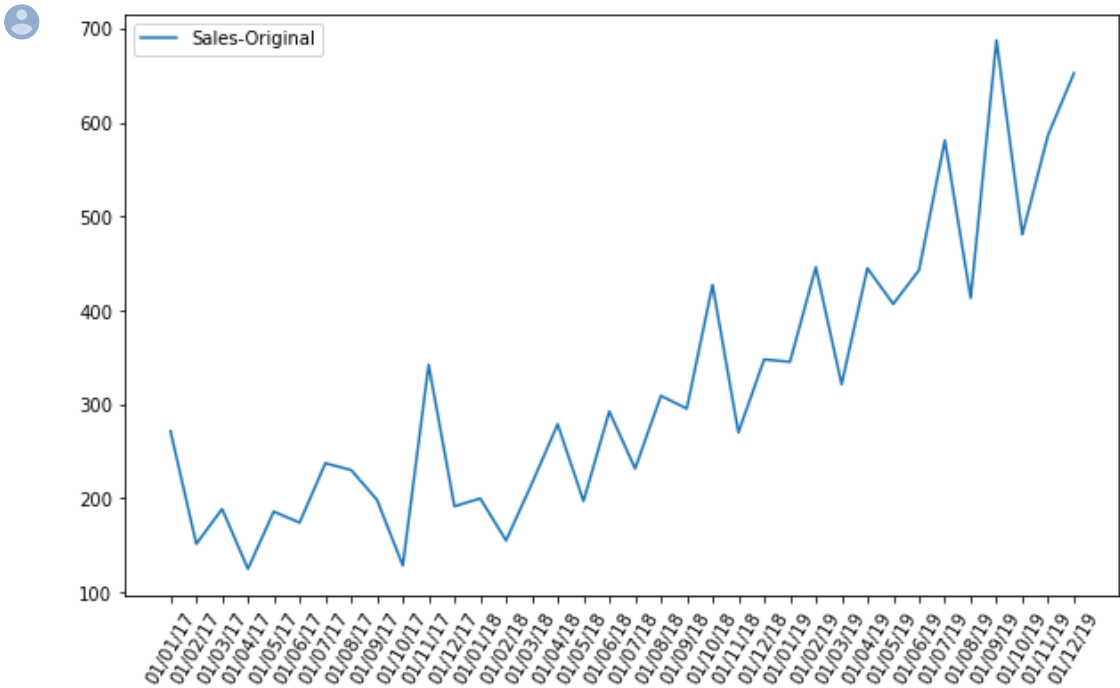


▼ Moving averages

```
1 # import needful libraries
2 import pandas as pd
3 import statsmodels.api as sm
4 import matplotlib.pyplot as plt
5
6 # Read dataset
7 sales_data = pd.read_csv('sales.csv')
8
9 # Setting figure size
10 plt.figure(figsize=(10,6))
11 # Plot original sales data
12 plt.plot(sales_data['Time'], sales_data['Sales'], label="Sales-Original")
13 # Rotate xlabels
14 plt.xticks(rotation=60)
15 # Add legends
16 plt.legend()
17 #display the plot
18 plt.show()
```

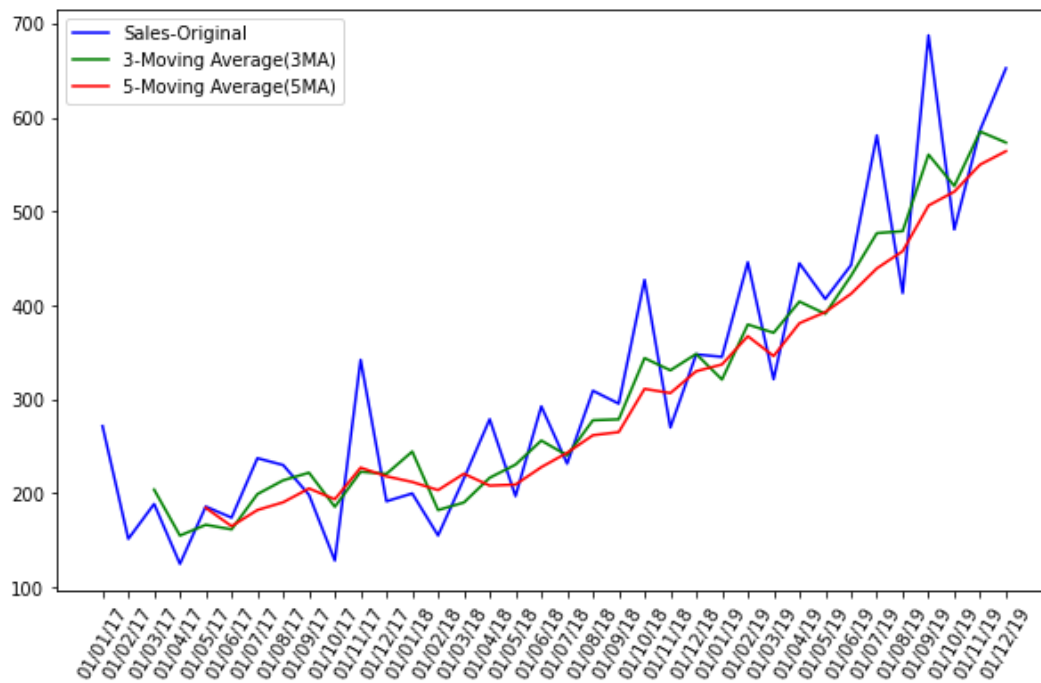


```
1 # Moving average with window 3
2 sales_data['3MA']=sales_data['Sales'].rolling(window=3).mean()
3 # Moving average with window 5
4 sales_data['5MA']=sales_data['Sales'].rolling(window=5).mean()
5 # Setting figure size
6 plt.figure(figsize=(10,6))
7 # Plot original sales data
8 plt.plot(sales_data['Time'], sales_data['Sales'], label="Sales-Original", color="blue")
9 # Plot 3-Moving Average of sales data
10 plt.plot(sales_data['Time'], sales_data['3MA'], label="3-Moving Average(3MA)", color="green")
11 # Plot 5-Moving Average of sales data
12 plt.plot(sales_data['Time'], sales_data['5MA'], label="5-Moving Average(5MA)", color="red")
13 # Rotate xlabels
14 plt.xticks(rotation=60)
15 # Add legends
16 plt.legend()
```

```

17 #display the plot
18 plt.show()

