

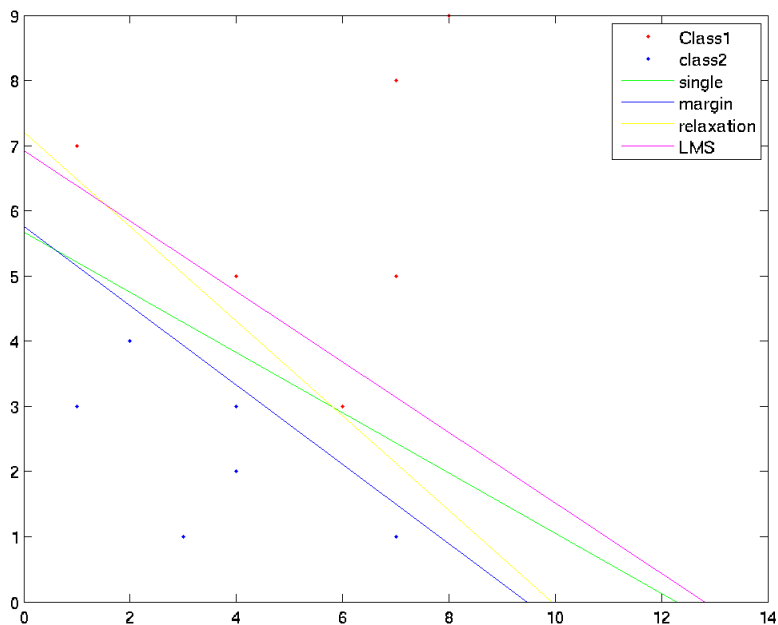
## Assignment 2

201364176

Noor Pratap Singh

### Problem 2

I) The graph is given below



Legend is self explanatory

II) The weight vectors have been initially randomized. But the farther the initial weight factor from my solution region the more time it took to converge towards the final solution. It was also dependent on my value of  $\eta$ .

III) From the figure it is quite evident that when margin was added no point actually lies on the solution vector (normal to solution vector). While in others it is possible.

#### IV)

##### Single Sample Perceptron

Algorithm:

```
begin
init  $a$ ,  $k = 0$ 
do
     $k = (k + 1) \bmod n$ 
    if  $y_k$  is misclassified by  $a$ 
        then  $a = a + y_k$ 
    until all patterns classified
return  $a$ 
end
```

As shown above in a single iteration we update our  $a$  based on only 1 misclassification at a time. At each iteration we again find new misclassified based on updated  $a$  and we run the above until all samples have been classified.

**Note** Solution will come only for linearly separable case.

As far as implementation is concerned it was done in Matlab and we first normalised the points. As soon as a misclassified sample is found we update  $a$  and move to next iteration.

We found a separating boundary after the process but in some case points were lying on the boundary.

### Single Sample Perceptron with margin

Algorithm:

```
begin initialize a, criterion  $\theta$ , margin b,  $\eta(\cdot)$ ,  $k = 0$ 
do  $k \leftarrow k + 1$ 
    if  $a \cdot t \cdot y_k + b < 0$  then  $a \leftarrow a - \eta(k)y_k$ 
        until  $a \cdot t \cdot y_k + b \leq 0$  for all k
    return a
end
```

The above algorithm is same as single sample but we have just added the condition that  $a \cdot t \cdot y_k + b < 0$  instead of  $a \cdot t \cdot y_k < 0$ .

All the analysis and results are similar except that no point lies on the boundary because of the margin.

### Relaxation with margin

Algorithm:

```
begin initialize a,  $\eta(\cdot)$ ,  $k = 0$ 
do  $k \leftarrow k + 1$ 
    if  $y_k$  is misclassified then  $a \leftarrow a + \eta(k) b - a$ 
         $y_k \geq y_k$ 
    until all patterns properly classified
    return a
end
```