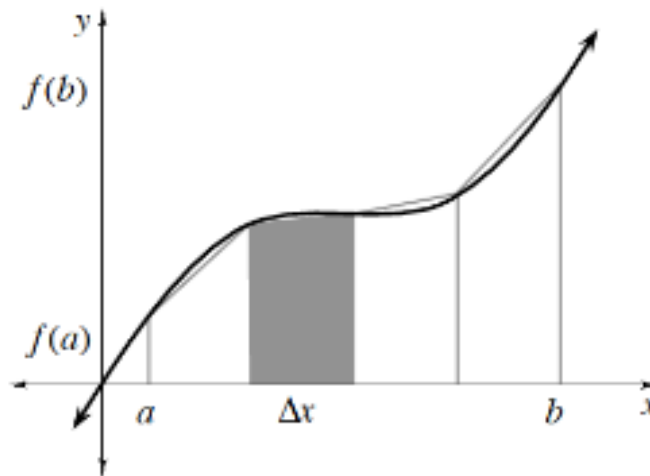


## Calculus 2.1 Key Points

### Trapezoid Rule:

Formula to approximate the area under a curve with trapezoids:

$$A = \frac{\Delta x}{2} (f(a) + 2f(a + \Delta x) + 2f(a + 2\Delta x) + \dots + 2f(b - \Delta x) + f(b))$$



### Summation/Sigma Notation:

$$\sum_{i=0}^2 (2i + 3) = [2(0) + 3] + [2(1) + 3] + [2(2) + 3] = 15$$

- The variable below the sigma symbol is called the **index** ( $i$  in this case)
- The numbers above & below the sigma symbol set the **upper & lower bounds**, respectively, for the summation (2 and 0 in this case)
- The term to the right of the sigma symbol is called the **argument** ( $2i + 3$  in this case)

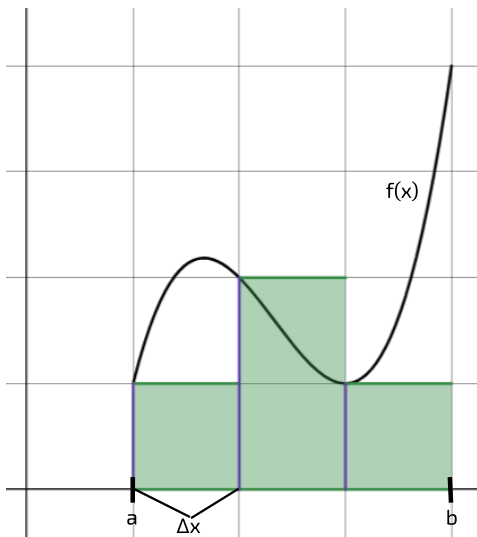
# Calculus 2.1 Key Points

## Left & Right Endpoint and Midpoint Rectangles:

We can approximate the area under a curve with a summation of rectangles.

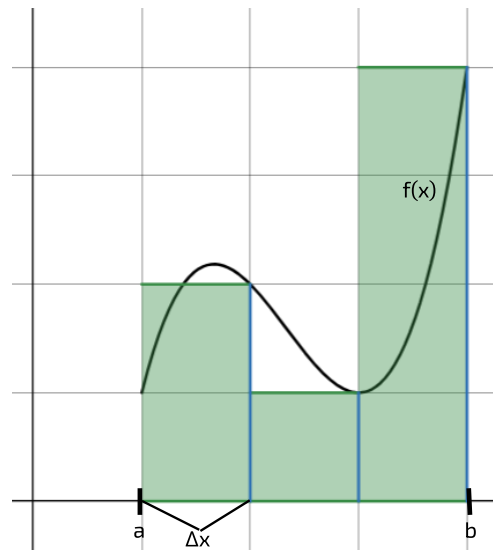
Left Endpoint:

$$\sum_{i=0}^{n-1} [\Delta x \cdot f(a + \Delta x \cdot i)]$$



Right Endpoint:

$$\sum_{i=1}^n [\Delta x \cdot f(a + \Delta x \cdot i)]$$



Midpoint:

$$\sum_{i=0}^{n-1} [\Delta x \cdot f((a + 0.5 \cdot \Delta x) + \Delta x \cdot i)]$$