```



▼ Window Function

```

1 # import needful libraries
2 import pandas as pd
3 import statsmodels.api as sm
4 import matplotlib.pyplot as plt
5
6 # Read dataset
7 sales_data = pd.read_csv('sales.csv', index_col ="Time")
8
9 # Show initial 5 records
10 sales_data.head()

```

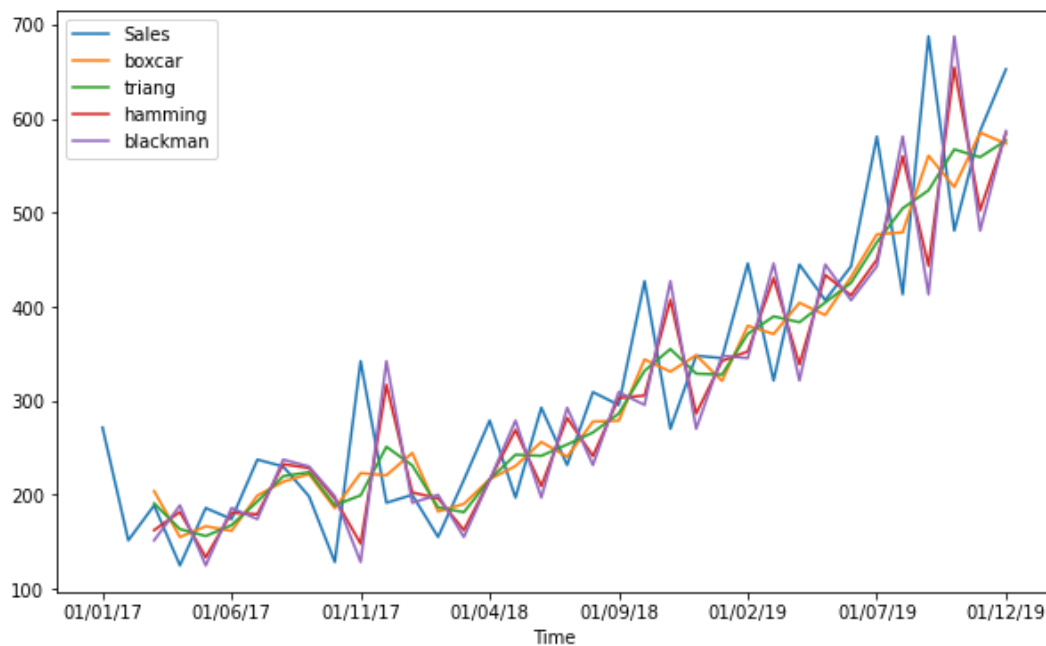
Sales	
Time	
01/01/17	271.5
01/02/17	151.4
01/03/17	188.6
01/04/17	124.8
01/05/17	185.8

```

1 # Apply all the windows on given DataFrame
2 sales_data['boxcar']=sales_data.Sales.rolling(3, win_type ='boxcar').mean()
3 sales_data['triang']=sales_data.Sales.rolling(3, win_type ='triang').mean()
4 sales_data['hamming']=sales_data.Sales.rolling(3, win_type ='hamming').mean()
5 sales_data['blackman']=sales_data.Sales.rolling(3, win_type ='blackman').mean()
6 #Plot the rolling mean of all the windows
7 sales_data.plot(kind='line',figsize=(10,6))

