AMATH 482/582: HOMEWORK 2

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ABSTRACT.

1. INTRODUCTION AND OVERVIEW

2. THEORETICAL BACKGROUND

3. ALGORITHM IMPLEMENTATION AND DEVELOPMENT

4. COMPUTATIONAL RESULTS

Plotting the sigma values (1000 values between 0 and 4) against accuracy for spectral clustering yields the following plot:
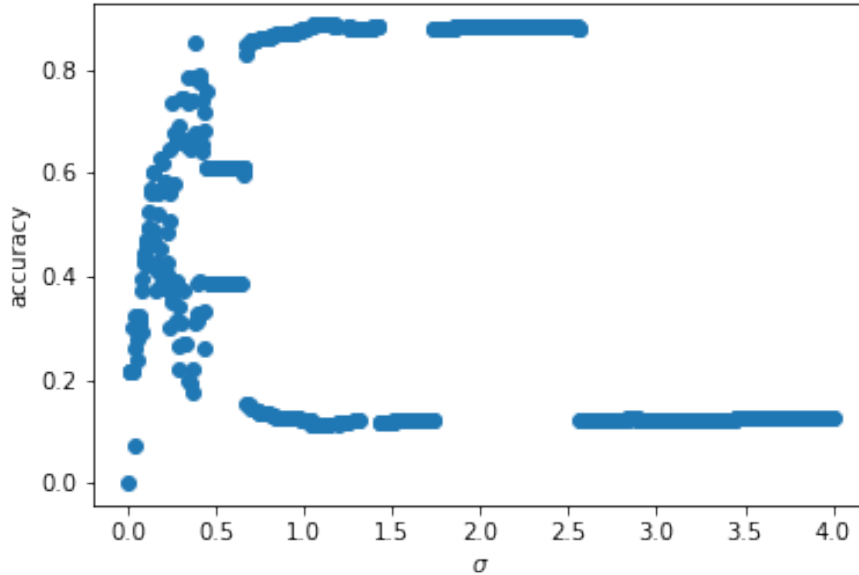

FIGURE 1. Plot of sigma values against accuracy for spectral clustering

We can see that the accuracy of the spectral clustering varies wildly according to small variations in sigma. After sigma = approximately 0.6, the accuracy seems to oscillate between values > 0.8 and values < 0.2. The maximum accuracy occurs when $\sigma = 1.\overline{053}$. The accuracy at this point is 0.887, which indicates that even though our spectral clustering seems to be unstable, we are still getting a good accuracy.

When using the semi-supervised learning technique, we get the following results for different values of M and J.

J \ M	2	3	4	5	6
5	0.8827	0.8827	0.8620	0.8827	0.8827
10	0.8781	0.8919	0.8873	0.8873	0.8160
20	0.8850	0.8873	0.8988	0.8735	0.7816
40	0.8850	0.8942	0.9011	0.9264	0.9310

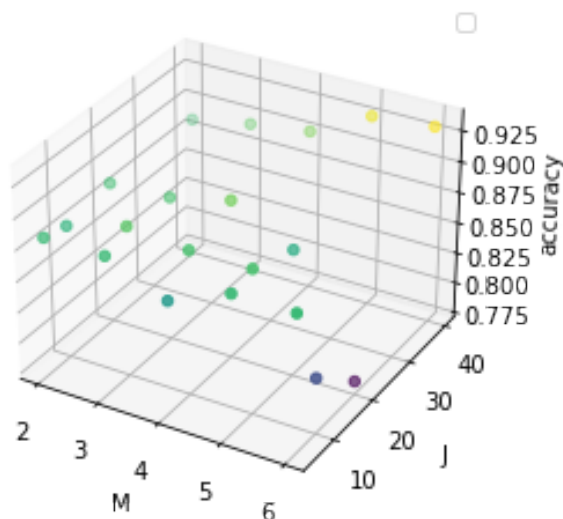FIGURE 2. Plot of M and J values against accuracy for semi-supervised learning

We can see that the accuracy of the semi-supervised learning algorithm is almost as good, if not better, than that of the spectral clustering algorithm in most cases. The best accuracy occurs when $M = 6$ and $J = 40$. At this point, the accuracy is 0.9310. Curiously, the lowest accuracy occurs when $M = 5$ as well (though $J = 20$ in this case). This indicates we might be seeing behavior similar to that of spectral clustering, where even the slightest variation in our hyperparameters can lead to wildly different results. To test this theory, I plotted many values of M and J against eachother in order to see if there is any correlation between the accuracy and the values of M and J. The plot below shows the accuracy of the semi-supervised learning algorithm in this case
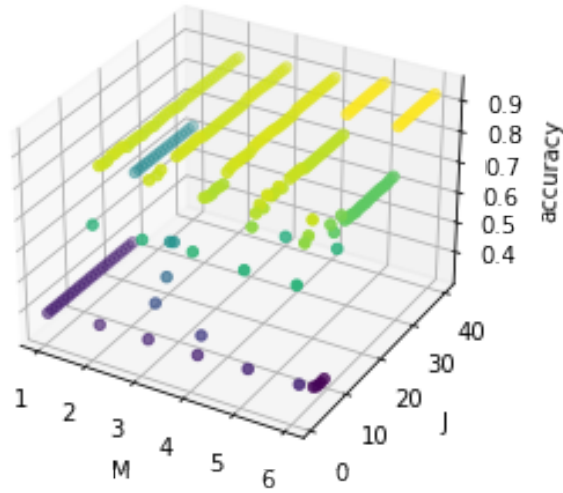
FIGURE 3. Plot of M and J values against accuracy for semi-supervised learning for a wide range of points

We can see that our hypothesis is almost correct. There does seem to be wild drifts in the accuracy, but not as erratic as we saw in the spectral clustering case. Instead, these seem to be linked to a drop of directly correlated to the J values. As J increases by a factor of 10, it seems that accuracy increases as well. As such, this methodology does seem to be much more stable (no more rapid oscillation between varying accuracies).

5. SUMMARY AND CONCLUSIONS

ACKNOWLEDGEMENTS