else if( peek == '\n' ) line = line + 1;  
4)     else break;  
5) }
```

- If S is the enclosing loop construct, then a **break**-statement is a jump to the first instruction after the code for S
- Code for **break** can be generated by
 - (1) Keeping track of the enclosing loop statement S
 - (2) generating an unfilled jump for the **break**-statement, and
 - (3) putting this unfilled jump on $S.\textit{nextlist}$
- In a two-pass front end that builds syntax trees, $S.\textit{nextlist}$ can be implemented as a field in the node for S
- We can keep track of S by using the symbol table to map a special identifier **break** to the node for the enclosing loop statement

Break-, Continue-, and Goto-Statements

- Alternatively, a pointer to the *S.nextlist* can be put in the symbol table.
- When a **break**-statement is reached,
 - a unfilled jump is generated,
 - the *nextlist* is looked up in the symbol table,
 - the jump added to the list, and
 - finally, the list is backpatched
- **Continue**-statement can be handled in a manner analogous to **break**-statement.
 - However, the target of the generated jump is different.

Switch- Statements

- The ‘switch’ or ‘case’ statement is available in a variety of languages
- Syntax:

Switch Syntax

```
switch ( E ) {  
    case V1: S1  
    case V2: S2  
    ...  
    case Vn-1: Sn-1  
    default: Sn  
}
```

E: Selector Expression

V₁, V₂, ..., V_{n-1}: constant values

default: any value other than V₁, V₂, ..., V_{n-1}

S₁, S₂, ..., S_n: Statements

- Translation of Switch-Statements
 1. Evaluate the expression of E
 2. Find the value of V_j in the list of cases that is the same as the value of the expression. If not match found, match to the default values
 3. Execute the statement S_j associated with the value found

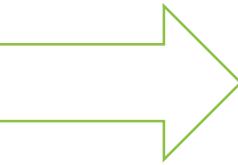
Translation of Switch- Statements

- Step (2) is a n-way branch that can be implemented in several ways
- If the number of cases is small, use a sequence of conditional jumps, each of which tests for an individual value and transfer to the code for the corresponding statement.
- A more compact way is to create a table of pairs, each pair consisting of a value and a label for the corresponding statement's code
 - The value for the expression E is paired with the label for the default statement and placed at the last of the table
 - A loop generated by the compiler compares the value of the expression to the values in the table
 - If the number of values is high, use a hash table
 - If the values all lies in some small range and the number of different values used is a reasonable fraction of the number of values in the range, then use 'buckets'

SDT for Translation of Switch- Statements

Switch Syntax

```
switch ( E ) {  
    case V1: S1  
    case V2: S2  
    ...  
    case Vn-1: Sn-1  
    default: Sn  
}
```



- Requires the compiler to do extensive analysis to find the most efficient implementation
- It is inconvenient in a one-pass compiler to place the branching statements at the beginning, because the compiler could not then emit code for each of statements S_i as it saw them

code to evaluate E into t

if $t \neq V_1$ goto L_1

code for S_1

goto **next**

L_1 : if $t \neq V_2$ goto L_2

code for S_2

goto **next**

L_2 :

...

L_{n-2} : if $t \neq V_{n-1}$ goto L_{n-1}

code for S_{n-1}

goto **next**

L_{n-1} :

code for S_n

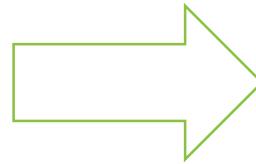
next:

Three Address Code (V.1)

SDT for Translation of Switch- Statements

Switch Syntax

```
switch ( E ) {
    case V1: S1
    case V2: S2
    ...
    case Vn-1: Sn-1
    default: Sn
}
```



1. When the keyword 'switch' is found, generate two labels **test** and **next** and a new temporary **t**
2. Then while E is parsed, generate code to evaluate E into t
3. After processing of E, generate the jump **goto test**
4. Then for each case keyword, create a new label **L_i** and enter in a queue in the symbol table value-label pair **<Vi, Li>**
5. Process each statement **case Vi:Si** by emitting the label **Li** attached to the code of **Si**, followed by the jump to **goto next**
6. When the end of the switch is found, generate the code for the n-way branch by reading from the queue of value-label pairs in the symbol table

	code to evaluate <i>E</i> into t
L₁:	goto test
	code for <i>S₁</i>
L₂:	goto next
	code for <i>S₂</i>
	goto next
	...
L_{n-1}:	code for <i>S_{n-1}</i>
	goto next
L_n:	code for <i>S_n</i>
	goto next
test:	if t = V₁ goto L₁
	if t = V₂ goto L₂
	...
	if t = V_{n-1} goto L_{n-1}
	goto L_n
next:	

Reference

- Compilers: Principles, Techniques, & Tools, by Alfred B. Aho, Monica S. Lam, Ravi Sethi, Jeffrey D. Ullman
 - Chapter 6
 - 6.1
 - 6.2
 - 6.3
 - 6.4
 - 6.6
 - 6.7
 - 6.8 (Self study)

Thank You!