```

<matplotlib.axes._subplots.AxesSubplot at 0x7f7f69669610>



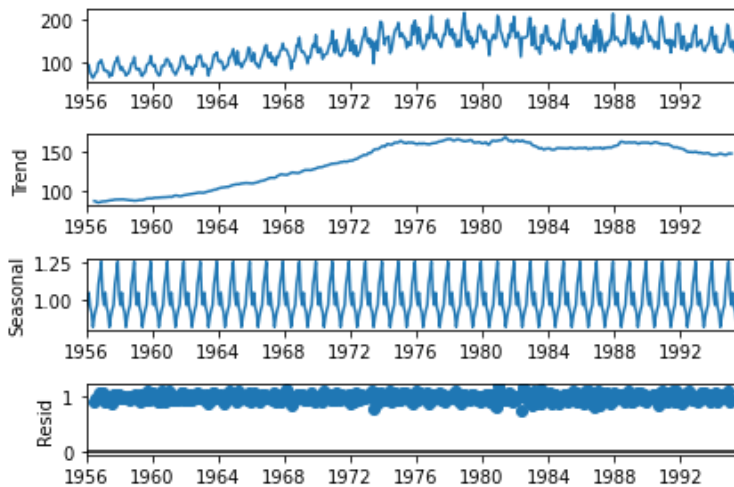
▼ Defining cointegration

```
1 # Import required library
2 import statsmodels.api as sm
3 import pandas as pd
4 import statsmodels.tsa.stattools as ts
5 import numpy as np
6
7 # Calculate ADF function
8 def calc_adf(x, y):
9     result = sm.OLS(x, y).fit()
10    return ts.adfuller(result.resid)
11
12 # Read the Dataset
13 data = sm.datasets.sunspots.load_pandas().data.values
14 N = len(data)
15
16 # Create Sine wave and apply ADF test
17 t = np.linspace(-2 * np.pi, 2 * np.pi, N)
18 sine = np.sin(np.sin(t))
19 print("Self ADF", calc_adf(sine, sine))
20
21 # Apply ADF test on Sine and Sine with noise
22 noise = np.random.normal(0, .01, N)
23 print("ADF sine with noise", calc_adf(sine, sine + noise))
24
25 # Apply ADF test on Sine and Cosine with noise
26 cosine = 100 * np.cos(t) + 10
27 print("ADF sine vs cosine with noise", calc_adf(sine, cosine + noise))
28
29 # Apply ADF test on Sine and sunspots dataset
30 print("Sine vs sunspots", calc_adf(sine, data))
```

```
Self ADF (-6.896689349349742e-16, 0.9585320860600559, 0, 308, {'1%': -3.45176116018037, '5%': -2.870970093607691, '10%': -2.57
ADF sine with noise (-4.091294292410859, 0.0010011179783234881, 12, 296, {'1%': -3.452636878592149, '5%': -2.8713543954331433
ADF sine vs cosine with noise (-19.959621318125926, 0.0, 16, 292, {'1%': -3.4529449243622383, '5%': -2.871489553425686, '10%': -2.
Sine vs sunspots (-6.724269181070102, 3.4210811915549028e-09, 16, 292, {'1%': -3.4529449243622383, '5%': -2.871489553425686, '
```

▼ Decomposing time series

```
1  # import needful libraries
2  import pandas as pd
3  import matplotlib.pyplot as plt
4  from statsmodels.tsa.seasonal import seasonal_decompose
5
6  # Read the dataset
7  data = pd.read_csv('beer_production.csv')
8  data.columns= ['date', 'data']
9  # Change datatype to pandas datetime
10 data['date'] = pd.to_datetime(data['date'])
11 data=data.set_index('date')
12
13 # Decompose the data
14 decomposed_data = seasonal_decompose(data, model='multiplicative')
15 # Plot decomposed data
16 decomposed_data.plot()
17 # Display the plot
18 plt.show()
```



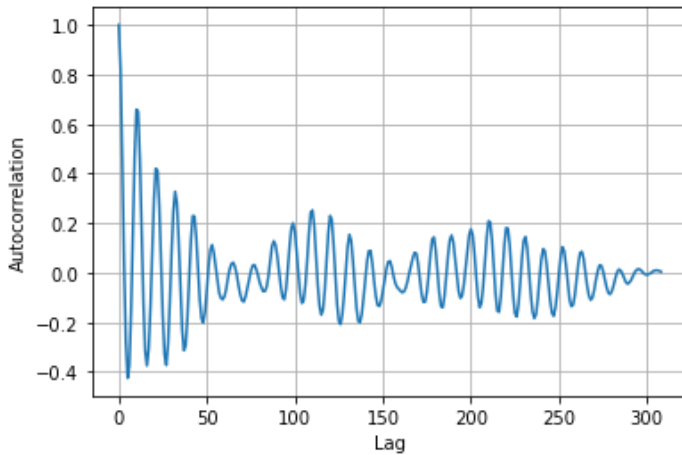
▼ Autocorrelation

```
1  # import needful libraries
2  import pandas as pd
3  import numpy as np
4  import statsmodels.api as sm
5  import matplotlib.pyplot as plt
6
7  # Read the dataset
8  data = sm.datasets.sunspots.load_pandas().data
9
10 # Calculate autocorrelation using numpy
11 dy = data.SUNACTIVITY - np.mean(data.SUNACTIVITY)
12 dy_square = np.sum(dy ** 2)
13
14 # Cross-correlation
15 sun_correlated = np.correlate(dy, dy, mode='full')/dy_square
16 result = sun_correlated[int(len(sun_correlated)/2):]
17
18 # Display the Chart
19 plt.plot(result)
```

```

19 plt.plot(result)
20 # Display grid
21 plt.grid(True)
22 # Add labels
23 plt.xlabel("Lag")
24 plt.ylabel("Autocorrelation")
25 # Display the chart
26 plt.show()

