編號:

221,223

## 國立成功大學一○○學年度碩士班招生考試試題

共 2頁 第/頁

系所組別: 資訊工程學系、醫學資訊研究所

考試科目: 程式設計

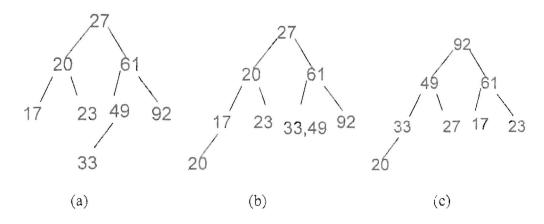
考試日期:0220:節次:2

# ※ 考生請注意:本試題 □可 □不可 使用計算機

## - Data Structures (50%)

#### 1 (15%)

Insert a sequence of keys (27, 49, 17, 20, 61, 23, 92, 33) into a data structure that has no keys in the beginning. The results are depicted as follows. Please answer the corresponding data structure for (a), (b), and (c), respectively.



#### 2.(25%)

We know the red-black tree is one of many search tree schemes that are approximately balanced in order to guarantee that basic dynamic set operations take  $O(\lg n)$  time in the worst case.

- (a) (15%) Please augment the red-black tree to maintain a dynamic set Q of numbers that supports the operation MIN-GAP, which gives the magnitude of the difference of the two closest numbers in Q. For example, if Q={1, 3, 9, 15, 18, 22}, then MIN-GAP(Q) returns 2, since 1 and 3 are the two closest numbers in Q. Make the operations MIN-GAP as efficient as O(lg n) where n is the size of Q.
- (b) (10%) According to the augmented red-black tree, it is also possible to simultaneously find the two closest numbers that result in the minimum gap in O(lg n) time. Please explain how to do it?

編號:

221.223

國立成功大學一○○學年度碩士班招生考試試題

共 7 頁,第2頁

系所組別: 資訊工程學系、醫學資訊研究所

考試科目: 程式設計

考試日期:0220,節次:2

#### ※ 考生請注意:本試題 □可 ☑不可 使用計算機

3. (10%) For the following applications (a)-(f), please choose the most suitable data structure or algorithm from the candidates (1)-(9) to handle them. We denote N(j)=i if application (j) is matched with data structure or algorithm (i) where  $j \in \{a, b, c, d, e, f\}$ 

and  $i \in \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ . Please find the value  $\sum_{i=1}^{A=f} (N(A))^2 = ?$ 

- (a) A network routing protocol in which the routing algorithm must determine a minimal spanning tree.
- (b) The process scheduler in an operation system that needs to dispatch processes in the order of arrival.
- (c) The dictionary look-up function that needs the index of words.
- (d) The maze problem that needs to keep track of the path visited.
- (e) The database query optimizer that needs the index of data records.
- (f) The database system that is used in a hospital in which the data of patients accessed will be accessed again frequently.

(1) Stack

(6) Kruskal's algorithm

(2) Queue

(7) Dijkstra's algorithm

(3) Splay tree

(8) Topological sorting

(4) B-tree

(9) Hashing

- (5) Red-Black tree
- Algorithms (50%)
- 4. (20%) Solving the recurrence  $T(n) = 2T(n/2) + n/\log_2 n$  using  $\Theta$  notation.
- 5. (10%) What is an optimal **Huffman code** for the following set of frequencies: a: 25, b: 3, c: 12, d: 16, e: 39, f: 5, g: 13.
- 6. (10%) Give a  $O(V^2 \lg V + VE)$ -time algorithm to find the shortest paths between all pairs of vertices in a weighted and directed graph G=(V, E).
- 1. (10%) Describe an algorithm that, given n integers in the range 0 to k, preprocesses its input and then answers any query about how many of the n integers fall into a range [a...b] in O(1) time, where  $a, b \in \{0,1,...,k\}$ . Your algorithm should use  $\Theta(n+k)$  preprocessing time.