```

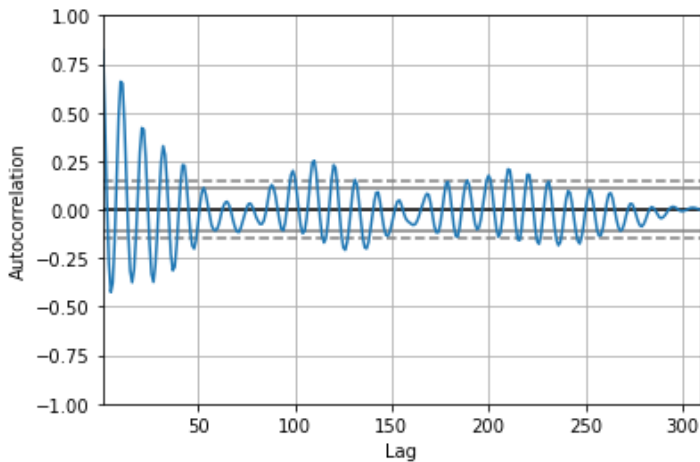


```

1 from pandas.plotting import autocorrelation_plot
2 # Plot using pandas function
3 autocorrelation_plot(data.SUNACTIVITY)

```

<matplotlib.axes._subplots.AxesSubplot at 0x7f7f621ec910>



▼ Auto Regression

```

1 # import needful libraries
2 from statsmodels.tsa.ar_model import AR
3 from sklearn.metrics import mean_absolute_error
4 from sklearn.metrics import mean_squared_error
5 import matplotlib.pyplot as plt
6 import statsmodels.api as sm
7 from math import sqrt
8
9 # Read the dataset
10 data = sm.datasets.sunspots.load_pandas().data
11
12 # Split data into train and test set
13 train_ratio=0.8
14 train=data[:int(train_ratio*len(data))]

```

```

15 test=data[int(train_ratio*len(data)):]
16
17
18 # AutoRegression Model training
19 ar_model = AR(train.SUNACTIVITY)
20 ar_model = ar_model.fit()
21
22 # print lags and
23 print("Number of Lags:", ar_model.k_ar)
24 print("Model Coefficients:\n", ar_model.params)

Number of Lags: 15
Model Coefficients:
const          9.382322
L1.SUNACTIVITY  1.225684
L2.SUNACTIVITY -0.512193
L3.SUNACTIVITY -0.130695
L4.SUNACTIVITY  0.193492
L5.SUNACTIVITY -0.168907
L6.SUNACTIVITY  0.054594
L7.SUNACTIVITY -0.056725
L8.SUNACTIVITY  0.109404
L9.SUNACTIVITY  0.108993
L10.SUNACTIVITY -0.117063
L11.SUNACTIVITY  0.200454
L12.SUNACTIVITY -0.075111
L13.SUNACTIVITY -0.114437
L14.SUNACTIVITY  0.177516
L15.SUNACTIVITY -0.091978
dtype: float64
/home/avinash/anaconda3/lib/python3.8/site-packages/statsmodels/tsa/ar_model.py:691: FutureWarning:
statsmodels.tsa.AR has been deprecated in favor of statsmodels.tsa.AutoReg and
statsmodels.tsa.SARIMAX.

```

AutoReg adds the ability to specify exogenous variables, include time trends, and add seasonal dummies. The AutoReg API differs from AR since the model is treated as immutable, and so the entire specification including the lag length must be specified when creating the model. This change is too substantial to incorporate into the existing AR api. The function `ar_select_order` performs lag length selection for AutoReg models.

AutoReg only estimates parameters using conditional MLE (OLS). Use SARIMAX to estimate ARX and related models using full MLE via the Kalman Filter.

To silence this warning and continue using AR until it is removed, use:

```

import warnings
warnings.filterwarnings('ignore', 'statsmodels.tsa.ar_model.AR', FutureWarning)

warnings.warn(AR_DEPRECATION_WARN, FutureWarning)

```

```

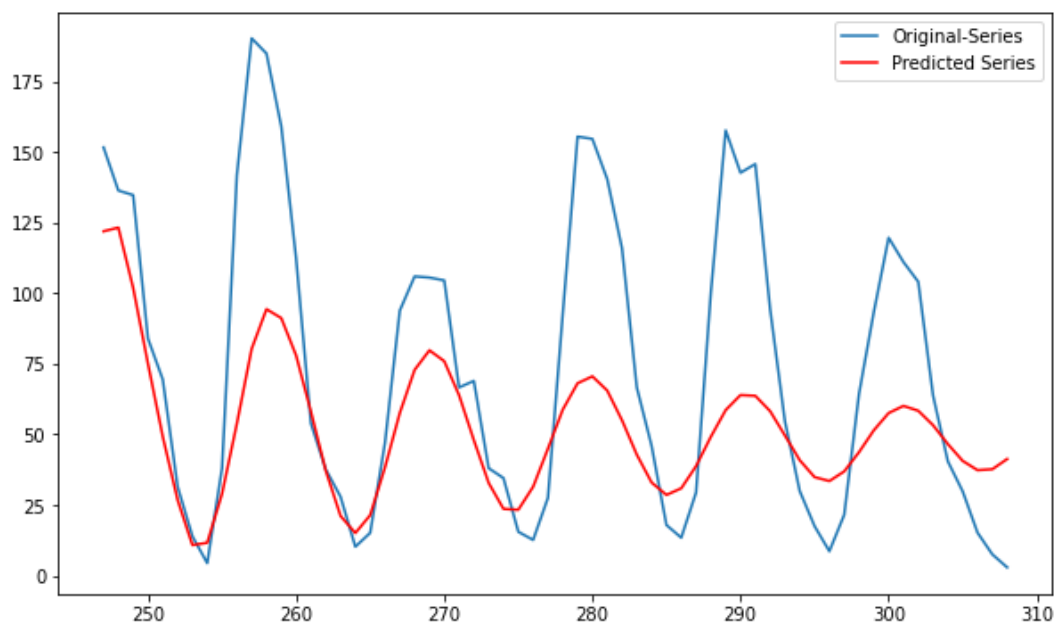
1 # make predictions
2 start_point = len(train)
3 end_point = start_point + len(test)-1
4 pred = ar_model.predict(start=start_point, end=end_point, dynamic=False)
5
6 # Calculate erros
7 mae = mean_absolute_error(test.SUNACTIVITY, pred)
8 mse = mean_squared_error(test.SUNACTIVITY, pred)
9 rmse = sqrt(mse)
10 print("MAE:",mae)
11 print("MSE:",mse)
12 print("EMSE:",rmse)

```

MAE: 31.178460983500255

MSE: 1776.9463826165686
EMSE: 42.15384184883471

```
1 # Setting figure size
2 plt.figure(figsize=(10,6))
3 # Plot test data
4 plt.plot(test.SUNACTIVITY, label='Original-Series')
5 # Plot predictions
6 plt.plot(pred, color='red', label='Predicted Series')
7 # Add legends
8 plt.legend()
9 # Display the plot
10 plt.show()
```



ARMA

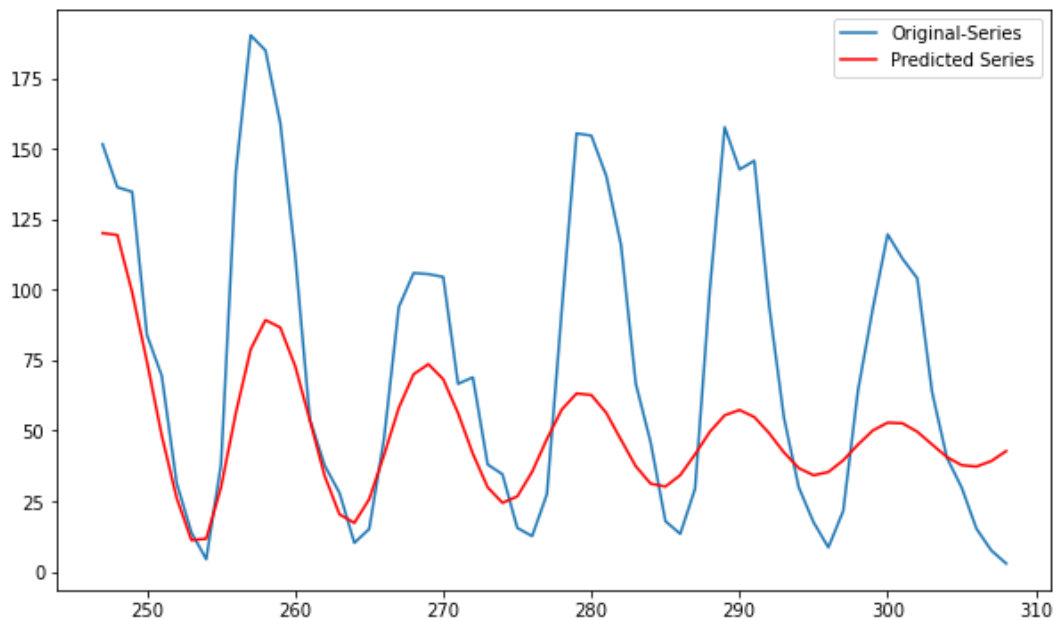
```
1 # import needful libraries
2 import statsmodels.api as sm
3 from statsmodels.tsa.arima_model import ARMA
4 from sklearn.metrics import mean_absolute_error
5 from sklearn.metrics import mean_squared_error
6 import matplotlib.pyplot as plt
7 from math import sqrt
8
9 # Read the dataset
10 data = sm.datasets.sunspots.load_pandas().data
11 data.drop('YEAR',axis=1,inplace=True)
12
13 # Split data into train and test set
14 train_ratio=0.8
15 train=data[:int(train_ratio*len(data))]
16 test=data[int(train_ratio*len(data)):]
17
18 # AutoRegression Model training
19 arma_model = ARMA(train, order=(10,1))
20 arma_model = arma_model.fit()
21
22 # make predictions
23 start_point = len(train)
24 end_point = start_point + len(test)-1
```

```

24 end_point = start_point + len(test)-1
25 pred = arma_model.predict(start_point,end_point)
26
27 # Calculate erros
28 mae = mean_absolute_error(test.SUNACTIVITY, pred)
29 mse = mean_squared_error(test.SUNACTIVITY, pred)
30 rmse = sqrt(mse)
31 print("MAE:",mae)
32 print("MSE:",mse)
33 print("EMSE:",rmse)
34
35 # Setting figure size
36 plt.figure(figsize=(10,6))
37 # Plot test data
38 plt.plot(test, label='Original-Series')
39 # Plot predictions
40 plt.plot(pred, color='red', label='Predicted Series')
41 # Add legends
42 plt.legend()
43 # Display the plot
44 plt.show()

```

MAE: 33.95456896482045
 MSE: 2041.3852298217791
 EMSE: 45.18169131209874



ARIMA

```

1 # import needful libraries
2 import statsmodels.api as sm
3 from statsmodels.tsa.arima_model import ARIMA
4 from sklearn.metrics import mean_absolute_error
5 from sklearn.metrics import mean_squared_error
6 import matplotlib.pyplot as plt
7 from math import sqrt
8
9 # Read the dataset
10 data = sm.datasets.sunspots.load_pandas().data
11 data.drop('YEAR',axis=1,inplace=True)
12
13 # Split data into train and test set
14 train_ratio=0.8

```



```

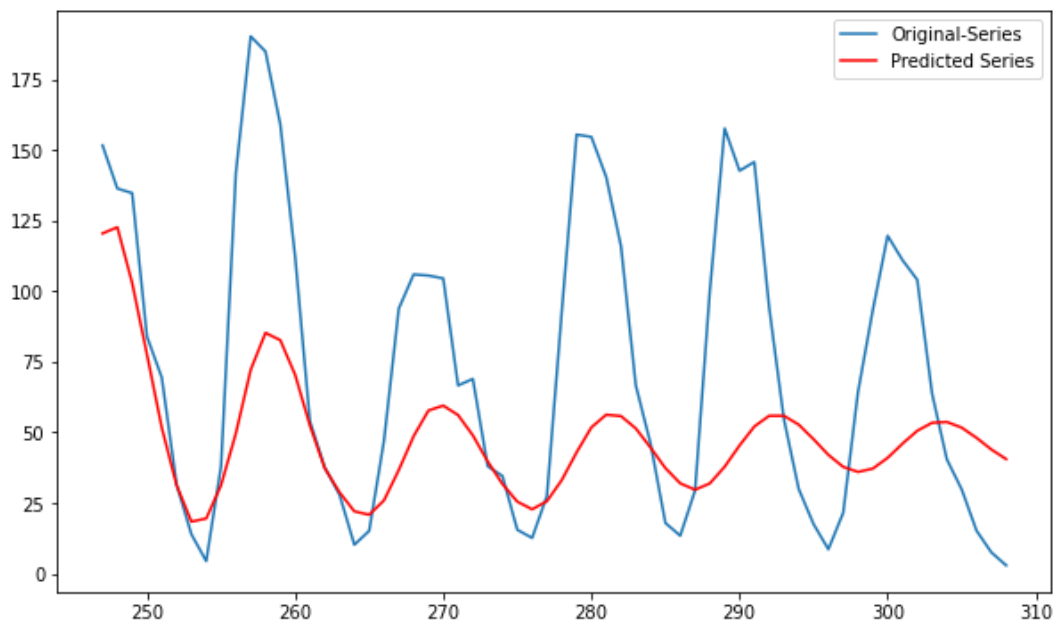
15 train=data[:int(train_ratio*len(data))]
16 test=data[int(train_ratio*len(data)):]
17
18 # AutoRegression Model training
19 arima_model = ARIMA(train, order=(20,0,1))
20 arima_model = arima_model.fit()
21
22 # make predictions
23 start_point = len(train)
24 end_point = start_point + len(test)-1
25 pred = arima_model.predict(start_point,end_point)
26
27 # Calculate erros
28 mae = mean_absolute_error(test.SUNACTIVITY, pred)
29 mse = mean_squared_error(test.SUNACTIVITY, pred)
30 rmse = sqrt(mse)
31 print("MAE:",mae)
32 print("MSE:",mse)
33 print("EMSE:",rmse)
34
35 # Setting figure size
36 plt.figure(figsize=(10,6))
37 # Plot test data
38 plt.plot(test, label='Original-Series')
39 # Plot predictions
40 plt.plot(pred, color='red', label='Predicted Series')
41 # Add legends
42 plt.legend()
43 # Display the plot
44 plt.show()

```

MAE: 36.934332860115326

MSE: 2527.6415003516413

EMSE: 50.27565514592168



▼ Generating Periodic Signals

```

1 # Import required libraries
2 import numpy as np
3 import statsmodels.api as sm
4 from scipy.optimize import leastsq

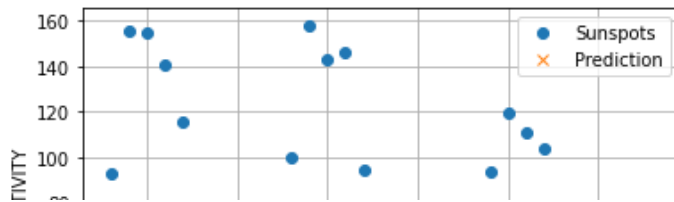
```

```

5 import matplotlib.pyplot as plt
6
7
8 # Create model function
9 def model(p, t):
10     C, p1, f1, phi1, p2, f2, phi2, p3, f3, phi3 = p
11     return C + p1 * np.sin(f1 * t + phi1) + p2 * np.sin(f2 * t + phi2) + p3 * np.sin(f3 * t + phi3)
12
13 # Create error function
14 def error(p, y, t):
15     return y - model(p, t)
16
17 # Create fit function
18 def fit(y, t):
19     p0 = [y.mean(), 0, 2 * np.pi/11, 0, 0, 2 * np.pi/22, 0, 0, 2 * np.pi/100, 0]
20     params = leastsq(error, p0, args=(y, t))[0]
21     return params
22
23 # Load the dataset
24 data_loader = sm.datasets.sunspots.load_pandas()
25 sunspots = data_loader.data["SUNACTIVITY"].values
26 years = data_loader.data["YEAR"].values
27
28 # Apply and fit the model
29 cutoff = int(.9 * len(sunspots))
30 params = fit(sunspots[:cutoff], years[:cutoff])
31 print("Params", params)
32
33 pred = model(params, years[cutoff:])
34 actual = sunspots[cutoff:]
35 print("Root mean square error", np.sqrt(np.mean((actual - pred) **
36 2)))
37 print("Mean absolute error", np.mean(np.abs(actual - pred)))
38 print("Mean absolute percentage error", 100 *
39 np.mean(np.abs(actual - pred)/actual))
40 mid = (actual + pred)/2
41 print("Symmetric Mean absolute percentage error", 100 *
42 np.mean(np.abs(actual - pred)/mid))
43 print("Coefficient of determination", 1 - ((actual - pred) **
44 2).sum()/ ((actual - actual.mean()) ** 2).sum())
45 year_range = data_loader.data["YEAR"].values[cutoff:]
46
47 # Plot the actual and predicted data points
48 plt.plot(year_range, actual, 'o', label="Sunspots")
49 plt.plot(year_range, pred, 'x', label="Prediction")
50 plt.grid(True)
51 # Add labels
52 plt.xlabel("YEAR")
53 plt.ylabel("SUNACTIVITY")
54 # Add legend
55 plt.legend()
56 # Display the chart
57 plt.show()

```

Params [47.1880006 28.89947462 0.56827279 6.51178464 4.55214564
0.29372076 -14.30924768 -18.16524123 0.06574835 -4.37789476]
Root mean square error 59.56205597915569
Mean absolute error 44.58158470150657
Mean absolute percentage error 65.16458348768887
Symmetric Mean absolute percentage error 78.4480696873044
Coefficient of determination -0.3635315489903188



Fourier Analysis

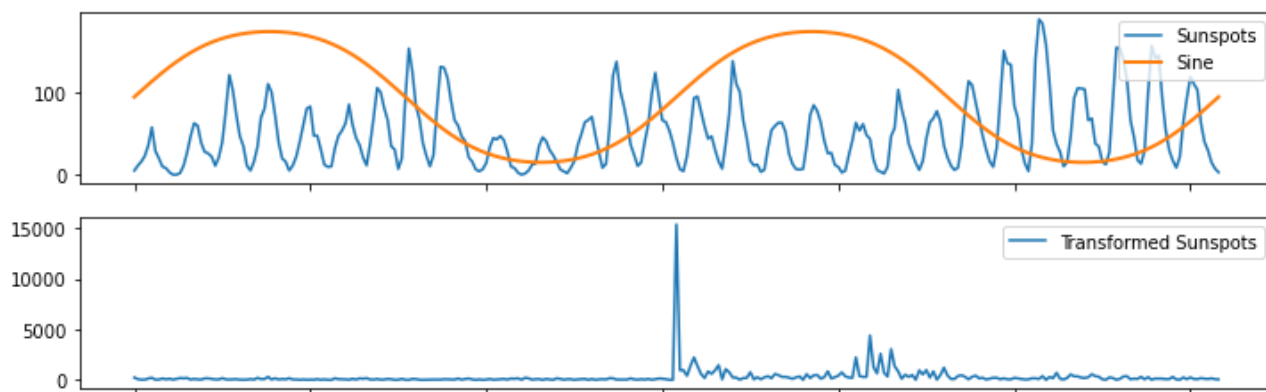
```

1  # Import required library
2  import numpy as np
3  import statsmodels.api as sm
4  import matplotlib.pyplot as plt
5  from scipy.fftpack import rfft
6  from scipy.fftpack import fftshift
7
8
9  # Read the dataset
10 data = sm.datasets.sunspots.load_pandas().data
11
12 # Create Sine wave
13 t = np.linspace(-2 * np.pi, 2 * np.pi, len(data.SUNACTIVITY.values))
14 mid = np.ptp(data.SUNACTIVITY.values)/2
15 sine = mid + mid * np.sin(np.sin(t))
16
17 # Compute FFT for Sine wave
18 sine_fft = np.abs(fftshift(rfft(sine)))
19 print("Index of max sine FFT", np.argsort(sine_fft)[-5:])
20
21 # Compute FFT for sunspots dataset
22 transformed = np.abs(fftshift(rfft(data.SUNACTIVITY.values)))
23 print("Indices of max sunspots FFT", np.argsort(transformed)[-5:])
24
25 # Create subplots
26 fig, axs = plt.subplots(3,figsize=(12,6),sharex=True)
27 fig.suptitle('Power Specturm')
28 axs[0].plot(data.SUNACTIVITY.values, label="Sunspots")
29 axs[0].plot(sine, lw=2, label="Sine")
30 axs[0].legend() # Set legends
31 axs[1].plot(transformed, label="Transformed Sunspots")
32 axs[1].legend() # Set legends
33 axs[2].plot(sine_fft, lw=2, label="Transformed Sine")
34 axs[2].legend() # Set legends
35
36 # Display the chart
37 plt.show()

```

Index of max sine FFT [160 157 166 158 154]
Indices of max sunspots FFT [205 212 215 209 154]

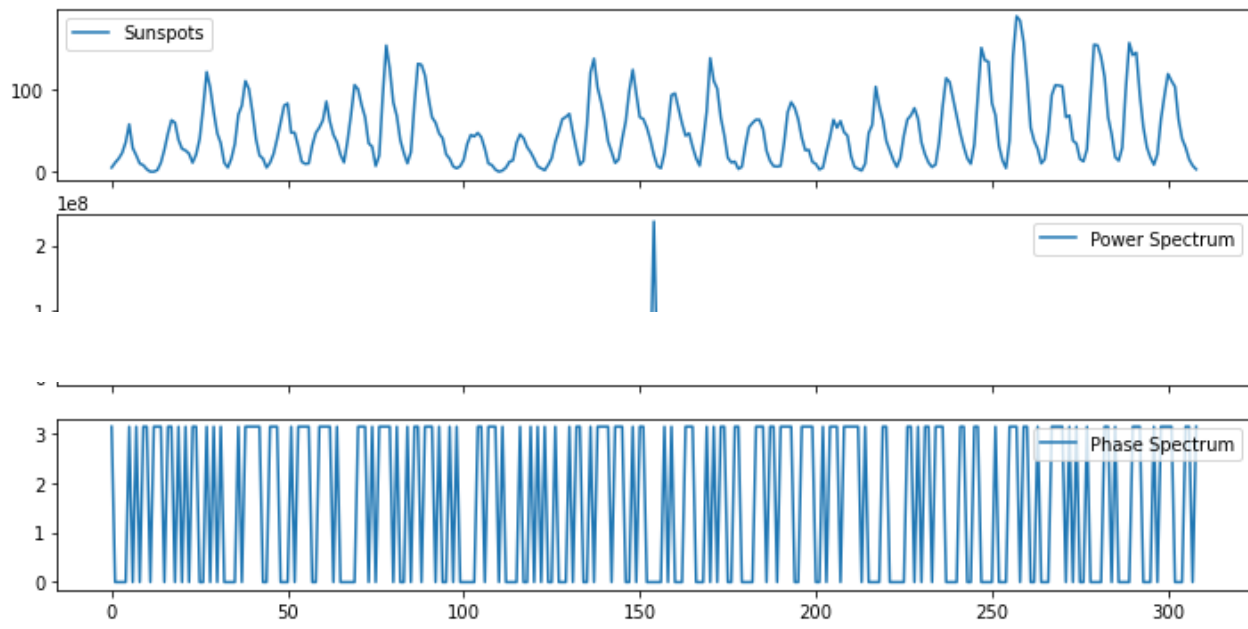
Power Spectrum



▼ Spectral Analysis Filtering

```
10000 | | |
1 # Import required library
2 import numpy as np
3 import statsmodels.api as sm
4 from scipy.fftpack import rfft
5 from scipy.fftpack import fftshift
6 import matplotlib.pyplot as plt
7
8 # Read the dataset
9 data = sm.datasets.sunspots.load_pandas().data
10
11 # Compute FFT
12 transformed = fftshift(rfft(data.SUNACTIVITY.values))
13 # Compute Power Spectrum
14 power=transformed ** 2
15 # Compute Phase
16 phase=np.angle(transformed)
17
18 # Create subplots
19 fig, axs = plt.subplots(3,figsize=(12,6),sharex=True)
20 fig.suptitle('Power Spectrum')
21 axs[0].plot(data.SUNACTIVITY.values, label="Sunspots")
22 axs[0].legend() # Set legends
23 axs[1].plot(power, label="Power Spectrum")
24 axs[1].legend() # Set legends
25 axs[2].plot(phase, label="Phase Spectrum")
26 axs[2].legend() # Set legends
27
28 # Display the chart
29 plt.show()
30
```

Power Spectrum



1